# **The role of longitudinal decorrelations for measurements of anisotropic flow in small collision systems**

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**Abstract.** Within a (3+1)D viscous hydrodynamic model we compute anisotropic flow in small system collisions as performed at the Relativistic Heavy Ion Collider and measured by the STAR and PHENIX Collaborations. We emphasize the importance of the rapidity dependence of the geometry for interpreting the differences encountered in measurements by the two collaborations.

# **1 Introduction**

The PHENIX Collaboration performed measurements of anisotropic flow in collisions of proton (p), deuteron (d), and helium-3 ( ${}^{3}$ He) projectiles with gold (Au) nuclei to determine if previously observed "flow-like" patterns in small system collisions [1–6] are geometry driven and attributable to the formation of quark-gluon plasma (QGP) droplets. PHENIX data [7] demonstrated hierarchies among the elliptic flow  $v_2$  and triangular flow  $v_3$  coefficients, a result that was expected if a strongly interacting system is created, based on the differences in initial geometries.

In contrast to the PHENIX data, results reported by the STAR Collaboration [8, 9] show that the observed  $v_3(p_T)$  are system independent. Sub-nucleon fluctuations are highlighted in [8, 9] as a possible explanation for why initial geometries could be more similar than expected from purely nucleon driven fluctuating geometries.

To understand the differences in the results from STAR and PHENIX, it is important to consider the two experiments' use of different pseudo-rapidity ranges in the two-particle correlation measurements that yield the azimuthal anisotropy coefficients.

While PHENIX measures two-particle correlations between backward rapidity and midrapidity regions [7, 10], STAR employs only the mid-rapidity region [8, 9]. As in small asymmetric systems longitudinal decorrelations are significant [11] and boost-invariance is broken [12–17], a full understanding of the RHIC results requires simulations considering the full (3+1)D dynamics and an initial state that describes the fluctuating geometry as a function of not just the transverse plane but also the longitudinal direction.

In this work, we perform calculations of anisotropic flow in small system collisions at  $\sqrt{s_{NN}}$  = 200 GeV using a (3+1)D framework combining a dynamic initial state with MUSIC viscous relativistic hydrodynamics and hadronic transport [18, 19].

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**Figure 1.** The ration of results for  $v_2(p_T)$  obtained using two different detector combinations compared to PHENIX data [29, 30].

### **2 Model**

We use the 3D-GLAUBER+MUSIC+UROMD hybrid model within the open-source IEBE-MUSIC framework [20] to study particle production and flow in  $p+Au$ ,  $d+Au$ , and  ${}^{3}He+Au$  collisions at  $\sqrt{s_{NN}}$  = 200 GeV. The initial state model deposits energy, momentum, and baryon number dy- $\sqrt{s_{NN}}$  = 200 GeV. The initial state model deposits energy, momentum, and baryon number dynamically into the fluid and obeys exact energy-momentum conservation [19, 21]. Colliding nucleons are determined as in conventional Monte Carlo Glauber models. Their interaction is then implemented by connecting a string between nucleon constituents and having them dynamically decelerate. The rapidity loss is sampled from a phenomenologically motivated distribution that depends on the initial constituent rapidity. The lost energy and momentum are then transferred to the medium via source terms. This method results in events with a fluctuating structure in all three spatial dimensions.

For the fluid system we use the equation of state NEOS-BQS [22] employing strangeness neutrality,  $n_s = 0$ , and setting the net electric charge-to-baryon density ratio to  $n_O/n_B = 0.4$ , a value most appropriate for large nuclei. The specific shear and bulk viscosities are parametrized as functions of baryon chemical potential and temperature with parameters chosen to reproduce the mean transverse momentum and differential flow in central  ${}^{3}He+Au$ collisions. The Cooper-Frye particlization of fluid cells is performed on a hyper-surface with a constant energy density of  $e_{sw}$  =0.50 GeV/fm<sup>3</sup> using the Cornelius algorithm [23] and the open-source code package iSS [24, 25]. The produced hadrons are then fed into the hadron cascade model, urqmd[26–28] for further scatterings and decays until kinetic freeze-out is achieved dynamically.

#### **3 Results**

Our main results, reported in [18], showed that a significant part of the differences between STAR and PHENIX measurements can be explained once the longitudinal structure is included. Here, we support the finding of the importance of longitudinal structure with additional results from our analysis that have not been shown in [18].

First, Fig. 1 shows the ratio of results for  $v_2(p_T)$  using the 3×2PC method for two different detector combinations in PHENIX, FVTXS-CNT-FVTXN (backward-forward, BF) and BBCS-FVTXS-CNT (backward-backward, BB) from our calculation, compared to the PHENIX data[29, 30]. The trends are well described across the different systems with very



**Figure 2.** The differential triangular flow coefficient  $v_3(p_T)$  for charged hadrons using two different methods in three different collision systems compared to PHENIX data [29, 30].

good agreement in p+Au and  ${}^{3}He+Au$  collisions.<sup>1</sup> This is another demonstration of the fact that the longitudinal decorrelations included in our model play an essential role in generating the differences between  $v_2(p_T)$  measurements that use detectors at different rapidities.

The differential triangular flow coefficients from the BB and BF detector combinations are shown in Fig. 2. We find good agreement with the BB data, particularly at  $p_T < 2 \text{ GeV}$ , using mostly backward (Au-going) detectors. In the case of the backward-forward (BF) detector combination, the experiment finds imaginary results (indicated by negative values in the plot) for p+Au and d+Au collision systems, most likely due to a dominance of non-flow, as the dilute proton or deuteron going direction is included.

# **4 Conclusions**

We have shown additional support for an earlier finding [18] that comparisons of hydrodynamic model calculations to small system anisotropic flow data require the consideration of the produced matter's longitudinal structure. The measured ratio of elliptic flow results from PHENIX backward-backward to forward-backward detector combinations is well described for  $p+Au$  and  ${}^{3}He+Au$  systems. For triangular flow no strong conclusion can be drawn as the experimental data is non-flow dominated in the two smallest systems, when the forward (small projectile going) direction is included in the analysis.

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<sup>&</sup>lt;sup>1</sup>We note that both  $v_2(p_T)_{3\times 2PC,BB}$  and  $v_2(p_T)_{3\times 2PC,BF}$  in p+Au collisions are underestimated by the model [18].

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