Probing the QGP to Hadron-Gas Phase Transition with Charge, Strange, and Baryon Balance Functions

C. Pruneau¹, V. Gonzalez¹, B. Hanley¹, Ana Marin², S. Basu³ (1) Wayne State University, (2) GSI, (3) Lund University



Introduction

Prior Works & Known Properties of Balance Functions (BFs)
 O Investigate particle production vs. collision centrality, seek evidence for delayed hadronization/two-stage quark emission w/ *π* and K BFs [1, 2, 3] Sensitivity to hadron decays, radial flow [4,5], diffusivity of light quarks

[6,7], chemical evolution of the hot matter formed in A–A collisions, quantum statistic effects [8],

• Related to net charge fluctuations cumulants κ_{γ}^{Q} [9].

New Developments - This Work

- Account for a system's net-charge with Unified Balance Functions
- Mixed Species, Baryons and Strangeness
- O Multi-particle BFs

Simulations shown performed with PYTHIA 8, pp collisions at selected collisions energies.

Unified Balance Functions [10, 11]

Original BF as Conditional Density $B^{+|-}(\vec{p}_1 | \vec{p}_2) = \rho_2^{+|-}(\vec{p}_1 | \vec{p}_2) - \rho_2^{-|-}(\vec{p}_1 | \vec{p}_2) \quad \text{w/} \quad \rho_2^{\alpha|\beta}(y_1 | y_2) = \frac{\rho_2^{\alpha\beta}(y_1, y_2)}{\rho_1^{\beta}(y_2)}$

Integral of BF

$$I^{+-} = \frac{1}{\langle N_1^- \rangle} \int_{\Omega} d\vec{p}_2 \int_{\Omega} d\vec{p}_1 B^{+|-}(\vec{p}_1 | \vec{p}_2) = \frac{1}{\langle N_1^- \rangle} \left[\langle N_2^{+-} \rangle - \langle N_2^{--} \rangle \right],$$

Unified Balance Functions: Defined for any combination $\alpha \beta$ of identified particles in an acceptance Ω . $B^{\alpha\bar{\beta}}(y_1, y_2 | \Omega) = \frac{1}{\langle N_1^{\bar{\beta}} \rangle} \left[C_2^{\alpha\bar{\beta}}(y_1, y_2) - C_2^{\bar{\alpha}\bar{\beta}}(y_1, y_2) \right]$ $w/ C_2^{\alpha|\beta}(\vec{p}_1, \vec{p}_2) = \rho_2^{\alpha\beta}(\vec{p}_1, \vec{p}_2) - \rho_2^{\bar{\alpha}\bar{\beta}}(\vec{p}_1, \vec{p}_2)$ Use charge/strangeness densities for particles with |q| > 1, |s| > 1. Integral of Unified Balance Functions $I^{+-} = \frac{1}{\sqrt{2}} \int d\vec{p}_2 \int d\vec{p}_1 B^{+|-}(\vec{p}_1 | \vec{p}_2) = 1$ for full acceptance Ω .

$$I^{+-} = \frac{1}{\langle N_1^- \rangle} \int_{\Omega} d\vec{p}_2 \int_{\Omega} d\vec{p}_1 B^{+|-}(\vec{p}_1 | \vec{p}_2) = 1 \text{ for full acceptance } \Omega.$$



Sum Rule [10, 11]

Example: Assume a pion π^+ is detected at \vec{p}_2 , then negative particles $\bar{\alpha}$ must also be emitted to balance the charge.

Sum rule:
$$B^{-|\pi^+}(\vec{p}_1 | \vec{p}_2) = \sum_{\alpha} B^{\alpha|\pi^+}(\vec{p}_1 | \vec{p}_2)$$

 $B^{\alpha|\pi^+}(\vec{p}_1|\vec{p}_2)$ integrates to a fraction of unity in the full acceptance. The fraction is determined by the relative abundances of specific particle production channels.

Probes details of particle production.



Multi-Particle Balance Functions [12]

Balance Functions Extended to 2n particle correlation functions based on n-particle cumulants. Example:

 $B_4^{2(+)2(-)}(\vec{p}_1, \vec{p}_2, \vec{p}_3, \vec{p}_4) = \frac{2}{4!/2!} \frac{\left[6C_4^{++--}(\vec{p}_1, \dots, \vec{p}_4) - 4C_4^{+---}(\vec{p}_1, \dots, \vec{p}_4) + C_4^{----}(\vec{p}_1, \dots, \vec{p}_4)\right]}{\langle N_-(N_- - 1)\rangle}$

These functions also satisfy sum rules.



- UBFs defined w/ cumulants, i.e., genuine measures of correlations.
 Generalized for PID, mix species, multi- strange, & charged particles.
 Generalized to multi-particle correlations as combinations of n-particle cumulants.
- Satisfy simple sum rules.
- Study vs. acceptance will enable added sensitivity to particle production, baryon stopping, measuring QGP properties.



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