

Transverse-momentum distributions of W and Z bosons at the Tevatron and at the LHC

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Based on a collaboration with:
G. Bozzi, S. Catani, D. de Florian & M. Grazzini

Outline

- 1 Drell-Yan q_T distribution
- 2 Fixed order results
- 3 Transverse-momentum resummation
- 4 Resummed results
- 5 Conclusions and Perspectives



Motivations

The study of Drell-Yan lepton pair production is well motivated:

- Large production rates and clean experimental signatures:
 - Important for detector calibration.
 - Possible use as luminosity monitor.
- Transverse momentum distributions needed for:
 - Precise prediction for M_W .
 - Beyond the Standard Model analysis.
- Test of perturbative QCD predictions.
- Constrain for fits of PDFs.



State of the art: fixed order calculations

Historically the Drell-Yan process [Drell,Yan('70)] was the first application of parton model ideas developed for deep inelastic scattering.

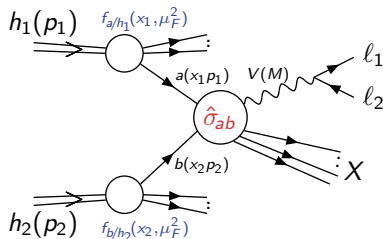
- QCD corrections:
 - Total cross section known up to NNLO ($\mathcal{O}(\alpha_S^2)$)
[Hamberg,Van Neerven,Matsuura('91)], [Harlander,Kilgore('02)]
 - Rapidity distribution known up to NNLO
[Anastasiou,Dixon,Melnikov,Petriello('03)]
 - Fully exclusive NNLO calculation completed
[Melnikov,Petriello('06)], [Catani,Cieri,de Florian,G.F., Grazzini('09)]
 - Vector boson transverse-momentum distribution known up to NLO ($\mathcal{O}(\alpha_S^2)$)
[Ellis et al.('83)], [Arnold,Reno('89)], [Gonsalves et al.('89)]
- Electroweak correction are know at $\mathcal{O}(\alpha)$
[Dittmaier et al.('02)], [Baur et al.('02)] [Carloni Calame, Montagna,Nicrosini,Vicini('06)]



The Drell-Yan q_T distribution

$$h_1(p_1) + h_2(p_2) \rightarrow V(M) + X \rightarrow \ell_1 + \ell_2 + X$$

where $V = \gamma^*, Z^0, W^\pm$ and $\ell_1 \ell_2 = \ell^+ \ell^-, \ell \nu_\ell$



According to the QCD factorization theorem:

$$\frac{d\sigma}{dq_T^2}(q_T, M, s) = \sum_{a,b} \int_0^1 dx_1 \int_0^1 dx_2 f_{a/h_1}(x_1, \mu_F^2) f_{b/h_2}(x_2, \mu_F^2) \frac{d\hat{\sigma}_{ab}}{dq_T^2}(q_T, M, \hat{s}; \alpha_S, \mu_R^2, \mu_F^2).$$

The standard fixed-order QCD perturbative expansions gives:

$$\int_0^{Q_T^2} dq_T^2 \frac{d\hat{\sigma}_{q\bar{q}}}{dq_T^2} \sim 1 + \alpha_S \left[c_{12} \log^2(M^2/Q_T^2) + c_{11} \log(M^2/Q_T^2) + c_{10}(Q_T) \right] \\ + \alpha_S^2 \left[c_{24} \log^4(M^2/Q_T^2) + \dots + c_{21} \log(M^2/Q_T^2) + c_{20}(Q_T) \right] + \mathcal{O}(\alpha_S^3)$$

Fixed order calculation theoretically justified only in the region $q_T \sim M_V$

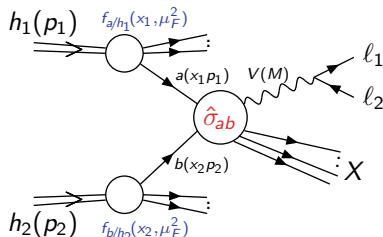
For $q_T \rightarrow 0$, $\alpha_S^n \log^m(M^2/q_T^2) \gg 1$: need for resummation of logarithmic corrections



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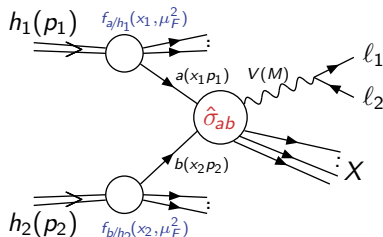
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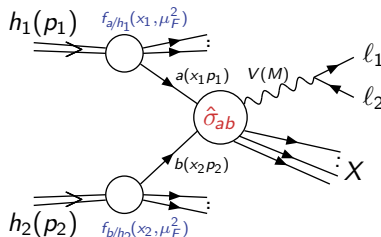
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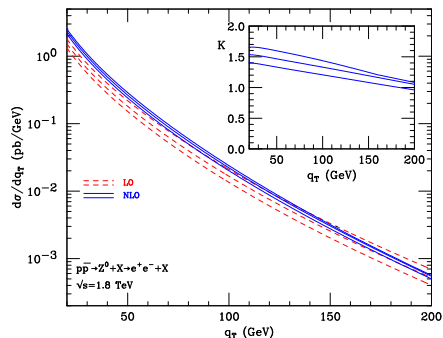
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Fixed order results: q_T spectrum of Drell-Yan e^+e^- pairs at $\sqrt{s} = 1.8$ TeV



- LO: pdf=MRST02 LO, 1-loop α_S
NLO: pdf=MRST04 NLO, 2-loop α_S
- Factorization and renormalization scale variations:
 $\mu_F = \mu_R = m_Z, \quad m_Z/2 \leq \mu_F, \mu_R \leq 2m_Z,$
 $1/2 \leq \mu_F/\mu_R \leq 2.$
 $q_T \sim m_Z : LO \pm 25\%, NLO \pm 8\%$
 $q_T \sim 20 \text{ GeV} : LO \pm 20\%, NLO \pm 7\%$
- q_T dependent K-factor:

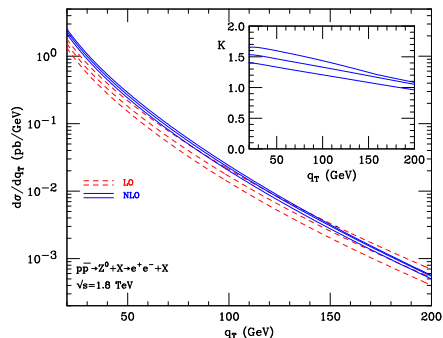
$$K(q_T) = \frac{d\sigma/dq_{T,NLO}(\mu_F, \mu_R)}{d\sigma/dq_{T,LO}(\mu_F = \mu_R = m_Z)}$$

$K \sim 1.1$ at $q_T \sim 200$ GeV up to
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LO and NLO scale variations bands overlap only for $q_T > 70$ GeV



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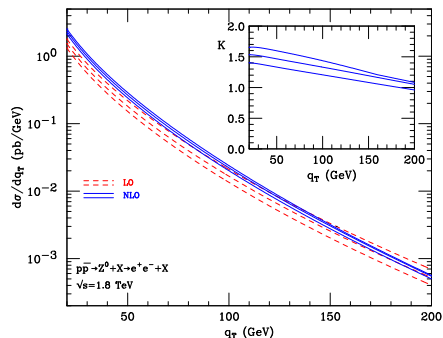
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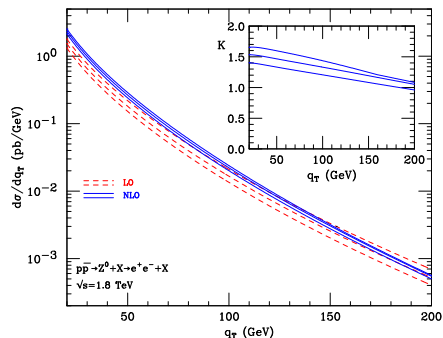
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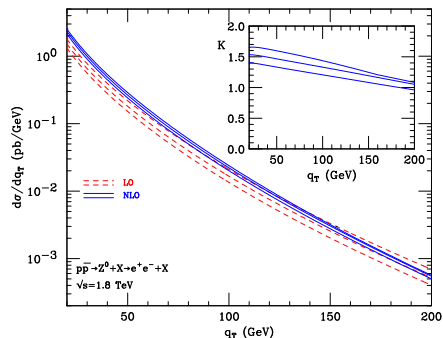
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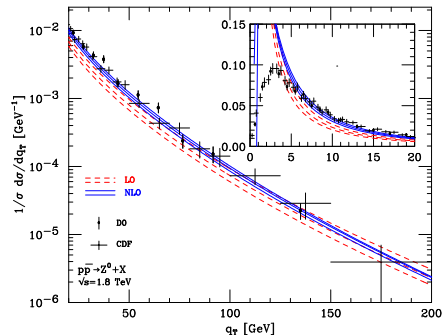
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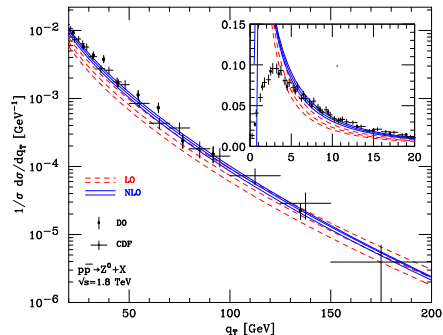
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- CDF data: $66 \text{ GeV} < M^2 < 116 \text{ GeV}$,
 $\sigma_{tot} = 248 \pm 11 \text{ pb}$
 [CDF Collaboration ('00)]
 D0 data: $75 \text{ GeV} < M^2 < 105 \text{ GeV}$,
 $\sigma_{tot} = 221 \pm 11 \text{ pb}$
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- Good agreement between NLO results and data up to $q_T \sim 20 \text{ GeV}$.
- In the small q_T region ($q_T \lesssim 20 \text{ GeV}$) LO and NLO result diverges to $+\infty$ and $-\infty$ (accidental partial agreement at $q_T \sim 5 - 7 \text{ GeV}$): need for resummation.



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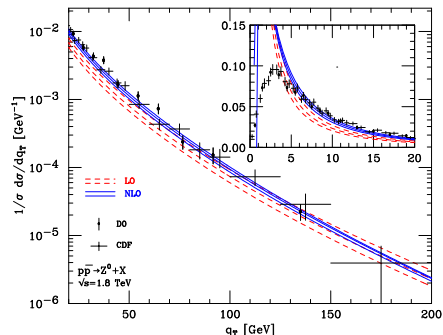


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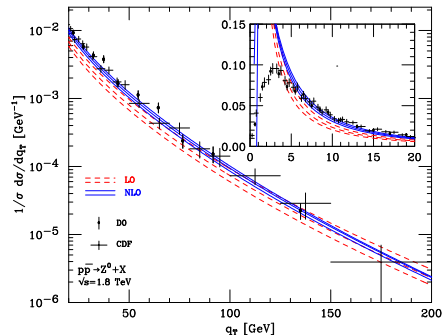
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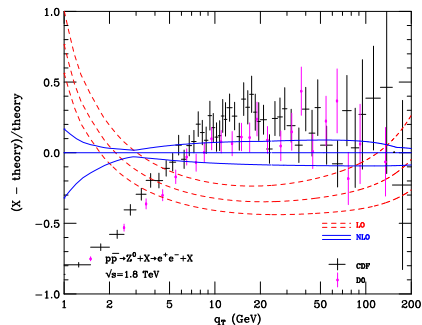
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- Percentage difference between data and theory:

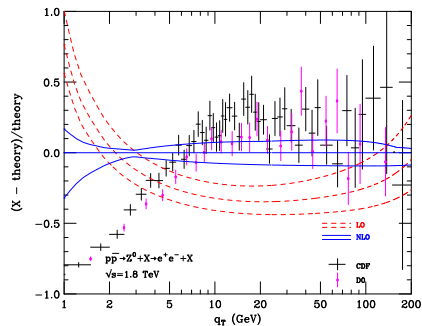
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$X = LO, NLO, data$

- Relative difference between LO and NLO:
very large at low q_T ,
 $\sim 40 - 50\%$ at intermediate q_T ,
small only at large q_T ($q_T \gtrsim m_Z$).
- Relative difference theory and data:
good agreement (one standard deviation) for
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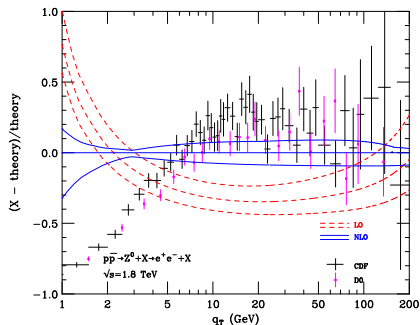
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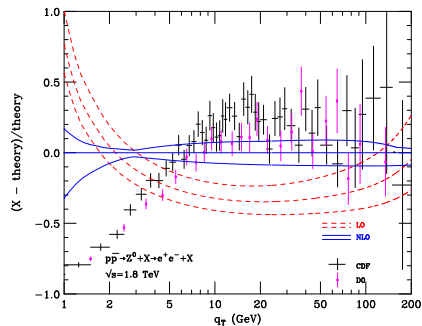
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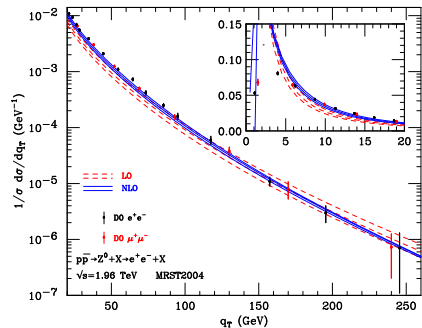
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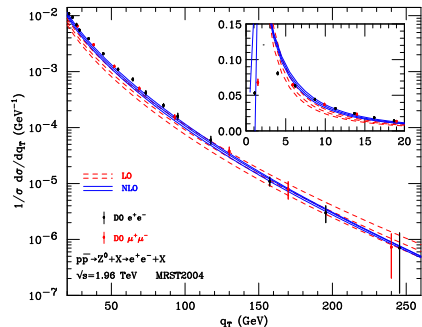
- D0 data normalized to 1: [D0 Coll.('08,'10)].
- Normalization reduces only marginally fixed order scale variations.
- Factorization and renormalization scale variations:
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 LO and NLO scale variations bands overlap only for $q_T > 60$ GeV
- Good agreement between NLO results and data up to $q_T \sim 20$ GeV.
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In the small q_T region ($q_T \lesssim 20$ GeV) effects of soft-gluon resummation are essential

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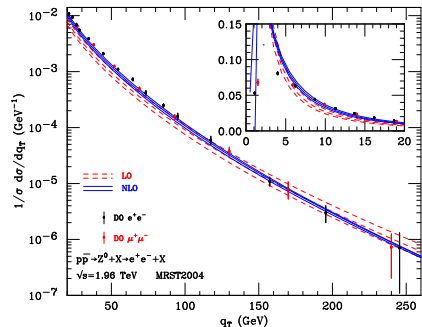
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Fixed order results: q_T spectrum of Drell-Yan l^+l^- pairs at $\sqrt{s} = 1.96$ TeV



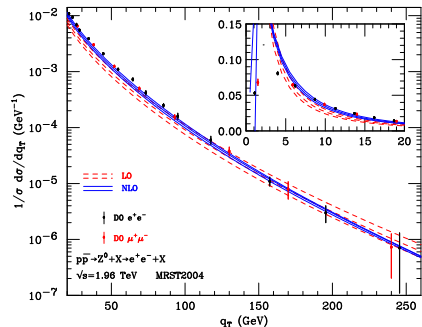
- D0 data normalized to 1: [D0 Coll.('08,'10)].
- Normalization reduces only marginally fixed order scale variations.
- Factorization and renormalization scale variations:
 $\mu_F = \mu_R = m_Z, \quad m_Z/2 \leq \mu_F, \mu_R \leq 2m_Z,$
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 LO and NLO scale variations bands overlap only for $q_T > 60$ GeV
- Good agreement between NLO results and data up to $q_T \sim 20$ GeV.
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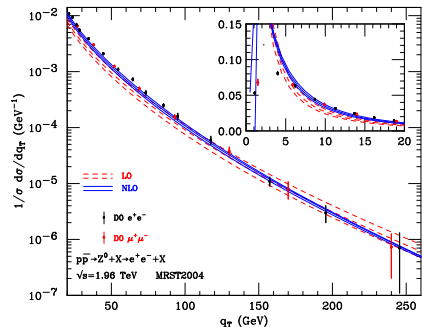
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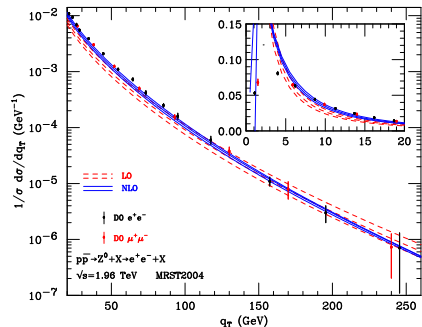
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State of the art: transverse-momentum resummation

- The method to perform the resummation of the large logarithms of q_T is known
 [Dokshitzer,Diakonov,Troian ('78)], [Parisi,Petronzio('79)],
 [Kodaira,Trentadue('82)], [Altarelli et al.('84)],
 [Collins,Soper,Sterman('85)], [Catani,de Florian,Grazzini('01)]
- Various phenomenological studies of the vector boson transverse momentum distribution exist
 [Balasz,Qiu,Yuan('95)], [Balasz,Yuan('97)], [Ellis et al.('97)],
 [Kulesza et al.('02)]
- Recently various results for transverse momentum resummation in the framework of Effective Theories appeared [Gao,Li,Liu('05), Idilbi, Ji, Yuan('05), Mantry,Petriello('10), Becher,Neubert('10)].



DY q_T resummation at NNLL+NLO:

Bozzi,Catani,G.F.,de Florian, Grazzini arXiv:1007.2351

- We have applied for Drell-Yan transverse-momentum distribution the resummation formalism developed by [Catani,de Florian, Grazzini('01)] already applied for the case of Higgs boson production [Bozzi,Catani,de Florian, Grazzini('03,'06,'08)].
- We have performed the resummation up to NNLL+NLO. It means that our complete formula includes:
 - NNLL logarithmic contributions to all orders;
 - NNLO corrections (i.e. $\mathcal{O}(\alpha_S^2)$) at small q_T ;
 - NLO corrections (i.e. $\mathcal{O}(\alpha_S)$) at large q_T ;
 - NNLO result for the total cross section (upon integration over q_T).
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Transverse momentum resummation

$$\frac{d\hat{\sigma}_{ab}}{dq_T^2} = \frac{d\hat{\sigma}_{ab}^{(res)}}{dq_T^2} + \frac{d\hat{\sigma}_{ab}^{(fin)}}{dq_T^2};$$

The finite component $\left(\lim_{Q_T \rightarrow 0} \int_0^{Q_T^2} dq_T^2 \left[\frac{d\hat{\sigma}_{ab}^{(fin)}}{dq_T^2} \right]_{f.o.} = 0 \right)$
ensure to reproduce the fixed order calculation at large q_T

Resummation holds in impact parameter space:

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The q_T resummation formalism

The main distinctive features of the formalism we are using are [Catani,de Florian, Grazzini('01)], [Bozzi,Catani,de Florian, Grazzini('03,'06,'08)]:

- Resummation performed at partonic cross section level: PDF evaluated at $\mu_F \sim M$: no PDF extrapolation in the non perturbative region, study of renormalization and factorization scale dependence as in fixed-order calculations.
- Possible to make prediction without introducing non perturbative effects: Landau singularity of the QCD coupling regularized using a *minimal prescription* [Laenen,Sterman,Vogelsang('00)], [Catani et al.('96)].
- Resummed effects exponentiated in a **universal** Sudakov form factor $\mathcal{G}_N(\alpha_S, L)$; process-dependence factorized in the hard scattering coefficient $\mathcal{H}_N(\alpha_S)$.
- Perturbative unitarity constrain and resummation scale Q :

$$\ln\left(\frac{M^2 b^2}{b_0^2}\right) \rightarrow \tilde{L} \equiv \ln\left(\frac{Q^2 b^2}{b_0^2} + 1\right)$$

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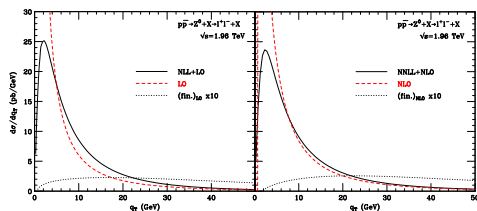
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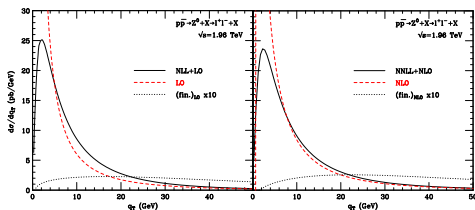
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- Left side: NLL+LO result compared with fixed LO result. Resummation cures the fixed order divergence at $q_T \rightarrow 0$.
- Right side: NNLL+NLO result compared with fixed NLO result.
- The q_T spectrum is slightly harder at NNLL+NLO accuracy than at NLL+LO accuracy.
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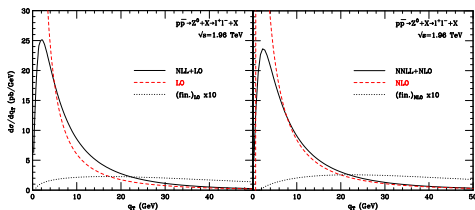
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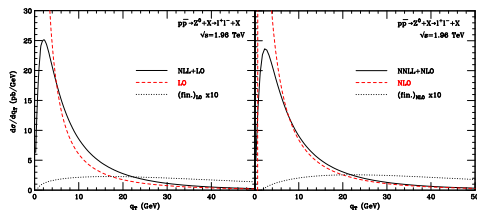
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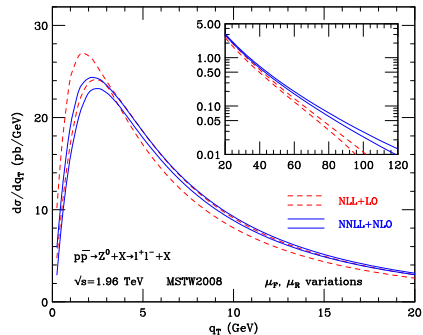
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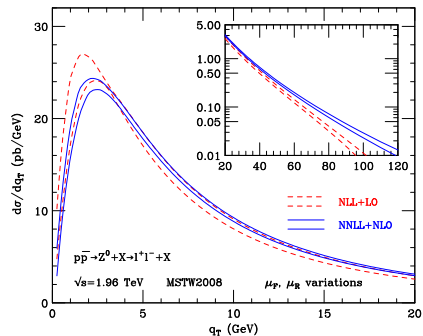
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- Our calculation implements γ^*Z interference and finite-width effects. Here we use the narrow width approximation (differences within 1% level).
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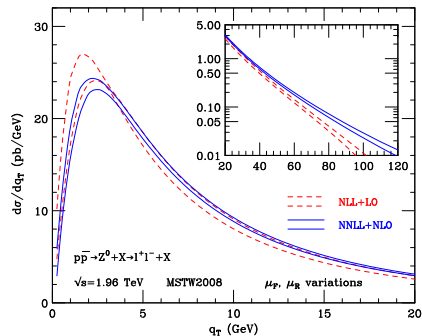
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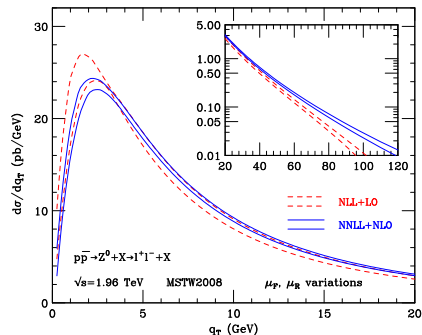
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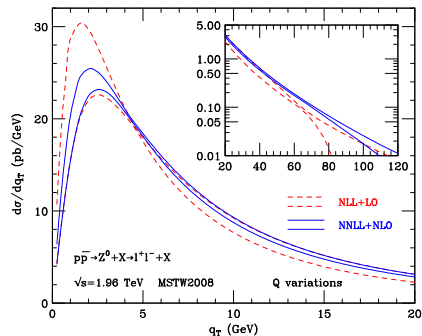
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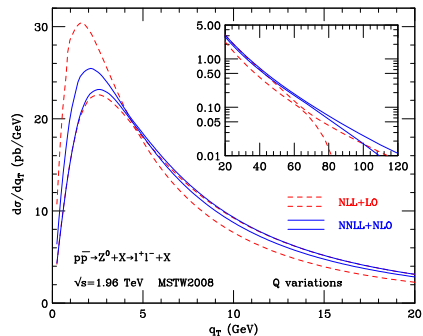
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- Uncertainty bands obtained by performing resummation scale variations (estimate of higher-order logarithmic contributions): $m_Z/4 \leq Q \leq m_Z$ with $\mu_F = \mu_R = m_Z$.
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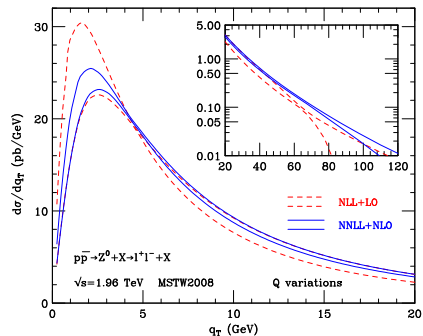
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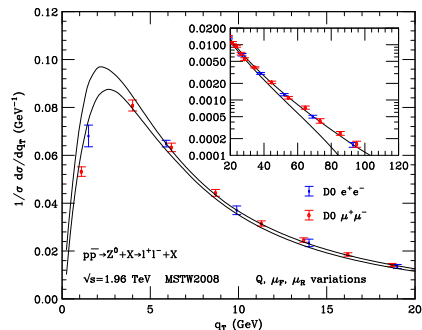
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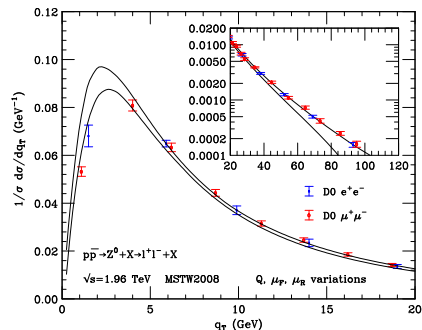
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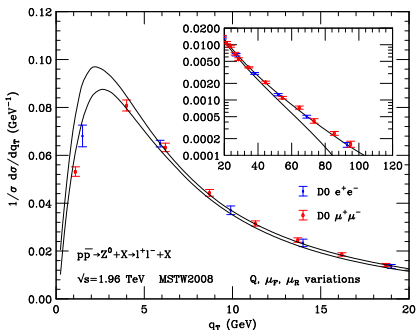
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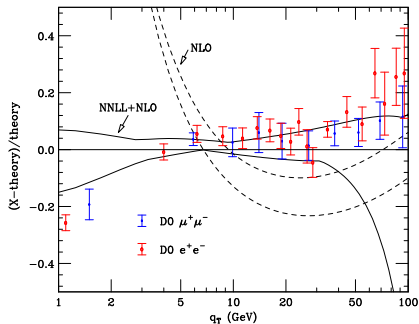
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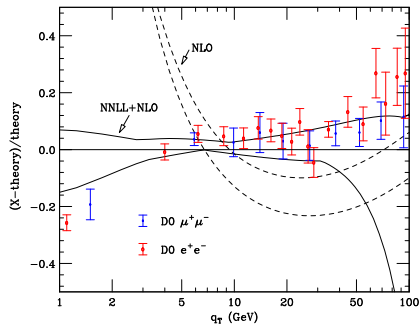
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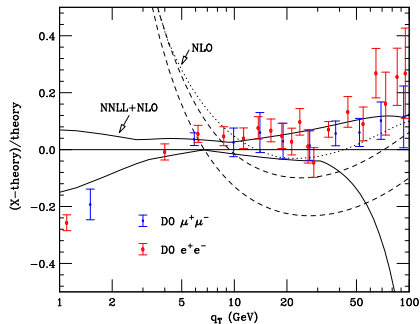
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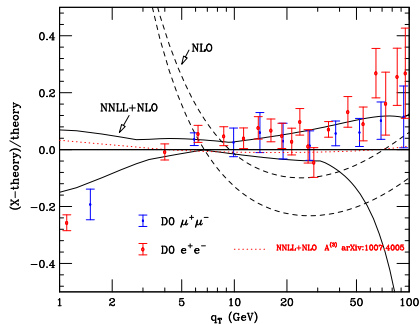
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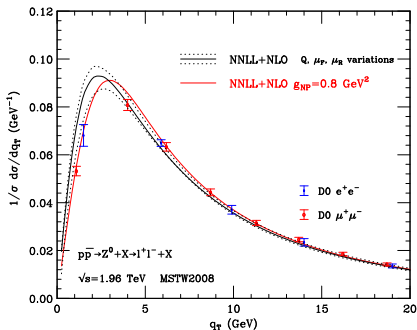
Resummed results: q_T spectrum of Drell-Yan l^+l^- pairs at $\sqrt{s} = 1.96$ TeV



- Fractional difference with respect to the reference result: NNLL+NLO, $\mu_R = \mu_F = 2Q = m_Z$.
- NNLL+NLO scale dependence is $\pm 6\%$ at the peak, $\pm 5\%$ at $q_T = 10$ GeV and $\pm 12\%$ at $q_T = 50$ GeV. For $q_T \geq 60$ GeV the resummed result loses predictivity.
- At large values of q_T , the NLO and NNLL+NLO bands overlap.
At intermediate values of transverse momenta the scale variation bands do not overlap: **we added the NLO curve with $\mu_F = m_Z/4$.**
The resummation improves the agreement of the NLO results with the data.
In the small- q_T region, the NLO result is theoretically unreliable and the NLO band deviates from the NNLL+NLO band.
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Non perturbative effects: q_T spectrum of Drell-Yan l^+l^- pairs at $\sqrt{s}=1.96$ TeV



- Up to now result in a complete perturbative framework.
- Non perturbative effects parametrized by a NP form factor $S_{NP} = \exp\{-g_{NP} b^2\}$:

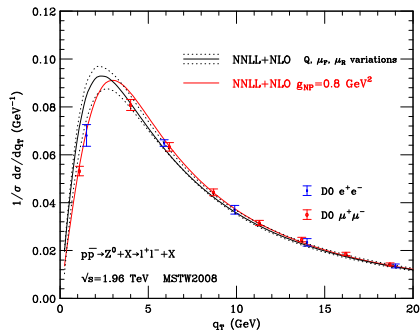
$$\exp\{\mathcal{G}_N(\alpha_S, \tilde{L})\} \rightarrow \exp\{\mathcal{G}_N(\alpha_S, \tilde{L})\} S_{NP}$$

$$g_{NP} = 0.8 \text{ GeV}^2 \quad [\text{Kulesza et al. ('02)}]$$

- With NP effects the q_T spectrum is harder.
- Quantitative impact of such NP effects is comparable with perturbative uncertainties.



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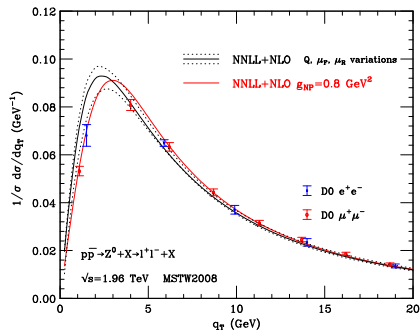
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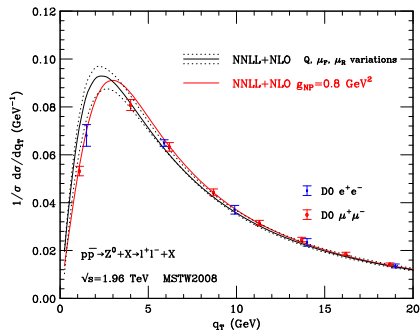
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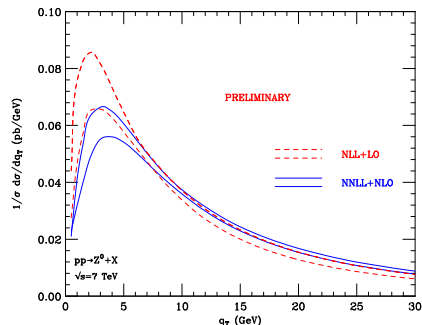
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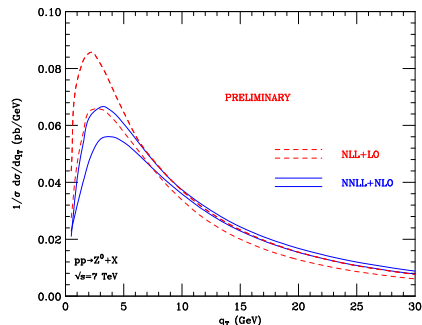
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Resummed results: q_T spectrum of Drell-Yan e^+e^- pairs for LHC at $\sqrt{s}=7$ TeV

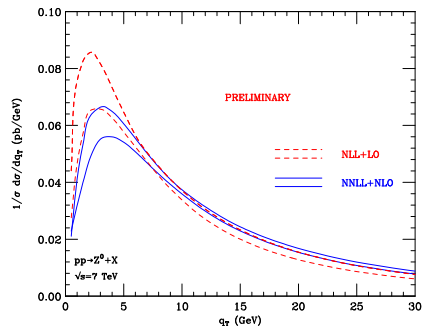
- Uncertainty bands obtained varying μ_R , μ_F , Q independently: $m_Z/2 \leq \{\mu_F, \mu_R, 2Q\} \leq 2m_Z$ with the constraints $0.5 \leq \{\mu_F/\mu_R, Q/\mu_R\} \leq 2$ which avoid large logarithmic contributions ($\sim \ln(\mu_F^2/\mu_R^2)$, $\ln(Q^2/\mu_R^2)$) in the evolution of the parton densities and in the the resummed form factor.
- The scale dependence at NNLL+NLO (NLL+LO) is about $\pm 9\%$ ($\pm 13\%$) around the peak and $\pm 4\%$ ($\pm 11\%$) in the $q_T \gtrsim 20$ GeV region and it is larger than the one at the Tevatron.
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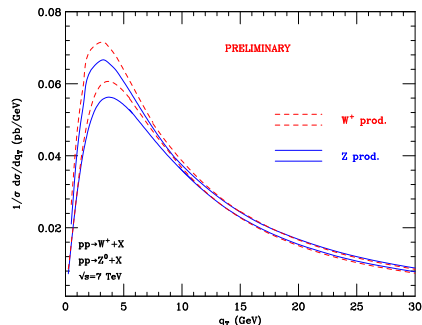
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Resummed results: q_T spectrum of Drell-Yan e^+e^- pairs for LHC at $\sqrt{s}=7\text{ TeV}$:

comparison between the Z and the W shape.

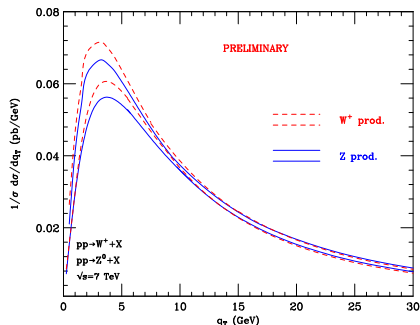


- Same uncertainty bands as before:
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It means **NNLL** resummation, **NNLO** corrections at small q_T ; **NLO** corrections at large q_T ; σ_{TOT} at **NNLO** (upon integration over q_T).
- A public version of our code **DYqT** will be available in the near future.
- The size of the scale uncertainties is considerably reduced in going from NLL+LO to NNLL+NLO accuracy.
- The NNLL+NLO results (without the inclusion of any non-perturbative effects) are consistent with the experimental data in a wide region of transverse momenta and improve the agreement of the NLO results with the data at small and intermediate values of q_T .
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