

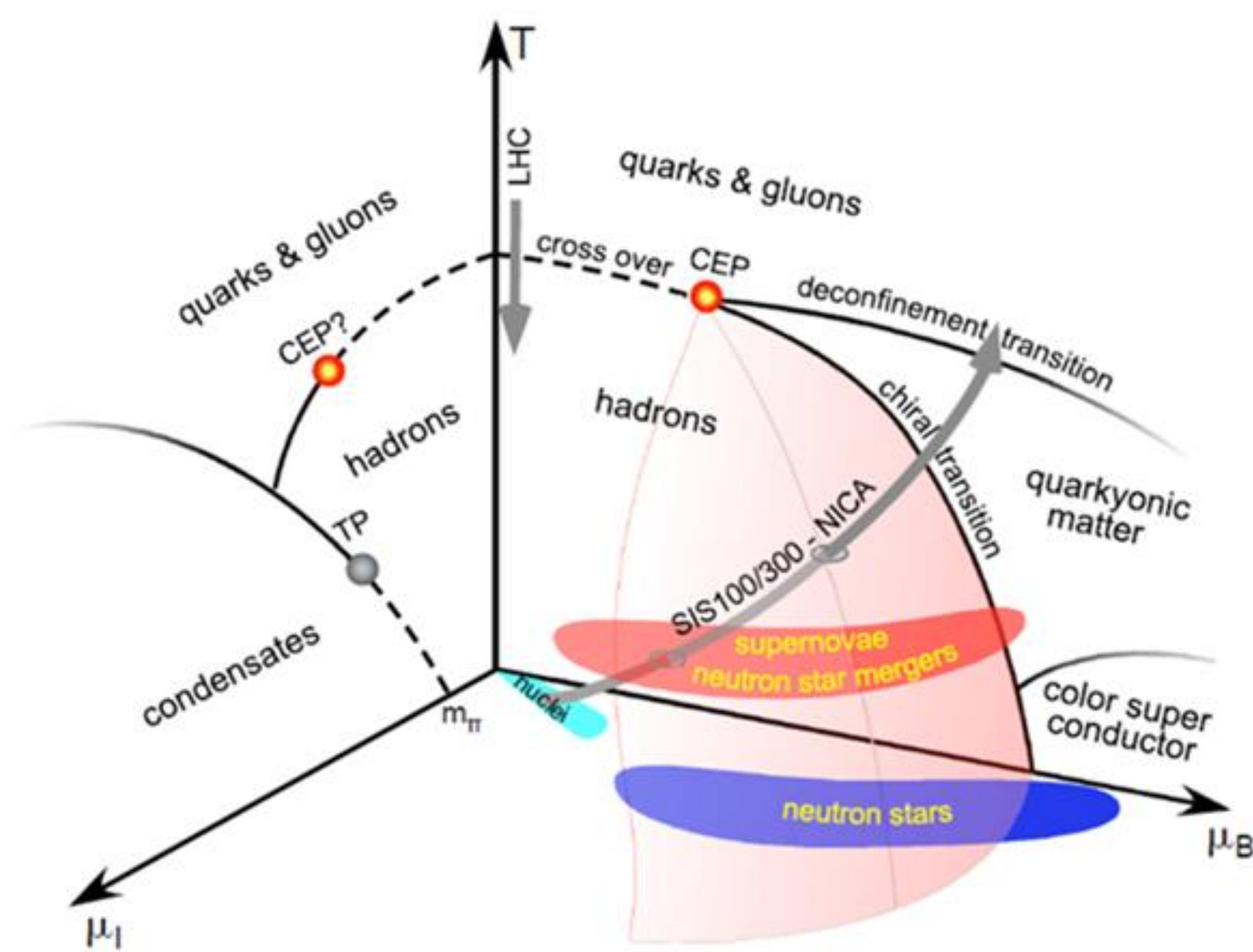
European Research Council  
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## First feasibility study for Asymmetric Cumulants of flow amplitudes in CBM at FAIR

### Phase diagram of QCD matter

- CBM experiment at FAIR is optimized to explore properties of QCD matter at very high densities, by colliding heavy ions

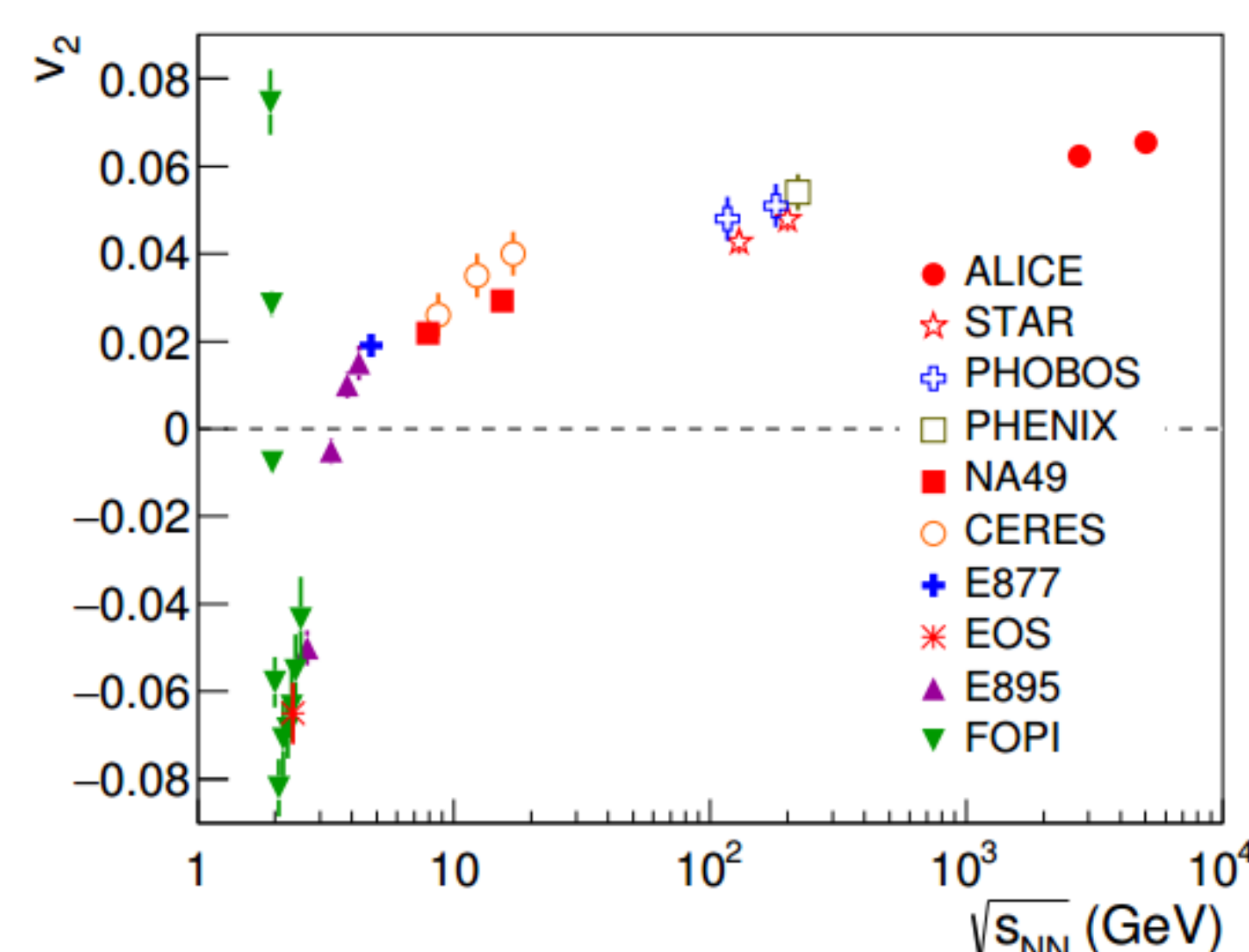
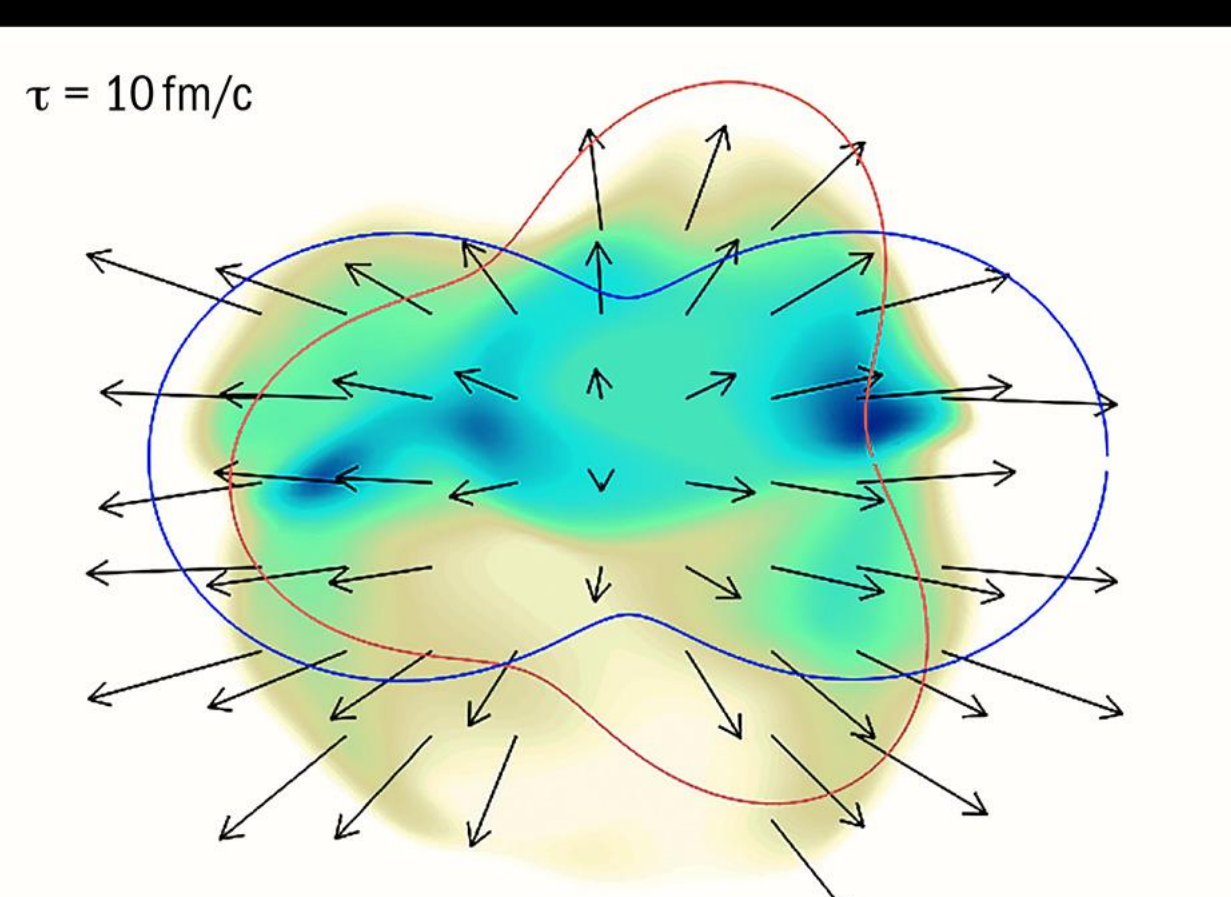
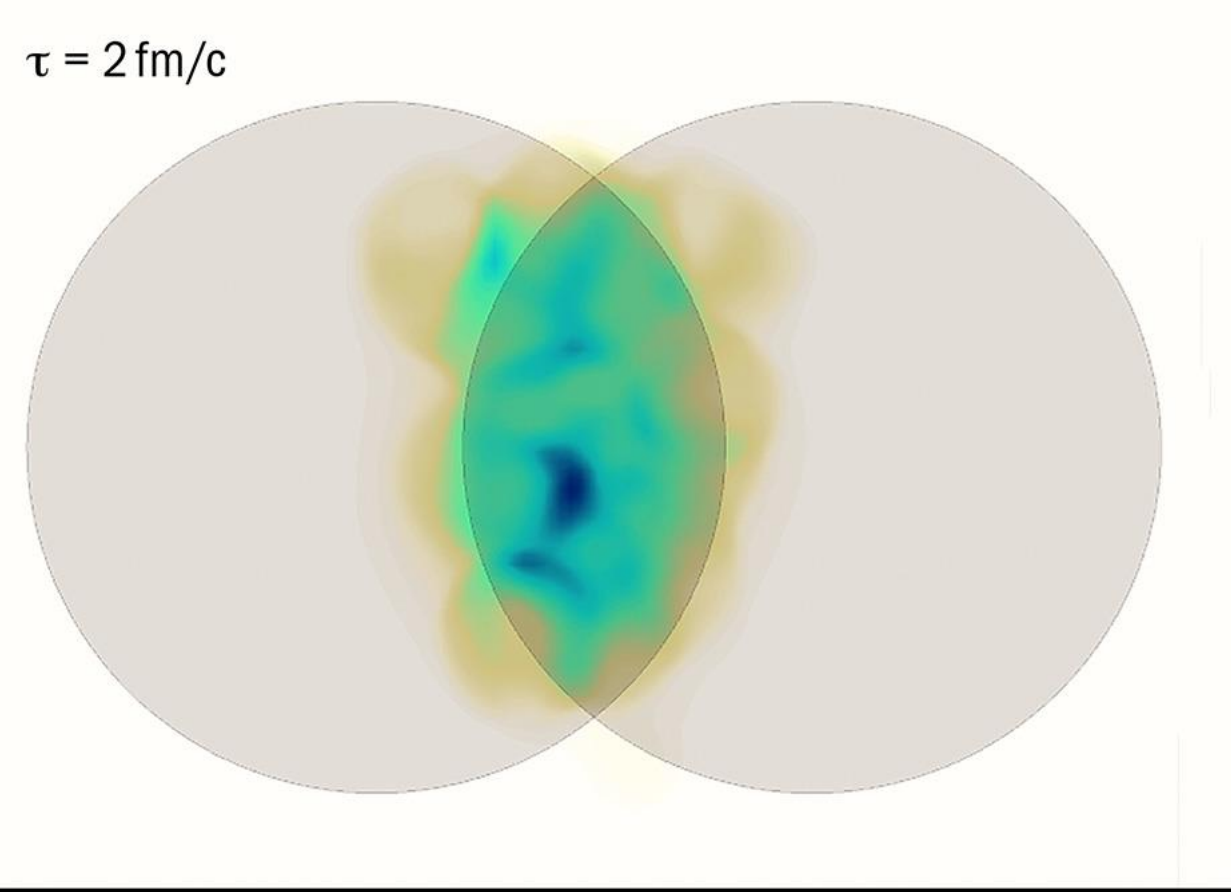


- Scientific objectives of CBM experiment:

- What is the equation-of-state (EoS) of QCD matter in the regime of very high densities?
- Does QCD phase diagram feature a critical point?
- What is the nature of phase transition between ordinary and deconfined nuclear matter?
- What are the fundamental degrees of freedom at high densities?

### Collective anisotropic flow

- Results from ultrarelativistic heavy-ion collisions are consistent with the scenario in which the produced nuclear matter undergoes collective expansion, dominated by its hydrodynamic response to anisotropies in the initial-state geometry ⇔ **collective anisotropic flow**



$$f(\varphi) = \frac{1}{2\pi} \left[ 1 + 2 \sum_{n=1}^{\infty} v_n \cos[n(\varphi - \Psi_n)] \right]$$

- Fourier harmonics  $v_n$  quantify collective anisotropic flow, and are sensitive probe of EoS of nuclear matter, its transport properties (shear and bulk viscosities), etc.

CERN Courier, April 2021

### Asymmetric Cumulants

- General mathematical formalism of multivariate cumulants can be applied to the stochastic event-by-event fluctuations of  $v_n$  harmonics

$$\bullet \bullet = \bullet \bullet + \bullet \bullet + \bullet \bullet + \bullet \bullet + \bullet \bullet$$

R. Kubo, J. Phys. Soc. Jpn. 17 (1962)

- Generalization is not trivial for correlations involving more than two  $v_n$  harmonics, and it was accomplished only recently

AB, M. Lesch, C. Mordasini, Seyed F. Taghavi, Phys.Rev.C 105 (2022) 2, 024912

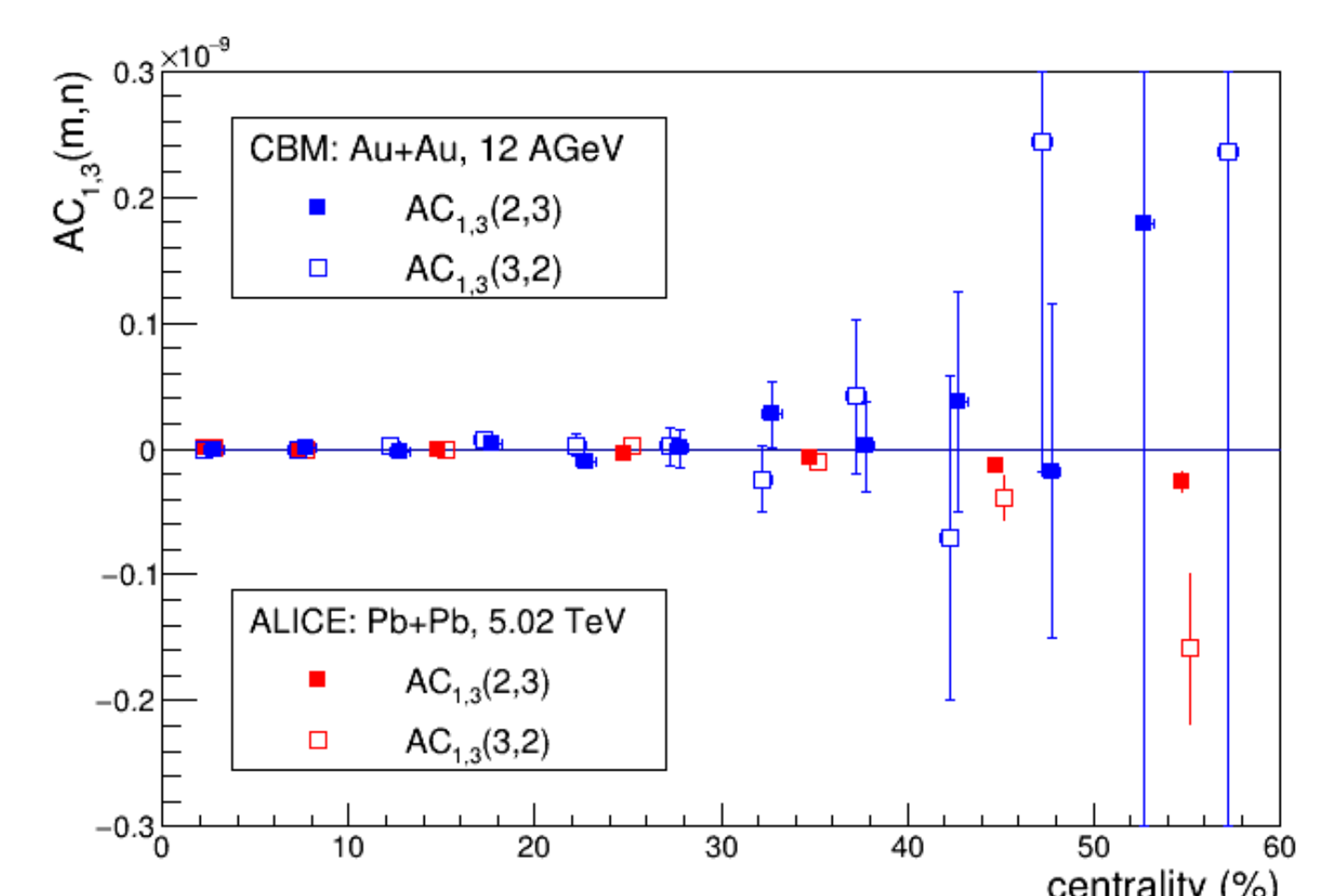
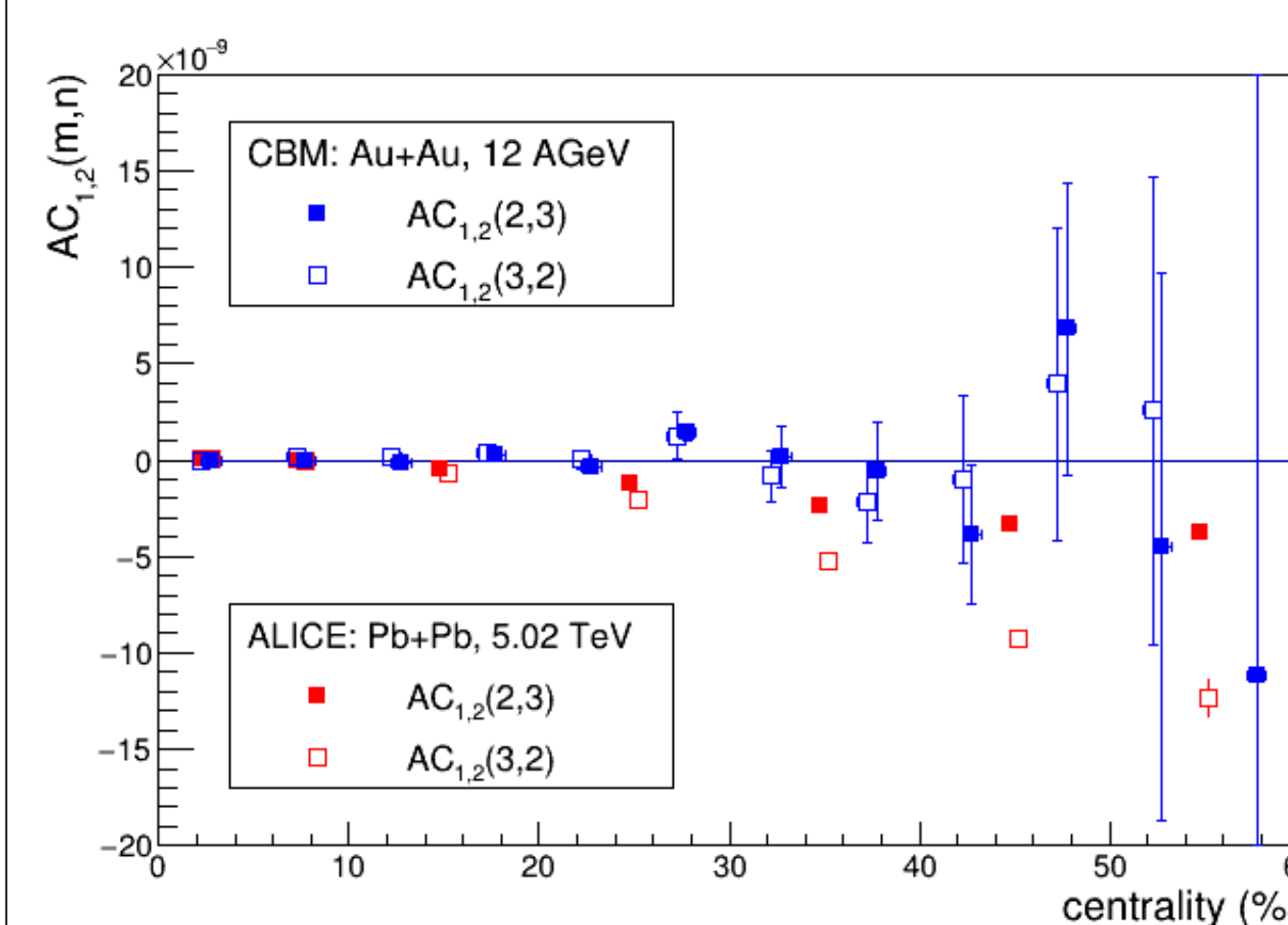
- New higher-order flow observables, which quantify correlations of different higher-order moments of  $v_n$ , and satisfy all fundamental properties of multivariate cumulants ⇔ **Asymmetric Cumulants (AC)**

$$AC_{2,1}(m,n) = \langle v_m^4 v_n^2 \rangle - \langle v_m^4 \rangle \langle v_n^2 \rangle - 2 \langle v_m^2 v_n^2 \rangle \langle v_m^2 \rangle + 2 \langle v_m^2 \rangle^2 \langle v_n^2 \rangle,$$

$$AC_{3,1}(m,n) = \langle v_m^6 v_n^2 \rangle - \langle v_m^6 \rangle \langle v_n^2 \rangle - 3 \langle v_m^2 v_n^2 \rangle \langle v_m^4 \rangle - 3 \langle v_m^4 v_n^2 \rangle \langle v_m^2 \rangle + 6 \langle v_m^4 \rangle \langle v_m^2 \rangle \langle v_n^2 \rangle + 6 \langle v_m^2 v_n^2 \rangle \langle v_m^2 \rangle^2 - 6 \langle v_m^2 \rangle^3 \langle v_n^2 \rangle,$$

$$AC_{2,1,1}(k,l,m) = \langle v_k^4 v_l^2 v_m^2 \rangle - \langle v_k^4 v_l^2 \rangle \langle v_m^2 \rangle - \langle v_k^4 v_m^2 \rangle \langle v_l^2 \rangle - \langle v_l^4 \rangle \langle v_k^2 v_m^2 \rangle + 2 \langle v_k^4 \rangle \langle v_l^2 \rangle \langle v_m^2 \rangle - 2 \langle v_k^2 v_l^2 \rangle \langle v_k^2 v_m^2 \rangle - 2 \langle v_k^2 v_l^2 v_m^2 \rangle \langle v_k^2 \rangle + 4 \langle v_k^2 v_l^2 \rangle \langle v_k^2 \rangle \langle v_m^2 \rangle + 4 \langle v_k^2 v_m^2 \rangle \langle v_k^2 \rangle \langle v_l^2 \rangle + 2 \langle v_k^2 \rangle^2 \langle v_l^2 v_m^2 \rangle - 6 \langle v_k^2 \rangle^2 \langle v_l^2 \rangle \langle v_m^2 \rangle.$$

- By definition, AC extract new and independent information when compared to the previous lower-order flow observables
- In general, AC are not invariant under permutations of different  $v_n$ , therefore  $AC_{1,2}(2,3)$  and  $AC_{1,2}(3,2)$  are independent of each other
- First feasibility studies for AC observables in the CBM environment, using Monte Carlo simulations of Au+Au collisions at 12 AGeV:



- AC observables are measured with multiparticle correlations, which are challenging for:
  - small multiplicities
  - detectors with non-uniform azimuthal acceptance

- Support for 'Generic Framework' available in CBMRoot

Phys. Rev. C 89 (2014) no.6, 064904

- Measurements of AC will be feasible in the CBM environment!

