



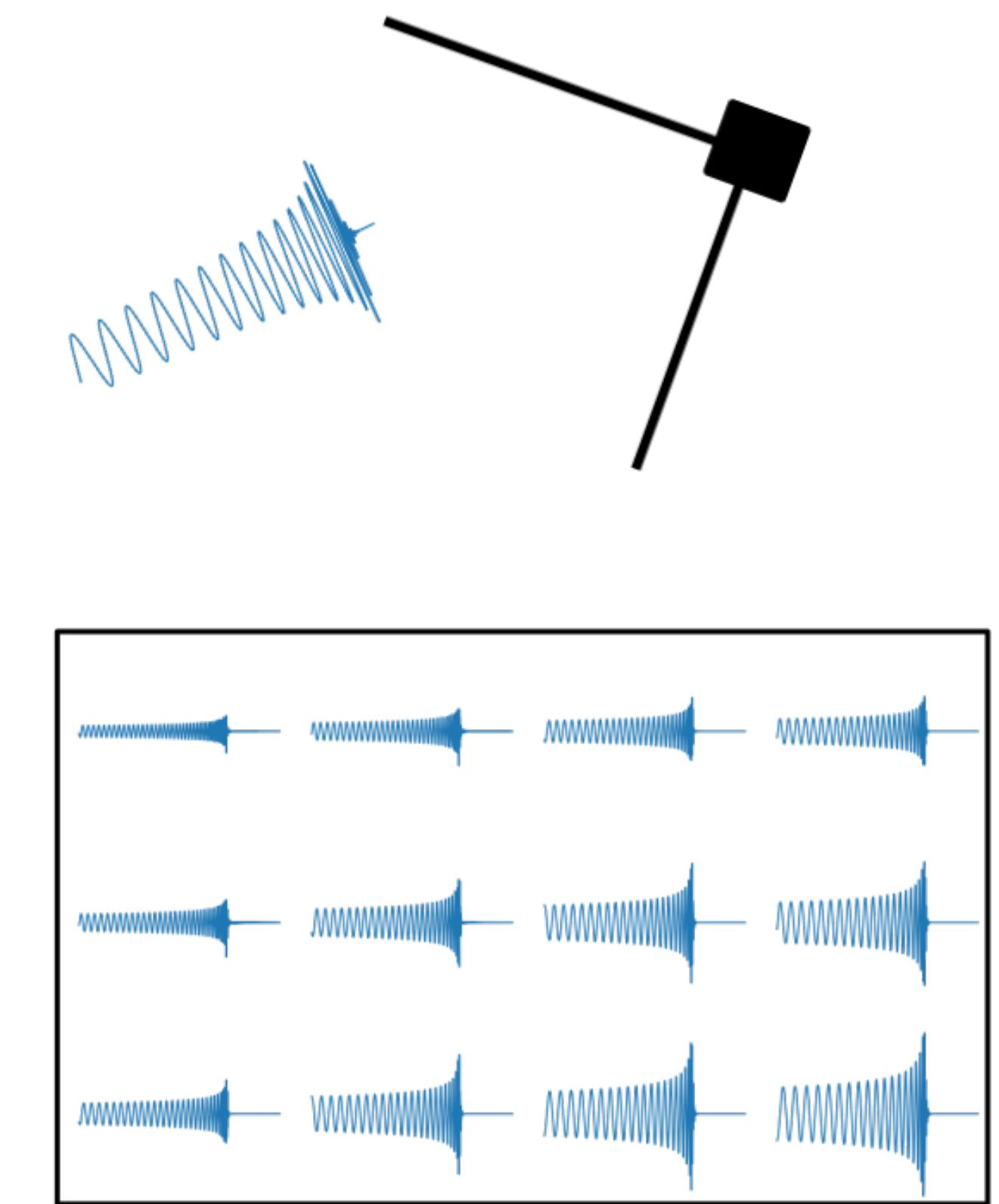
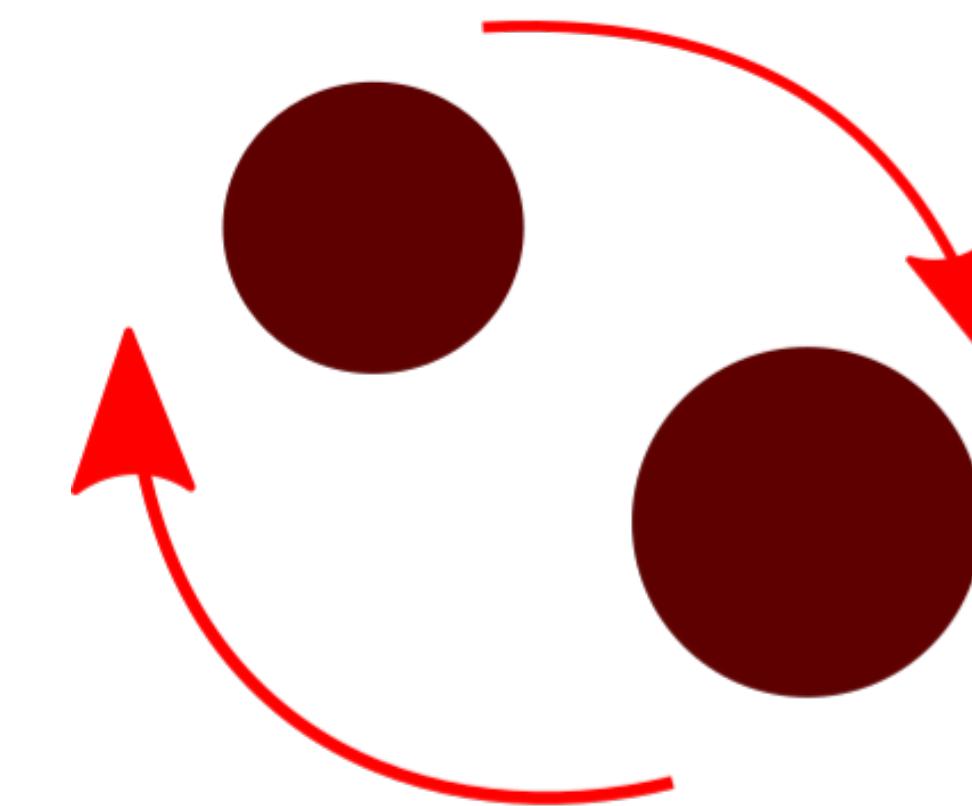
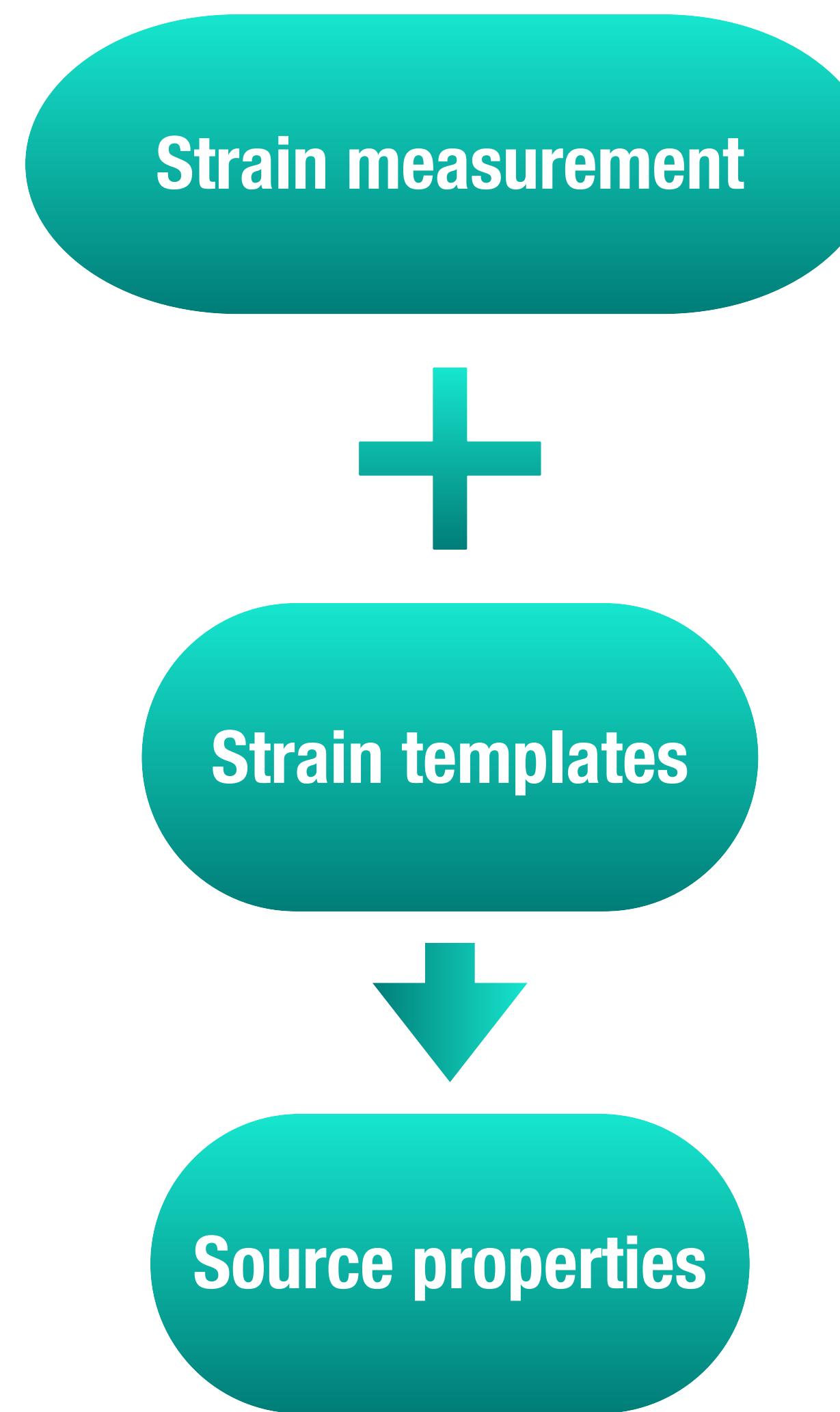
Gravitational-wave parameter inference with the Newman-Penrose scalar

**Juan Calderón Bustillo, Isaac C. F. Wong, Nicolas Sanchis-Gual,
Samson H. W. Leong, Alejandro Torres-Forné, Koustav Chandra,
José A. Font, Carlos Herdeiro, Eugen Radu, and Tjonne G. F. Li**

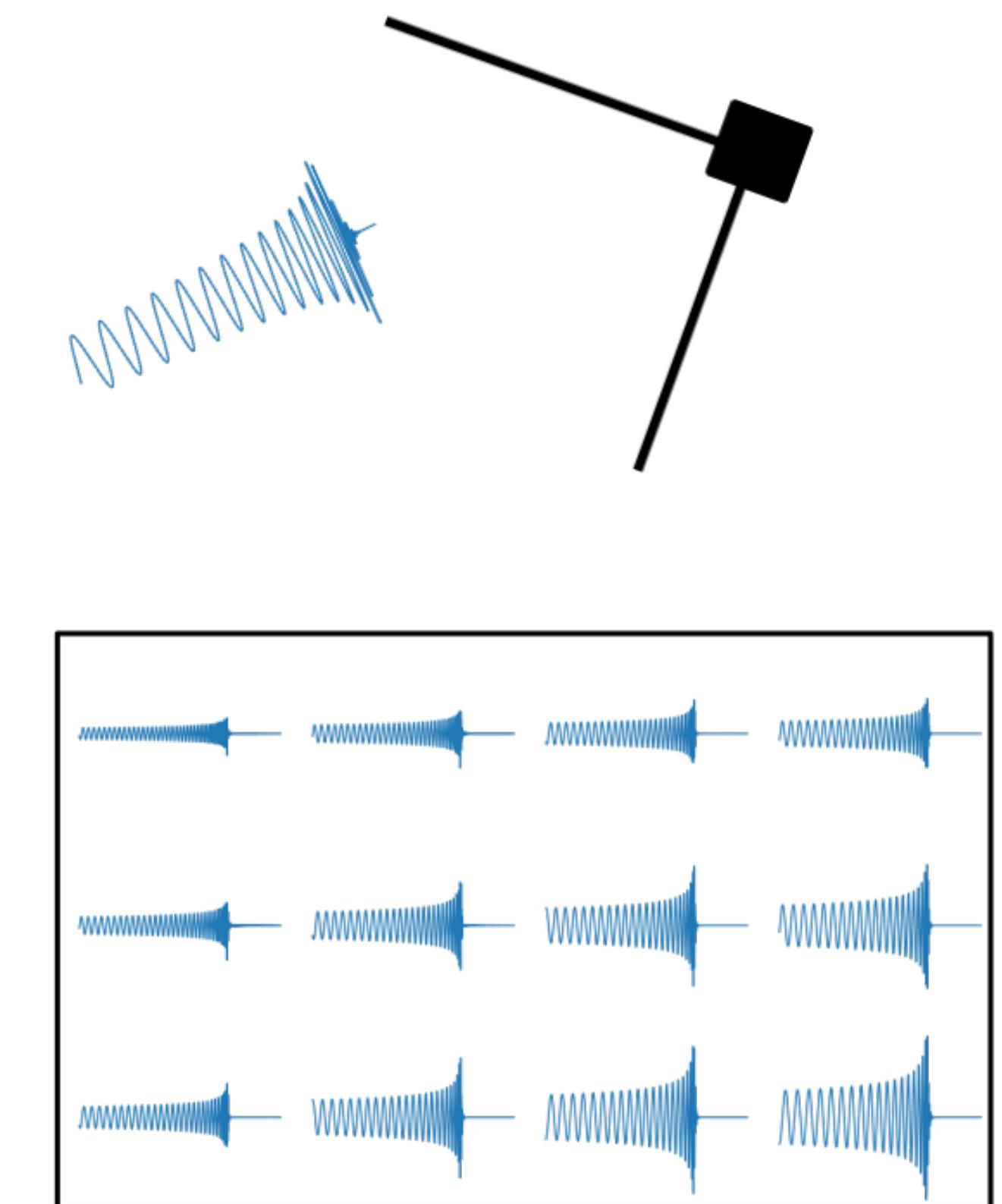
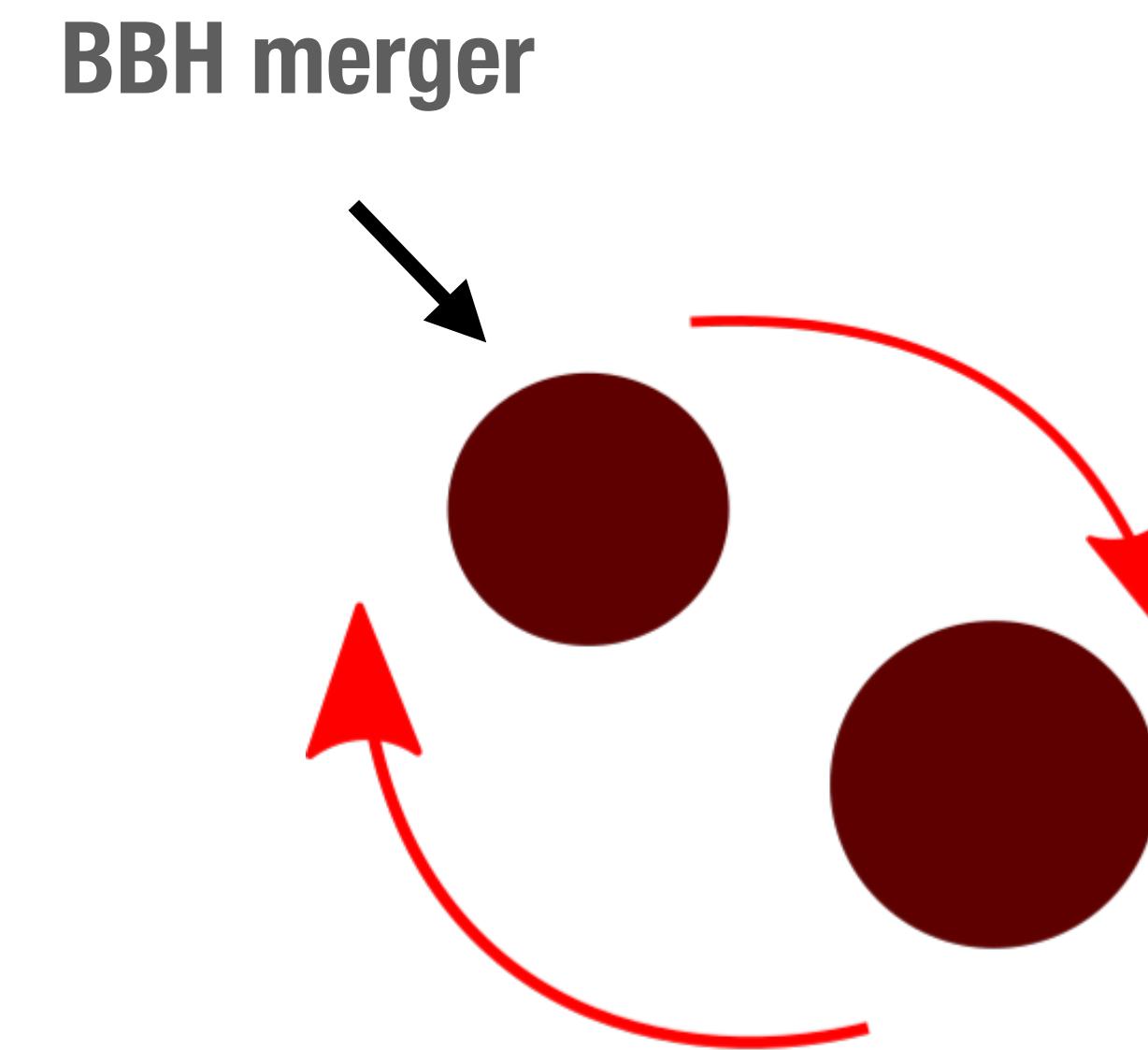
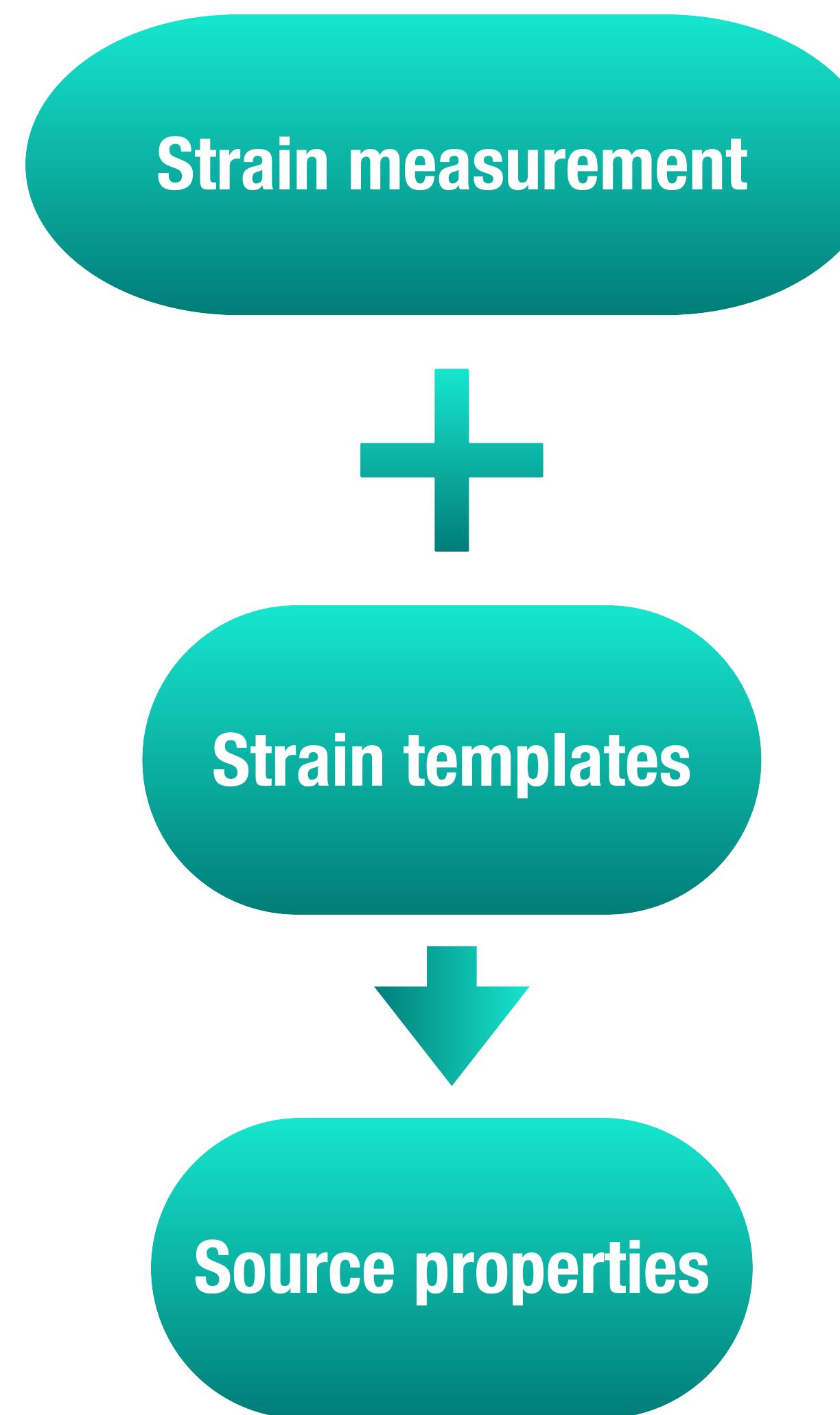
Speaker: Isaac C. F. Wong

arXiv: 2205:15029

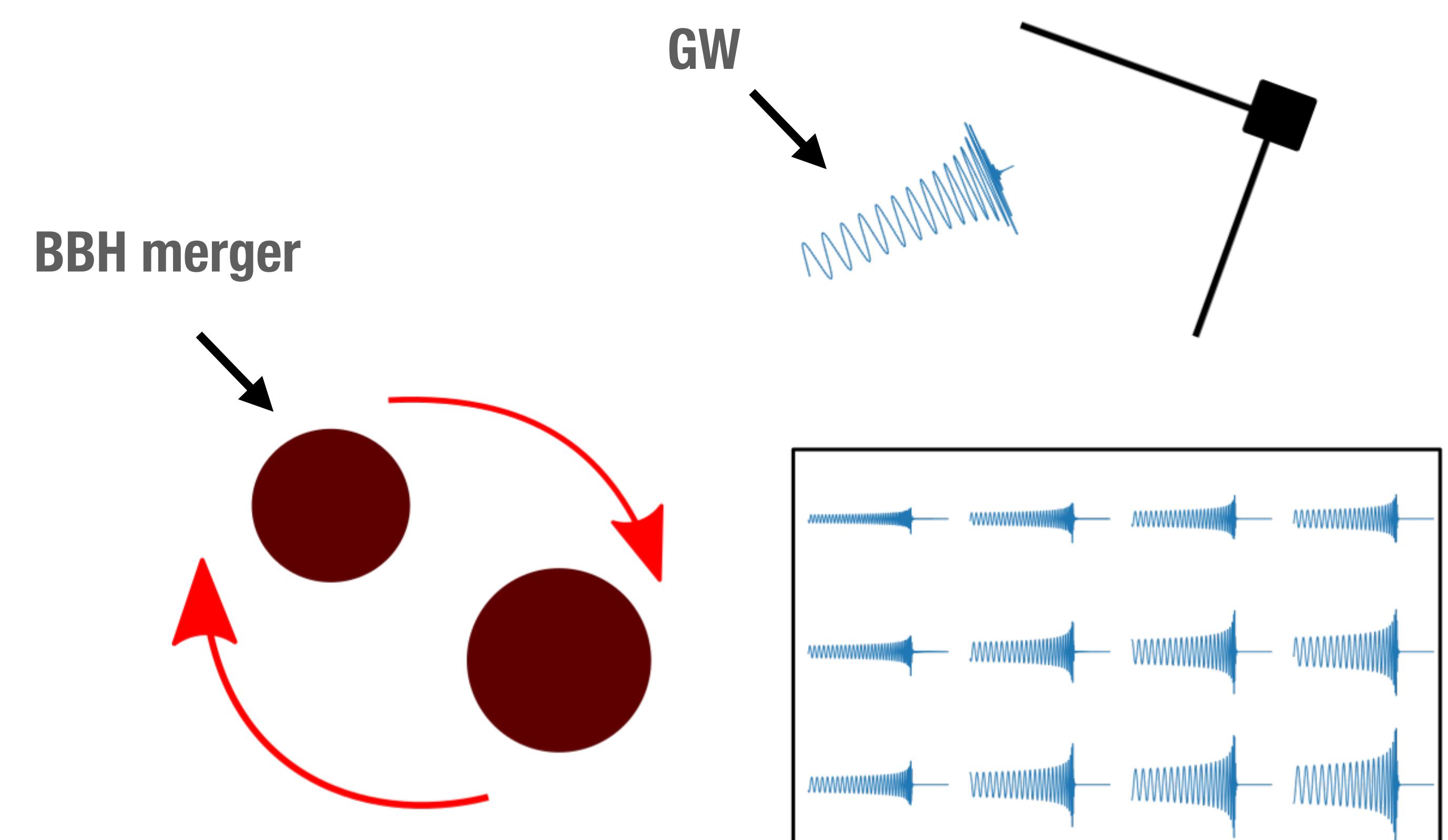
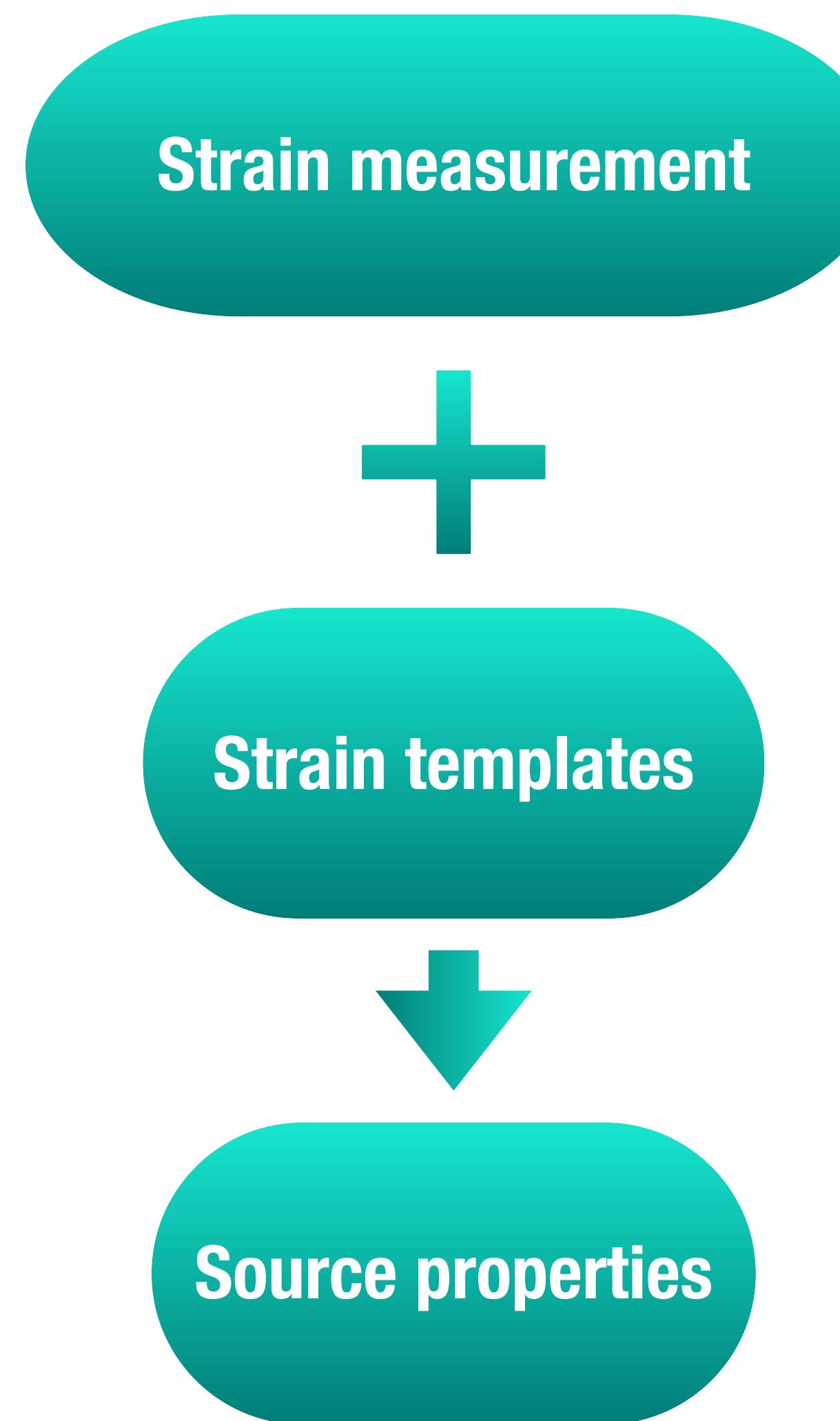
The usual way that we perform data analysis



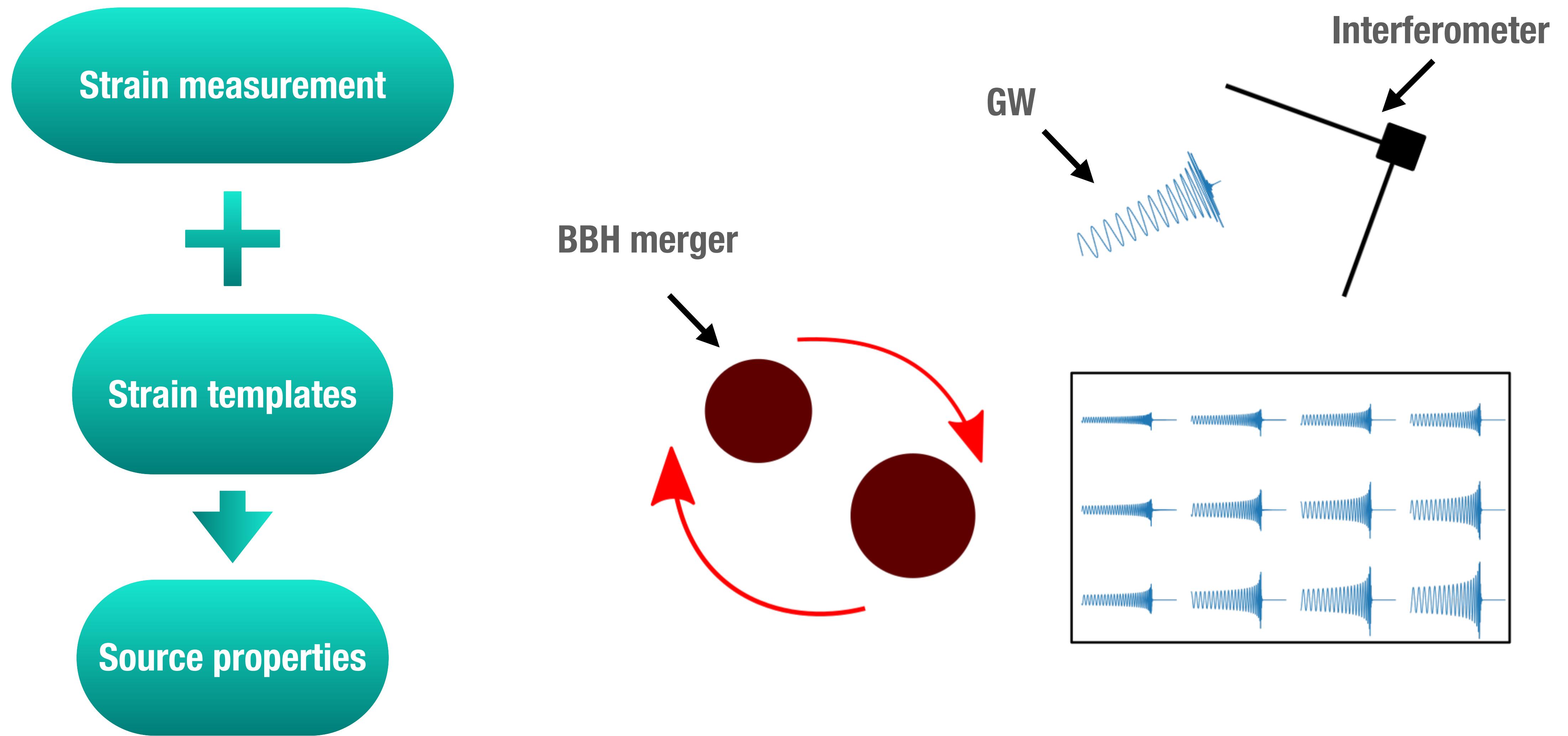
The usual way that we perform data analysis



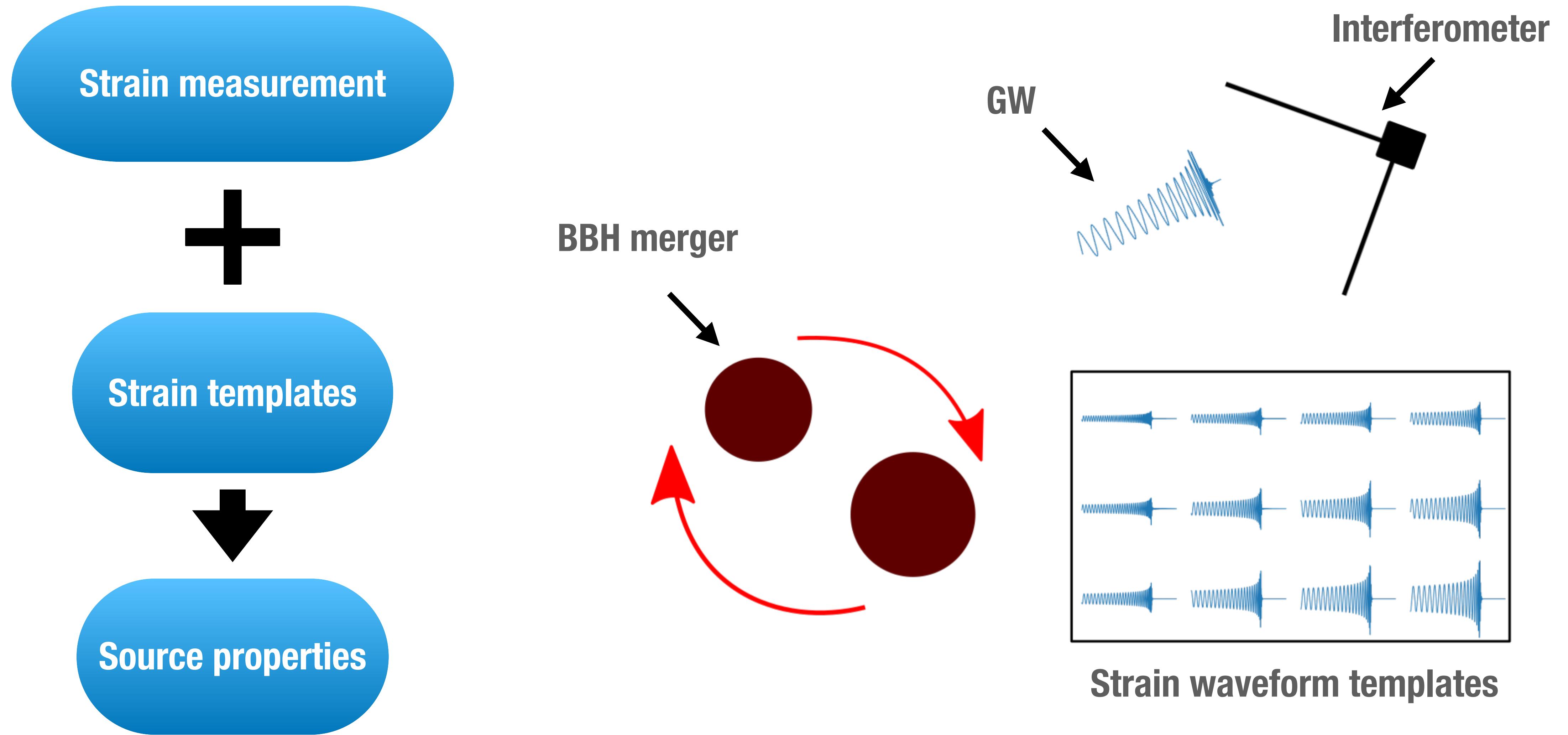
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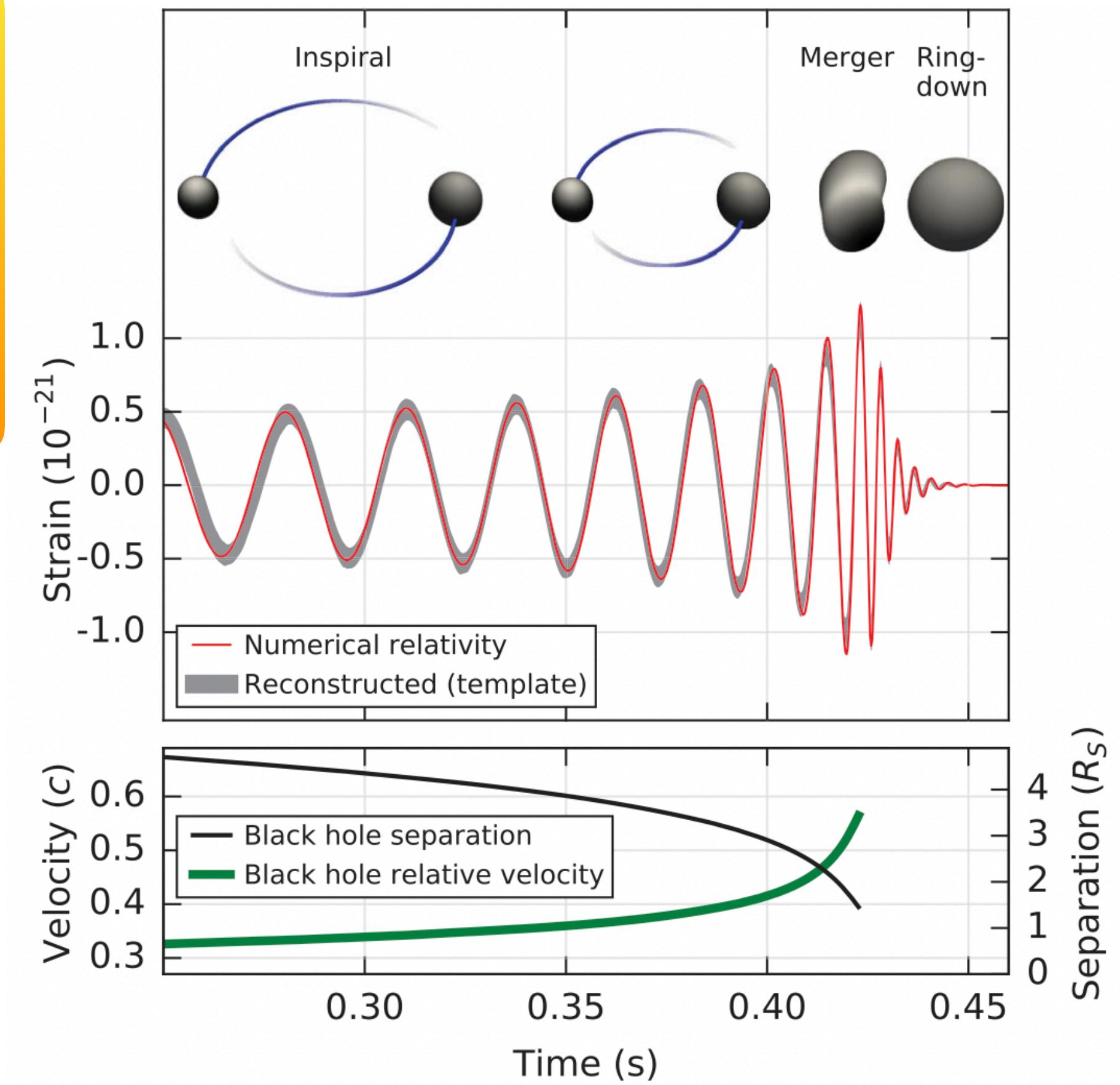
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The usual way that we perform data analysis

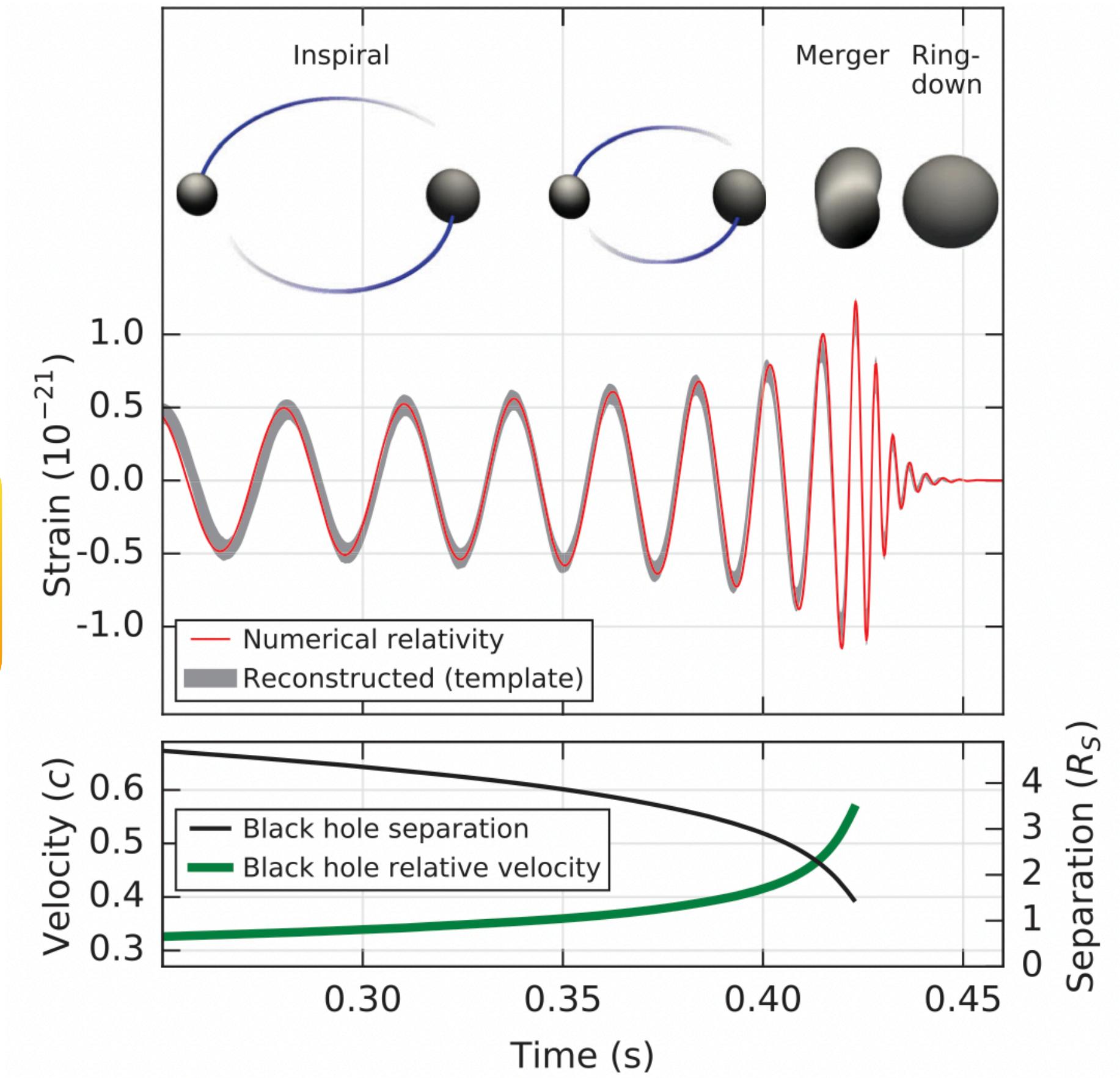


We need NR simulations



LIGO and Virgo Collaboration [1602.03837]

We need NR simulations



LIGO and Virgo Collaboration [1602.03837]

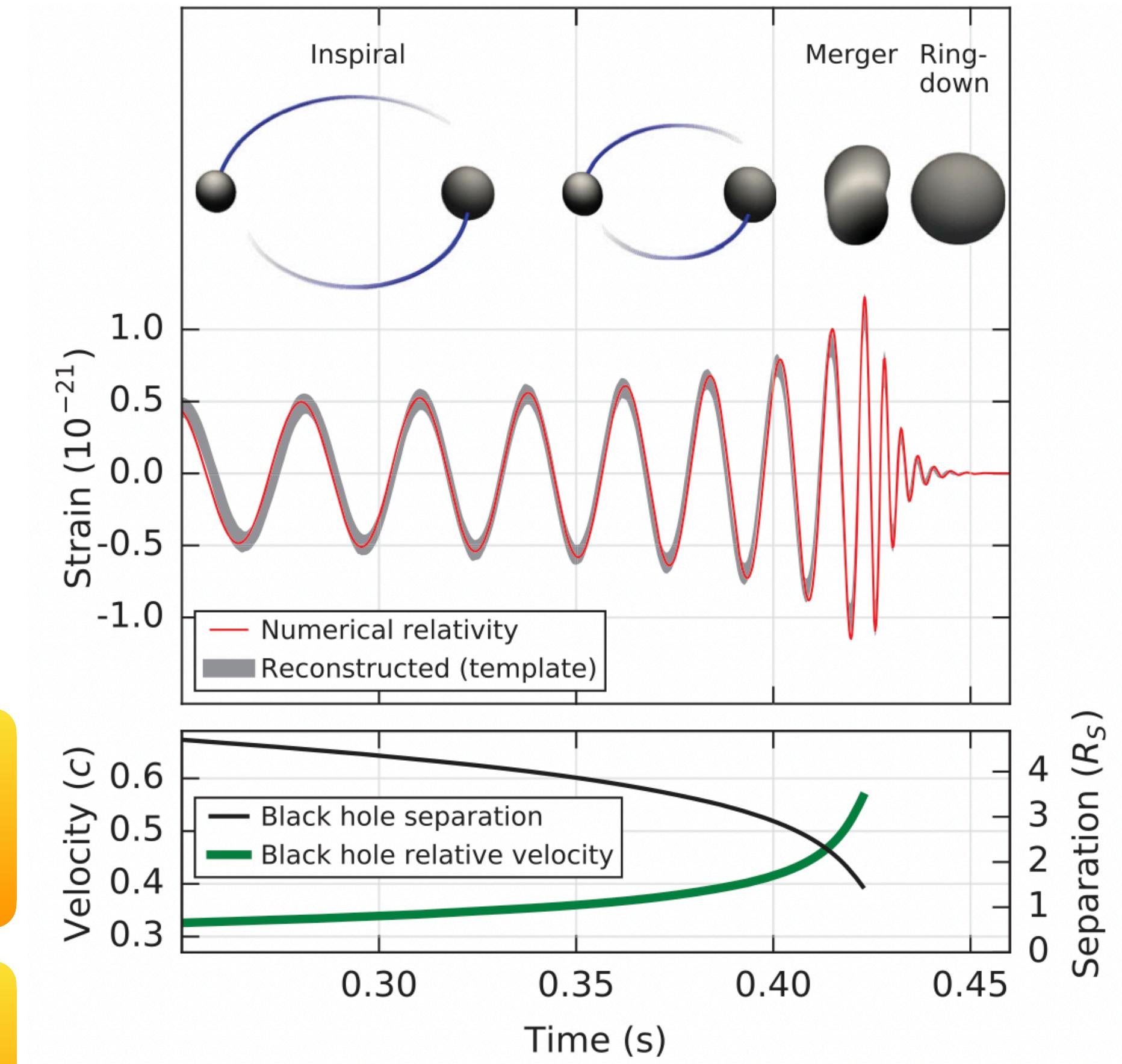
We need NR simulations

Highly eccentric & precessing

NR simulation

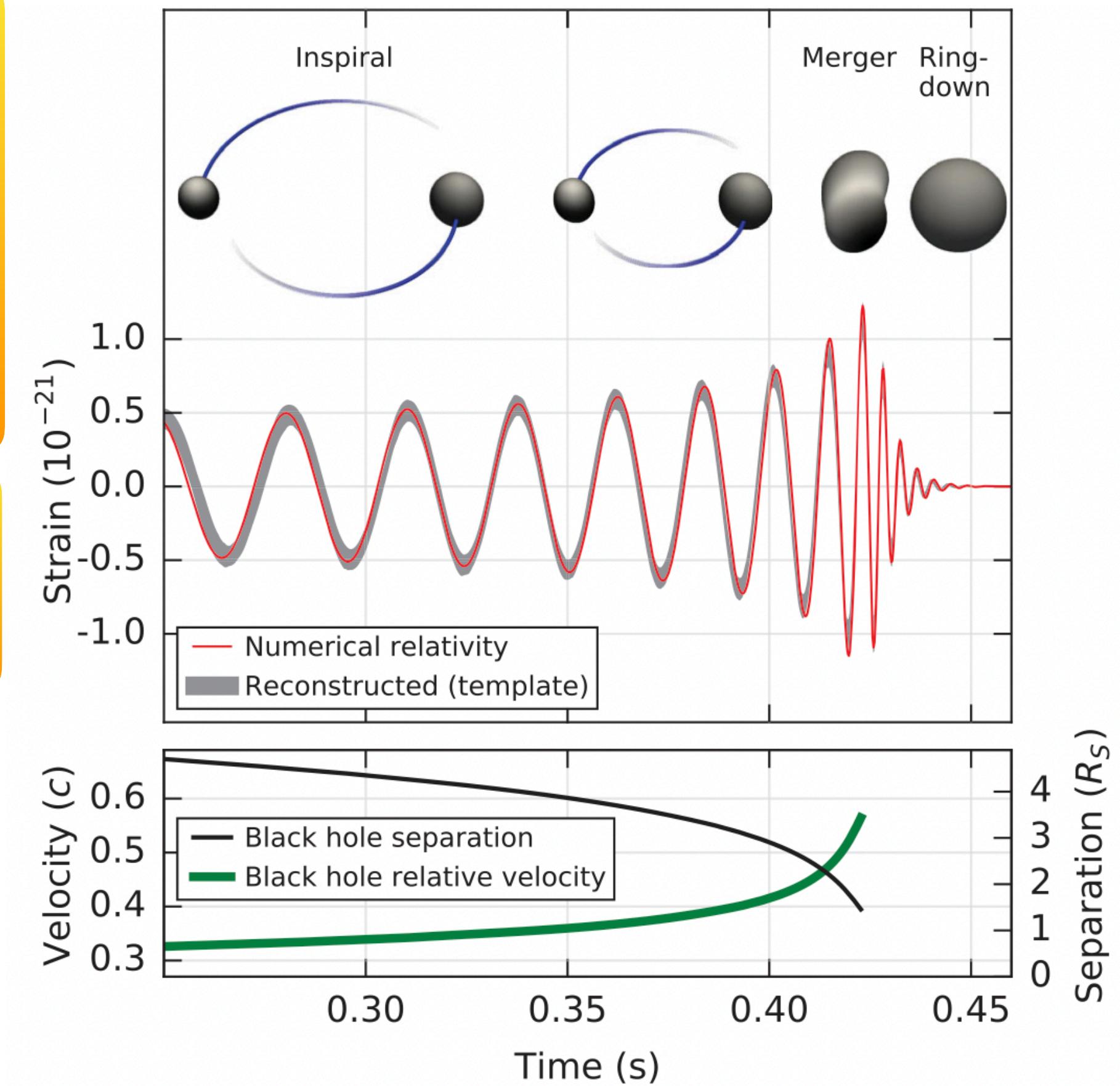
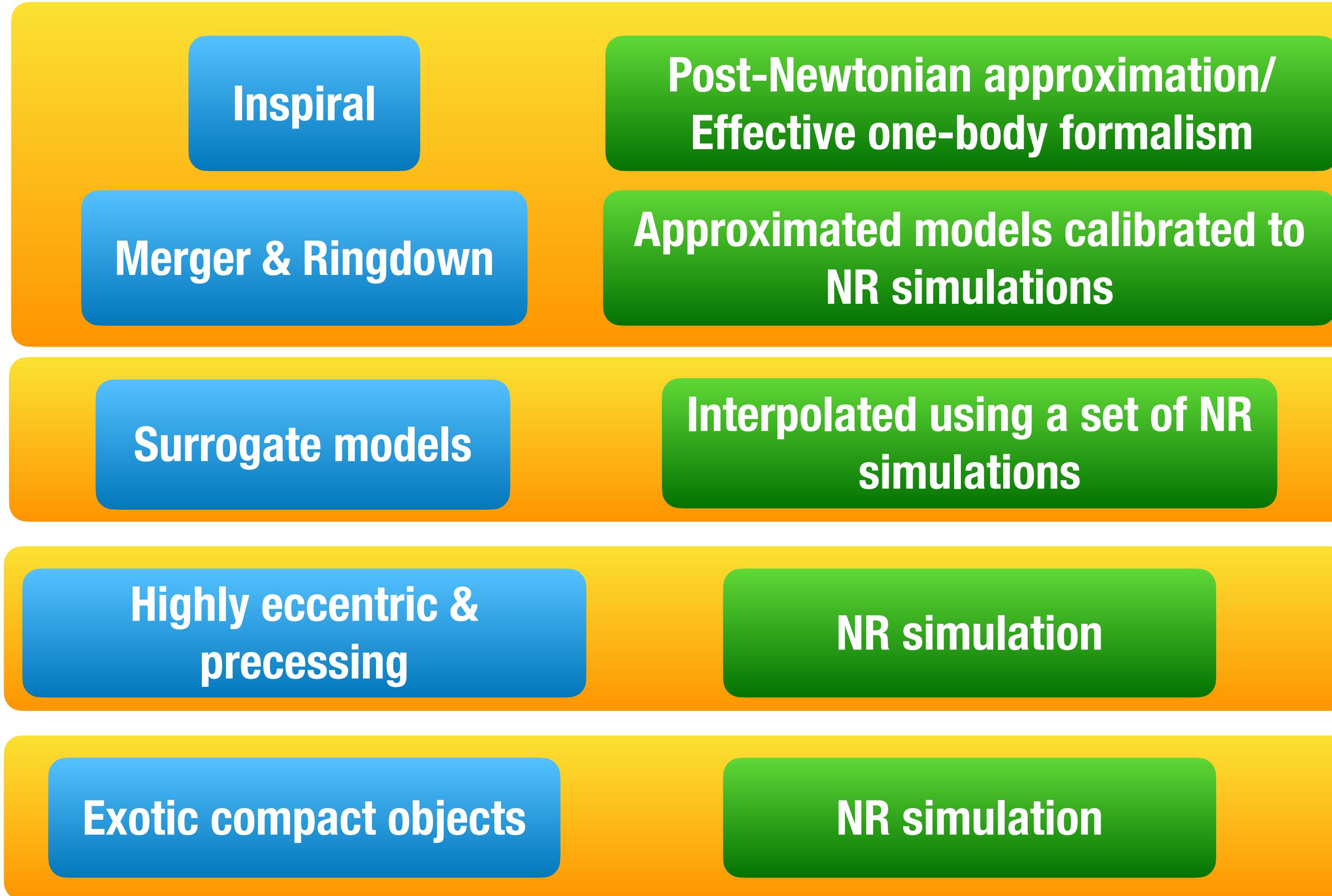
Exotic compact objects

NR simulation



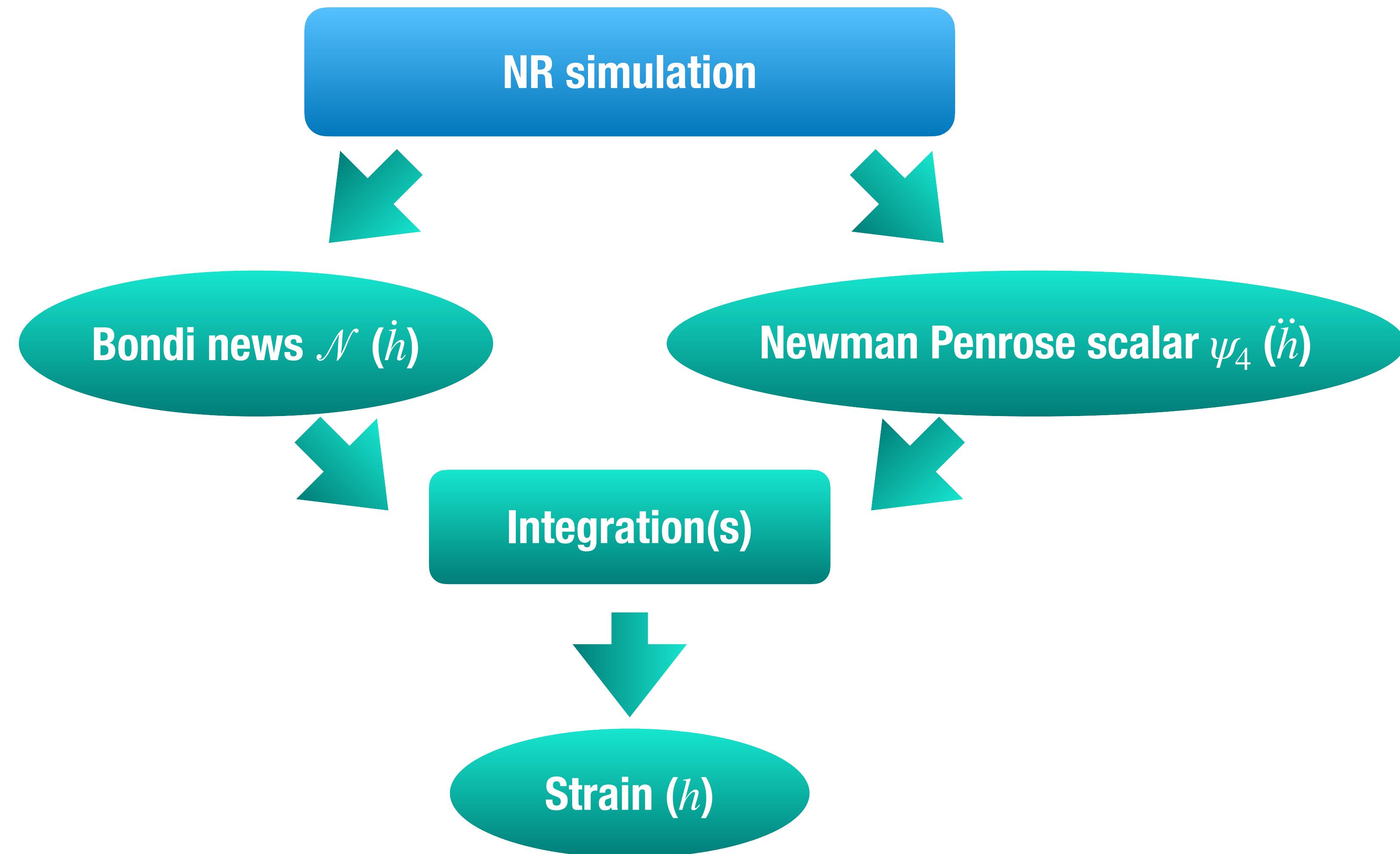
LIGO and Virgo Collaboration [1602.03837]

We need NR simulations

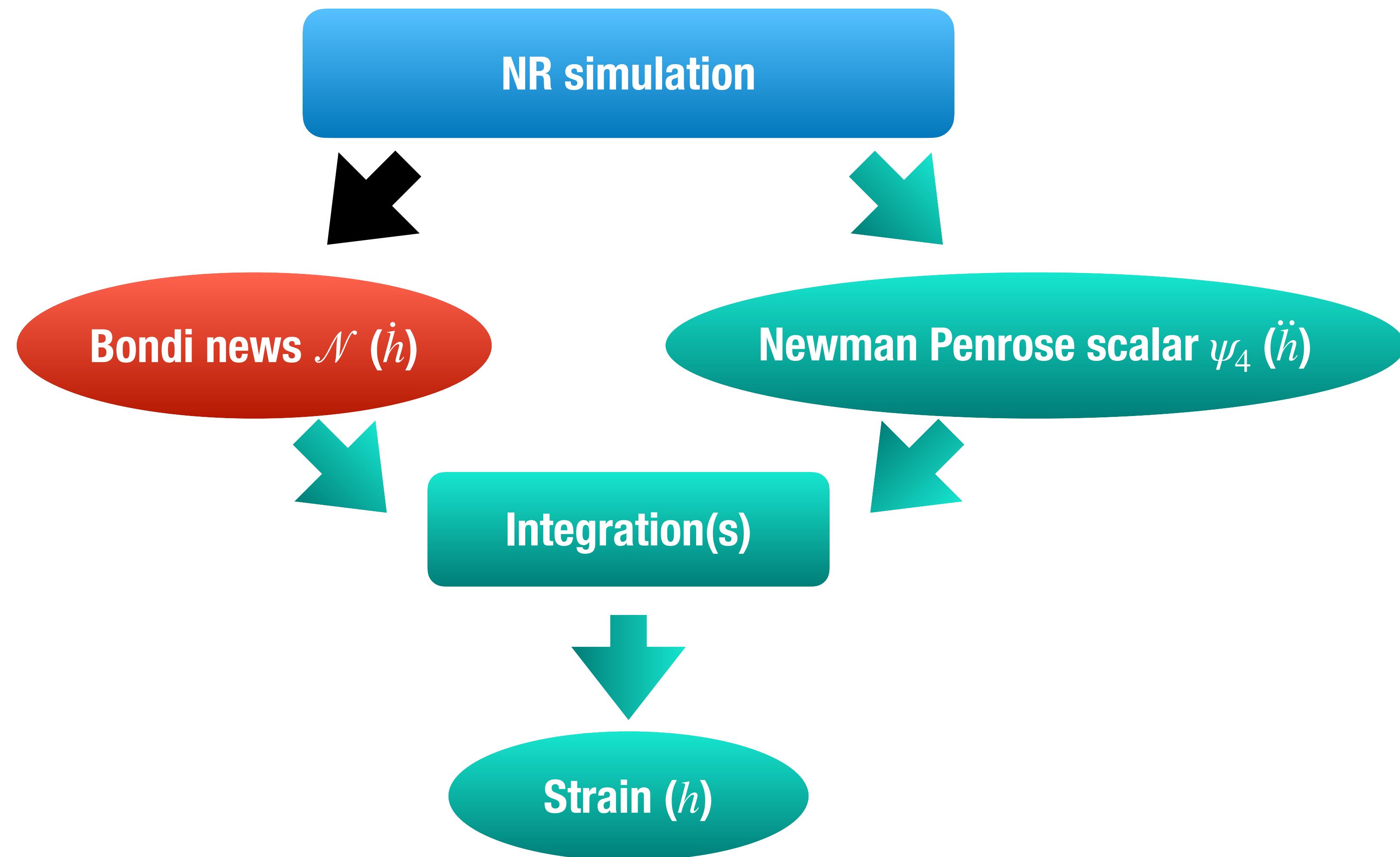


LIGO and Virgo Collaboration [1602.03837]

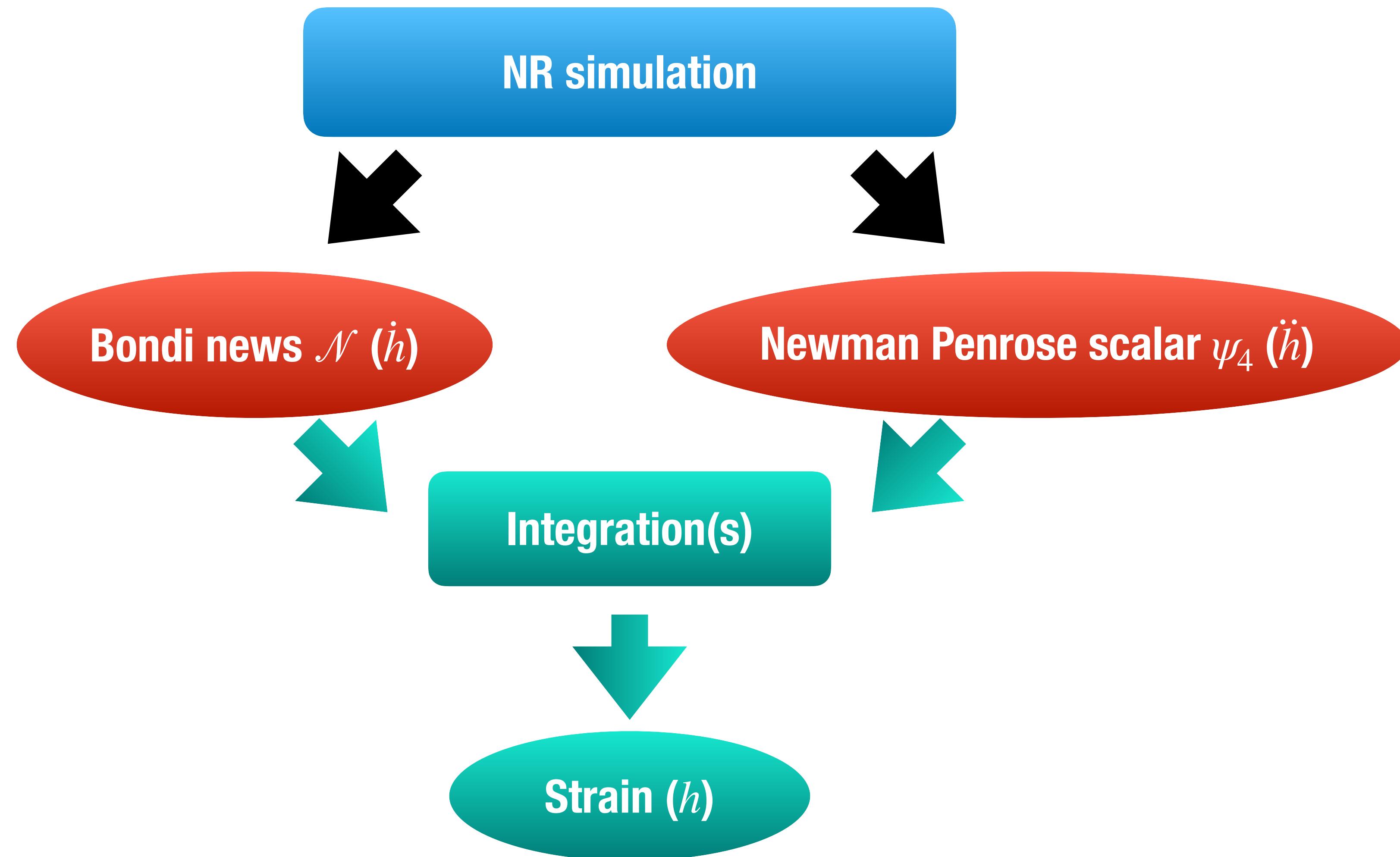
But... NR simulations do not give strain



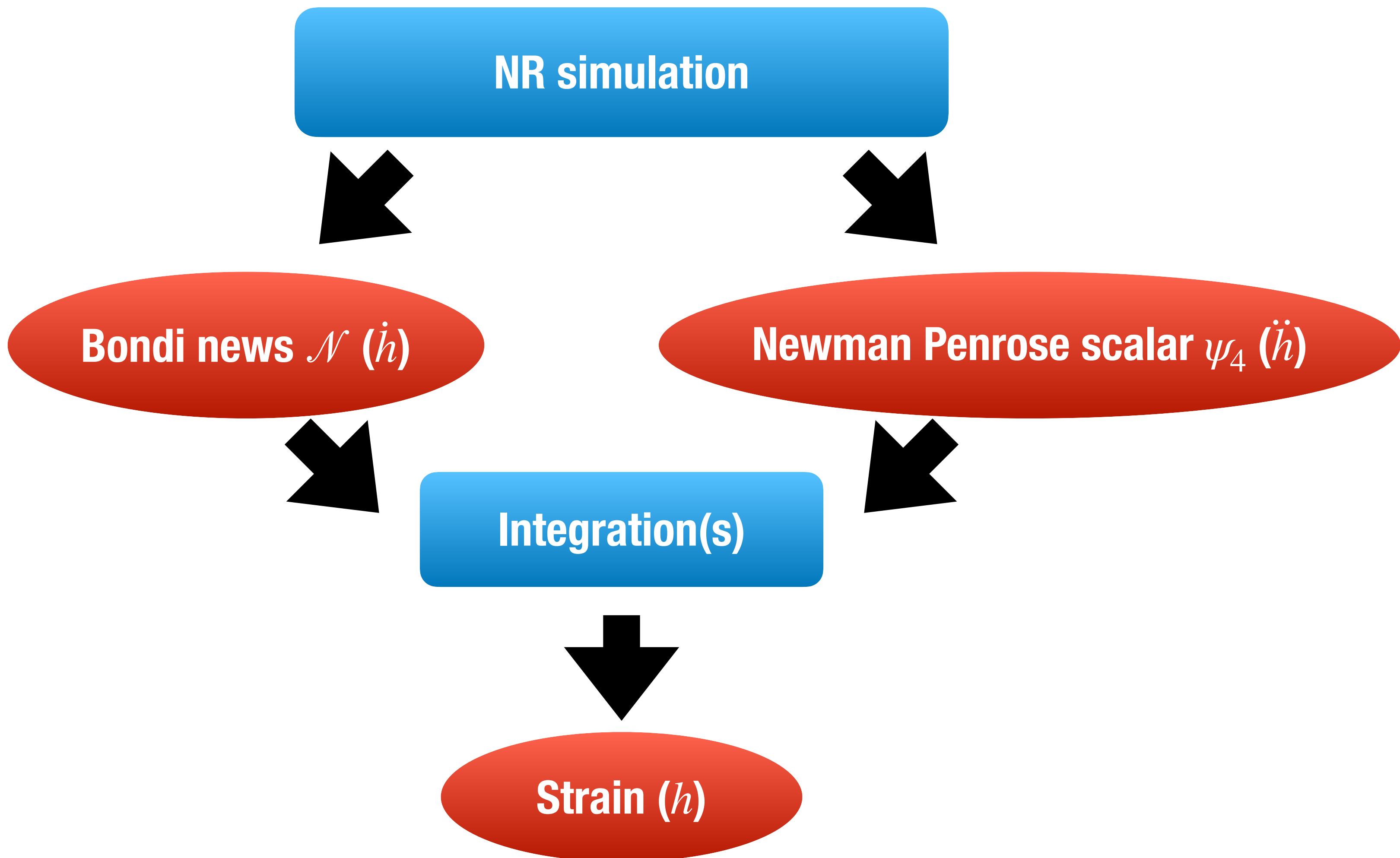
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But... NR simulations do not give strain



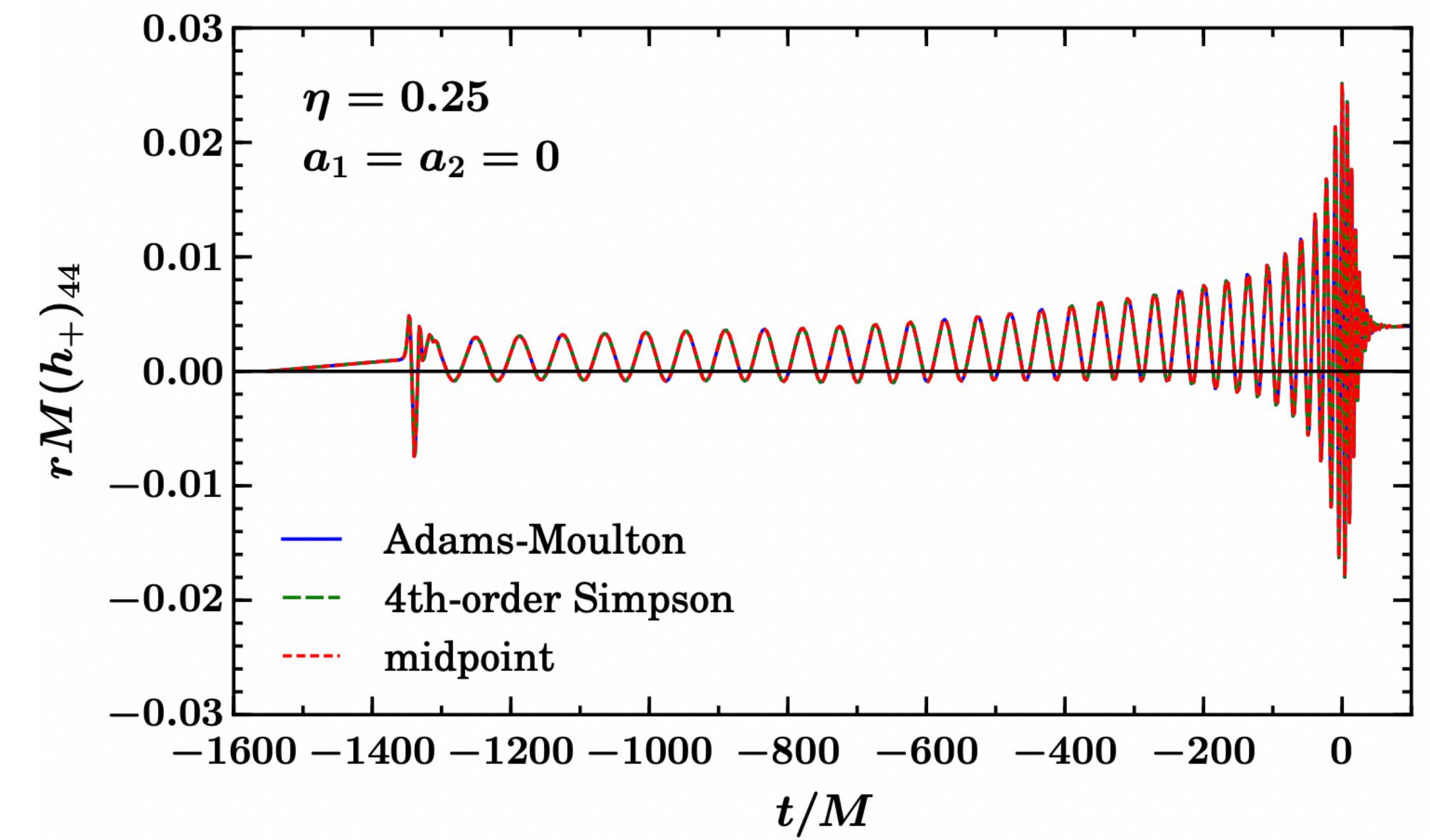
But... NR simulations do not give strain



Caveats

Time-domain integration

$$h = h_+ - i h_\times = \int_{-\infty}^t dt' \int_{-\infty}^{t'} dt'' \psi_4$$



Reisswig + Pollney (2011) [1006.1632]

Caveats

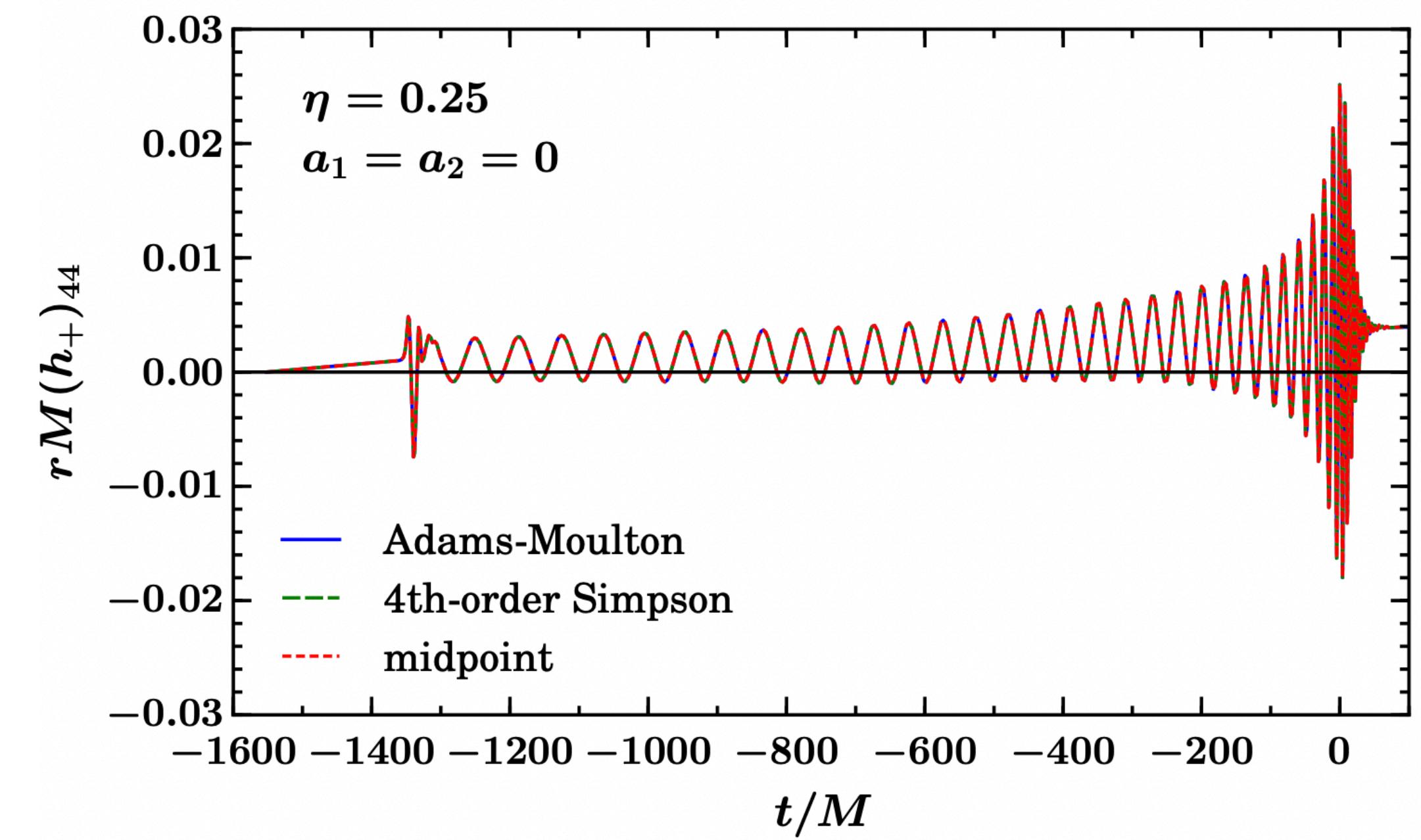
Time-domain integration

Discretely sampled

Finite length

Numerical noise

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Reisswig + Pollney (2011) [1006.1632]

Caveats

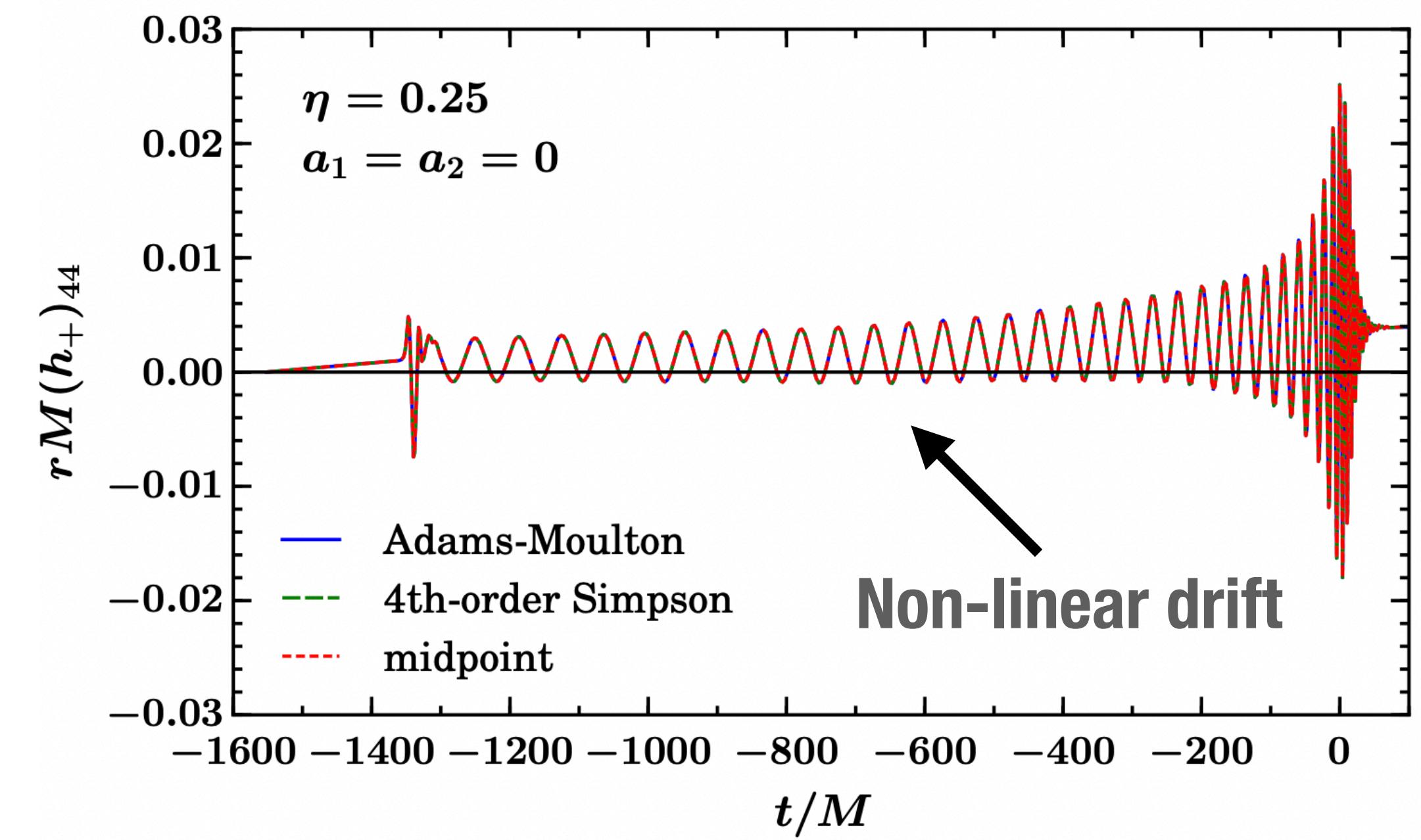
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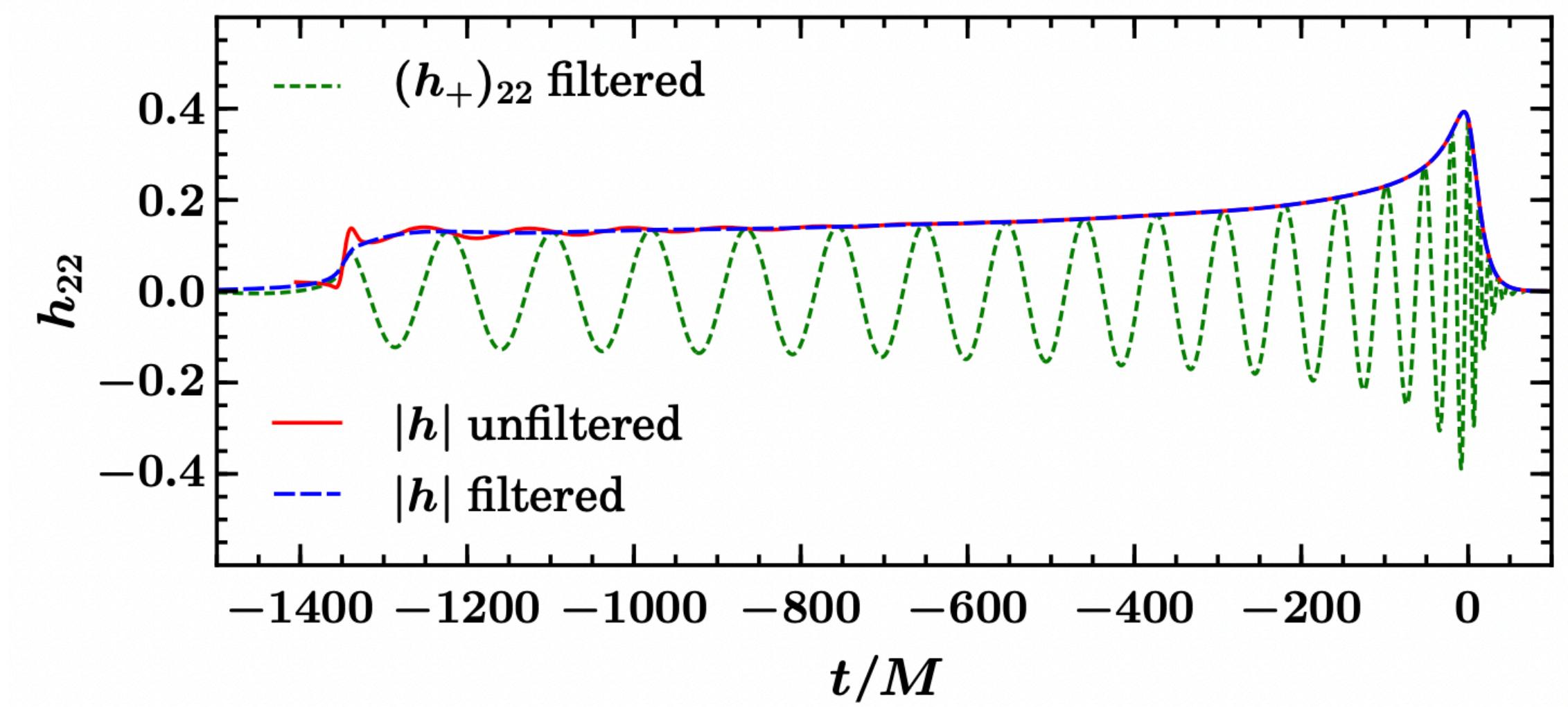
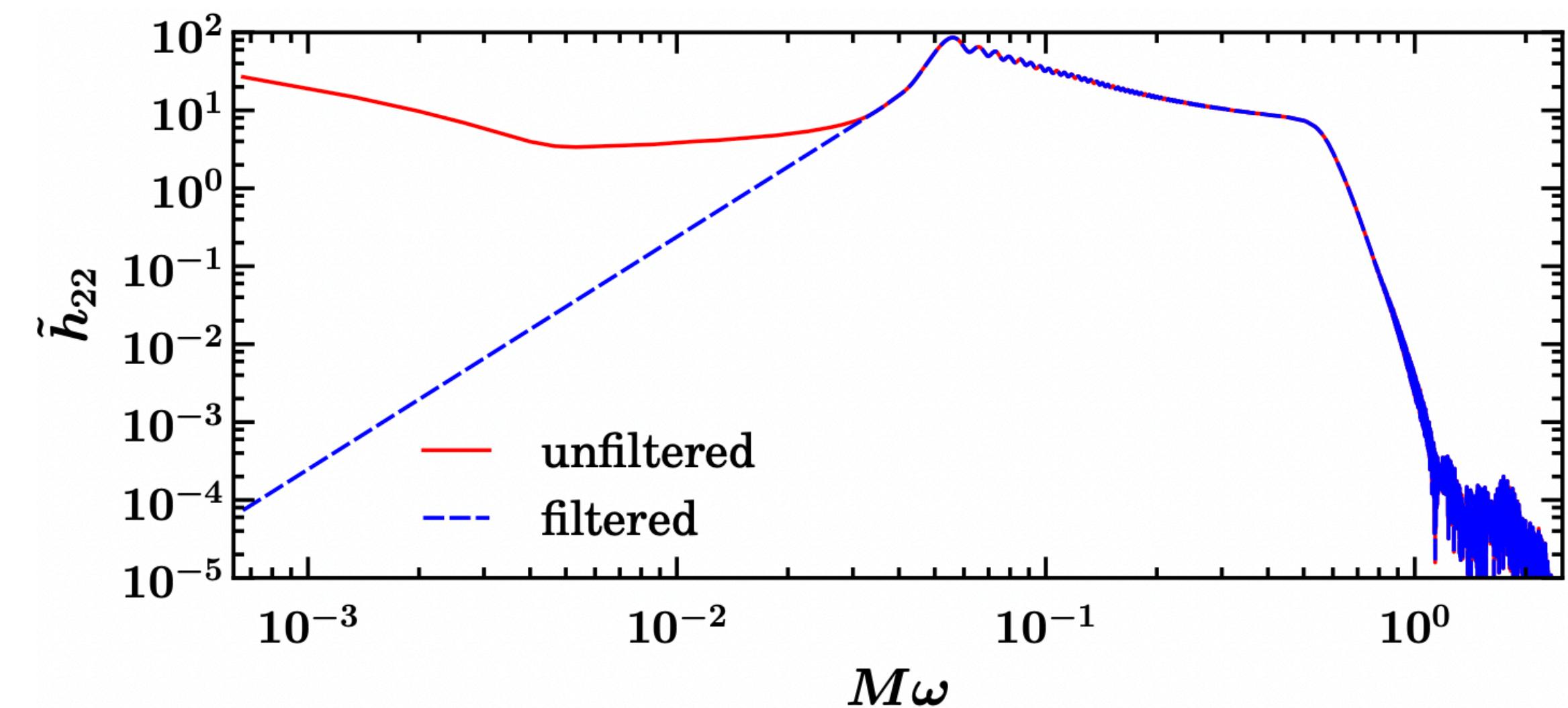


Reisswig + Pollney (2011) [1006.1632]

Caveats

Frequency-domain integration

$$h = h_+ - ih_\times = \mathcal{F}^{-1} \left[-\frac{1}{\omega^2} \tilde{\psi}_4(\omega) \right]$$



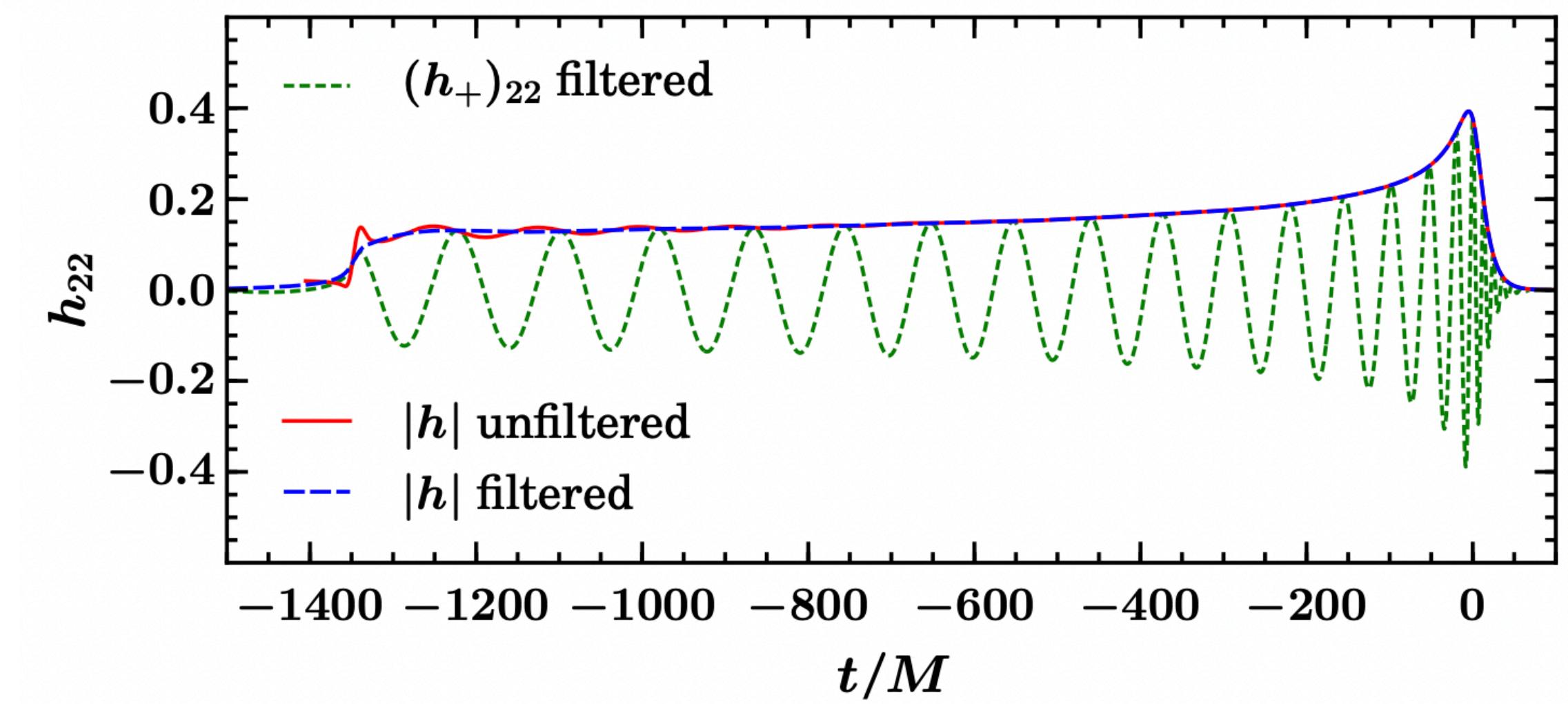
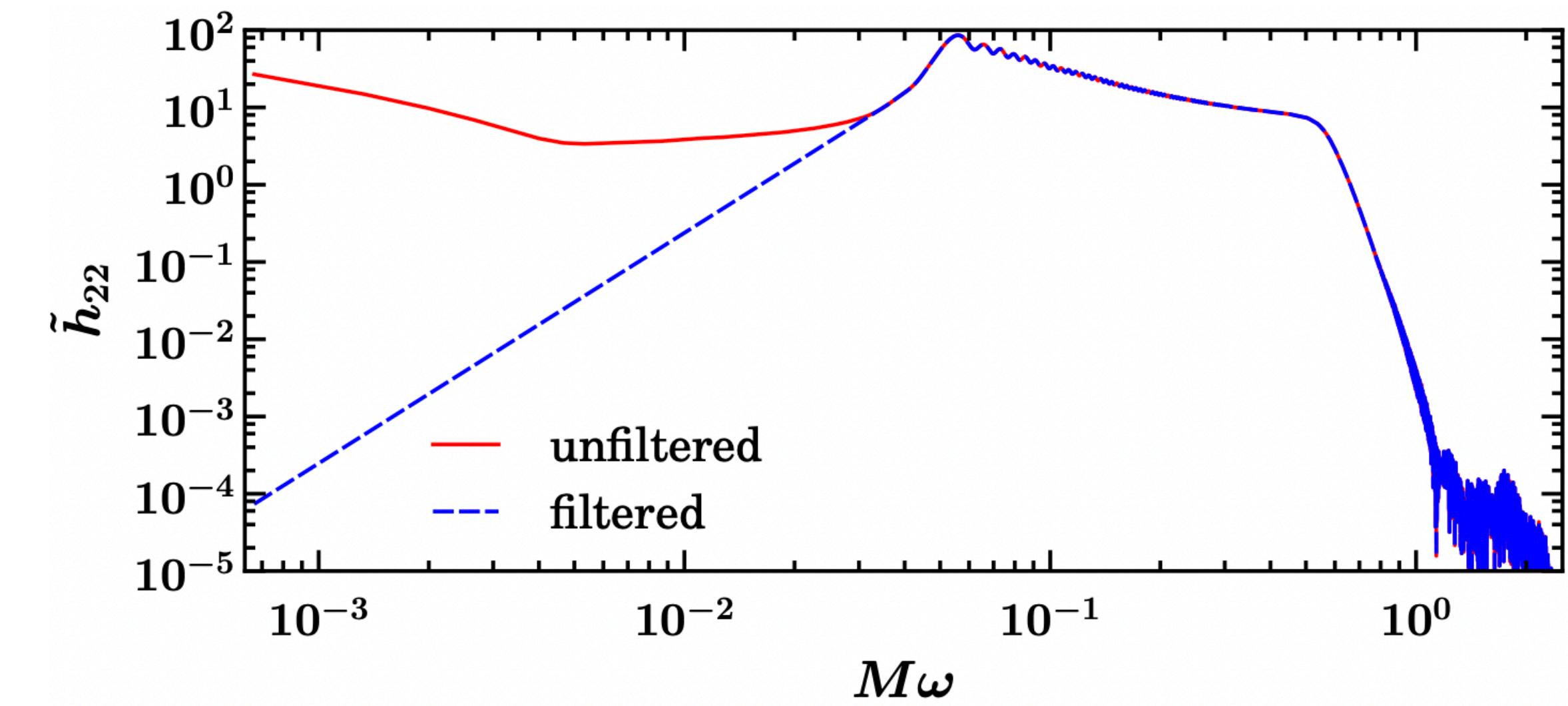
Caveats

Frequency-domain integration

Spectral leakage

Aliasing

$$h = h_+ - ih_\times = \mathcal{F}^{-1} \left[-\frac{1}{\omega^2} \tilde{\psi}_4(\omega) \right]$$



Caveats

Frequency-domain integration

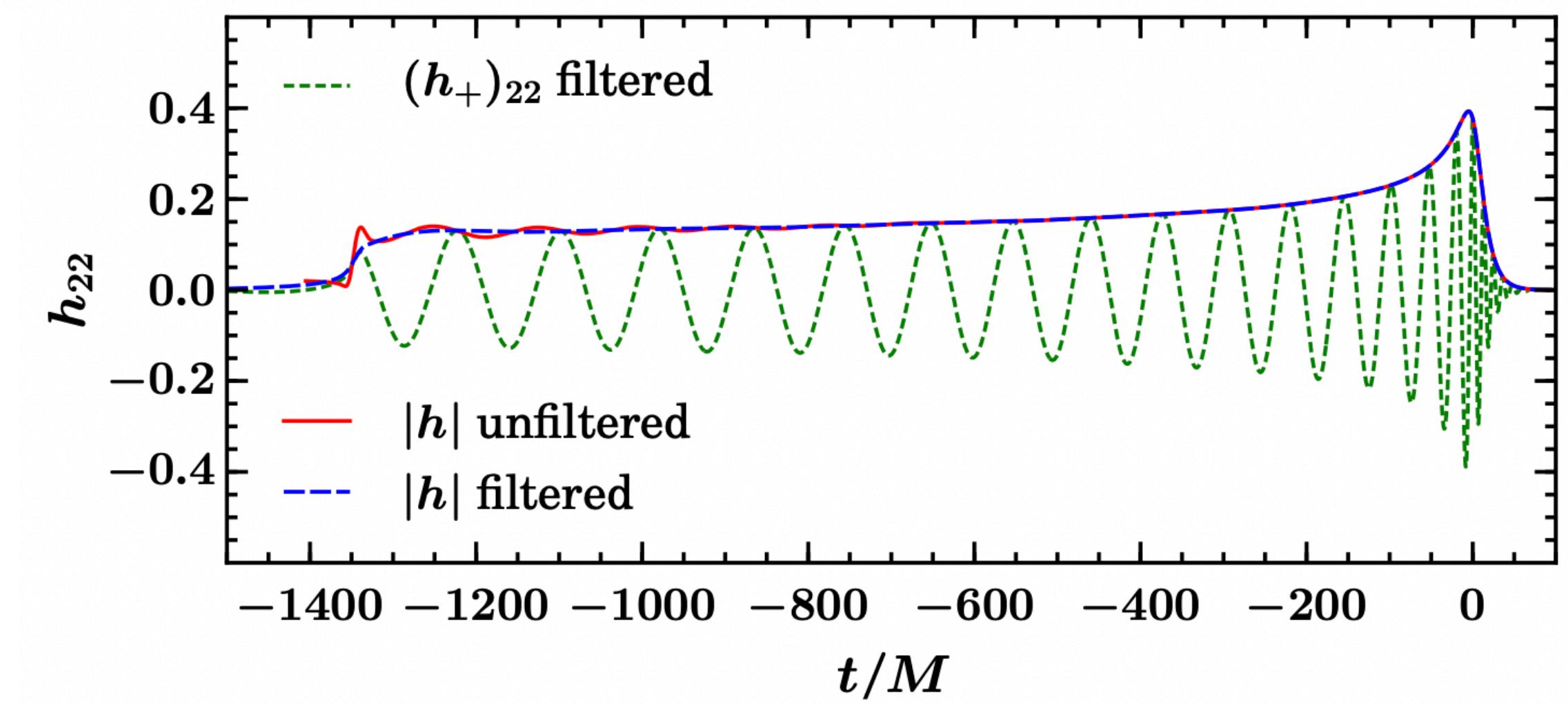
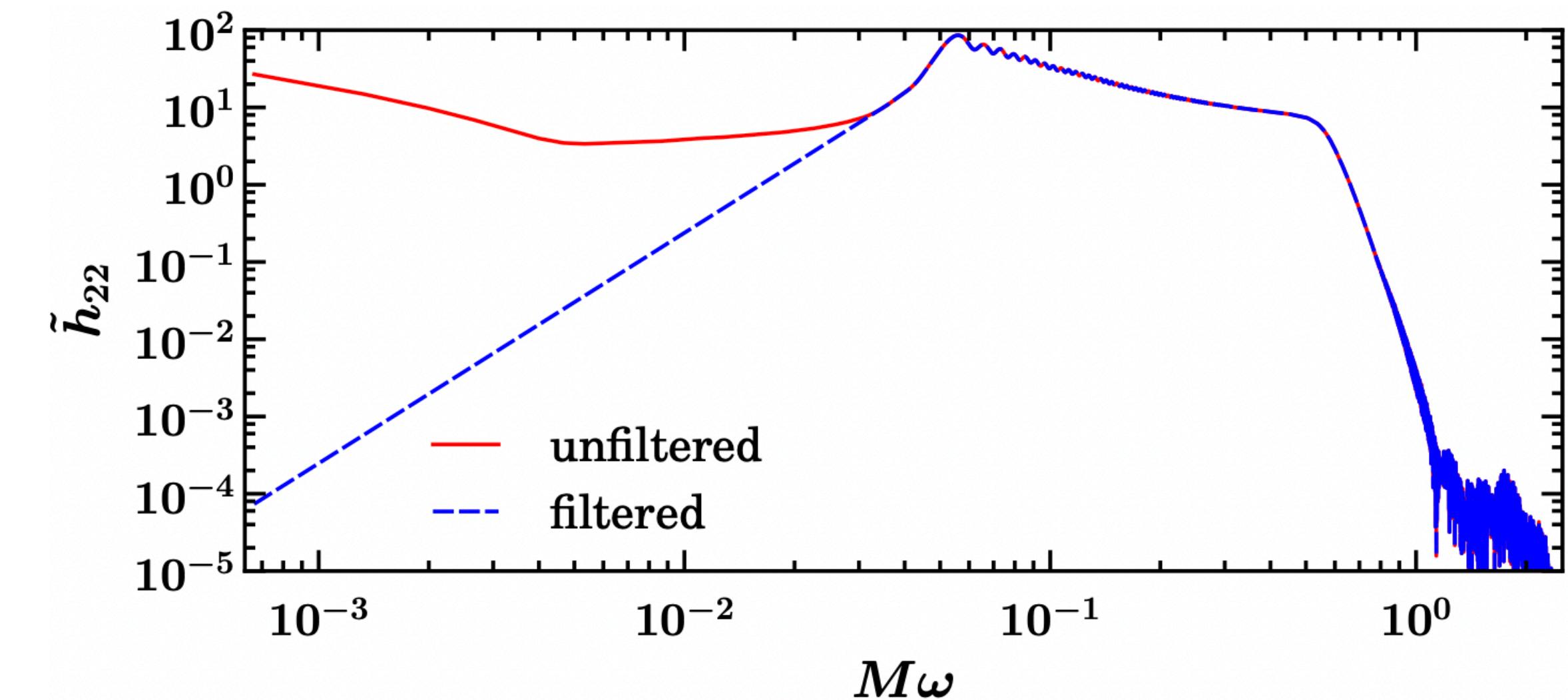
Spectral leakage

Aliasing

High-pass filters

Fixed frequency integration

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Caveats

Frequency-domain integration

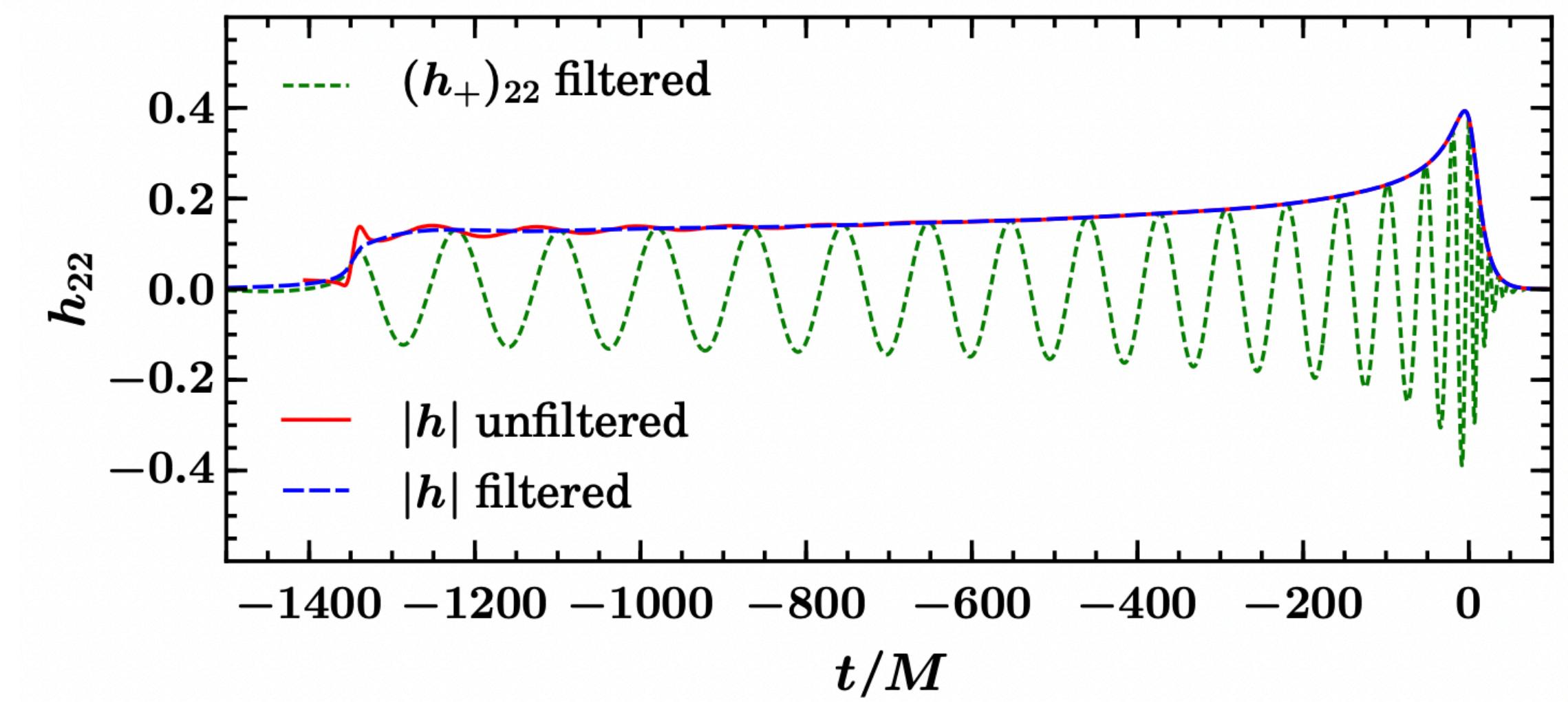
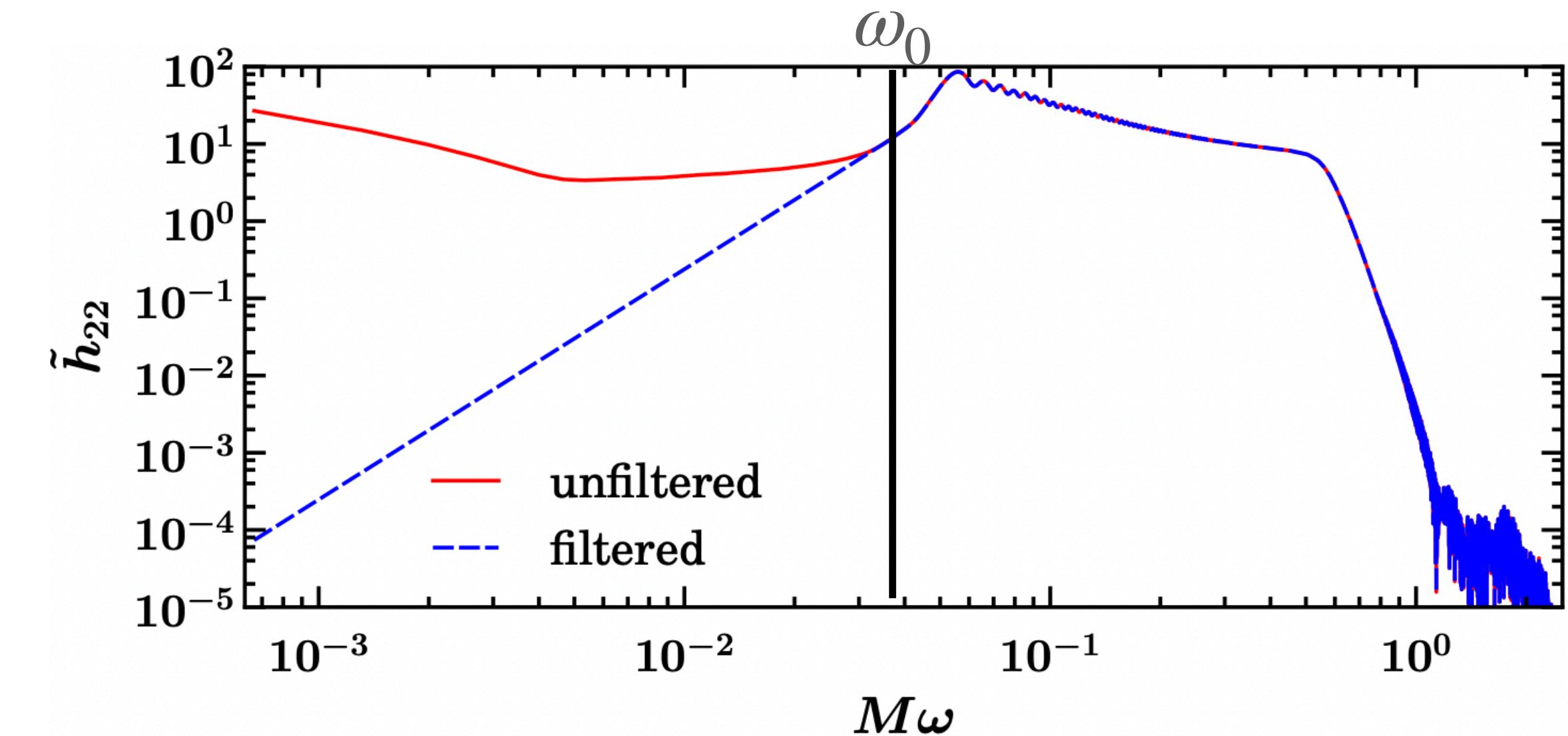
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Caveats

Frequency-domain integration

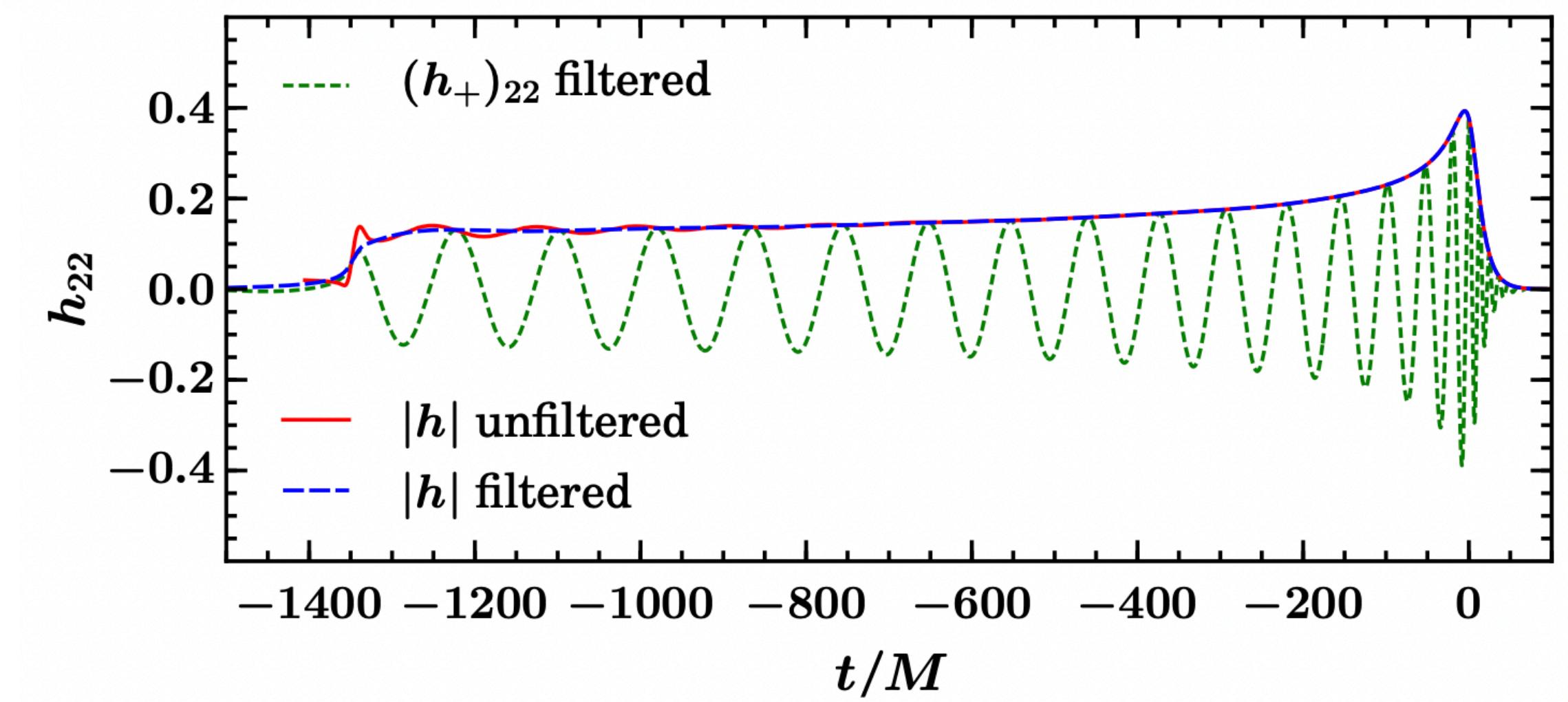
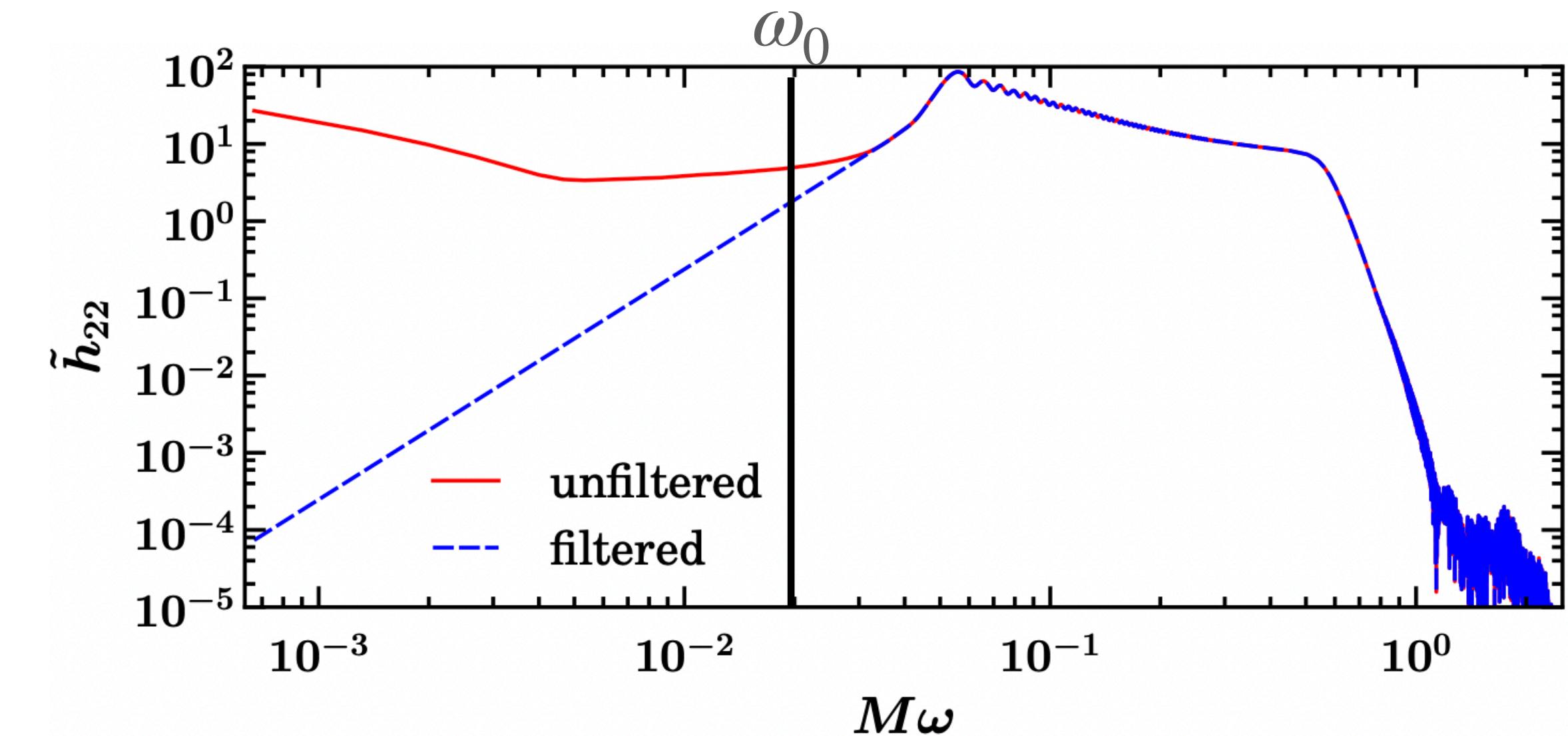
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Caveats

Frequency-domain integration

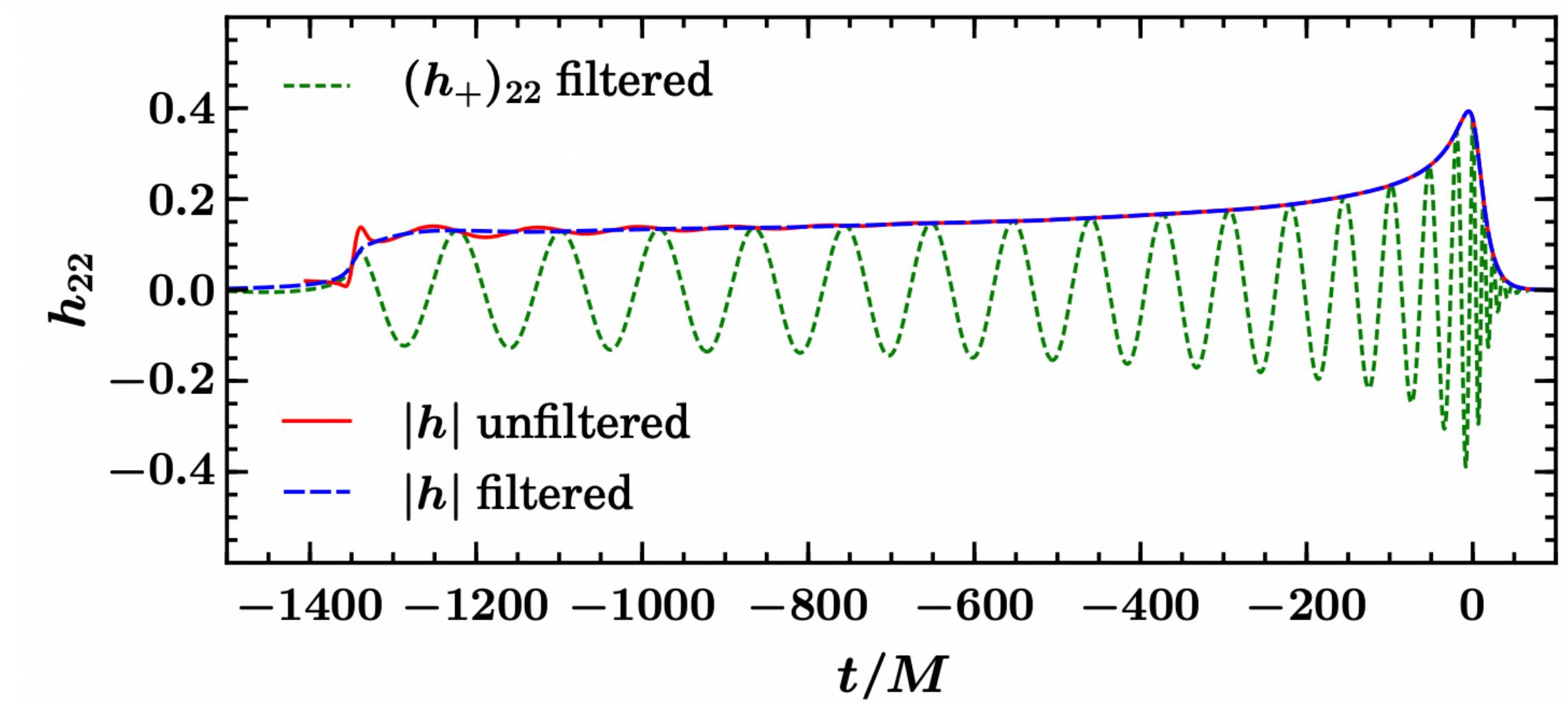
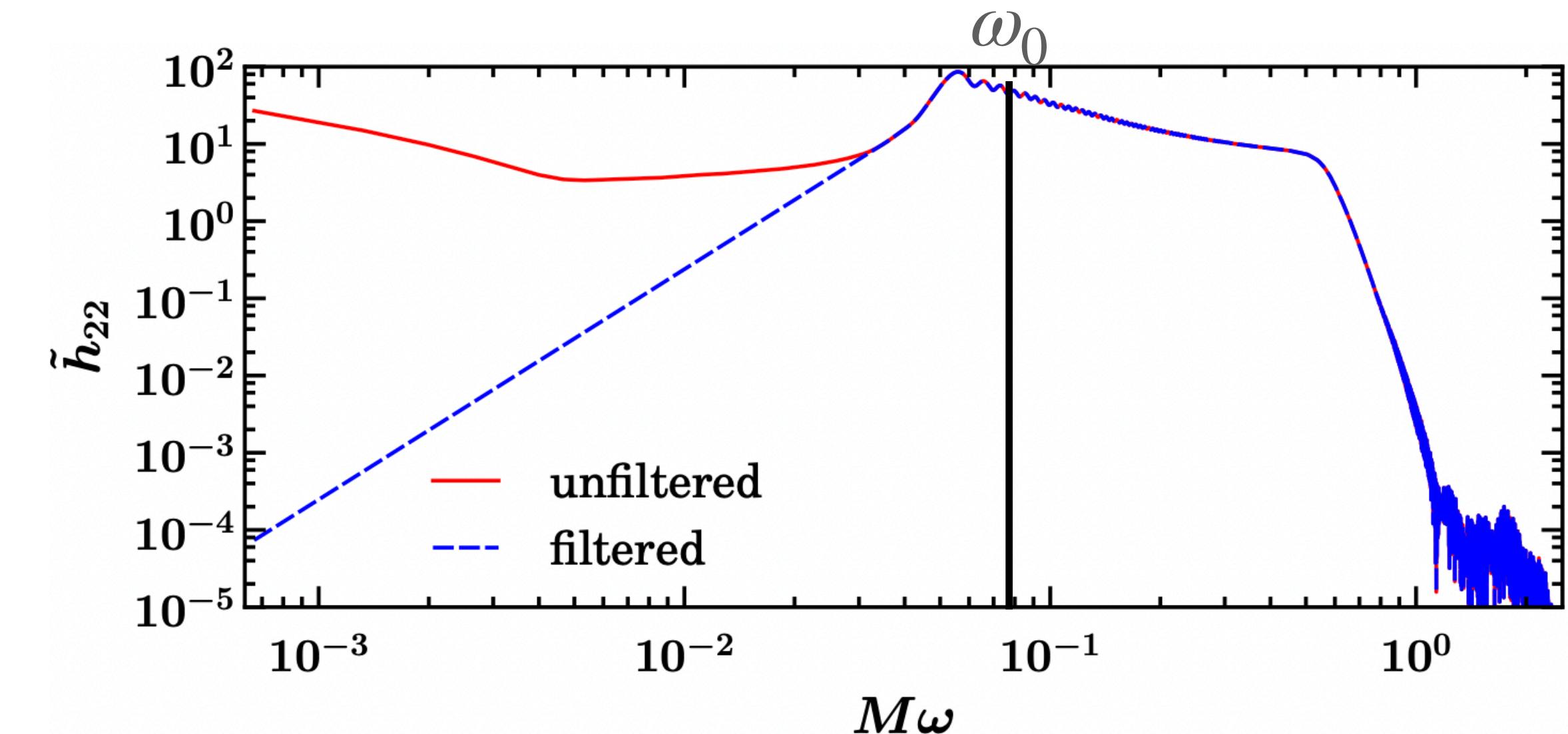
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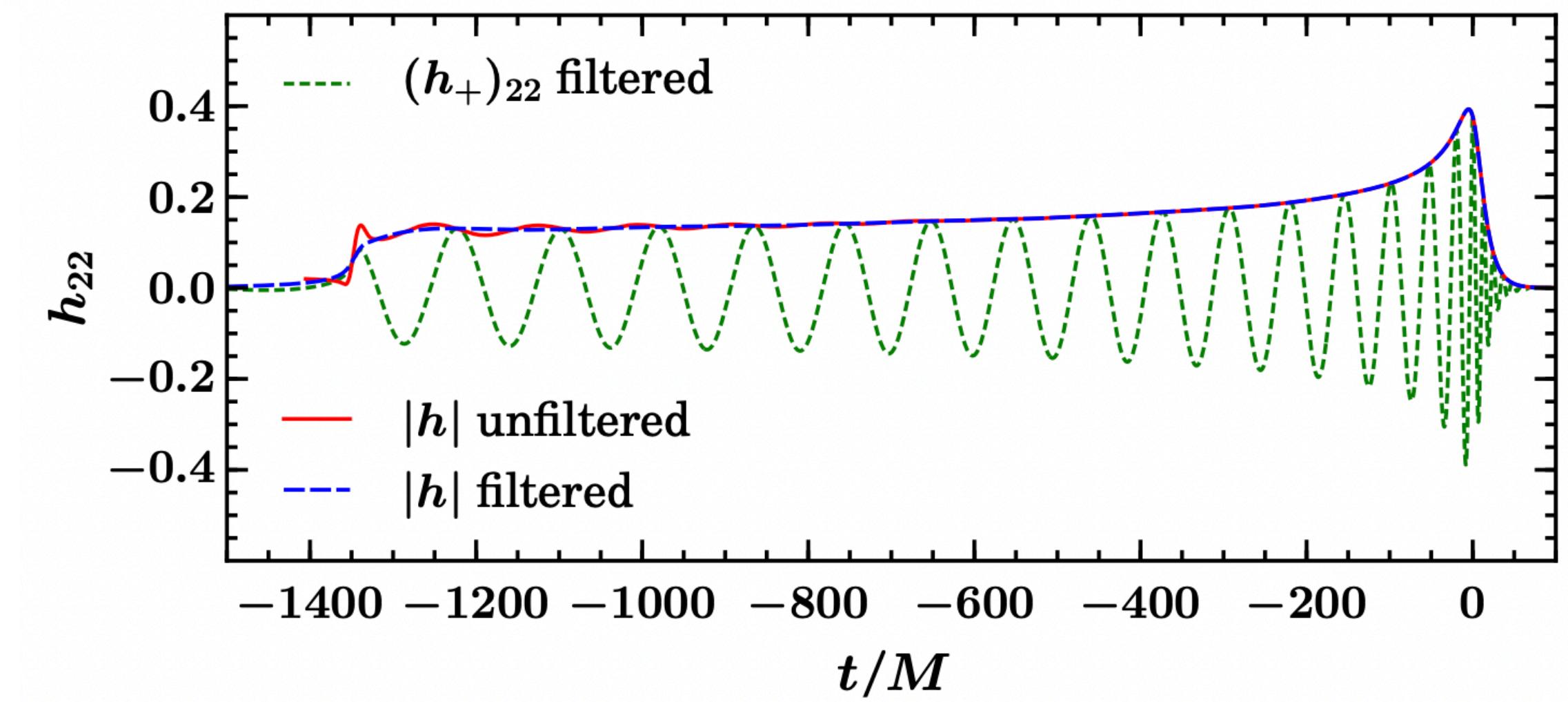
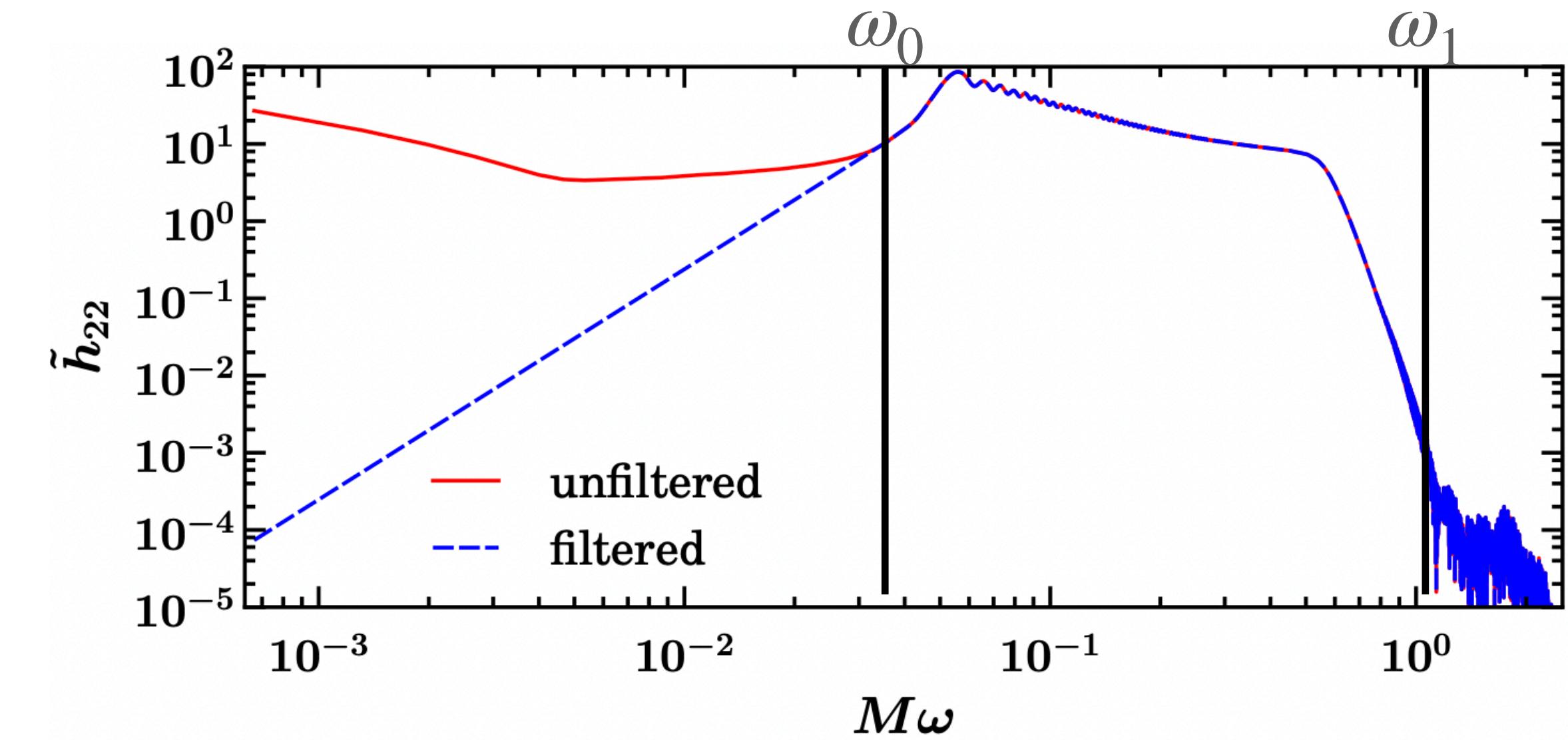


Caveats

Frequency-domain integration

Initial orbital frequency

Ringdown frequency



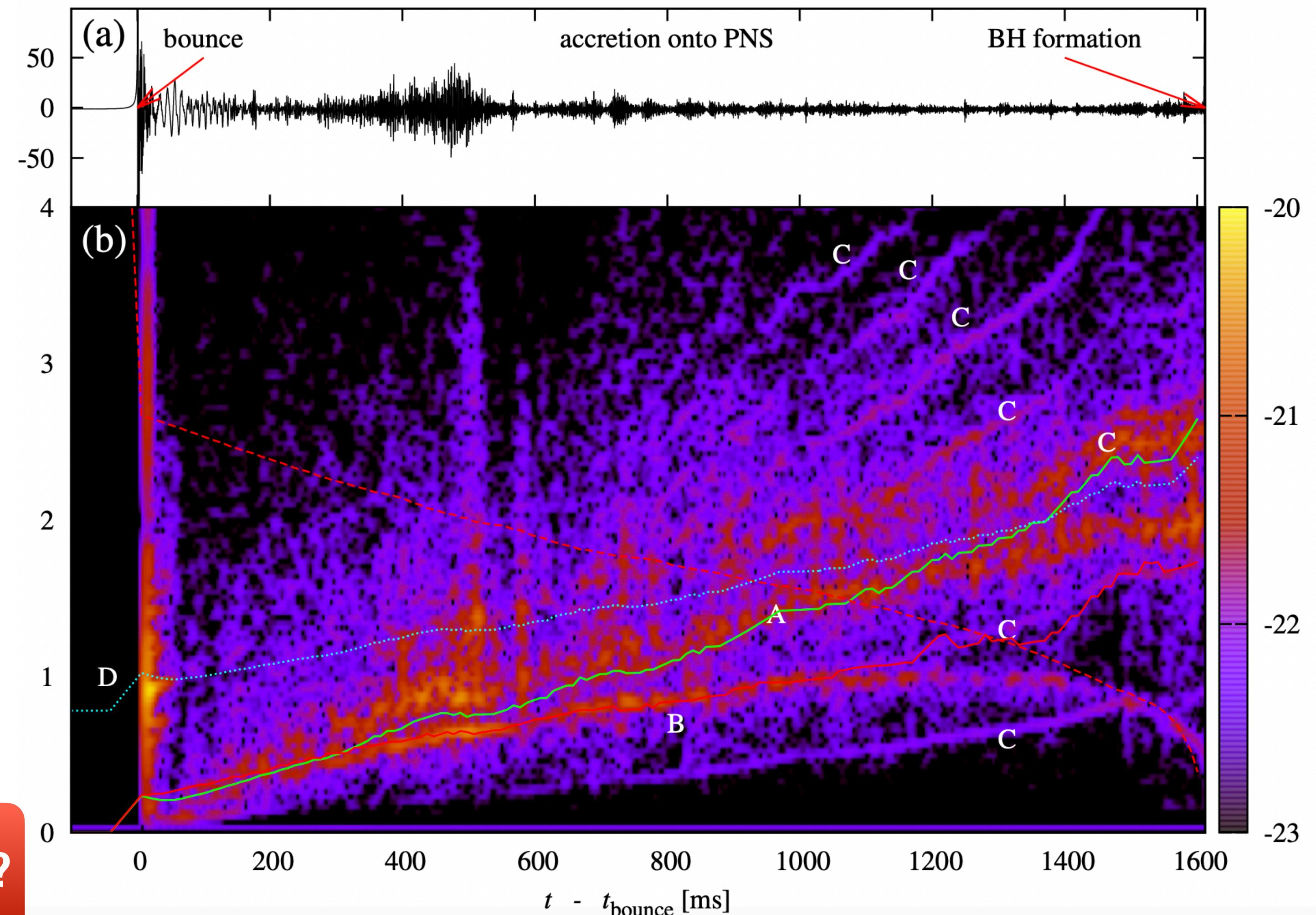
Caveats

Frequency-domain integration

Eccentric systems?

Core-collapse supernova?

What if there is no natural way to choose ω_0 ?



Pablo et al. (2013) [1310.8290]

Parameter inference with ψ_4

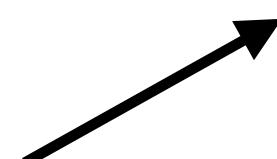
Not to do the integration!

Parameter inference with ψ_4

Not to do the integration!

Strain

$$d(t) = h(t) + n(t)$$



Strain data

Parameter inference with ψ_4

Not to do the integration!

The diagram illustrates the decomposition of strain data. A blue rounded rectangle labeled "Strain" is positioned above the equation $d(t) = h(t) + n(t)$. An arrow points from the word "Strain" to the term $h(t)$, indicating that $h(t)$ represents the "Strain waveform". Another arrow points from the word "Strain data" to the term $n(t)$, indicating that $n(t)$ represents "noise".

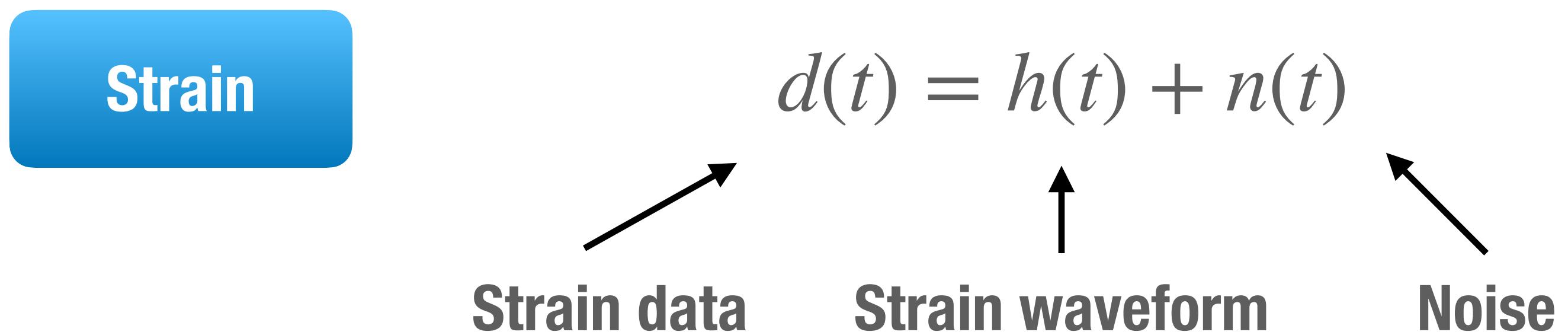
$$d(t) = h(t) + n(t)$$

Strain

Strain data Strain waveform

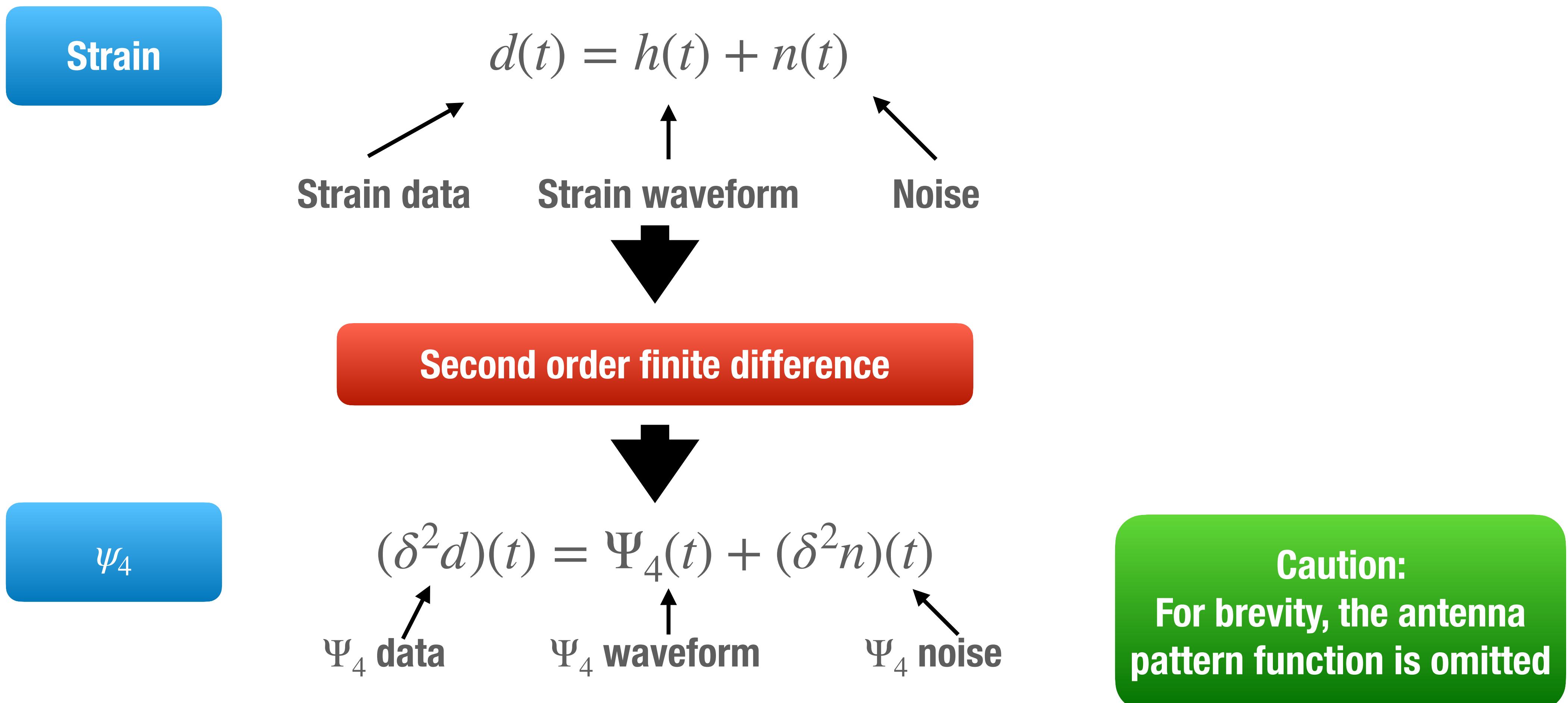
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Parameter inference with ψ_4

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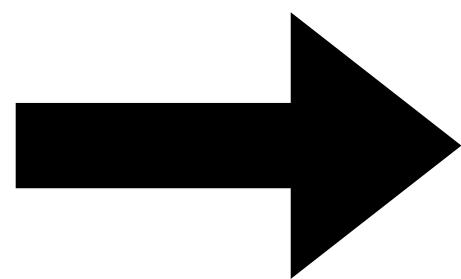


Parameter inference with ψ_4



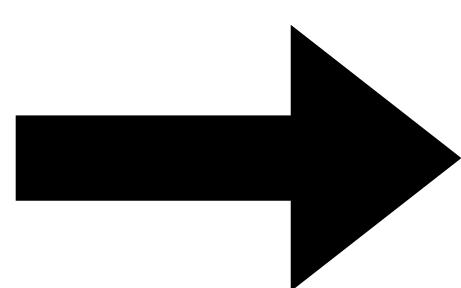
Parameter inference with ψ_4

Strain data d



$$d_{\Psi_4}[m] = \frac{d[m+1] - 2d[m] + d[m-1]}{(\Delta t)^2}$$

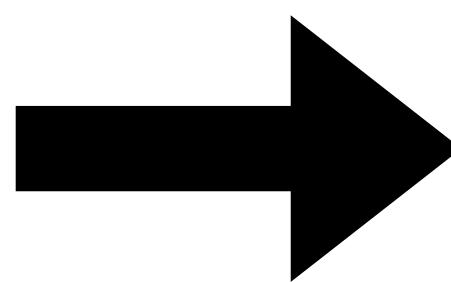
Noise PSD $S_n[k]$



$$S_{n_{\Psi_4}}[k] = \frac{1}{(\Delta t)^4} \left(6 - 8 \cos \frac{2\pi k}{M} + 2 \cos \frac{4\pi k}{M} \right) S_n[k]$$

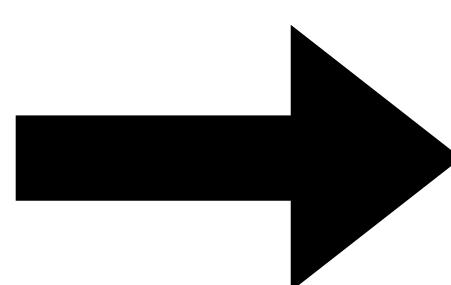
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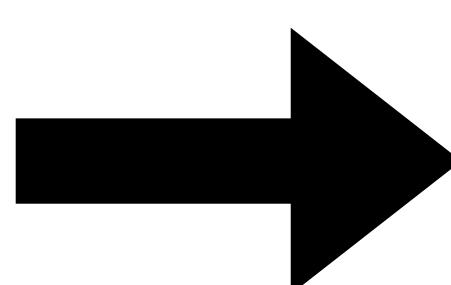
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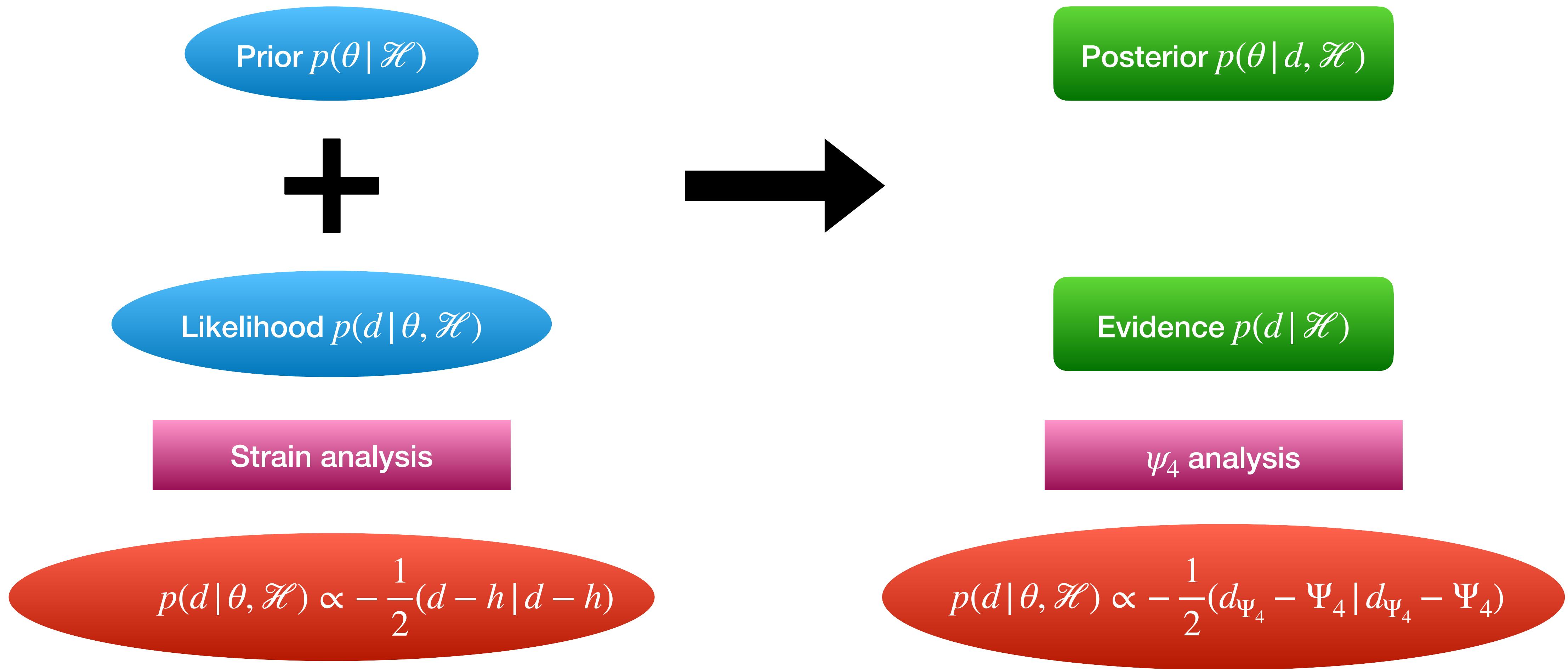
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Strain template h

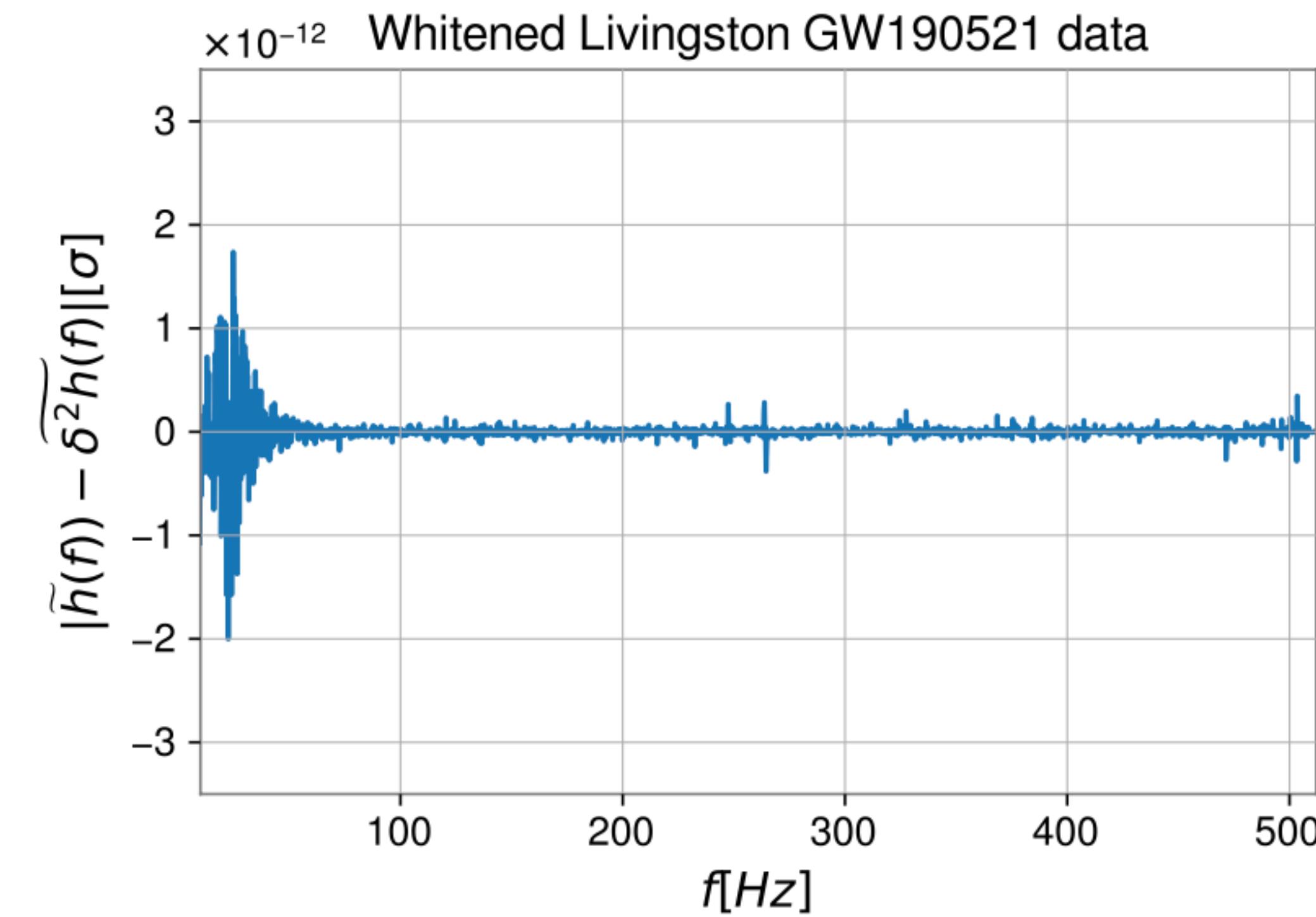
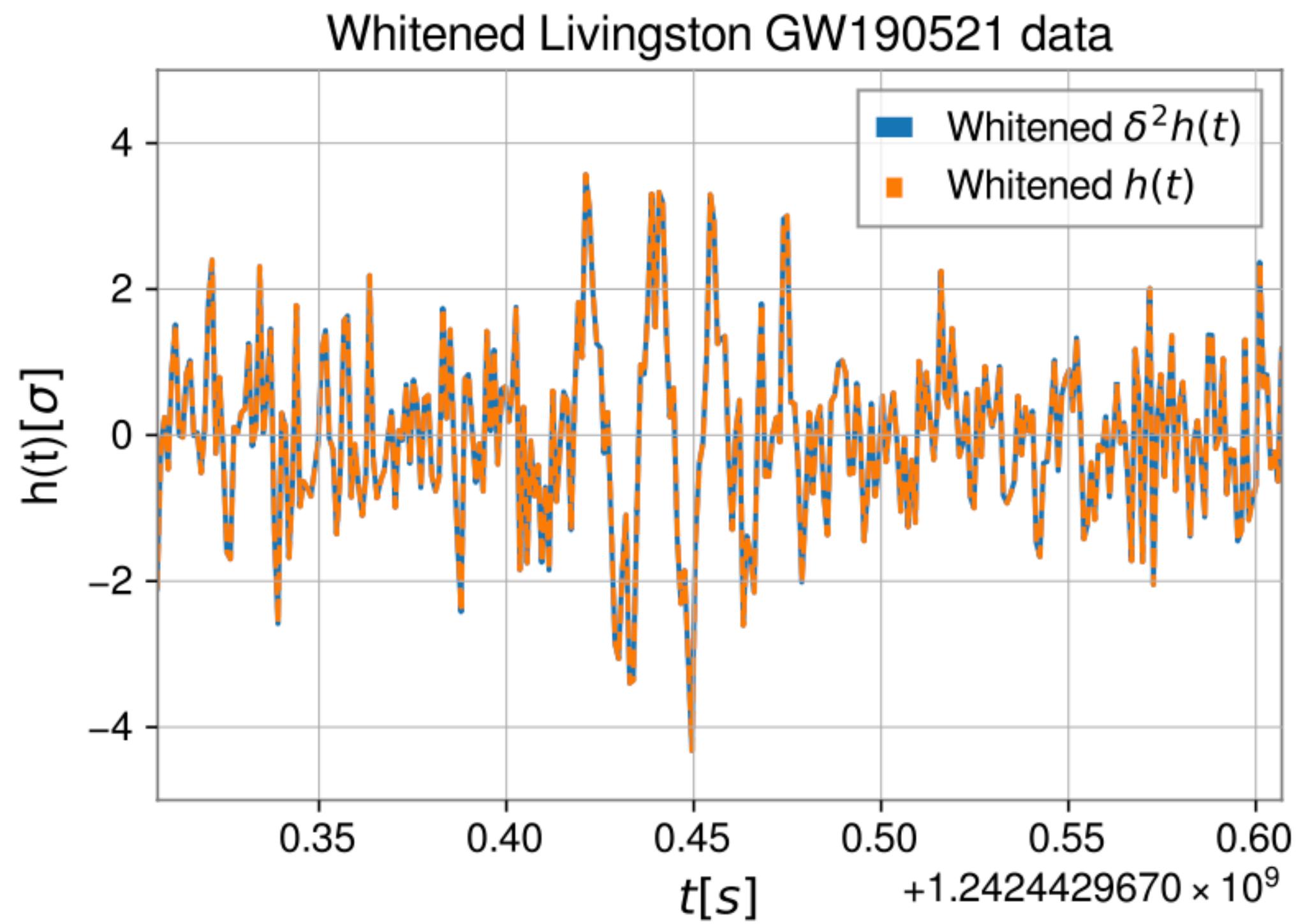


$$\tilde{\Psi}_4 = \frac{1 - \cos(2\pi k \Delta f \Delta t)}{2\pi^2(k \Delta f \Delta t)^2} \tilde{\psi}_4[k]$$

Parameter inference with ψ_4

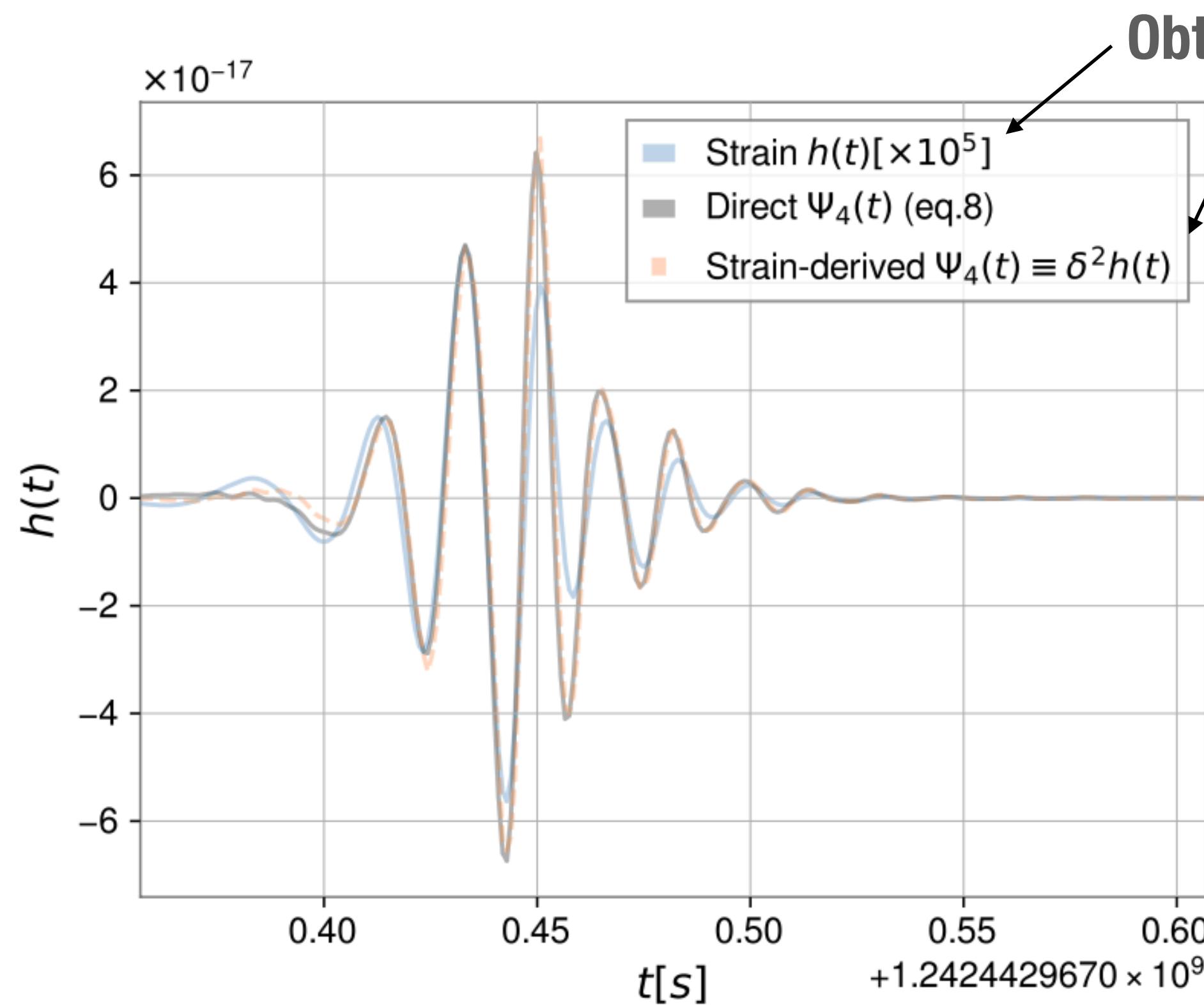


Testing the formalism with the whitened data

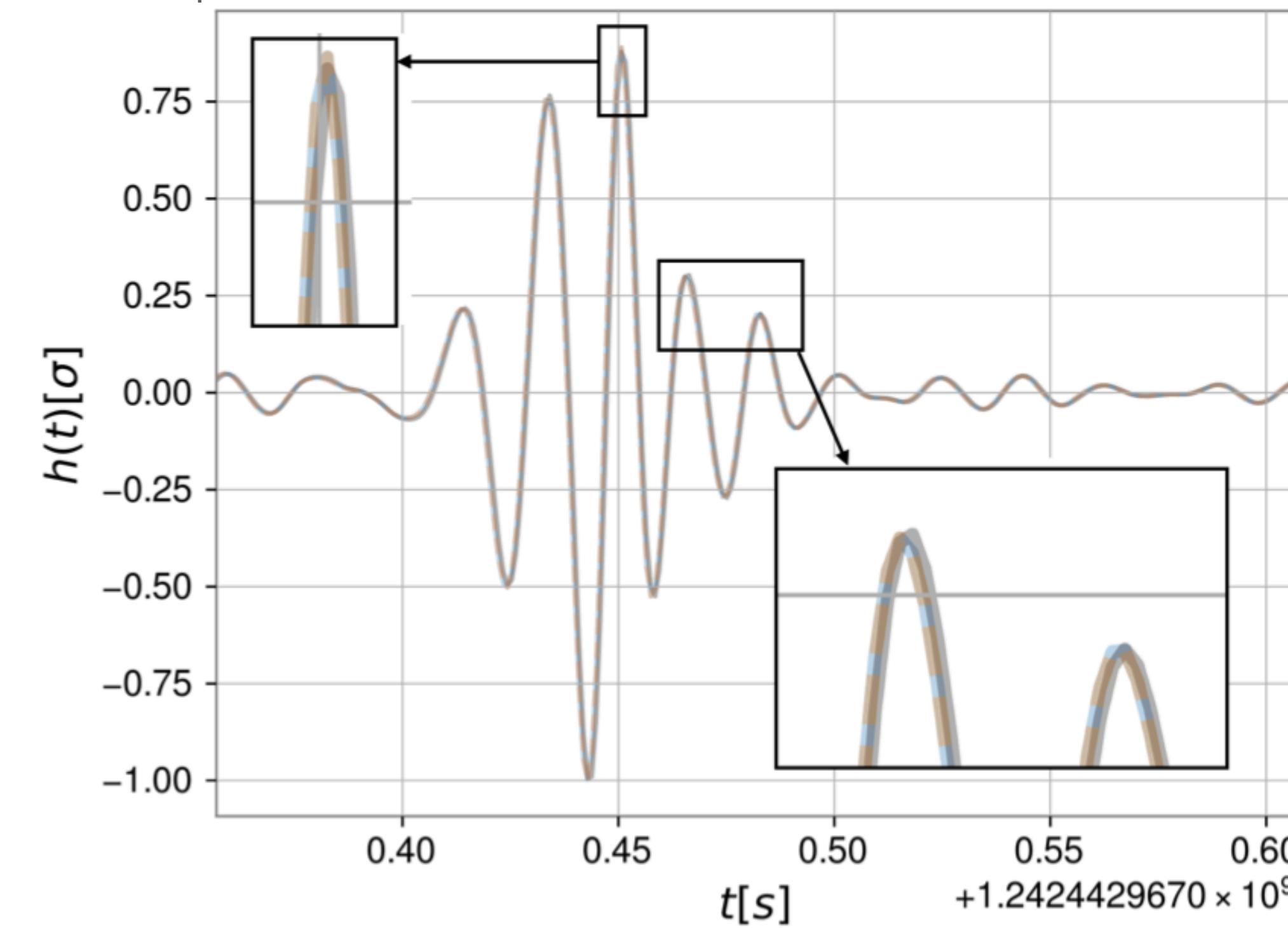


Testing the formalism with the whitened data

Appropriate ω_0



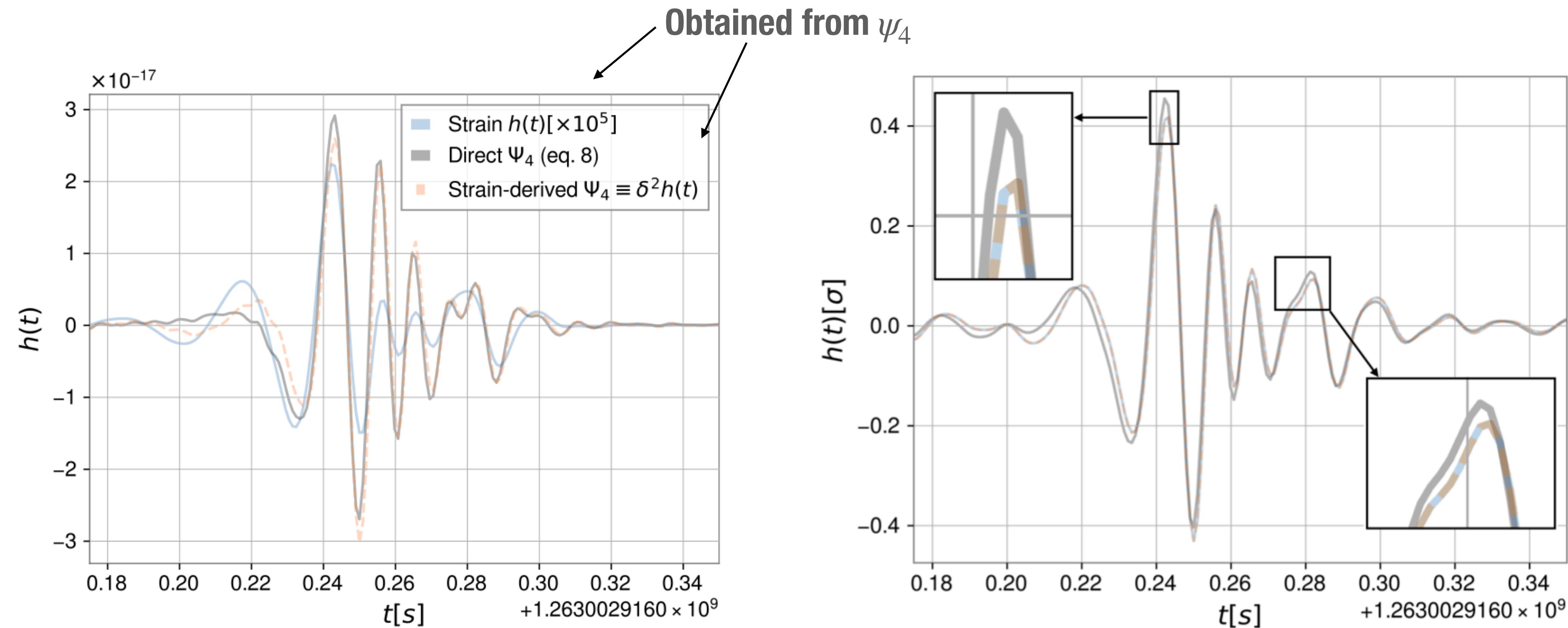
Obtained from ψ_4



Head-on Proca-star merger consistent with GW190521

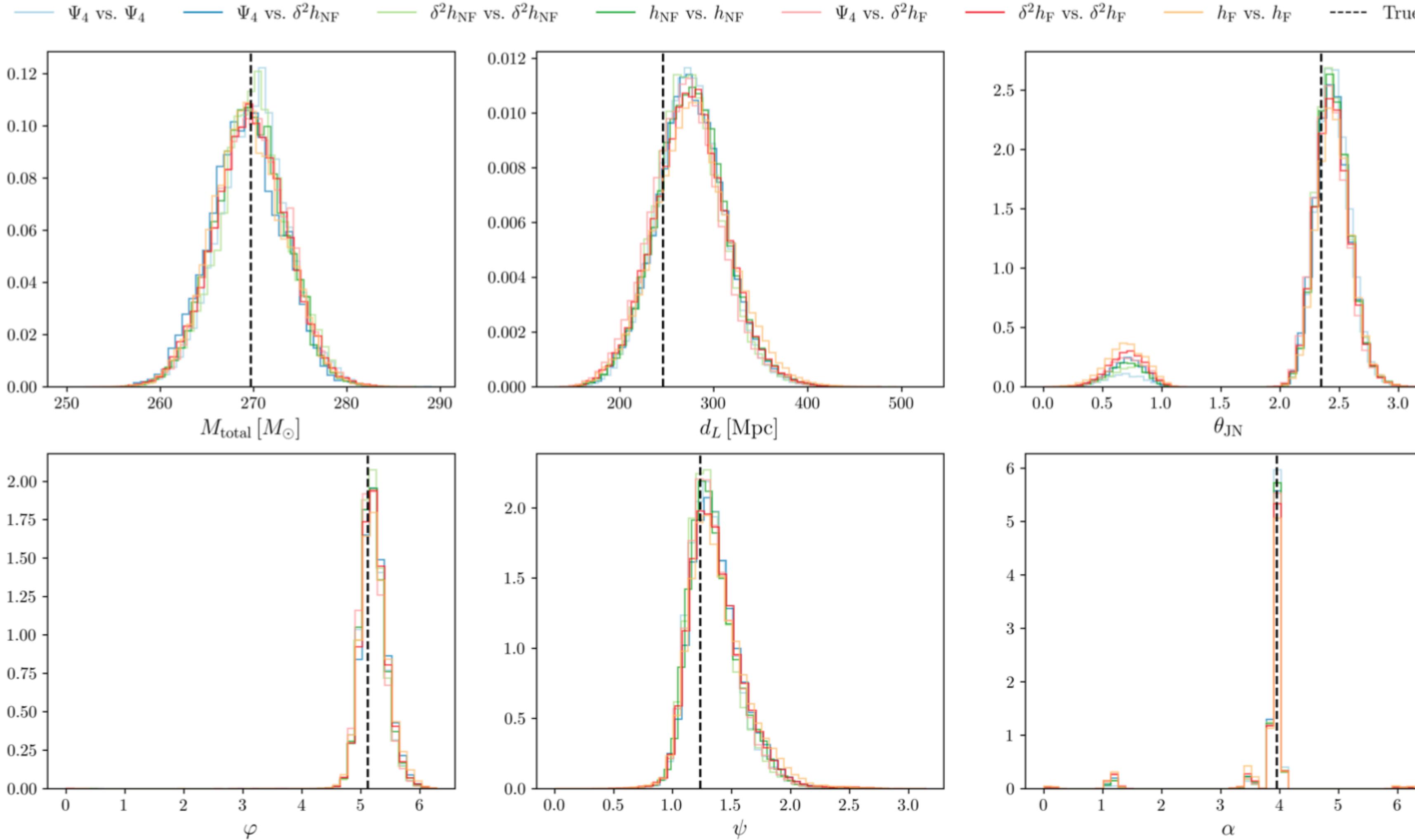
Testing the formalism with the whitened data

Too aggressive ω_0



Head-on Proca-star merger consistent with S200114f

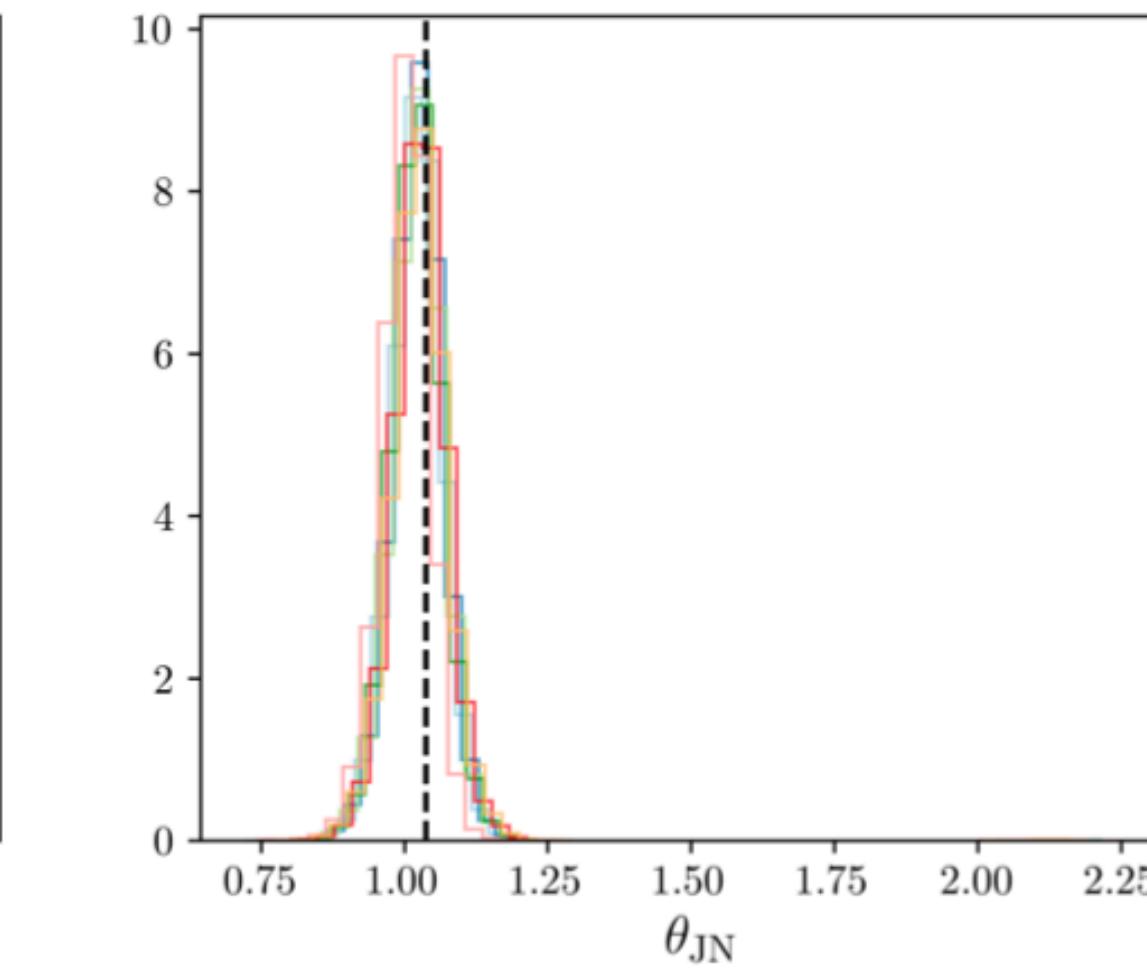
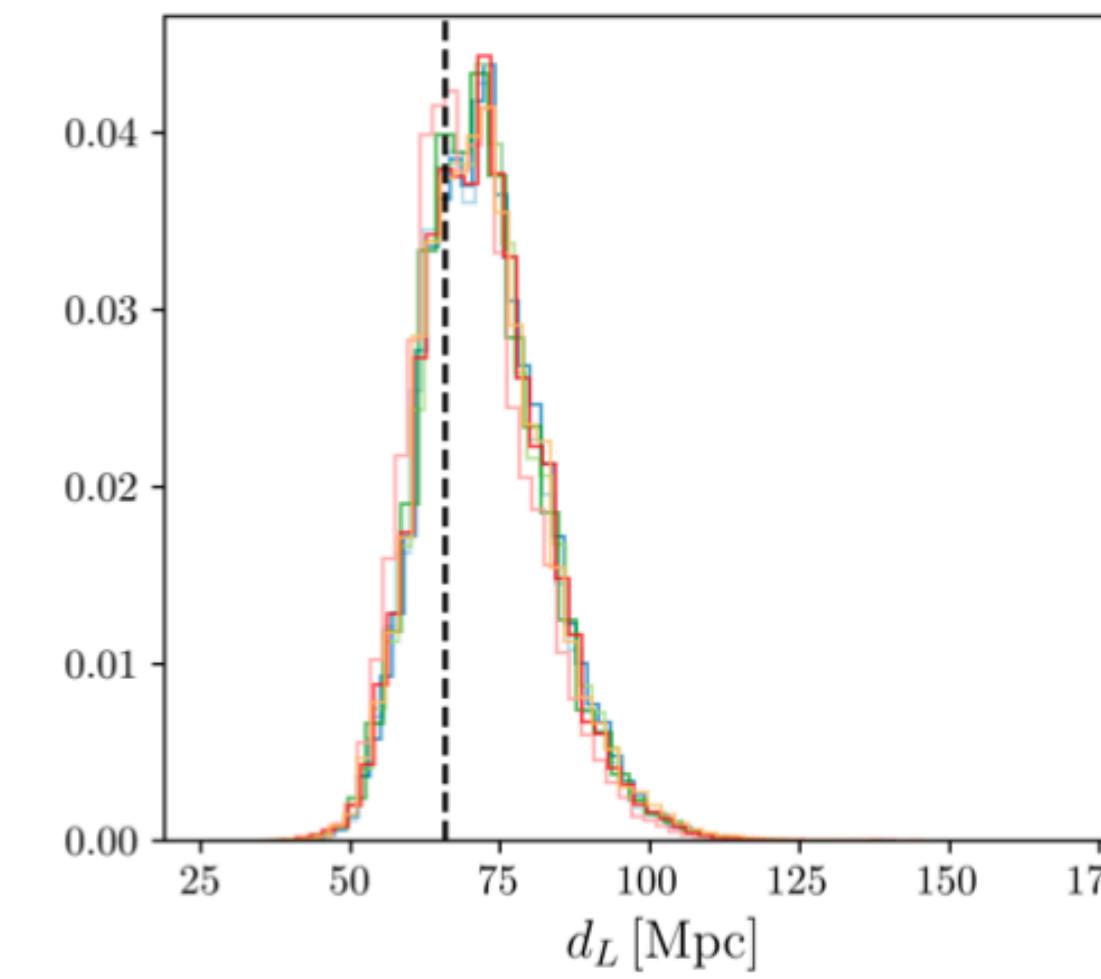
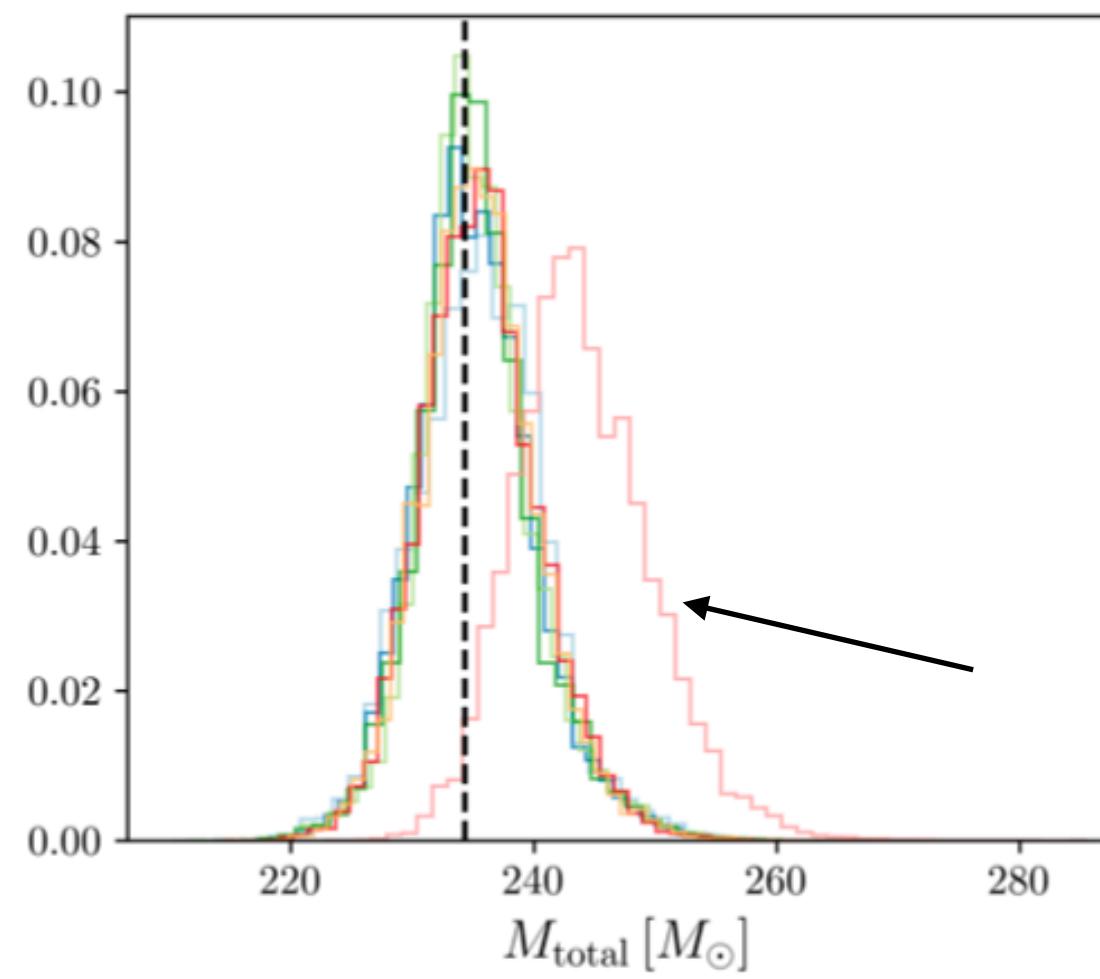
Testing the formalism with parameter estimation



Head-on Proca-star merger consistent with GW190521

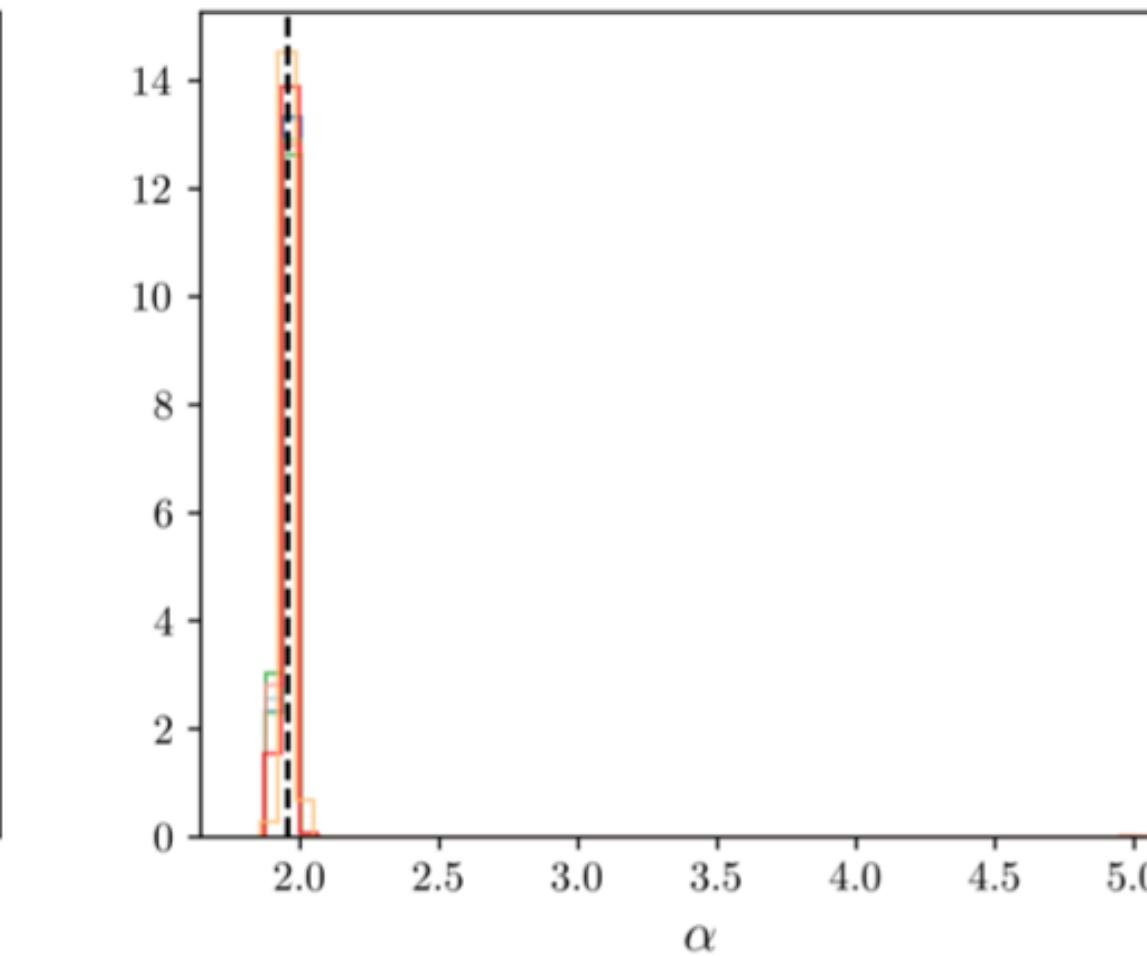
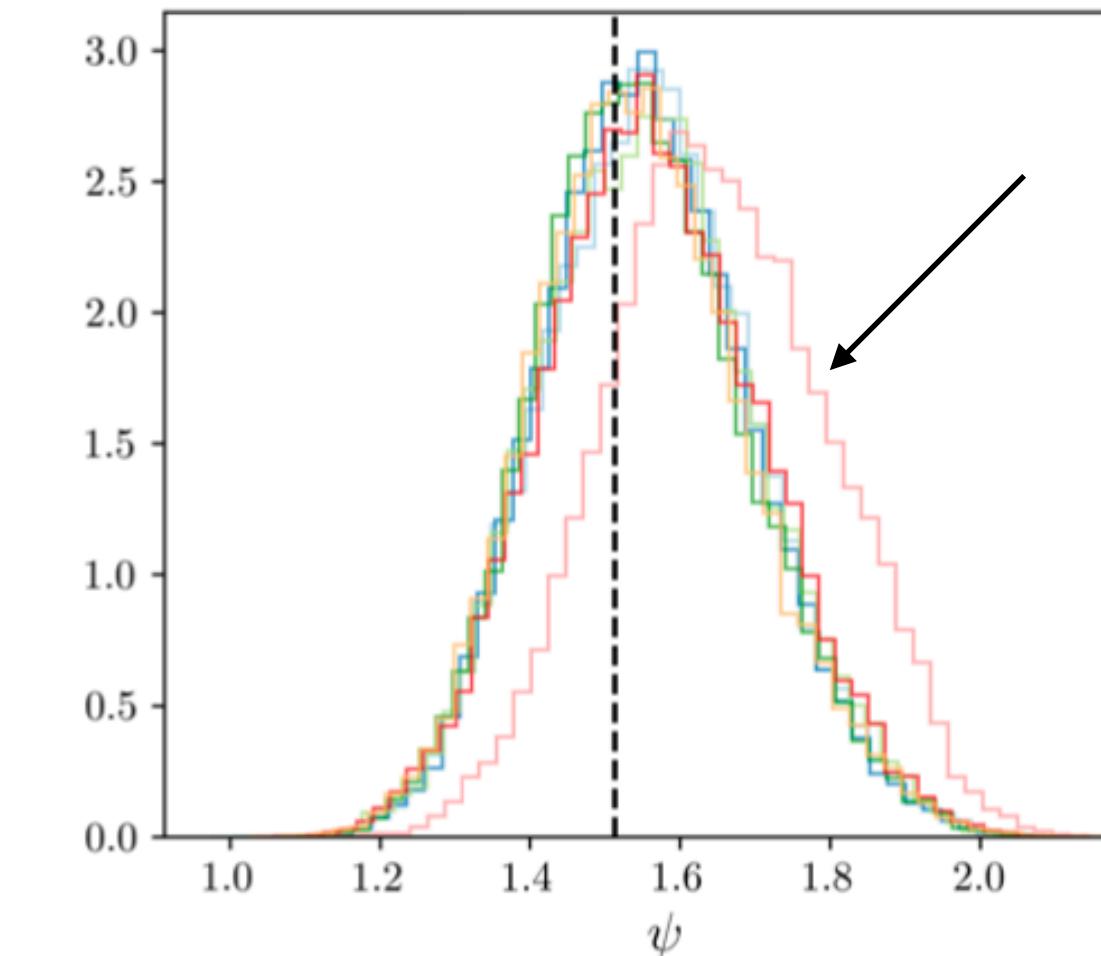
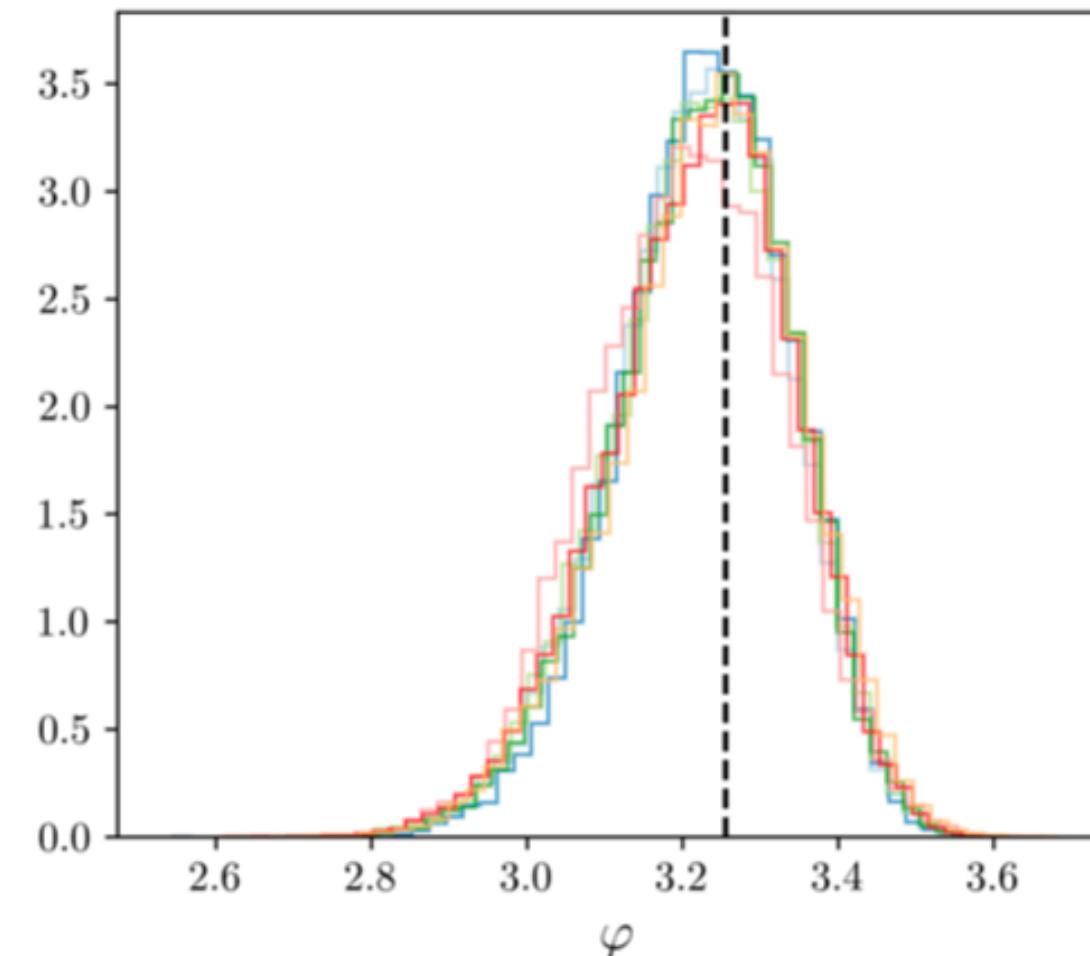
Testing the formalism with parameter estimation

— Ψ_4 vs. Ψ_4 — Ψ_4 vs. $\delta^2 h_{\text{NF}}$ — $\delta^2 h_{\text{NF}}$ vs. $\delta^2 h_{\text{NF}}$ — h_{NF} vs. h_{NF} — Ψ_4 vs. $\delta^2 h_F$ — $\delta^2 h_F$ vs. $\delta^2 h_F$ — h_F vs. h_F ----- True



Inject ψ_4

Recover with $\delta^2 h_F$



Head-on Proca-star merger consistent with S200114f

Conclusion

- We propose a statistical framework to perform data analysis directly with ψ_4
- Time-integration of ψ_4 suffers from several issues, such as
 - amplifying the numerical noise that leads to a non-linear drift
 - the choice of frequency cutoff in the filter might not be trivial
- We show that the systematic induced by the integration can have huge impacts on data analysis
- Direct parameter inference with ψ_4 avoids the artefacts from performing numerical integration

Backup slides

Impact on model selection

Waveform model		GW190521		S200114f	
Injection	Template	$\log \mathcal{B}$	$\log \mathcal{L}_{\max}$	$\log \mathcal{B}$	$\log \mathcal{L}_{\max}$
Ψ_4	Ψ_4	94.1	123.2	90.0	124.2
Ψ_4	$\delta^2 h_{\text{NF}}$	93.9	123.2	89.9	124.0
$\delta^2 h_{\text{NF}}$	$\delta^2 h_{\text{NF}}$	93.8	123.1	89.2	123.9
h_{NF}	h_{NF}	93.6	123.1	89.3	123.8
Ψ_4	$\delta^2 h_F$	93.6	122.9	83.9	117.8
$\delta^2 h_F$	$\delta^2 h_F$	92.4	121.5	64.1	98.2
h_F	h_F	92.2	121.5	64.1	98.3