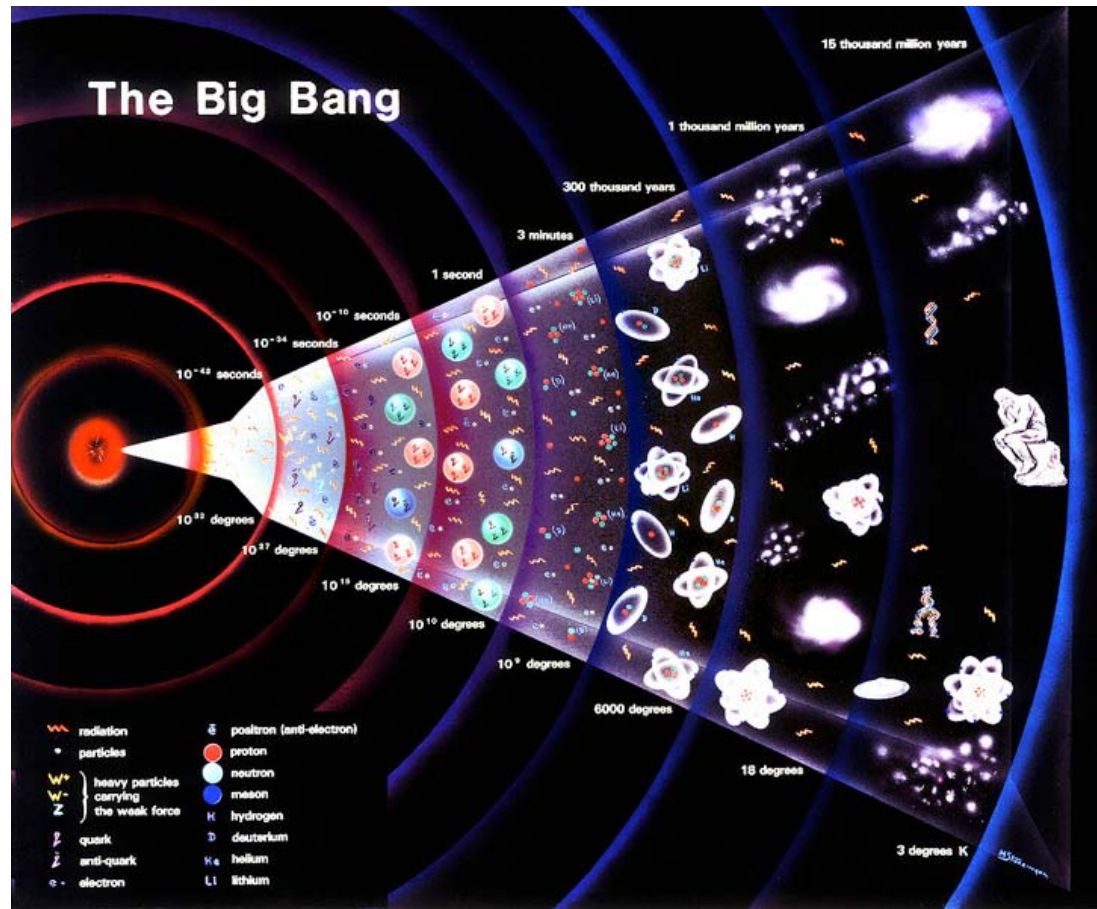


# Precision Electroweak Physics at CDF

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Duke University



Workshop on Precision LHC Physics  
Paris, December 16, 2010

# Precision Physics at CDF

- QCD and PDF-related measurements
  - $P_T$  spectrum of Z bosons
  - Measurement of angular decay distribution coefficients in W and Z boson decays to leptons
  - Charge asymmetry in W boson production and decay
  - Z boson rapidity spectrum
- Measurements related to electroweak sector
  - Top quark mass measurement
  - W boson mass measurement
  - W boson width measurement (analysis issues very similar to  $M_W$ )
  - Forward-backward asymmetry ( $A_{FB}$ ) in Z boson decays
    - On-peak and high-mass

# Decay Angular Coefficients in Z boson decay

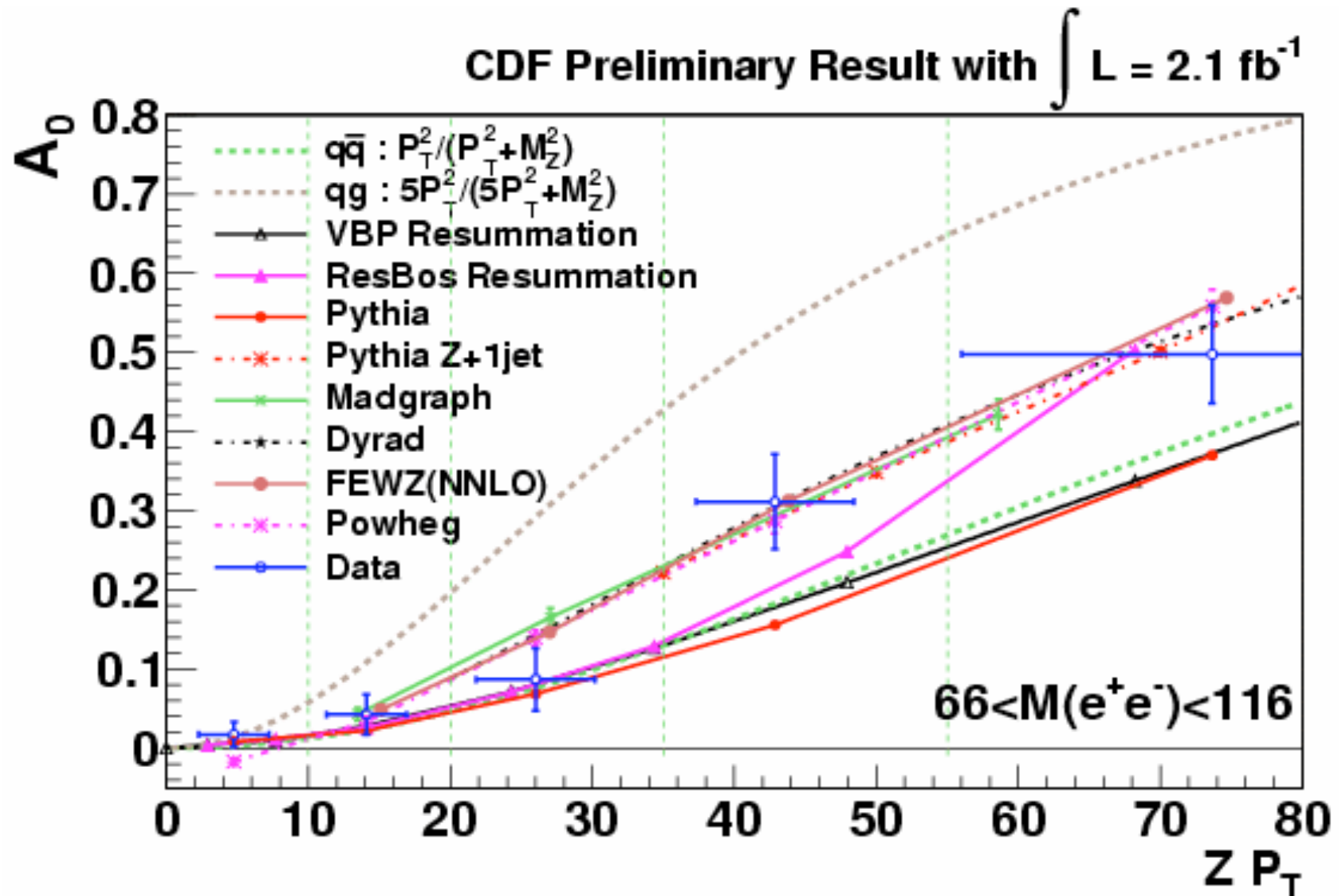
- Measurements using  $2.1 \text{ fb}^{-1}$

$$\begin{aligned} d\sigma/d \cos\theta d\varphi \propto & (1 + \cos^2\theta) + 0.5A_0(1 - 3 \cos^2\theta) + A_1 \sin 2\theta \cos \varphi \\ & + 0.5A_2 \sin^2\theta \cos 2\varphi + A_3 \sin\theta \cos \varphi + A_4 \cos \theta + A_5 \sin^2\theta \sin 2\varphi \\ & + A_6 \sin 2\theta \sin \varphi + A_7 \sin \theta \sin \varphi \end{aligned}$$

*Important to check theoretical calculations, which feed into other precision measurements (eg.  $M_W$  measurement in the case of W boson's decay angular coefficients)*

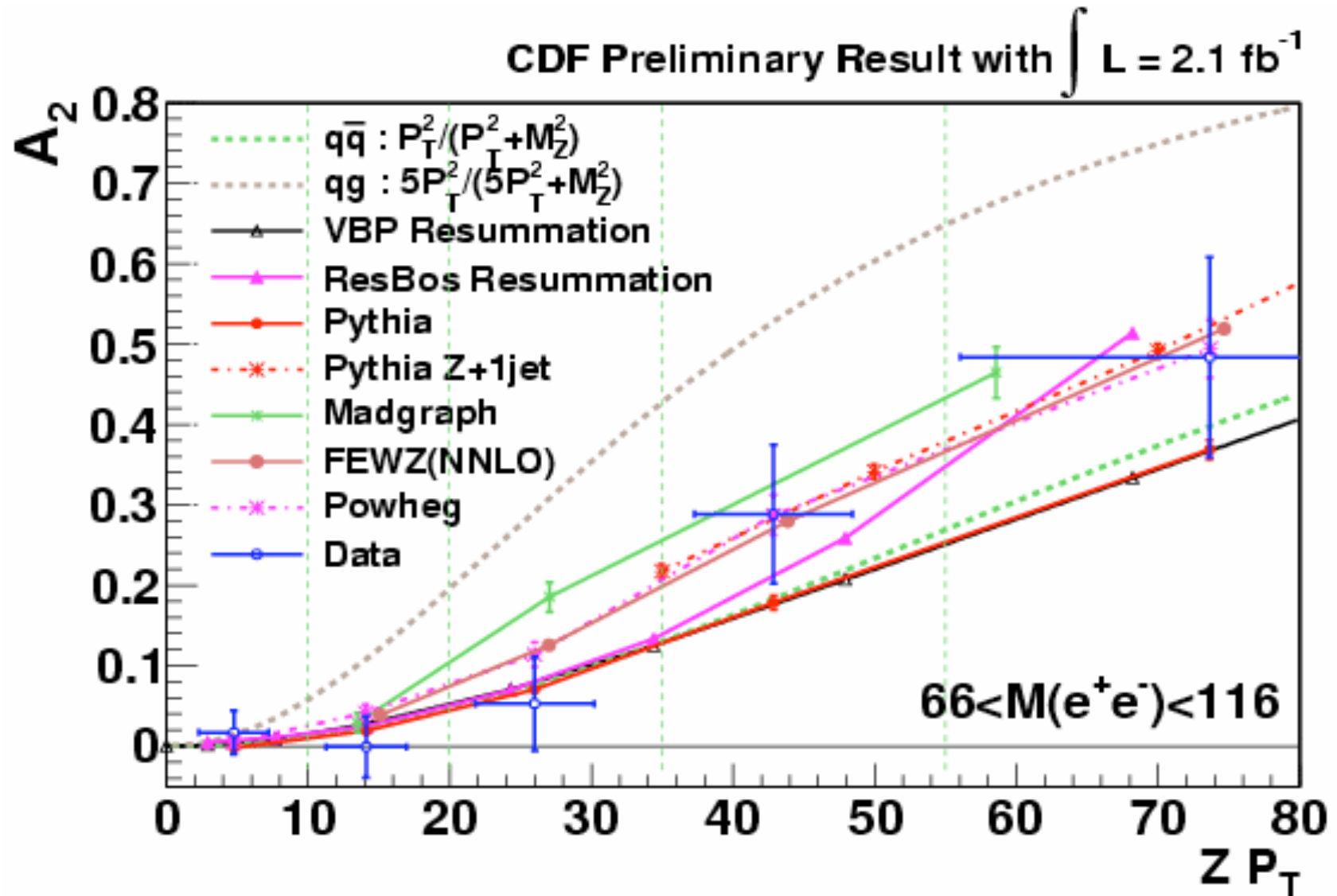
# Decay Angular Coefficients in Z boson decay

- Uncertainty dominated by statistical uncertainty



# Decay Angular Coefficients in Z boson decay

- Lam-Tung relation for spin-1 gluons:  $A_2 = A_0$  confirmed

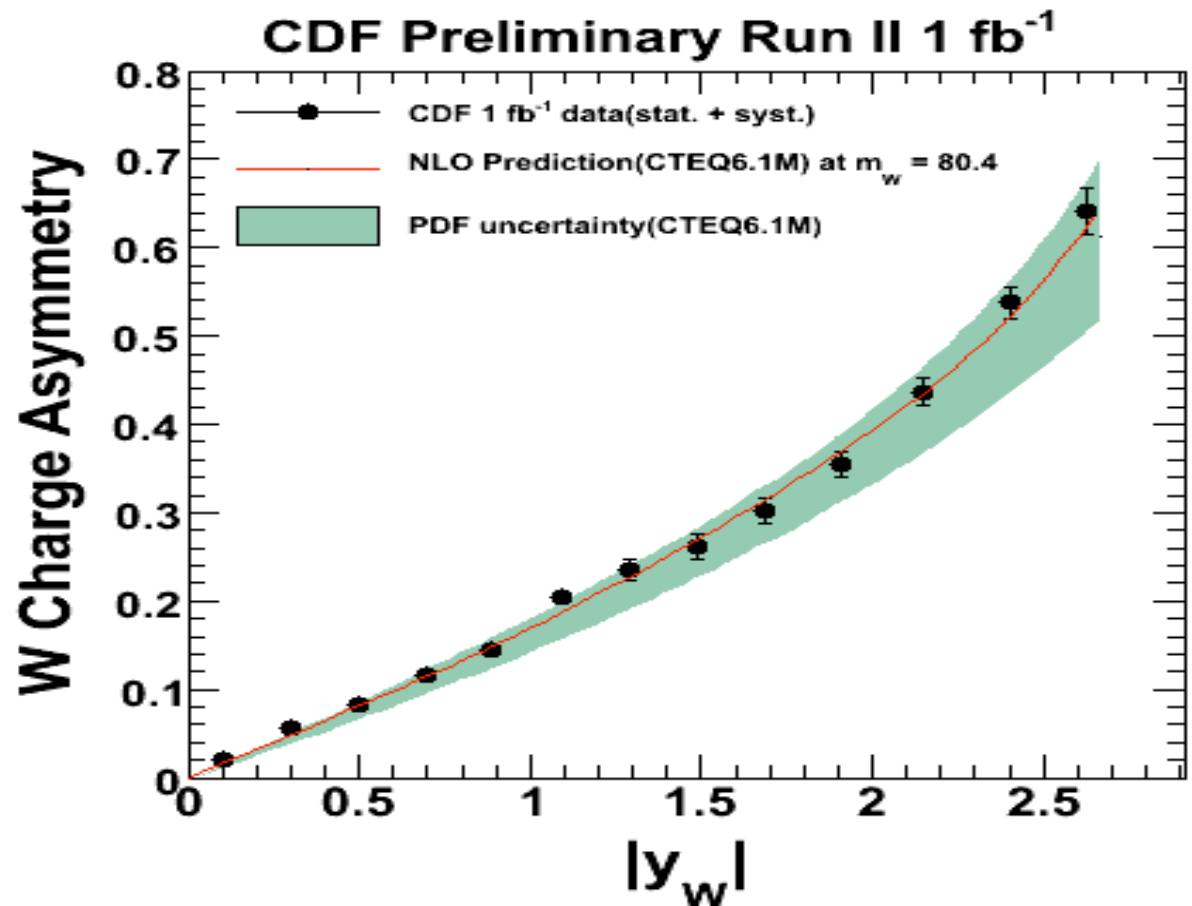


## W charge asymmetry vs W rapidity

- Traditionally, lepton charge asymmetry is measured; V-A decay of W boson dilutes the observed lepton asymmetry
- CDF has also used  $p_T(W)$  measured in the event, and  $M_W$  to measure asymmetry vs boson rapidity directly
- Removes V-A dilution

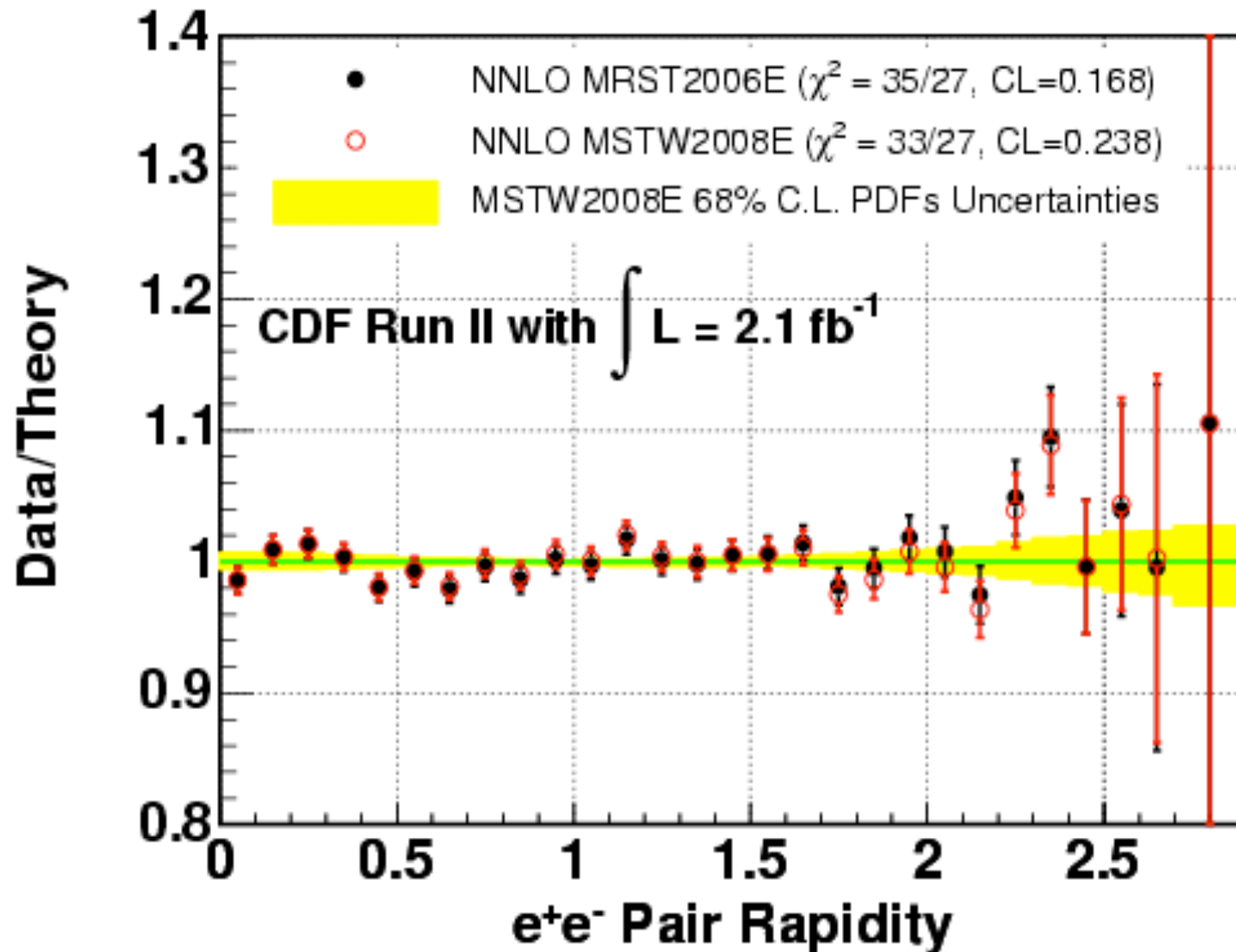
At the expense of small additional systematics due to recoil

- At Tevatron, very powerful in constraining relevant PDFs



# Rapidity distribution of Drell-Yan

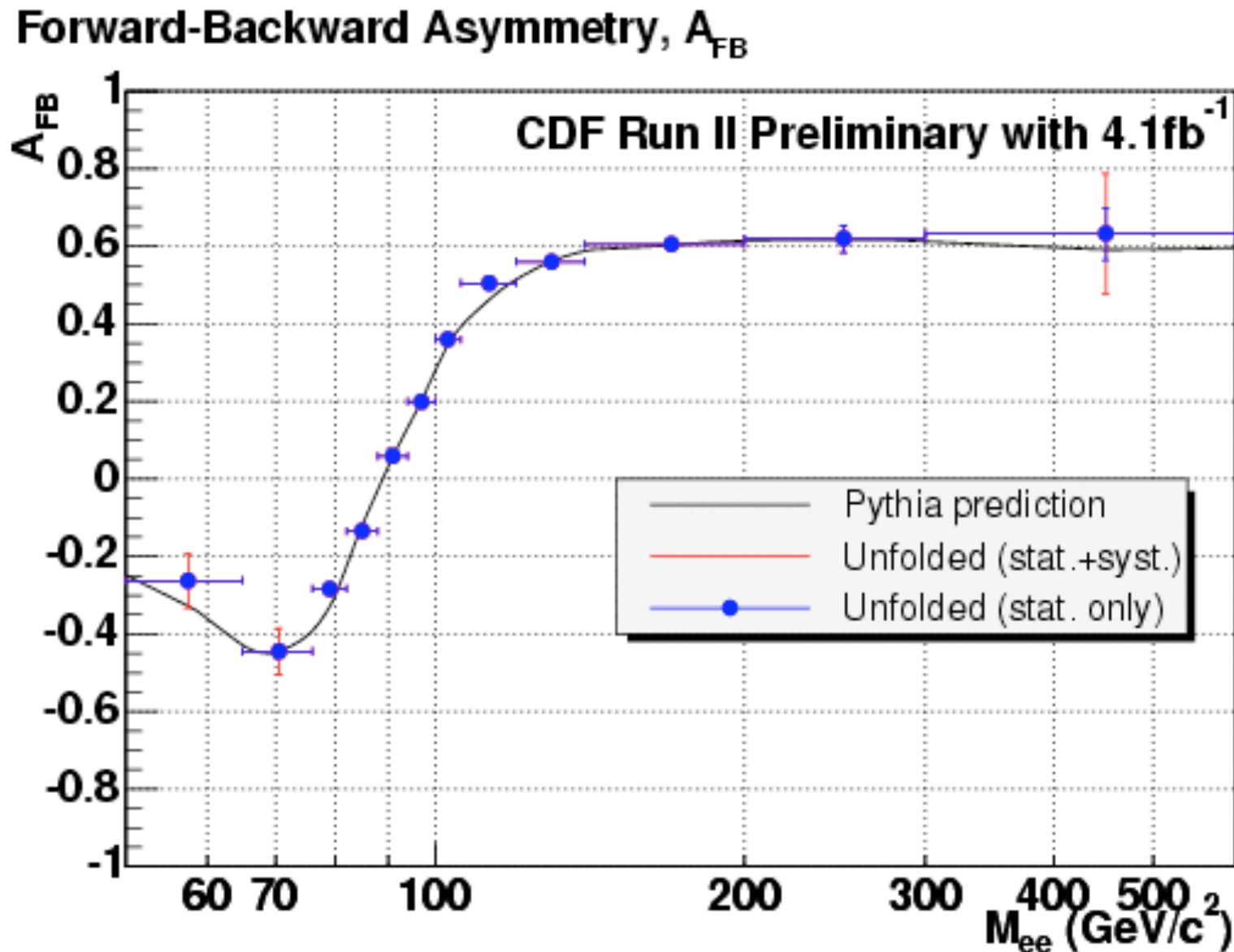
- Powerful (and independent of W charge asymmetry) constraint on PDFs





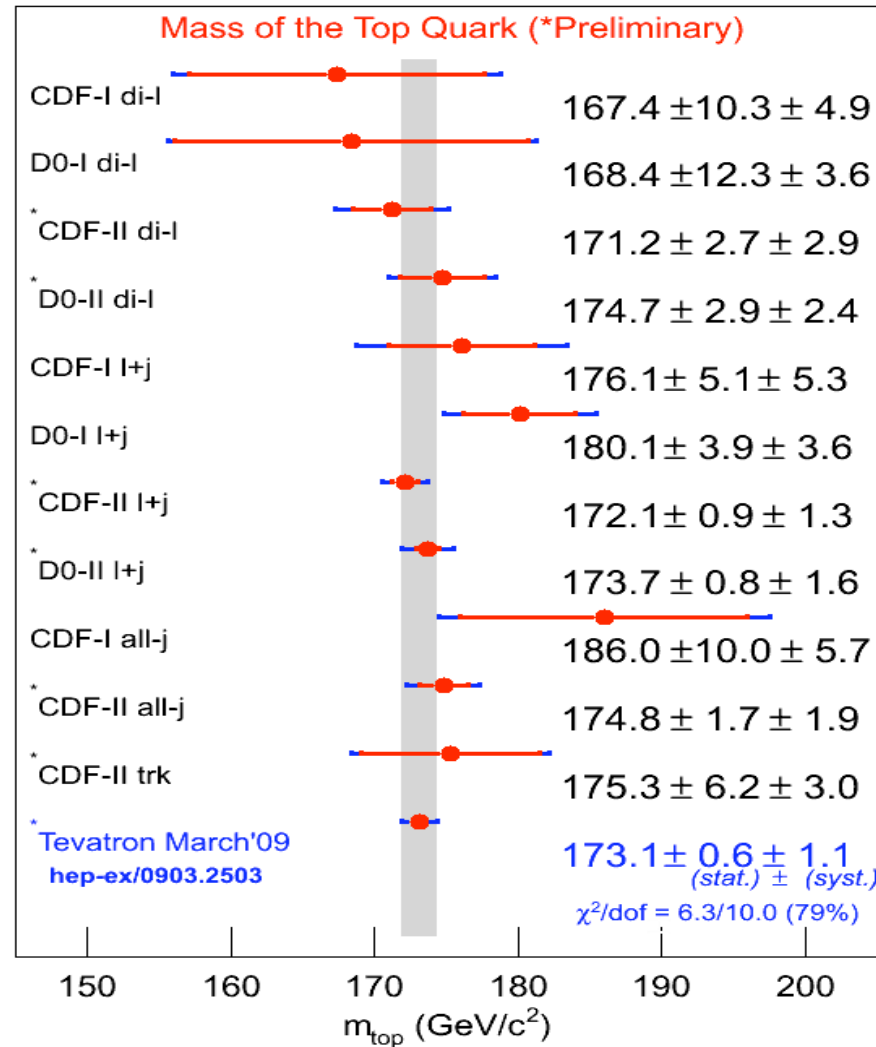
# Forward-backward Asymmetry in Drell-Yan

- Z-pole not yet competitive with LEP/SLD, but measurement at high mass is sensitive to new physics (eg,  $Z'$ ) via interference





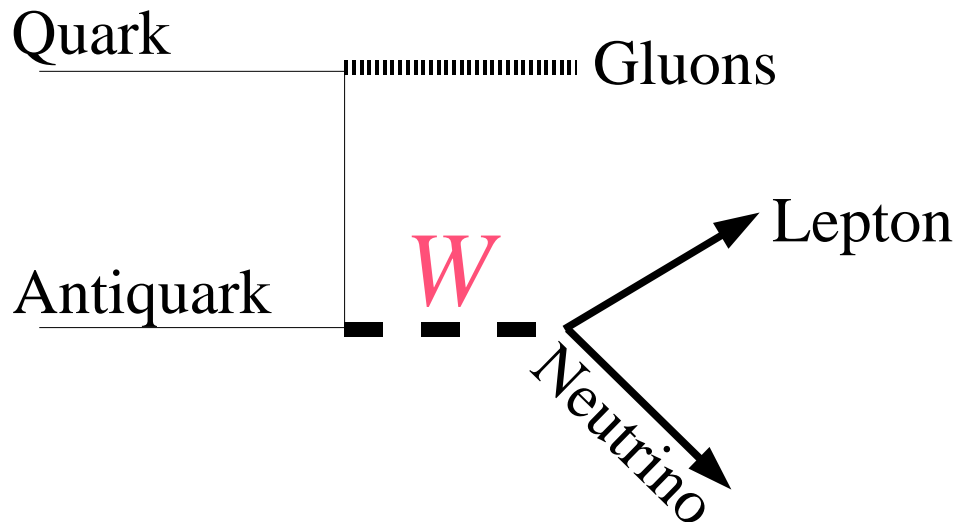
# Progress on $M_{\text{top}}$ at the Tevatron



- From the Tevatron,  $\delta M_{\text{top}} = 1.3 \text{ GeV} \Rightarrow \delta M_{\text{H}} / M_{\text{H}} = 11\%$
- equivalent  $\delta M_{\text{W}} = 8 \text{ MeV}$  for the same Higgs mass constraint
- Current world average  $\delta M_{\text{W}} = 23 \text{ MeV}$ 
  - progress on  $\delta M_{\text{W}}$  now has the biggest impact on Higgs constraint!

# W Mass Analysis Strategy

# W Boson Production at the Tevatron

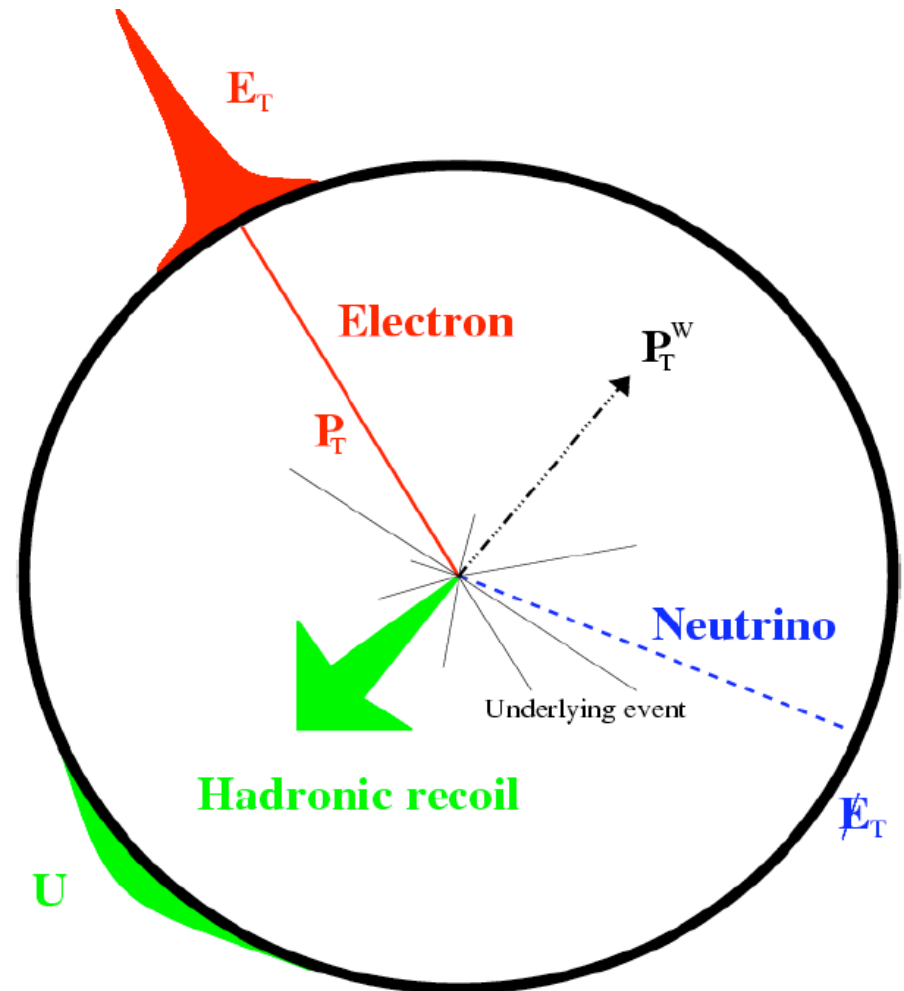


Quark-antiquark annihilation dominates (80%)

Lepton  $p_T$  carries most of  $W$  mass information, can be measured precisely (achieved 0.03%, aiming for 0.01%)

Initial state QCD radiation is  $O(10 \text{ GeV})$ , measure as soft 'hadronic recoil' in calorimeter (calibrated to  $\sim 1\%$ , aiming for 0.05%)

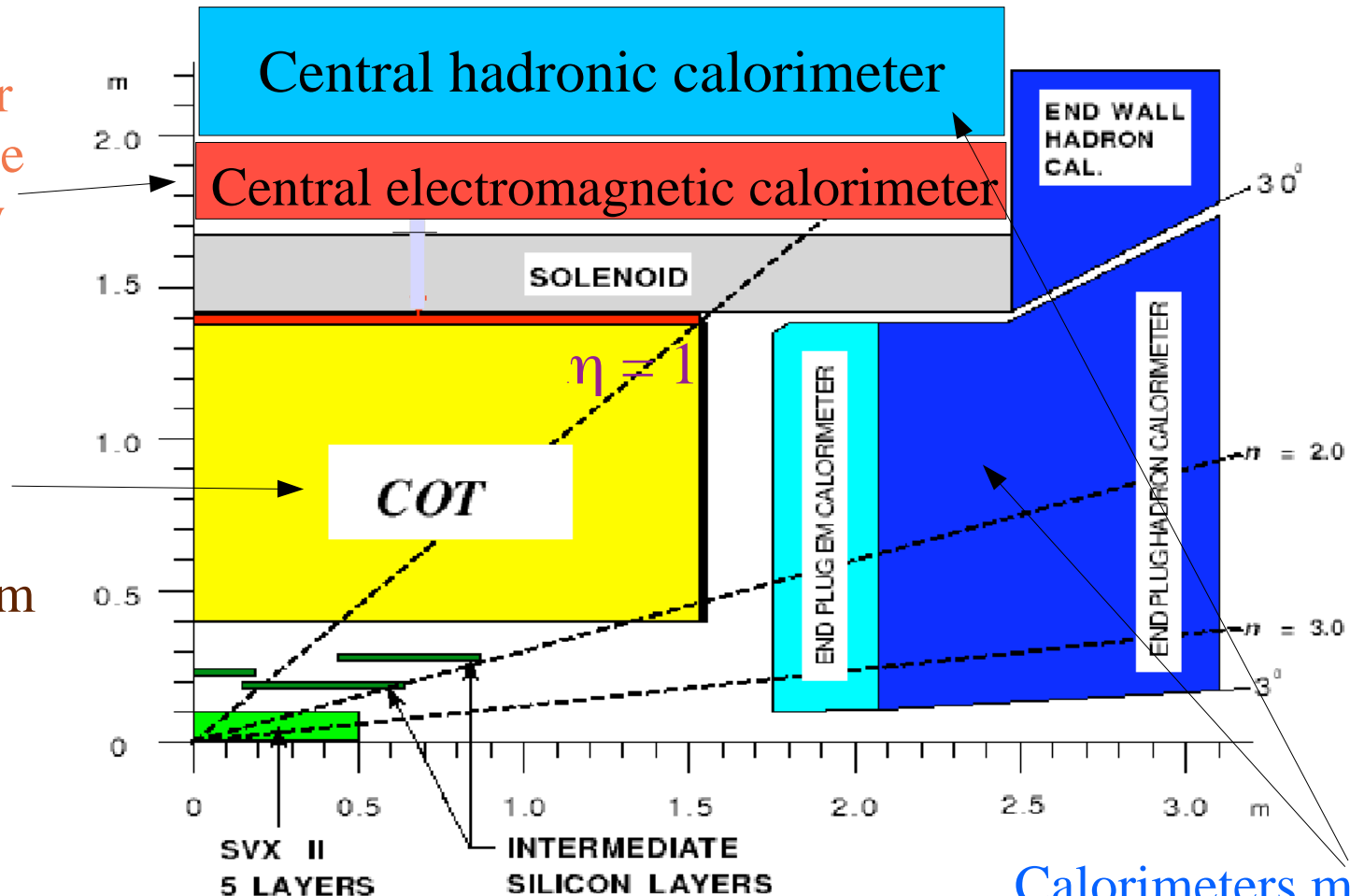
Pollutes  $W$  mass information, fortunately  $p_T(W) \ll M_W$



# Quadrant of Collider Detector at Fermilab (CDF)

EM calorimeter  
provides precise  
electron energy  
measurement

drift chamber  
provides  
precise lepton  
track momentum  
measurement

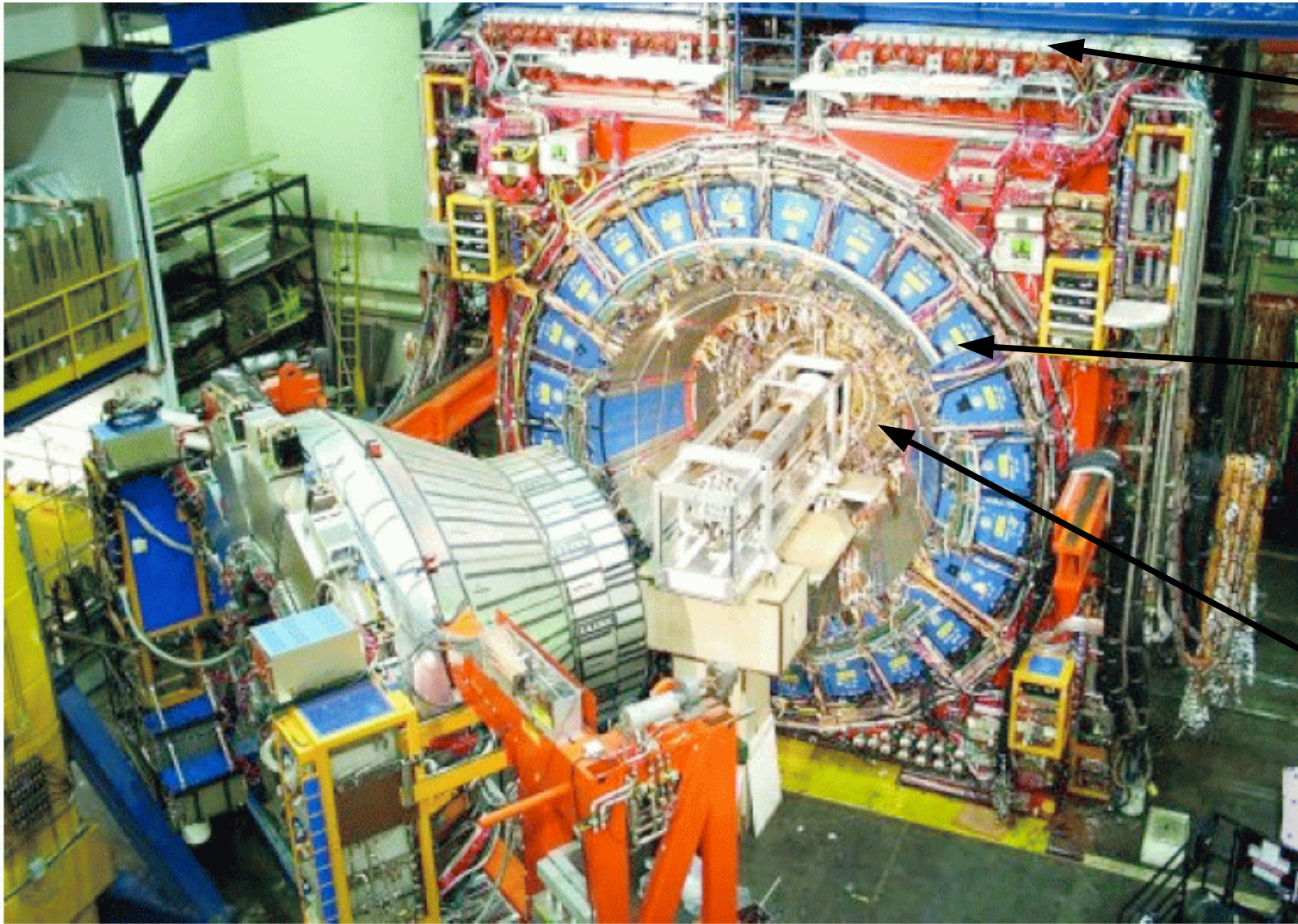


Calorimeters measure  
hadronic recoil particles

Select W and Z bosons with central ( $|\eta| < 1$ ) leptons



# Collider Detector at Fermilab (CDF)



Muon  
detector

Central  
hadronic  
calorimeter

Central  
outer  
tracker  
(COT)

# CDF W & Z Data Samples

- W, Z, J/ψ and Upsilon decays triggered in the dilepton channel
- Analysis of 2.3 fb<sup>-1</sup> data in progress
- CDF's analysis published in 2007, based on integrated luminosity (collected between February 2002 – September 2003):
  - Electron channel:  $\mathcal{L} = 218 \text{ pb}^{-1}$
  - Muon channel:  $\mathcal{L} = 191 \text{ pb}^{-1}$
- Event selection gives fairly clean samples
  - W boson samples' mis-identification backgrounds ~ 0.5%

Sample	Candidates
$W \rightarrow e\nu$	63964
$W \rightarrow \mu\nu$	51128
$Z \rightarrow e^+e^-$	2919
$Z \rightarrow \mu^+\mu^-$	4960

# Founding Principle of CDF Analysis

*Energy scale measurements drive the  $W$  mass measurement*

- Develop an energy calibration procedure based on fundamental principles
  - Push the “first-principles” philosophy as far as it will go
- Measure the  $Z$  boson mass in three different ways
  - Dimuon mass using tracks
  - Dielectron mass using tracks
  - Dielectron mass using calorimeter cluster energies
- Consistency of these three  $Z$  boson mass measurements with LEP measurement (within quoted uncertainties) provides very strong validation of the fundamental understanding of the physics and detector model used for  $M_W$  measurement
  - Huge effort at CDF invested in demonstrating this validation, in order to build maximum confidence in  $M_W$  measurement
  - We believe this investment is needed to trust ultimate precision of 5-10 MeV on  $M_W$  at any hadron collider



# Outline of CDF Analysis

*Energy scale measurements drive the  $W$  mass measurement*

- Tracker Calibration

- alignment of the central drift chamber (COT with  $\sim 2400$  cells) using cosmic rays
- COT momentum scale and tracker non-linearity constrained using  $J/\psi \rightarrow \mu\mu$  and  $\Upsilon \rightarrow \mu\mu$  mass fits
  - Confirmed using  $Z \rightarrow \mu\mu$  mass fit and  $Z \rightarrow ee$  mass fit using tracks

- EM Calorimeter Calibration

- COT momentum scale transferred to EM calorimeter using a fit to the peak of the  $E/p$  spectrum, around  $E/p \sim 1$  (an *in-situ* test beam)
- Calorimeter energy scale confirmed using  $Z \rightarrow ee$  mass fit

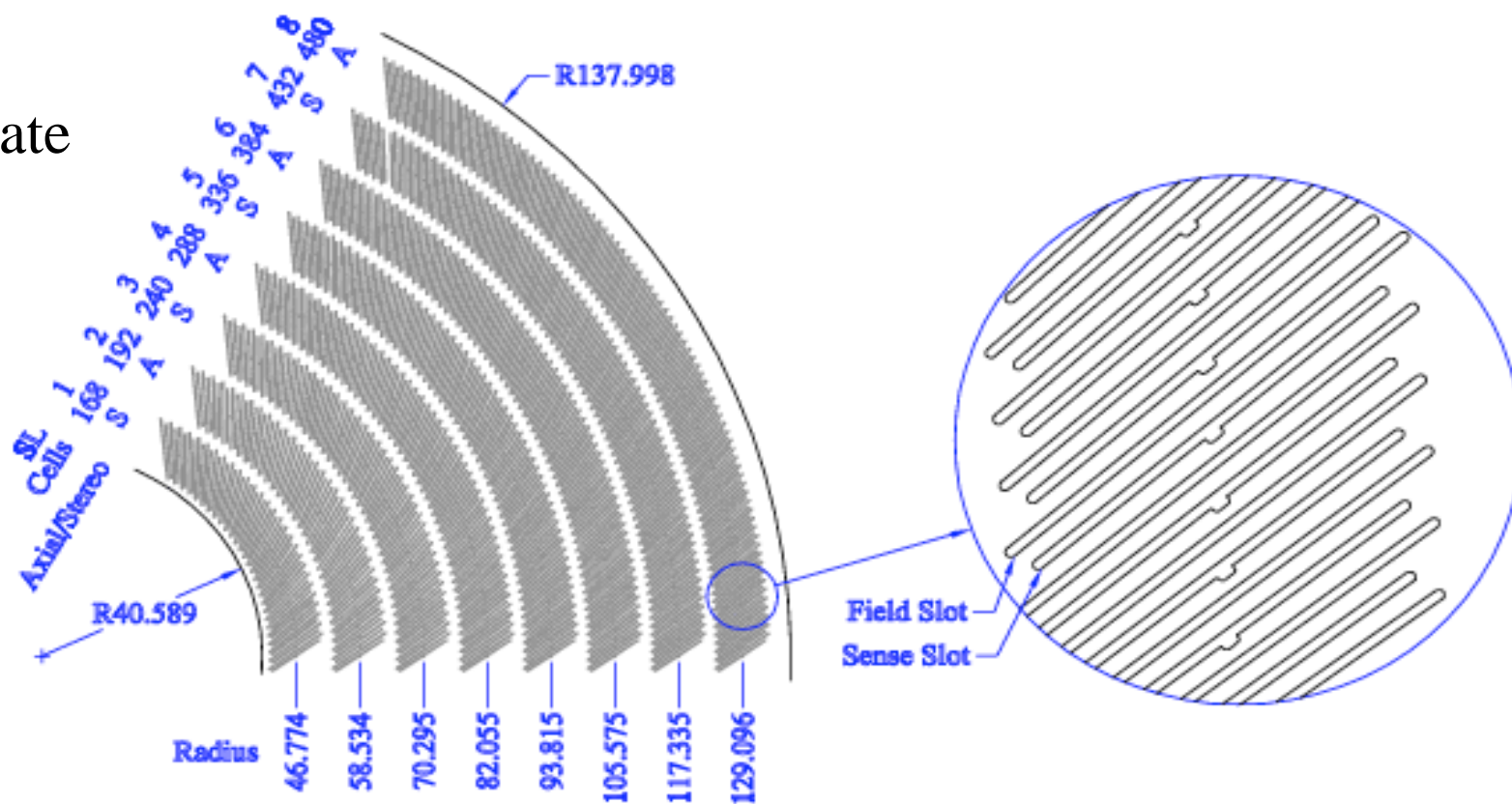
- Tracker and EM Calorimeter resolutions

- Hadronic recoil modelling

- Characterized using  $p_T$ -balance in  $Z \rightarrow ll$  events

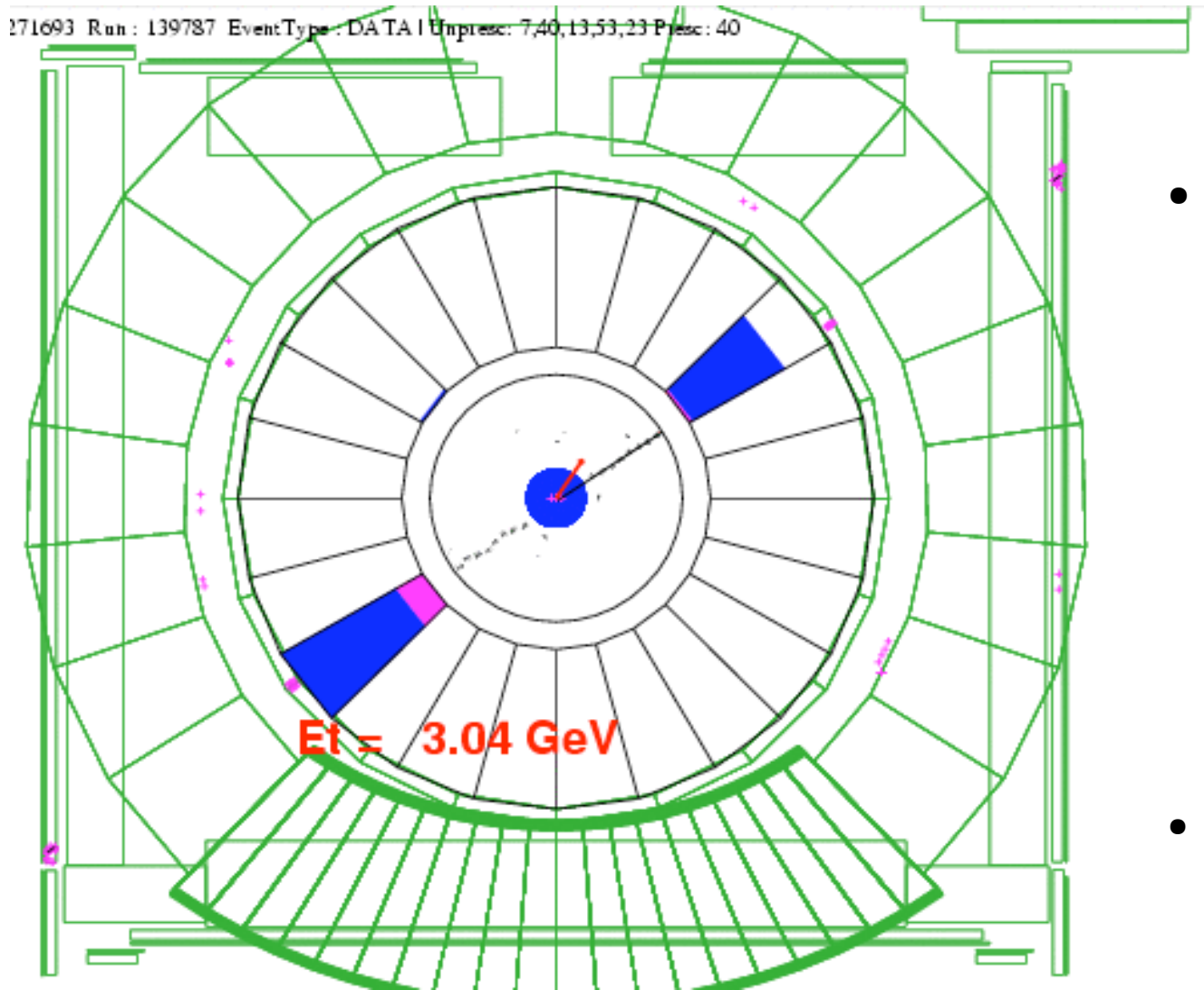
# Drift Chamber (COT) Alignment

COT endplate geometry



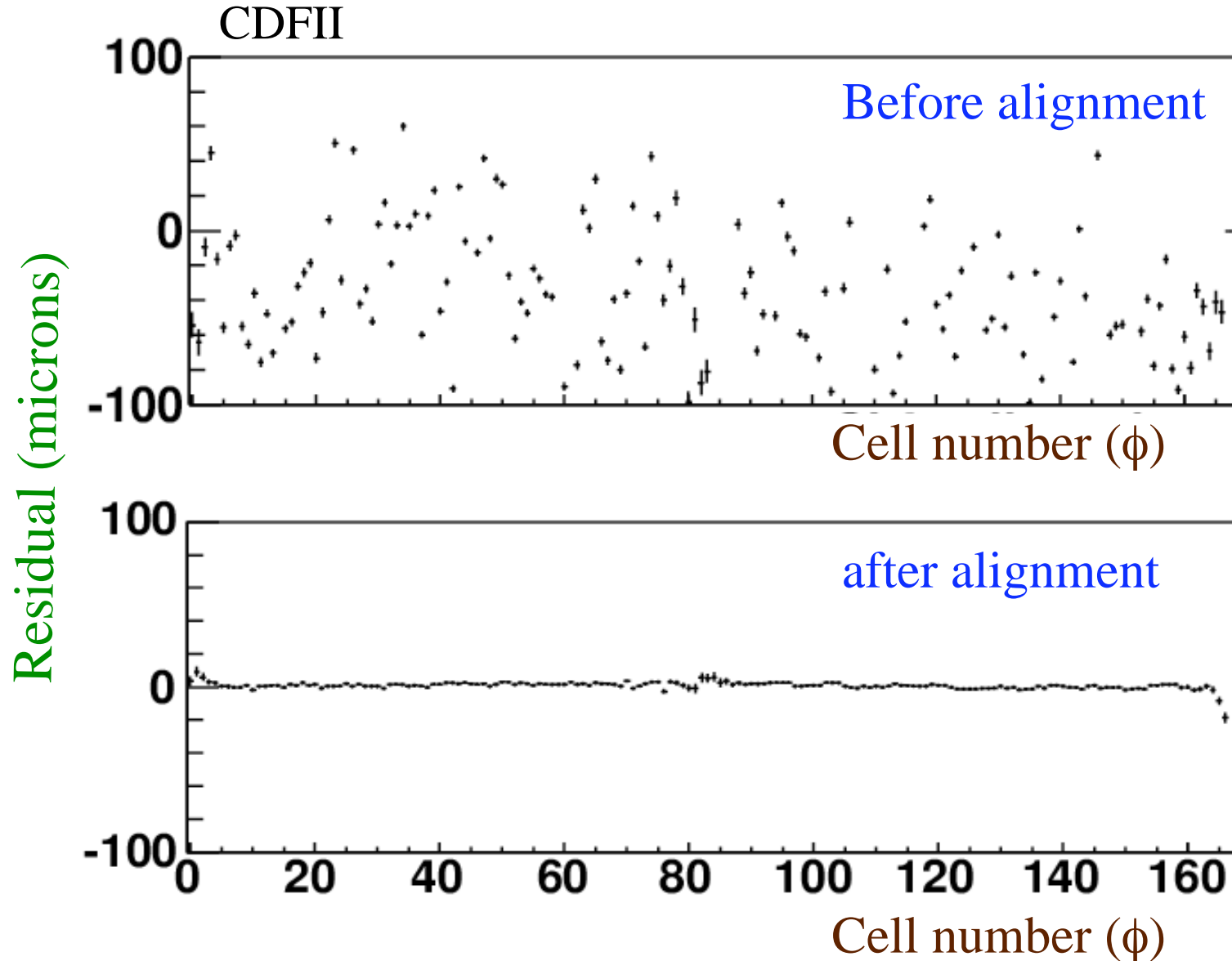
# Internal Alignment of COT

- Use a clean sample of  $\sim 200k$  cosmic rays for cell-by-cell internal alignment



- Fit COT hits on both sides simultaneously to a single helix  
(A Kotwal, H. Gerberich and C. Hays, NIM A 506, 110 (2003))
  - Time of incidence is a floated parameter
- Same technique being used on ATLAS and CMS

## Residuals of COT cells after alignment



Final relative alignment of cells  $\sim 5 \mu\text{m}$  (initial alignment  $\sim 50 \mu\text{m}$ )

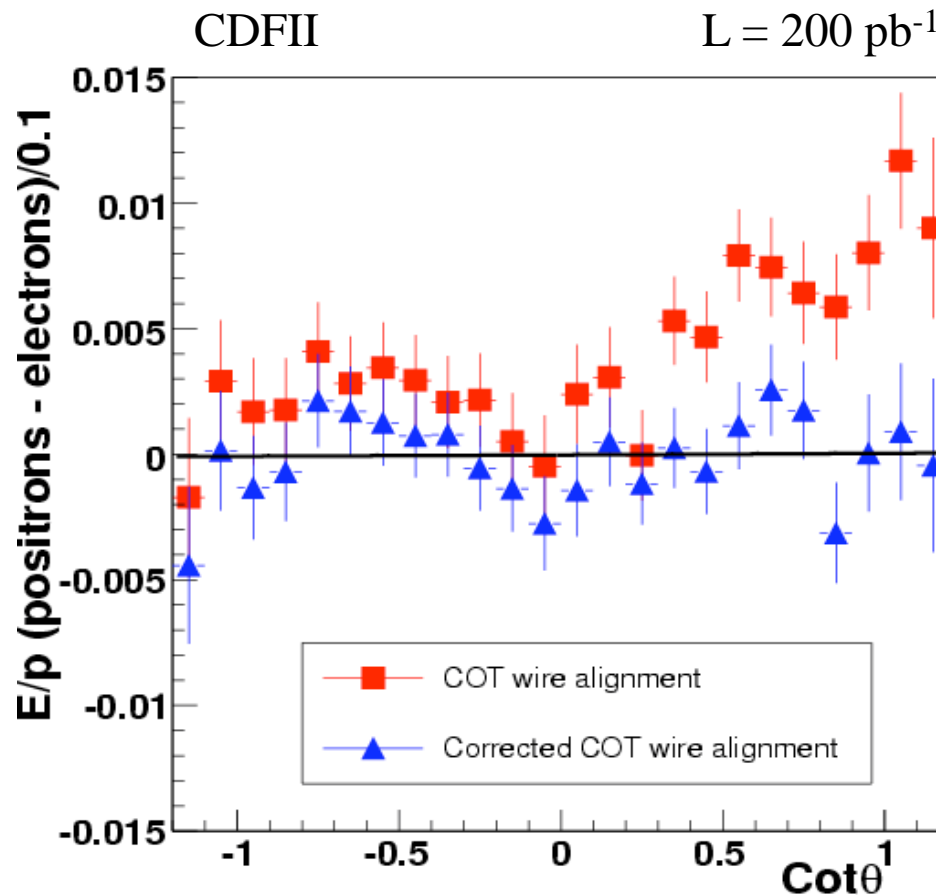
Many additional constraints on global deformations of tracking chamber

# Constraints on Global Deformations of Drift Chamber

- Alignment based on Cosmic Rays provides powerful constraints on
  - Curl (coaxial rotations at different radii)
  - Twist (relative rotation of two end-plates)
  - Telescoping (relative longitudinal movements at different radii)
  - Gravitational sag of drift chamber wires
  - Electrostatic deflections of drift chamber wires
- We obtain substantial control on the fundamental degrees of freedom of the drift chamber misalignment

# Cross-check of COT alignment

- Final cross-check and correction to track curvature based on difference of  $\langle E/p \rangle$  for positrons vs electrons (red points)
- Smooth ad-hoc curvature corrections applied  $\Rightarrow \delta M_W = 6 \text{ MeV}$
- Systematic effects also relevant for LHC trackers

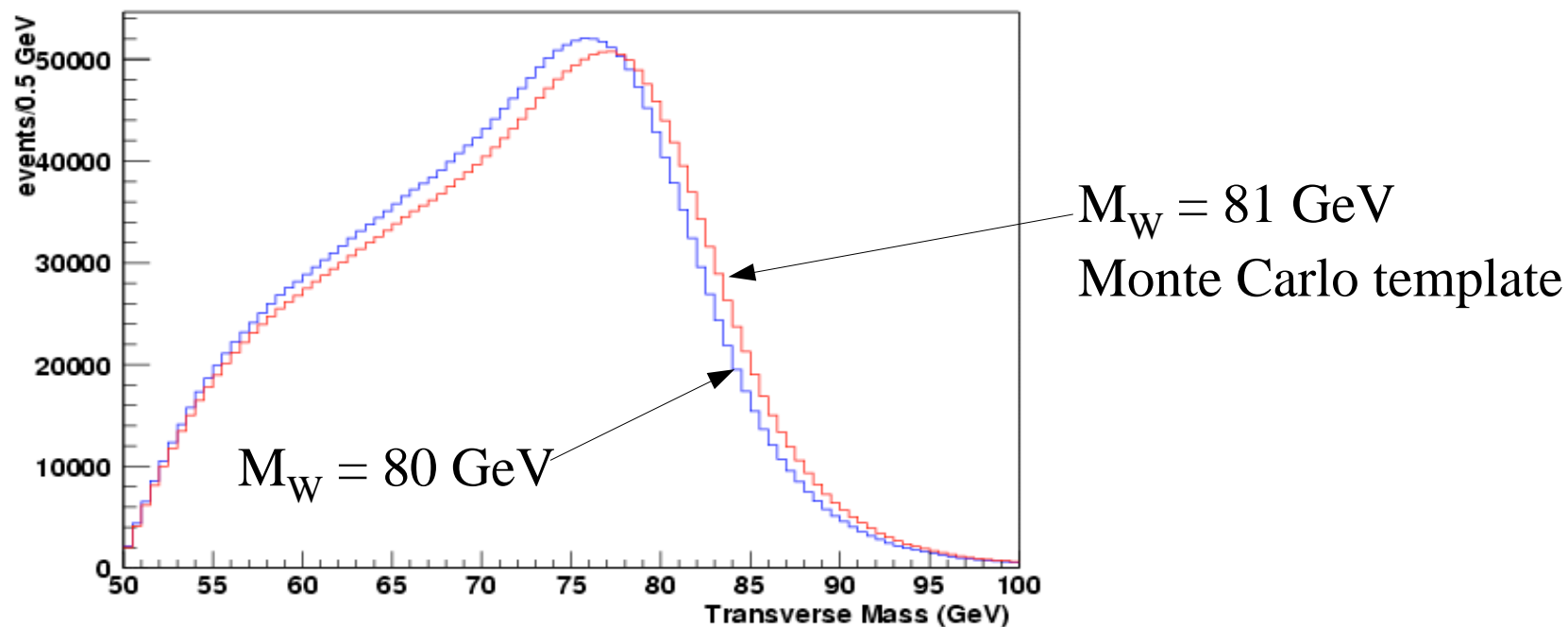


# Signal Simulation and Fitting



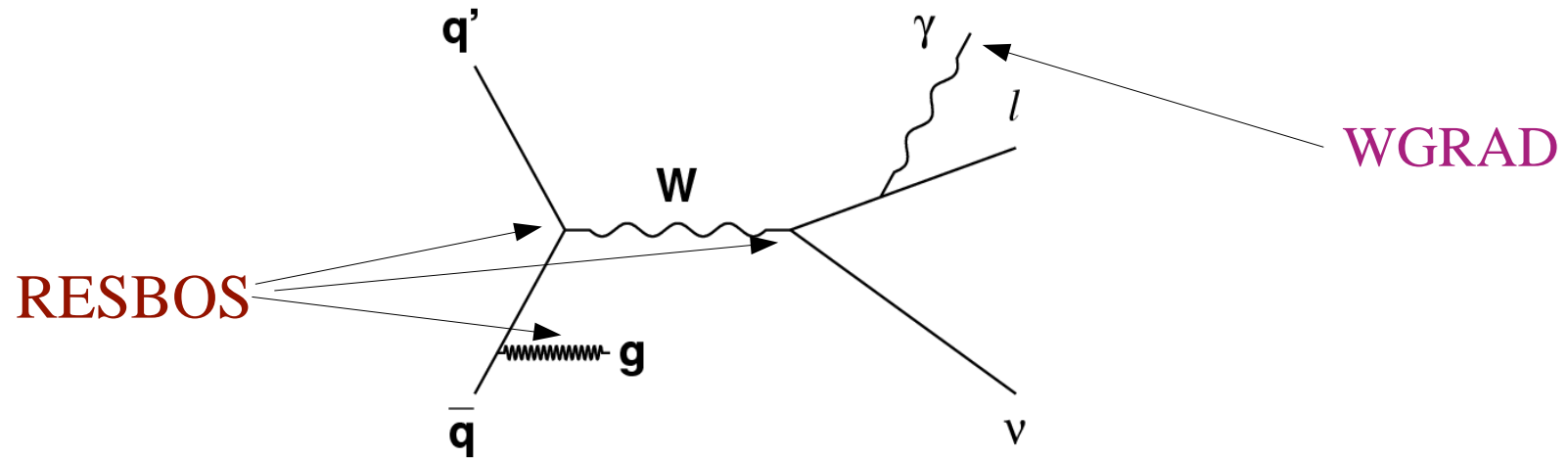
# Signal Simulation and Template Fitting

- All signals simulated using a custom Monte Carlo
  - Generate finely-spaced templates as a function of the fit variable
  - perform binned maximum-likelihood fits to the data
- Custom fast Monte Carlo makes smooth, high statistics templates
  - And provides analysis control over fundamental physics inputs



- CDF (and D0) extract the W mass from three kinematic distributions: Transverse mass, charged lepton  $p_T$  and neutrino  $p_T$ : different recoil systematics

# Generator-level Signal Simulation

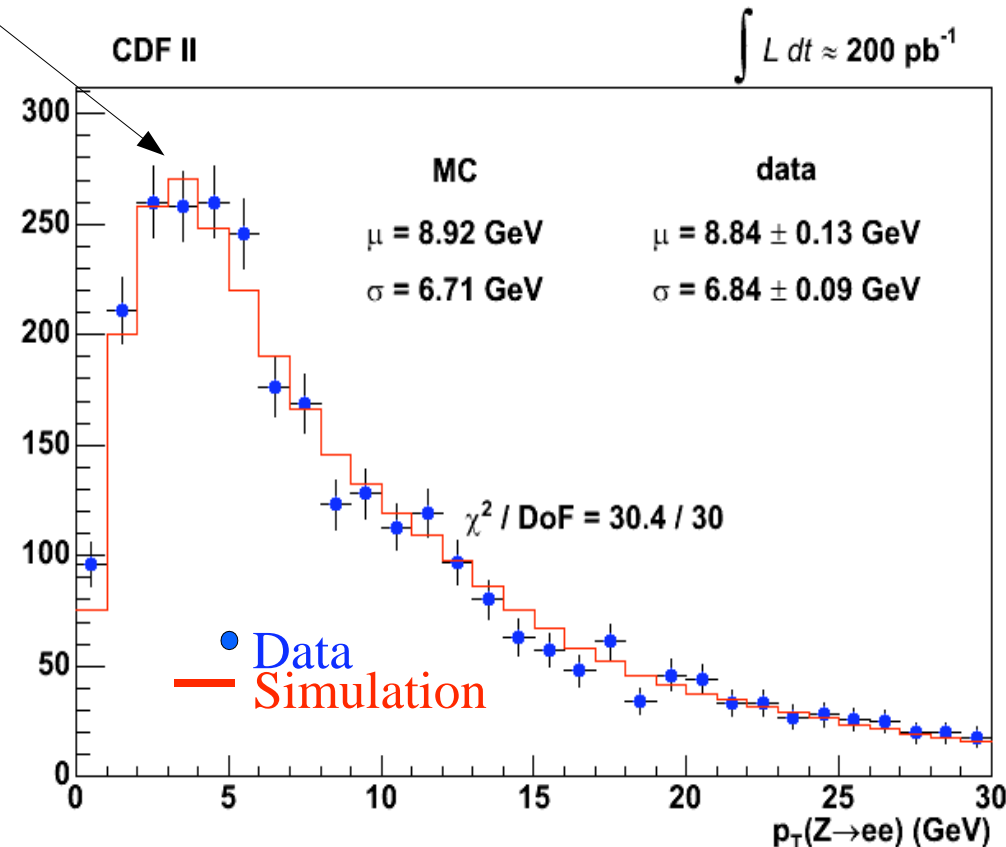
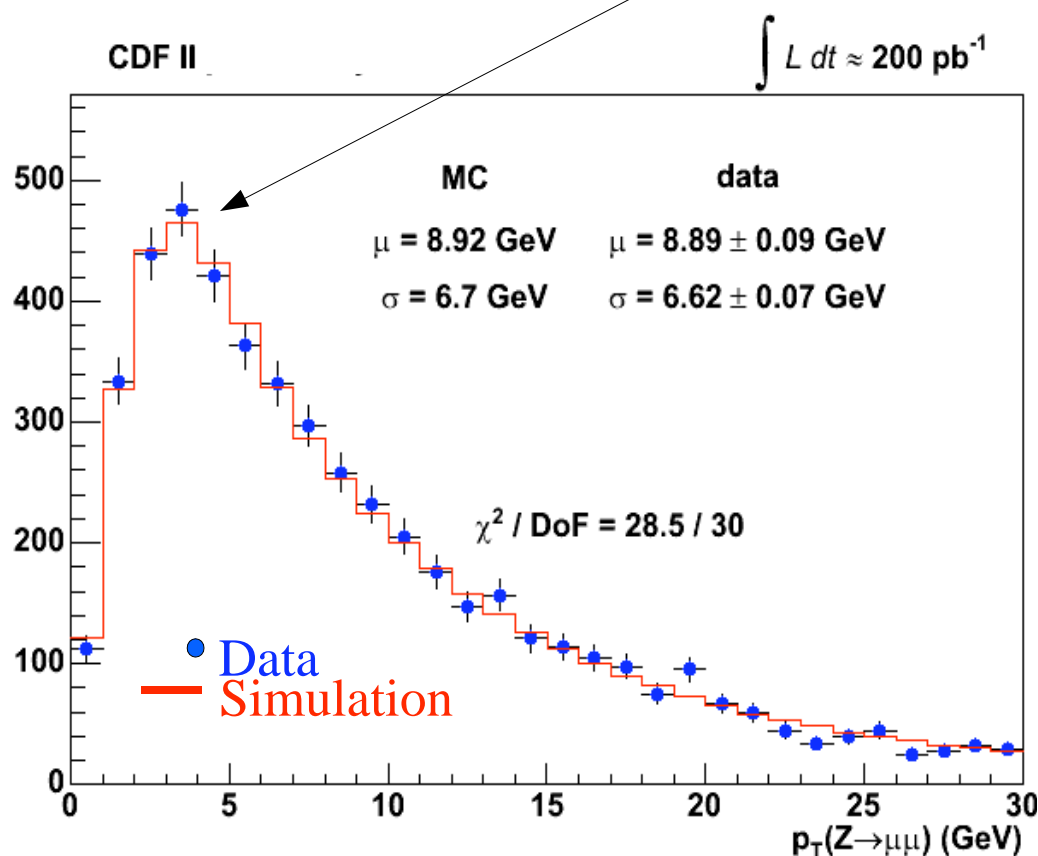


- Generator-level input for  $W$  &  $Z$  simulation provided by **RESBOS** (C. Balazs & C.-P. Yuan, PRD56, 5558 (1997) and references therein), which
  - Calculates triple-differential production cross section, and  $p_T$ -dependent double-differential decay angular distribution
  - calculates boson  $p_T$  spectrum reliably over the relevant  $p_T$  range: includes tunable parameters in the non-perturbative regime at low  $p_T$
- Radiative photons generated according to energy vs angle lookup table from **WGRAD** (U. Baur, S. Keller & D. Wackeroth, PRD59, 013002 (1998))

# Constraining Boson $p_T$ Spectrum

- Fit the non-perturbative parameter  $g_2$  in RESBOS to  $p_T(l\bar{l})$  spectra:  
find  $g_2 = 0.685 \pm 0.048$   $\Delta M_W = 3 \text{ MeV}$ 
  - Consistent with global fits (Landry *et al*, PRD67, 073016 (2003))
- Negligible effect of second non-perturbative parameter  $g_3$

Position of peak in boson  $p_T$  spectrum depends on  $g_2$

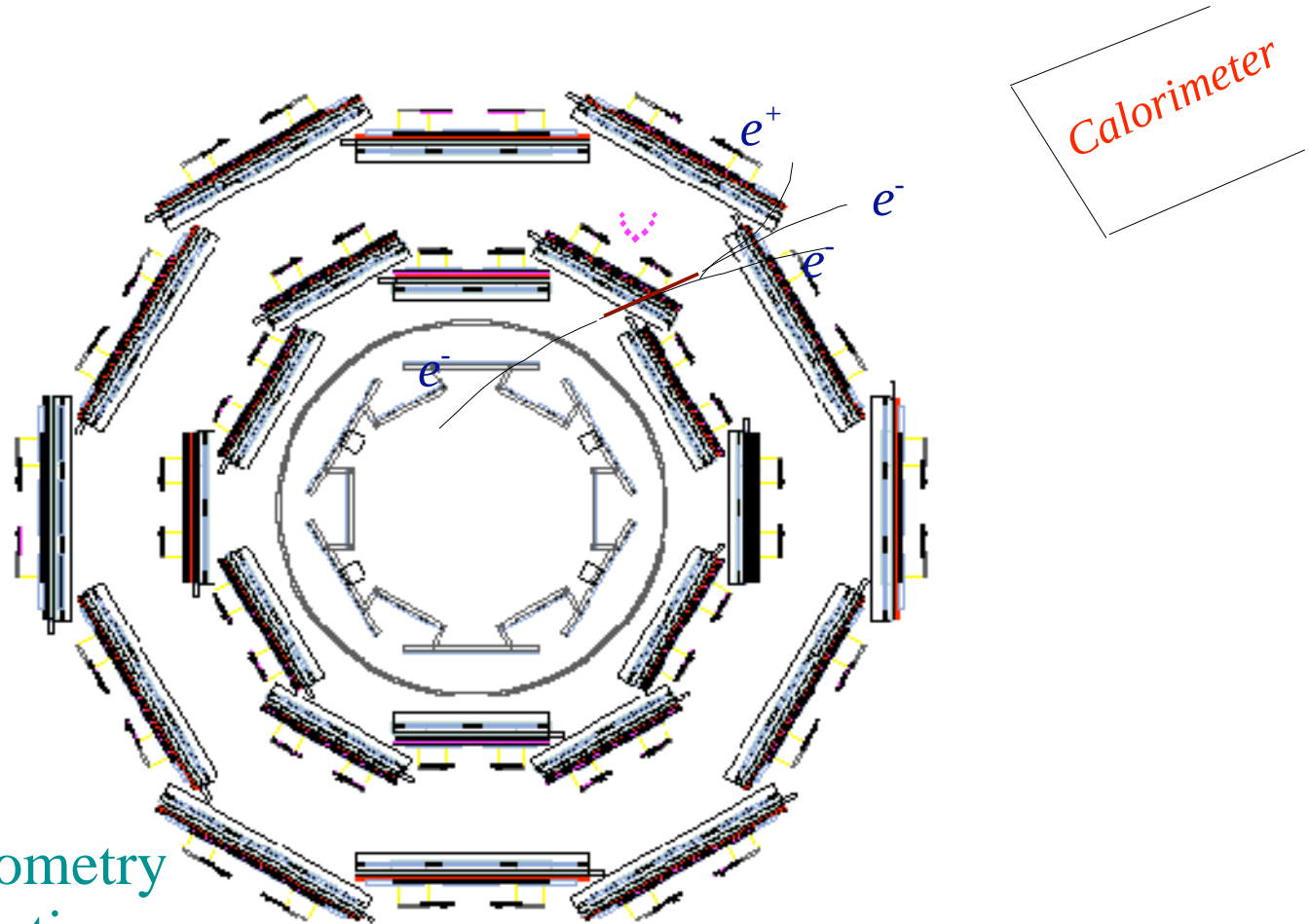


# Custom Monte Carlo Detector Simulation

- A complete detector simulation of all quantities measured in the data
- First-principles simulation of tracking
  - Tracks and photons propagated through a high-resolution 3-D lookup table of material properties for silicon detector and drift chamber
  - At each material interaction, calculate
    - Ionization energy loss according to analytic formulae
    - Generate bremsstrahlung photons down to 0.4 MeV, using detailed cross section and spectrum calculations and LPM effect
    - Simulate photon conversion and compton scattering
    - Propagate bremsstrahlung photons and conversion electrons
    - Simulate multiple Coulomb scattering, including non-Gaussian tail
  - Deposit and smear hits on COT wires, perform full helix fit including beam-constraint

# Fast Monte Carlo Detector Simulation

- A complete detector simulation of all quantities measured in the data
- First-principles simulation of tracking
  - Tracks and photons propagated through a high-resolution 3-D lookup table of material properties for silicon detector and drift chamber



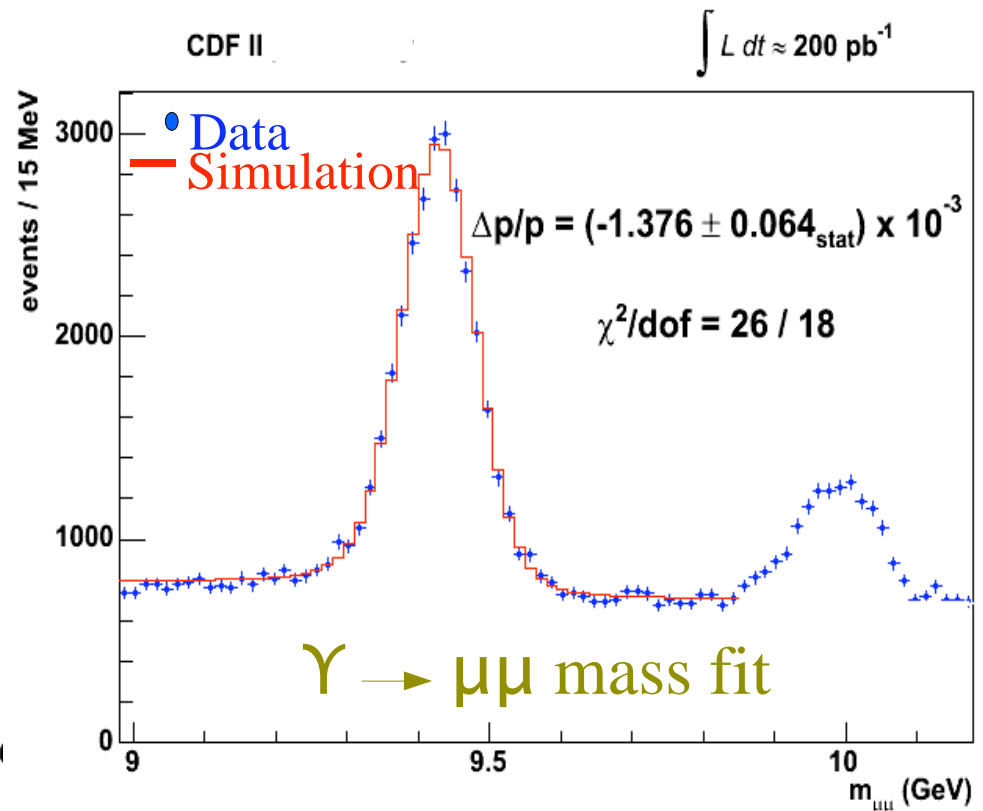
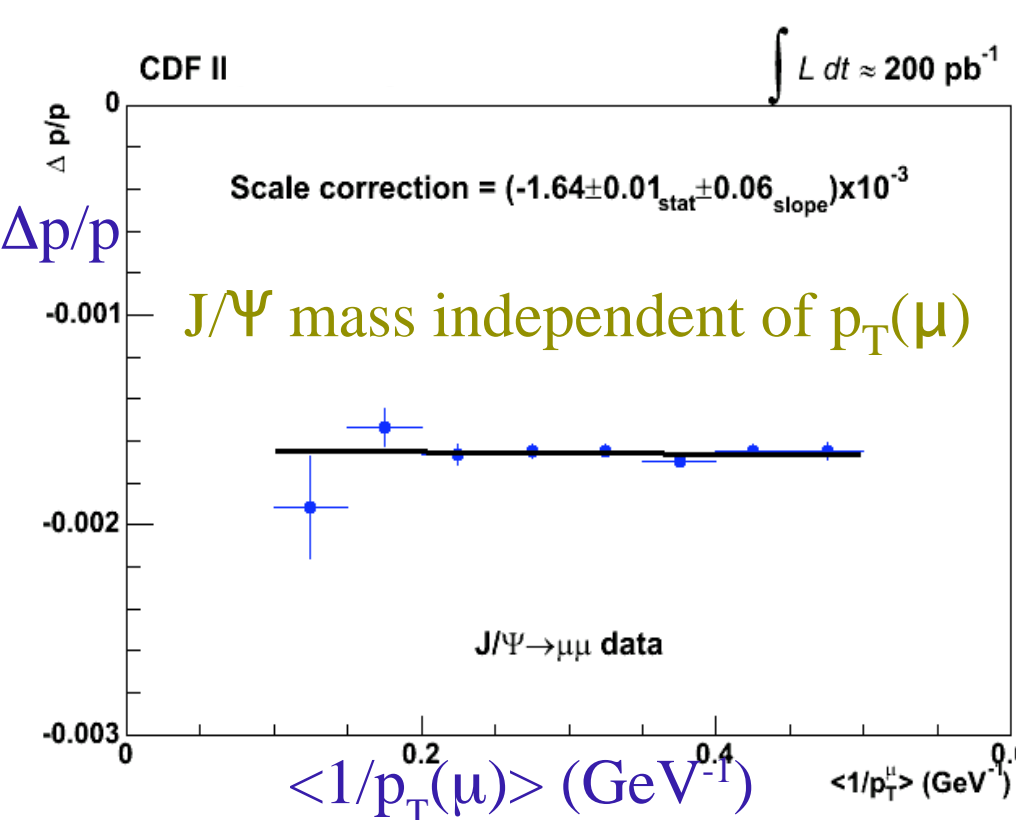
Silicon detector geometry  
and material description

Calorimeter

# Tracking Momentum Scale

# Tracking Momentum Calibration

- Set using  $J/\Psi \rightarrow \mu\mu$  and  $\Upsilon \rightarrow \mu\mu$  resonances
  - Measured to be consistent within total uncertainties
- Use  $J/\Psi$  to study and calibrate ionizing material accounting (6% correction needed)





# Tracking Momentum Scale Systematics

## Systematic uncertainties on momentum scale

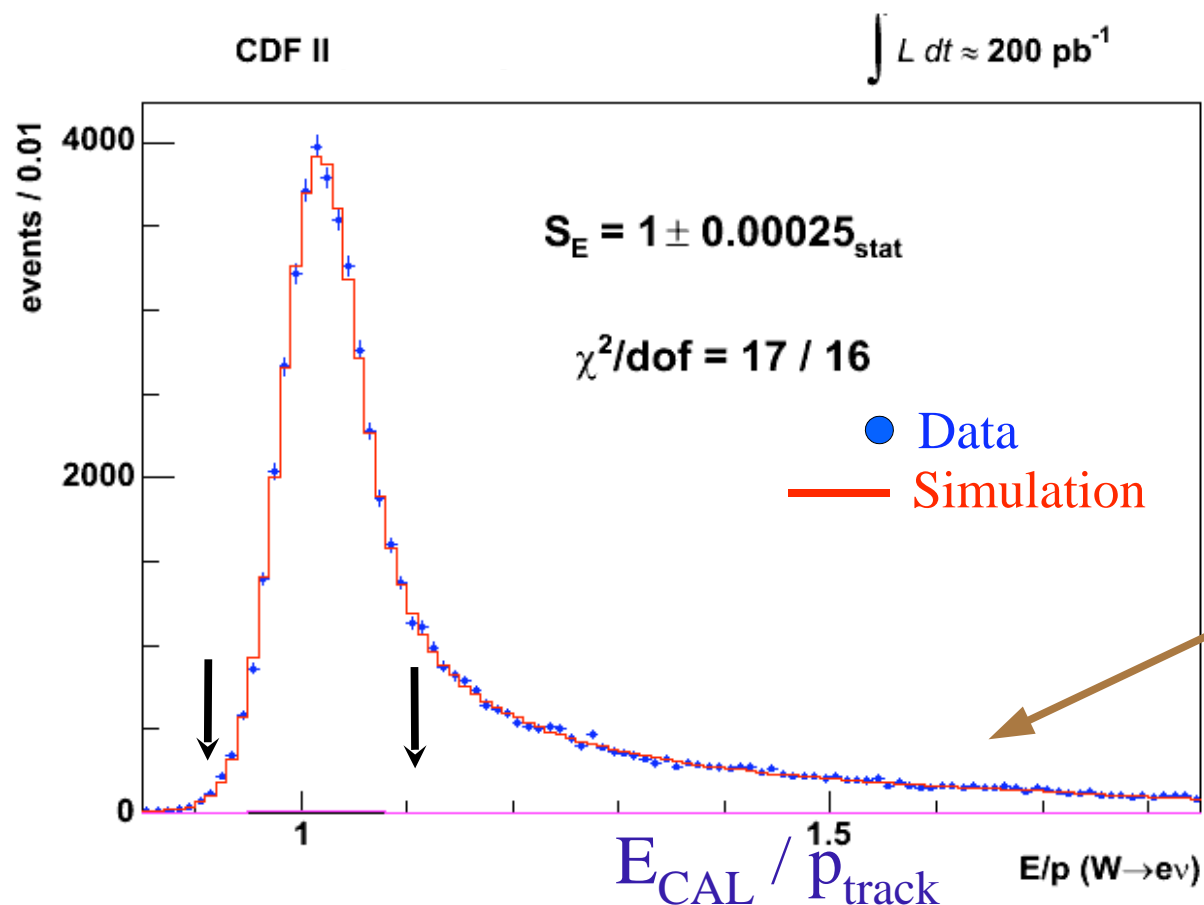
Source	$J/\psi$ ( $\times 10^{-3}$ )	$\Upsilon$ ( $\times 10^{-3}$ )	Common ( $\times 10^{-3}$ )
→ QED and energy loss model	0.20	0.13	0.13
→ Magnetic field nonuniformities	0.10	0.12	0.10
Beam constraint bias	N/A	0.06	0
Ionizing material scale	0.06	0.03	0.03
COT alignment corrections	0.05	0.03	0.03
Fit range	0.05	0.02	0.02
$p_T$ threshold	0.04	0.02	0.02
Resolution model	0.03	0.03	0.03
Background model	0.03	0.02	0.02
World-average mass value	0.01	0.03	0
Statistical	0.01	0.06	0
Total	0.25	0.21	0.17

Uncertainty dominated by QED radiative corrections and magnetic field non-uniformity

# EM Calorimeter Response

# Electromagnetic Calorimeter Calibration

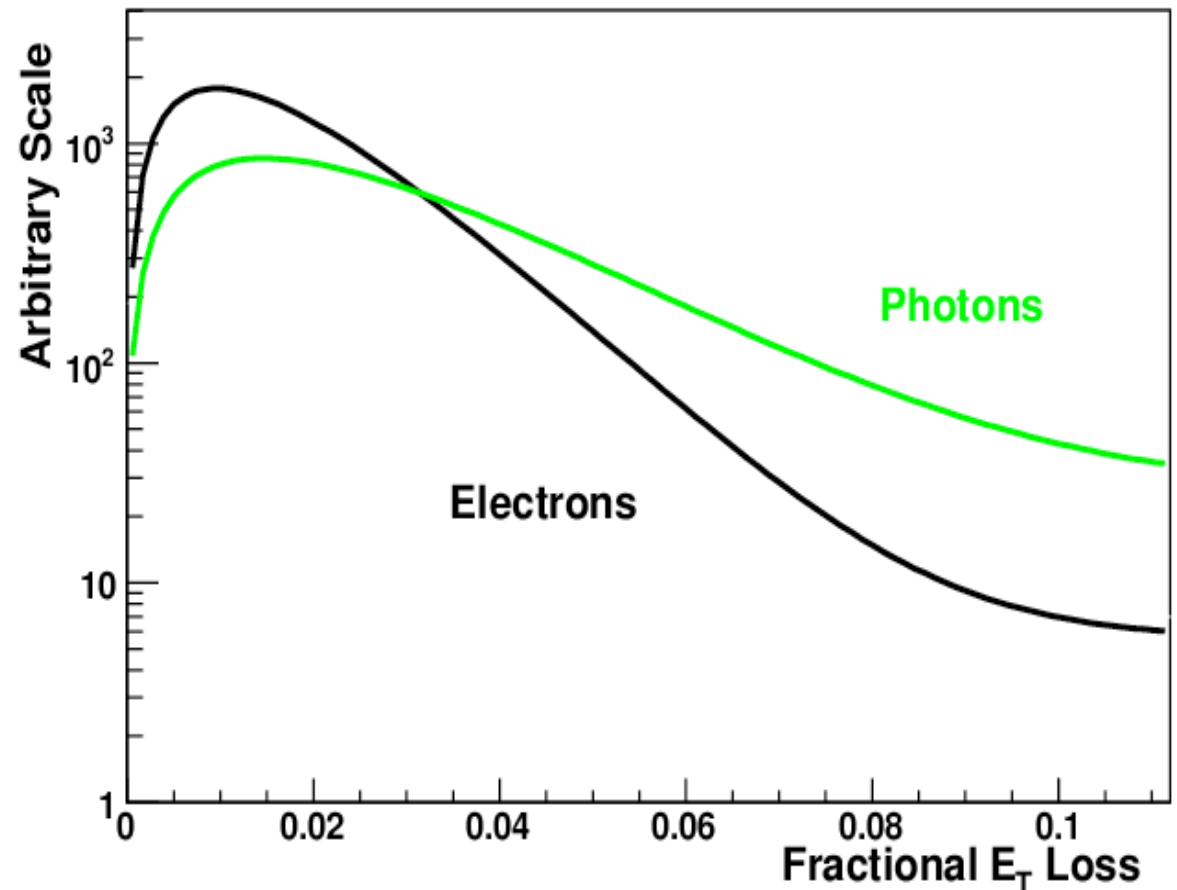
- E/p peak from  $W \rightarrow e\nu$  decays provides EM calorimeter calibration relative to the tracker
  - Calibration performed in bins of electron energy



Tail region of E/p spectrum  
used for tuning model of  
radiative material

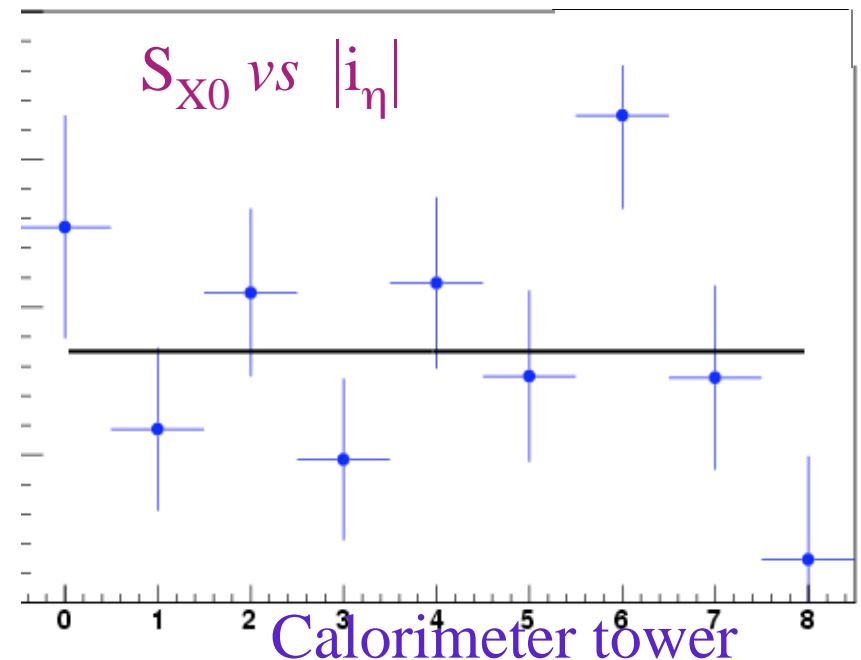
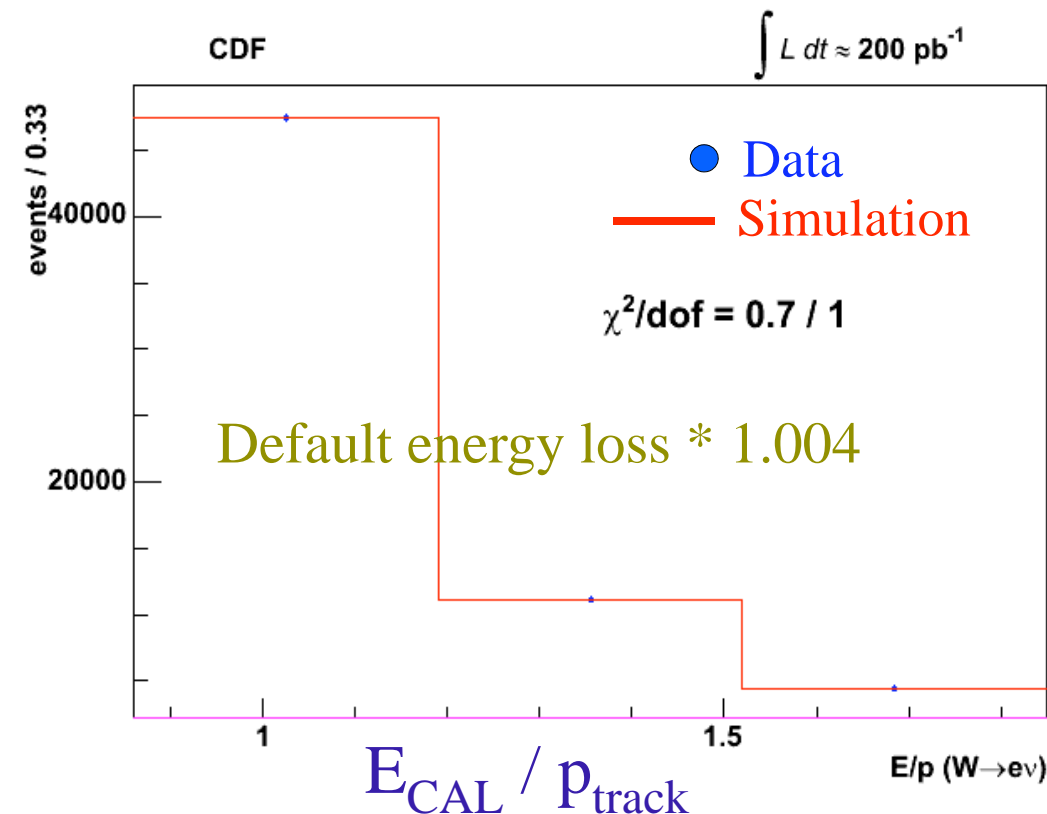
# Calorimeter Simulation for Electrons and Photons

- Distributions of energy loss calculated based on expected shower profiles as a function of  $E_T$ 
  - Leakage into hadronic calorimeter
  - Absorption in the coil
  - Relevant for E/p lineshape



# Consistency of Radiative Material Model

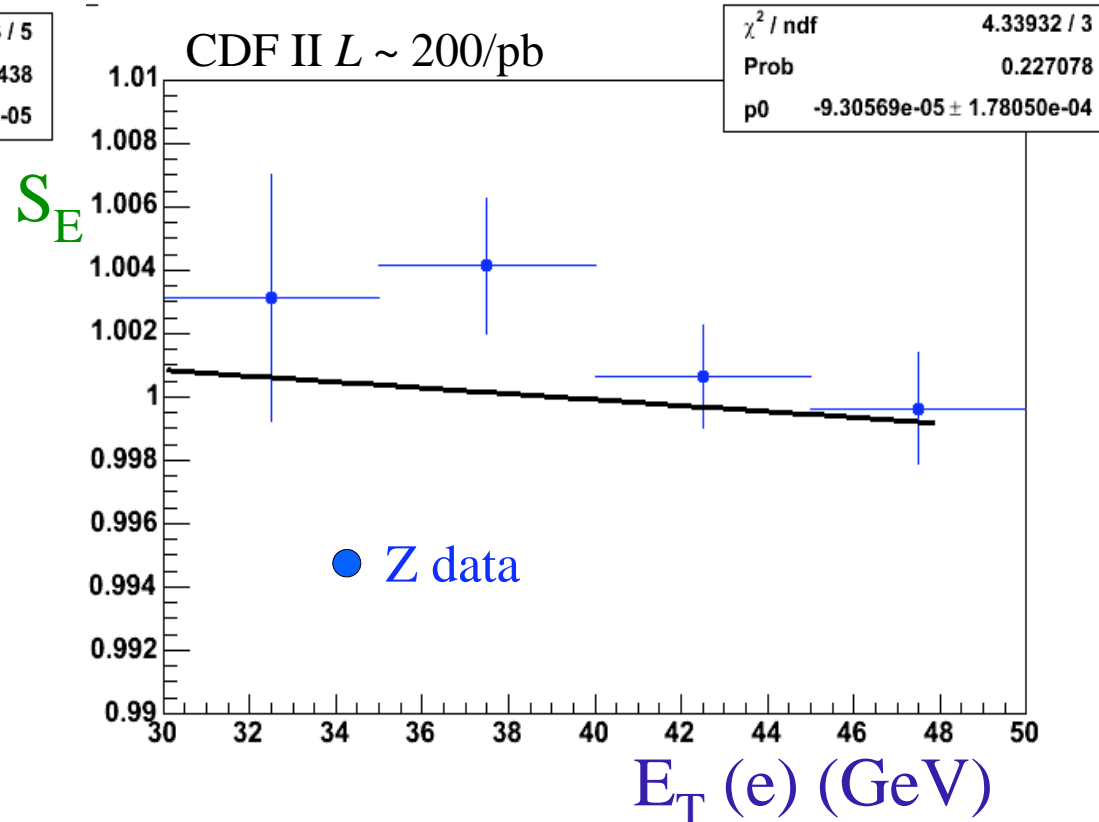
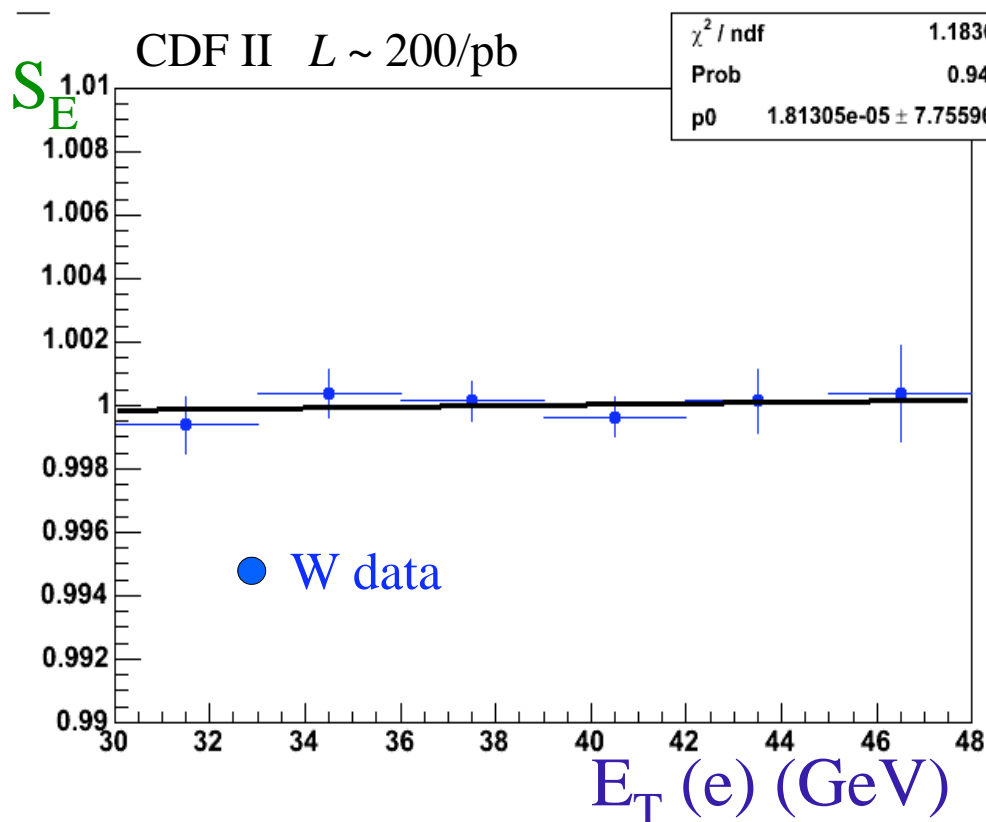
- Excellent description of E/p spectrum tail
- radiative material tune factor:  $S_{X0} = 1.004 \pm 0.009_{\text{stat}} \pm 0.002_{\text{background}}$  achieves consistency with E/p spectrum tail
  - CDF detector geometry confirmed as a function of pseudorapidity:  $S_{\text{MAT}}$  independent of pseudorapidity



# Measurement of EM Calorimeter Non-linearity

- Perform E/p fit-based calibration in bins of electron  $E_T$
- Parameterize non-linear response as:  $S_E = 1 + \zeta (E_T/\text{GeV} - 39)$
- Tune on W and Z data:  $\zeta = (6 \pm 7_{\text{stat}}) \times 10^{-5}$

$$\Rightarrow \Delta M_W = 23 \text{ MeV}$$

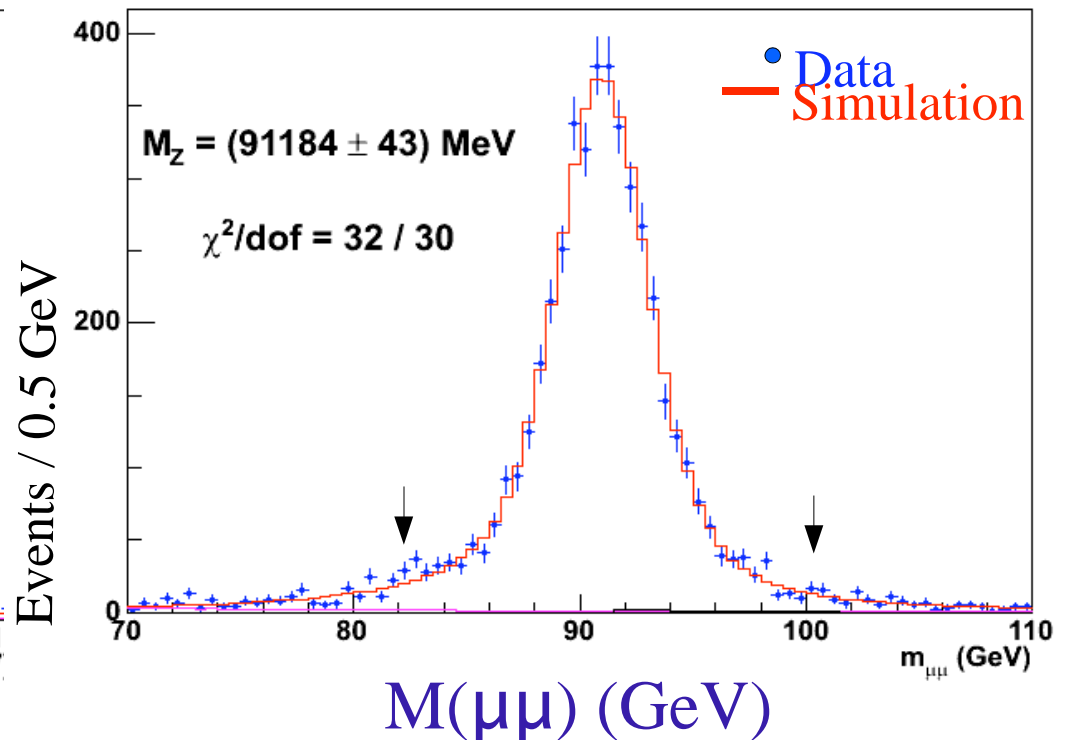
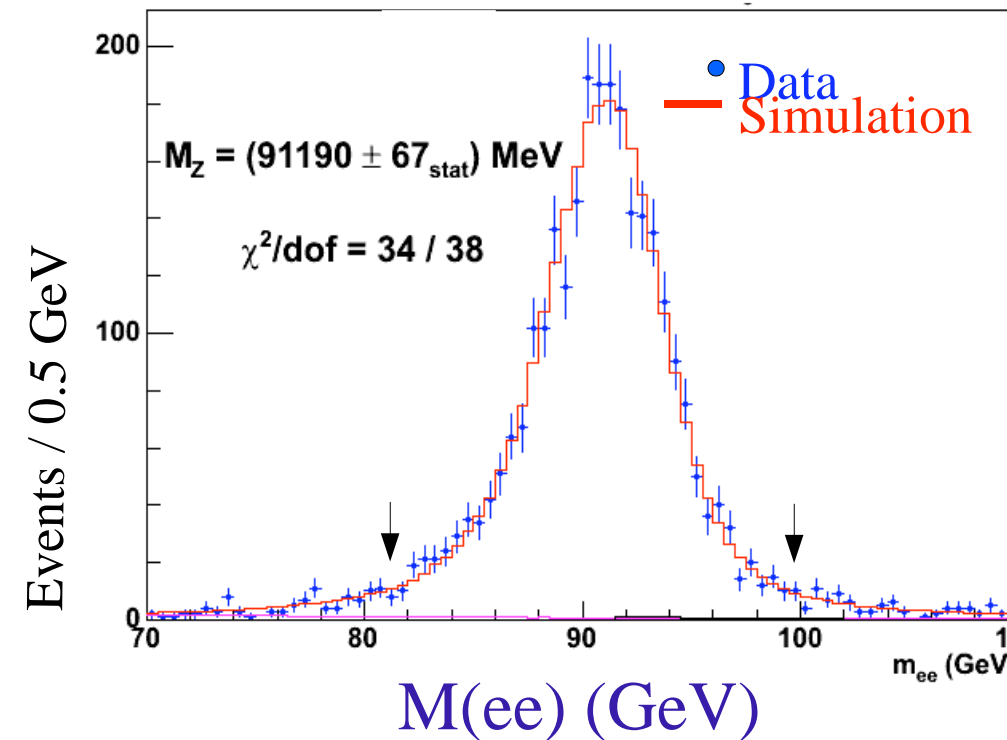


## $Z \rightarrow ll$ Mass Cross-checks

- Z boson mass fits consistent with tracking and E/p-based calibrations
- This cross-check is statistics-limited, its validation power will keep improving with larger datasets

CDF II

$L \sim 200/\text{pb}$



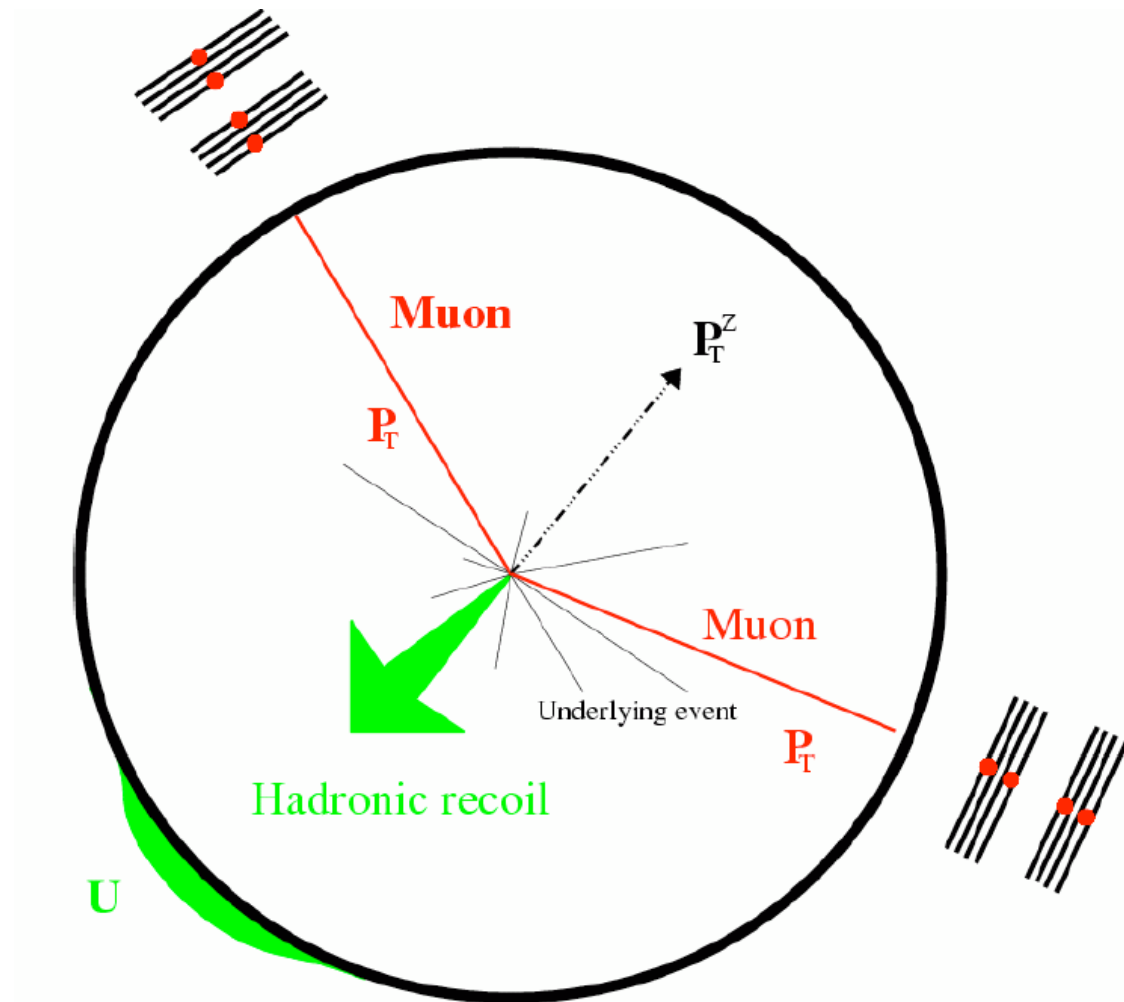


# Hadronic Recoil Model

# Constraining the Hadronic Recoil Model

Exploit similarity in production and decay of  $W$  and  $Z$  bosons

Detector response model for hadronic recoil tuned using  $p_T$ -balance in  $Z \rightarrow ll$  events

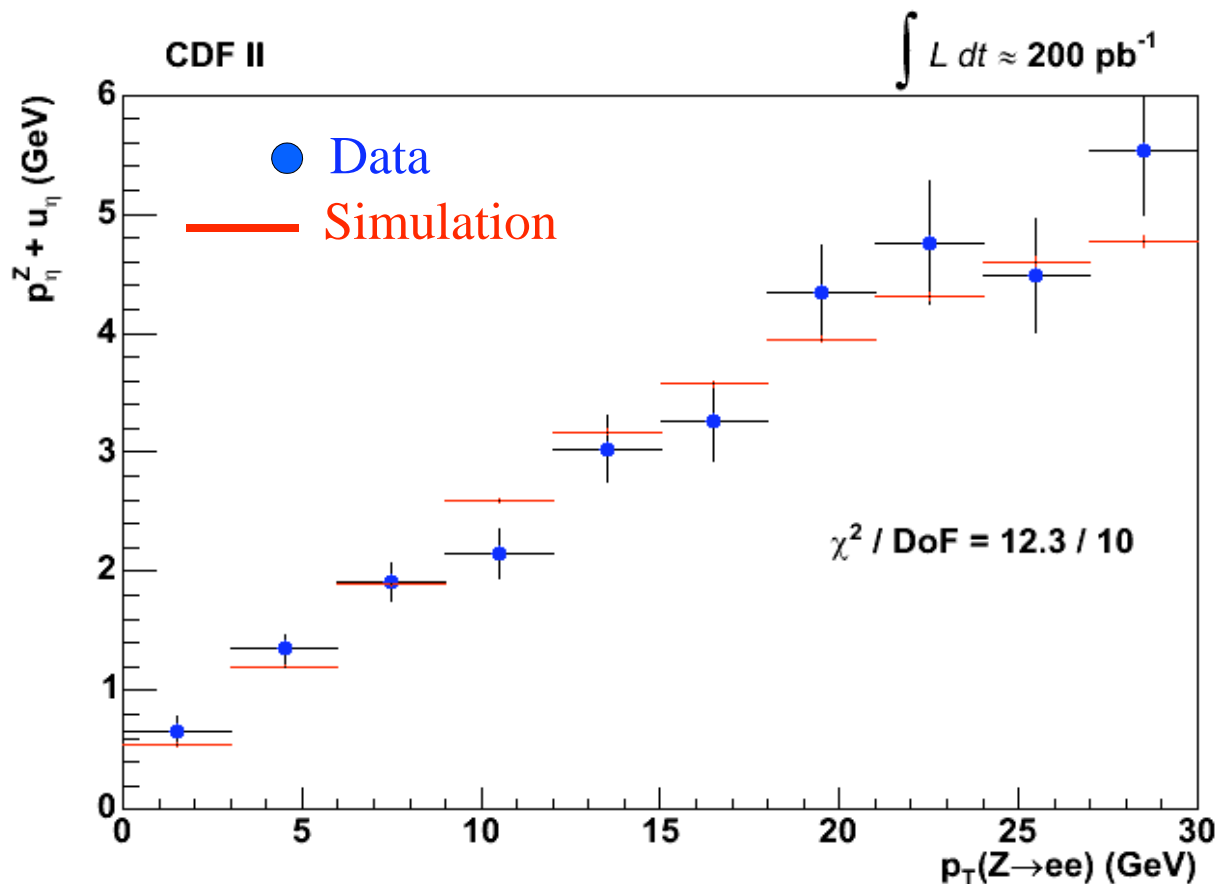
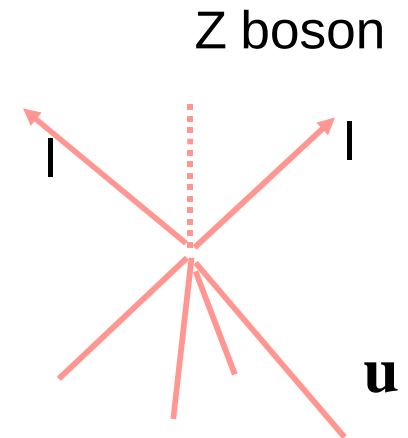


Transverse momentum of Hadronic recoil ( $u$ ) calculated as 2-vector-sum over calorimeter towers

# Tuning Recoil Response Model with Z events

Project the vector sum of  $p_T(l\bar{l})$  and  $\mathbf{u}$  on a set of orthogonal axes defined by lepton directions

Mean and rms of projections as a function of  $p_T(l\bar{l})$  provide information hadronic model parameters



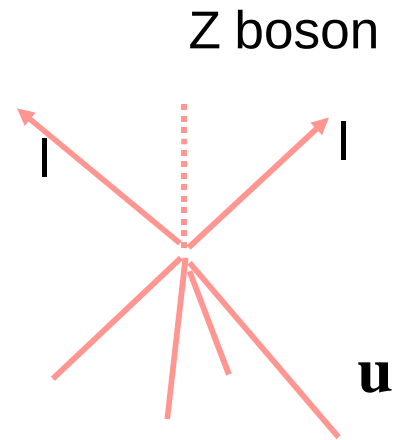
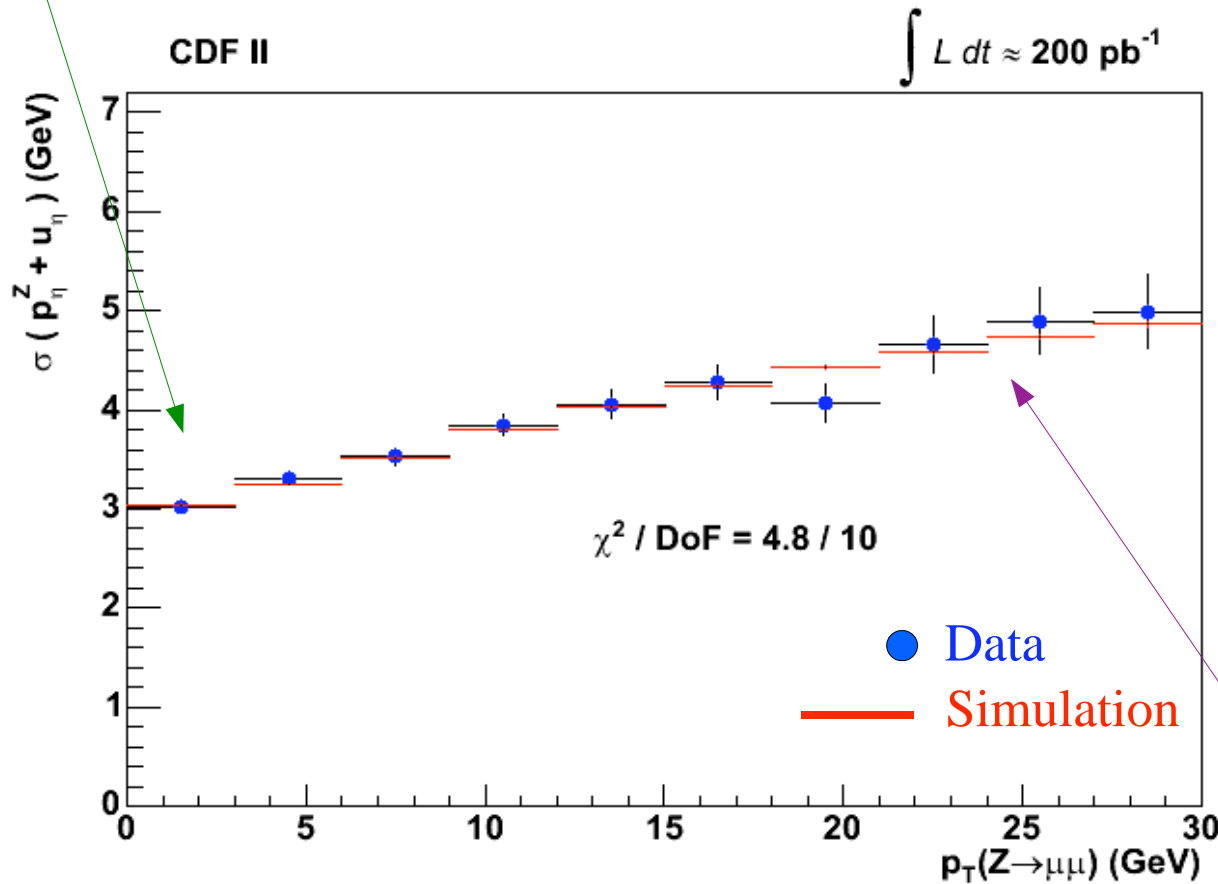
Hadronic model parameters tuned by minimizing  $\chi^2$  between data and simulation

$$\Delta M_W = 9 \text{ MeV}$$

# Tuning Recoil Resolution Model with Z events

At low  $p_T(Z)$ ,  $p_T$ -balance constrains hadronic resolution due to underlying event

Resolution of  $p_T$ -balance (GeV)

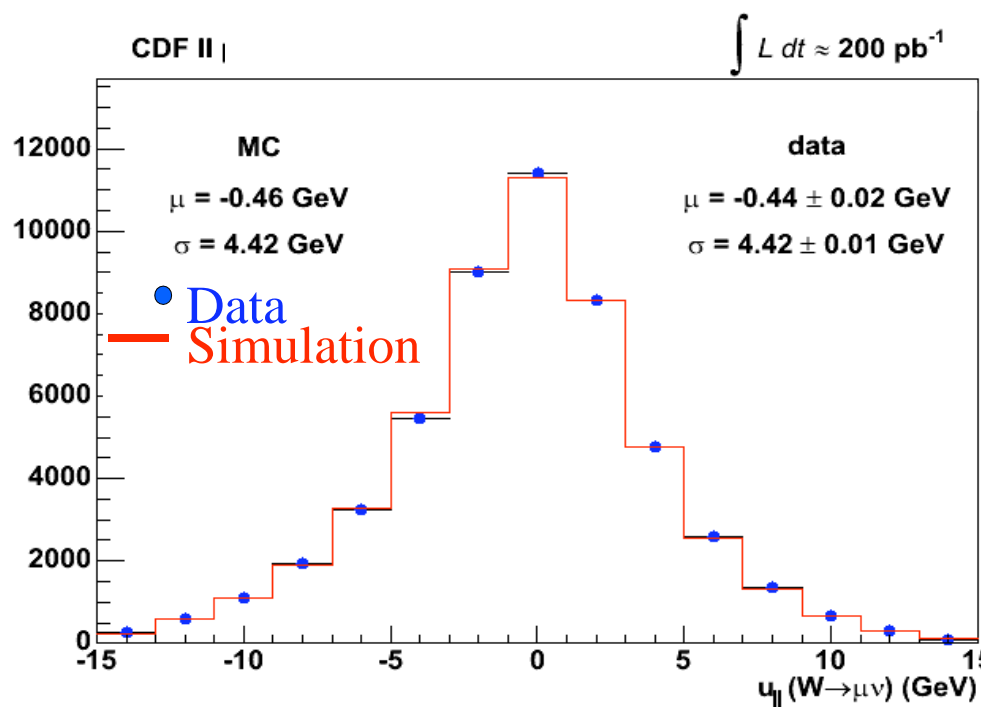
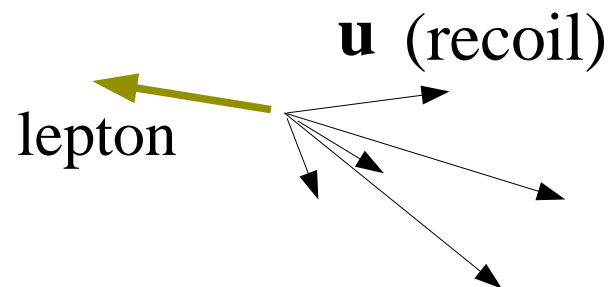


$$\Delta M_W = 7 \text{ MeV}$$

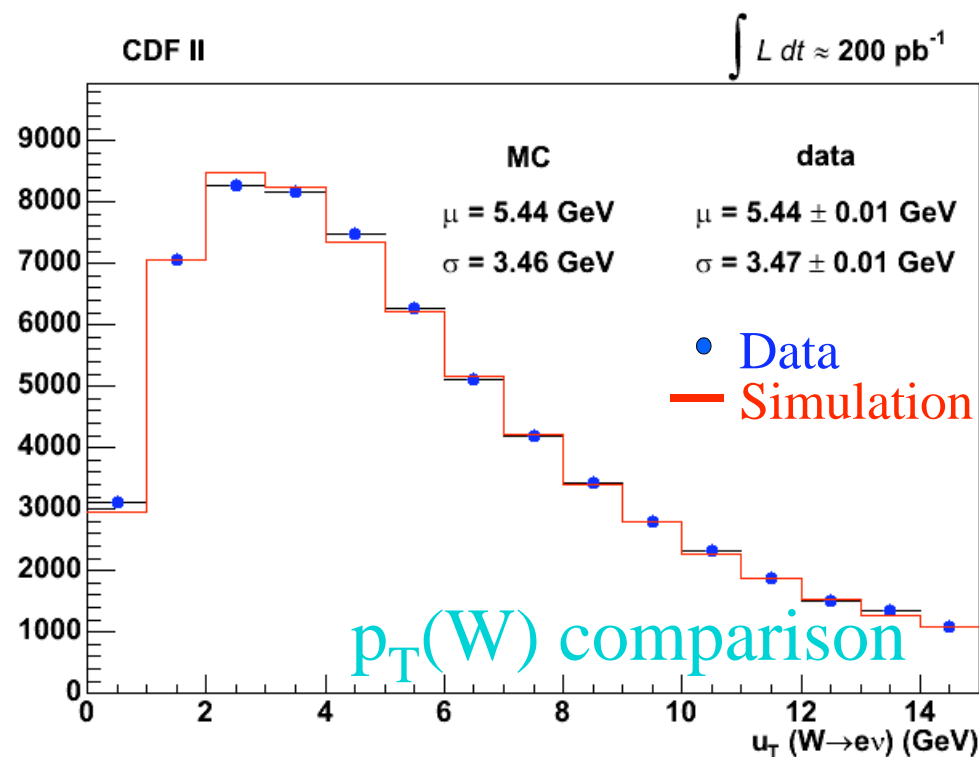
At high  $p_T(Z)$ ,  $p_T$ -balance constrains jet resolution

# Testing Hadronic Recoil Model with $W$ events

Compare recoil distributions  
between simulation and data

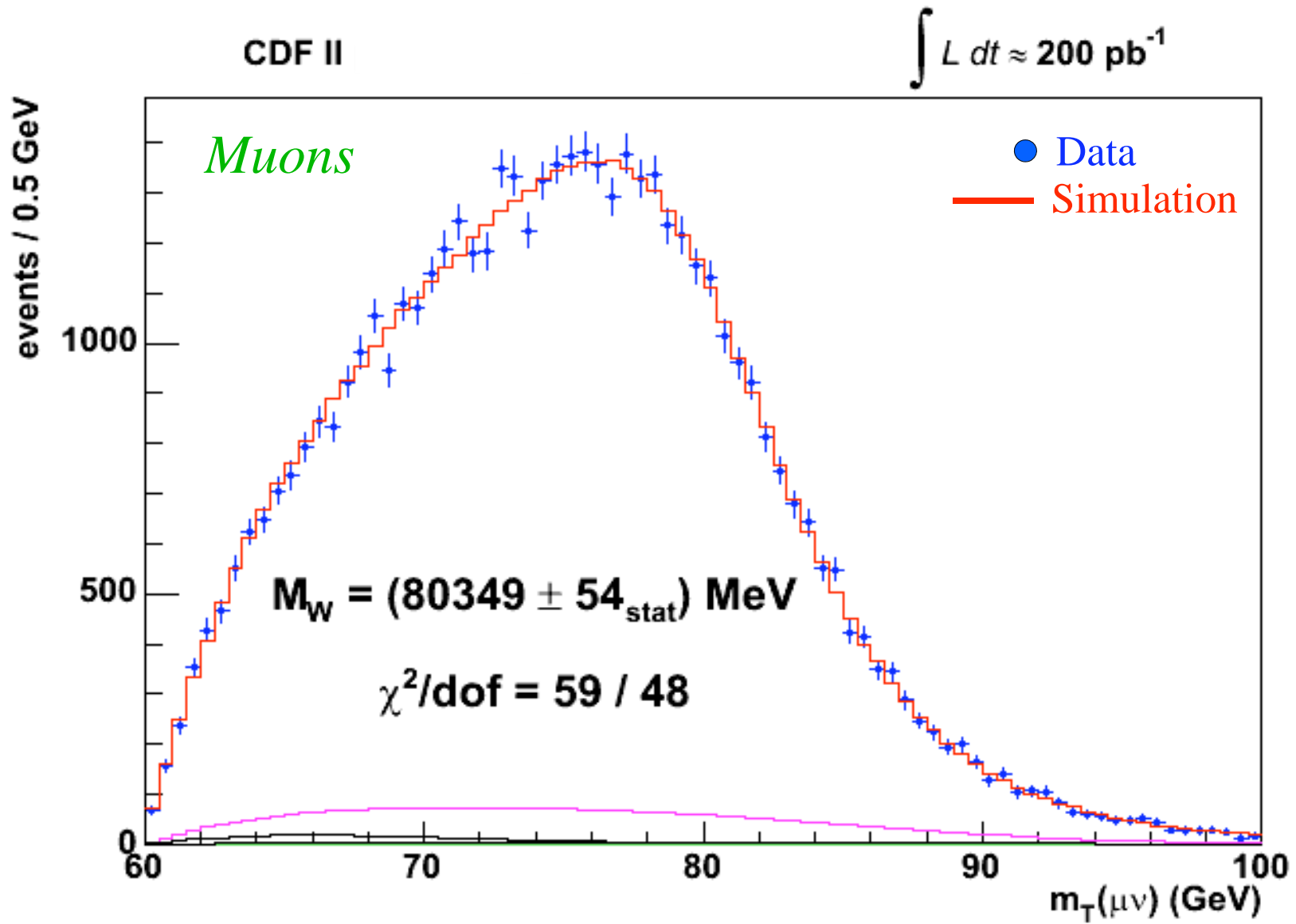


Recoil projection (GeV) on lepton direction

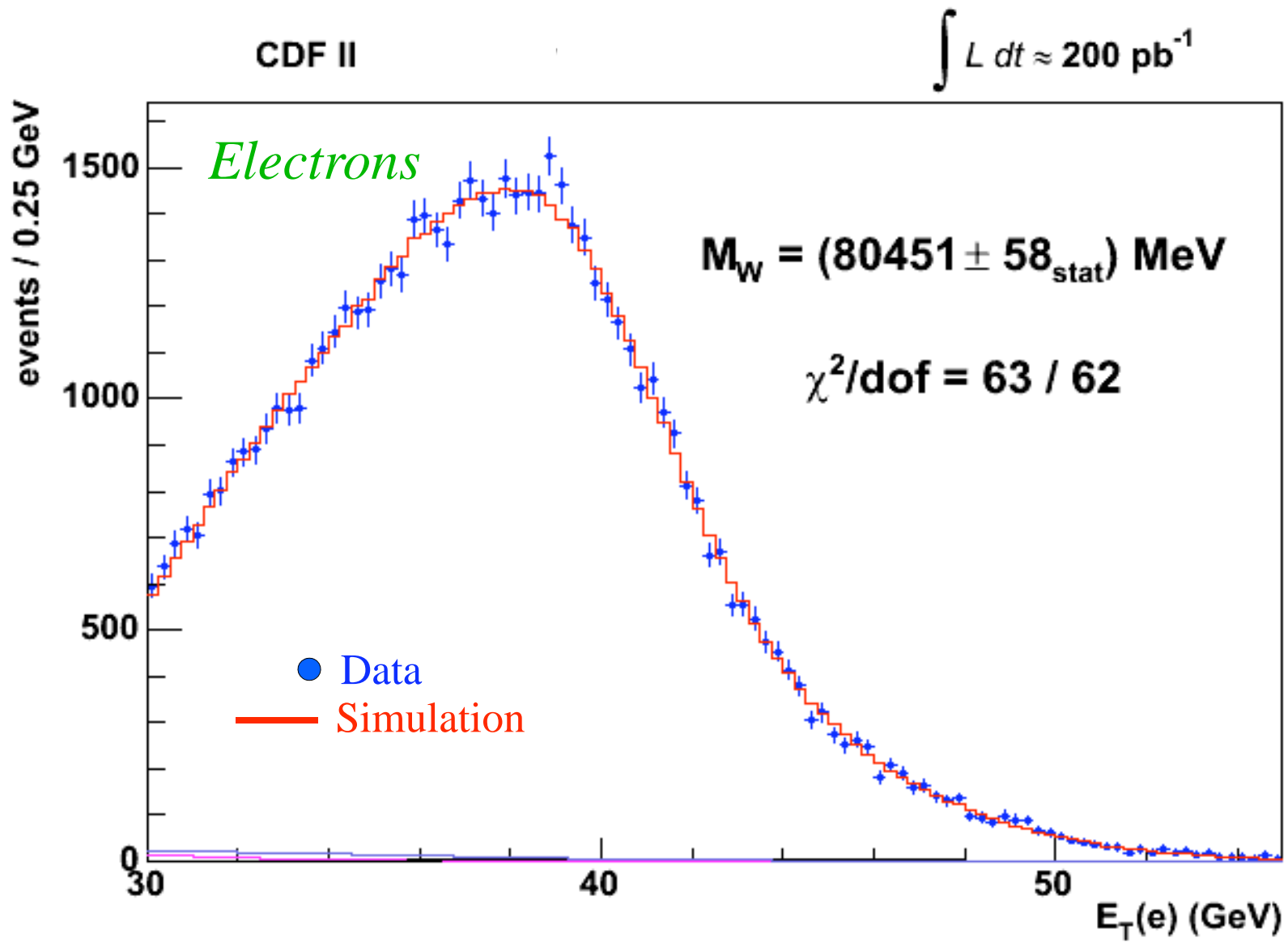


# W Mass Fits

# W Transverse Mass Fits



# W Lepton $p_T$ Fits





# Transverse Mass Fit Uncertainties (MeV)

(CDF, PRL 99:151801, 2007; Phys. Rev. D 77:112001, 2008)

	<i>electrons</i>	<i>muons</i>	<i>common</i>
W statistics	48	54	0
Lepton energy scale	30	17	17
Lepton resolution	9	3	-3
Recoil energy scale	9	9	9
Recoil energy resolution	7	7	7
Selection bias	3	1	0
Lepton removal	8	5	5
Backgrounds	8	9	0
production dynamics	3	3	3
Parton dist. Functions	11	11	11
QED rad. Corrections	11	12	11
Total systematic	39	27	26
Total	62	60	

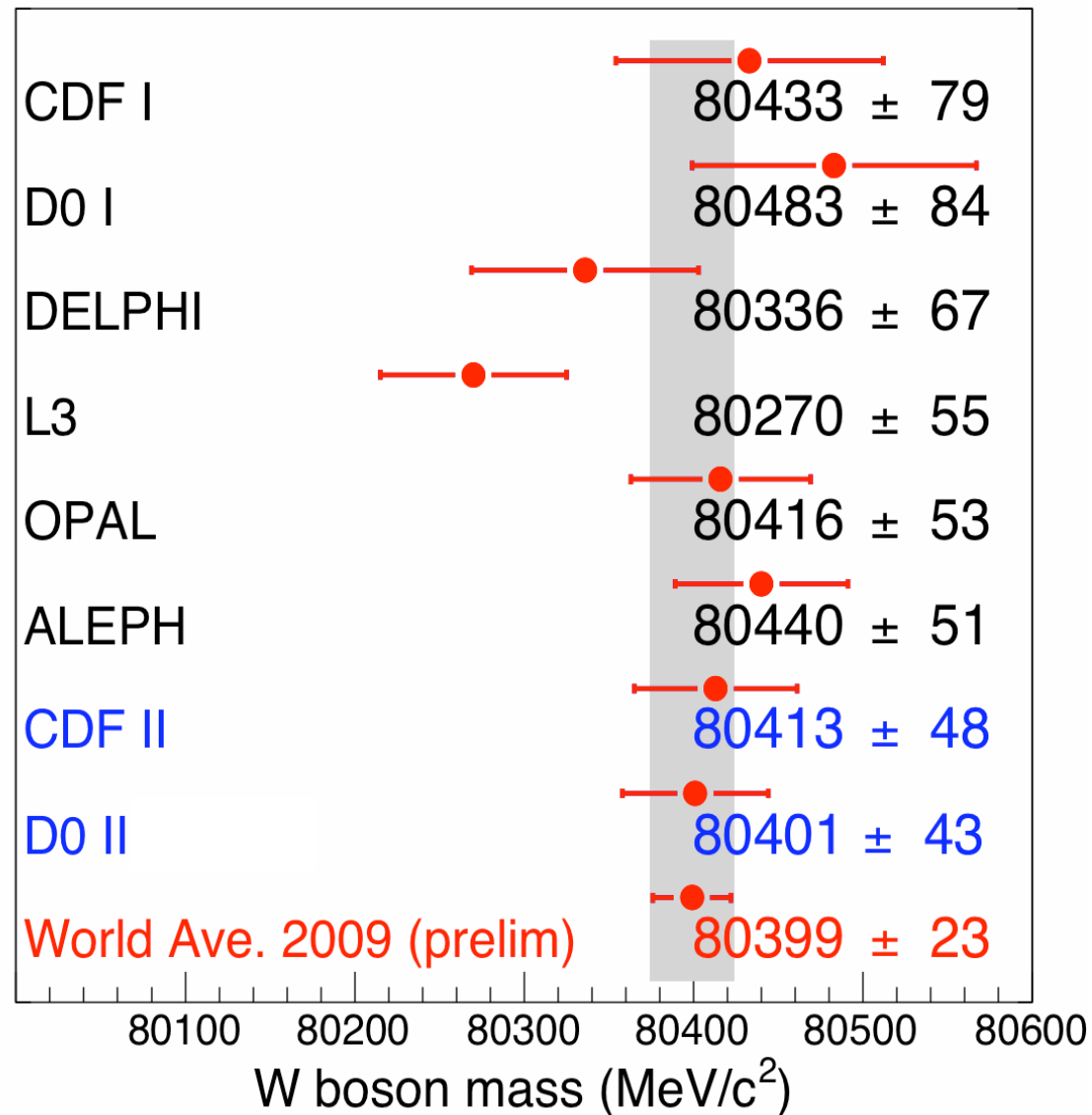
*W charge asymmetry from Tevatron helps with PDFs* →

Systematic uncertainties shown in green: statistics-limited by control data samples

# W Boson Mass Measurements

CDF: 200 pb<sup>-1</sup>, electron  
and muon channels

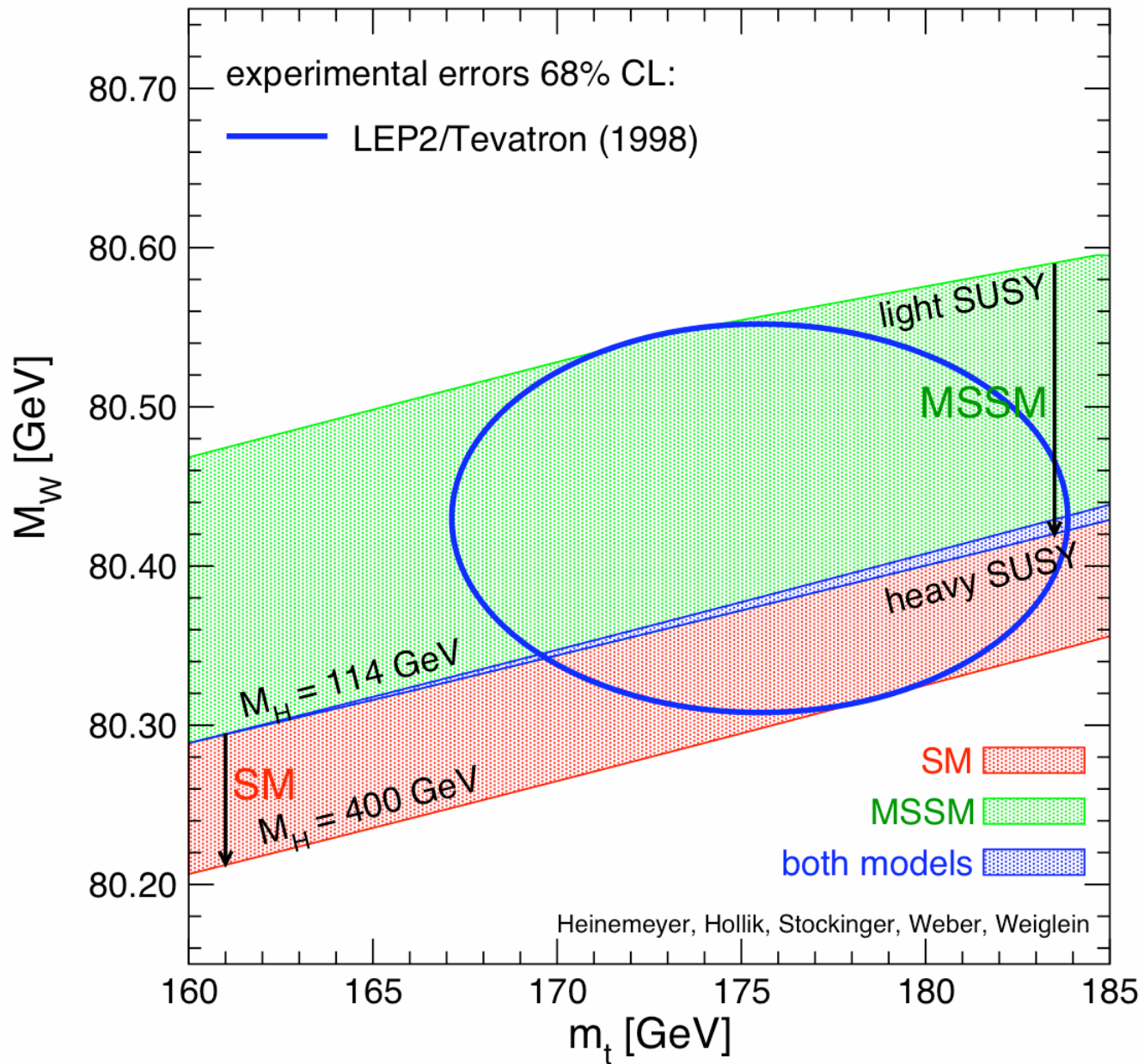
D0: 1 fb<sup>-1</sup>, electron  
channel



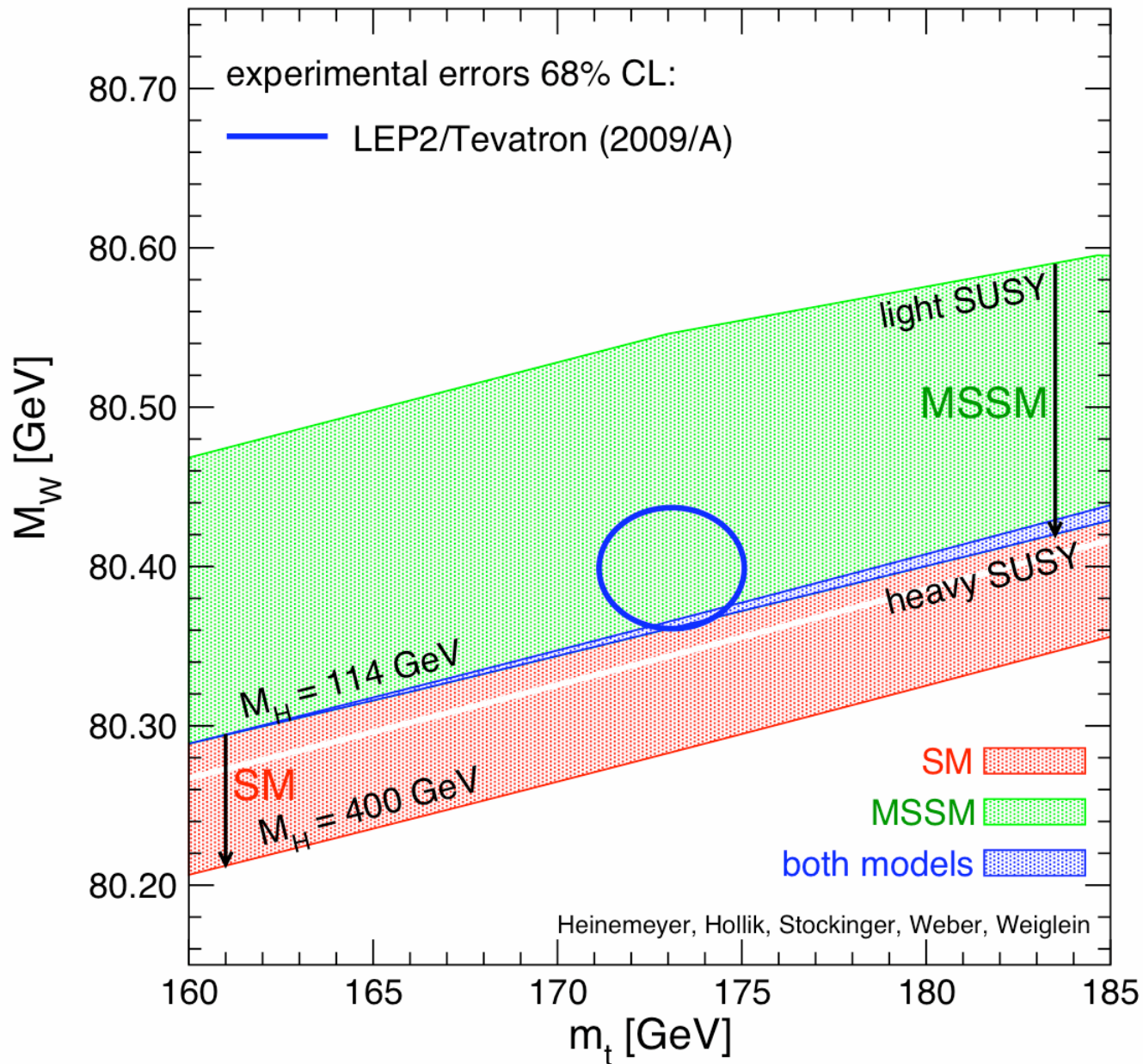
(D0 Run II: PRL 103:141801, 2009)

(CDF Run II: PRL 99:151801, 2007; PRD 77:112001, 2008)

# Pre-Run 2 $M_W$ vs $M_{\text{top}}$



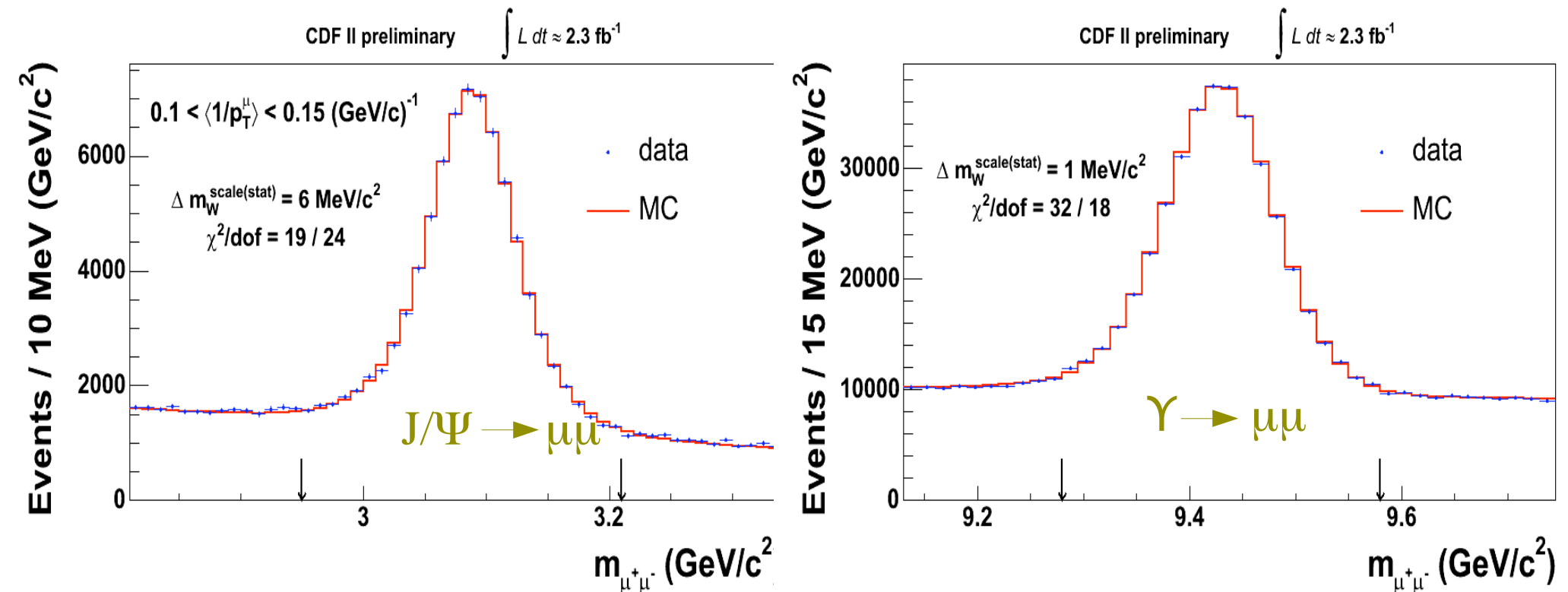
# Post-Run 2 & LEP II $M_W$ vs $M_{top}$



# Preliminary Studies of $2.3 \text{ fb}^{-1}$ Data from CDF

CDF analysis of  $2.3 \text{ fb}^{-1}$  of data is in progress, with the goal of measuring  $M_W$  with precision better than 25 MeV

Lepton resolutions as good as they were in  $200 \text{ pb}^{-1}$  sample



# Summary

- The  $W$  boson mass is a very interesting parameter to measure with increasing precision
- CDF Run 2  $W$  mass result with 200 pb<sup>-1</sup> data:
  - $M_W = 80413 \pm 48$  MeV
- D0 Run 2  $W$  mass result with 1 fb<sup>-1</sup> data:
  - $M_W = 80401 \pm 43$  MeV
- Many systematics limited by statistics of control samples
  - CDF and D0 are both working on  $\delta M_W < 25$  MeV measurements from  $\sim 2$  fb<sup>-1</sup> (CDF) and  $\sim 4$  fb<sup>-1</sup> (D0)
- Learning as we go: Tevatron  $\rightarrow$  LHC may produce  $\delta M_W \sim 5$ -10 MeV



## Combined Results

- Combined electrons (3 fits):  $M_W = 80477 \pm 62 \text{ MeV}$ ,  $P(\chi^2) = 49\%$
- Combined muons (3 fits):  $M_W = 80352 \pm 60 \text{ MeV}$ ,  $P(\chi^2) = 69\%$
- All combined (6 fits):  $M_W = 80413 \pm 48 \text{ MeV}$ ,  $P(\chi^2) = 44\%$

## Lepton $p_T$ and Missing $E_T$ Fit Uncertainties

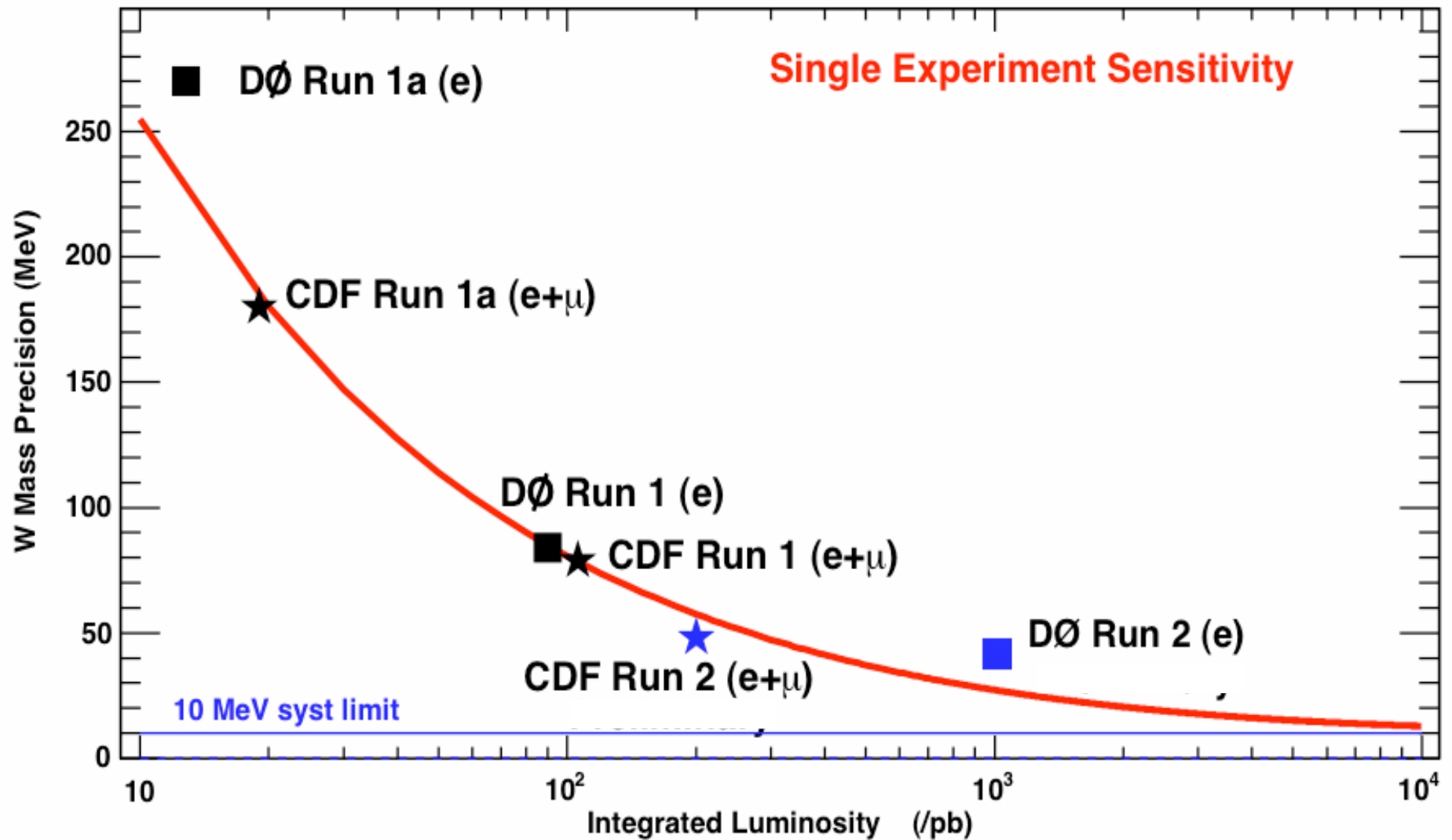
CDF II preliminary

Uncertainty ( $p_T$ )	Electrons	Muons	Common
Lepton Scale	30	17	17
Lepton Resolution	9	3	0
Recoil Scale	17	17	17
Recoil Resolution	3	3	3
Lepton Removal	0	0	0
$u_{  }$ Efficiency	5	6	0
Backgrounds	9	19	0
$p_T(W)$	9	9	9
PDF	20	20	20
QED	13	13	13
Total Systematic	45	40	35
Statistical	58	66	0
Total	73	77	35

CDF II preliminary

Uncertainty (MET)	Electrons	Muons	Common
Lepton Scale	30	17	17
Lepton Resolution	9	5	0
Recoil Scale	15	15	15
Recoil Resolution	30	30	30
Lepton Removal	16	10	10
$u_{  }$ Efficiency	16	13	0
Backgrounds	7	11	0
$p_T(W)$	5	5	5
PDF	13	13	13
QED	9	10	9
Total Systematic	54	46	42
Statistical	57	66	0
Total	79	80	42

# Improvement of $M_W$ Uncertainty with Sample Statistics



Next target: 15-20 MeV measurement of  $M_W$  from the Tevatron

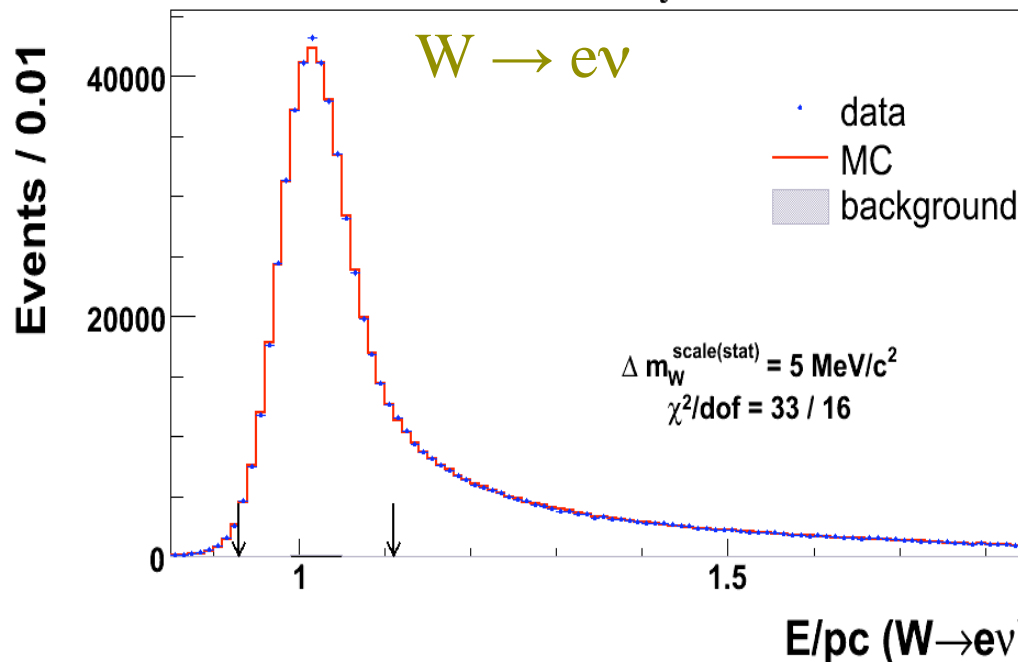
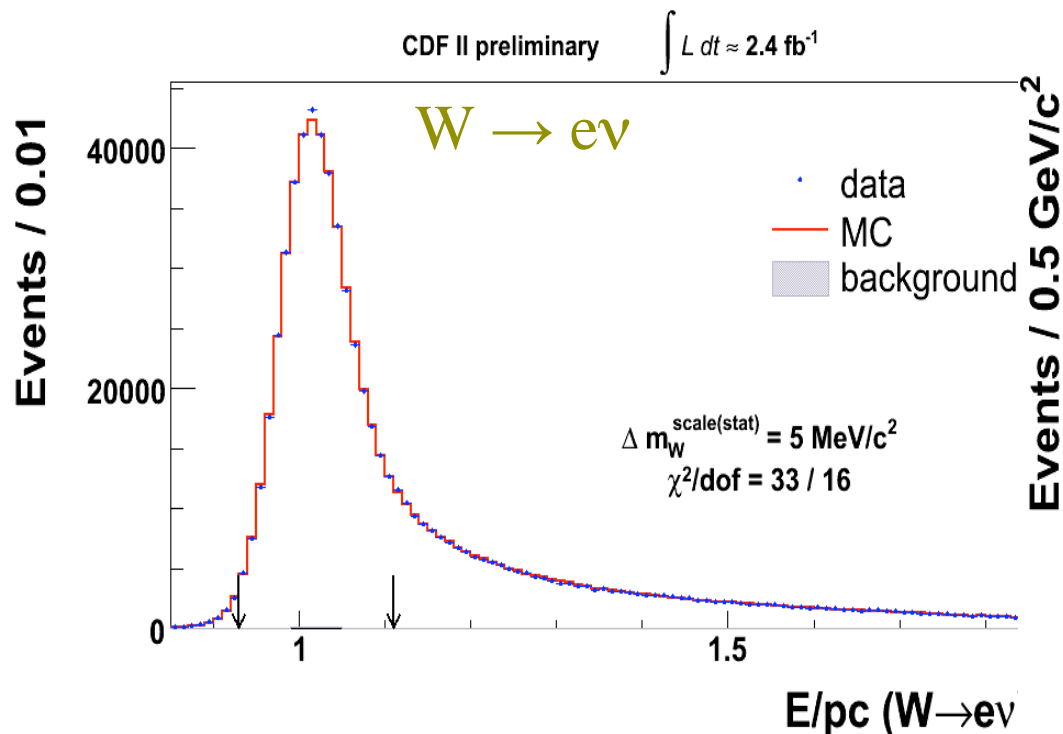
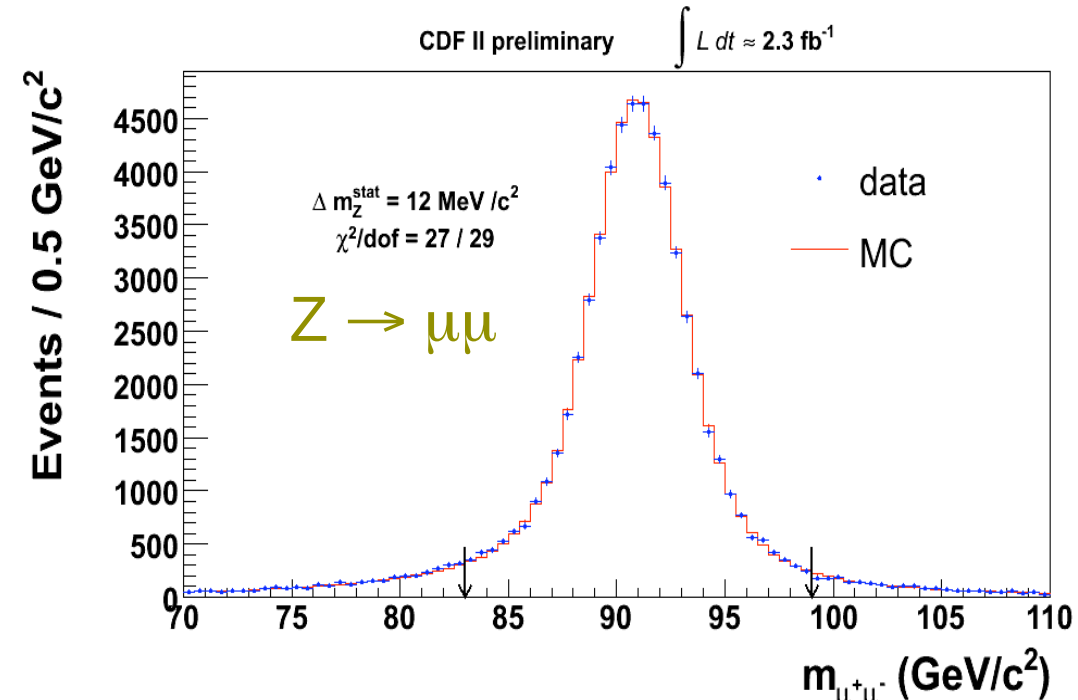


# Preliminary Studies of 2.3 fb<sup>-1</sup> Data

Statistical errors on all lepton calibration fits have scaled with statistics

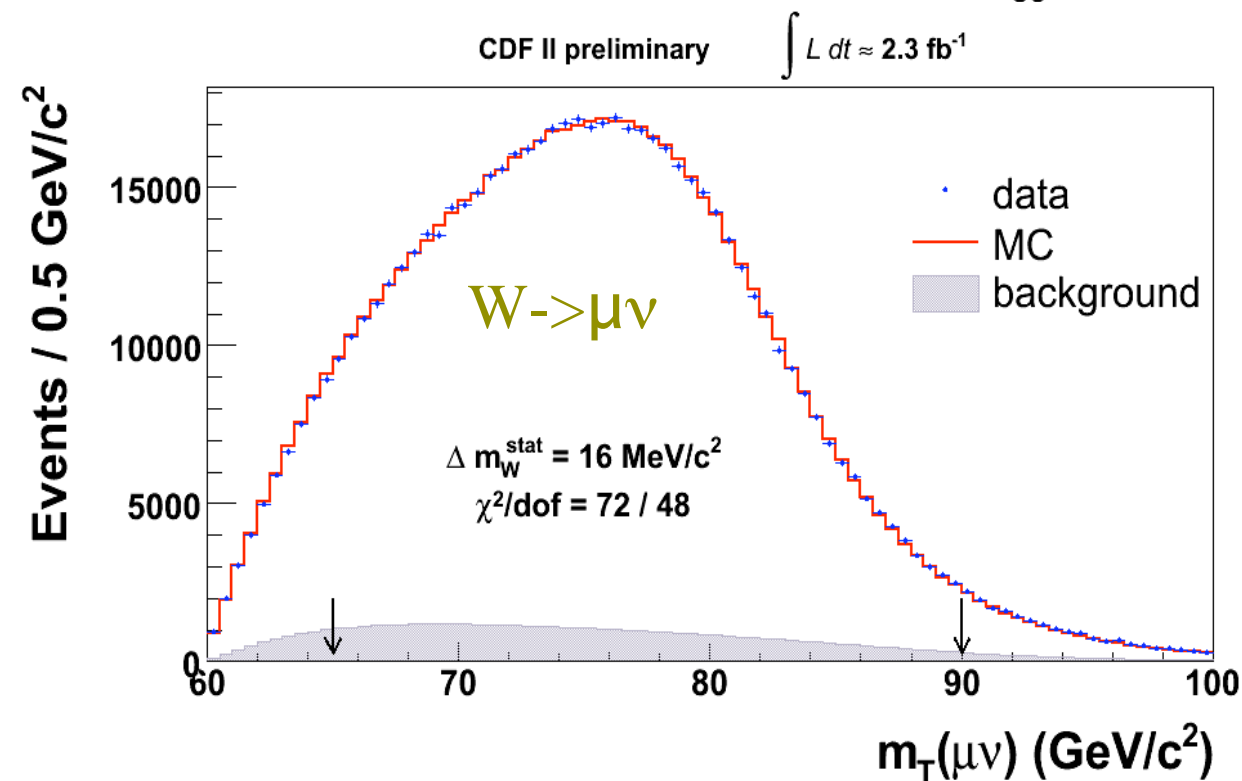
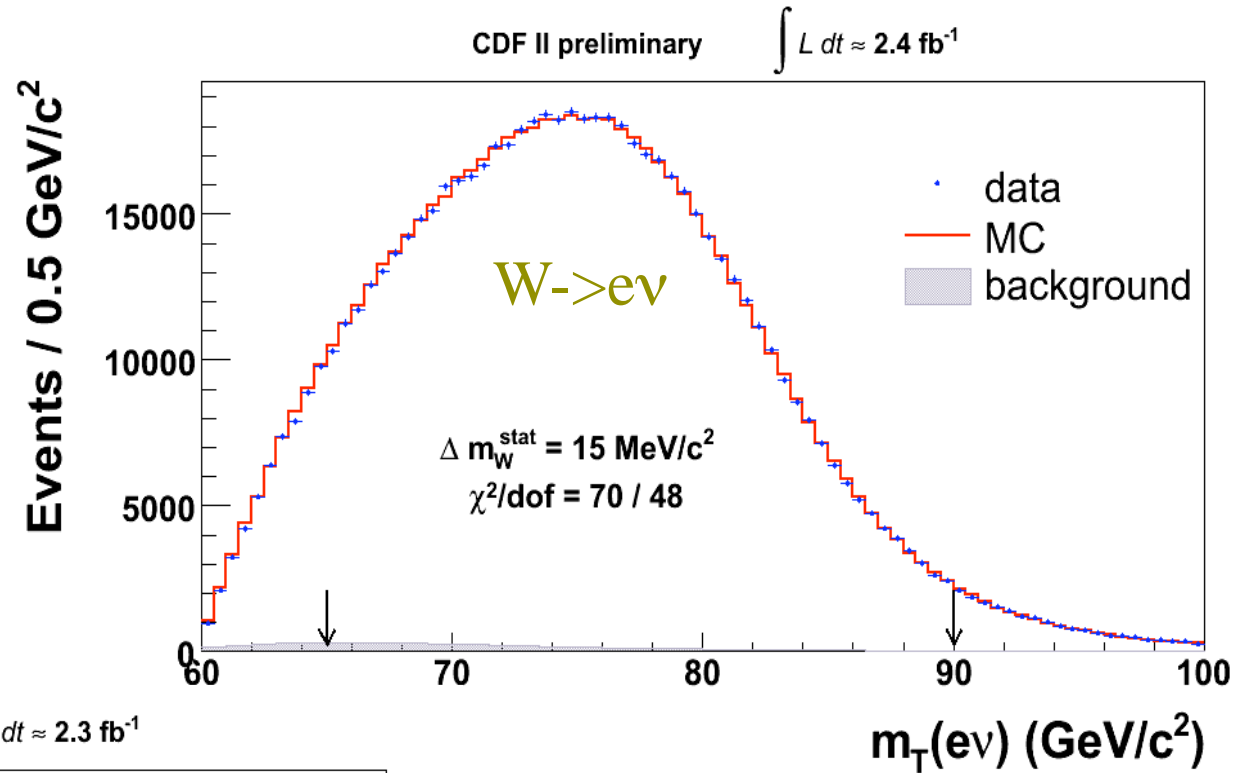
Detector and data quality maintained over time

detailed calibrations in progress



# Preliminary Studies of 2.3 fb<sup>-1</sup> Data

Recoil resolution not significantly degraded at higher instantaneous luminosity



statistical errors on transverse mass fits are scaling with statistics

# $M_W$ Measurement at LHC

- Very high statistics samples of W and Z bosons
  - $10 \text{ fb}^{-1}$  at 14 TeV: 40 million W boson and 4 million Z boson candidates per decay channel per experiment
- Statistical uncertainty on W mass fit  $\sim 2 \text{ MeV}$
- Calibrating lepton energy response using the  $Z \rightarrow ll$  mass resonance, best-case scenario of statistical limit  $\sim 5 \text{ MeV}$  precision on calibrations
- Calibration of the hadronic calorimeter based on transverse momentum balance in  $Z \rightarrow ll$  events also  $\sim 2 \text{ MeV}$  statistical limit
- Total uncertainty on  $M_W \sim 5 \text{ MeV}$  if  $Z \rightarrow ll$  data can measure all the W boson systematics

# $M_W$ Measurement at LHC

- Can the  $Z \rightarrow ll$  data constrain all the relevant W boson systematics?
- Can we add other constraints from other mass resonances and tracking detectors ?
- With every increase in statistics of the data samples, we climb a new learning curve on the systematic effects
  - Improved calculations of QED radiative corrections available
  - Better understanding of parton distributions from global fitting groups (CTEQ, MSTW, Giele *et al*)
- large sample statistics at the LHC imply the potential is there for 5-10 MeV precision on  $M_W$

# $M_W$ Measurement at LHC

- Can the  $Z \rightarrow ll$  data constrain all the relevant W boson systematics?
- Production and decay dynamics are slightly different
  - Different quark parton distribution functions
  - Non-perturbative (e.g. charm mass effects in  $cs \rightarrow W$ ) effects
  - QCD effects on polarization of W vs Z affects decay kinematics
- Lepton energies different by  $\sim 10\%$  in W vs Z events
- Presence of second lepton influences the Z boson event relative to W
- Reconstructed kinematic quantity different (invariant vs transverse mass)
- Subtle differences in QED radiative corrections
- .....
- ..... (A.V. Kotwal and J. Stark, Ann. Rev. Nucl. Part. Sci., vol. 58, Nov 2008)