

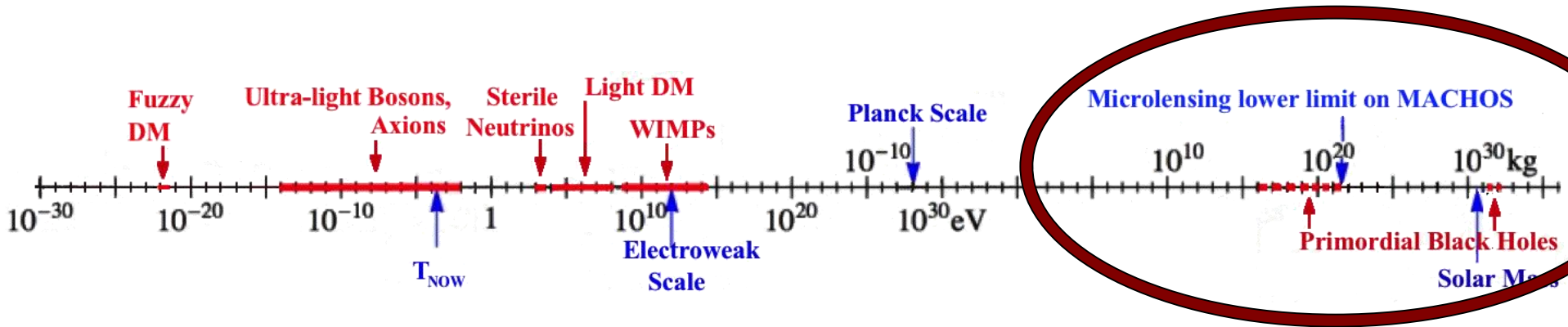
The background of the slide is a composite image. On the left, there is a view of Earth from space, showing the curvature of the planet and the dark void of space. The rest of the image is filled with a deep space scene featuring a bright galaxy in the center, surrounded by numerous stars. Overlaid on this scene is a complex network of purple and blue lines, representing a visualization of gravitational waves or spacetime curvature. In the upper right corner, there is a bright, multi-colored (green, blue, red) circular pattern, possibly representing a black hole or a specific gravitational event.

# Searching for Primordial Black Holes with Gravitational Waves

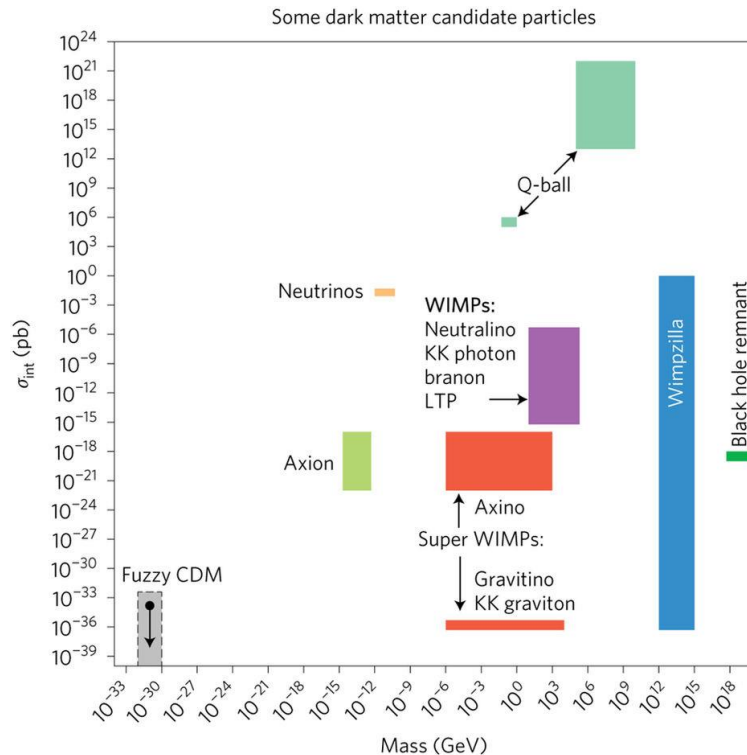
Iberian GW Meeting, Braga, 8<sup>th</sup> June 2022

Juan García-Bellido  
IFT-UAM/CSIC Madrid

# What is Dark Matter?



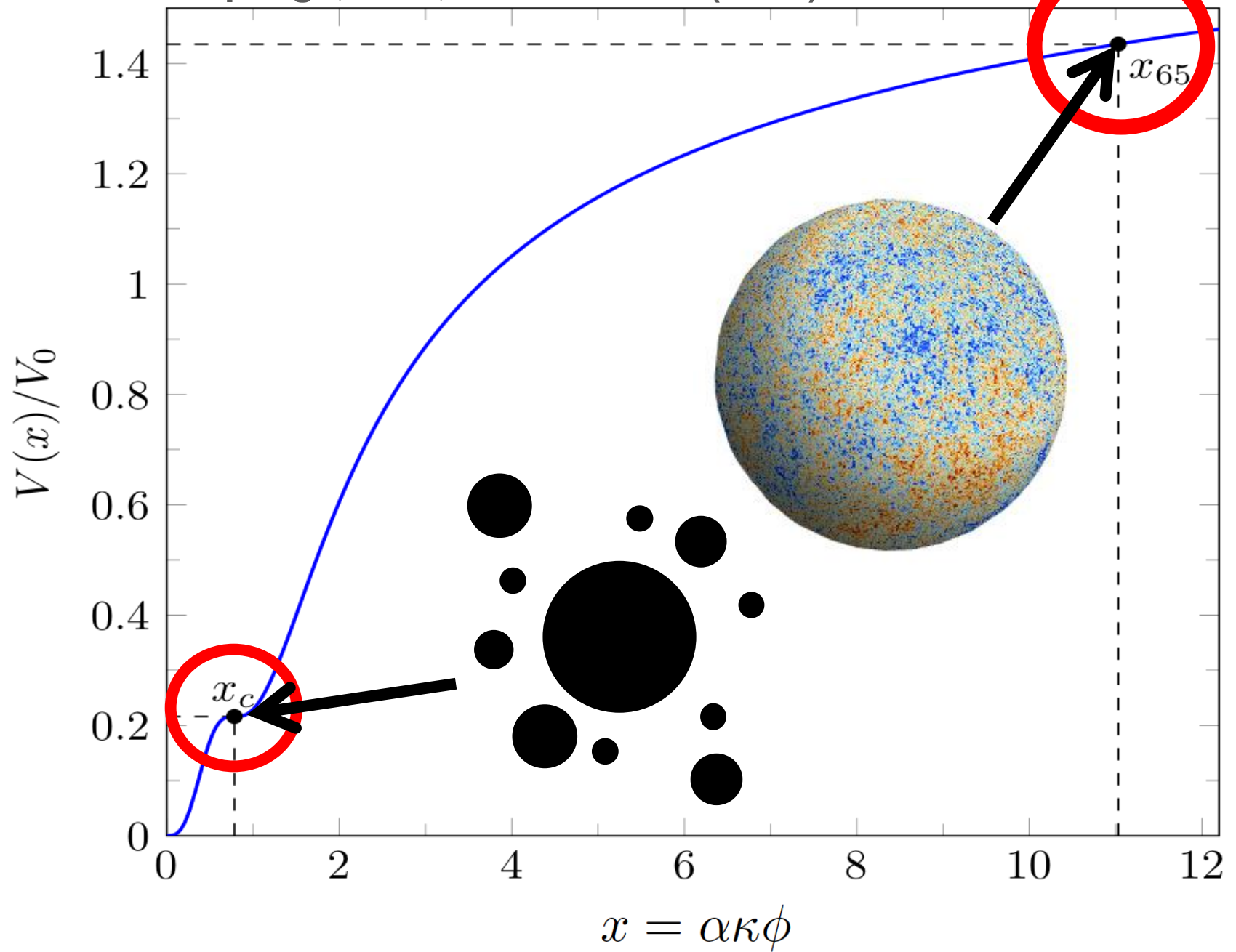
90 orders of magnitude in mass



80 orders of magnitude in strength

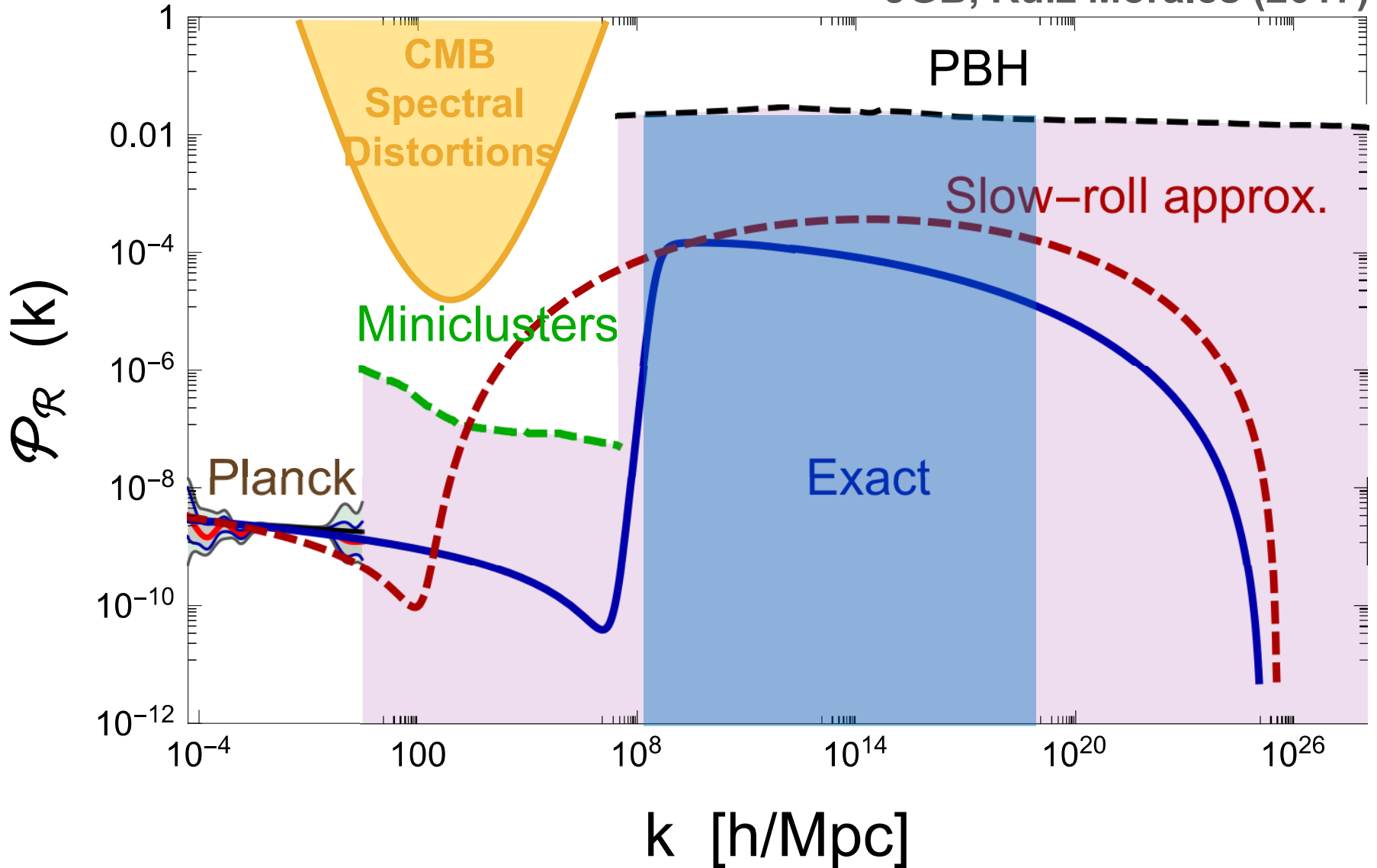


Ezquiaga, JGB, Ruiz Morales (2017)



# Primordial Spectrum PBH

JGB, Ruiz Morales (2017)



# Critical Higgs Inflation

## Standard Model Lagrangian

Ezquiaga, JGB, Ruiz Morales  
(2017)

$$\begin{aligned} \mathcal{L} = & -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} \\ & + i \bar{\psi} \not{D} \psi + h.c. \\ & + \bar{\psi}_i y_{ij} \psi_j \phi + h.c. \\ & + \frac{1}{2} \partial_\mu \phi^2 - V(\phi) \\ & + \sum |\phi|^2 R \end{aligned}$$

$$S = \int d^4x \sqrt{g} \left[ \left( \frac{1}{2\kappa^2} + \frac{\xi(\phi)}{2} \phi^2 \right) R - \frac{1}{2} (\partial\phi)^2 - \frac{1}{4} \lambda(\phi) \phi^4 \right]$$

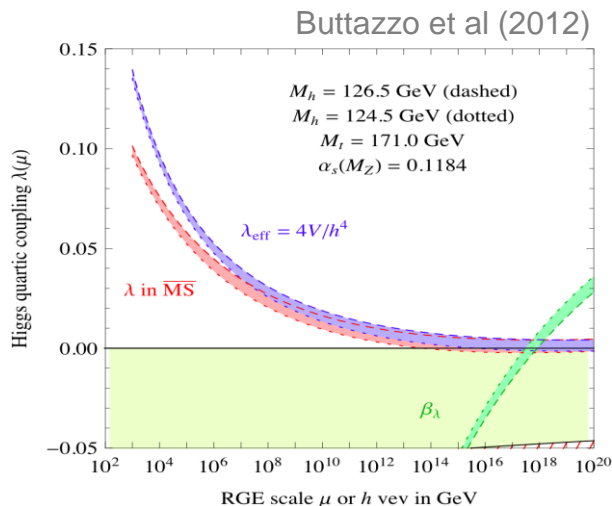
$$\lambda(\phi) = \lambda_0 + b_\lambda \ln^2(\phi/\mu),$$

$$\xi(\phi) = \xi_0 + b_\xi \ln(\phi/\mu),$$

$$\frac{d\phi}{d\phi} = \frac{\sqrt{1 + \xi(\phi) \phi^2 + 6 \phi^2 (\xi(\phi) + \phi \xi'(\phi)/2)^2}}{1 + \xi(\phi) \phi^2}$$

$$V(x) = \frac{V_0 (1 + a \ln^2 x) x^4}{(1 + c(1 + b \ln x) x^2)^2} \quad x = \phi/\mu$$

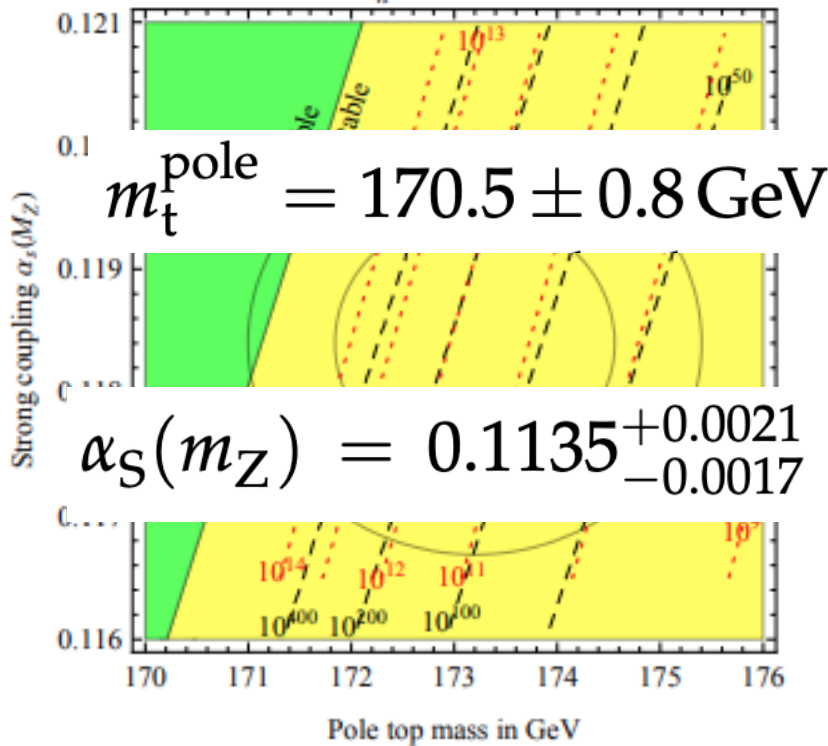
$$V_0 = \lambda_0 \mu^4 / 4, \quad a = b_\lambda / \lambda_0, \quad b = b_\xi / \xi_0 \quad \text{and} \quad c = \xi_0 \kappa^2 \mu^2$$



# EW vacuum meta-stability

Buttazzo et al.  
(2012)

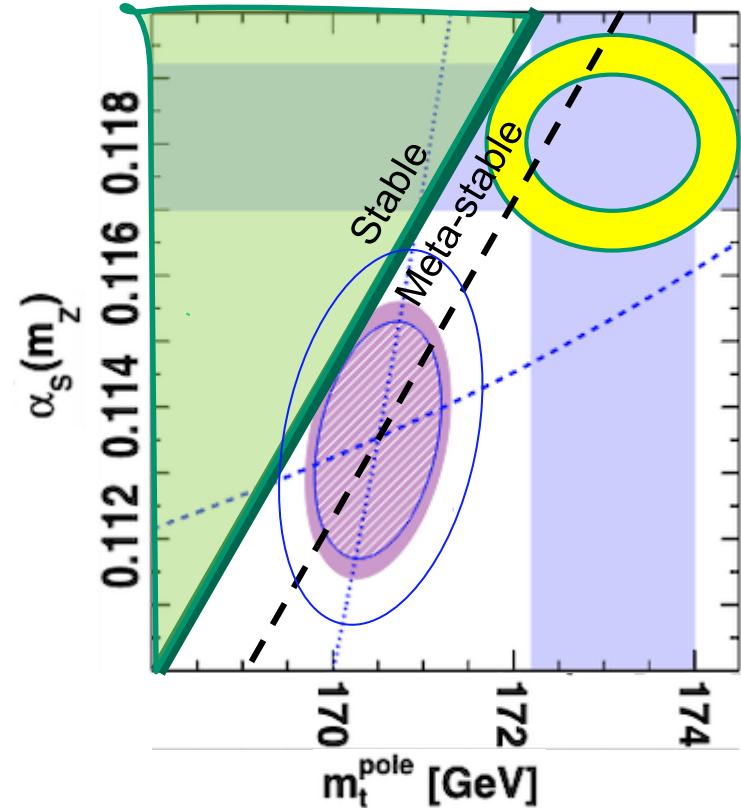
$m_h = 126 \text{ GeV}$



<https://arxiv.org/pdf/1112.3022.pdf>

CMS Collab. (2020)

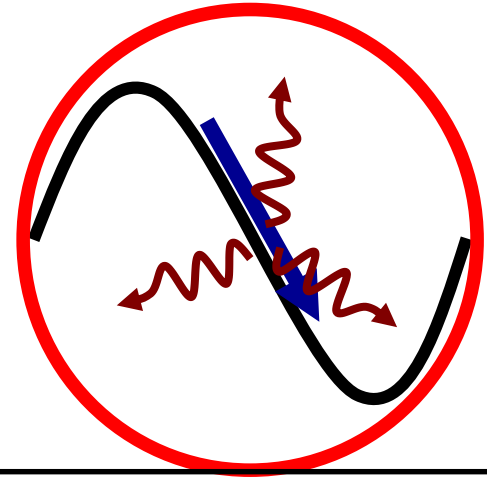
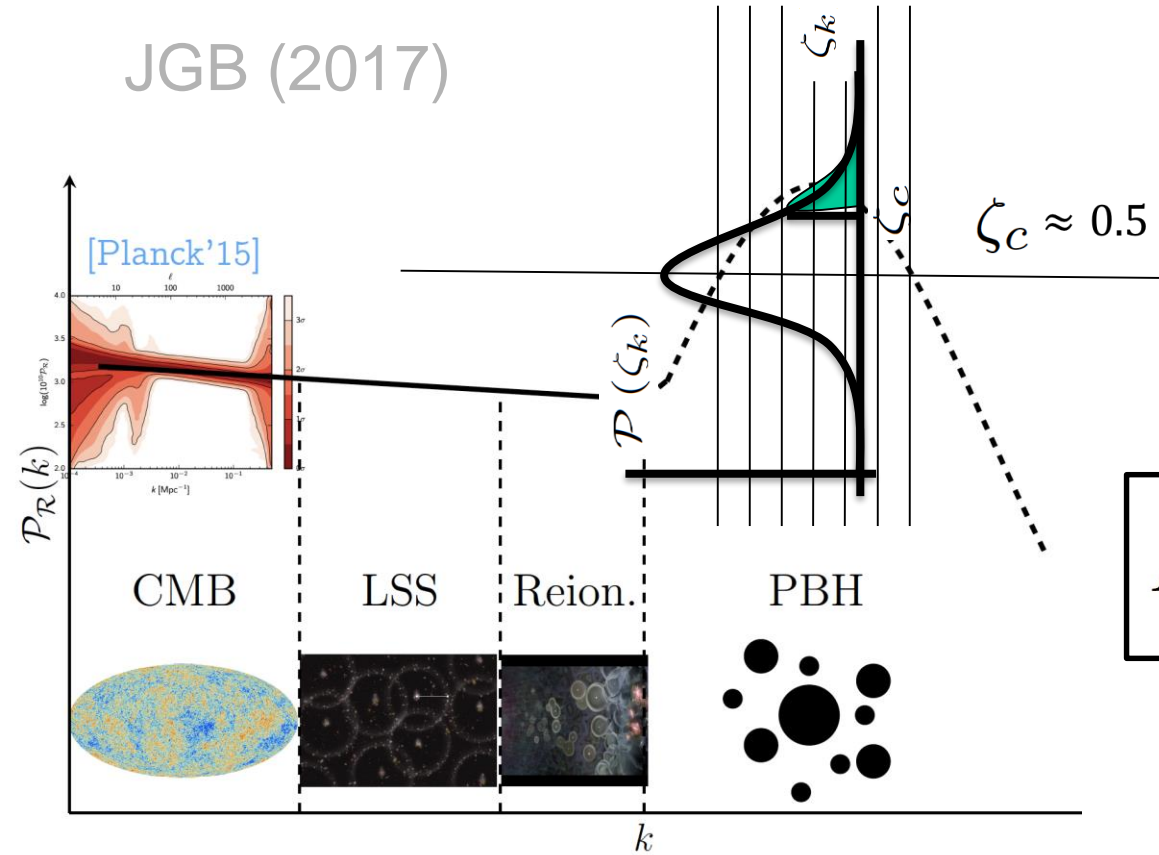
$m_h = 125.5 \text{ GeV}$



<https://arxiv.org/abs/1904.05237>

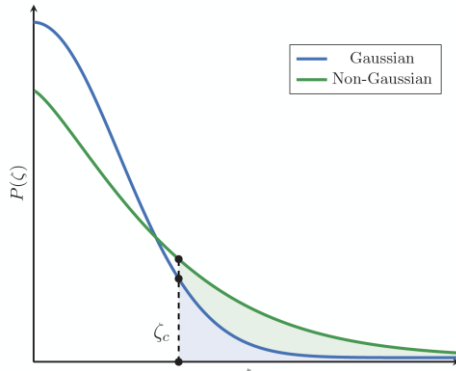
# Gravitational Collapse of PBH

JGB (2017)



$$M_{\text{PBH}} \simeq 30 M_{\odot} e^{2(N-36)}$$

$$\beta^{\text{form}}(M_k) = \int_{\zeta_c}^{\infty} \mathcal{P}(\zeta_k) d\zeta_k$$



$$\beta(N) = \begin{cases} \text{Erfc} \left( \frac{\zeta_c}{\sqrt{2P_{\zeta}(N)}} \right), & \text{Gaussian statistics,} \\ \text{Erfc} \left( \sqrt{\frac{1}{2} + \frac{\zeta_c}{\sqrt{2P_{\zeta}(N)}}} \right), & \chi^2 \text{ statistics} \end{cases}$$



# Stochastic $\delta N$ - formalism

## Coarse-grained curvature perturbation

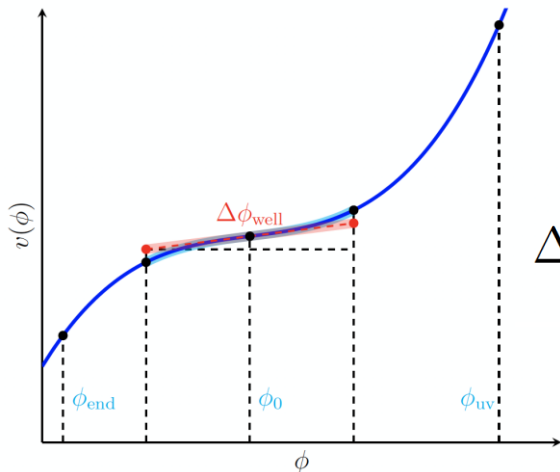
$$ds^2 = -dt^2 + a^2(t)e^{2\zeta(t, \mathbf{x})} \delta_{ij} dx^i dx^j \quad \zeta_{\text{cg}}(\mathbf{x}) = \delta N_{\text{cg}}(\mathbf{x}) = \mathcal{N}(\mathbf{x}) - \langle \mathcal{N} \rangle$$

$$\frac{1}{M_{\text{pl}}^2} \frac{d}{d\mathcal{N}} P_{\Phi}(\mathcal{N}) = \left( - \sum_i \frac{v_{\phi_i}}{v} \frac{\partial}{\partial \phi_i} + v \sum_i \frac{\partial^2}{\partial \phi_i^2} \right) \cdot P_{\Phi}(\mathcal{N}) \quad \text{Fokker-Planck Diffusion Eq.}$$

Determined by the poles of the characteristic function

$$P_{\phi}(\mathcal{N}) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{-it\mathcal{N}} \chi_{\mathcal{N}}(t, \phi) dt = \sum_n a_n(\phi) e^{-\Lambda_n \mathcal{N}}$$

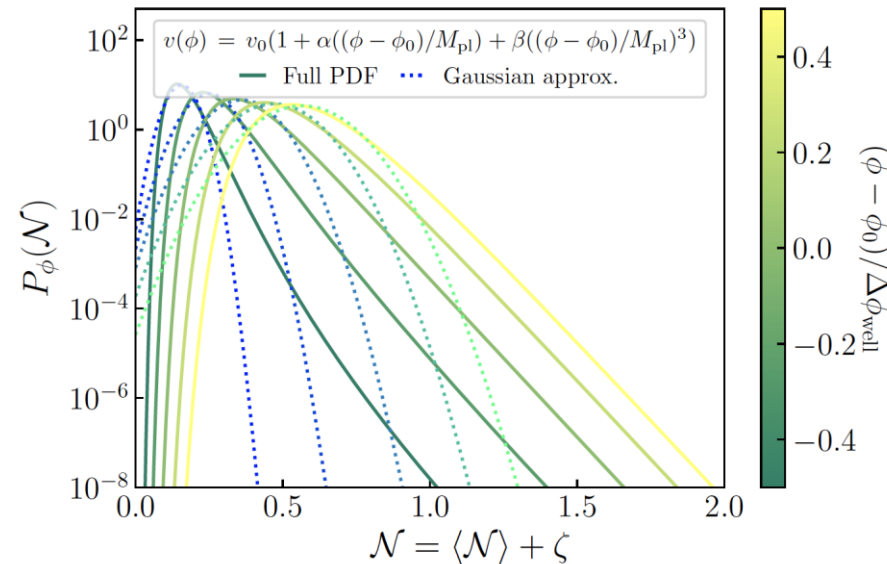
$$\chi_{\mathcal{N}}(t, \phi) = \sum_n \frac{a_n(\phi)}{\Lambda_n - it} + \text{regular func.}$$



$$\alpha \gg (v_0^2 \beta)^{1/3}$$

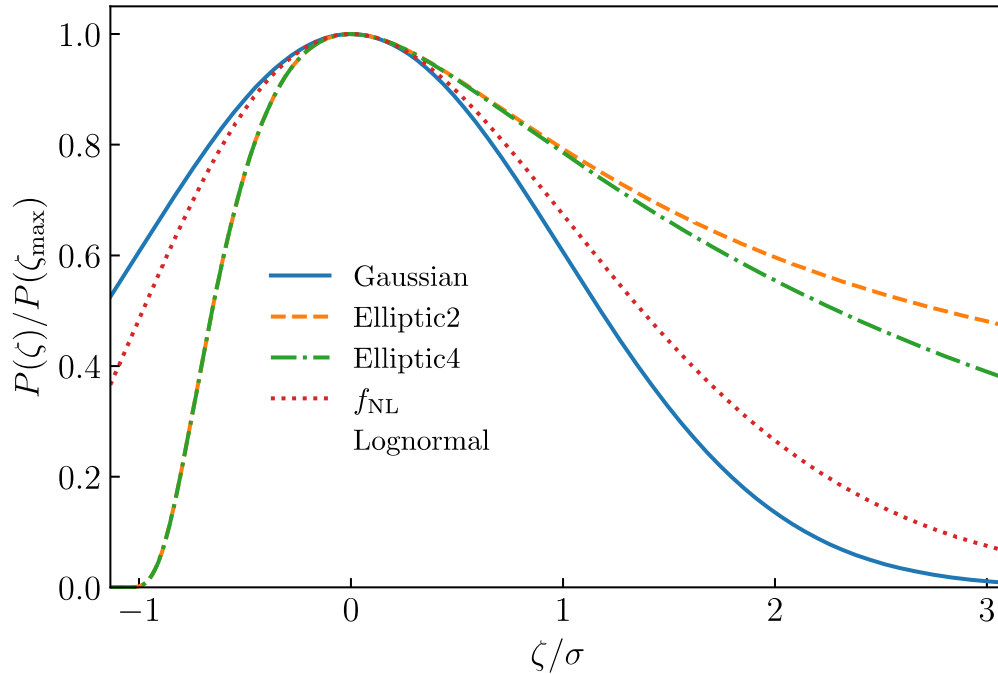
$$\Delta\phi_{\text{well}} \simeq 2M_{\text{pl}} \sqrt{\frac{\alpha}{3\beta}}$$

Ezquiaga, JGB, Vennin (2019)



# Quantum Diffusion @ CMB & LSS

Ezquiaga, JGB, Vennin (2022)



$$P_2(\zeta_k) = -\frac{\pi}{2\mu^2} \vartheta'_2 \left( \frac{\pi\alpha_k}{2}, e^{-\frac{\pi^2}{\mu^2} \mathcal{N}_k} \right)$$

$$P_4(\zeta_k) = \frac{\pi}{2\mu^2\alpha_k} \vartheta'_4 \left( \frac{\pi\alpha_k}{2}, e^{-\frac{\pi^2}{\mu^2} \mathcal{N}_k} \right)$$

$$\zeta(x) = \zeta_G(x) + \frac{3}{5} f_{\text{NL}} \left[ \zeta_G^2(x) - \sigma_G^2(x) \right]$$

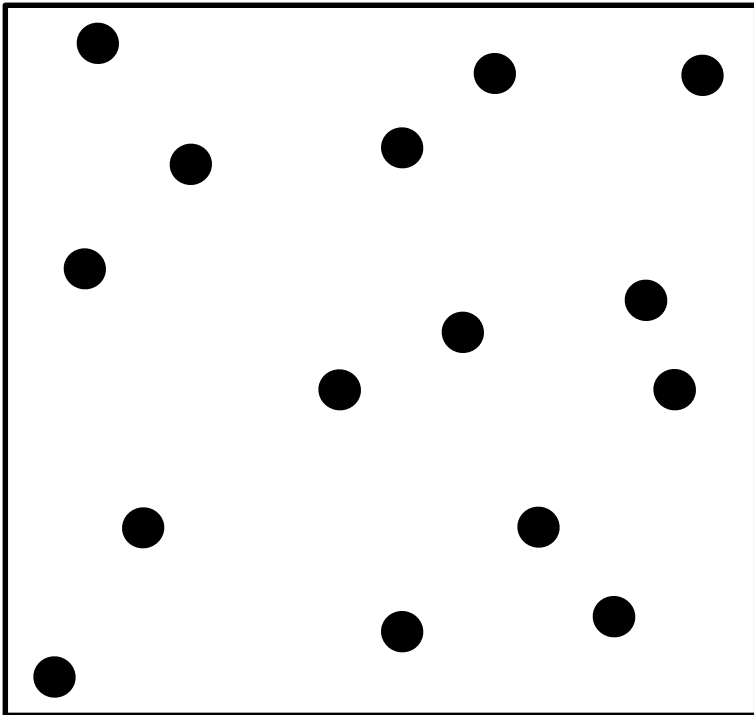
$$\text{LN}(x, \rho, \sigma) = \frac{1}{\rho\sigma\sqrt{2\pi}} \exp \left[ -\frac{\ln(x/\rho)^2}{2\sigma^2} - \frac{\sigma^2}{2} \right]$$

$$P_{\text{NL}}(\zeta) = \frac{1}{\sqrt{2\pi\sigma_G^2\Delta}} \left[ e^{-\frac{25(\sqrt{\Delta}-1)^2}{72f_{\text{NL}}^2\sigma_G^2}} + e^{-\frac{25(\sqrt{\Delta}+1)^2}{72f_{\text{NL}}^2\sigma_G^2}} \right]$$

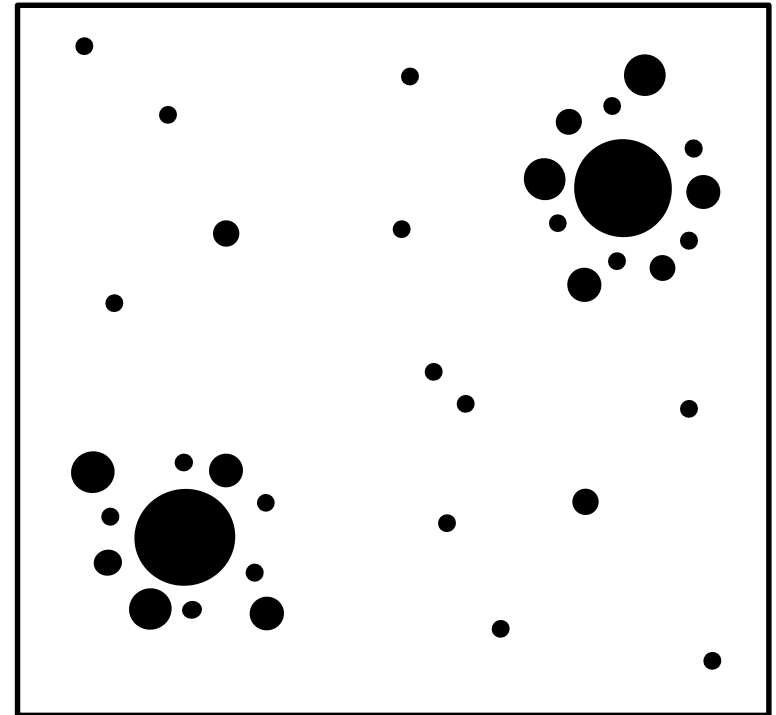
$$G(x, \rho, \sigma_G) = \frac{1}{\sigma_G\sqrt{2\pi}} \exp \left[ -\frac{(x-\rho)^2}{2\sigma_G^2} \right]$$

where  $\Delta(\zeta) = 1 + \frac{12}{5} f_{\text{NL}}\zeta + \frac{36}{25} f_{\text{NL}}^2\sigma_G^2$ .

# Spatial Distribution PBH



- Monochromatic
- Uniformly distributed



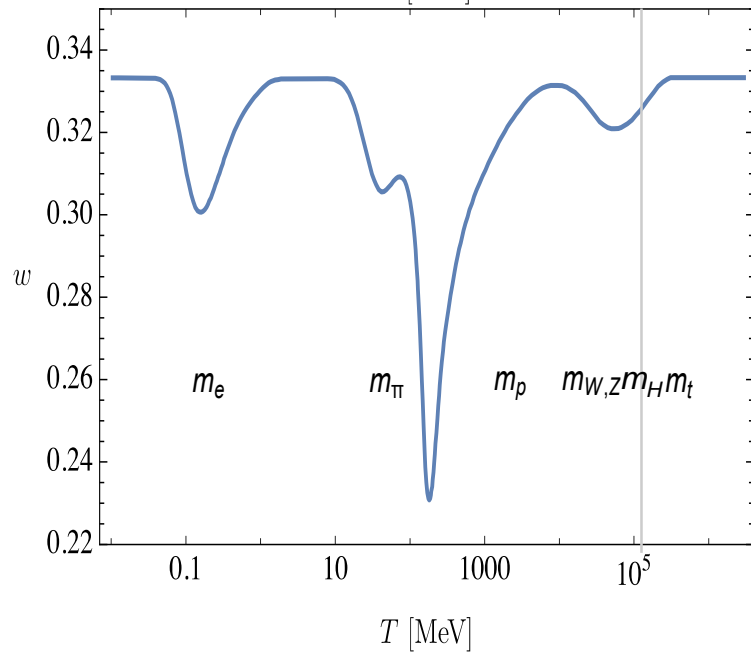
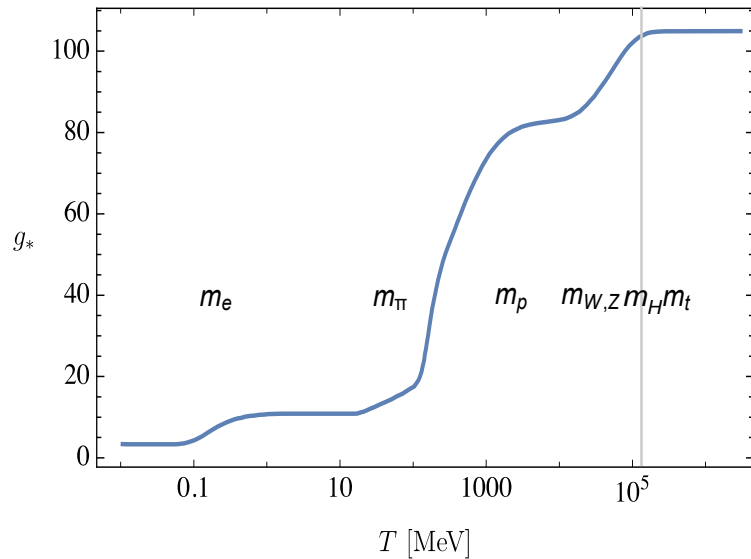
- Broad range masses
- PBH clusters



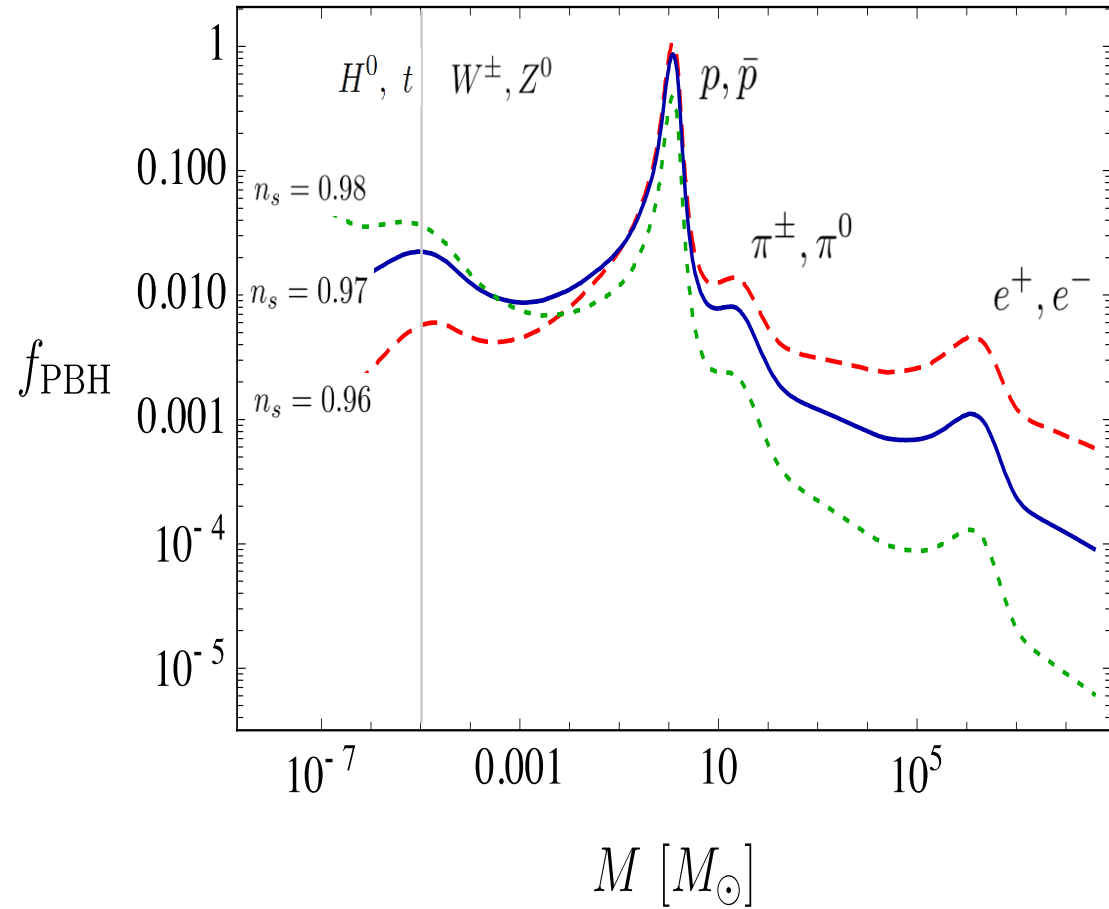
JGB (2017)

# Thermal history of the universe

Carr, Clesse, JGB, Kühnel (2019)



## PBH mass spectrum



# Electroweak baryogenesis @ QCD

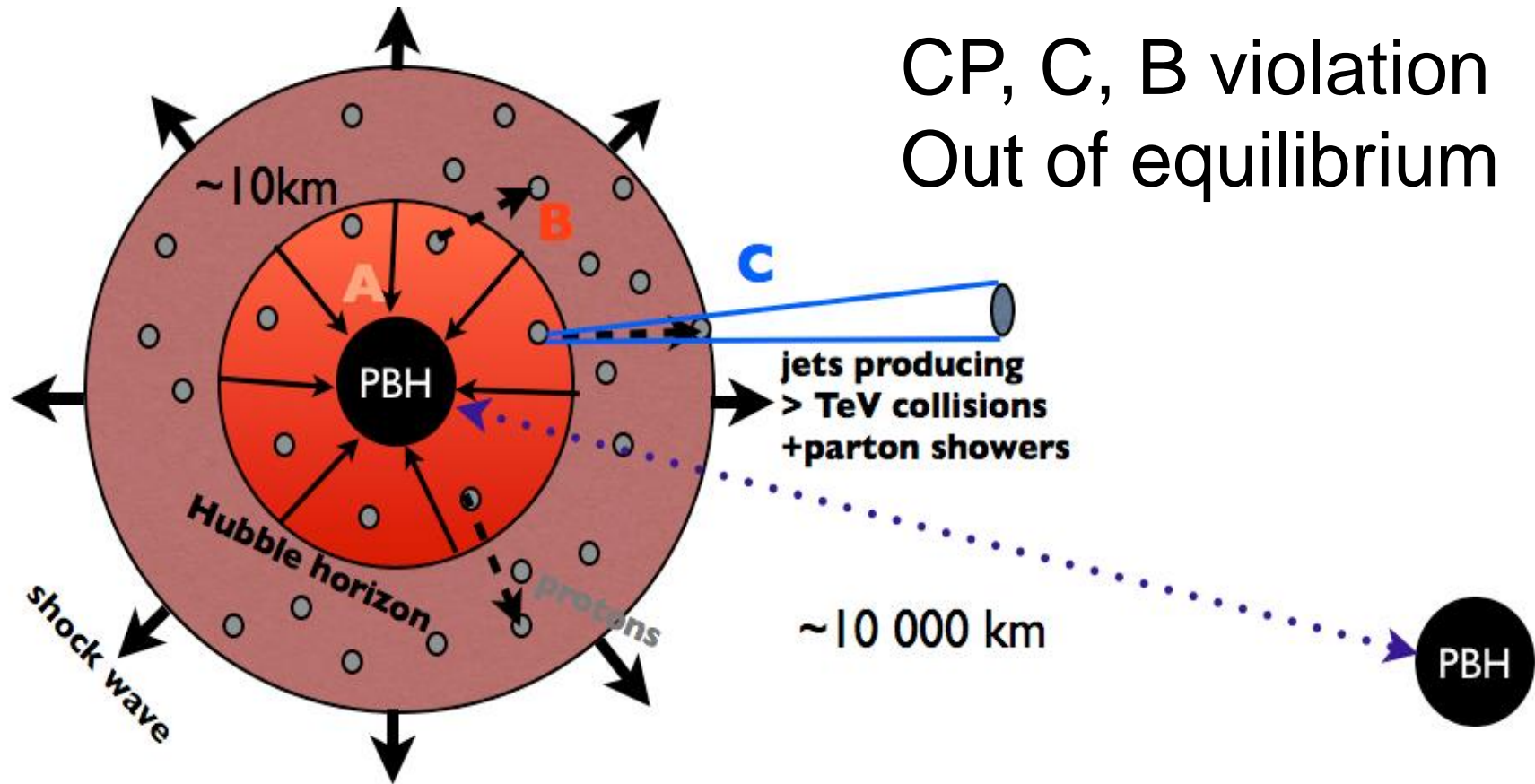
## “Primordial supernova”

JGB, Carr, Clesse (2019)

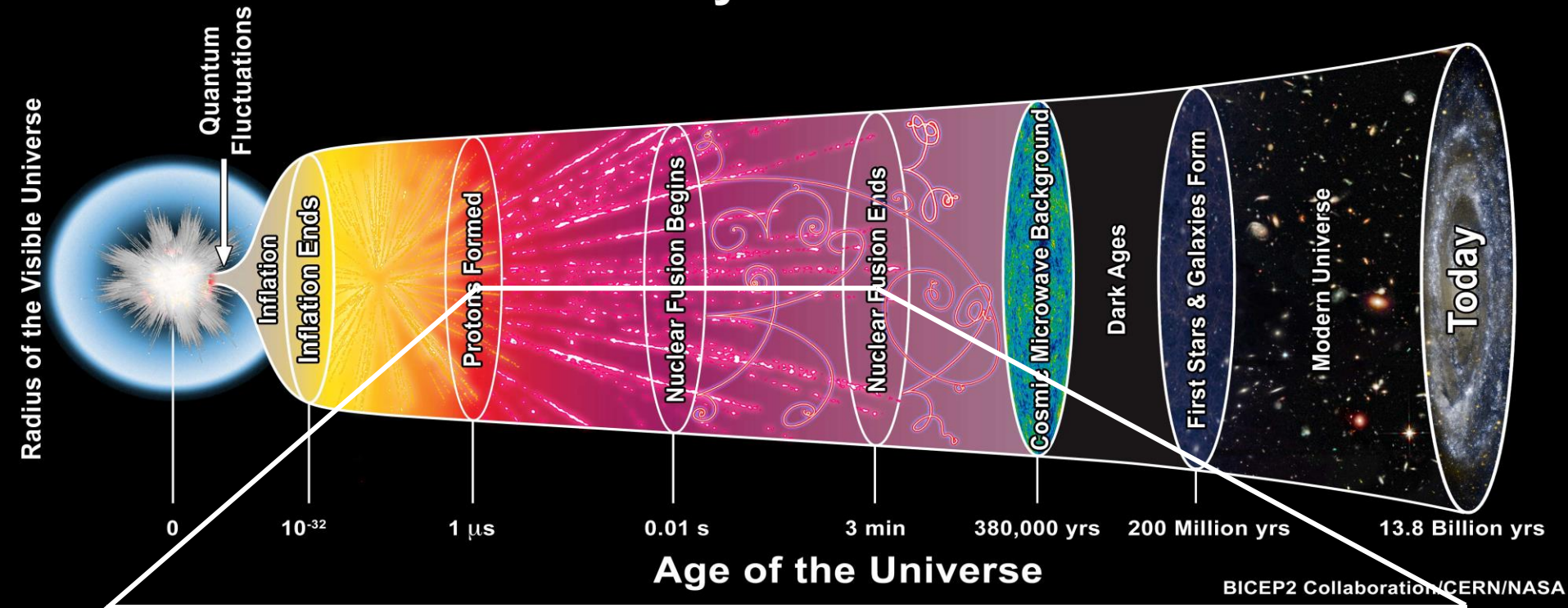
Sakharov conditions:

CP, C, B violation

Out of equilibrium



# History of the Universe



JGB  
(2019)

PBH=DM  
collapse

Baryogenesis

Nucleosynthesis

quark-hadron  
transition

hot-spot  
EWB

baryon  
dilution

light  
elements

200 MeV

100 MeV

10 MeV

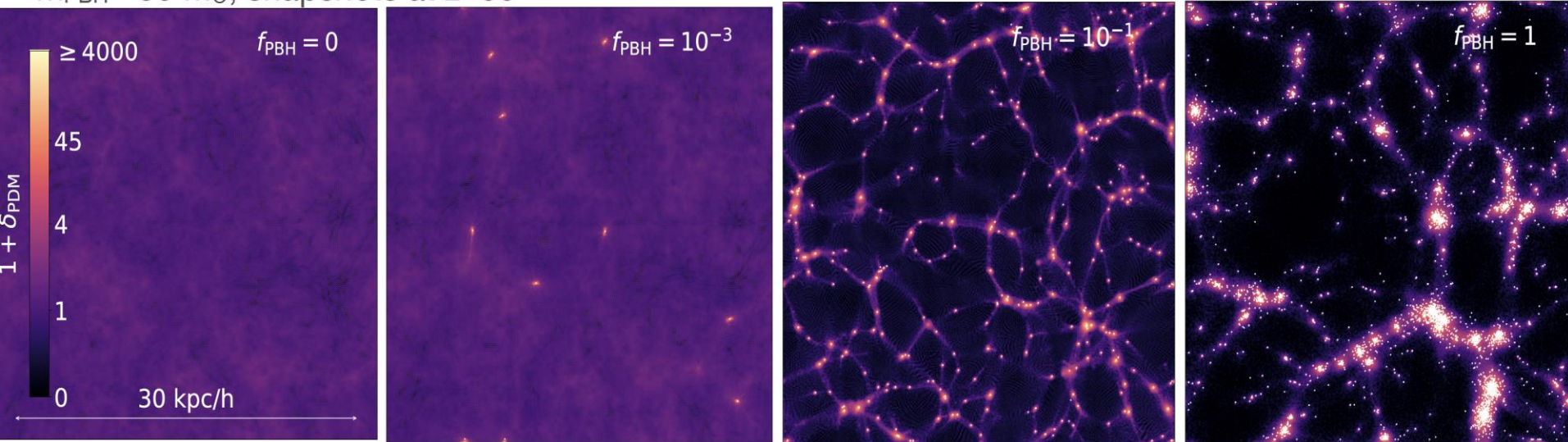
1 MeV

# Can (stellar-mass) PBHs be the dark matter?

## Poisson in a PBH sea...

N-body simulations by Inman & Ali-Haimoud, 1907.08129

$m_{\text{PBH}} = 30 M_{\odot}$ , snapshots at  $z=99$

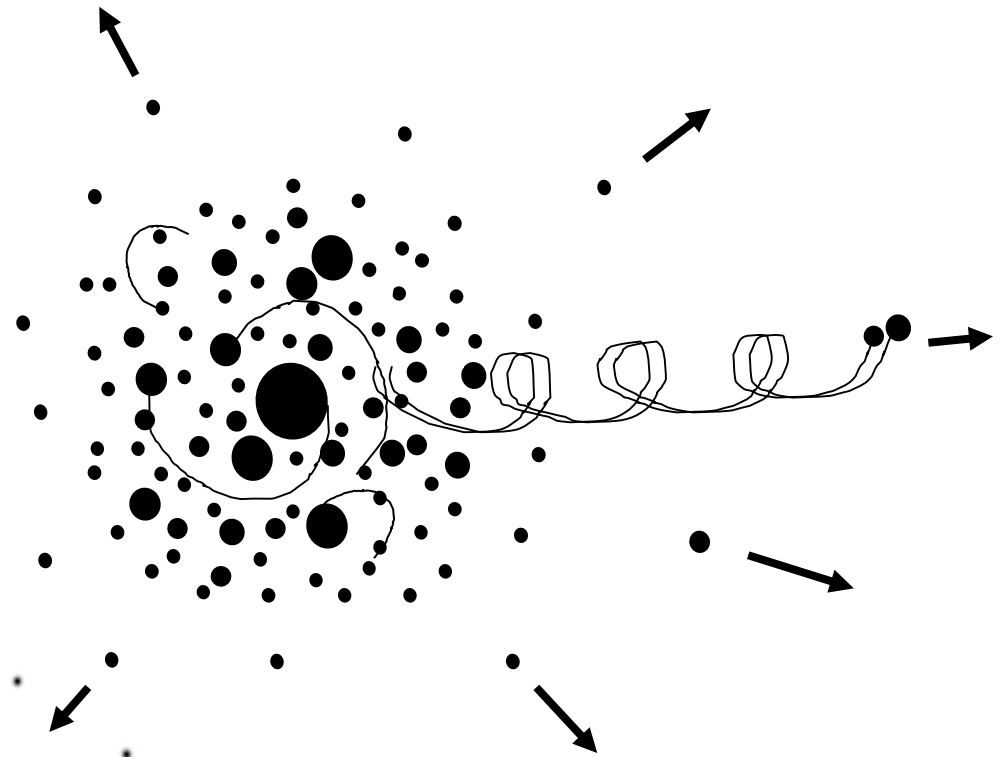
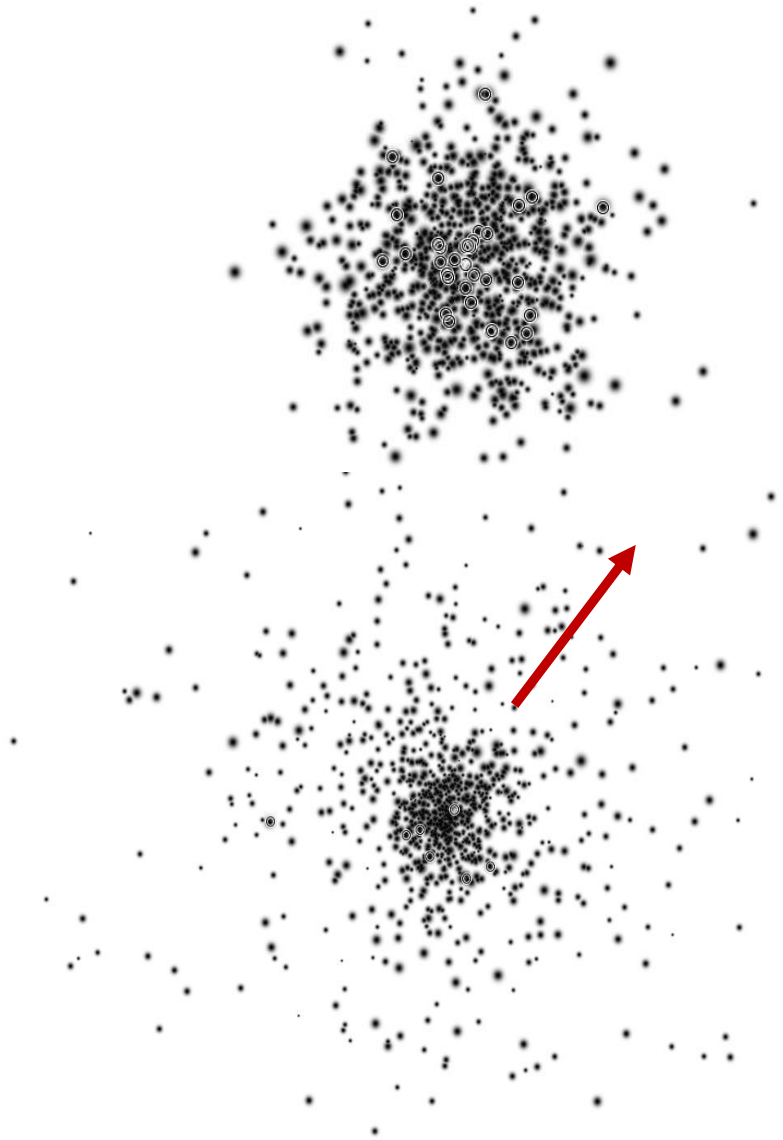


Halos of  $10^6 - 10^7 M_{\odot}$

On small scales, completely different than particle-CDM !  
 Potential implications for 21cm, recombination, etc... [Hasinger+20]

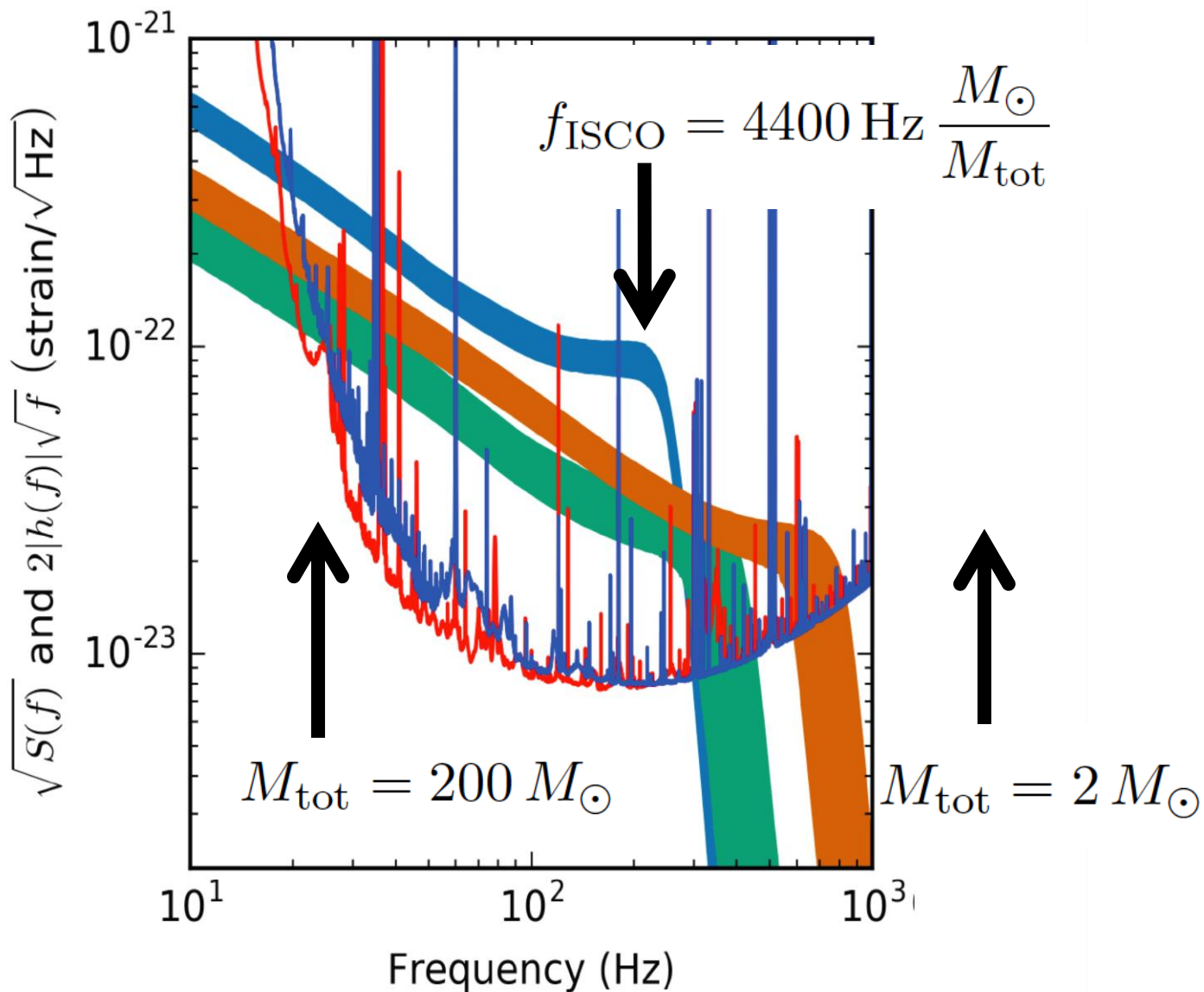
# PBH clusters

Trashorras , JGB, Nesseris (2020)

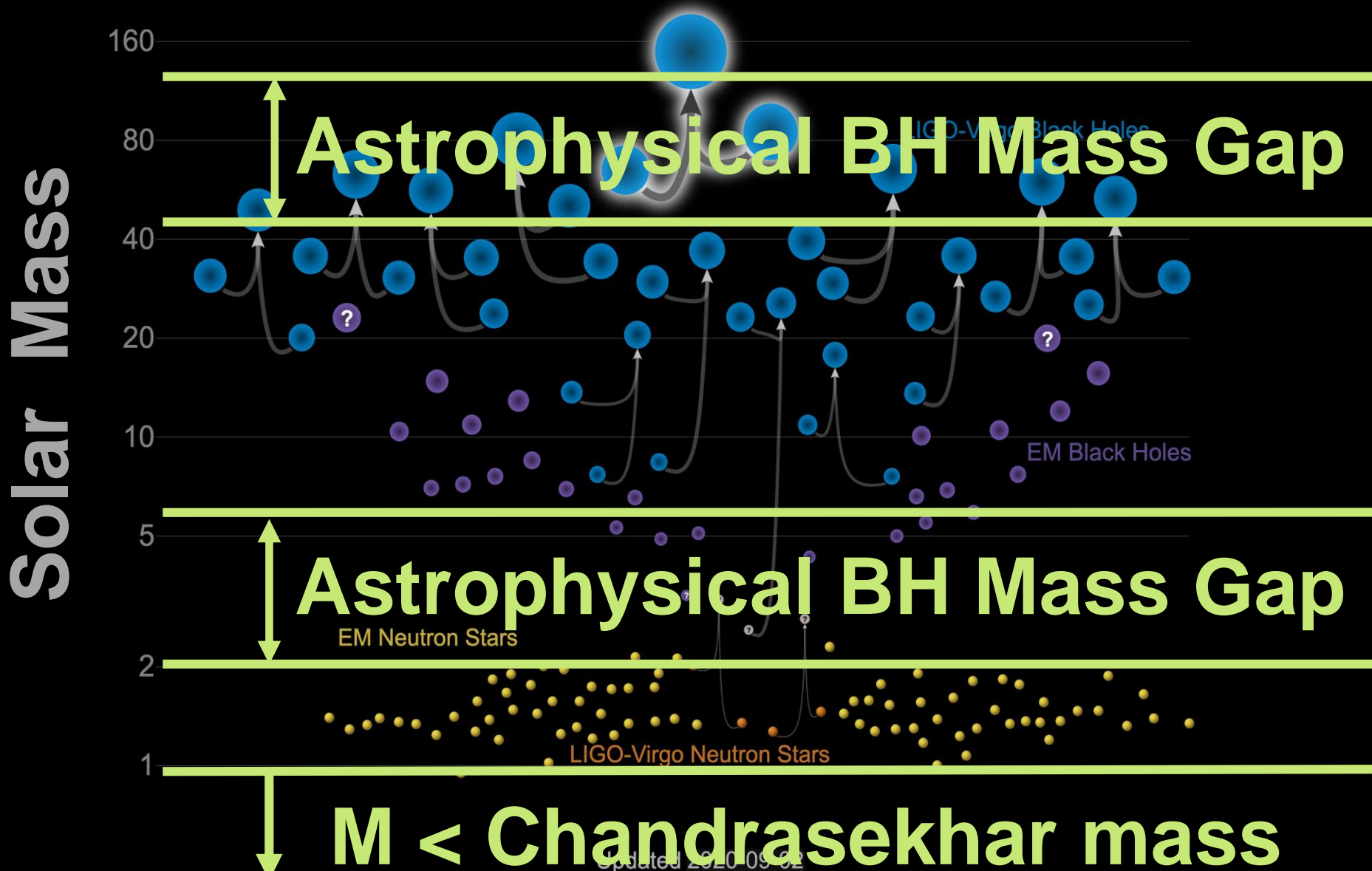




# LVC BBH events

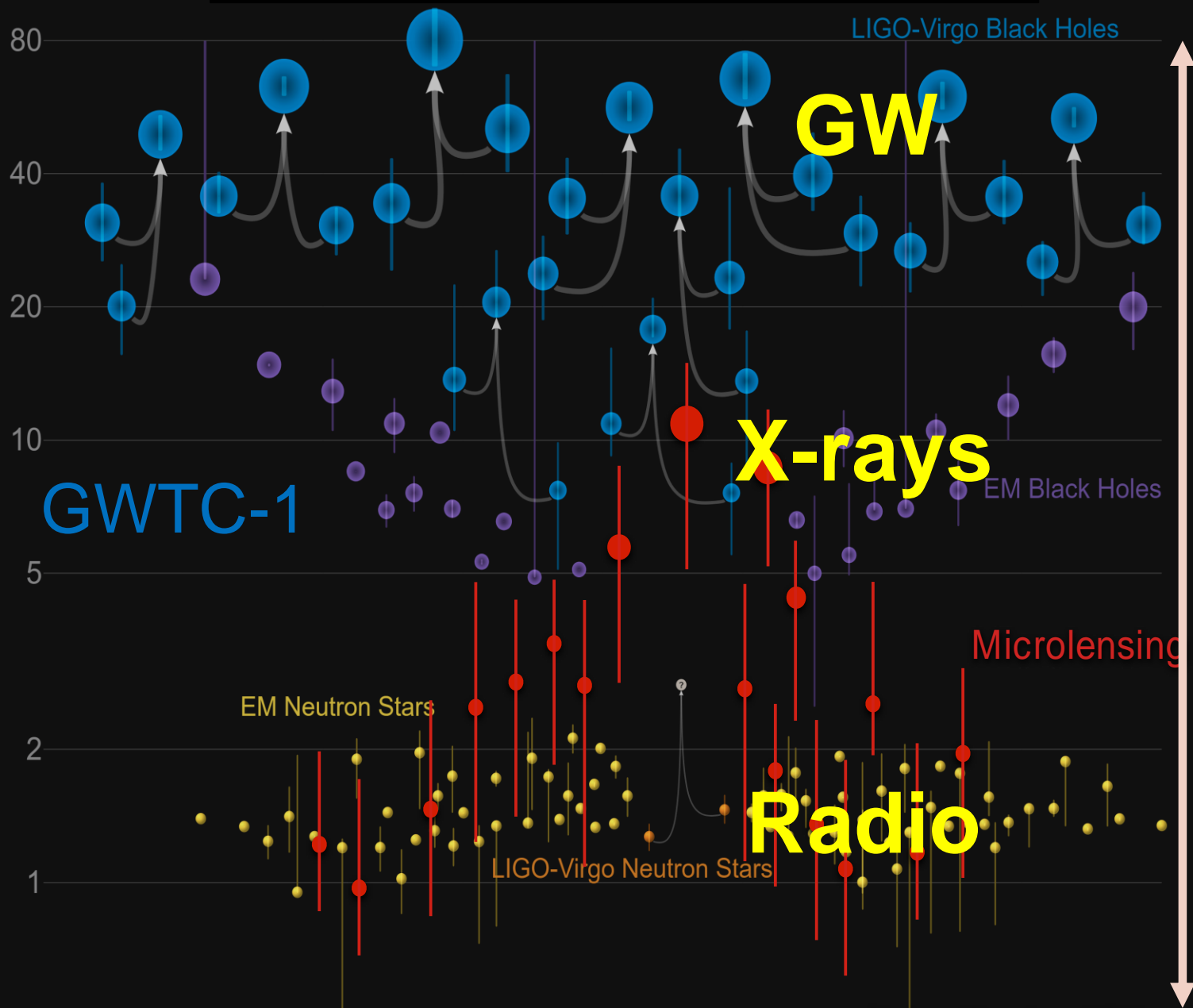


# Black Holes and Neutron Stars



# Black Holes and Neutron Stars

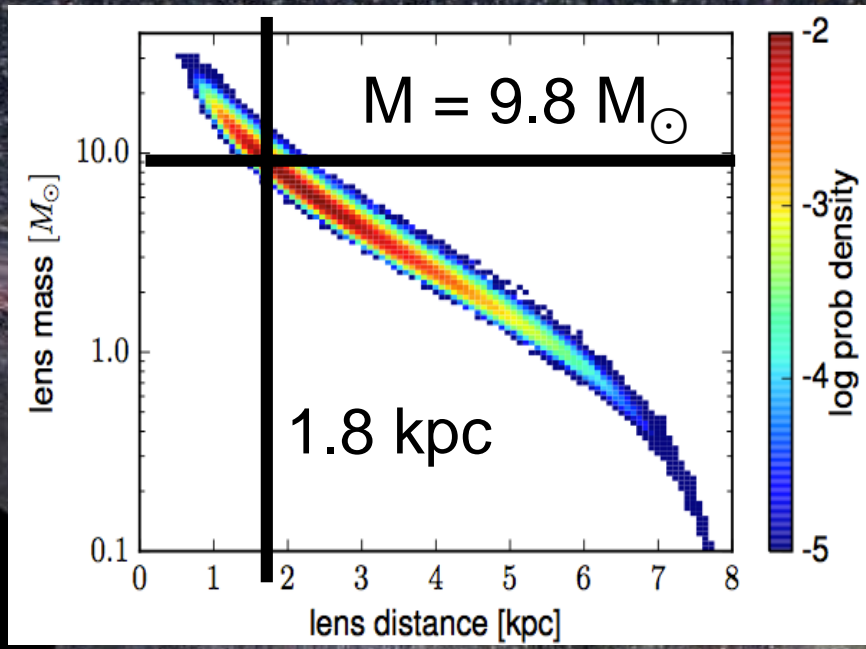
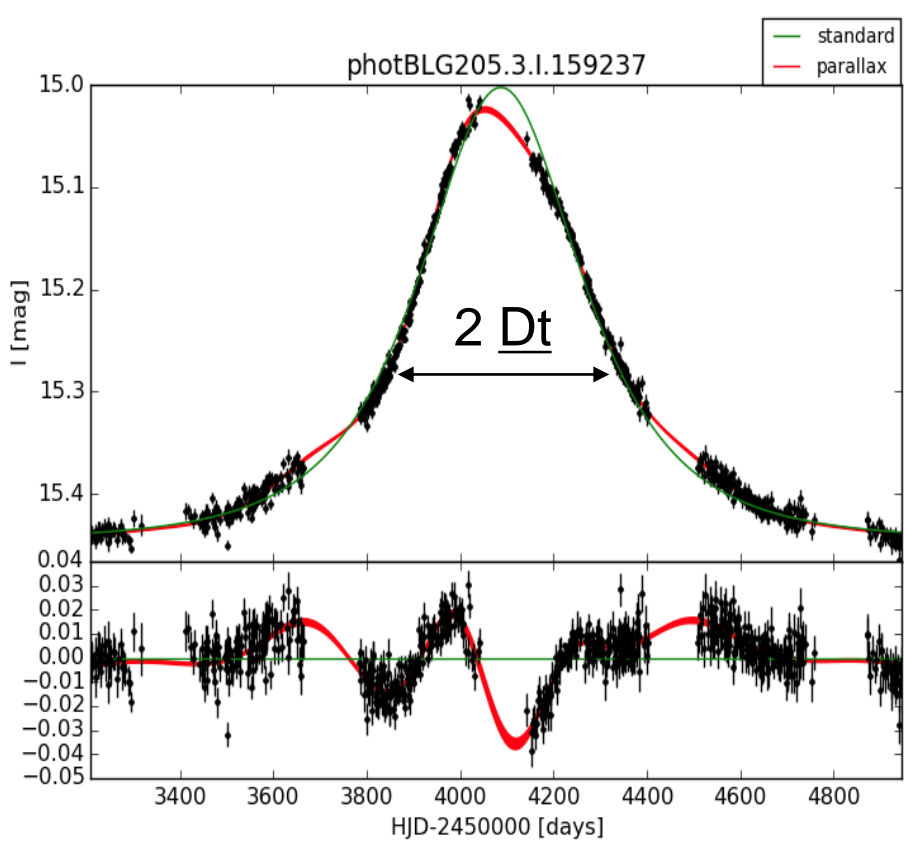
Solar Mass



Microlensing

# OGLE3-UL-PAR-02 - candidate BH

Wyrzykowski (2016)



OGLE photometry  
from 2001-2008  
and microlensing model



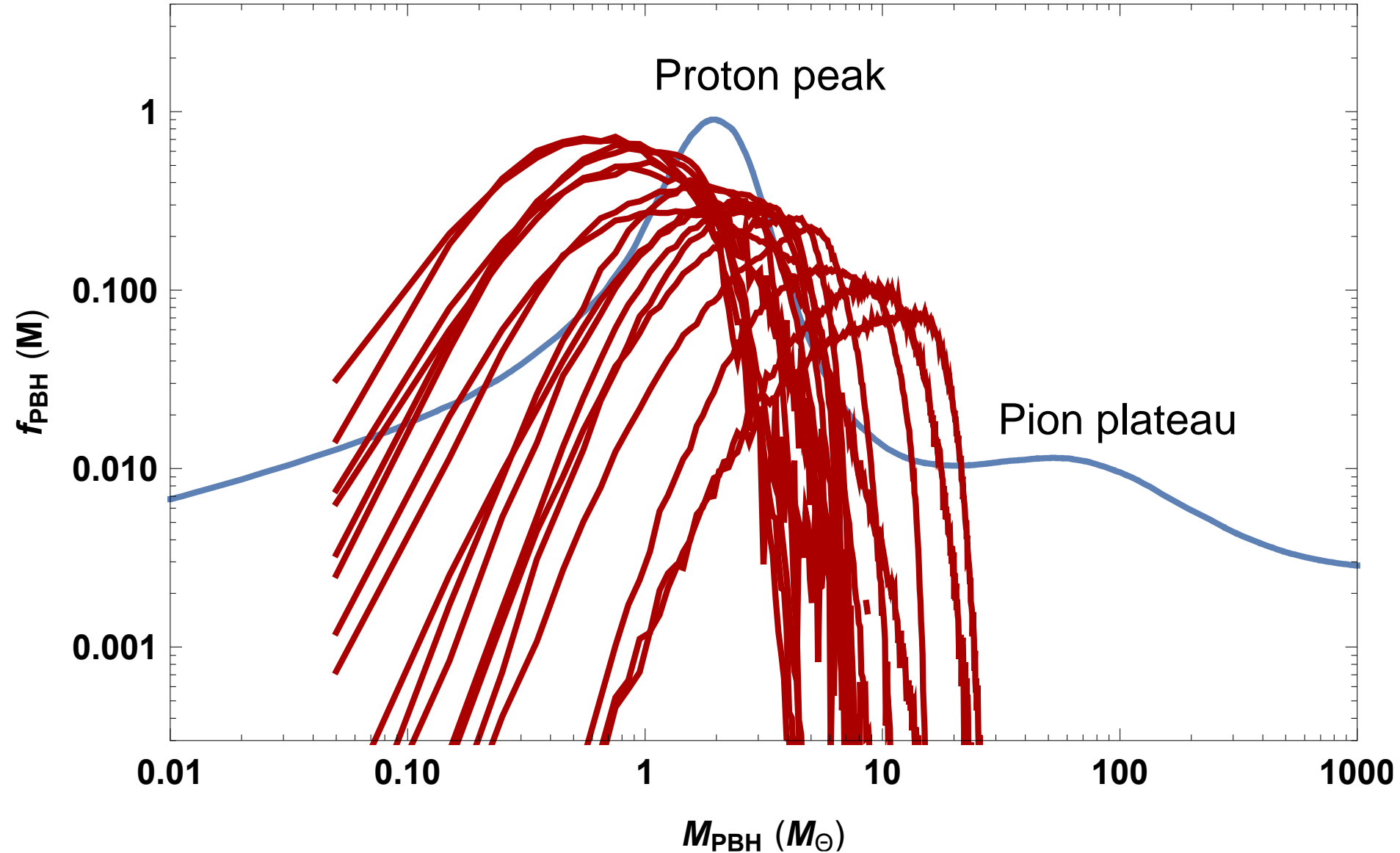
$$\underline{Dt} = \frac{r_E}{v} = \frac{\sqrt{4GM_D d}}{v}$$

**Mass, Distance** (degenerated estimate)

# Primordial Black Holes & OGLE

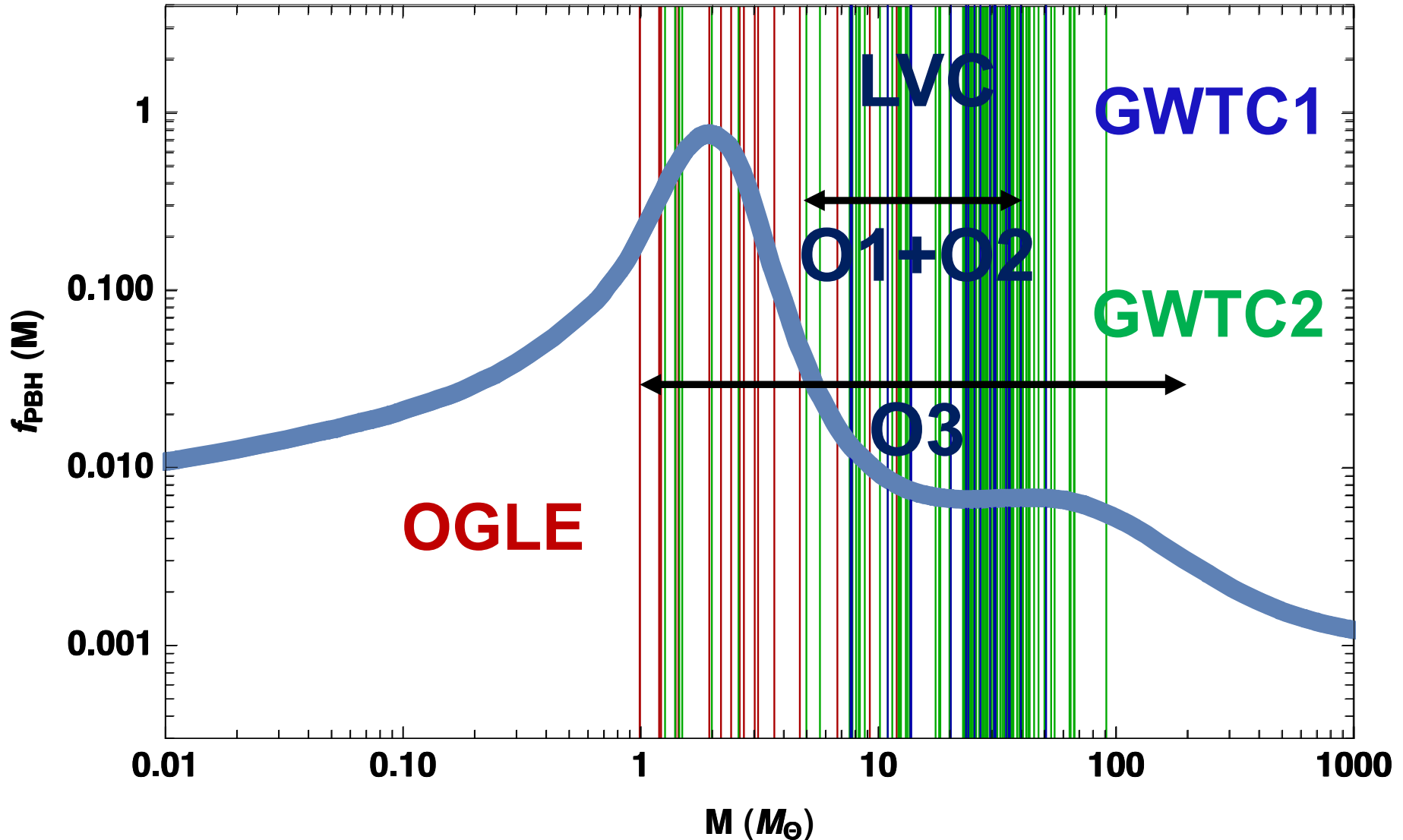
Wyrzykowski & Mandel (2018)

JGB (2019)

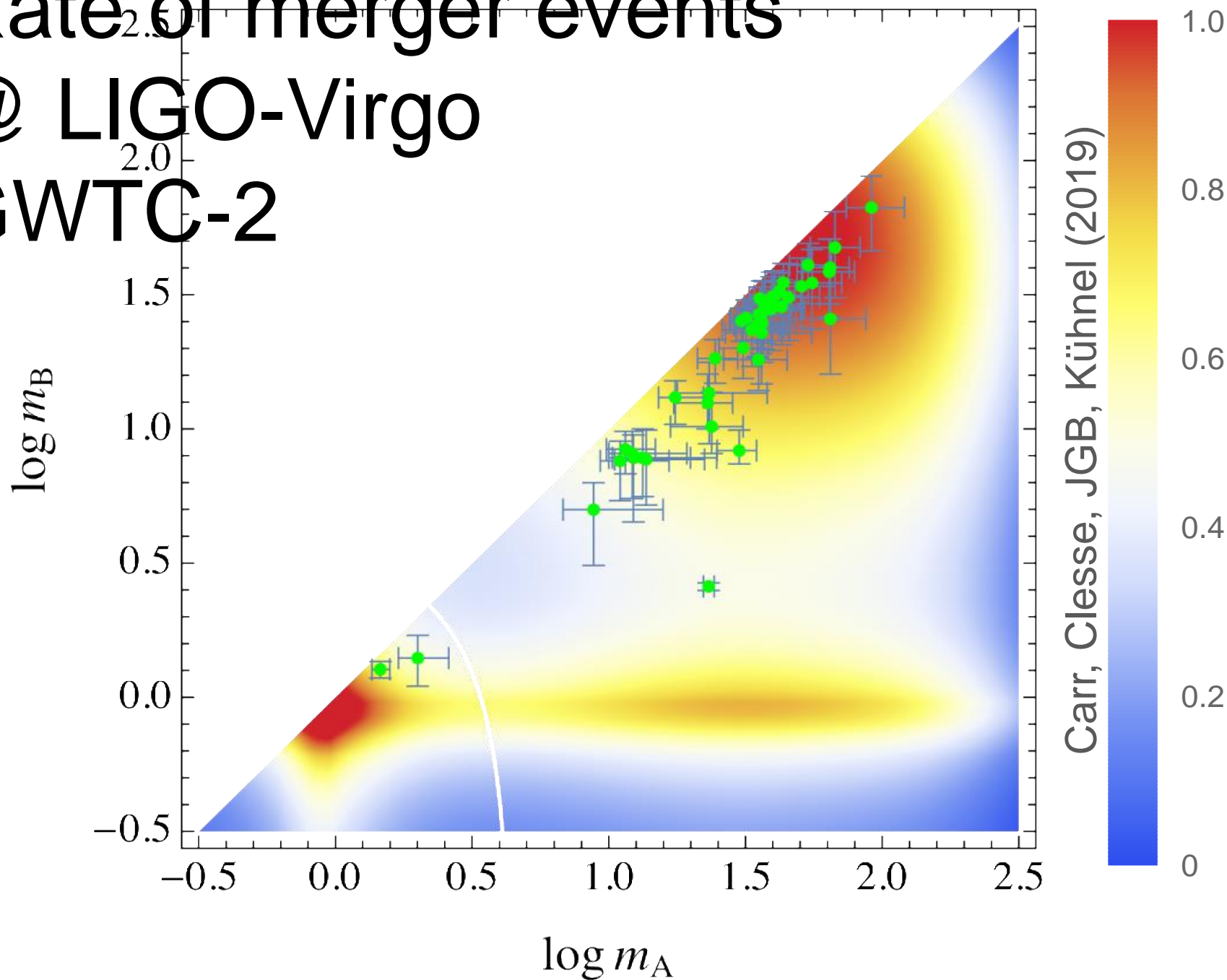


# Model prediction: mass spectrum

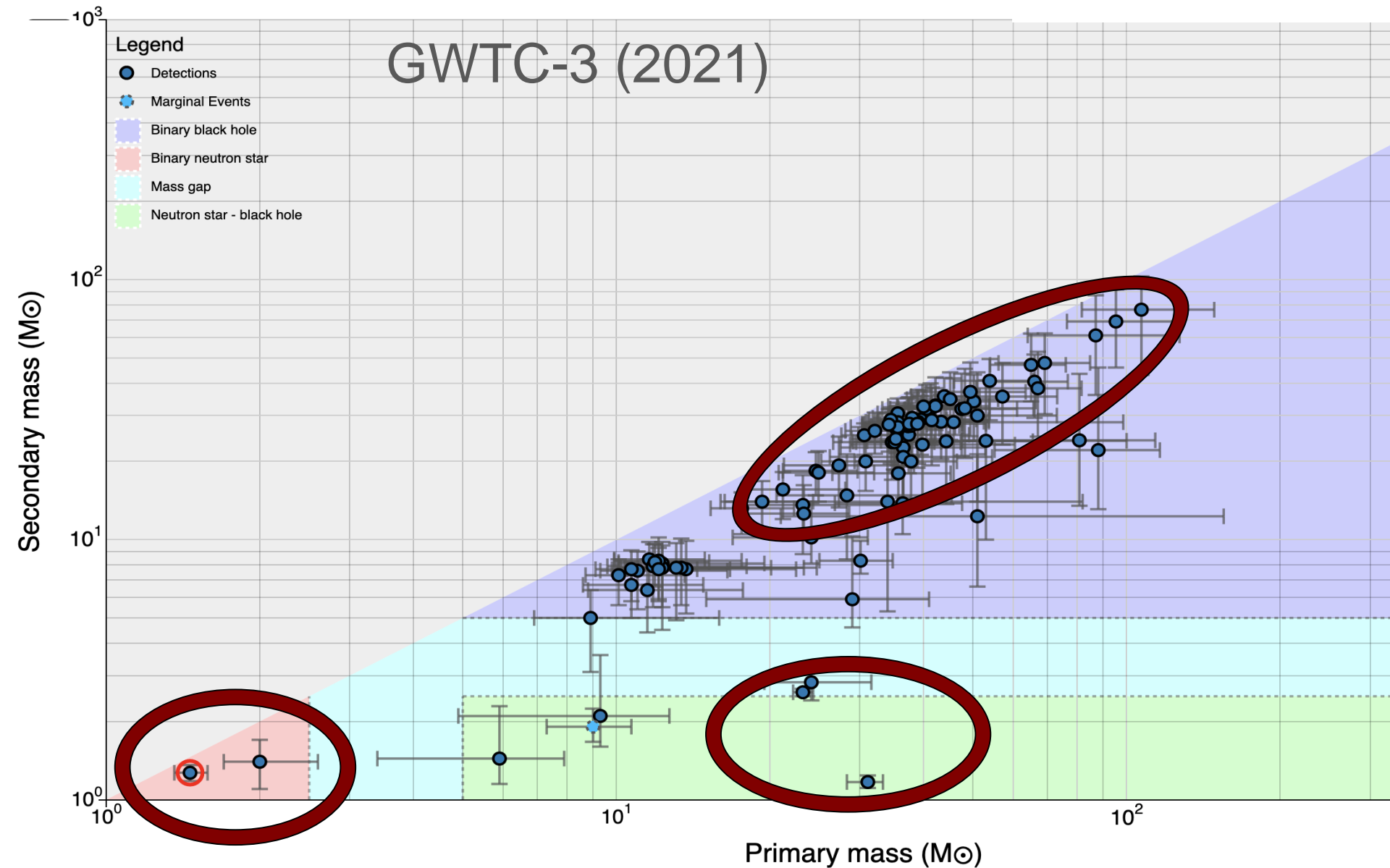
JGB, Clesse (2020)



# Rate of merger events @ LIGO-Virgo GWTC-2



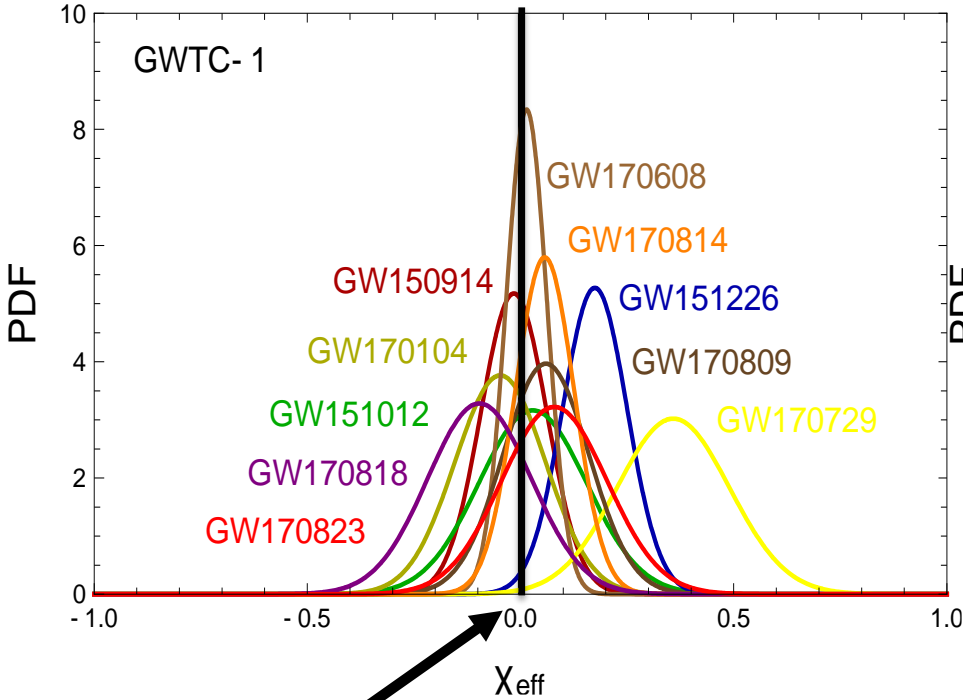
# Primary and secondary masses



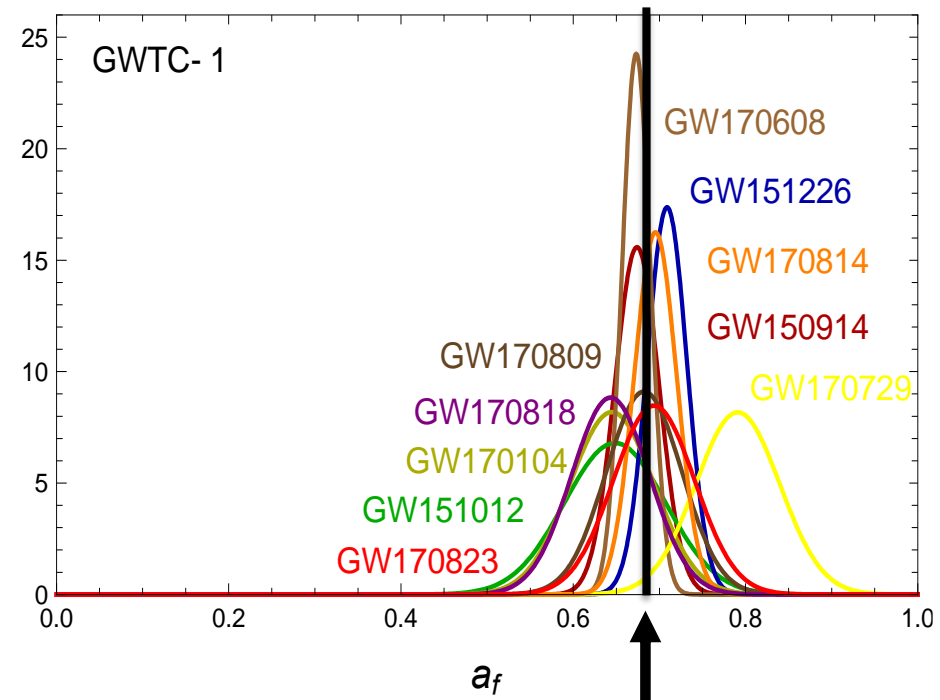


# Effective & Final Spin

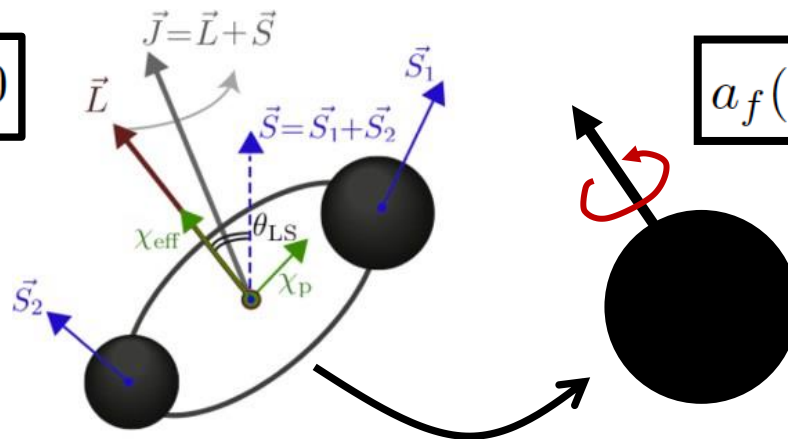
JGB (2019)



$$\chi_{\text{eff}}(S_1 = S_2 = 0) = 0$$



$$a_f(S_1 = S_2 = 0) = 0.686$$



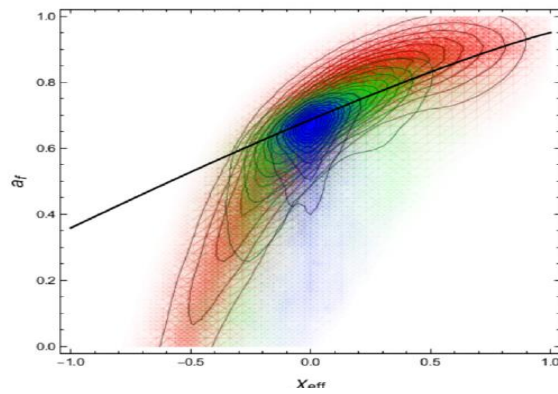
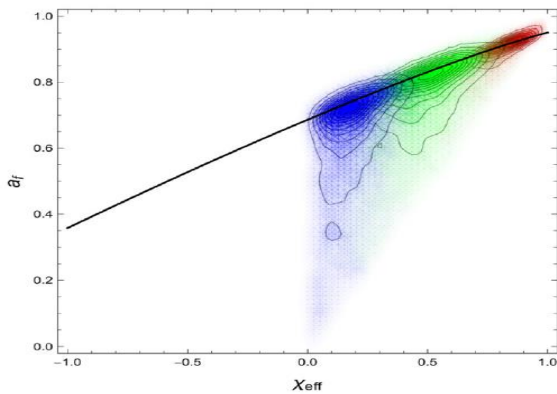
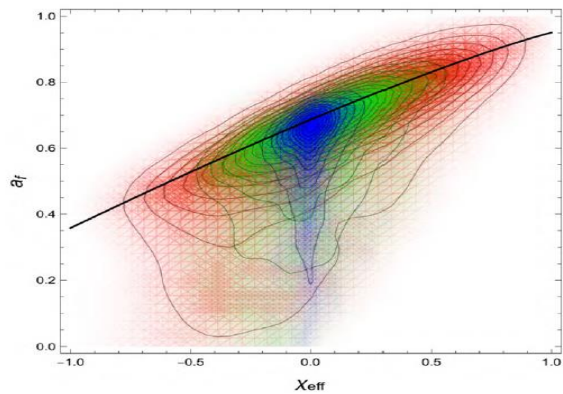
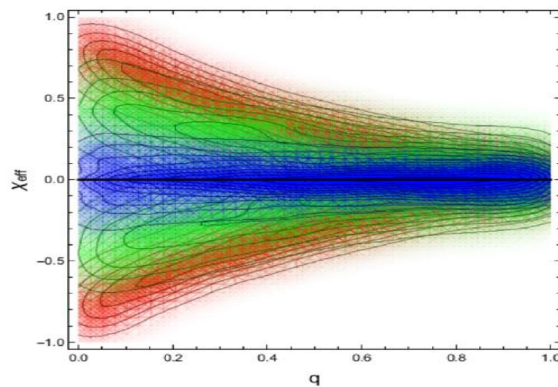
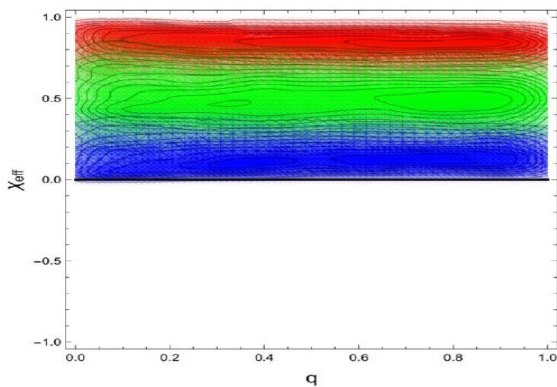
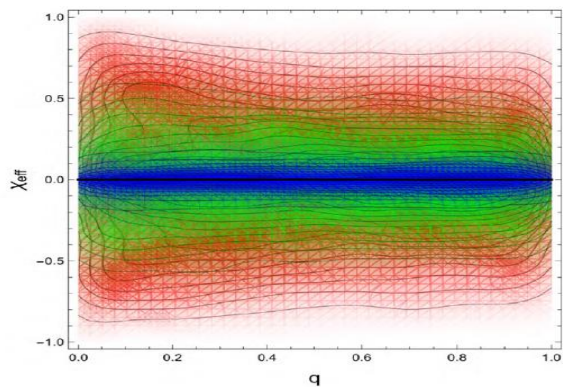
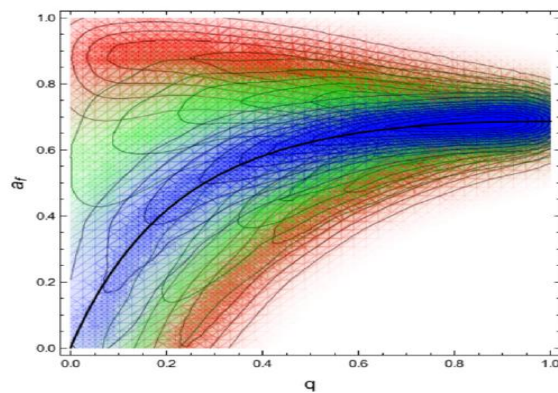
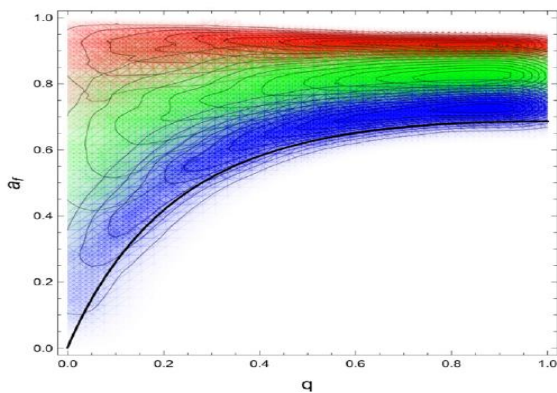
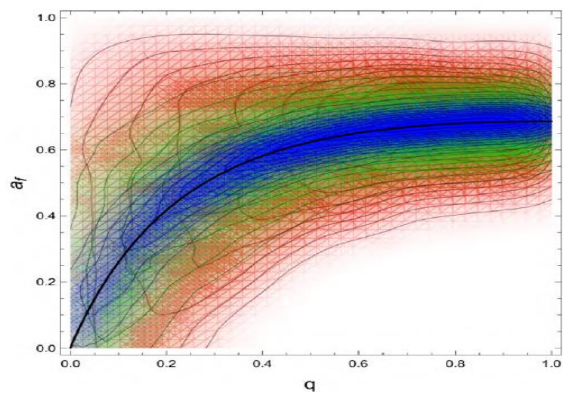
# M-ratio, Effective & Final Spin: Priors

isotropic spin

aligned spin

anti-aligned spin

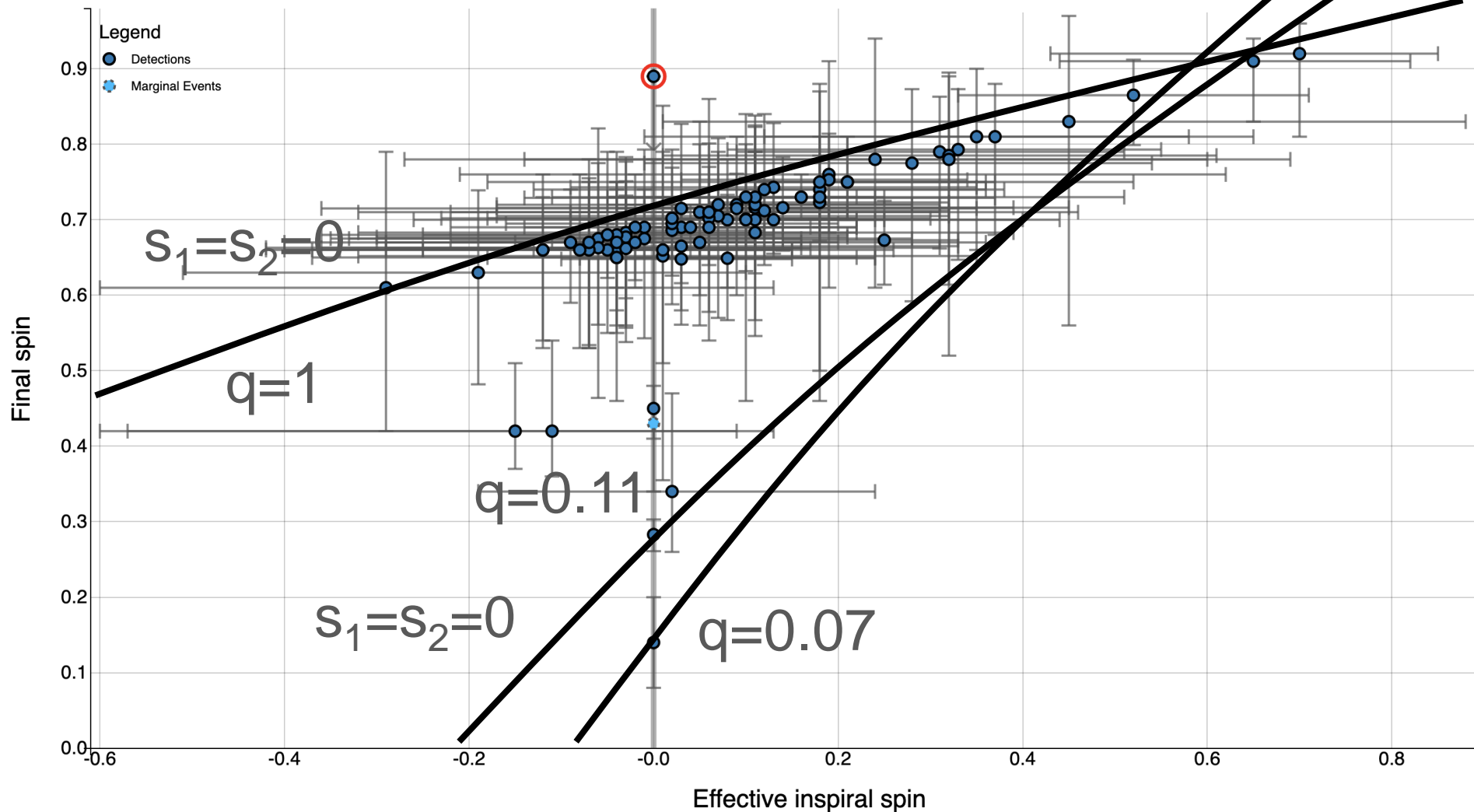
JGB, Nuño Siles, Ruiz Morales (2020)





# Final spin and effective spin

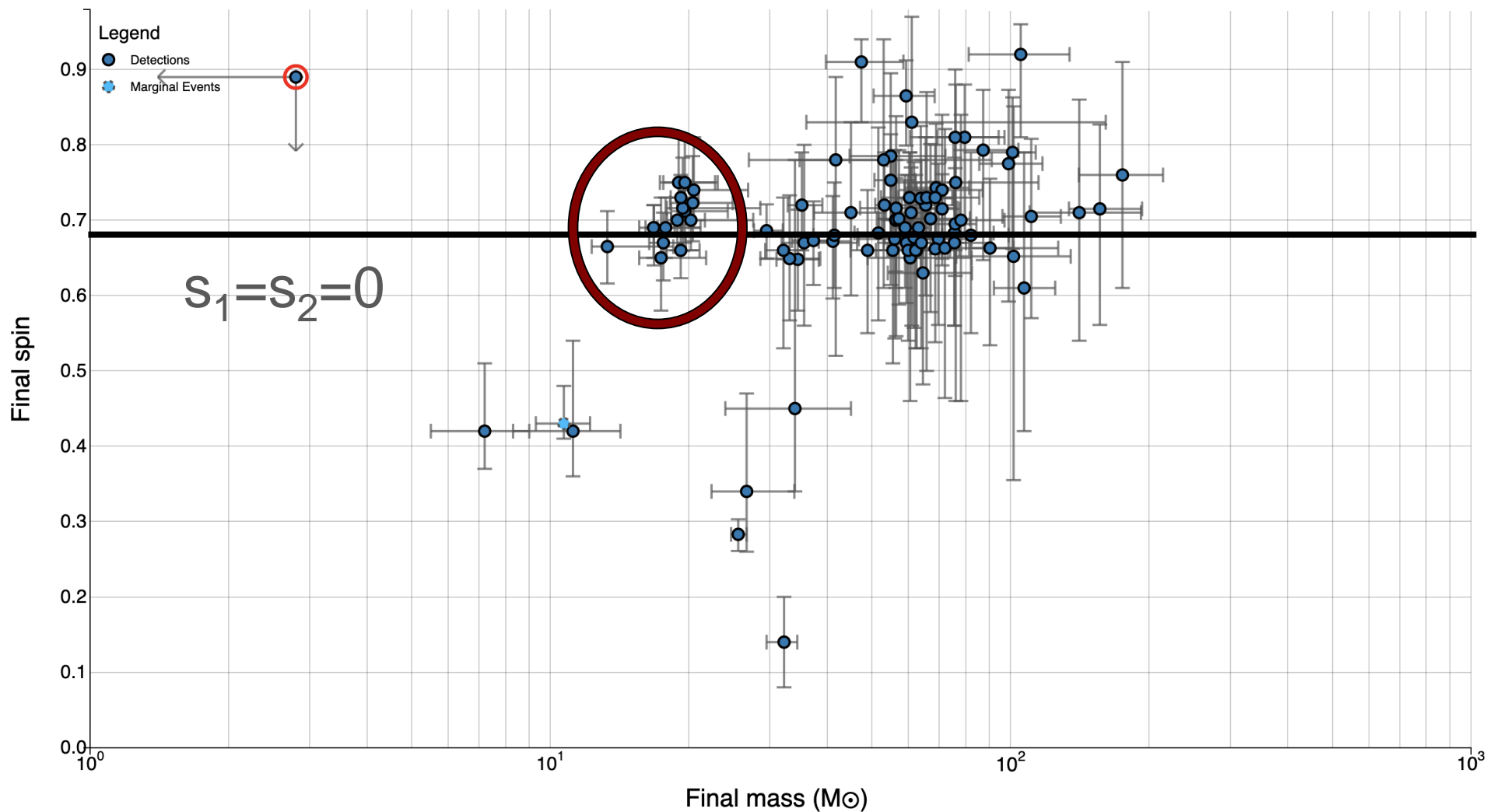
GWTC-3 (2021)



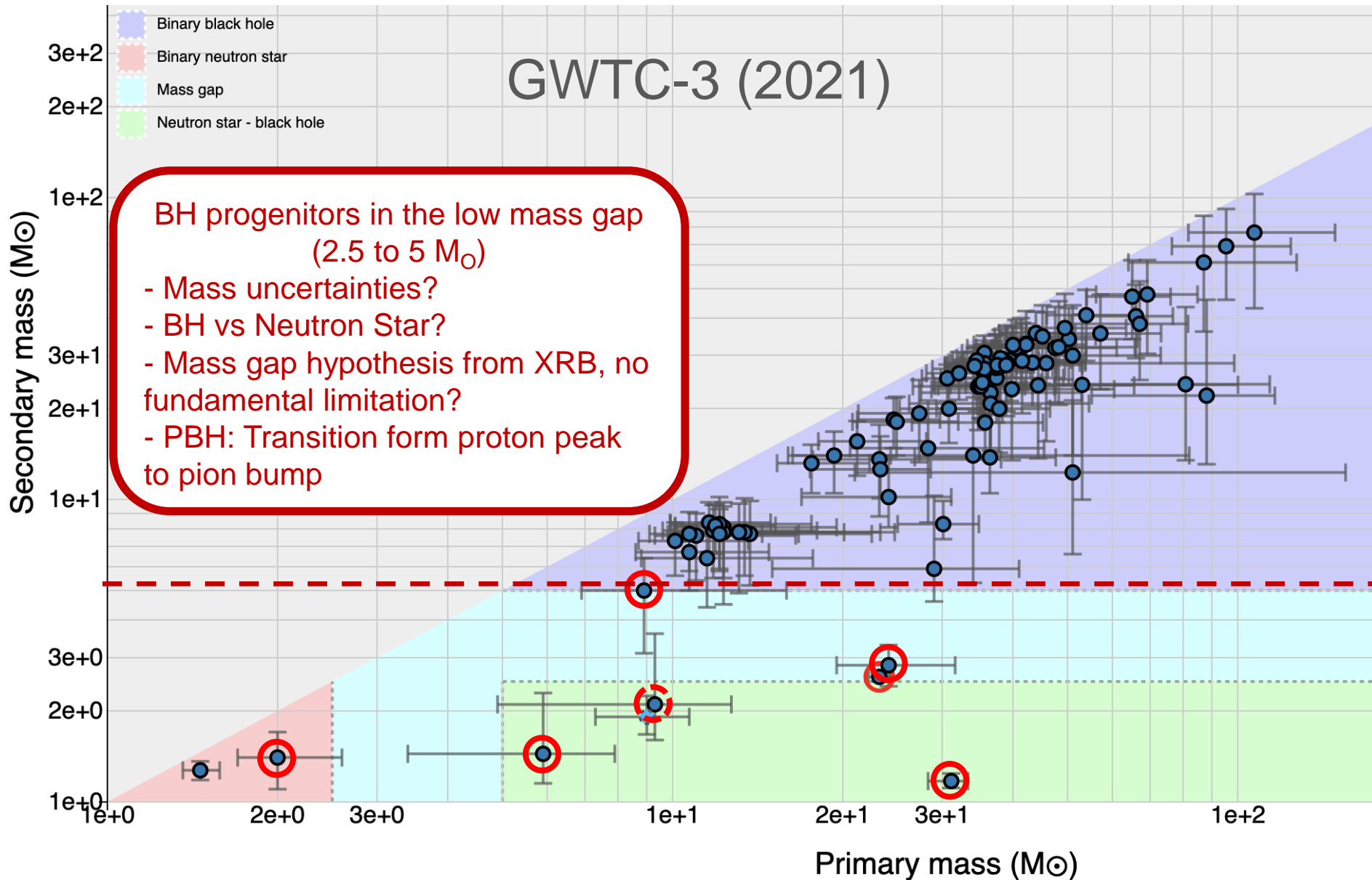


# Final mass and final spin

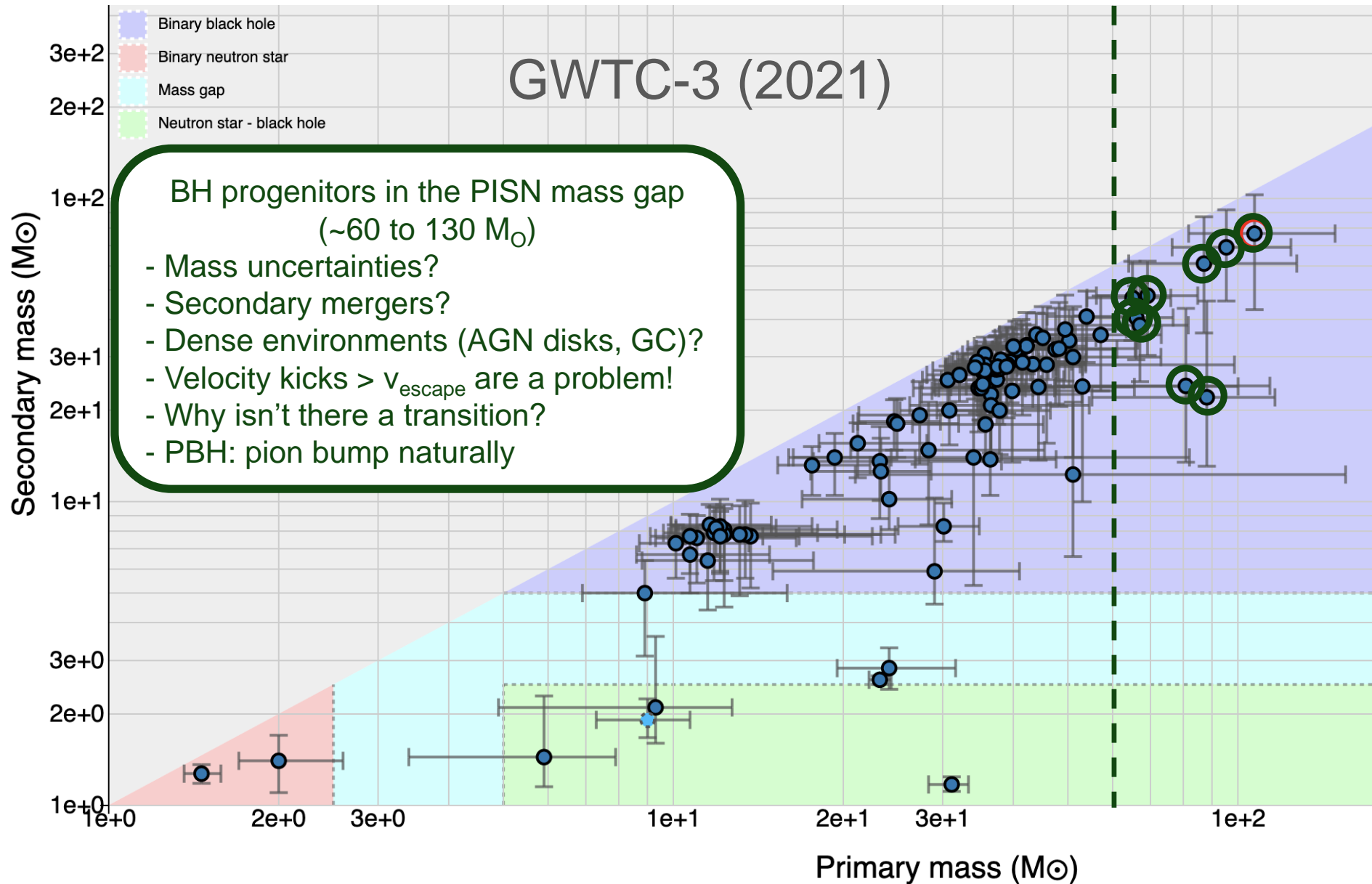
GWTC-3 (2021)



# Are LIGO/Virgo BH Primordial?

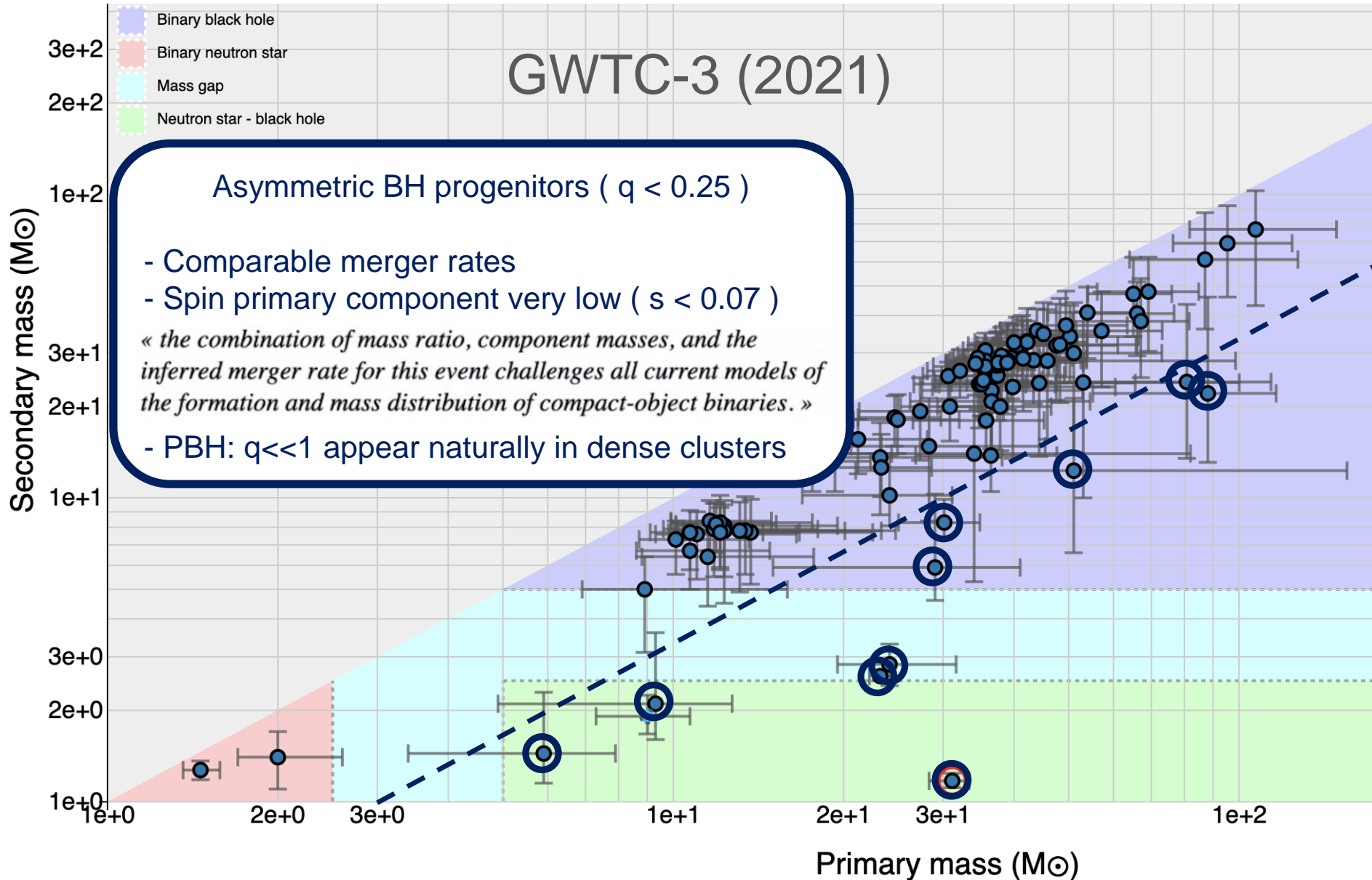


# Are LIGO/Virgo BH Primordial?

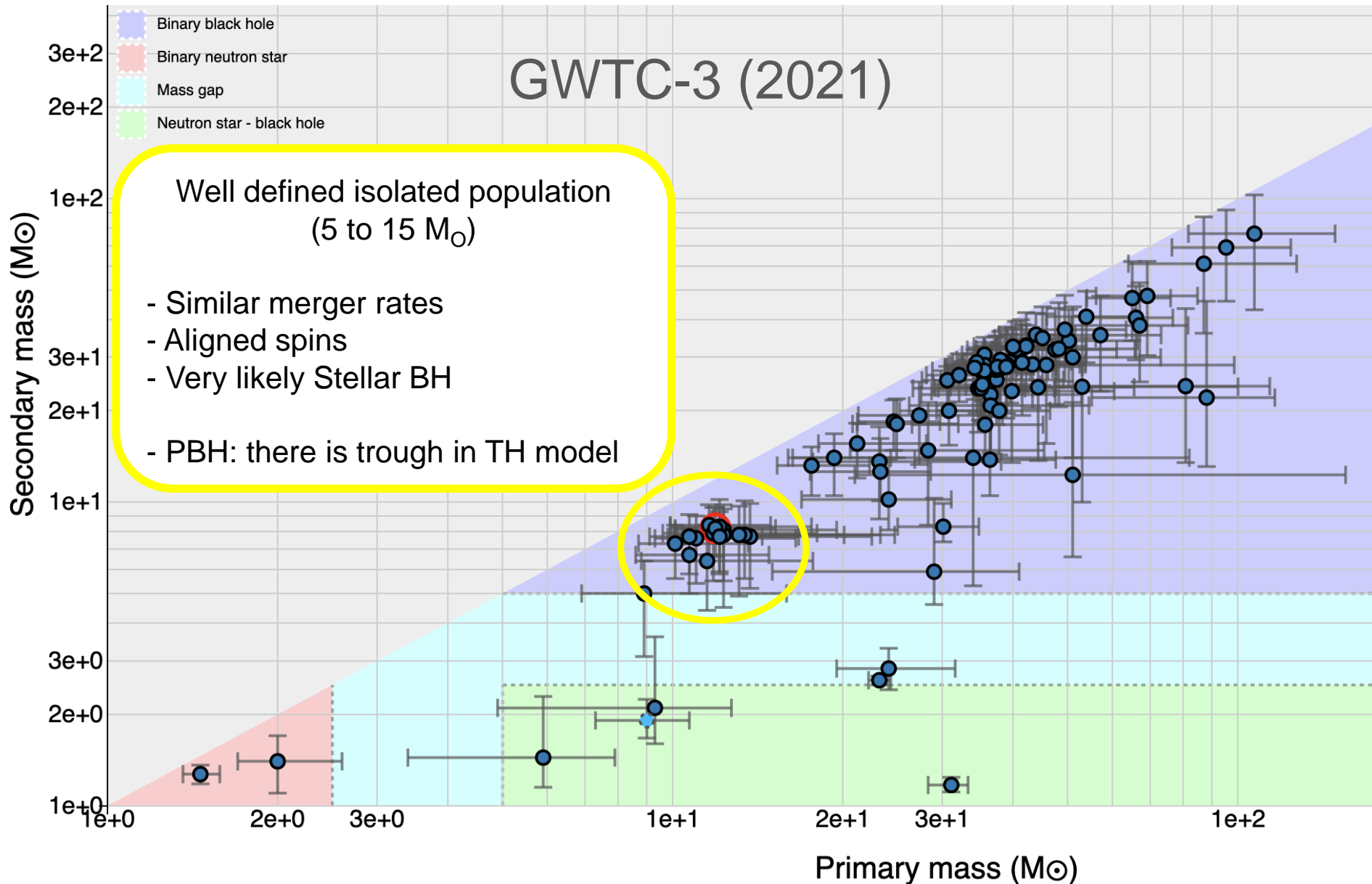




# Are LIGO/Virgo BH Primordial?

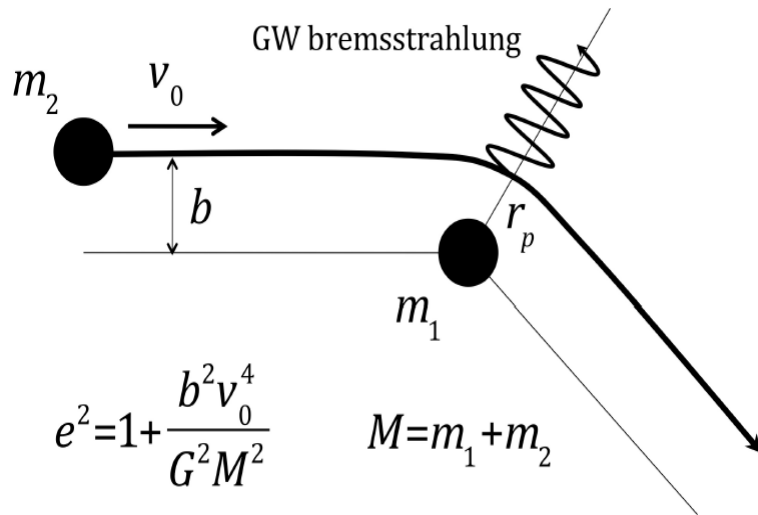


# Are LIGO/Virgo BH Primordial?



# Close Hyperbolic Encounters

Primordial Black Holes in dense clusters scatter off each other



$$r(\varphi) = \frac{b \sin \varphi_0}{\cos(\varphi - \varphi_0) - \cos \varphi_0} = \frac{a(e^2 - 1)}{1 + e \cos(\varphi - \varphi_0)}$$

$$r_{\min} = a(e - 1) = b \sqrt{\frac{e - 1}{e + 1}} > R_s \equiv \frac{2GM}{c^2}$$

$$b v_0 = r_{\min} v_{\max} \quad v_{\max} < c$$

$$\varphi_0 = \arccos\left(-\frac{1}{e}\right)$$

$$\beta \equiv \frac{v_0}{c} < \sqrt{\frac{e - 1}{e + 1}} \quad b > R_s \frac{(e + 1)^{3/2}}{2(e - 1)^{1/2}}$$

JGB, Nesseris (2018)

# Close Hyperbolic Encounters

Amplitude and Power emitted in GW

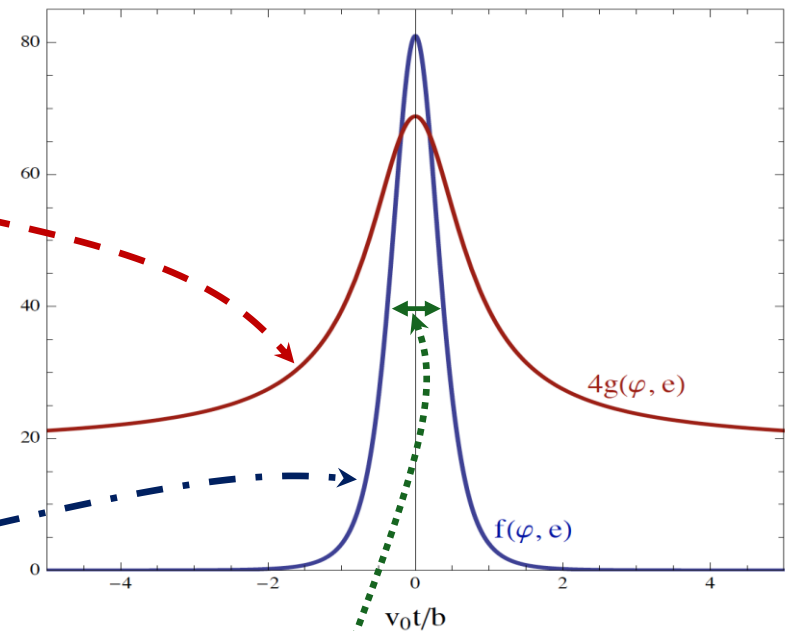
$$h_c = \frac{2G}{Rc^4} \langle \ddot{Q}_{ij} \ddot{Q}^{ij} \rangle_{i,j=1,2}^{1/2} = \frac{2G\mu v_0^2}{Rc^4} g(\varphi, e)$$

$$g(\varphi, e) = \frac{\sqrt{2}}{e^2 - 1} \left[ 36 + 59e^2 + 10e^4 + (108 + 47e^2)e \cos(\varphi - \varphi_0) + 59e^2 \cos 2(\varphi - \varphi_0) + 9e^3 \cos 3(\varphi - \varphi_0) \right]^{1/2}$$

$$P = \frac{dE}{dt} = -\frac{G}{45c^5} \langle \dddot{Q}_{ij} \dddot{Q}^{ij} \rangle = \frac{32G\mu^2 v_0^6}{45c^5 b^2} f(\varphi, e)$$

$$f(\varphi, e) = \frac{3(1 + e \cos(\varphi - \varphi_0))^4}{8(e^2 - 1)^4} \left[ 24 + 13e^2 + 48e \cos(\varphi - \varphi_0) + 11e^2 \cos 2(\varphi - \varphi_0) \right]$$

$$Q_{ij} = \mu r^2(\varphi) \begin{pmatrix} 3 \cos^2 \varphi - 1 & 3 \cos \varphi \sin \varphi & 0 \\ 3 \cos \varphi \sin \varphi & 3 \sin^2 \varphi - 1 & 0 \\ 0 & 0 & -1 \end{pmatrix}$$



Time duration of Burst:

$$t_{1/2} \simeq 1ms \left( \frac{b}{10^{-8} \text{AU}} \right) \left( \frac{0.01}{\beta} \right) (e - 1) \sqrt{\frac{3 \ln 2}{e + 35(1 + e)}}$$

JGB, Nesseris (2018)

# Close Hyperbolic Encounters

Power spectrum (frequency domain)

$$\Delta E = \int_{-\infty}^{\infty} P(t) dt = \frac{1}{\pi} \int_0^{\infty} P(\omega) d\omega = -\frac{8}{15} \frac{G^{7/2}}{c^5} \frac{M^{1/2} m_1^2 m_2^2}{r_{min}^{7/2}} f(e)$$

$$f(e) = \frac{1}{(1+e)^{7/2}} \left[ 24 \arccos\left(-\frac{1}{e}\right) \left(1 + \frac{73}{24}e^2 + \frac{37}{96}\right) + \sqrt{e^2 - 1} \left(\frac{301}{6} + \frac{673}{12}e^2\right) \right]$$

Quadrupole tensor

$$Q_{ij} = \frac{1}{2} a^2 \mu \begin{pmatrix} (3 - e^2) \cosh 2\xi - 8e \cosh \xi & 3\sqrt{e^2 - 1}(2e \sinh \xi - \sinh 2\xi) & 0 \\ 3\sqrt{e^2 - 1}(2e \sinh \xi - \sinh 2\xi) & (2e^2 - 3) \cosh 2\xi + 4e \cosh \xi & 0 \\ 0 & 0 & 4e \cosh \xi - e^2 \cosh 2\xi \end{pmatrix}$$

$$r(\xi) = a(e \cosh \xi - 1) \quad t(\xi) = \nu_0(e \sinh \xi - \xi) \quad \nu_0 = \sqrt{a^3 / GM}$$

# Close Hyperbolic Encounters

Power spectrum (frequency domain)

$$\begin{aligned}
 P(\omega) &= \frac{G}{45c^5} \sum_{i,j} |\widehat{\ddot{Q}}_{ij}|^2 \\
 &= \frac{G^3 \mu^2 M^2}{a^2 c^5} \left( \frac{\pi^2}{180} \nu^4 \sum_{i,j} |\widehat{C}_{ij}|^2 \right) \\
 &= \frac{G^3 \mu^2 M^2}{a^2 c^5} \frac{16\pi^2}{180} \nu^4 F_e(\nu),
 \end{aligned}$$

$$\begin{aligned}
 F_e(\nu) &= \left| \frac{3(e^2 - 1)}{e} H_{iv}^{(1)'}(ive) + \frac{e^2 - 3}{e^2} \frac{i}{\nu} H_{iv}^{(1)}(ive) \right|^2 \\
 &+ \left| \frac{3(e^2 - 1)}{e} H_{iv}^{(1)'}(ive) + \frac{2e^2 - 3}{e^2} \frac{i}{\nu} H_{iv}^{(1)}(ive) \right|^2 \\
 &+ \left| \frac{i}{\nu} H_{iv}^{(1)}(ive) \right|^2 + \frac{18(e^2 - 1)}{e^2} \times \\
 &\times \left| \frac{(e^2 - 1)}{e} i H_{iv}^{(1)}(ive) + \frac{1}{\nu} H_{iv}^{(1)'}(ive) \right|^2
 \end{aligned}$$

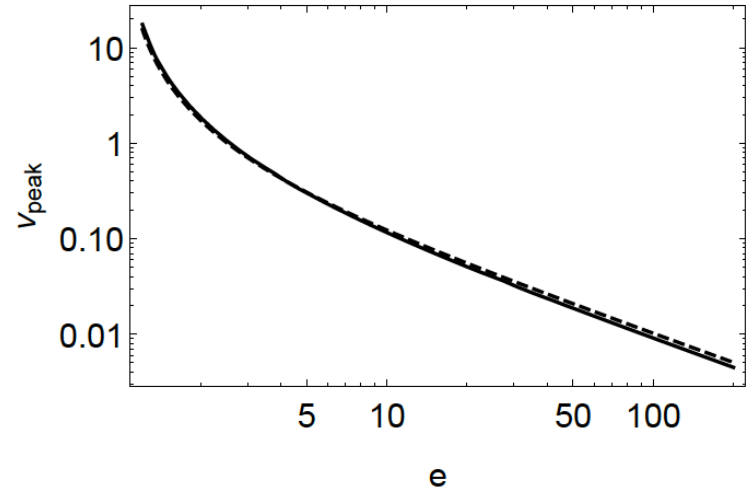
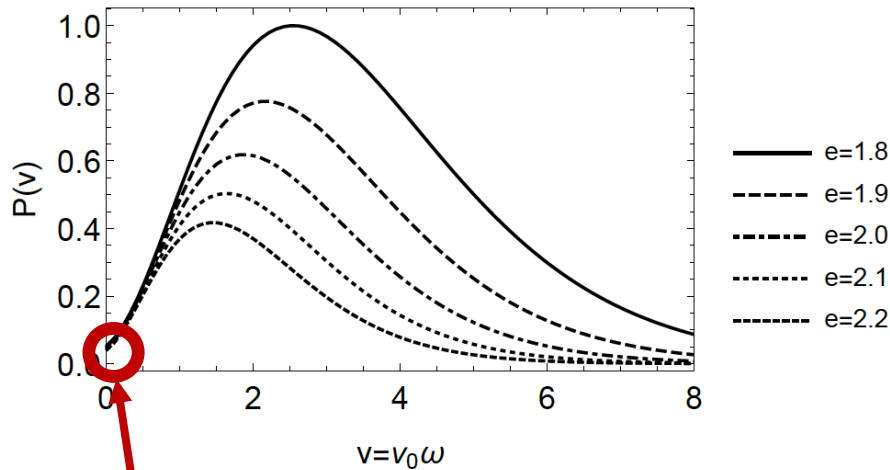
Total energy emitted:

$$\begin{aligned}
 \Delta E &= \int_{-\infty}^{+\infty} P(t) dt = \int_0^{+\infty} \frac{P(\omega)}{\pi} d\omega \\
 &= \left( \frac{G^{7/2} \mu^2 M^{5/2}}{c^5 a^{7/2}} \right) \frac{16\pi}{180} \int_0^{+\infty} \nu^4 F_e(\nu) d\nu.
 \end{aligned}$$

$$\begin{aligned}
 \nu^4 F_e(\nu) &\simeq \frac{12 F_y(\nu)}{\pi y (y^2 + 1)^2} e^{-2\nu z(y)} \\
 F_y(\nu) &= \nu (1 - y^2 - 3\nu y^3 + 4y^4 + 9\nu y^5 + 6\nu^2 y^6) \\
 z(y) &= y - \arctan y, \quad y \equiv \sqrt{e^2 - 1}
 \end{aligned}$$

# Close Hyperbolic Encounters

Peak frequency:  $P_{\max} = \frac{32}{45} \frac{q^2 \beta^{10}}{(1+q)^4} \frac{9(e+1)}{(e-1)^5} \frac{c^5}{G}$        $c^5/G = M_P/t_P = 3.6295 \times 10^{59} \text{ erg/s} = 9.3064 \times 10^{25} \mathcal{L}_{\odot}$



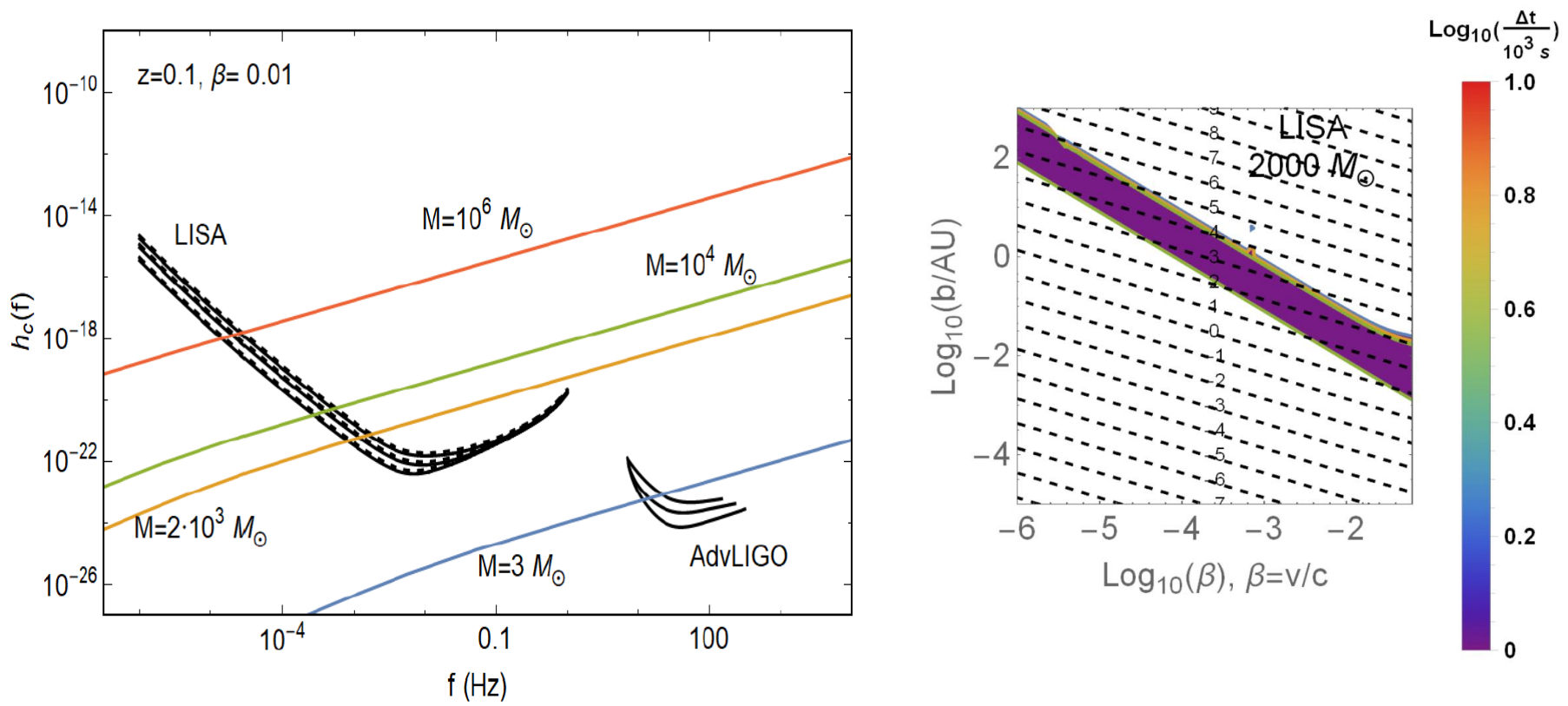
GW memory effect (after scattering, s.t. remembers the event)

$$P(\omega = 0) = \frac{G^3 \mu^2 M^2}{a^2 c^5} \frac{32(e^2 - 1)}{5e^4}$$

except for  $e = 1$  and  $e \rightarrow \infty$ .

# Close Hyperbolic Encounters

Detection at LIGO/Virgo/KAGRA and LISA

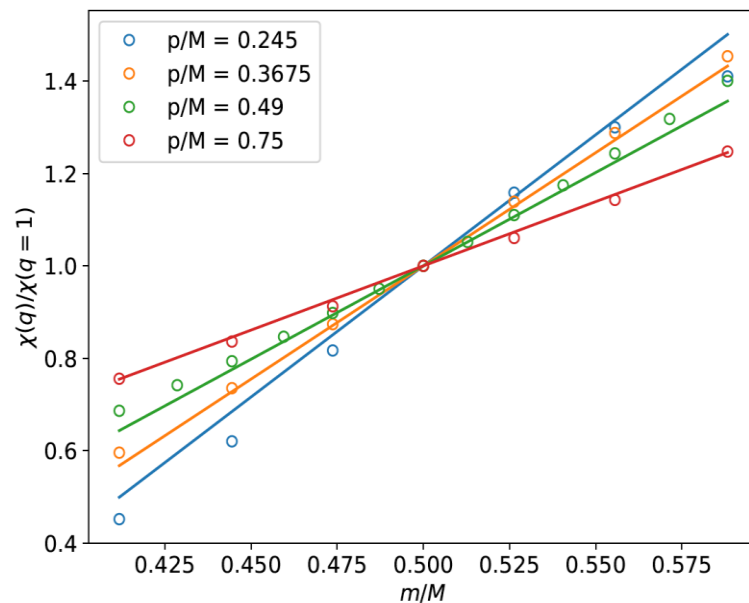
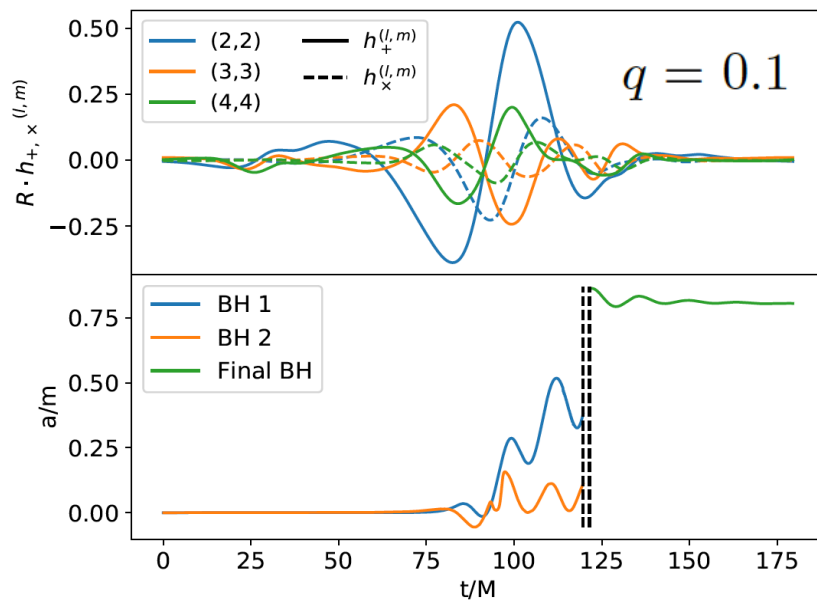
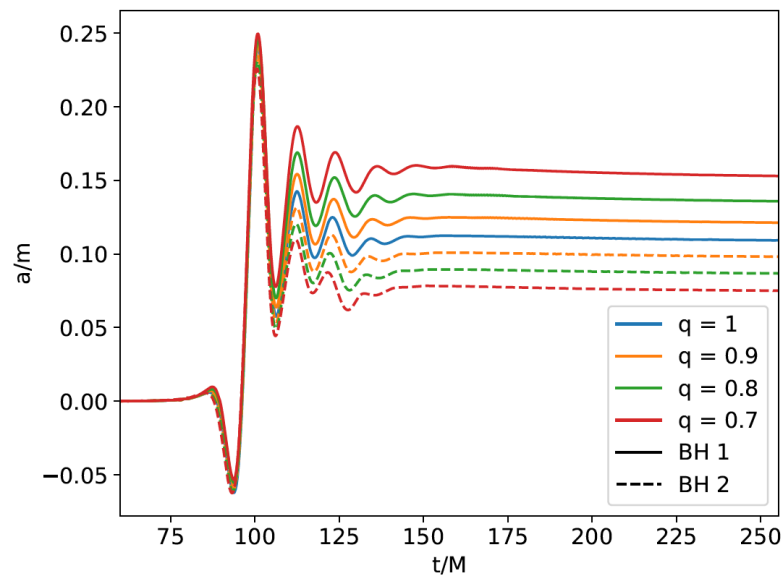
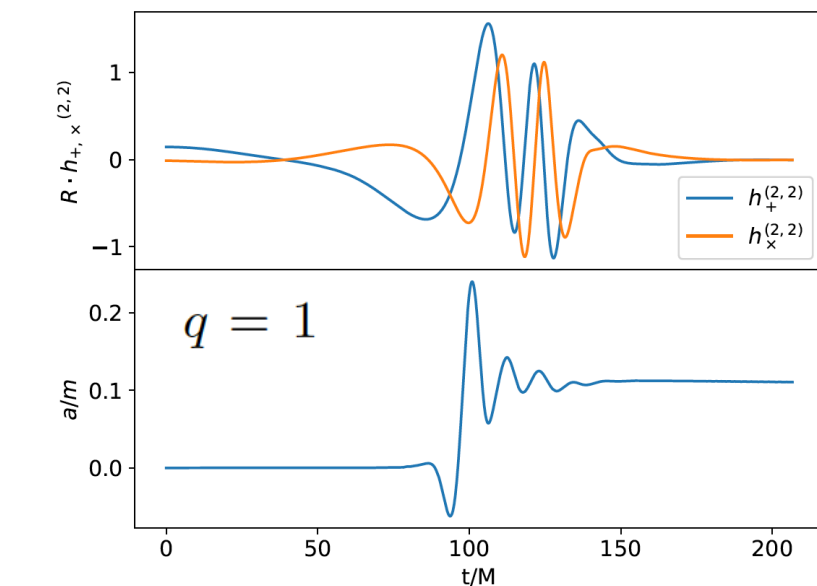


JGB, Nesseris (2018)



# PBH spin-up by CHE

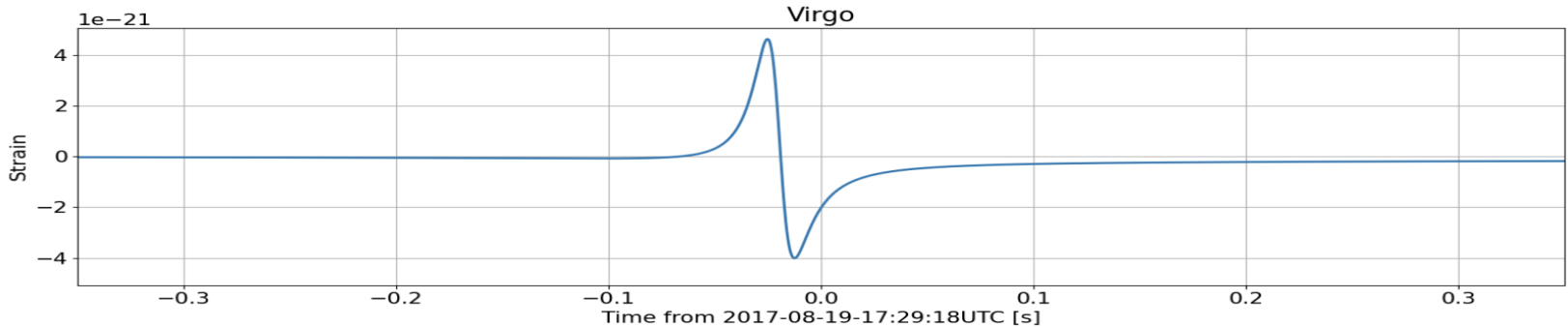
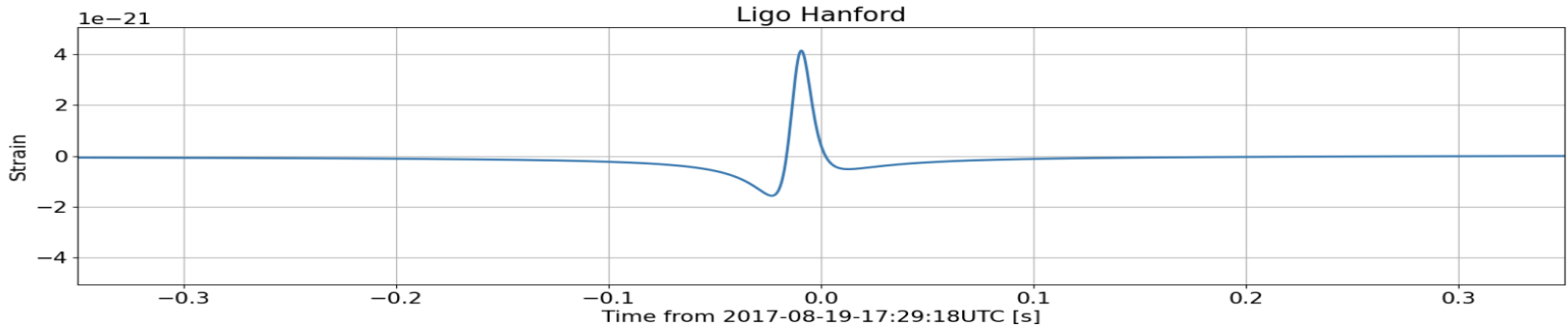
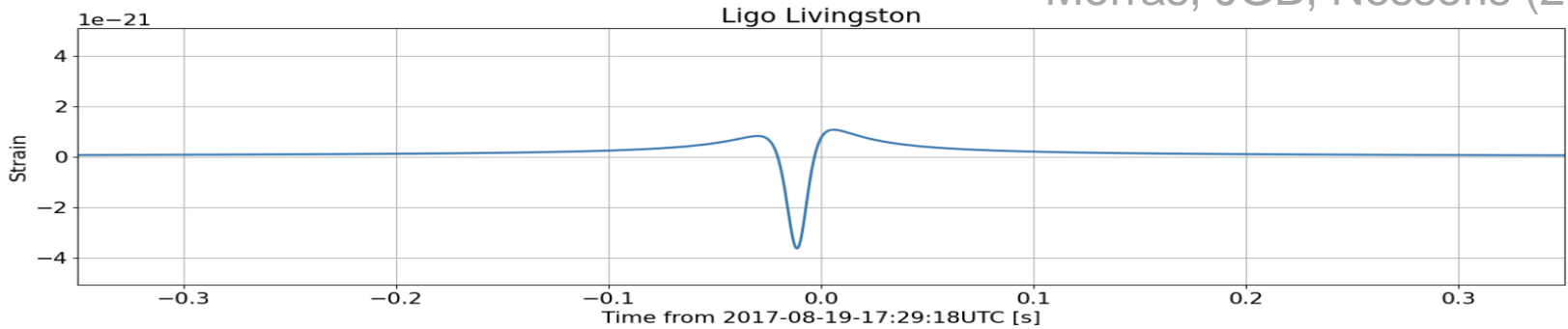
Jaraba, JGB (2021)



# Close Hyperbolic Encounters

How do they look like? Simulated injections

Morras, JGB, Nesseris (2021)

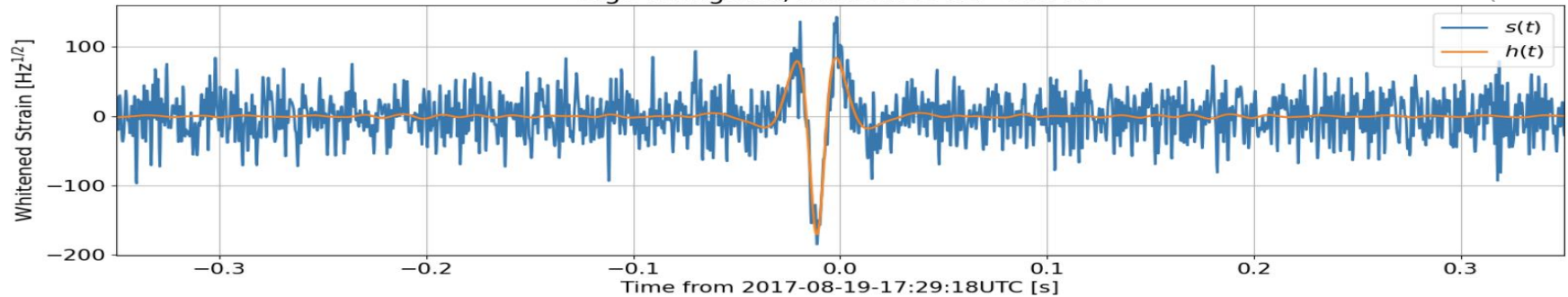


# Close Hyperbolic Encounters

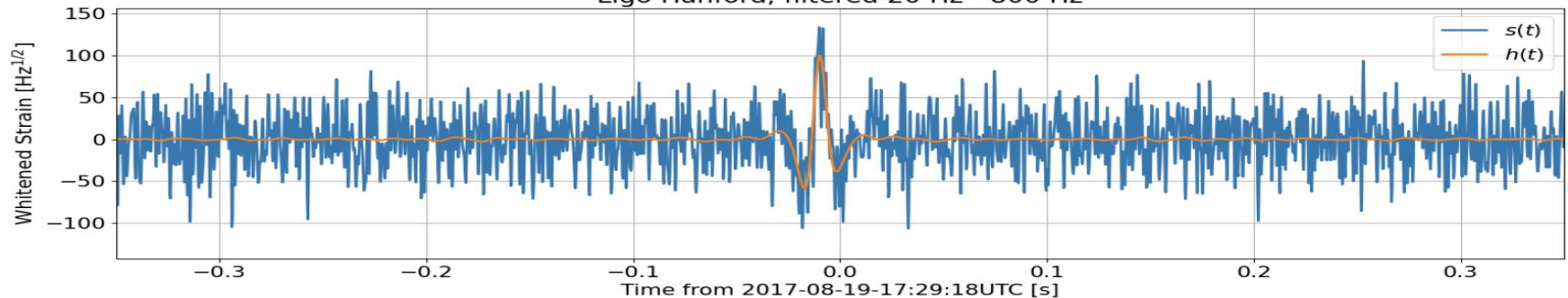
How do they look like? Strain amplitude  $h(t)$

Morras, JGB, Nesseris (2021)

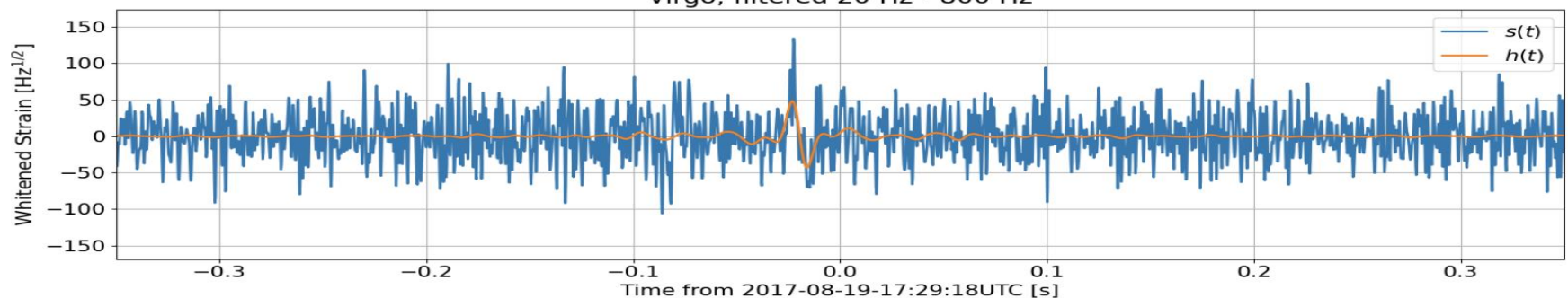
Ligo Livingston, filtered 20 Hz - 800 Hz



Ligo Hanford, filtered 20 Hz - 800 Hz



Virgo, filtered 20 Hz - 800 Hz

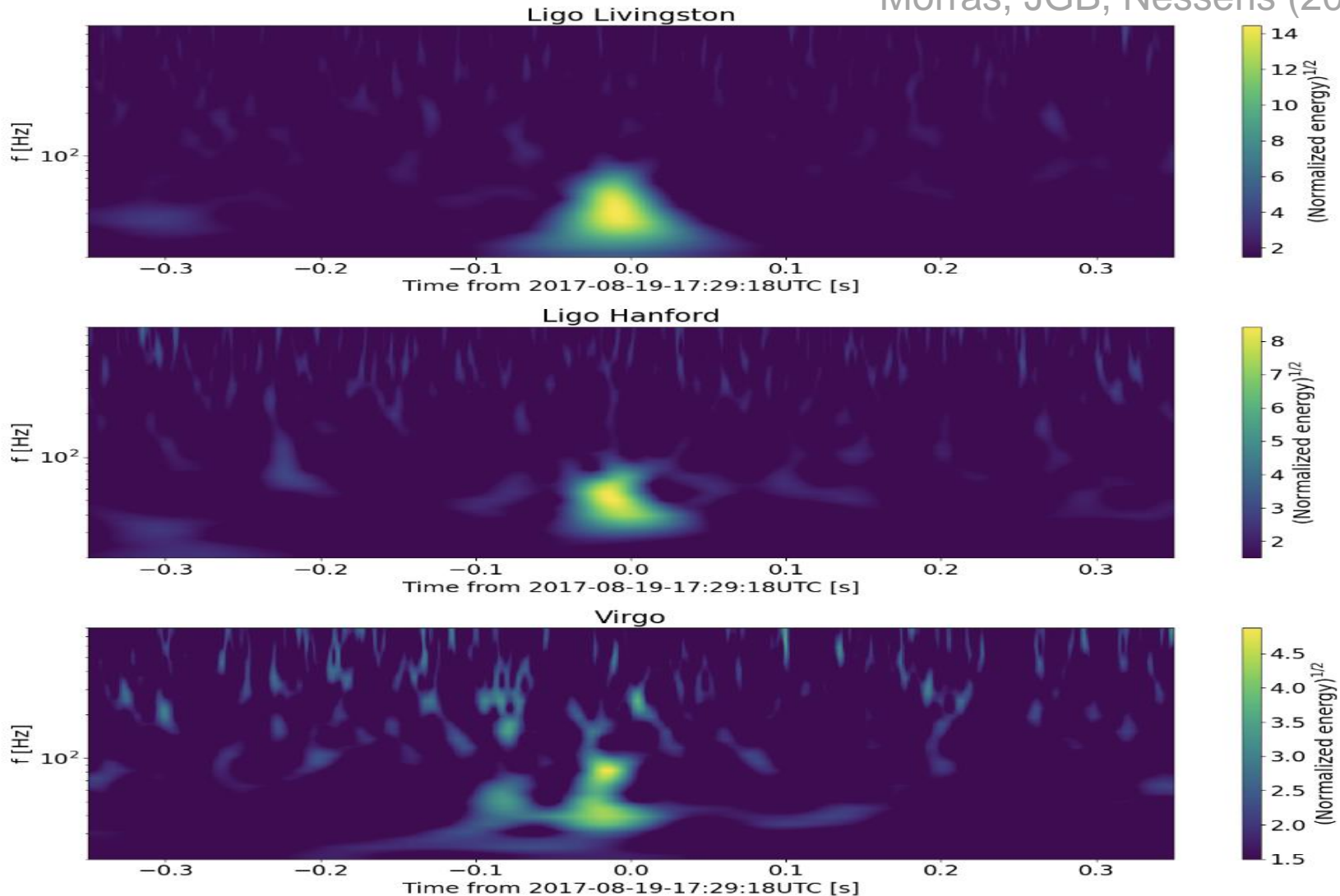


# Close Hyperbolic Encounters

How do they look like?

Spectrogram  $f(t)$

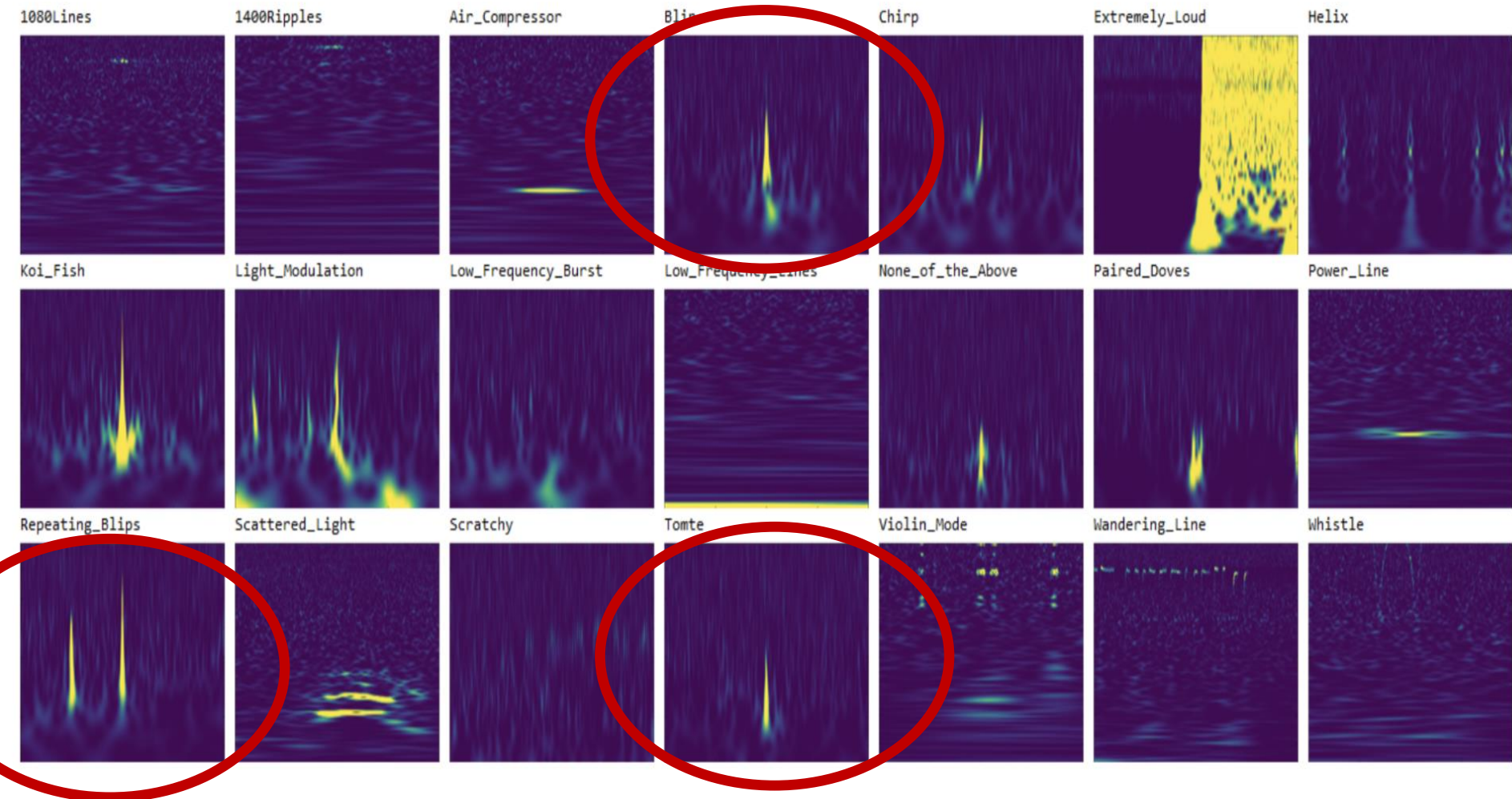
Morras, JGB, Nesseris (2021)



# Close Hyperbolic Encounters

How do they look like?

Can they be confused with glitches?



# SGWB from BBH & CHE

JGB, Jaraba, Kuroyanagi (2022)

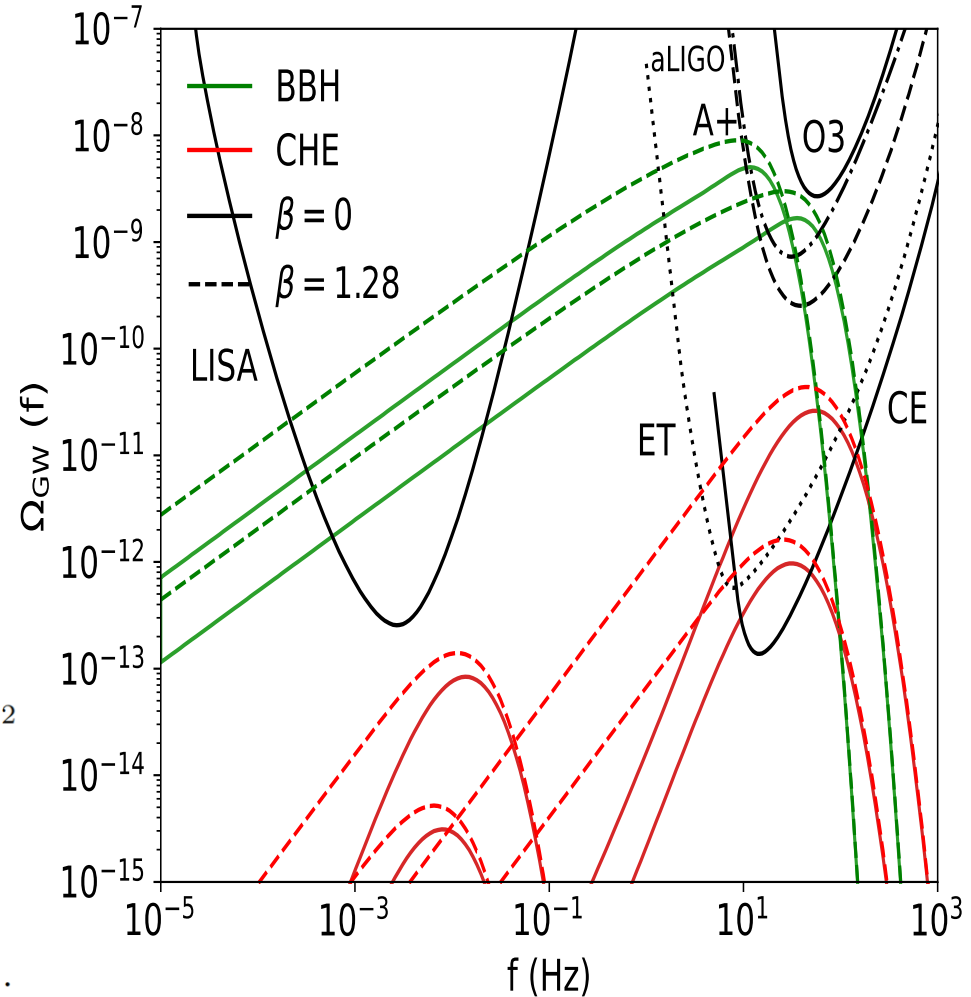
## SGWB from Black Hole Binaries

$$\Omega_{\text{GW}}^{\text{BBH}}(f) \approx 2.39 \times 10^{-13} h_{70} \times \left(\frac{\Omega_{\text{DM}}}{0.25}\right)^2 \left(\frac{\delta_{\text{loc}}}{10^8}\right) \left(\frac{v_0}{10 \text{ km/s}}\right)^{-11/7} \left(\frac{f}{\text{Hz}}\right)^{2/3} \times \int dm_1 dm_2 \frac{f(m_1) f(m_2) (m_1 + m_2)^{23/21}}{(m_1 m_2)^{5/7}},$$

$$\mathcal{T}(z) \propto (1+z)^\beta$$

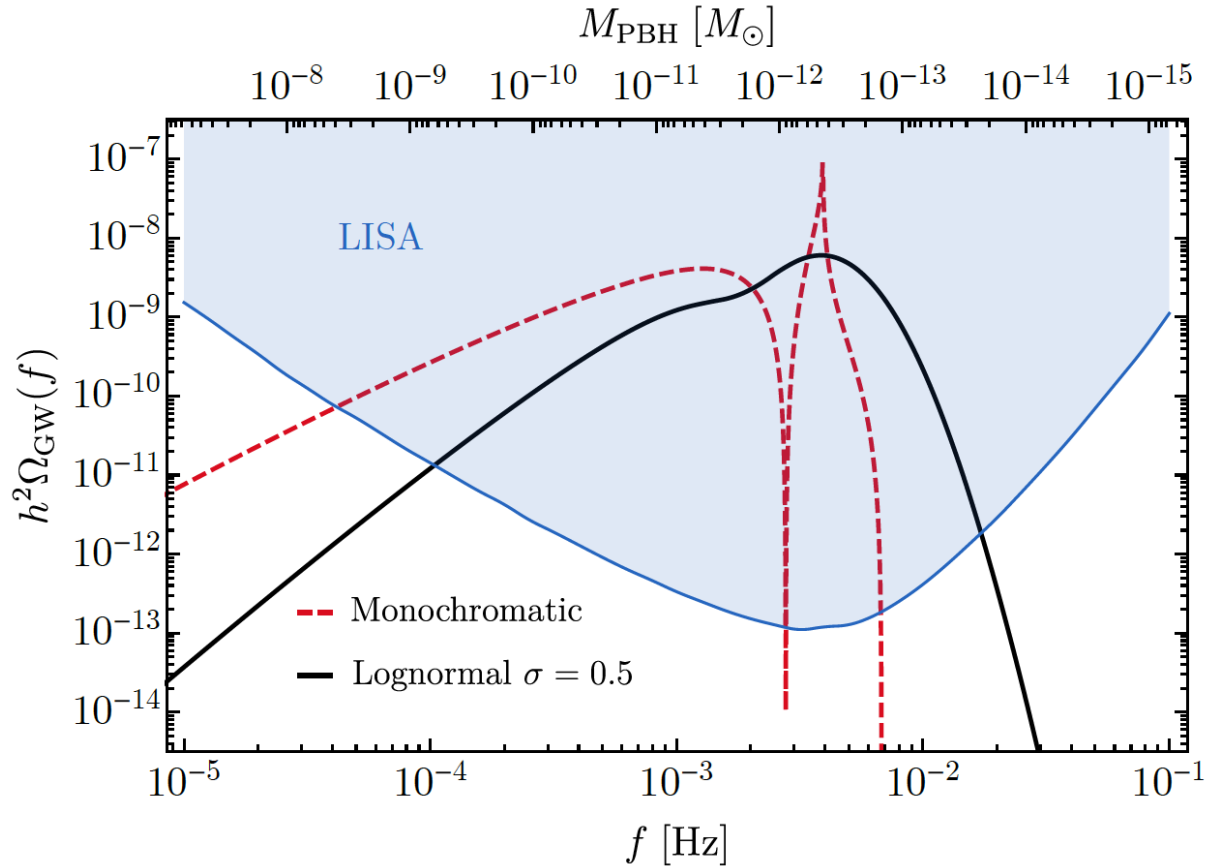
## Close Hyperbolic Encounters

$$\Omega_{\text{GW}}^{\text{CHE}}(f) \approx 9.81 \times 10^{-13} h_{70} \left(\frac{\Omega_{\text{M}}}{0.3}\right)^{-1/2} \left(\frac{\Omega_{\text{DM}}}{0.25}\right)^2 \times \left(\frac{\delta_{\text{loc}}}{10^8}\right) \left(\frac{a}{0.1 \text{ AU}}\right) \left(\frac{f}{10 \text{ Hz}}\right)^2 \left(\frac{y}{0.01}\right) \times \int \frac{dm_1}{100 M_\odot} \frac{dm_2}{100 M_\odot} f(m_1) f(m_2) e^{-2x_0 \xi(y)} \tilde{I}[y, x_0].$$



# SGWB: second order perturb.

JGB, Peloso, Unal (2018)  
Bartolo et al. (2019)



Gaussian  $P(k)$

Lognormal

$$\mathcal{P}_\zeta(k) = A_\zeta \exp\left(-\frac{\ln^2(k/k_\star)}{2\sigma^2}\right)$$

**Monochromatic**

$$\mathcal{P}_\zeta(k) = A_s k_\star \delta(k - k_\star)$$

$$\Omega_{\text{GW}}(\eta_0, k) = \frac{\Omega_{r,0} A_s^2 g_*(\eta_f)}{15552 g_*(\eta_0)} \left(\frac{g_{*S}(\eta_0)}{g_{*S}(\eta_f)}\right)^{4/3} \left(\frac{4k_\star}{k} - \frac{k}{k_\star}\right)^2 \theta(2k_\star - k) \left[ \mathcal{I}_c^2\left(\frac{k_\star}{k}, \frac{k_\star}{k}\right) + \mathcal{I}_s^2\left(\frac{k_\star}{k}, \frac{k_\star}{k}\right) \right]$$

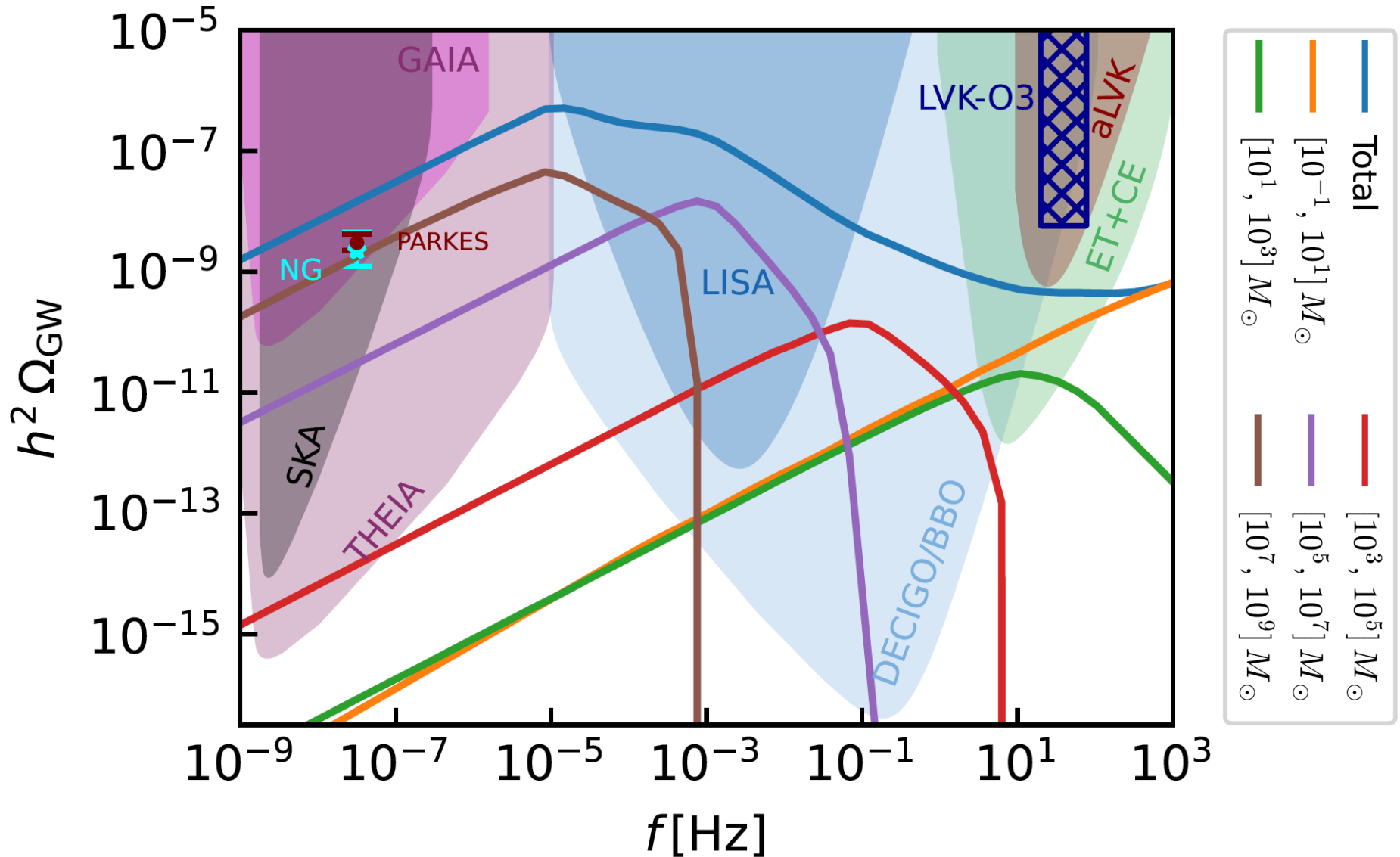
$$\mathcal{I}_c(x, y) = -36\pi \frac{(s^2 + d^2 - 2)^2}{(s^2 - d^2)^3} \theta(s - 1),$$

$$d \equiv \frac{1}{\sqrt{3}}|x - y|, \quad s \equiv \frac{1}{\sqrt{3}}(x + y), \quad (d, s) \in [0, 1/\sqrt{3}] \times [1/\sqrt{3}, +\infty).$$

$$\mathcal{I}_s(x, y) = -36 \frac{(s^2 + d^2 - 2)}{(s^2 - d^2)^2} \left[ \frac{(s^2 + d^2 - 2)}{(s^2 - d^2)} \log \frac{(1 - d^2)}{|s^2 - 1|} + 2 \right]$$

# SGWB: Thermal History Model

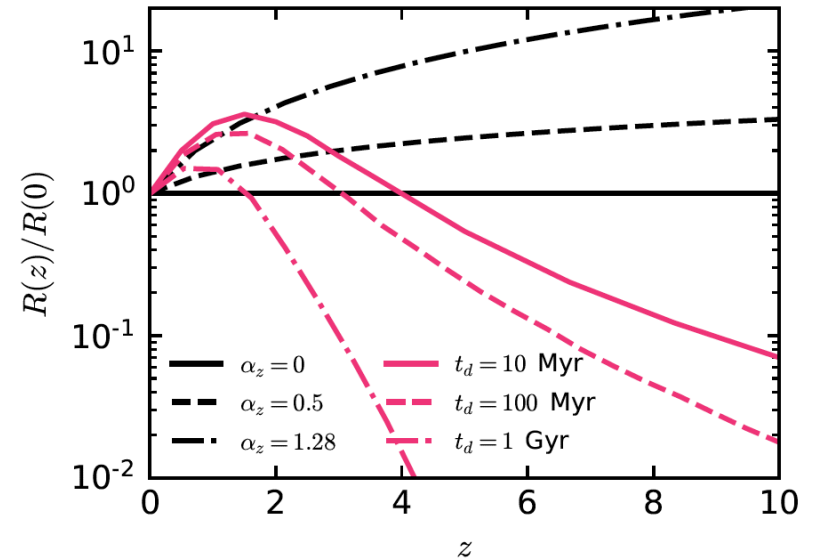
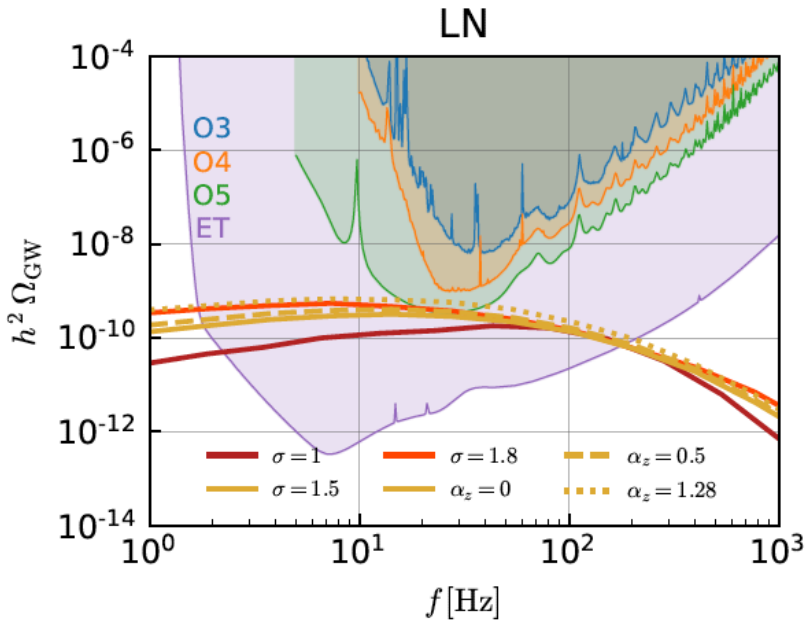
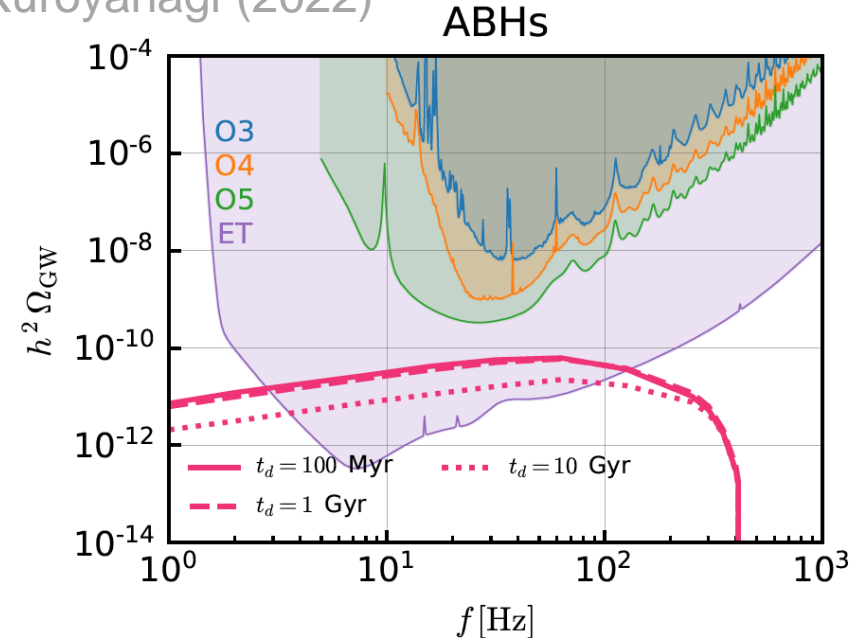
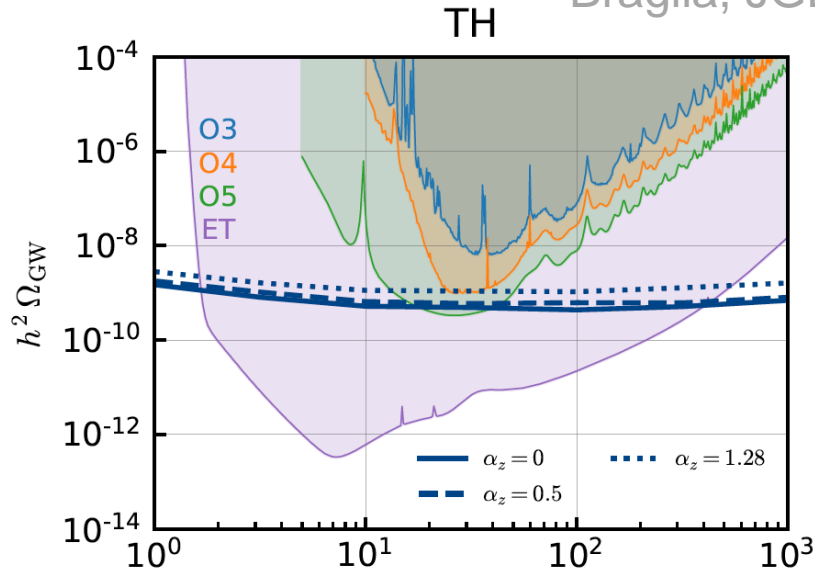
Braglia, JGB, Kuroyanagi (2022)





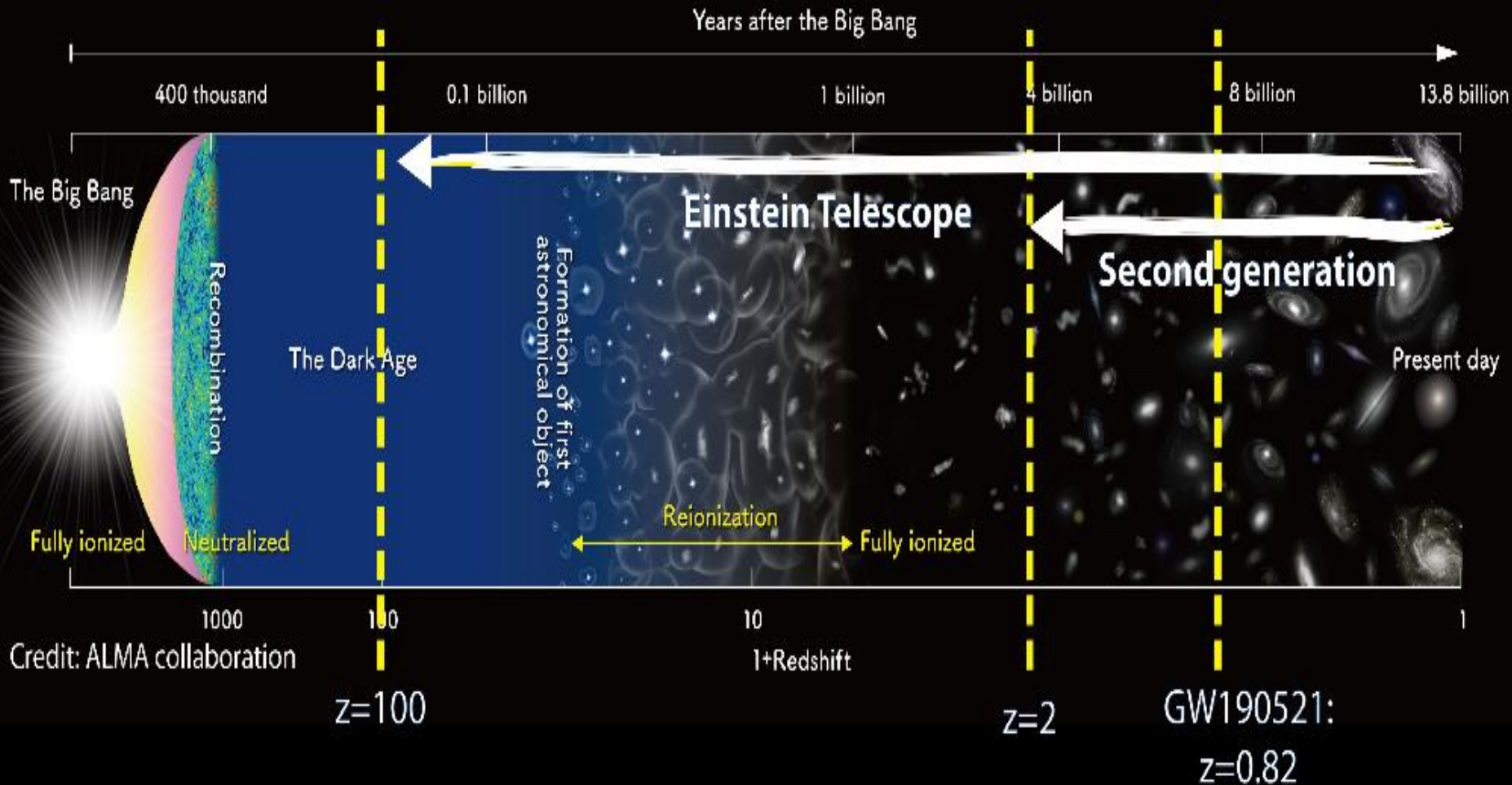
# SGWB: TH vs LN vs ABH

Braglia, JGB, Kuroyanagi (2022)

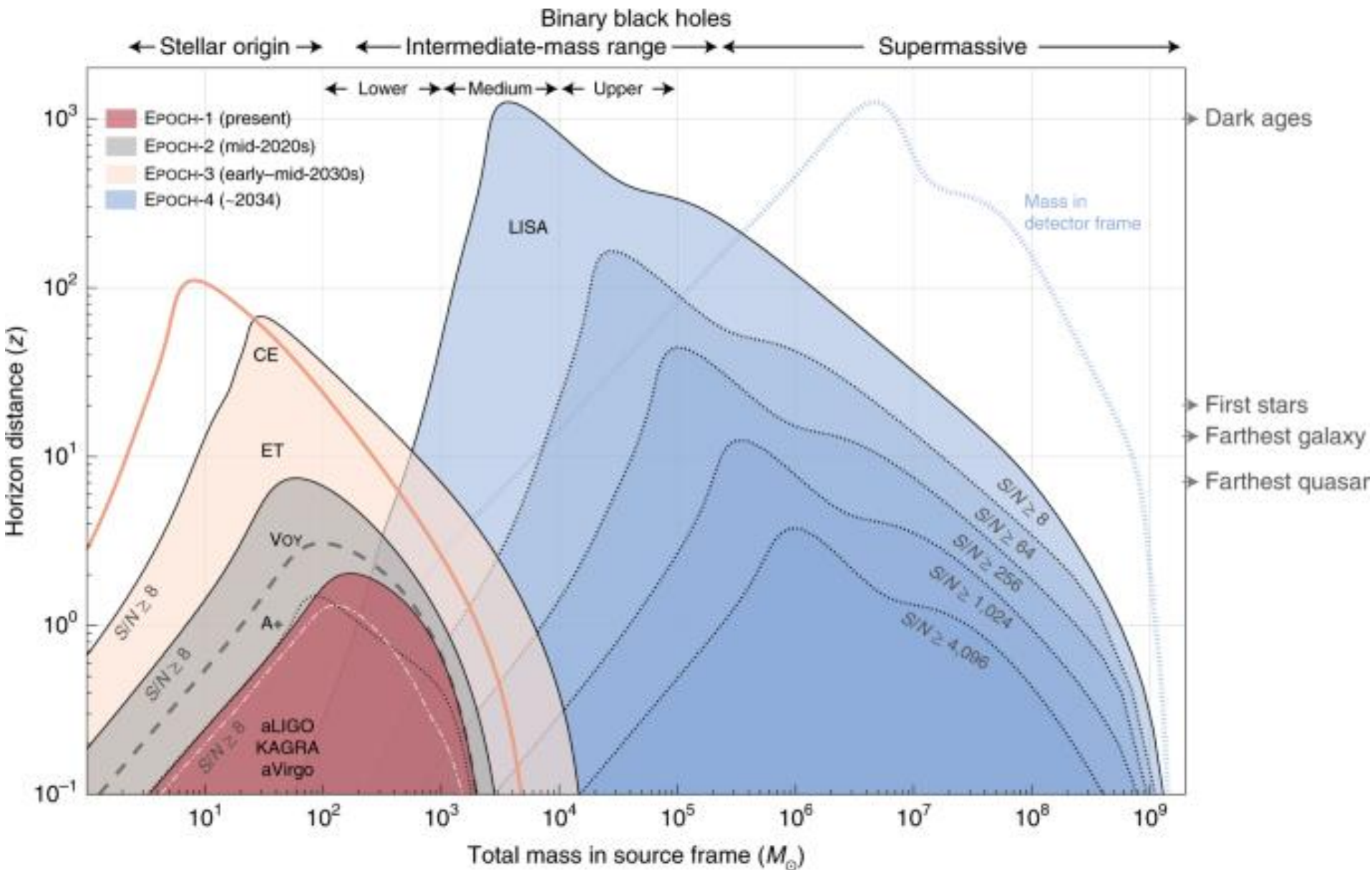


# The future of GW (G3)

## Detection horizon for black-hole binaries



# BBH sensitivity in future G3 GW



# Conclusions

- Quantum diffusion inevitably generates PBH
- Thermal history predicts PBH have multimodal mass distribution  $\sim 1E-5, 1, 100, 1E5$  Msun (1E-10 also?)
- The predicted PBH spin and mass distribution has been measured by LIGO/Virgo + OGLE around 1-100 Msun (features: peak+plateau)
- Other peaks could be explored with microlensing
- PBH scenario can explain various cosmic conundra
- Paradigm shift in Structure Formation of Universe
- Very rich phenomenology: multiscale, multiepoch, multiprobe => Future G3 detectors (ET, LISA, GAIA)

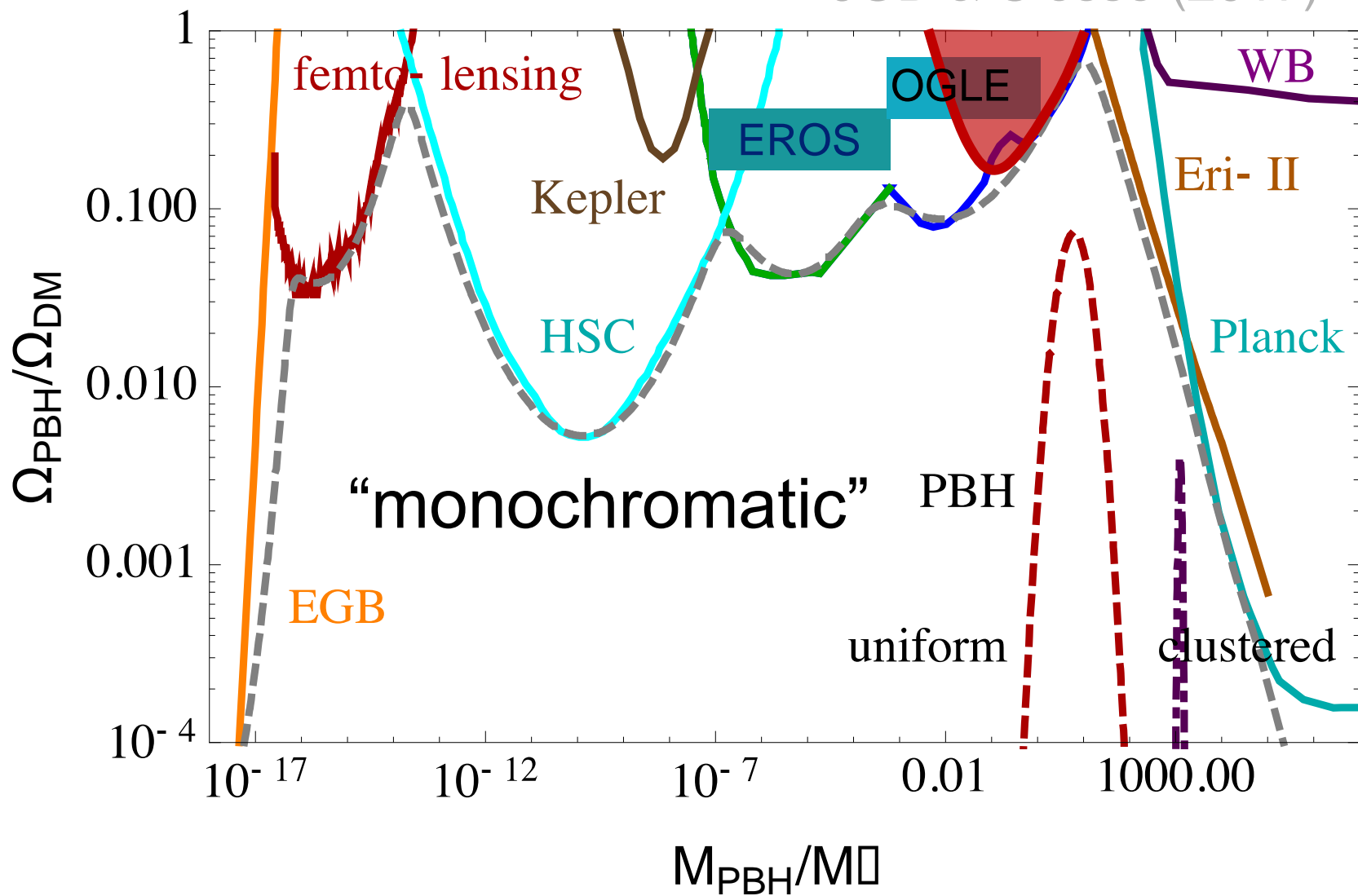
**Backup slides**

# PBH scenario (1996-2022)

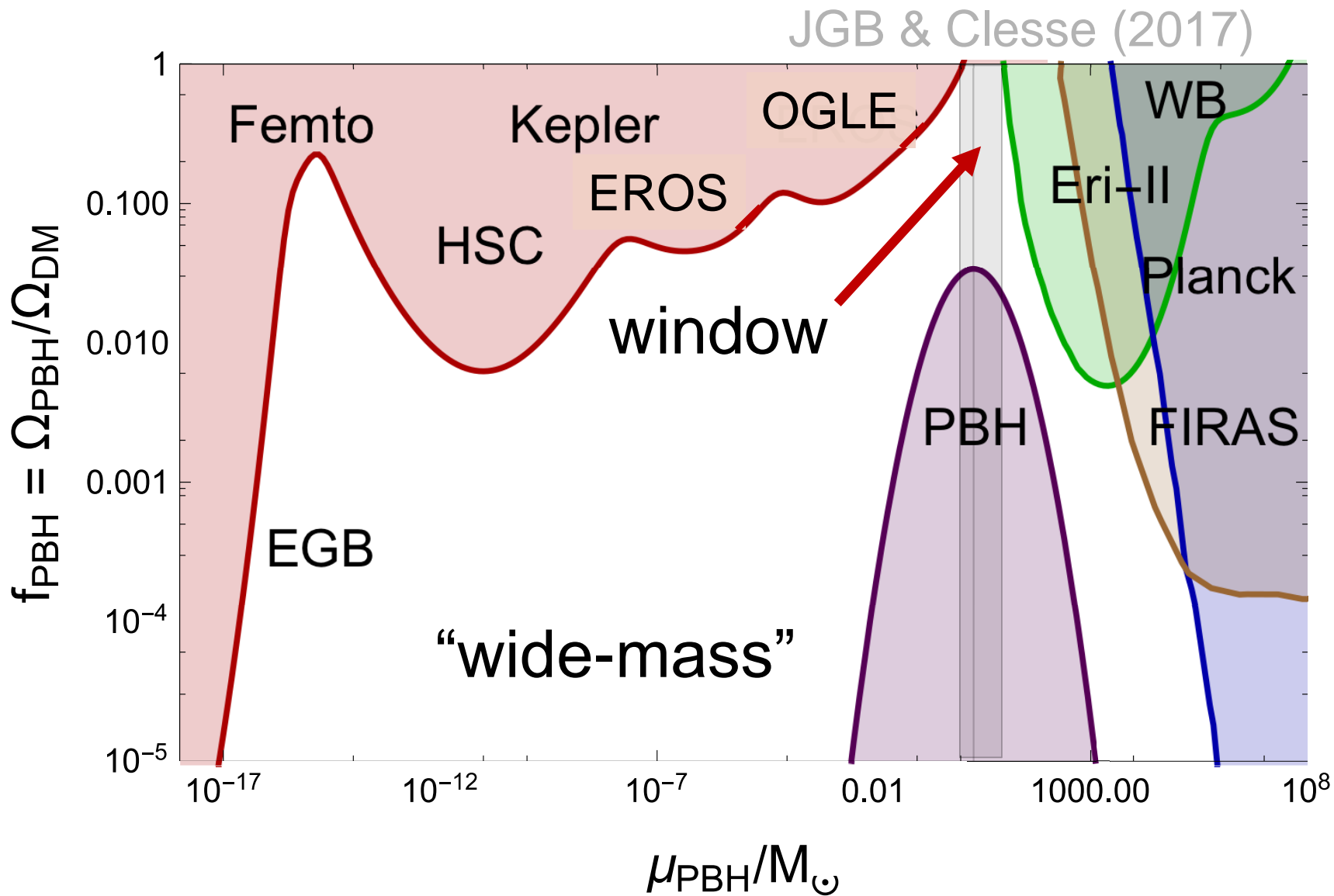
- From Quantum Fluctuations during inflation to PBH as all of DM
- Quantum diffusion  $\rightarrow$  NG tails  $\rightarrow$  PBH inevitable @ small scales
- Gravitational collapse during radiation era: Thermal History
- Origin of matter (baryons) and DM at QCD transition:  $\Omega_{\text{DM}} \sim 5\Omega_{\text{B}}$
- Multimodal mass distribution PBH:  $10^{-5}$ , 1, 50,  $10^5$  Msun
- PNG  $\rightarrow$  Clustered PBH:  $10^6$  Msun evades all “monochromatic”
- Seeds for Large Scale Structure: IMBH and SMBH
- Resolve Small Scale Structure CDM crisis: UFDG, core-cusp...
- Very rich phenomenology: wealth of observational signatures
- Gravitational Lensing probes: strong, weak, micro, etc.
- Gravitational Waves probe: mass, spin, merger rate, clustering
- CMB spectral distortions: mass range, clustering prop. PBH
- Galactic structures: UFDG, rot. curves, MBH(Mhalo), HVS-GAIA
- Bright future: G3 GWO ET & LISA, LSST, Pixie, Theia,

# PBH constraints

JGB & Clesse (2017)

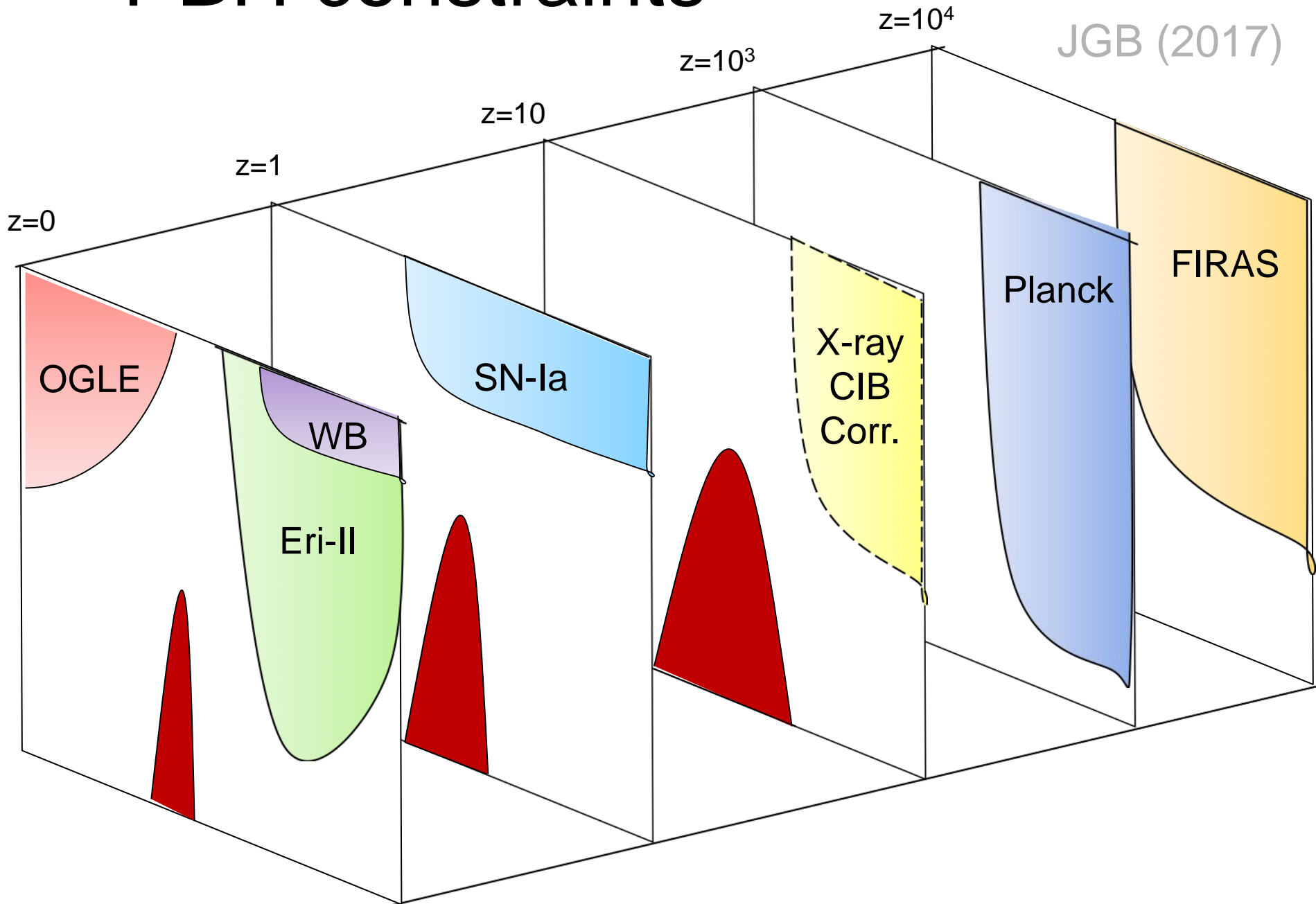


# PBH constraints





# PBH constraints





# Cosmic Conundra explained

Clesse, JGB (2017)

Carr, Clesse, JGB, Kühnel (2019)

- Planetary-mass microlensing
- Quasar microlensing
- OGLE/GAIA microlensing Gal. Bulge
- CIB/X-ray background
- UFDG substructure large M/L
- IMHB & SMBH seeds for LSS
- Mass, spin & merger rate LVC BBH

# Massive PBH = seeds of structure

- Massive primordial black holes with  $10^{-5} M_{\odot} < M_{\text{PBH}} < 10^6 M_{\odot}$ , which **cluster and merge** and could resolve some of the most acute problems of  $\Lambda$ CDM paradigm.
- $\Lambda$ CDM N-body simulations never reach the  $10^3 M_{\odot}$  particle resolution, so for them **PBH DM is as good as Particle DM.**
- PBH DM paradigm naturally incorporates all properties of collisionless CDM scenario on large scales but **differs on small scales.**

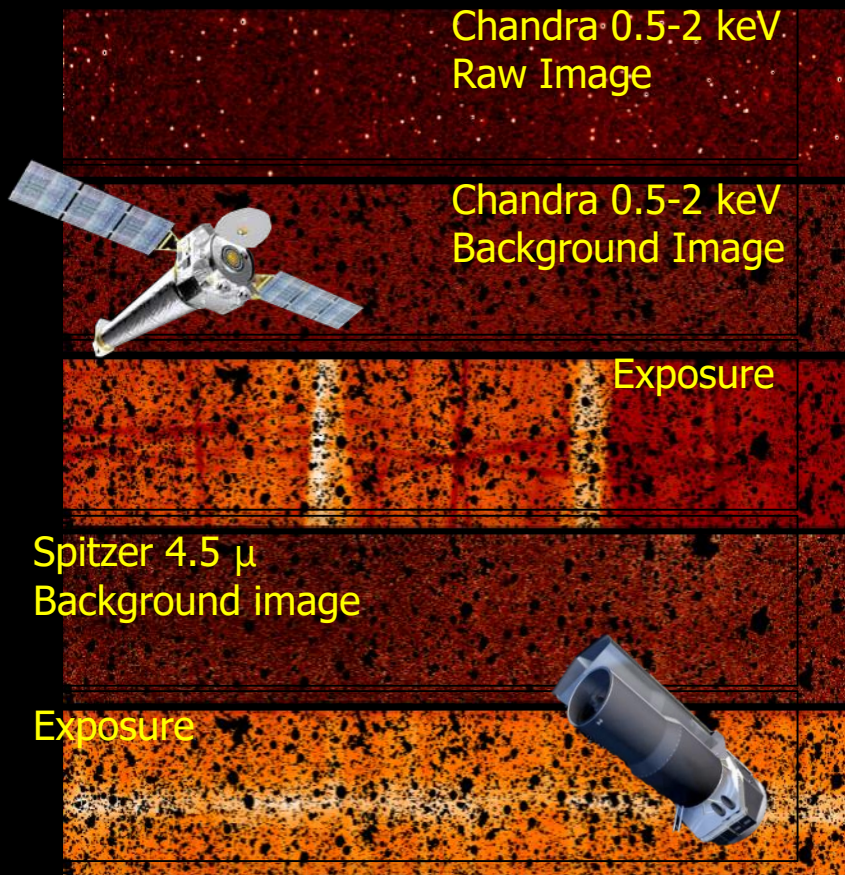
# CIB x CXB fluctuations indicate high-z BH population



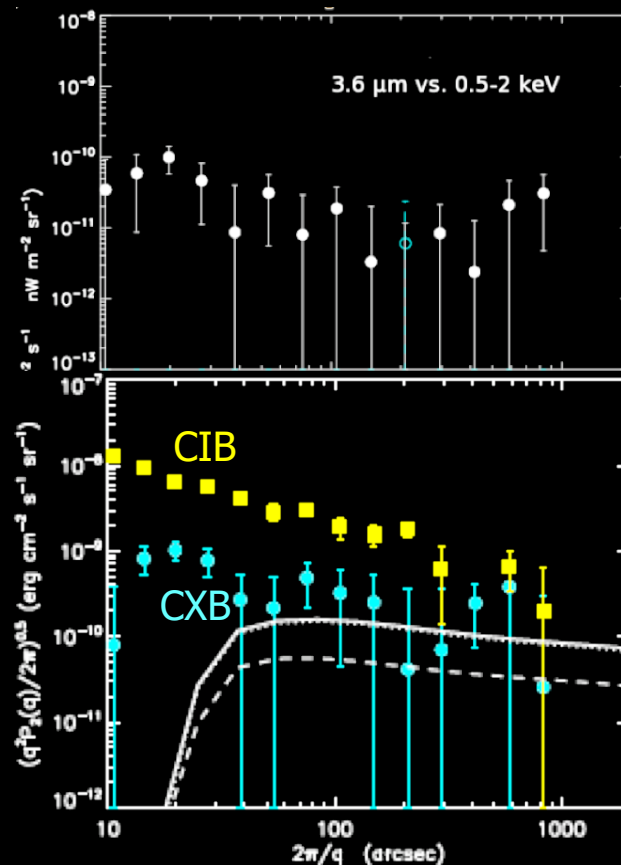
Hasinger (2021)

# Fingerprint of the first Black Holes?

Hasinger (2021)



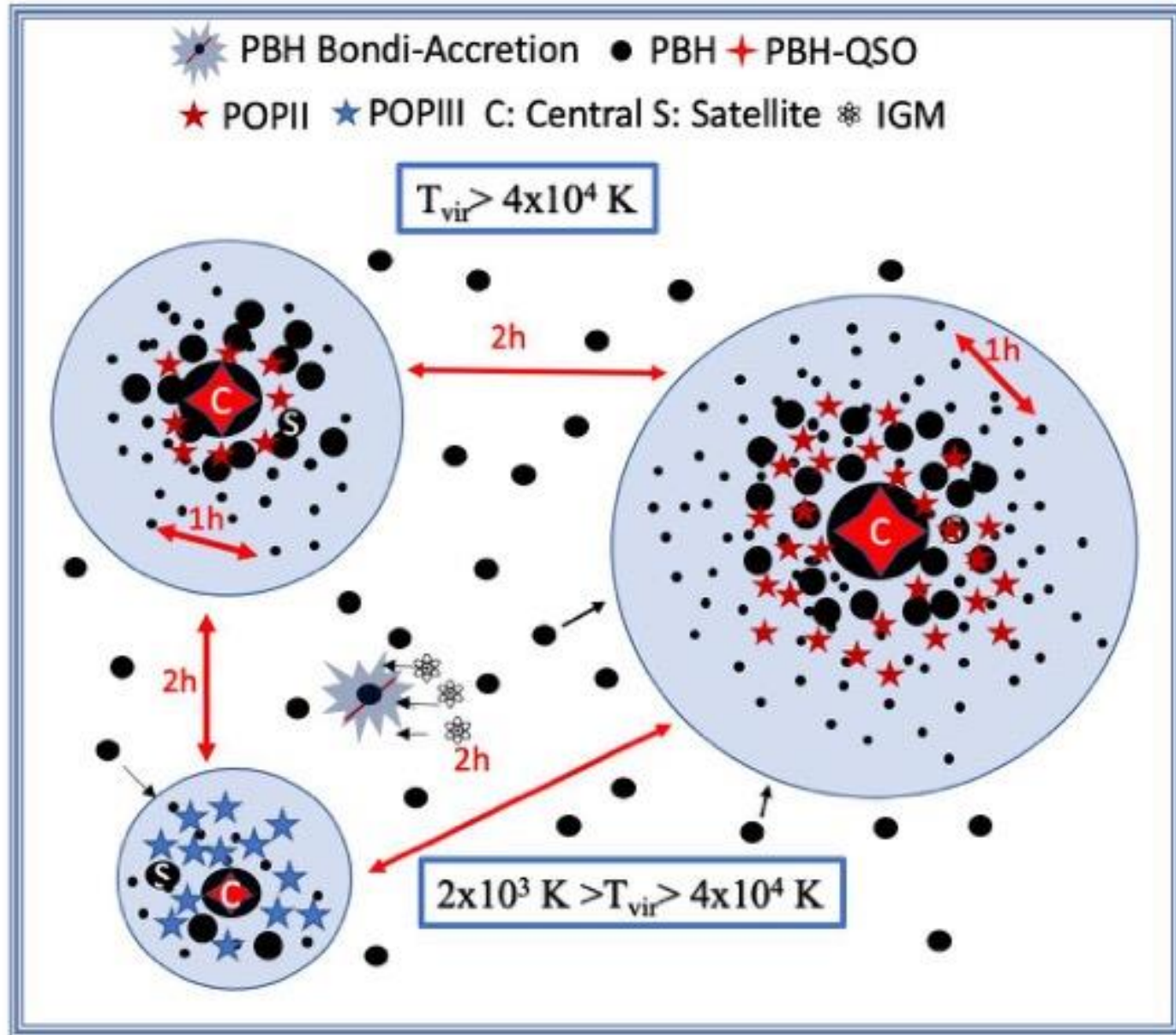
CIB x CXB Cross-Power



CAPPELLUTI+ 13, MITCHELL-WYNNE+ 16, YUE+ 13, PACUCCI+ 15, HELGASON+ 14

# Early Star Formation

Hasinger (2021)



Hasinger (2021)

