

5.4.11

Quarkonia as Probes in QCD

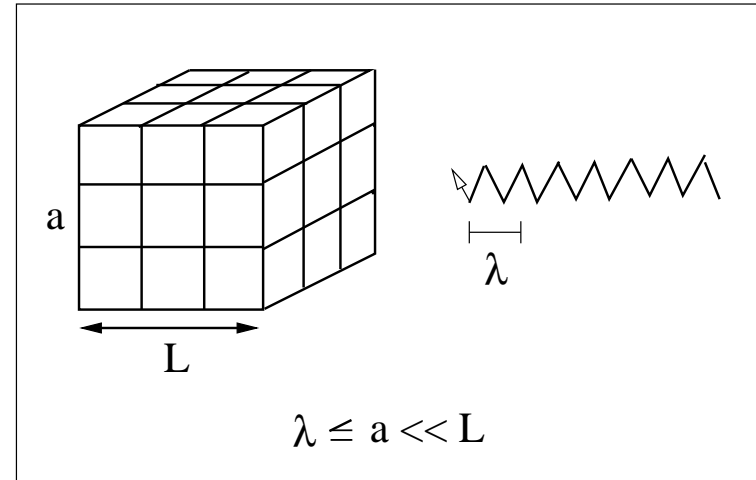
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Quarkonium Production

Wien, April 18, 2011

What is a probe?



resolve substructure
state of matter

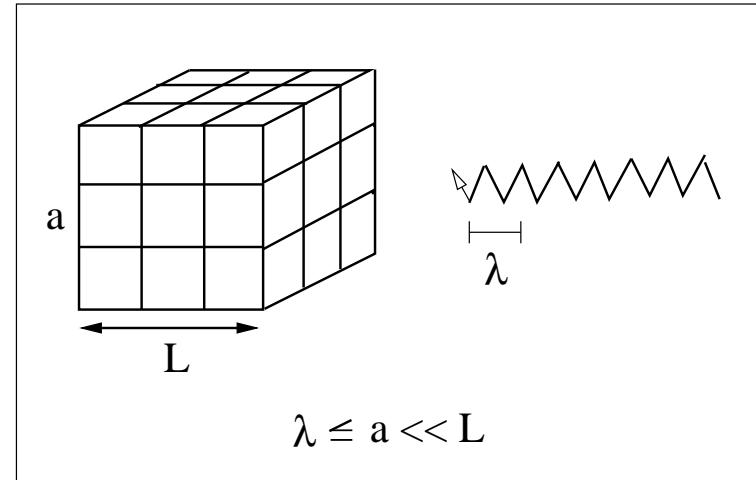
What is a probe?

Substructure in QCD:

hadrons, quarks, gluons

hadrons ~ 1 fm

constituent quarks ~ 0.3 fm



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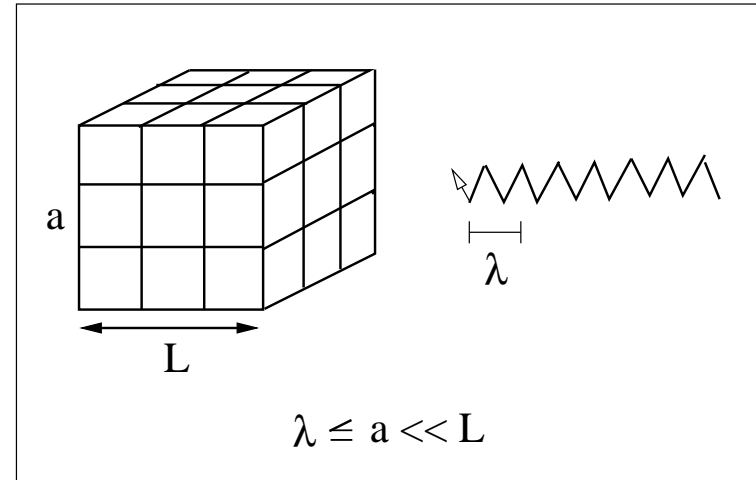
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resolve substructure
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Probes in QCD:

- hard photons (DIS)
- hard gluons (jets)
- quarkonia (J/ψ , Υ)

Quarkonium Physics

- Spectroscopy
- Decay
- Production
- **In-Medium Behavior**
- Determination of QCD Parameters

⇒ *Quarkonium Working Group*

N. Brambilla et al. (QWG), *Heavy Quarkonium Physics*, CERN-2005-005

N. Brambilla et al. (QWG), *Heavy Quarkonium: Progress, Puzzles, and Opportunities*, TUM-EFT 11/10

Quarkonia as probe of deconfinement and QGP

- quarkonia have larger binding energies, smaller radii than usual hadrons
- can therefore survive color screening up to $T > T_c$
- dissociation points of different quarkonium states provide

spectral analysis of QGP

1. What does the probe look like? \Rightarrow the spectrum
2. How can we make the probe? \Rightarrow production dynamics
3. How can we use the probe? \Rightarrow collision aspects

1. The Spectrum

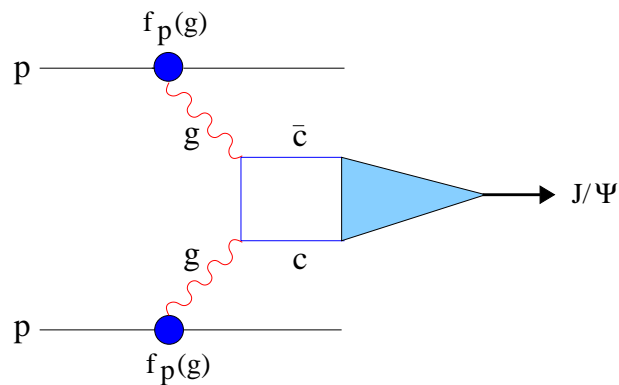
- In Vacuum
 - potential models/Schrödinger equation
 - direct lattice studies
 - NRQCD, pNRQCD

$$\left\{ 2m_c - \frac{1}{m_c} \nabla^2 + \left[\sigma r - \frac{\alpha}{r} \right] \right\} \Phi_i(r) = M_i \Phi_i(r)$$

- In Medium
 - potential models
 - potential from $Q\bar{Q}$ lattice studies
 - direct finite T lattice studies
 - finite T NRQCD, pNRQCD
 - weak coupling studies

2. Production Dynamics

● In Vacuum

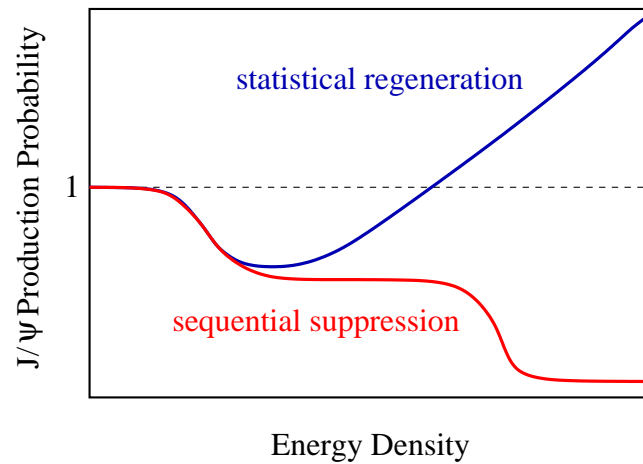


● In Medium

- $Q\bar{Q}$ production
 - PDF
 - LO, NLO, NNLO,...
- color neutralisation
 - color singlet, color octet, NLO...
 - color evaporation
- initial state effects
 - shadowing
 - higher twist, parton energy loss
- final state effects
 - cold nuclear matter
 - hadron interactions
 - parton interactions, color screening

3. Collision Aspects

- In Vacuum
 - feed-down
- In Medium
 - sequential suppression
 - spectral analysis of medium
 - corona
 - regeneration



How does the Production of Quarkonia
differ from that of “usual” Hadrons?

usual hadrons: consist of u, d, s quarks

basic observation in all high energy multihadron production:
statistical production of usual hadrons

partition function of ideal resonance gas

$$\ln Z(T) = V \sum_i \frac{d_i \gamma_s^{n_i}}{(2\pi)^3} \phi(m_i, T)$$

Boltzmann factor $\phi(m_i, T) = 4\pi m_i^2 T K_2(m_i/T)$

hadronisation temperature $T = T_H$,

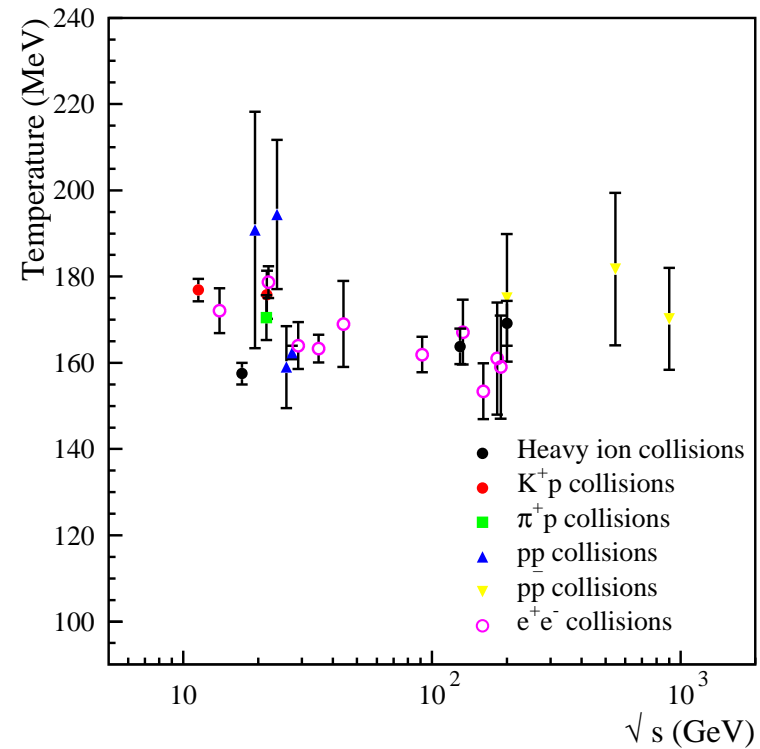
strangeness reduction factor γ_s

all relative abundances given
in terms of T_H and γ_s

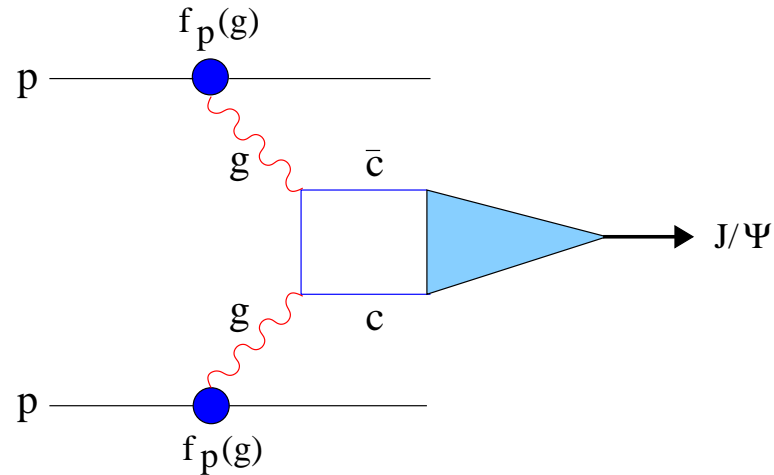
$$\frac{N_i}{N_j} = \frac{d_i \gamma_s^{n_i} \phi(m_i, T)}{d_j \gamma_s^{n_j} \phi(m_j, T)}$$

determines universal
hadronisation temperature
 $T_H \simeq 175 \text{ MeV}$

What about
quarkonium production?



primary production via partonic interaction dynamics



given parton distribution functions from DIS,
 $c\bar{c}$ production is perturbatively calculable (cum grano salis)

J/ψ binding is not, but it is independent of collision energy:

$$R[(J/\psi)/c\bar{c}] \sim |\phi_{J/\psi}(0)|^2 \neq f(s)$$

results for/from elementary collisions:

- $(dN_{c\bar{c}}/dy) \sim s^a$
- $(dN_{\text{ch}}/dy) \sim \ln s$
- $N_{c\bar{c}}/N_{\text{ch}}$ grows with collision energy;
in contrast $N_{s\bar{s}}/N_{\text{ch}} \simeq \text{const.}$

⇒ heavy flavor production is dynamical and not statistical

- $(dN_{J/\psi}/dy)/(dN_{c\bar{c}}/dy) \simeq 0.02,$

statistical weight 0.003; experimental result more than a factor 5 bigger; N_{ρ}/N_{ch} in accord with statistical prediction

⇒ partitioning of heavy flavor production into hidden vs. open is dynamical and not statistical

- $(dN_{\psi'}/dy)/dN_{J/\psi}/dy) \simeq 0.2,$

statistical weight 0.04; experimental result about a factor 5 bigger; N_{ρ}/N_{ω} in accord with statistical prediction

⇒ quarkonium binding is dynamical and not statistical;
ratios of states \sim wave functions, not Boltzmann factors

task for theory:

find QCD description of quarkonium production in elementary collisions

question to experiment:

does QGP formation in nuclear collisions provide a **new mechanism** for the binding of $c\bar{c}$ pairs to quarkonium, in accord with statistical predictions?

What can we (perhaps soon) learn from the LHC?

Schrödinger eq'n $\left\{ 2m_c - \frac{1}{m_c} \nabla^2 + \left[\sigma r - \frac{\alpha}{r} \right] \right\} \Phi_i(r) = M_i \Phi_i(r)$

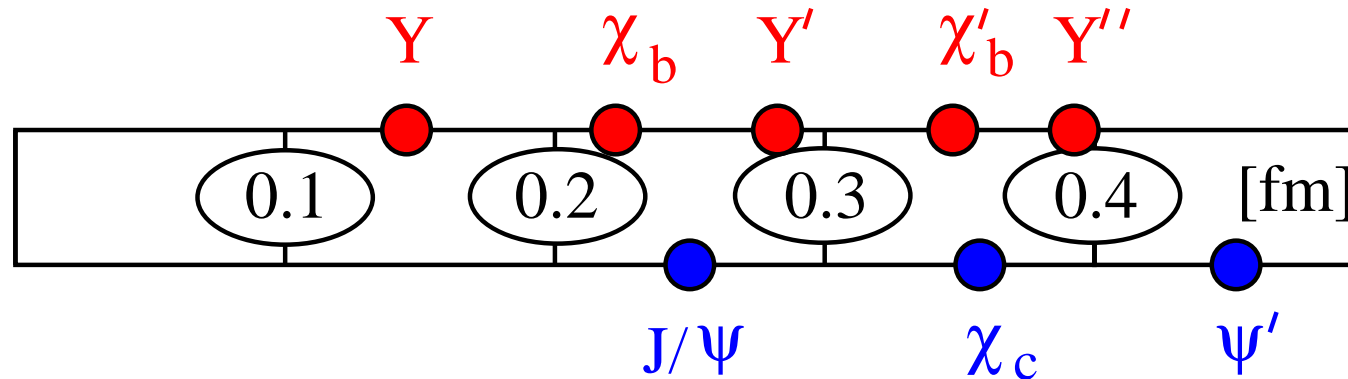
state	J/ψ	χ_c	ψ'	Υ	χ_b	Υ'	χ'_b	Υ''
mass [GeV]	3.10	3.53	3.68	9.46	9.99	10.02	10.26	10.36
ΔE [GeV]	0.64	0.20	0.05	1.10	0.67	0.54	0.31	0.20
radius [fm]	0.25	0.36	0.45	0.14	0.22	0.28	0.34	0.39

$(m_c = 1.25 \text{ GeV}, m_b = 4.65 \text{ GeV}, \sqrt{\sigma} = 0.445 \text{ GeV}, \alpha = \pi/12)$

excellent account of full quarkonium spectroscopy:

spin-averaged masses , binding energies, bound state radii.

consider bound state radii:



color screening:

dissociation when QGP screening radius \leq bound state radius

in-medium quarkonium studies \Rightarrow dissociation temperatures, energy densities

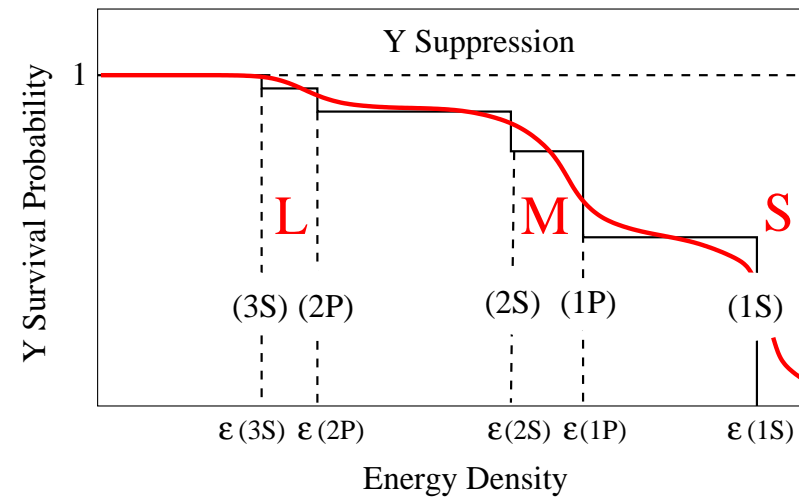
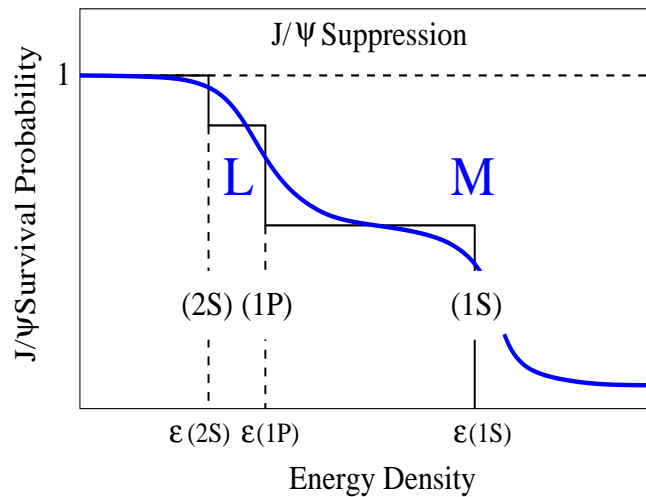
in progress; until then, three groups

- L: ψ' , χ_c , Υ'' , χ'_b
- M: J/ψ , Υ' , χ_b
- S: Υ

sequential suppression of J/ψ and Υ :
observed states are due to direct and feed-down production

state	$J/\psi(1S)$	$\chi_c(1P)$	$\psi'(2S)$
%	60 ± 6	10 ± 5	30 ± 7

state	$\Upsilon(1S)$	$\chi_b(1P)$	$\Upsilon(2S)$	$\chi_b(2P)$	$\Upsilon(3S)$
%	50 ± 10	27 ± 10	11 ± 6	11 ± 5	1 ± 0.5



NB:

J/ψ feed-down from B decay to be removed in comparison.

General qualitative picture:

Where J/ψ disappears, except for corona effect and B decay, Υ production drops to about 50 %.

Dissociation points and L , M , S splittings are in principle calculable through in-medium QCD quarkonium studies.

⇒ Possible direct comparison between QCD results and data.

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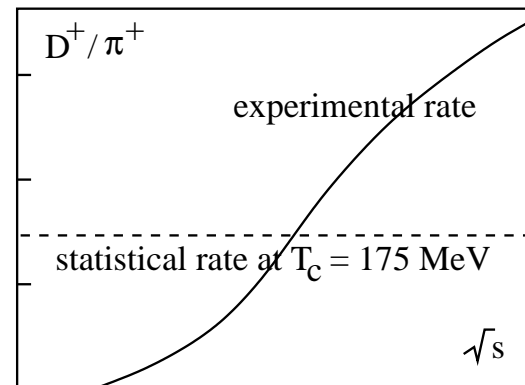
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Impossible: statistical J/ψ formation at hadronization

Statistical hadronization of charmonia

- $c\bar{c}$ production is a dynamical “hard process”:
with increasing energy,
charm to light quark ratio increases
- assume
 - charm quarks form part of equilibrium QGP at T_c
 - equilibrium QGP at T_c hadronizes statistically
 - **charmonium production via statistical $c\bar{c}$ fusion**
- “secondary” charmonium production by fusion of c and \bar{c} produced in different primary collisions
- insignificant at “low” energy, since very few charm quarks;
could be dominant production mechanism at high energy



- simplified illustration...assume at “LHC” per event

100 $c\bar{c}$ pairs

1000 $q\bar{q}$ pairs

charm supersaturation;

chemical equilibrium: charm/light $\sim 10^{-3}$ at $T_c = 175$ MeV

primary rates:

1 J/ψ , 99 D , 99 \bar{D} , 901 light hadrons $\Rightarrow R_{AA} \simeq 1$

statistical combination of given quark abundances:

10 J/ψ , 90 D , 90 \bar{D} , 910 light hadrons $\Rightarrow R_{AA} \simeq 10$

ratio of hidden/open charm

$\Rightarrow (J/\psi)/D \simeq 0.1$ instead of 0.01 in pp

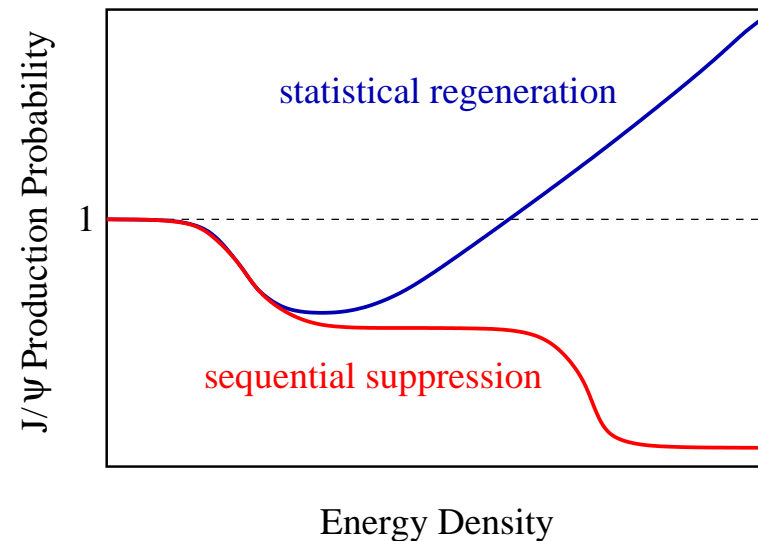
For statistical recombination, re scaled pp rate

$\Rightarrow J/\psi$ production strongly enhanced

\Rightarrow ratio of hidden/open charm strongly enhanced

while for sequential suppression, both are strongly reduced

two readily distinguishable
predictions for
anomalous J/ψ production



also: dynamical vs. statistical momentum spectra

NB: model of statistical quarkonium binding
mechanism existing only in AA ?

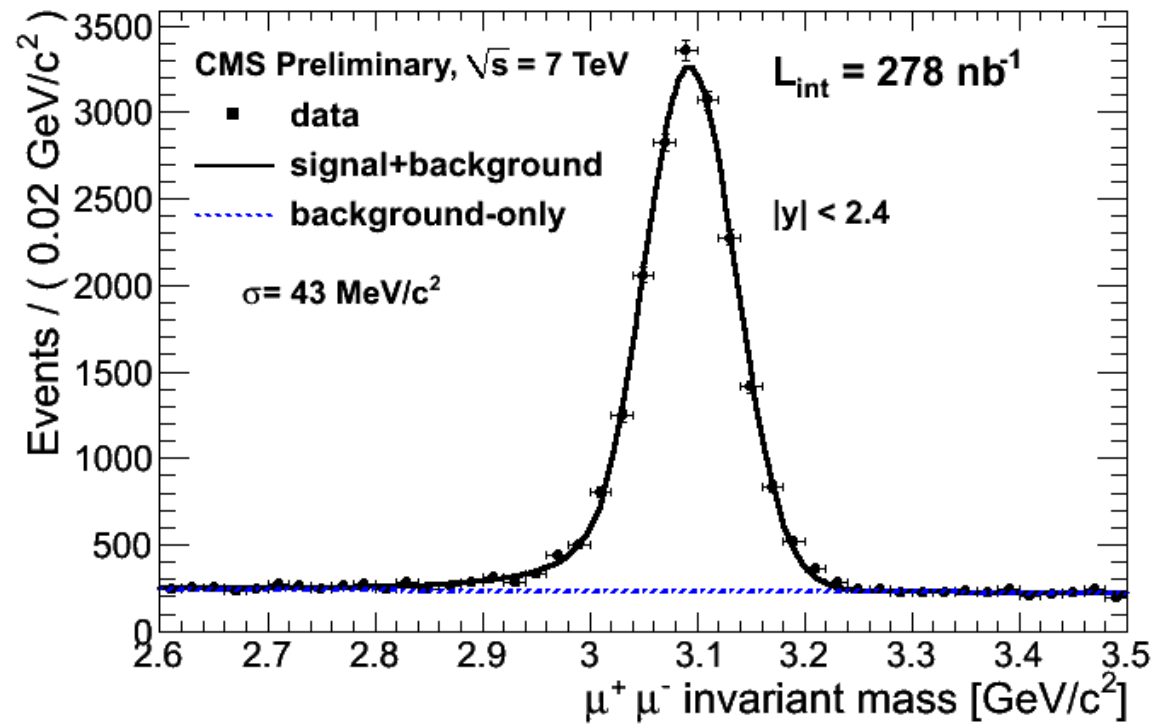
For $c\bar{c}$ production in pp at LHC, per rapidity interval

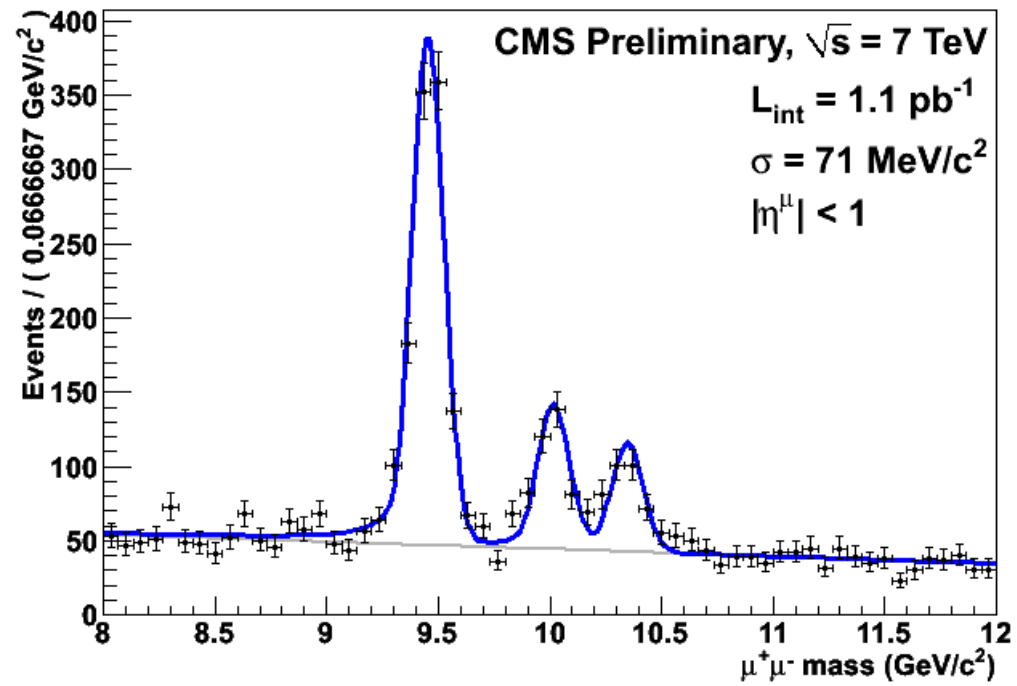
$$\exists \text{ per } c\bar{c} \text{ pair } \sim 10 \text{ } q\bar{q} \text{ pairs}$$

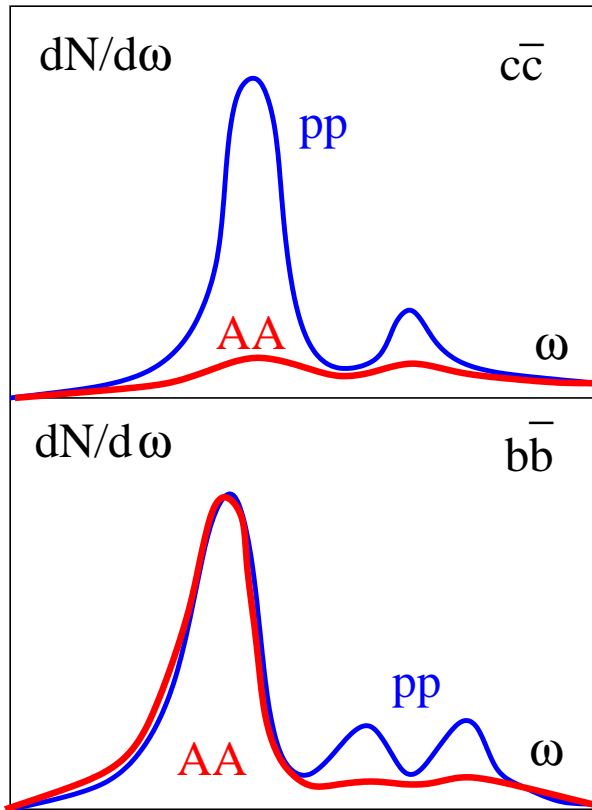
statistical combination implies

- ratio hidden/open charm ~ 0.1
- experimental ratio ~ 0.01

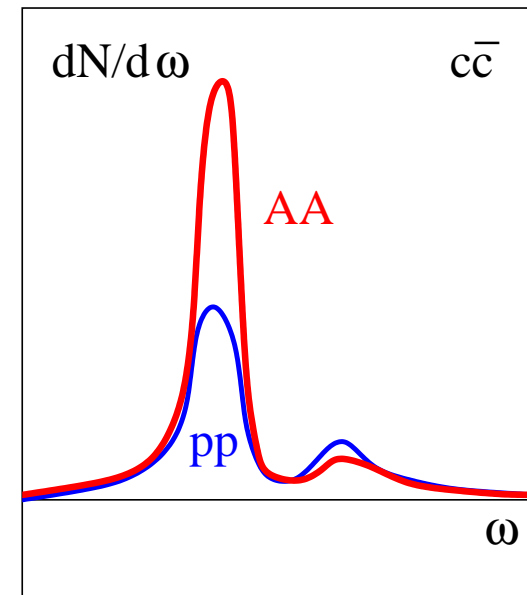
at T_c ,
 $c\bar{c}$ separation scale too large to allow charmonium binding?







sequential suppression
by color screening:
only (possible) survivor is Υ



statistical regeneration:
more J/ψ than in
scaled pp

Conclusions

Given reference measurements of open charm/bottom production,
experimental quarkonium studies at the LHC can ask
conceptual questions and provide
conceptual answers to these.

Quantitative details require specific theory/model input.