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# Tests of GR with GWs from compact binary coalescences

12th Iberian Gravitational Waves meeting

6th June 2022

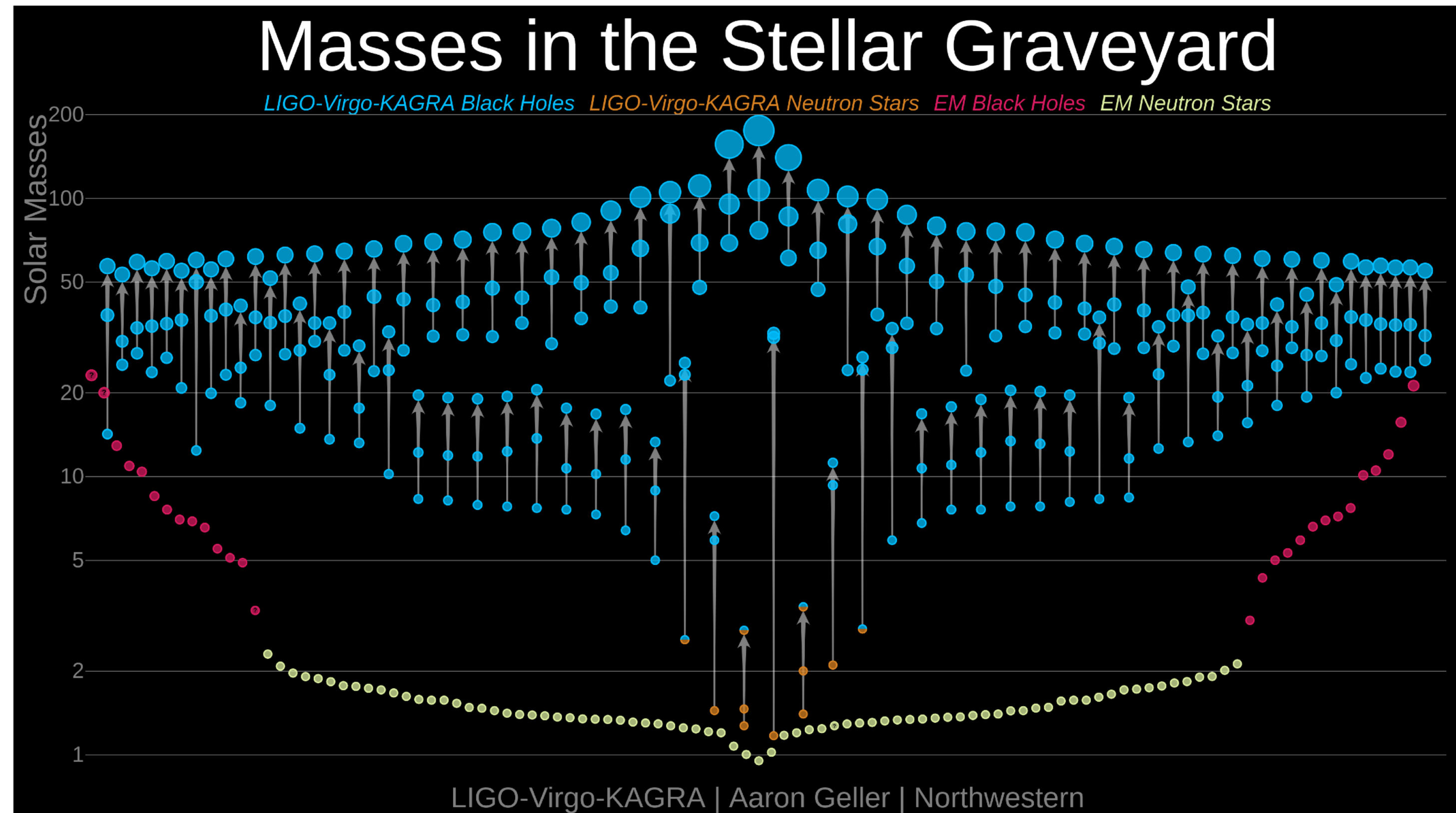
Marta Colleoni, University of the Balearic Islands

# GWTC-3: the family is getting larger

**When:** Incorporate events detected in the second half of the 3rd observing run, from 1 November 2019, 15:00 UTC and 27 March 2020, 17:00 UTC

**Where:** Livingston, Hanford, Virgo (Kagra will join in O4, brief observing run of two weeks in April 2020)

**What:** 35 new compact binaries, 17 of which reported for the first time -> Total number of events for GWTC-3 is **90!**

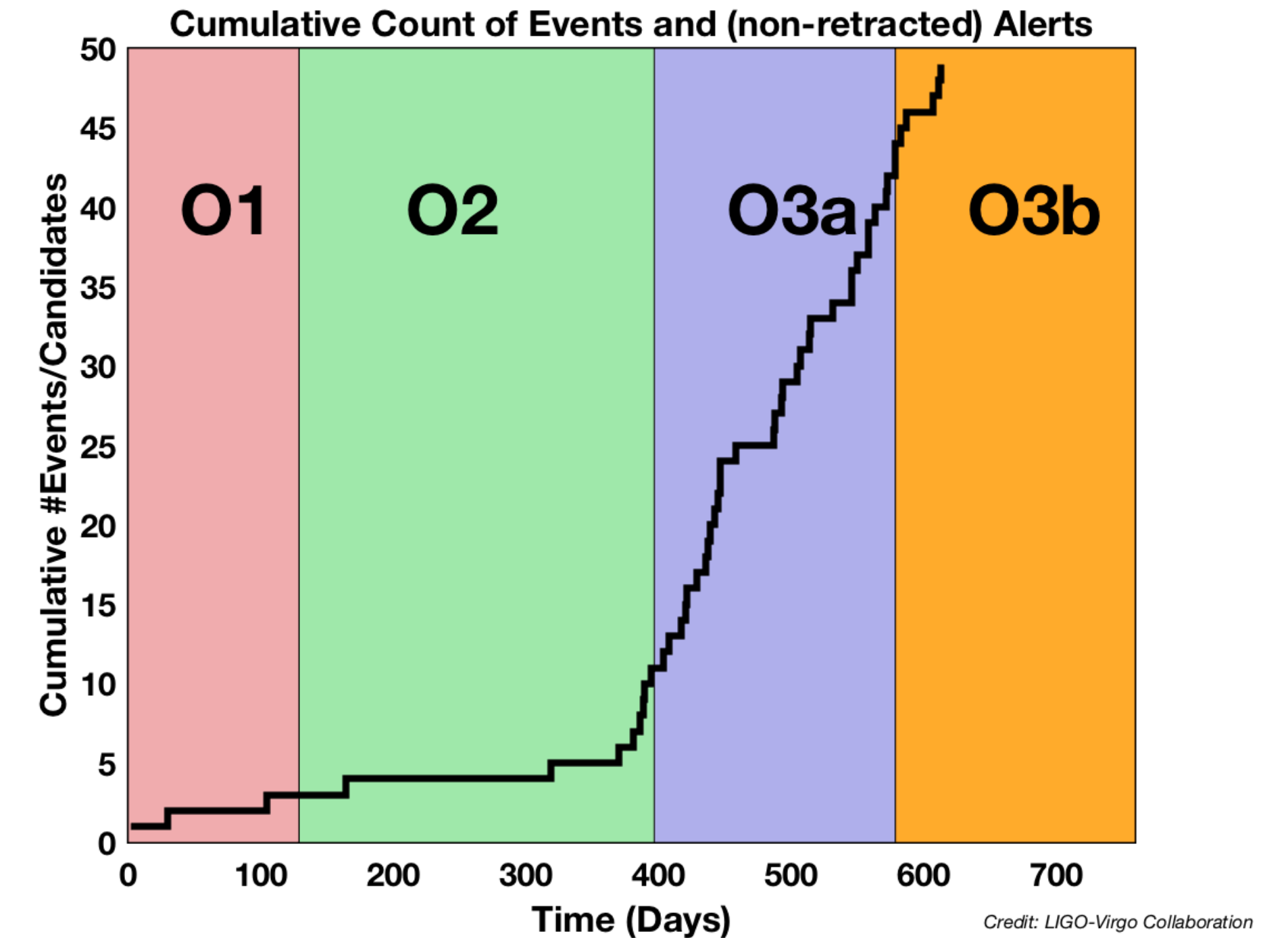


# Better instruments, better data

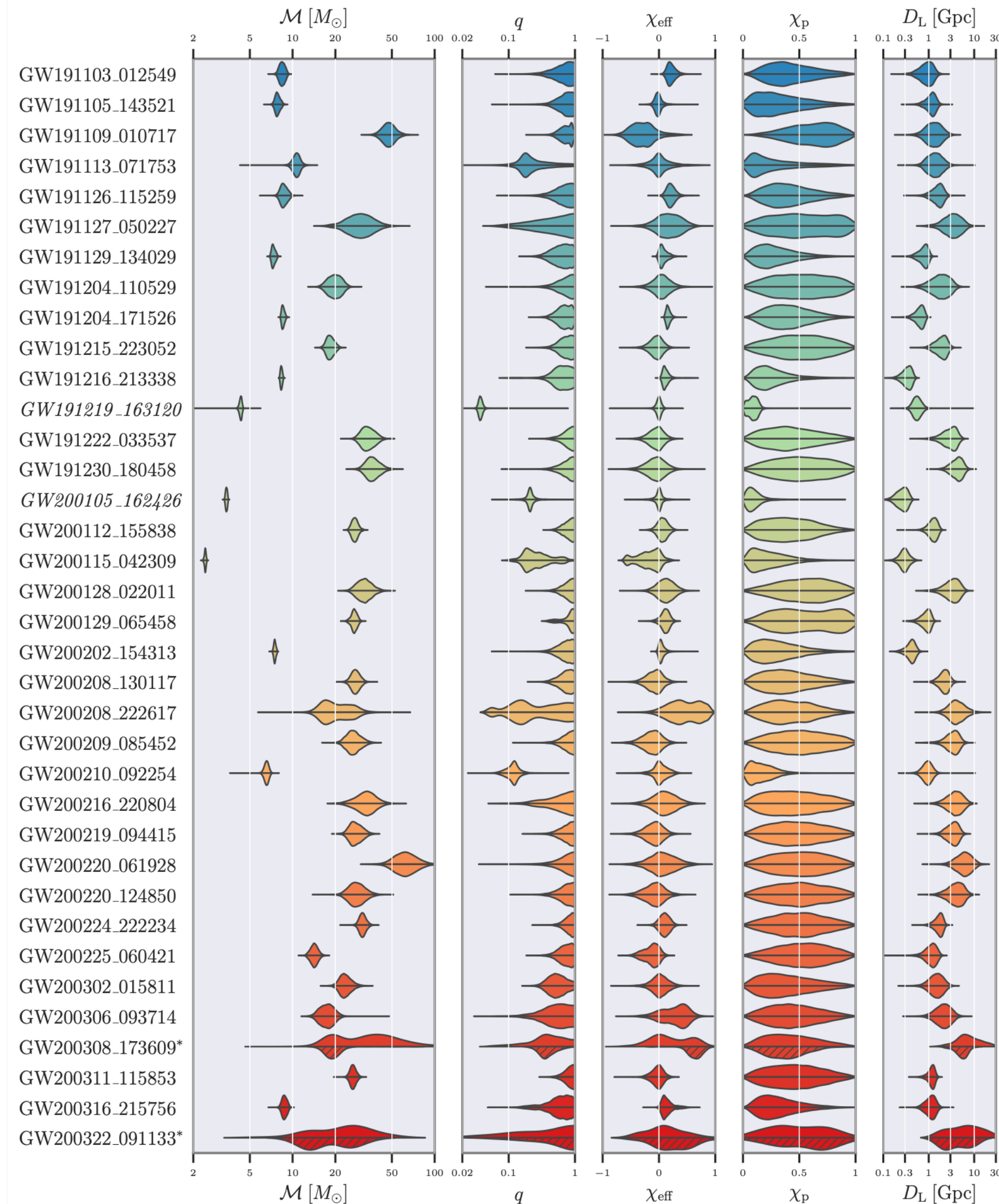
- Constant improvements to the instruments
  - Increased duty cycle: full network was in observing mode for 51.0% of the time in O3b (vs 44.5% in O3a)
  - Increased BNS inspiral range (the maximum distance at which a fiducial BNS system could be detected)



Credit: LIGO-Caltech



# Black holes of all sizes



- All three types of 'canonical' compact binaries have been observed in different observing runs
- Huge variety of source parameters, lots of stress-tests for current models → big motivation for constant upgrades!

LIGO-Virgo-Kagra  
Collaboration arXiv:  
arXiv:2111.03606

# Implications for tests of GR

## POSITIVE

- More stringent combined bounds expected due to the increased number of events

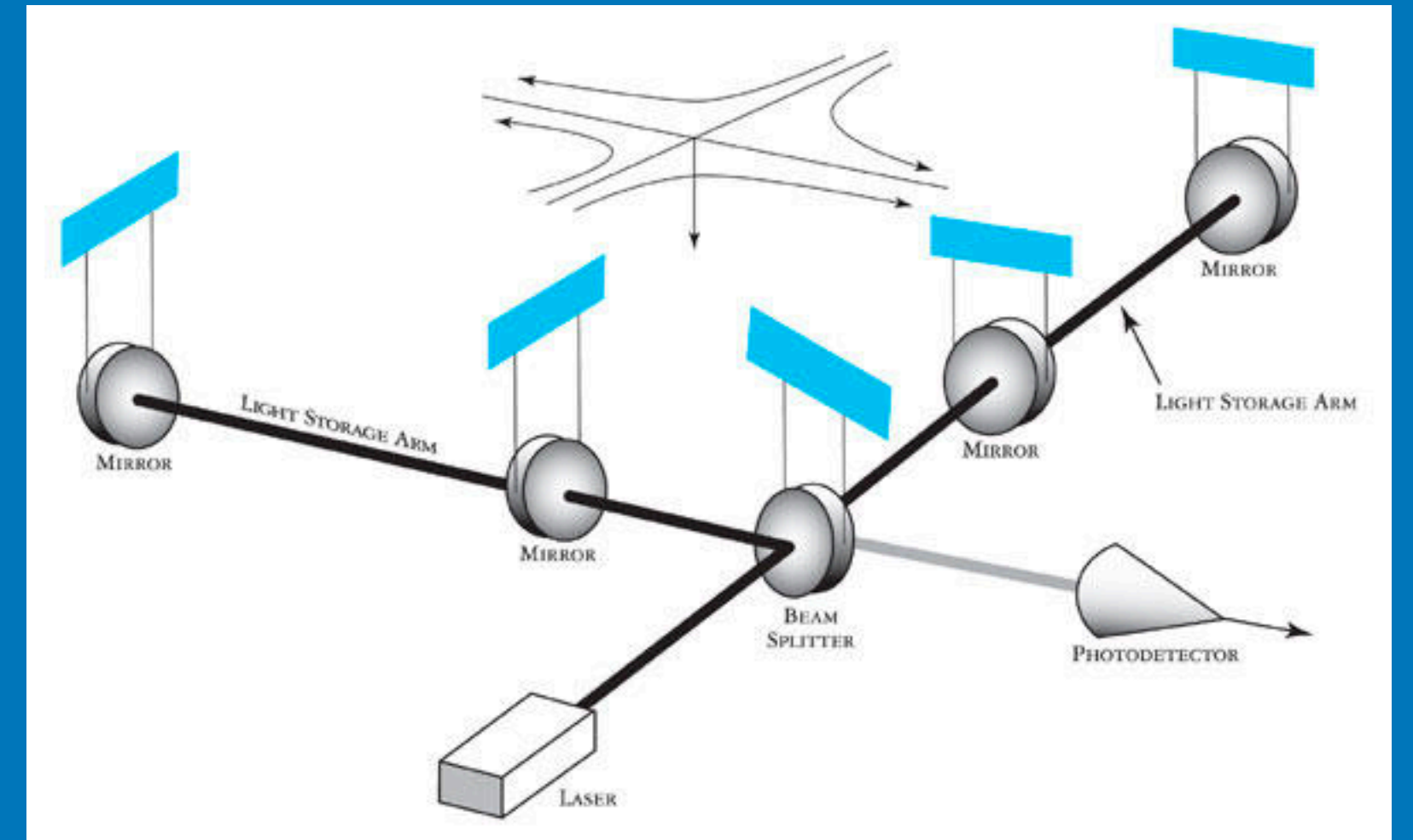
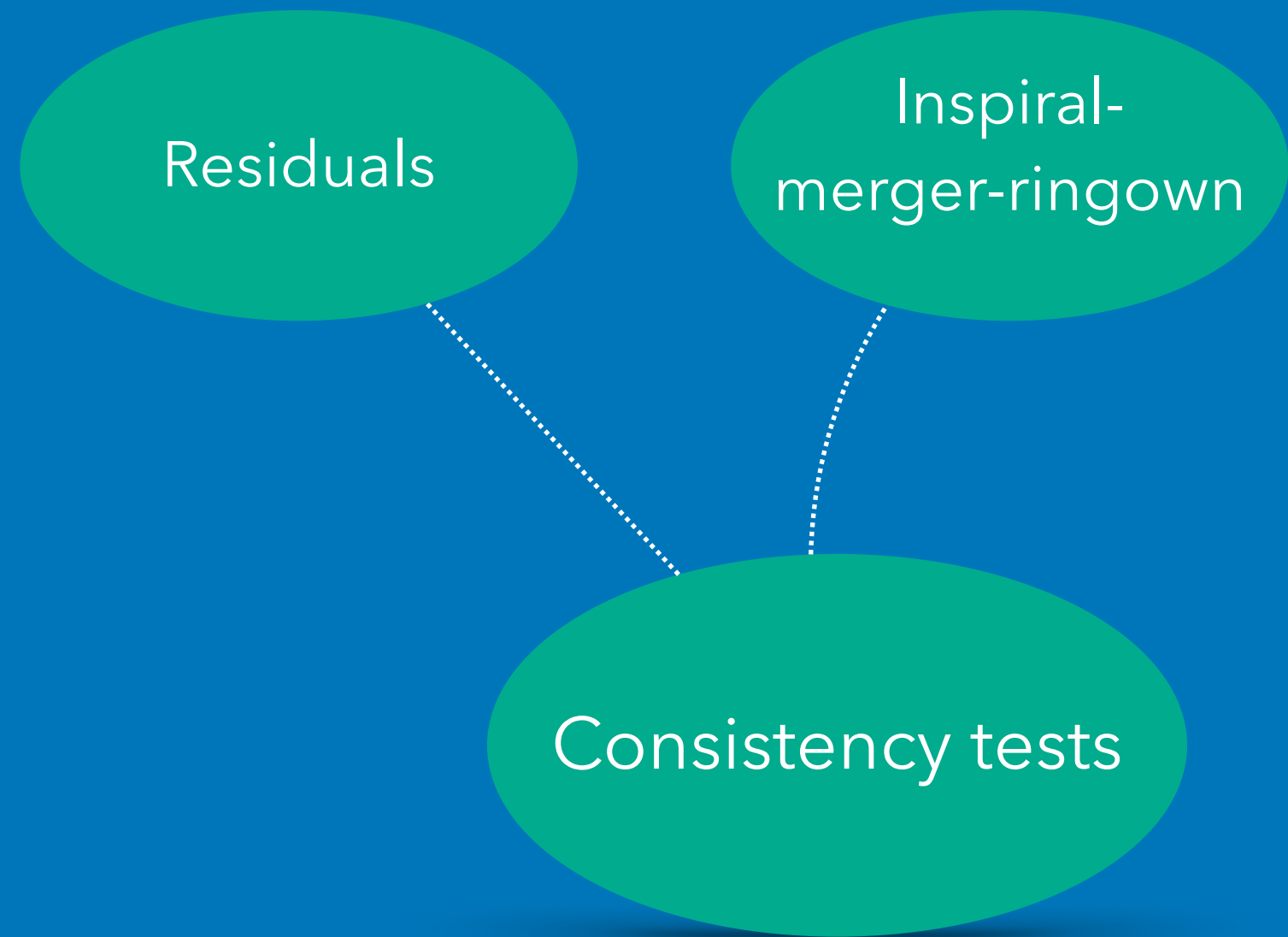
## NEGATIVE

- Increased computational burden -> need to focus on loudest / most suitable events (depending on type of test)
- More non-vanilla events for which even GR models deliver contrasting results

# Was Einstein wrong?

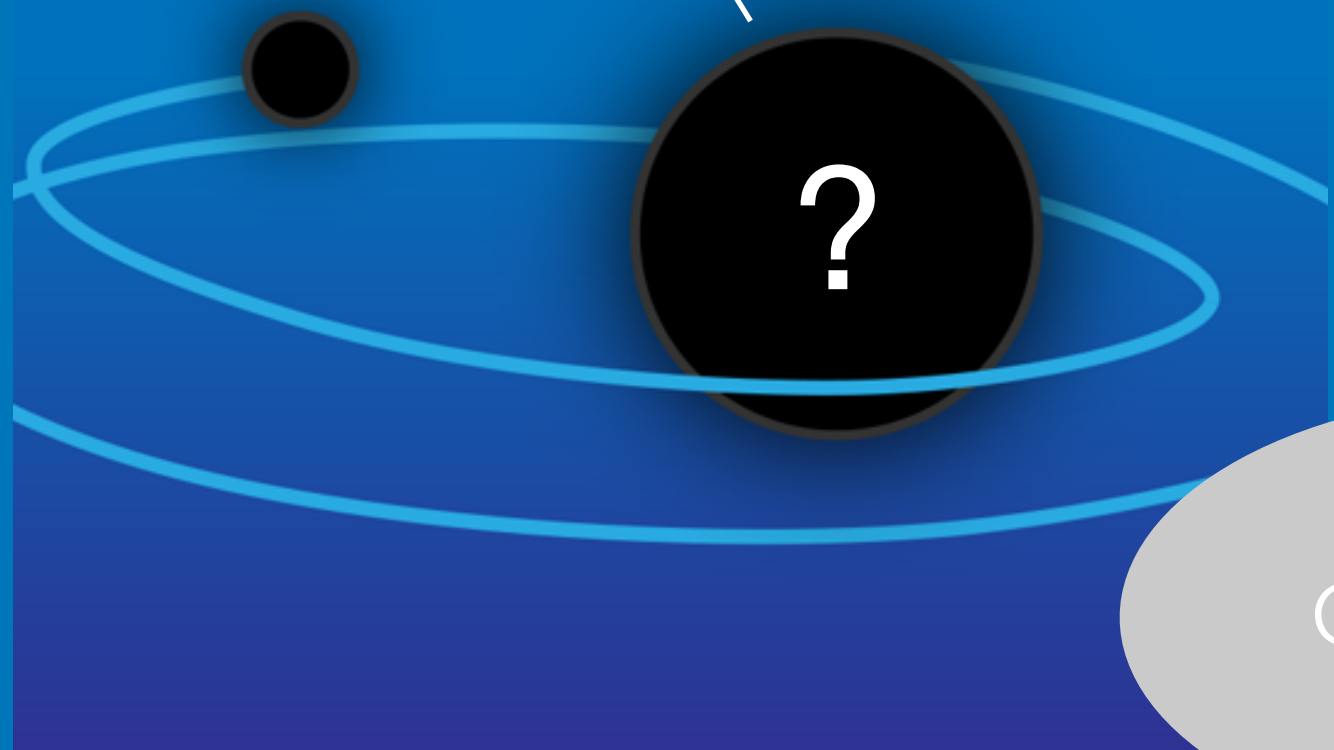
- Through genuine beyond-GR/exotic templates
  - Scarcity of templates, though catalogs of exotic waveforms are growing. Can deep learning come to the rescue? [Freitas+ arXiv:2203.01267v1]
  - PE on real data was using non-BH templates: e.g. GW190521(Bustillo+ PRL 126, 081101 (2021)). Discreteness of templates makes Bayesian inference tasks more subtle
- Common concerns raised about alternative theories of GR:
  - Stability
  - Well-posedness? Progress made in the weak-coupling limit (Okounkova+ PRD 96, 044020 (2017), Kovács&Reall, PRD 101, 124003 (2020))
- Parametrised tests are common but they come with caveats

**Where can we look for  
departures from GR?**

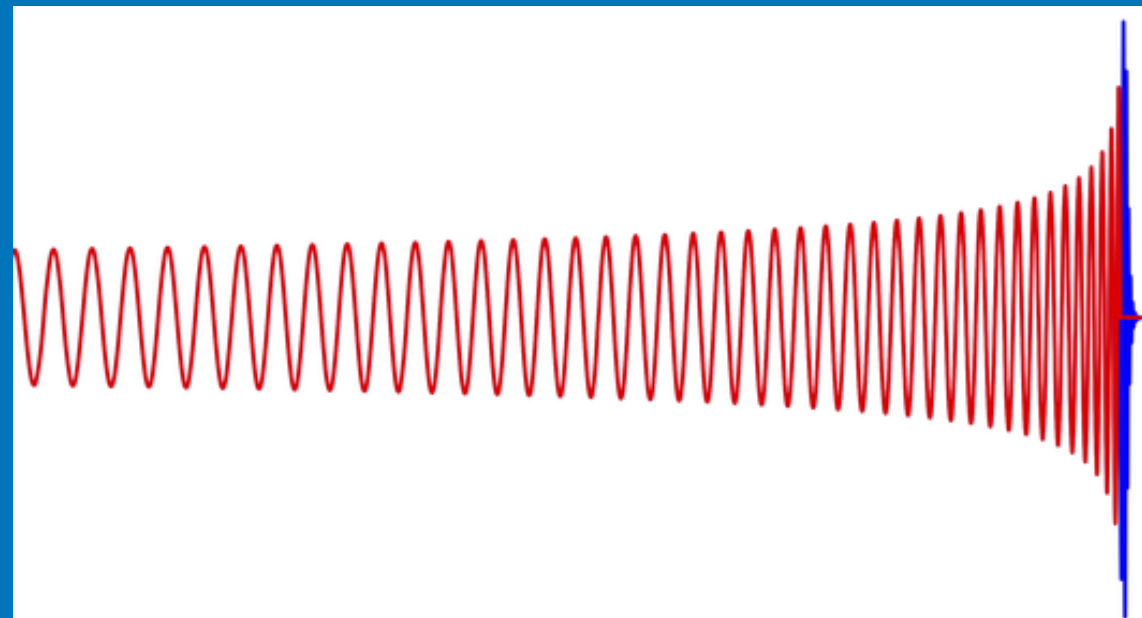


Caltech/MIT/LIGO Lab

Tests of BH nature



APS/Alan Stonebraker



$h_+, h_x$   
...or...?

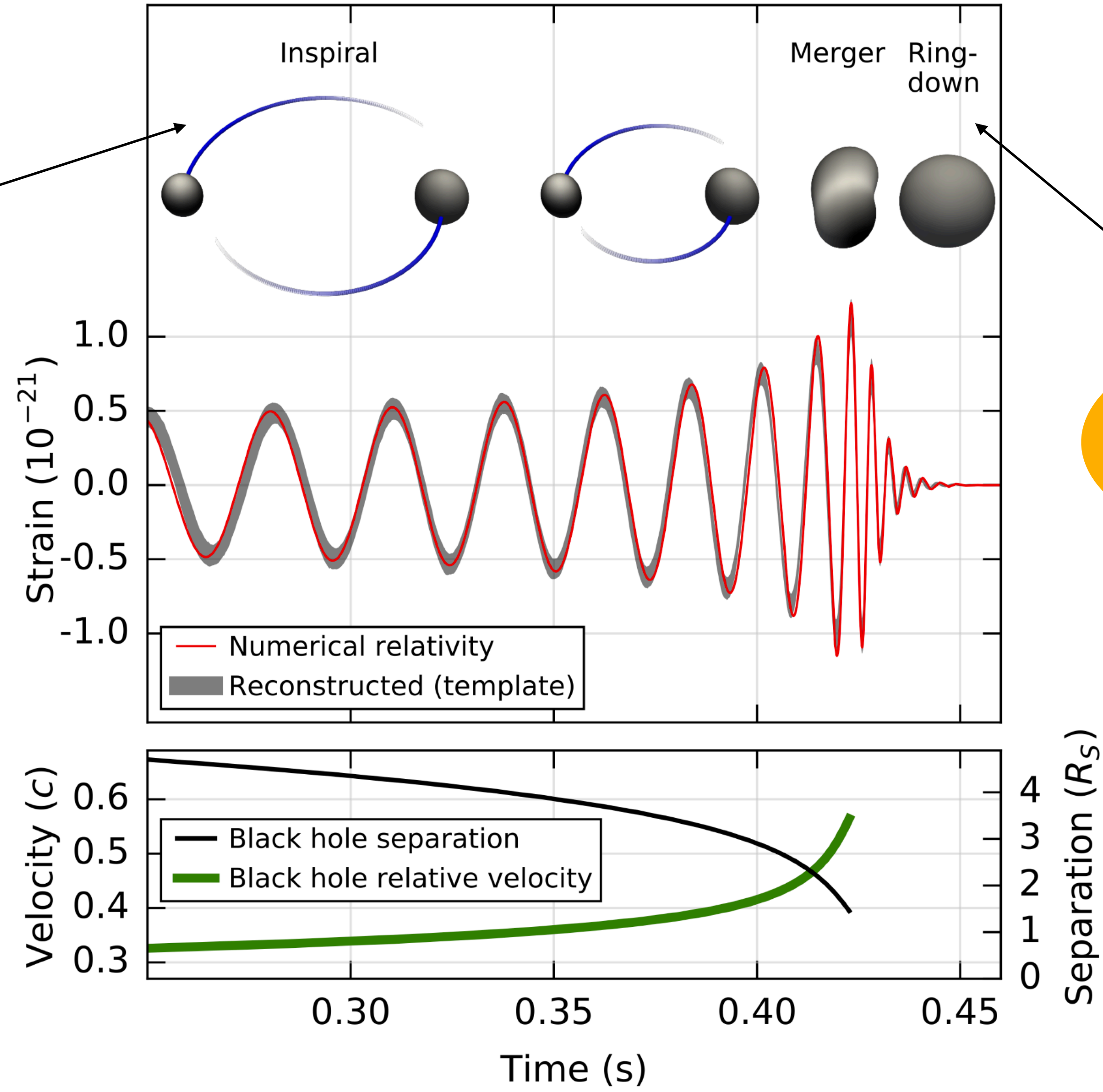
Polarization

Propagation

Generation



Tests based on PN



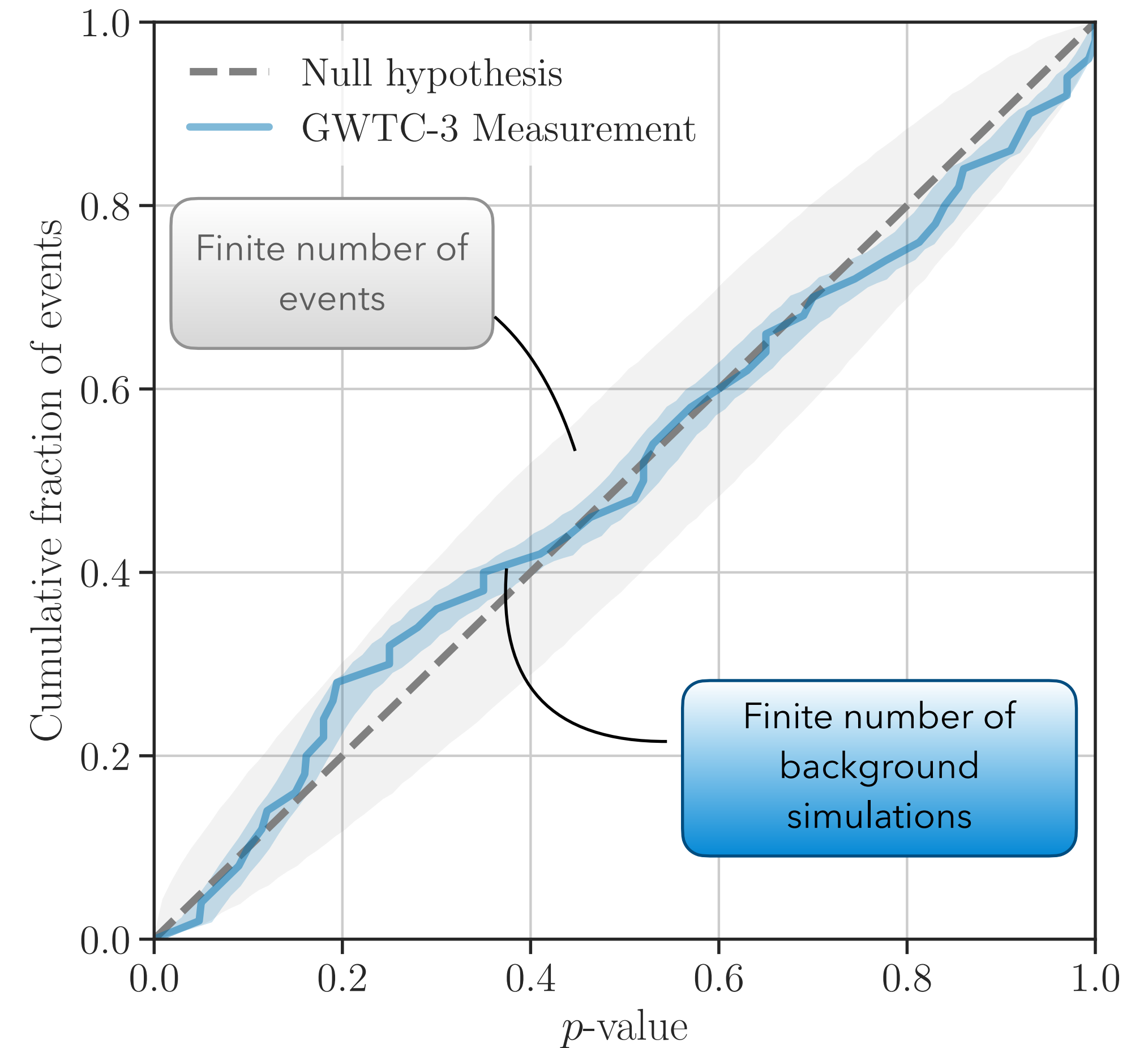
Ringdown tests, echoes...

# Residuals tests

LVK Collaboration, arXiv 2112.06861 [gr-qc]

- Compute 90% credible upper limit on the left-over coherent network SNR after subtraction of  $\max \mathcal{L}$  of fiducial template in a window of  $\sim 1$ s around the trigger
- For each event perform hundreds (200 for GWTC-3) additional runs on time segments near the trigger  $\rightarrow p$ -values:  
$$p = P(\text{SNR}_{90}^n \geq \text{SNR}_{90})$$
- Measurements consistent with null hypothesis within current uncertainties

LVC Collaboration, PRL, 116, 221101 (2016), LVC Collaboration, PRD, 100, 104036 (2019)[GWTC-1], LVC Collaboration PRD 103, 122002 (2021)[GWTC-2]

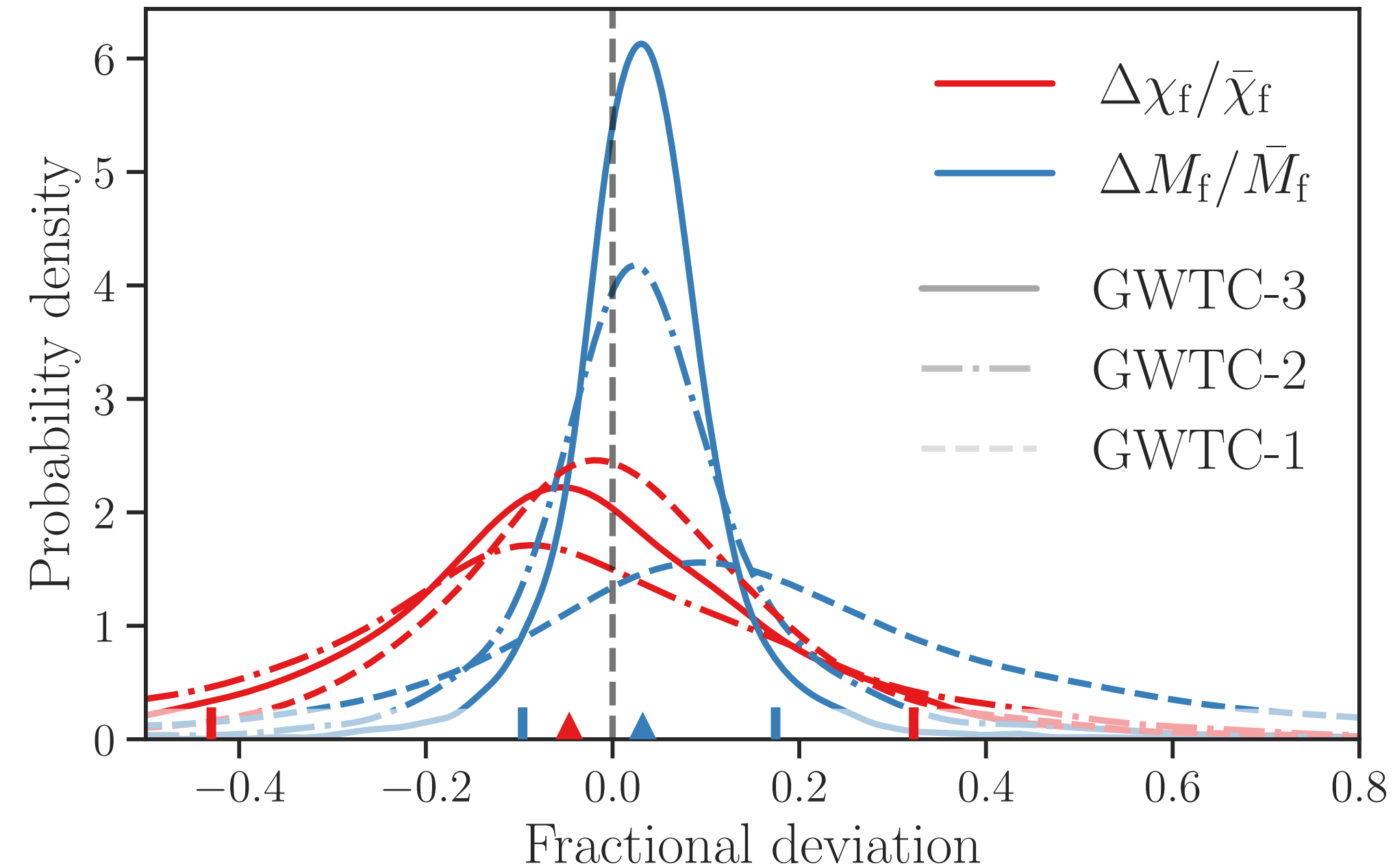


# Inspiral-merger-consistency tests

- Compare inferred final mass and spin of the remnant using only inspiral or post-inspiral part of the signal

$$\frac{\Delta M_f}{\bar{M}_f} = 2 \frac{M_f^{\text{insp}} - M_f^{\text{postinsp}}}{M_f^{\text{insp}} + M_f^{\text{postinsp}}}, \quad \frac{\Delta \chi_f}{\bar{\chi}_f} = 2 \frac{\chi_f^{\text{insp}} - \chi_f^{\text{postinsp}}}{\chi_f^{\text{insp}} + \chi_f^{\text{postinsp}}}$$

- Expect consistency between the two measurements when SNR is high enough in both regions



LVK Collaboration, arXiv 2112.06861 [gr-qc]

# Propagation effects

## Modified dispersion relationship

- Consider propagation of GWs on cosmological background and assume generalized dispersion relation, assuming generation effects are suppressed by powers of  $r/\lambda_g$

$$E = p^2 c^2 + A_\alpha p^\alpha c^\alpha$$

- For  $\alpha = 0$ , can put bound on graviton mass [Will, PRD 57, 2061 (1998)]

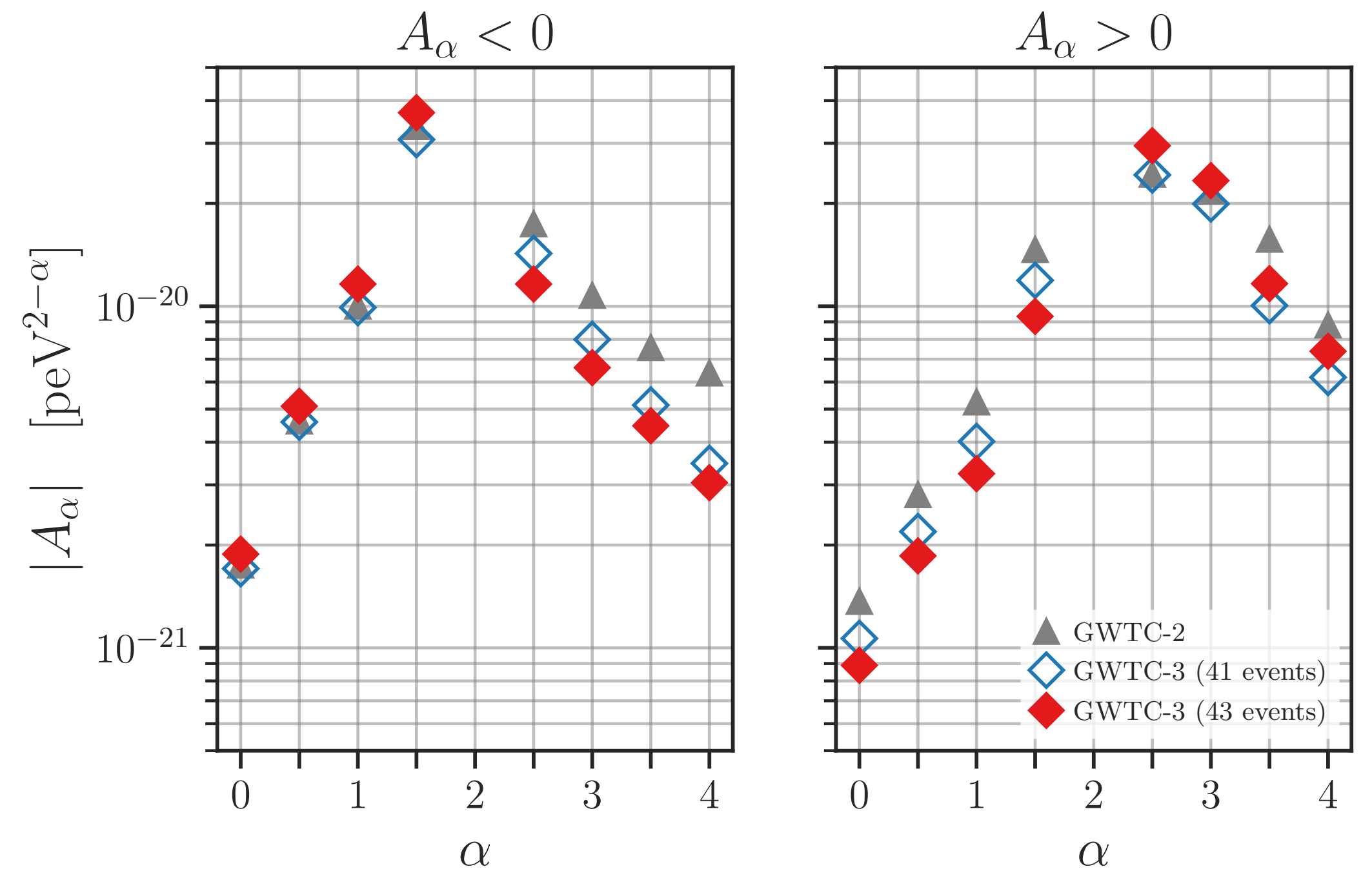
$$m_g = \sqrt{A_0} c^{-2} \quad (\text{requires } A_0 > 0)$$

Fisher-matrix analysis gives

$$\lambda_g > \sqrt{\frac{\rho D_0 \mathcal{M}}{(1+Z)} \frac{\pi}{\Delta^{1/4}}} \quad \text{Mirshekari+ PRD 85, 024041 (2012)}$$

- Non-birefringent analysis
- Allows to test modified dispersion relations even in the absence of electromagnetic counterpart

LVK Collaboration, arXiv 2112.06861 [gr-qc]



# Dispersion tests with bright sirens

- GWs are dark sirens: they give information on luminosity distance but not redshift (redshift can be inferred by assuming a certain cosmological model)
- **Bright sirens**: events with EM counterpart
- Redshift: counterpart (e.g. GW170817) or statistical association to host galaxy to produce probabilistic constraint on it
- Measuring the interval between the arrival time of GWs and electromagnetic radiation, we can put limits on Lorentz invariance (LIGO-Virgo, *Astrophys. J. Lett.* 848, L13 (2017))



# Dispersion tests with bright sirens



- GWs are dark sirens. **Bright sirens**: events with EM counterpart
- Good sky localisation helps: best localised source in O3b was had 90% credible area of 30 deg<sup>2</sup> (was observed with all three detectors (LVK [arXiv:2111.03606v2 \[gr-qc\]](#))).
- Only a few percent of the sources detected until now have a localisation within 20 deg<sup>2</sup>.
- Median sky-localisation during O4 expected to be down to a few tens of square degrees during O4 (LVK Living Rev Relativity 23, 3 (2020))
- Measuring the interval between the arrival time of GWs and electromagnetic radiation, we can put limits on Lorentz invariance (LIGO-Virgo, *Astrophys. J. Lett.* 848, L13 (2017))



# Tests of extra dimensions

- In higher-dimensional theories of gravity, propagation of GWs might be affected by their leakage into extra dimensions beyond a certain screening radius  $R_c$
- This effect was constrained with GW170817 (LIGO-Virgo PRL 123, 011102 (2019))

$$\frac{1}{d_L^{\text{GW}}} = \frac{1}{d_L^{\text{EM}}} \left[ 1 + \left( \frac{d_L^{\text{EM}}}{R_c} \right)^n \right]^{-(D-4)/(2n)}$$

- Magaña-Hernandez ([arXiv:2112.07650v1](https://arxiv.org/abs/2112.07650)) analysed GWTC-3 events (redshifts informed by population model): updated constraints on D both with and without screening are consistent with propagation in four dimensions

# Constraints on massive graviton

- Yukawa suppression of the gravitational potential applies in linearised regime of some massive gravity theories
- Solar system bound test from Bernus+, PRD 102, 021501 (2020):
  - Fit planetary ephemeris to GR plus correction due to Yukawa suppression, for various Compton wavelengths -> Use likelihood threshold to determine bound on  $\lambda_g$  ( $m_g$ ) at 90% C.L.
- $m_g \leq 3.16 \times 10^{-23} \text{eV}/c^2$  Solar System
- $m_g \leq 1.27 \times 10^{-23} \text{eV}/c^2$  GWs
- Will (Class Quantum Grav Letters, 17, 17LT01 (2018)) derives a bound of  $\mathcal{O}(10^{-24})$  using solar system data. Bernus+ argue fits should depend on  $\lambda_g$  as beyond-GR parameters are highly correlated to other parameters of the ephemeris



# Other tests of Lorentz violations

- CPT violation can be related to Lorentz violation (Greenberg PRL 89:231602,2002)
- In the most general case, Lorentz-violating corrections can lead to anisotropic, birefringent and dispersive propagation of GWs
- Study gravitational waves in the presence of Lorentz-violating operators of arbitrary dimension, and compute covariant dispersion relation [Kostelecký&Mewes Physics Letters B,757,510-514 (2016)]
- Asymmetry in the propagation speed and amplitude damping between left and right-hand polarizations of a GW, which leads to phase and amplitude birefringence, respectively.
- Tests performed on GWTC-3 events
  - Zhao+ ApJ 930:139, 2022 (birefringence disfavoured)
  - Wang+ [arXiv:2109.09718](https://arxiv.org/abs/2109.09718): for GW190521 and GW191109, find evidence in support of GW birefringence, however, authors underlines possible role of waveform systematics in interpreting results

# Lensing and propagation effects

- Birefringent propagation can introduce time delays between different metric polarisations, leading to effect qualitatively similar to those expected for lensed signals
- Even if there's no perfect degeneracy between strong lensing and MDR effects lensing might be mistaken for MDR Ezquiaga+ arXiv:2203.13252 [gr-qc]
- Waveform morphology of lensed dispersive GWs depends on the graviton mass more sensitively than unlensed waves.
  - Chung&Li PRD 104 124060 (2022): conclude that 1 lensed signal could constrain graviton's mass as tightly as  $\sim 1000$  unlensed events. Considered microlensing (point-mass lenses), which is expected to be rare for LIGO

# Parametrised tests of GR

- Additional fields in alternative theories of gravity might get activated in the strong-field region, providing new radiative channels
- No monopole or dipole radiation in GR due to the conservation of the stress-energy tensor
- No longer true in beyond-GR models. E.g.: scalarized objects  $\rightarrow$  dipole radiation  $\rightarrow$  faster inspiral (Barausse+ 2013, Palenzuela+ 2014, Sennett+ 2017)
- Flexible, though implicitly requires a certain smoothness in the activation of beyond-GR effects: might not capture more abrupt changes, induced by e.g. dynamical scalarization, resonances

# Parametrised PN tests in LIGO-Virgo analyses

- In the inspiral, introduce theory-agnostic deviations at individual PN orders in the phasing resulting from applying the stationary phase approximation to the chirp

- $$\varphi_{\text{PN}} = 2\pi f t_c - \varphi_c - \frac{\pi}{4} + \frac{3}{128\eta} (\pi\tilde{f})^{-5/3} \sum_{i=0}^7 [\varphi_i + \varphi_{il} \log(\pi\tilde{f})] (\pi\tilde{f})^{i/3}$$

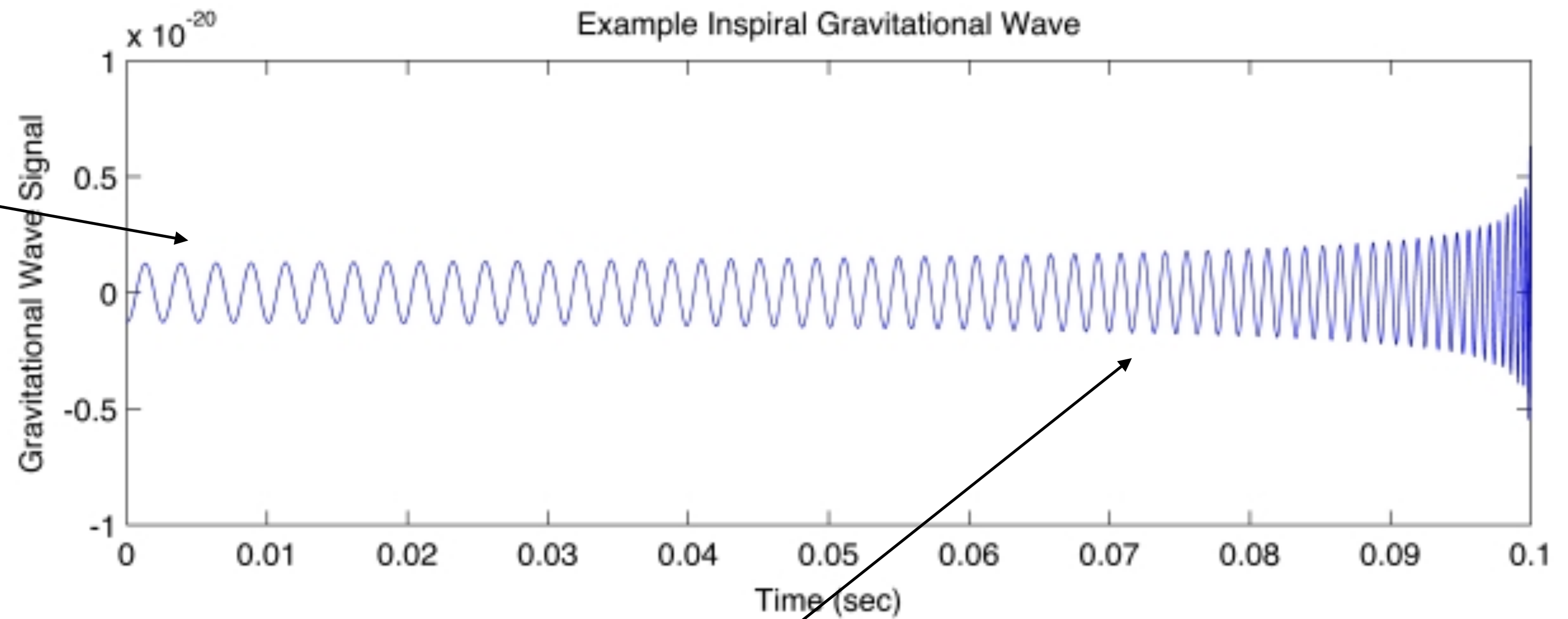
Terms scaling like  $\approx \tilde{f}^{(-5+i)/3}$  at  $i/2$ -th PN order

- LIGO/Virgo analyses constrain -1PN plus orders in the [0 PN, 3.5 PN] interval, in terms of fractional/absolute deviations  $\delta\hat{\varphi}_i$
- -1PN has been used to place constrain on dipole radiation. Other types of negative terms might come from environmental effects [Cardoso&Maselli *Astron.Astrophys.* 644 (2020)], time-varying G or extra dimensions (see Chamberlain&Yunes *PRD* **96**, 084039)

# PN-based inspiral tests

Low order PN terms

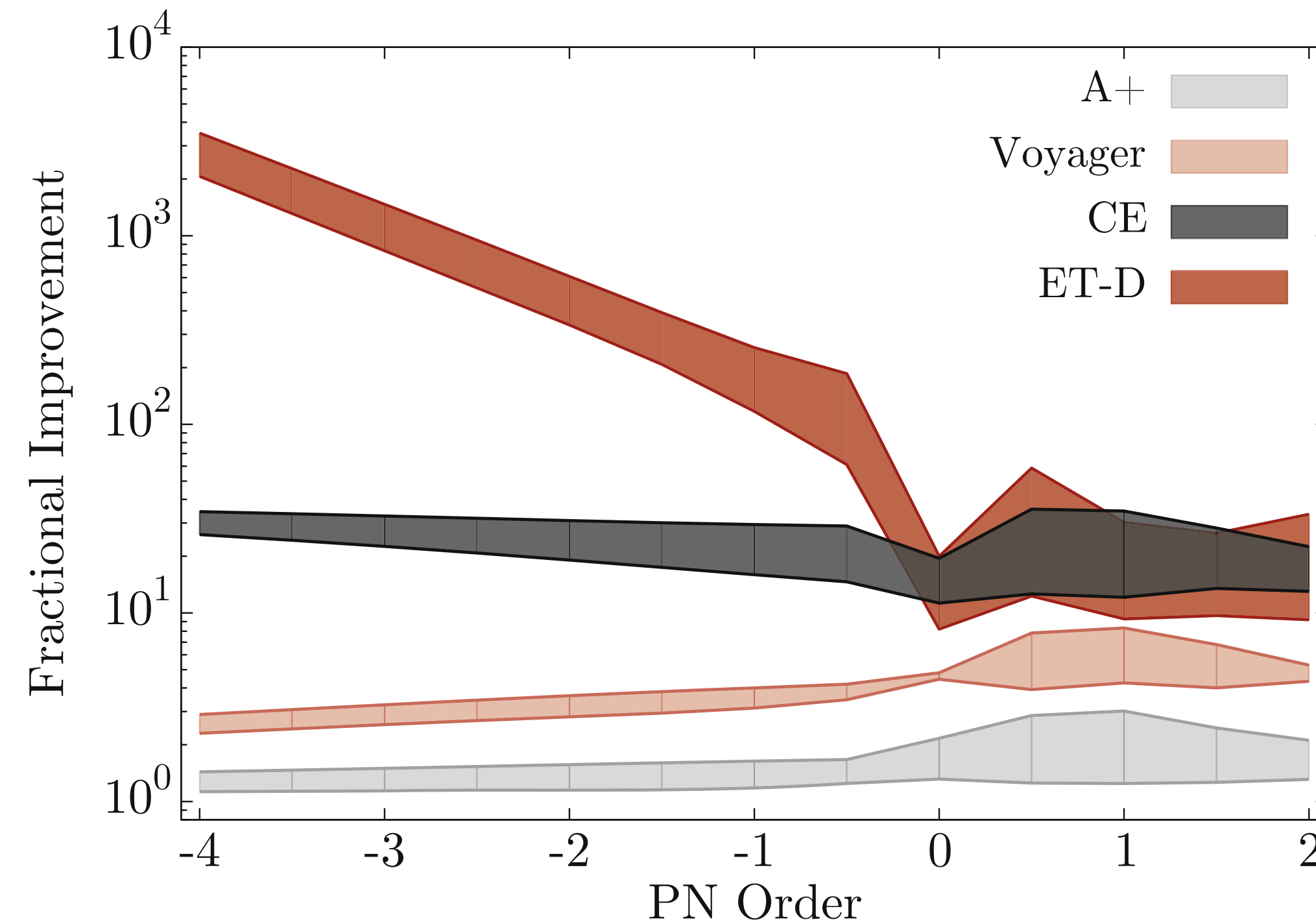
Terms scaling like  $\approx \tilde{f}^{(-5+i)/3}$  at  $i/2$ -th PN order



Credit: LIGO

High order PN terms

# Expected improvements with 3G detectors

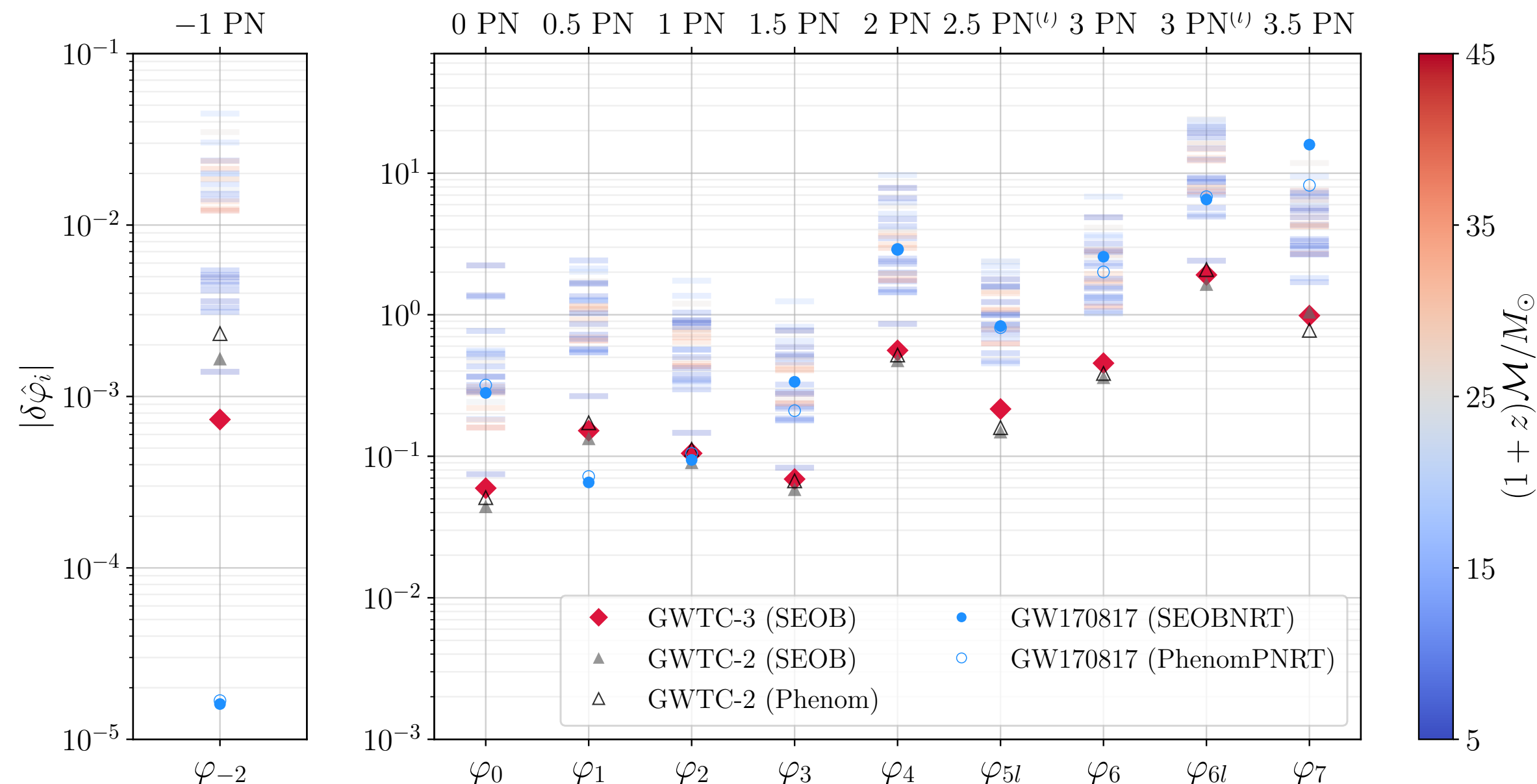
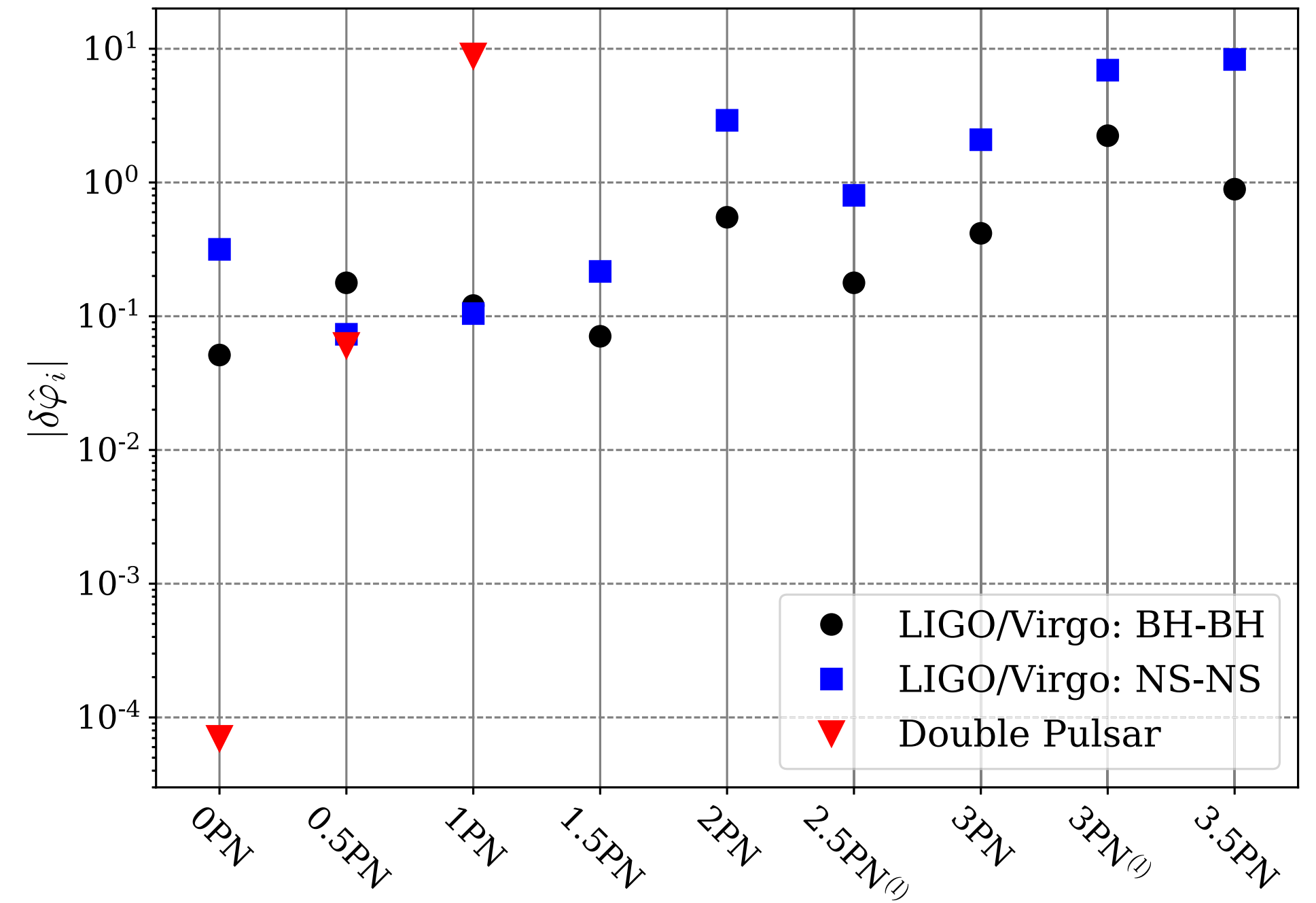


From: Chamberlain&Yunes PRD **96**, 084039

- Estimate on individual events, compared to aLIGO design sensitivity
- Combined bounds will be in general stronger by a factor  $\sim\sqrt{N}$

# LIGO vs double-pulsar constraints

- Double-pulsar constraints obtained with double pulsar PSR J0737-3039A/B in Kramer+ PRX 11, 041050 (2021)
- Complementary tests
  - different regimes (mildly vs strongly relativistic)
  - different binary systems (BNS vs BBH/NSBH): in some scalar-tensor theories, source for scalar field might depend also on matter-independent terms (Yagi+ PRD 93, 024010 (2016))
  - DP tests degrade at high frequencies (higher PN orders)



Joint-likelihood approach  
(assume shared value of deviations across **all** events)

# Constraints on dipole radiation

- If we parametrise deviations from GR emission as

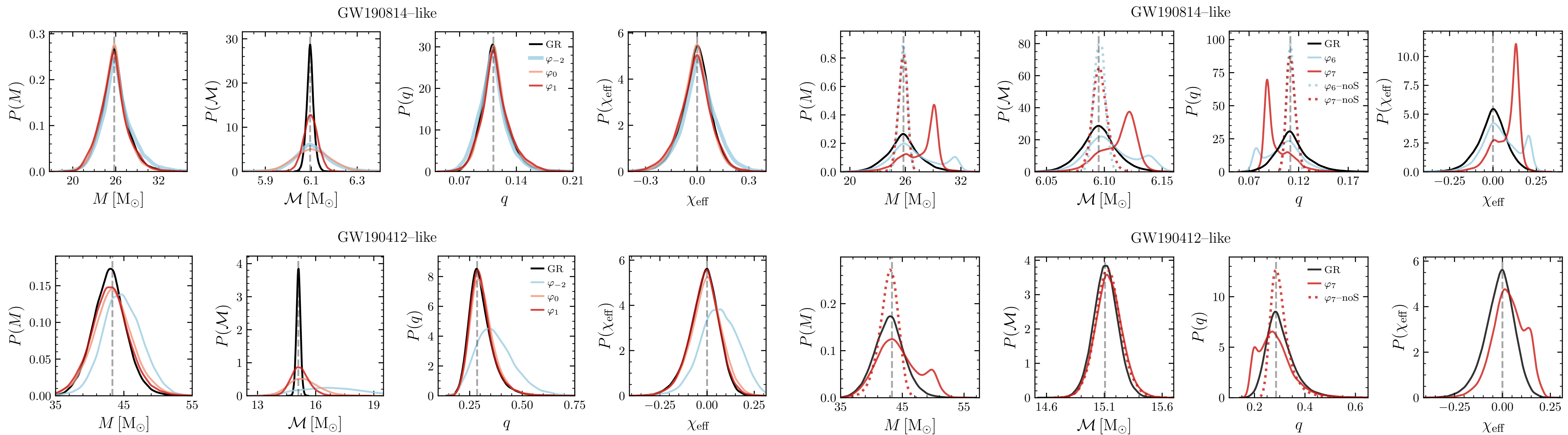
$$\mathcal{F}_{\text{GW}} = \mathcal{F}_{\text{GR}}(1 + Bv^2/c^2)$$

- GW170817 :  $B \leq 1.2 \times 10^{-5}$  *LIGO-Virgo PRL* **123**, 011102 (2019)
- Double pulsar:  $B \leq 4 \times 10^{-10}$  *Kramer+ PRX* 11, 041050 (2021)
- Better sensitivity of double-pulsar tests at low PN orders (low frequencies) due to the large number of cycles observed: approximately 60000 since 2003 for the double pulsar! Observed cycles for GW170817 were one order of magnitude less.



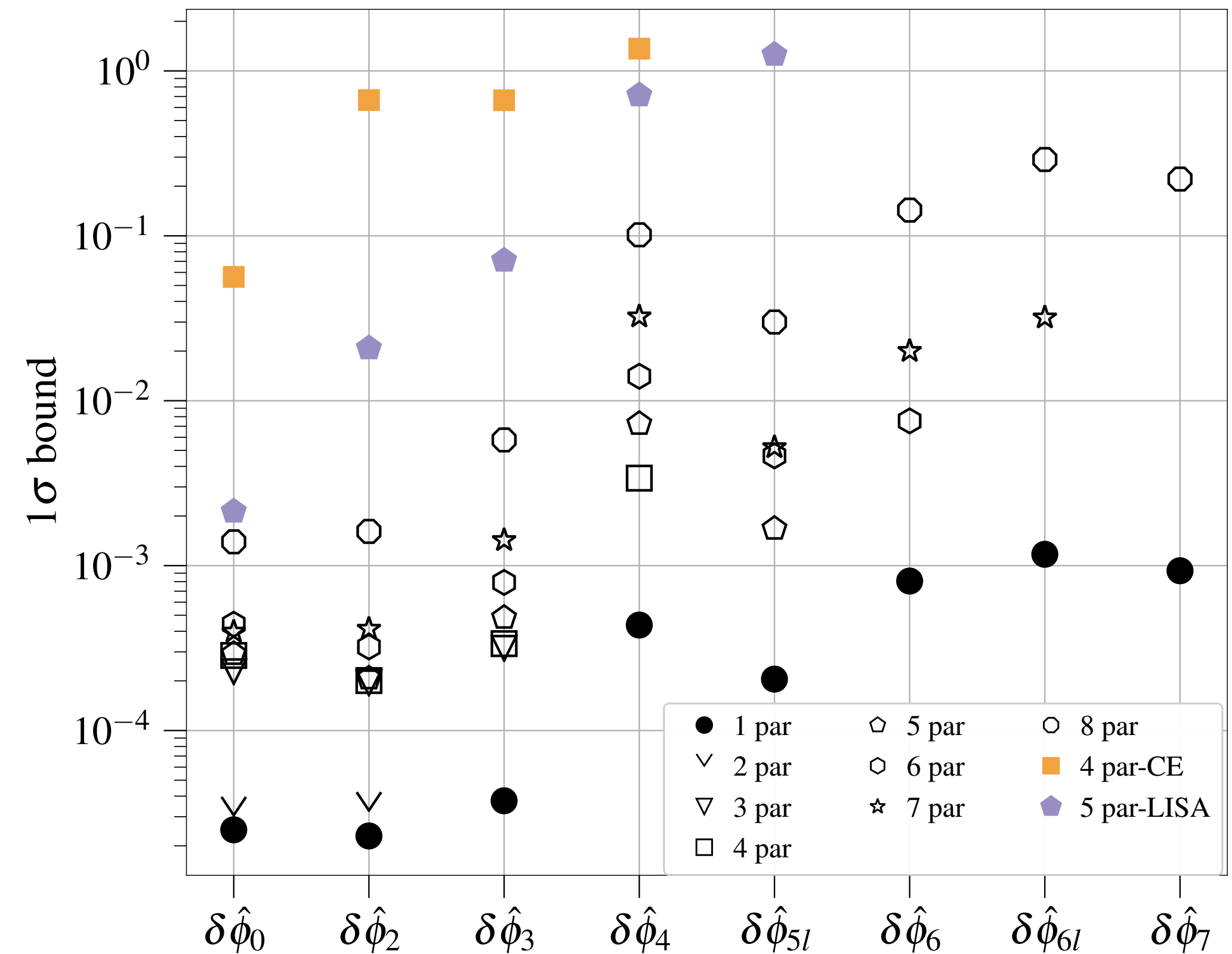
# Parametrised post-Newtonian tests

- Bounds depend on **many** details: PSDs, internal choices of the analysis, characteristics of the events, waveform model used to approximate GR signal etc...
- Parametrised deviations can be strongly correlated with source parameters



# Parametrised post-Newtonian tests (The tricky parts II)

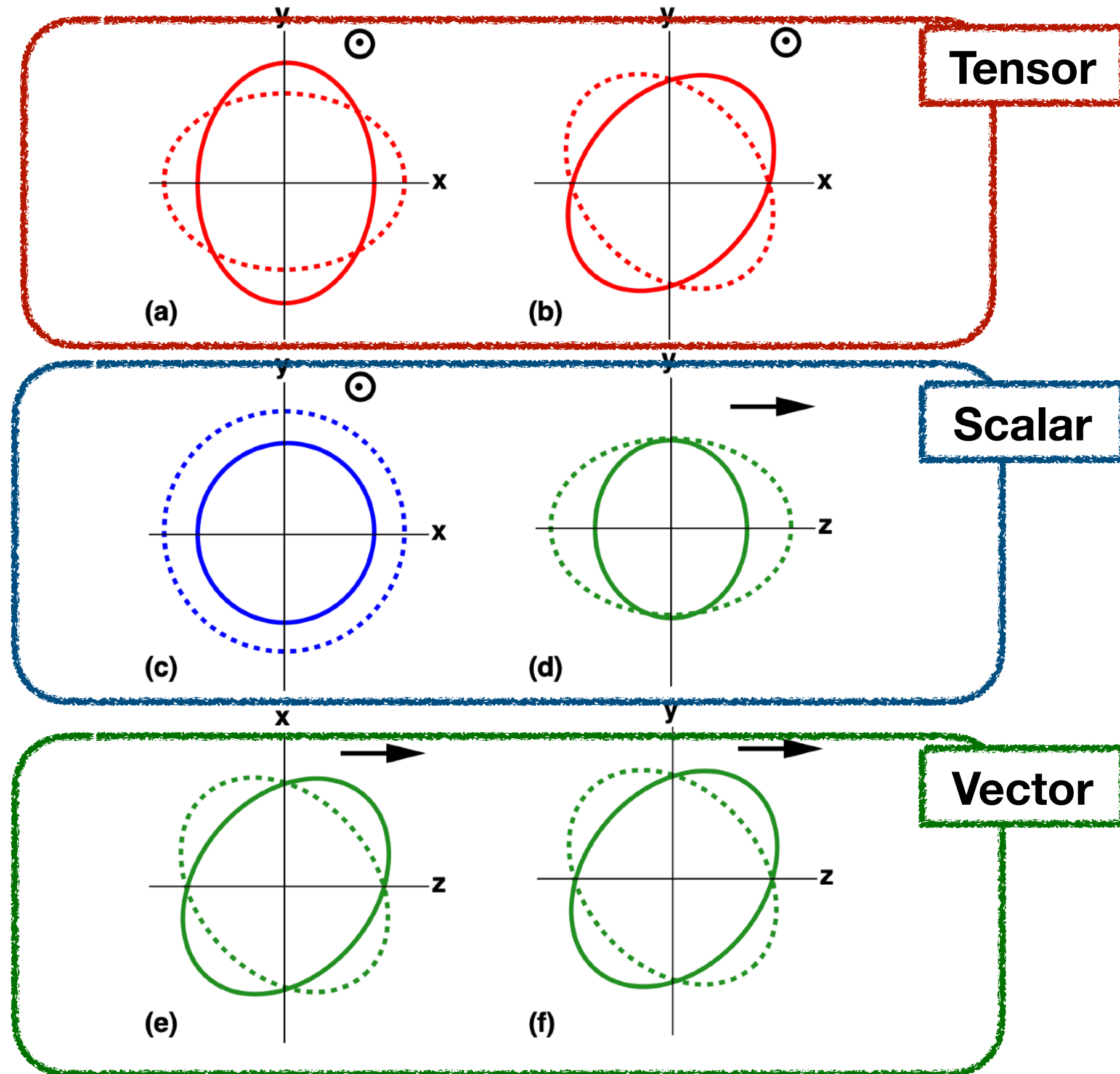
- Bounds on individual PN deviation coefficients, but in alternative theories of gravity multiple coefficients will be different from GR
- Multiparameter tests: Multiband observations of stellar-mass binary black holes will help [Gupta+ PRL 125, 201101 (2020)]
- Can use PCA to find linear combinations of parameters yielding best constraints. Diagonalization of covariant matrix is event-dependent so "combined" PCA parameters need to be computed from combined N-dimensional posterior (for N event). [Pai&Arun, CQG 30, 025011 (2013), Saleem+ PRD 105, 084062 (2022)]
- Neglect of physical information, such as eccentricity, might lead to biases in the PN deviation coefficients [Saini+ [arXiv:2203.04634](https://arxiv.org/abs/2203.04634)]



From: Gupta+ PRL 125, 201101 (2020)

# Polarizations

## Gravitational-Wave Polarization

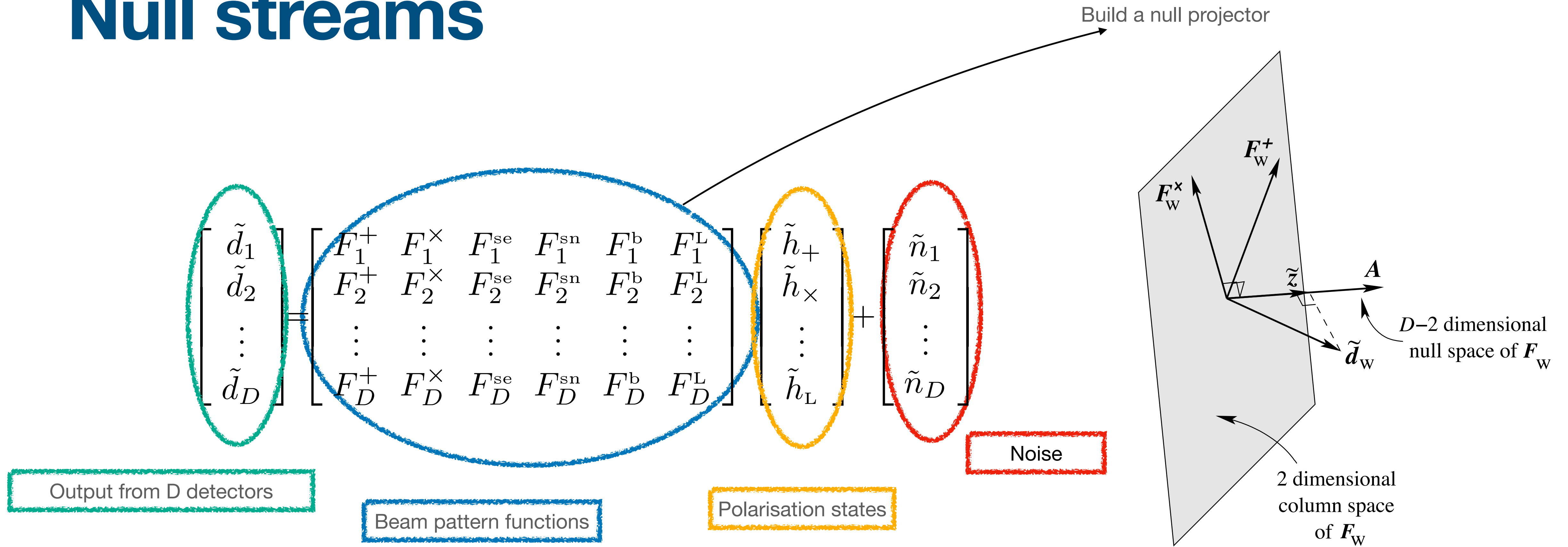


- Generic metric theory of gravity can have up to 6 polarisation states
- Longitudinal and breathing modes for interferometers are not linearly independent
- Detector has a specific response to different polarisations encoded in the antenna pattern functions

$$h(t) = F_+ h^+ + F_\times h^\times + F_{se} h^{se} + F_{sn} h^{sn} + F_b h^b + F_L h^L$$

- The addition of new detectors to the network (KAGRA, LIGO India) will improve the sensitivity to different polarisations

# Null streams



From: Chatziioannou + PRD 86 022004, 2012

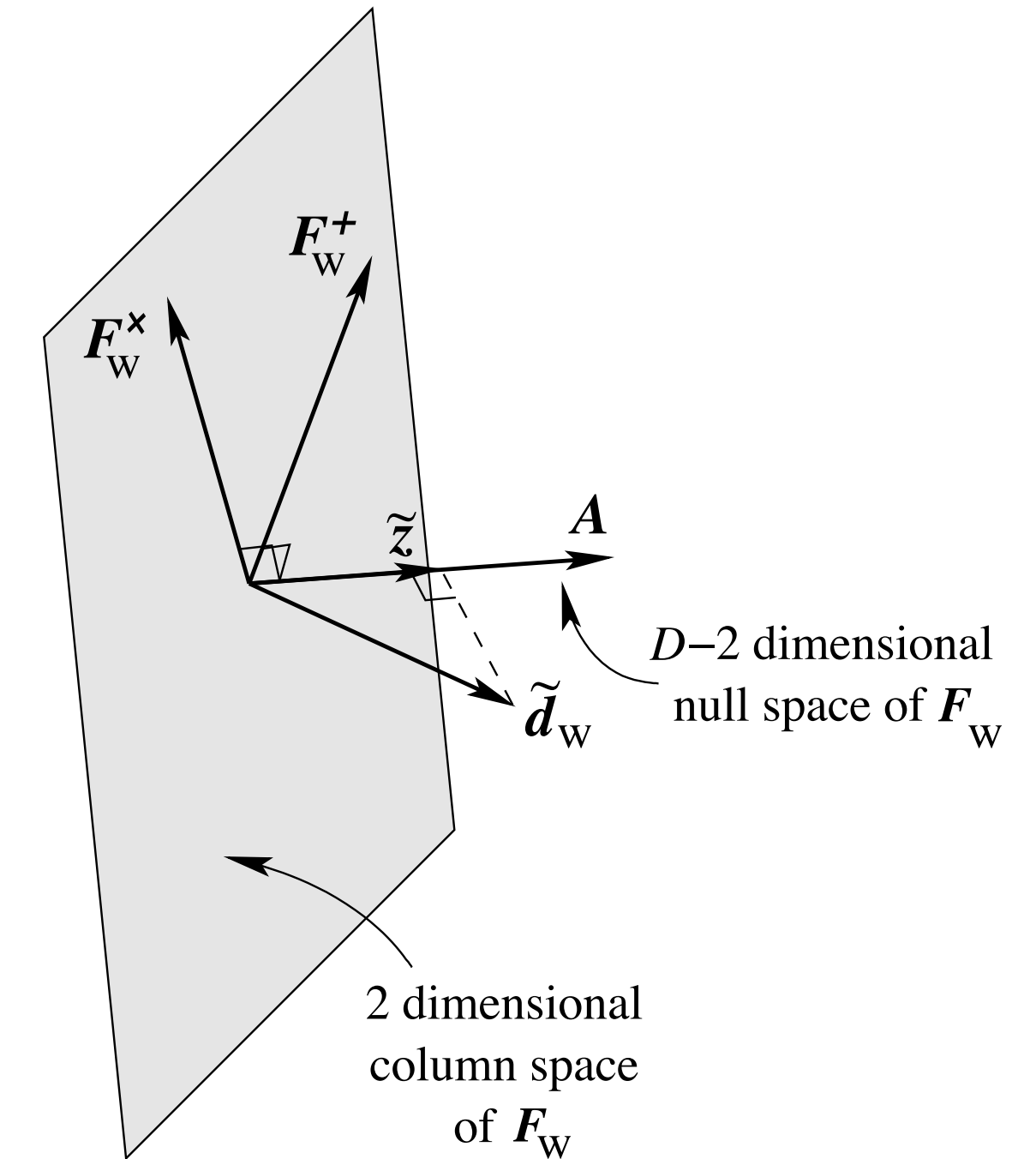
From: Chatterji+ Phys.Rev.D74:082005,2006

One can construct at most  $D-N_{pol}$  independent null streams: e.g. for  $N_{pol}=2$  (GR) we can construct one null stream with the output of 3 detectors

# Polarisation tests

## NULL STREAM

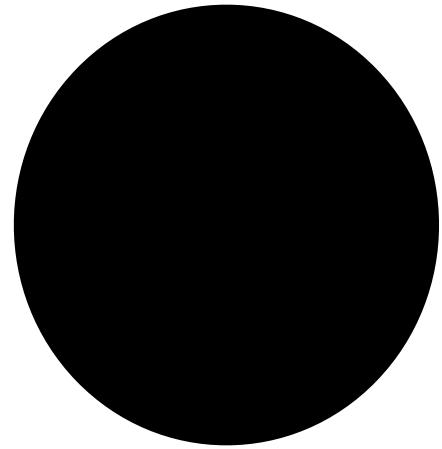
- Can compute excess power after null projection and check whether it's consistent with noise -- originally applied to distinguish GW bursts from instrumental noise [Gürsel&Tinto 1989, Wen&Schutz 1996, Chatterji+ 2006]
  - Depending on the way the projector operator is built, can test either pure (as in LIGO-Virgo [GWTC-1, GWTC-2] or mixed polarisations LIGO-Virgo [GWTC-3], Wong+ 2021).
  - Strongest single-event constraint coming from GW170817 (BF~20 in favour of purely tensorial polarisation of signal) (LIGO-Virgo [1811.00364].)
  - Latest LIGO analysis combines BFs of events from O1-O2-O3 events finding no statistically significant evidence of alternative polarisations
- 
- Mixed polarizations could be also tested using sums of sine-Gaussian wavelets (BayesWave) [Chatziioannou+ 2021]
  - Constraints on mixed polarisation possible even w/out fully breaking degeneracies among all possible states



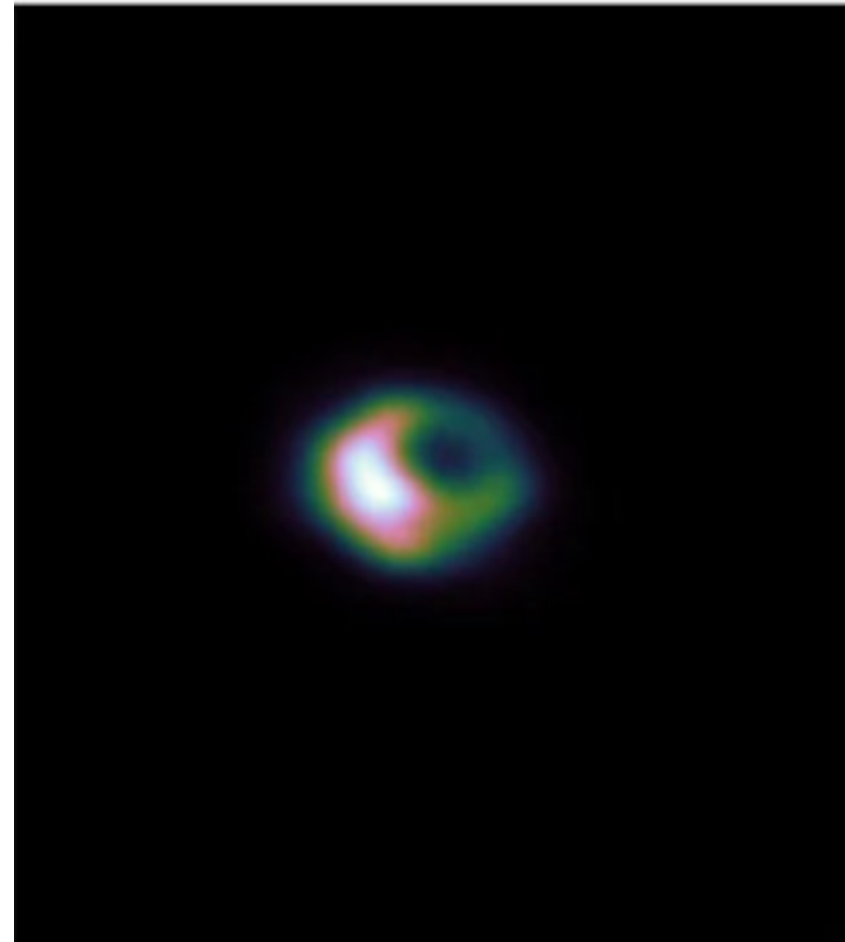
# Tests of black hole nature

# Was it a BH after all?

Classical BH



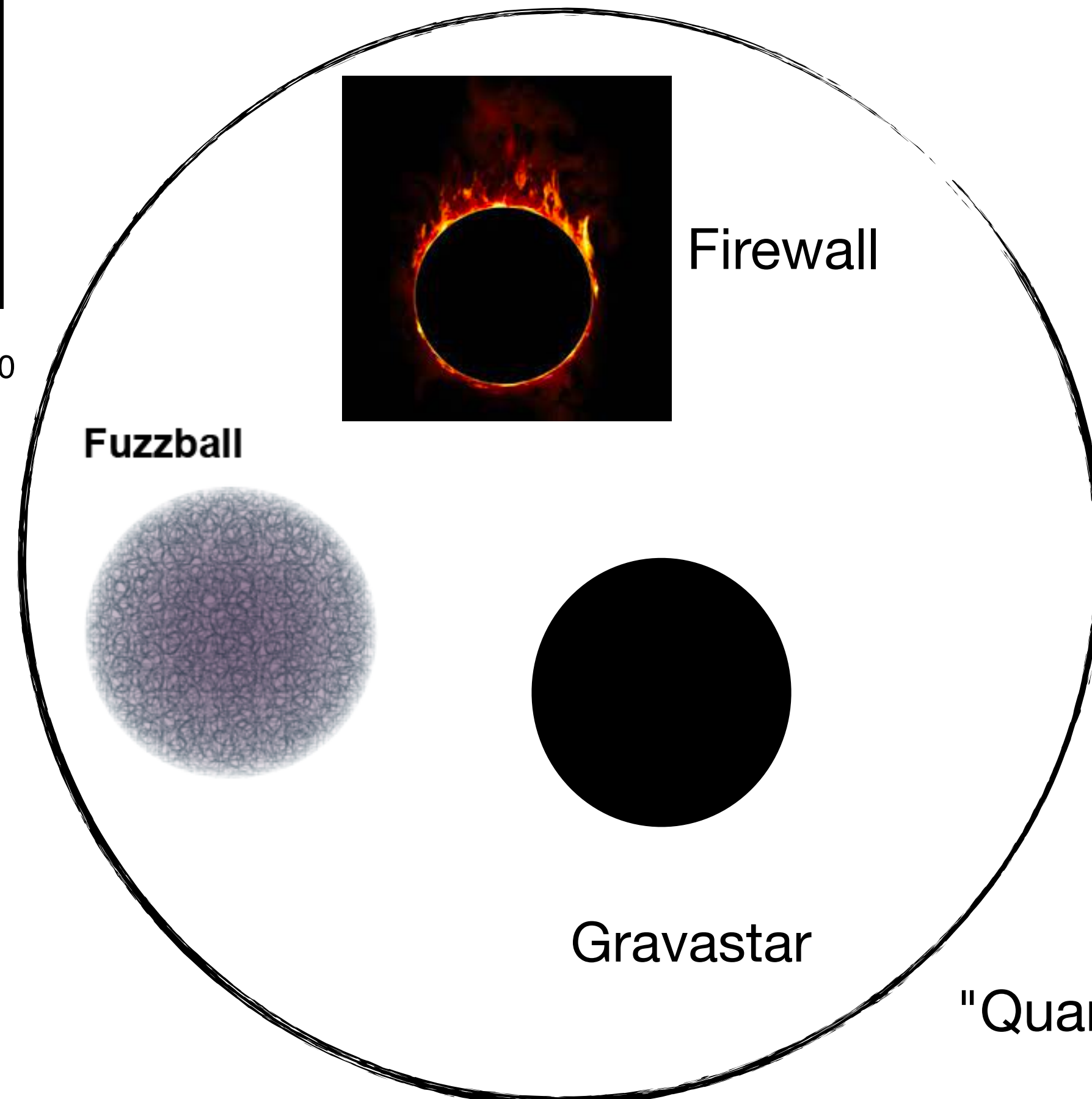
Boson star



Credit: Olivares et al., MNRAS, 2020



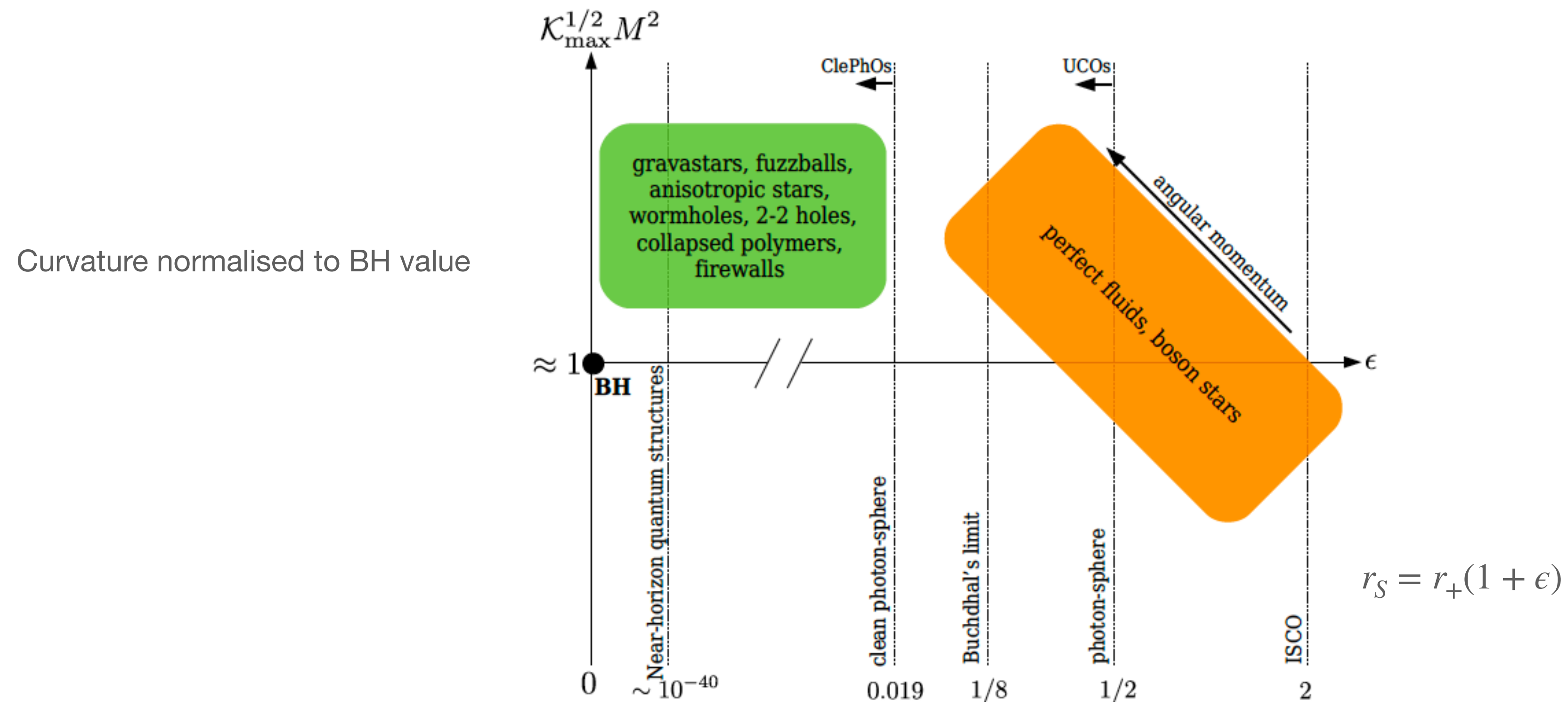
Wormholes



- Semi-classical description of BH  
-> information paradox
- Horizons as a probe of quantum effects
- CBCs considered as good candidates to observe effects coming from new types of weakly interacting particles and new fields addressing fundamental physics puzzles
- Not all the available alternatives have been equally explored in terms of formation/stability/observation signatures (see Cardoso&Pani arXiv:1904.05363v3)

# Was it a BH after all?

- Some tests directly question the nature of the compact objects we detect through GWs
- The different properties of the object can manifest themselves during the inspiral or during the ringdown phase of the coalescence.





# Spin-induced quadrupole moments tests

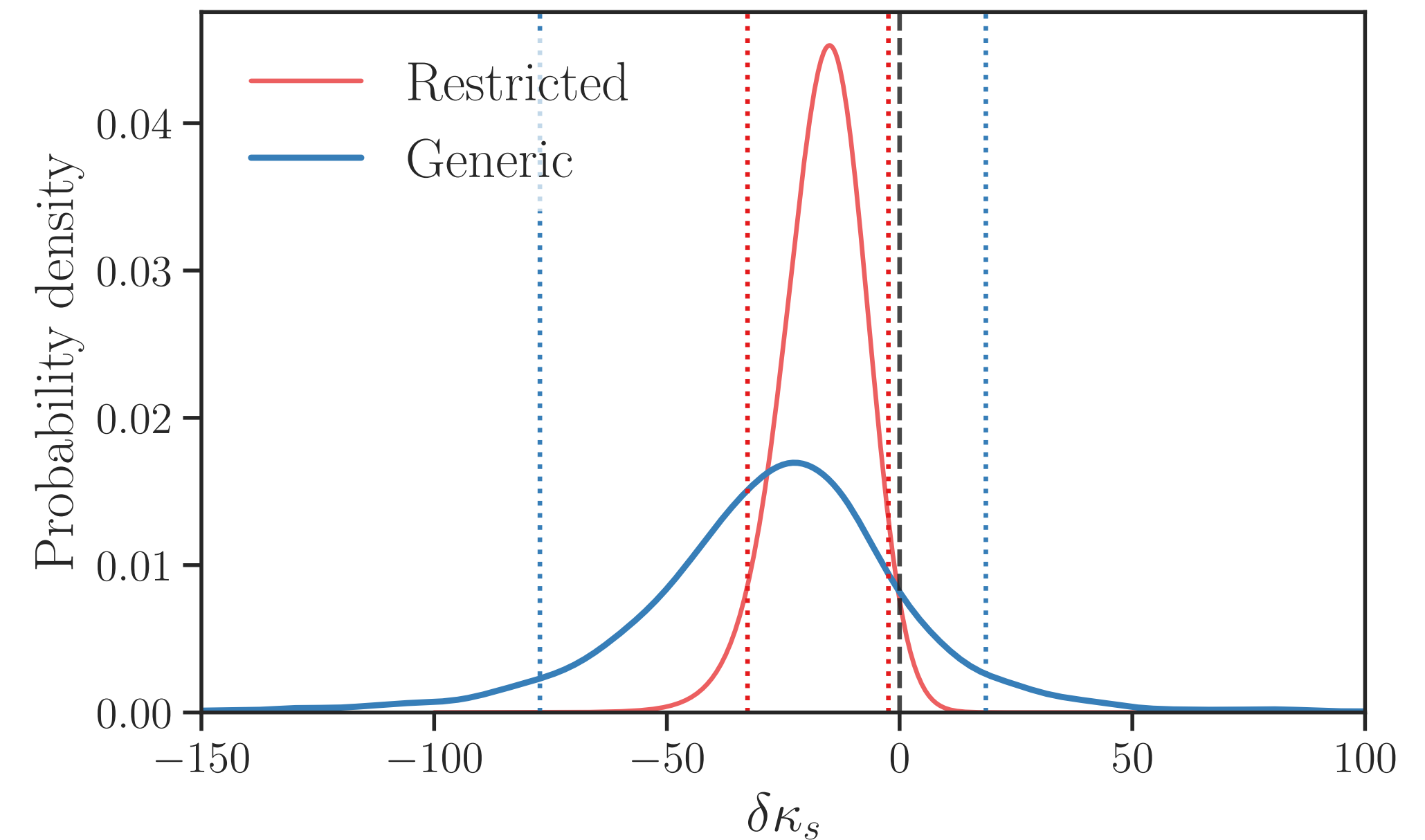
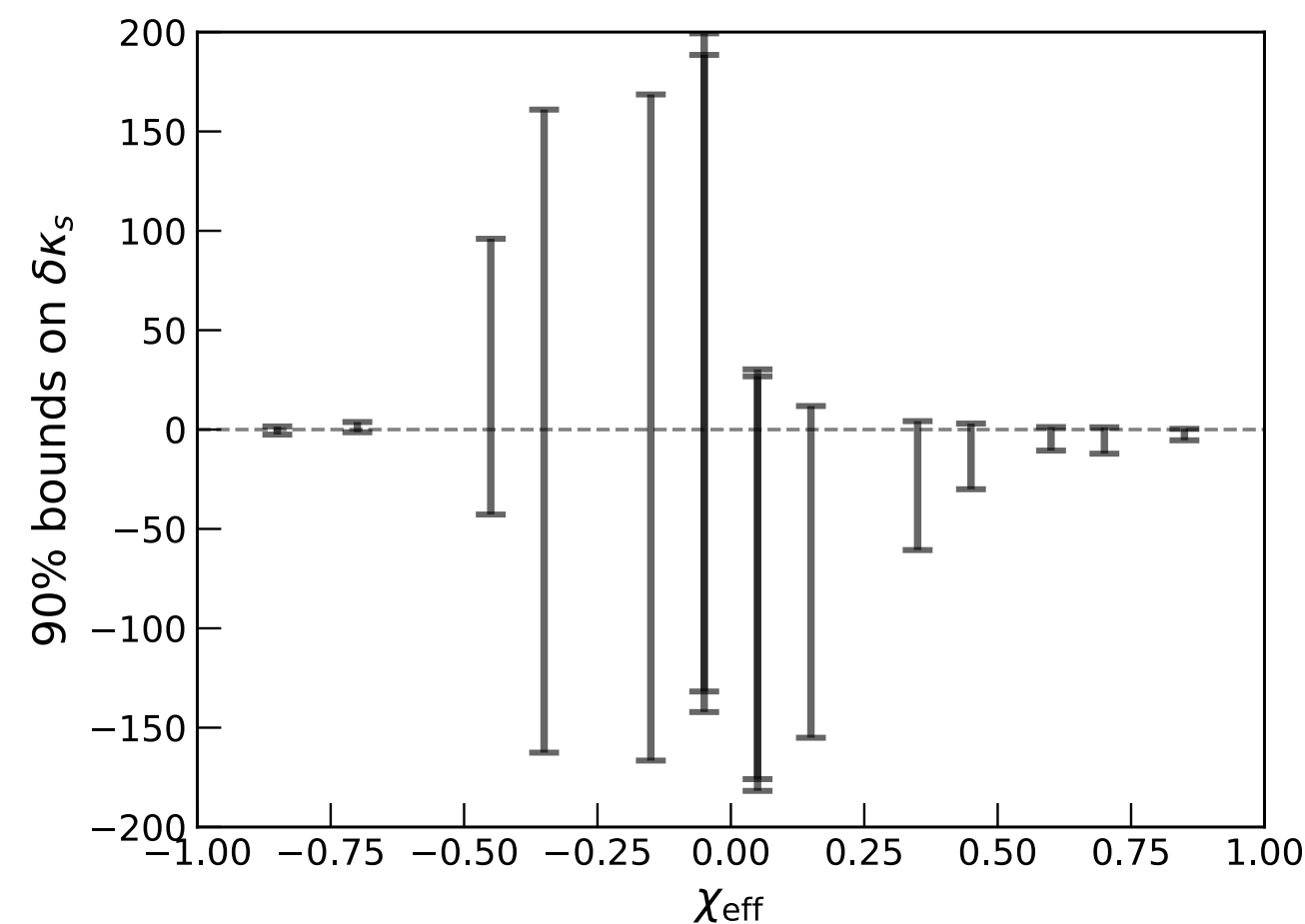
- No-hair theorem → multipole moments of a Kerr BH are entirely determined by its mass and spin
- Spin-induced quadrupole moments leave observable signatures in GWs, leading-order correction at 2PN

$$Q = -\kappa\chi^2 m^3$$

- Assume two objects have the same  $\kappa$ , and measure symmetric combination

$$\kappa_s = \frac{\kappa_1 + \kappa_2}{2} \longrightarrow 1 + \delta\kappa_s$$

Krishnendu+ PRL 119, 091101 (2017)  
 PRD 99, 064008 (2019), PRD 100, 104019 (2019)



LVK Collaboration, arXiv 2112.06861 [gr-qc]

Constraints expected to drastically improve with LISA/DECIGO Krishnendu&Yelikar CQG, 37 205019 (2020)

From: Krishnendu+ PRD 100, 104019 (2019)

# Tidal Love numbers

- Tidal Love numbers are different for ECOs than BHs, tidal corrections appear at 5PN [Cardoso, PRD 95, 084014 (2017)]
- Encapsulate conservative response to external fields
- Recent controversies about Love and Kerr BHs [Le Tiec&Casals,2020, Chia 2020, Goldberger+ 2020, Charalambous+ 2021].
- It is now accepted that Love numbers are 0 for Kerr BHs in 4 dimensions

		Tidal Love numbers			
		$k_2^E$	$k_3^E$	$k_2^B$	$k_3^B$
NSs		210	1300	11	70
ECOs	Boson star	41.4	402.8	-13.6	-211.8
	Wormhole	$\frac{4}{5(8+3 \log \xi)}$	$\frac{8}{105(7+2 \log \xi)}$	$\frac{16}{5(31+12 \log \xi)}$	$\frac{16}{7(209+60 \log \xi)}$
	Perfect mirror	$\frac{8}{5(7+3 \log \xi)}$	$\frac{8}{35(10+3 \log \xi)}$	$\frac{32}{5(25+12 \log \xi)}$	$\frac{32}{7(197+60 \log \xi)}$
	Gravastar	$\frac{16}{5(23-6 \log 2+9 \log \xi)}$	$\frac{16}{35(31-6 \log 2+9 \log \xi)}$	$\frac{32}{5(43-12 \log 2+18 \log \xi)}$	$\frac{32}{7(307-60 \log 2+90 \log \xi)}$
BHs	Einstein-Maxwell	0	0	0	0
	Scalar-tensor	0	0	0	0
	Chern-Simons	0	0	$1.1 \frac{\alpha_{CS}^2}{M^4}$	$11.1 \frac{\alpha_{CS}^2}{M^4} ?$

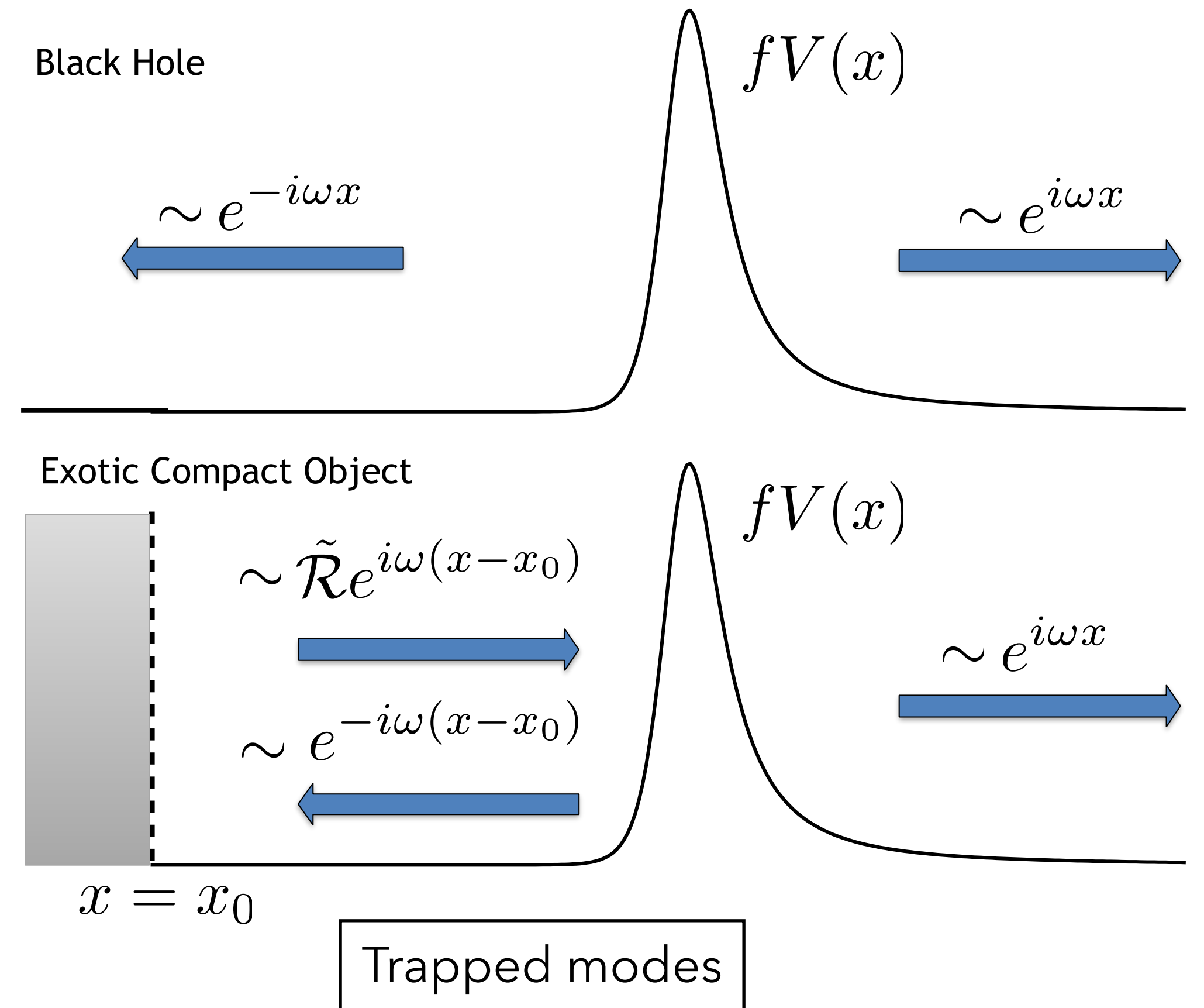
# Tidal heating

- BHs: the horizon is a one-way surface. Flux of energy and angular momentum across the BH's will change its mass and spin leading to tidal heating (torquing) (Poisson&Sasaki PRD 51, 5753 (1995), Alvi PRD64, 104020 (2001)). These tidal effects will backreact on the orbit leaving an imprint in the GW signal.
- GWs can escape from horizonless objects -> Dissipation is expected to be small for ECOs as compared to BHs -> tidal heating can be taken as a measure of the black-hole nature of a compact object (even when external geometry of the objects is very similar)
- In PN, gives corrections starting at 2.5PN order (for spinning objects, else at 4PN) .
- Measurability for 2G and 3G detectors investigated in Mukhrejee+ arXiv:2202.08661 [gr-qc]. Poor constraints from LIGO, would need golden binary (exceptionally close, low mass event),
- Expected to be mostly negligible for LIGO except for high mass ratio high aligned spins (Isoyama&Nakano CQG 35, 2, 024001 (2018), importance of tidal heating increases with mass ratio [Mano+ Prog. Theor. Phys., 98:829-850, 1997, Hartle, PRD, 8:1010-1024 (1973), Hughes PRD, 64,084004 (2001)]
- Absorption expected to be significant for EMRIs with tidal heating suggested as probe of reflective properties of ECOs [Datta+ PRD 101, 044004 (2020), Datta, PRD 102, 064040 (2020)]

# Echoes

From: Mark+ PRD 96, 084002 (2017)

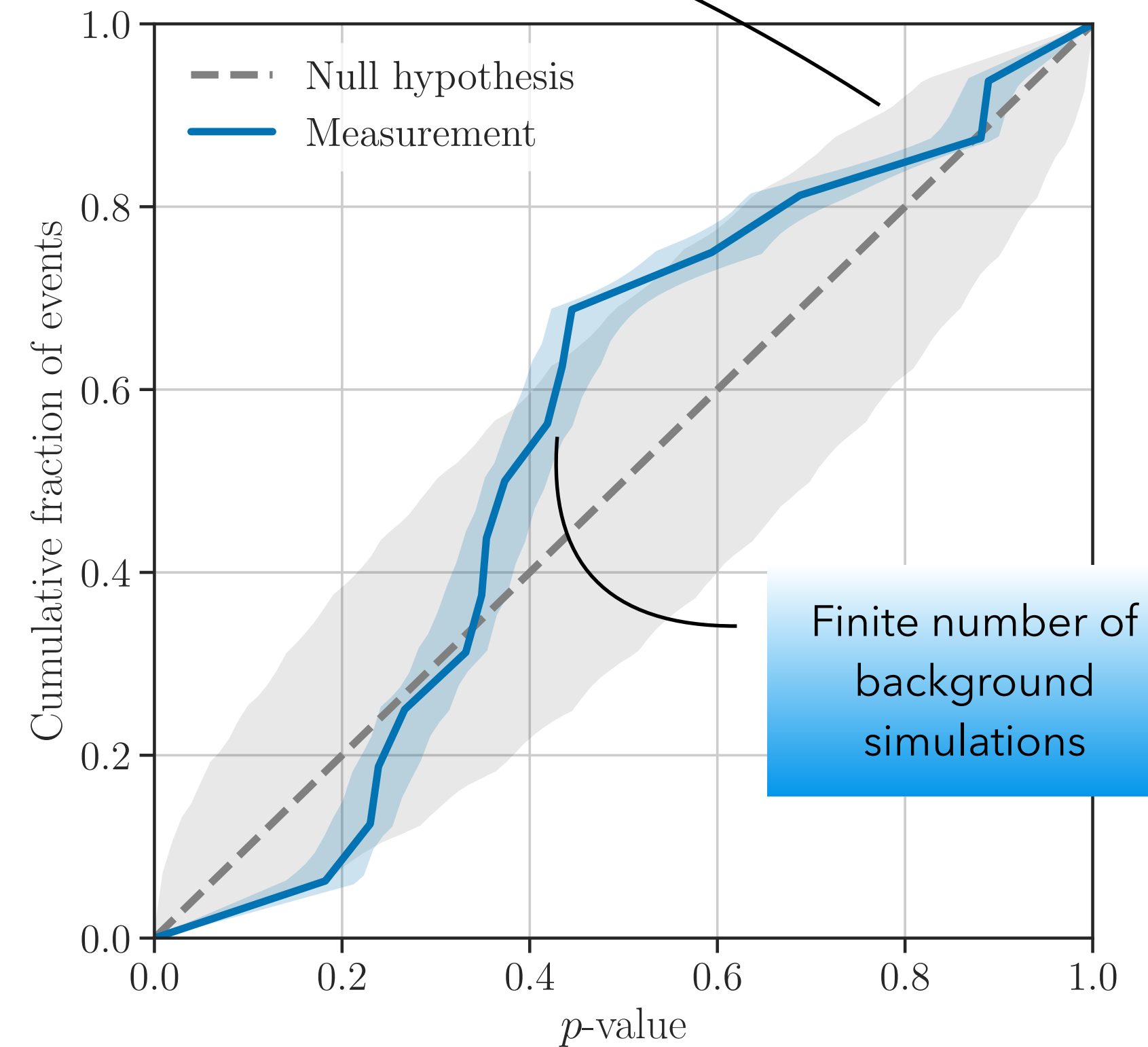
- If event horizon is not there, no purely ingoing boundary conditions
- For ultra-compact objects, prompt ringdown might be followed from echoes: trapped modes slowly leak out of potential barrier producing a train of pulses in the post-merger signal
- Can be modeled
  - by adding the echo signal to an IMR BBH template (LIGO-Virgo, PRD 103, 122002 (2021))
  - in waveform-agnostic way (LIGO-Virgo arXiv 2112.06861, TGR-GWTC-3).
- Contrasting claims in the literature following Abedi+ arXiv:1612.00266v2, in which the authors looked at O1 data. See Abedi+ arXiv:2001.09553v1 for a review.



# Echoes

- Latest LIGO-Virgo analysis models pulses as combs of decaying sine-Gaussians using BAYESWAVE to perform a morphology-independent search method
- Echo signals are expected to be close to detection threshold, so understanding of background behaviour is crucial -> Compute background distributions for the log Bayes factors  $\log_{10} \mathcal{B}_N^S$  in 200 trials around the event
- Hard to understand best parametrization and choice of priors

Finite number of events



LVK Collaboration, arXiv 2112.06861 [gr-qc]

# Ringdown tests

- In GR, mass and spin determine the spectrum of post-merger emission (consequence of no-hair theorem)
- Typically modelled as a linear superposition of damped sinusoids (follows from linear perturbation theory)

$$h_+(t) - ih_\times(t) = \sum_{\ell=2}^{+\infty} \sum_{m=-\ell}^{\ell} \sum_{n=0}^{+\infty} \mathcal{A}_{\ell mn} \exp\left[-\frac{t-t_0}{(1+z)\tau_{\ell mn}}\right] \exp\left[-\frac{2\pi i f_{\ell mn}(t-t_0)}{1+z}\right] {}_{-2}S_{\ell mn}(\theta, \phi, \chi_f)$$

- Despite apparent simplicity of the template used, many subtle points that can lead to discrepant results:
  - Impact of noise
  - Choice of ringdown regime start time
  - FD vs TD
  - Contribution of inspiral-merger signal



## ***Beyond linear effects...***

*Nonlinear effects might play a non-negligible role through non-linear, self-coupling of first-order modes (Ripley+ PRD 103, 104018 (2021)), and dynamically excited due to variation of the remnant's parameters ("absorption-induced mode excitation" - Sberna+ PRD **105**, 064046 (2022))*

# Ringdown tests

- Controversies related to various detection claims:
  - **221 Overtone in GW150914**: total mass of system and high SNR make it an ideal candidate for RD tests (MRD falls in detector's sweet spot).
    - **YES!** Isi+ arXiv:1905.00869v2, arXiv:2202.02941v2
    - **NO!** Cotesta+ arXiv:2201.00822
    - **MAYBE?** Finch&Moore arXiv:2205.07809v1
  - **Higher modes in GW190521 ringdown:**
    - **NO** (LIGO-Virgo [TGR-GWTC-2, arXiv:2010.14529v2])
    - **YES** (Capano+, arXiv:2105.05238): find statistically significant evidence of (2,2) and (3,3) harmonics



Credit: iTHEMS

As it's common in tests of GR, results appear to strongly depend on how the background is factored in, as well as on internal settings of the analysis

# Parametrised ringdown tests

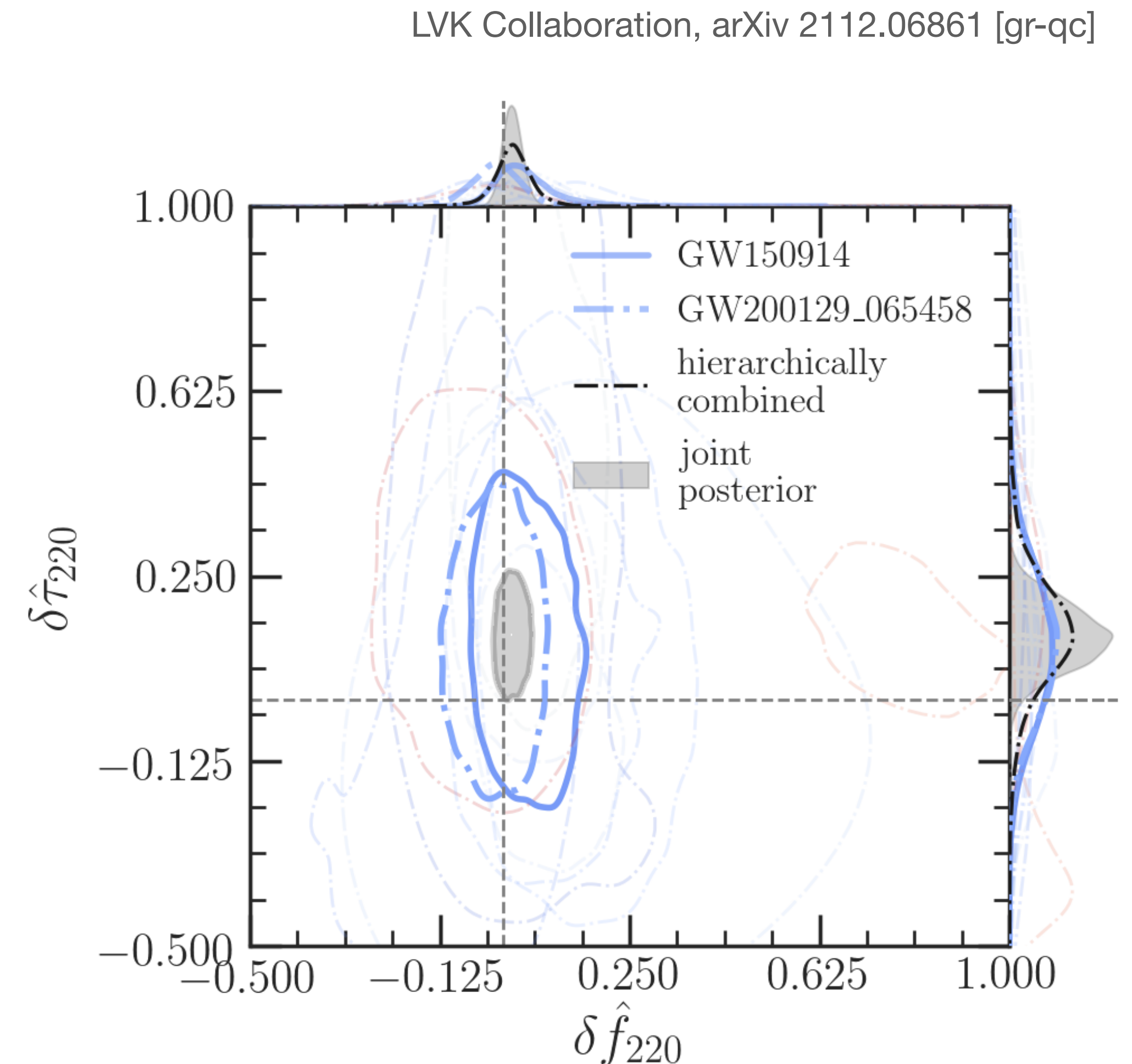
## pSEOBH

- Complementary to ringdown analyses focussing only on post-merger signal, ringdown start time is in-built in the model
- Introduce fractional deviations in the frequency and damping time of least-damped dominant QNM in the IMR model SEOBNRv4HM

$$f_{220} = f_{220}(1 + \delta\hat{f}_{220})$$

$$\tau_{220} = \tau_{220}(1 + \delta\hat{\tau}_{220})$$

- Possible issues:
  - Known degeneracies between deviation parameters and source parameters
  - Choice of priors
  - Impact of noise

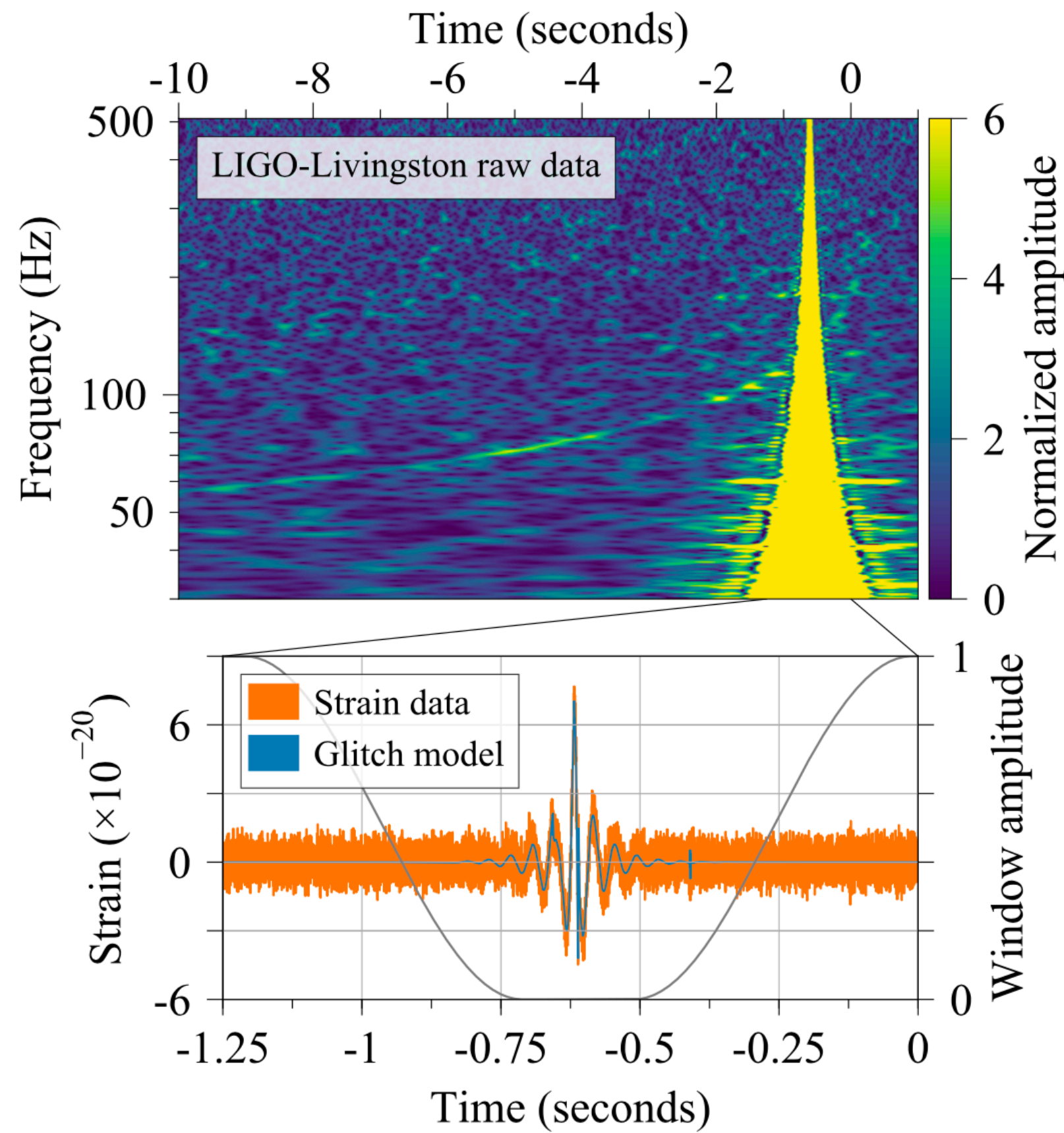




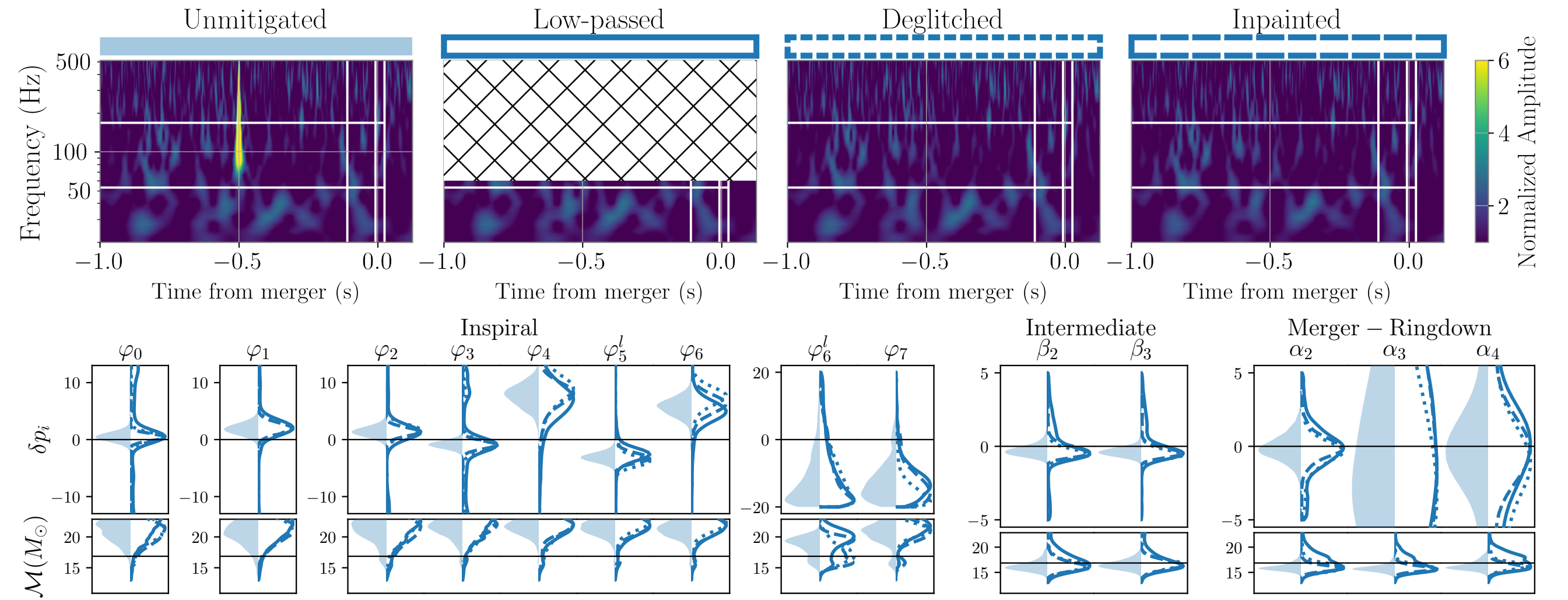
# Practical challenges in TGR: a recap

- Phenomenological parametrization chosen to describe beyond-GR effects and its degeneracies to source parameters
- Non-trivial choice of priors for theory-agnostic models
- Gaussian noise fluctuations expected to impact a fraction of the events: different combination methods might be less/more sensitive to this
- For template-based tests, missing physics might also mimic GR violations .
- Detector data can be affected by glitches which can mimic deviations from GR
  - Kwok et al. arXiv:2109.07642v3 studied the effect of glitches and mitigated glitches on tests of GR, by injecting PhenomPv2 waveforms into H1-L1-V1 at times when all three detectors are operating and a glitch is affecting either H1 or L1

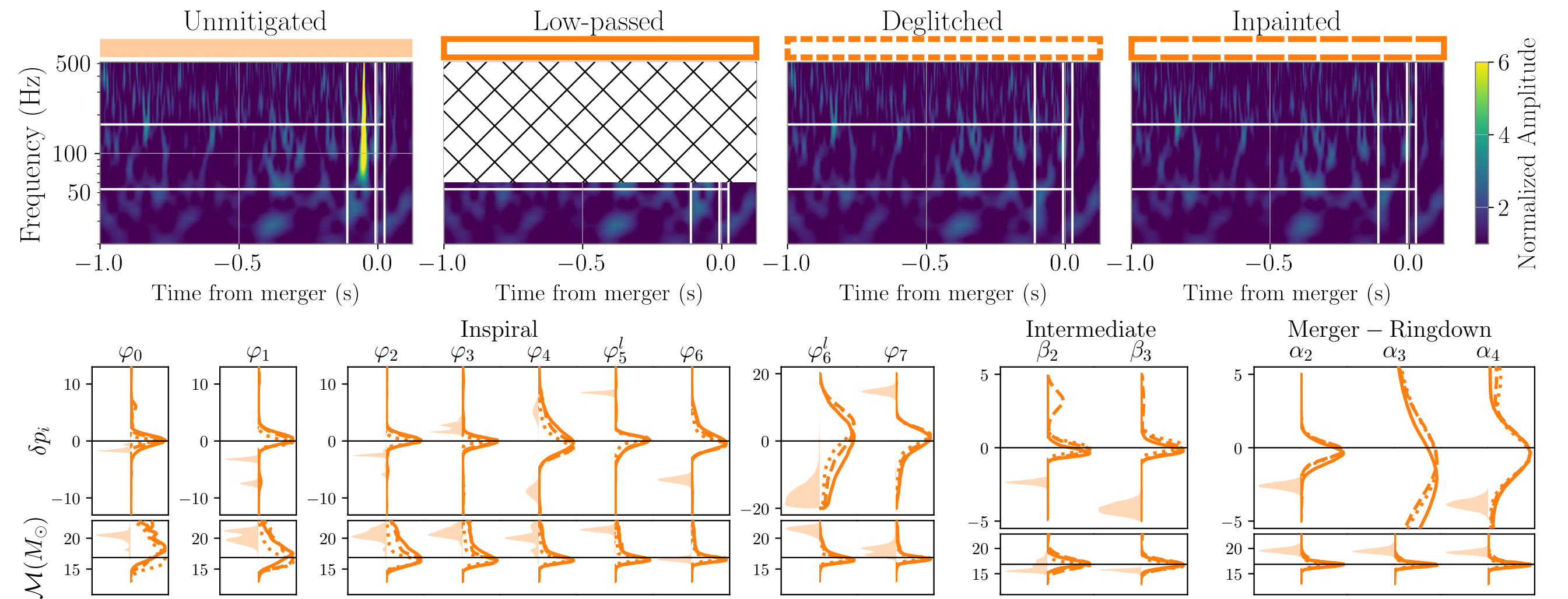
# What if there is a glitch?



The blip glitch affecting L1 data for GW170817.  
From: LIGO-Virgo 119 161101 (2017)



(a) Simulated GW190828\_065509-like signal overlapped with a H1 blip glitch at inspiral stage in the time domain.



(b) Simulated GW190828\_065509-like signal overlapped with a H1 blip glitch at intermediate stage in the time domain.

# Conclusions

- Current 2G detectors: training camp for tests of GR.
- Many subtleties which need to be addressed before more sensitive instruments become operational, which will drastically reduce statistical uncertainties.
- Further work on GR templates is required to allow unbiased tests based on them!
- Template banks of beyond-GR waveforms: a great tool to cross-check theory-agnostic results.