

Degeneracy between Interacting Dark Energy and Primordial Non-Gaussianity

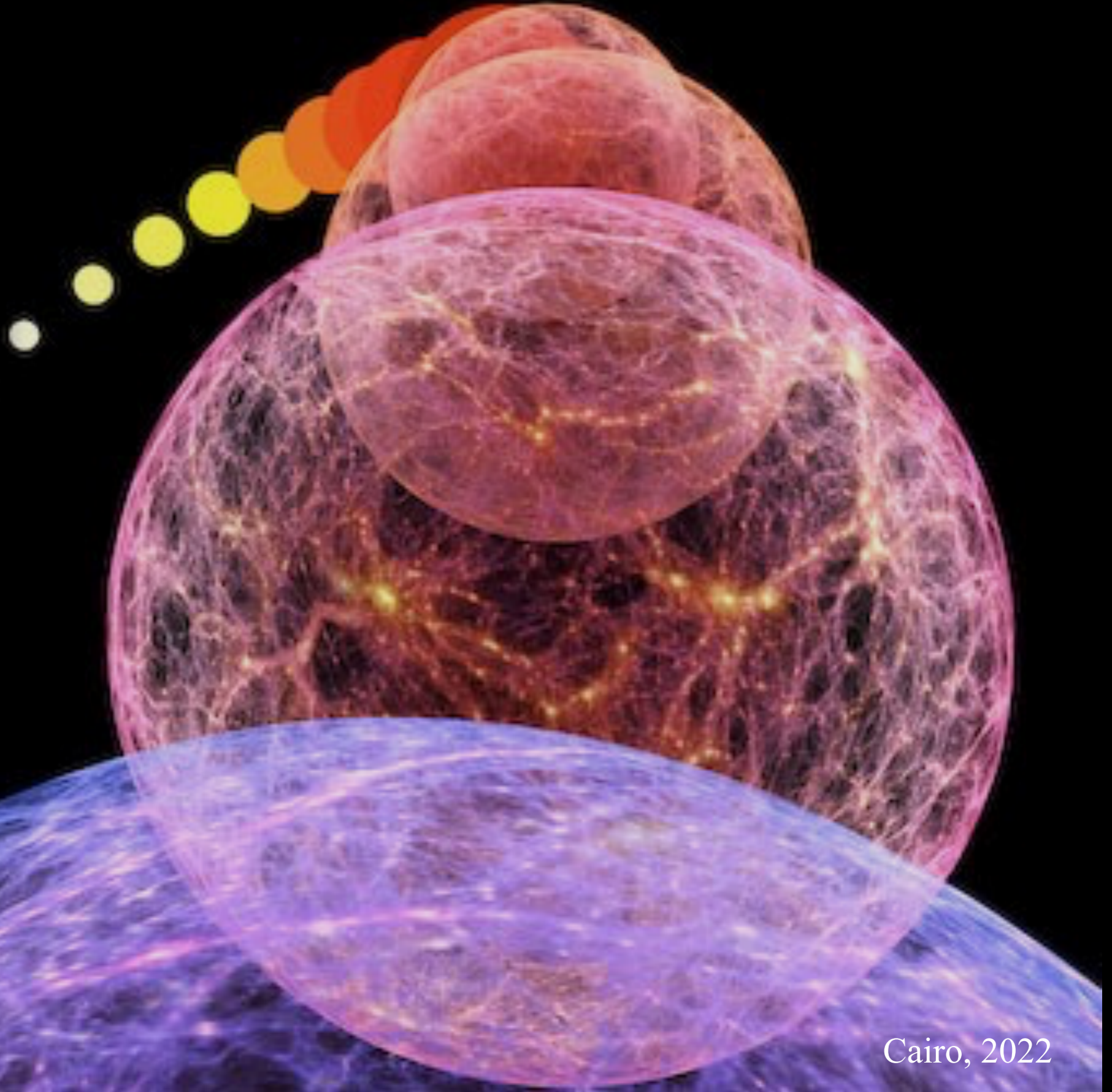
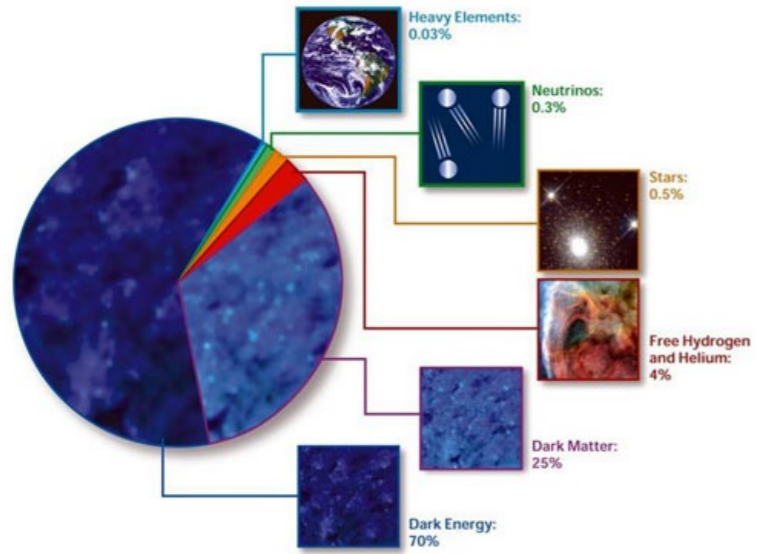
Mahmoud Hashim
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The British University in Egypt



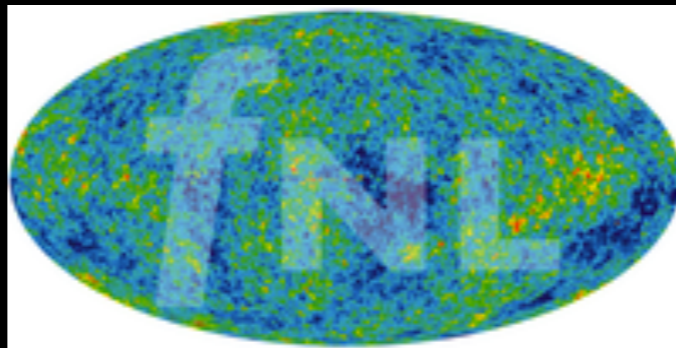
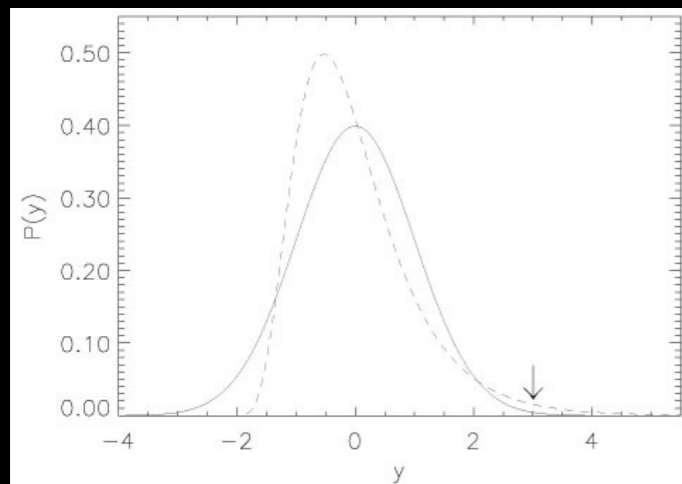
Workshop on Astro-particles and Gravity, Cairo U., 20-22 Sept, 2022

Structure Formation

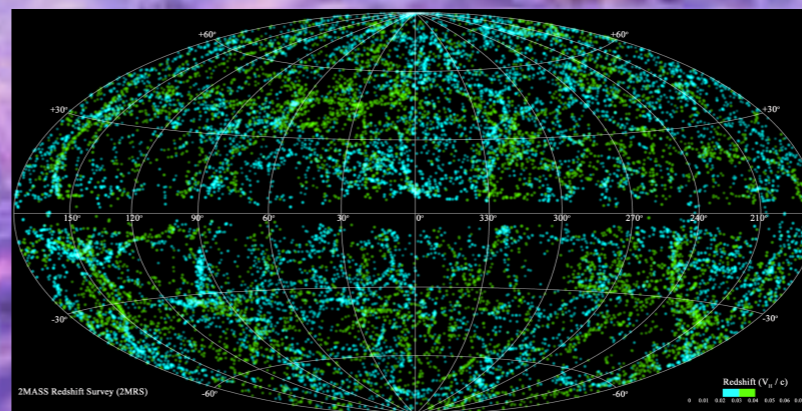
COMPOSITION OF THE COSMOS



primordial non-Gaussianity (Inflation)



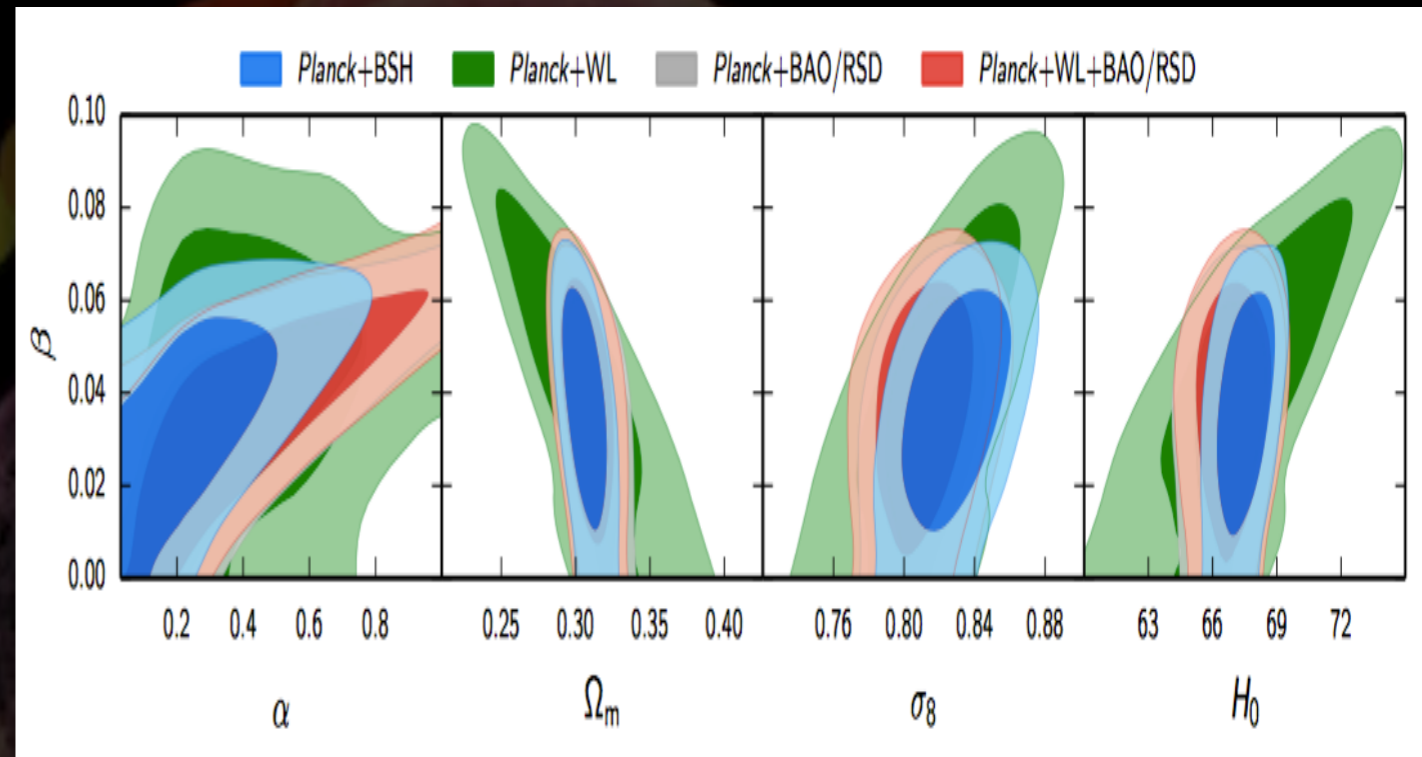
Dark Sector
(Dark Matter & Dark Energy)



Interacting Dark Energy

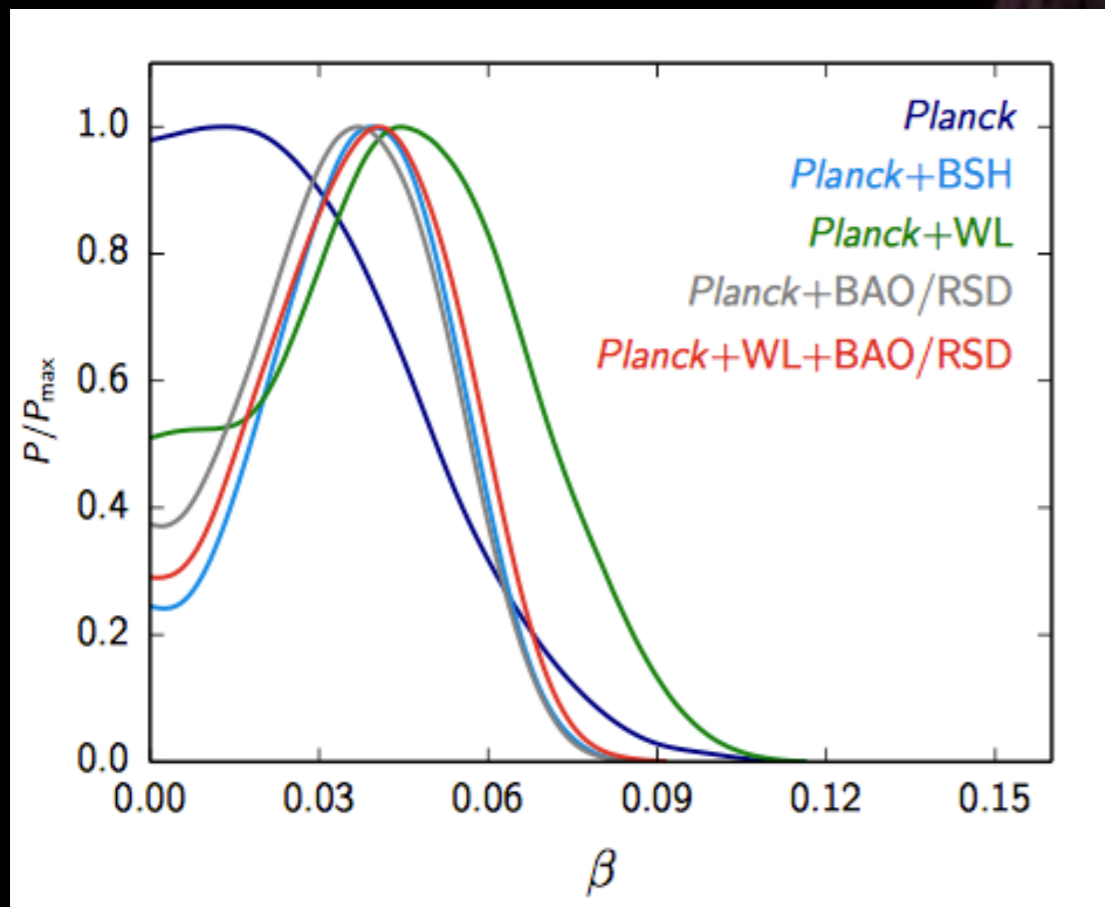
Interaction between Dark Energy and Dark Matter is a theoretical possibility that may help to solve the **coincidence problem**.

Dark energy and dark matter interact via **energy-momentum** exchange.



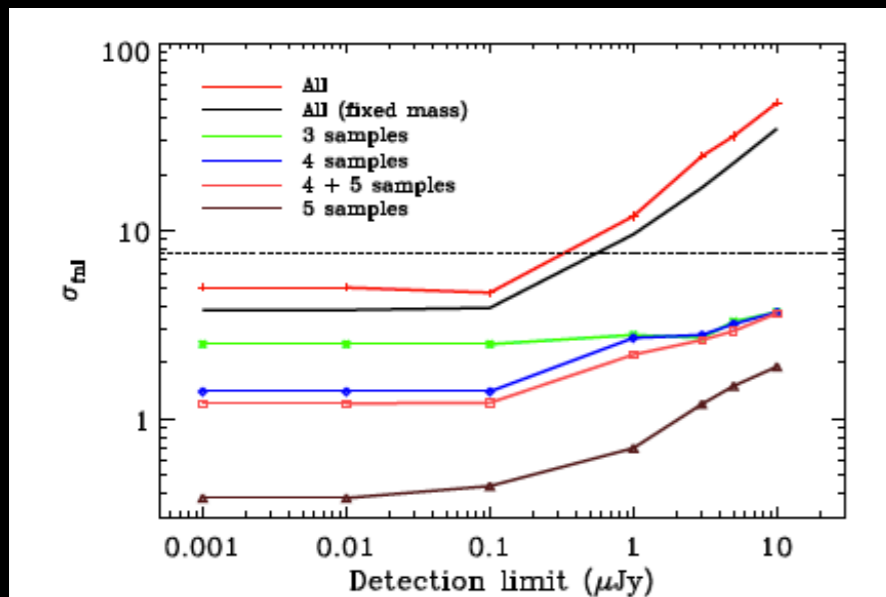
Planck Collaboration 2015 (arXiv:1502.01590)

The transfer of energy-momentum between dark matter and dark energy is **not ruled out** by current observations.

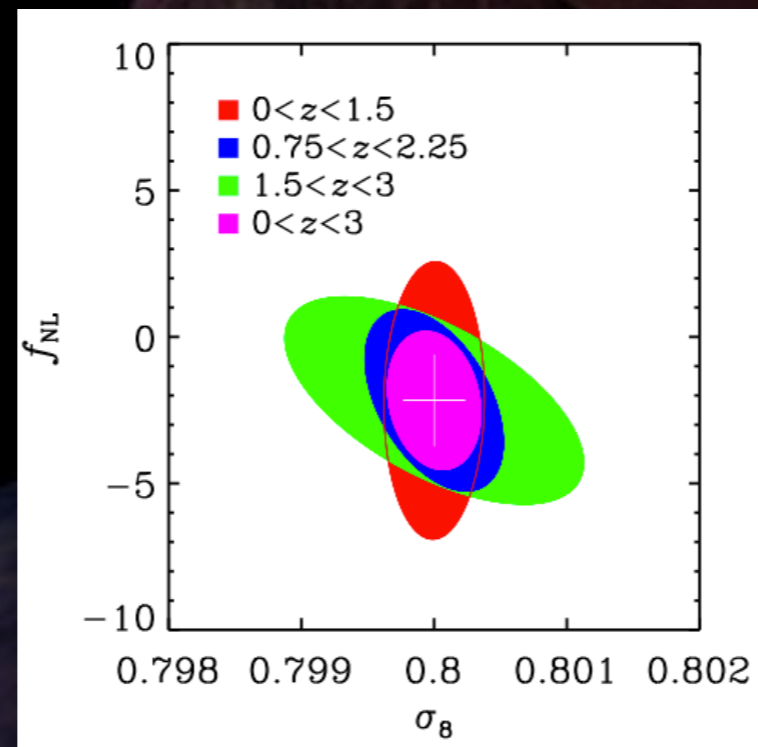


Primordial Non-Gaussianity

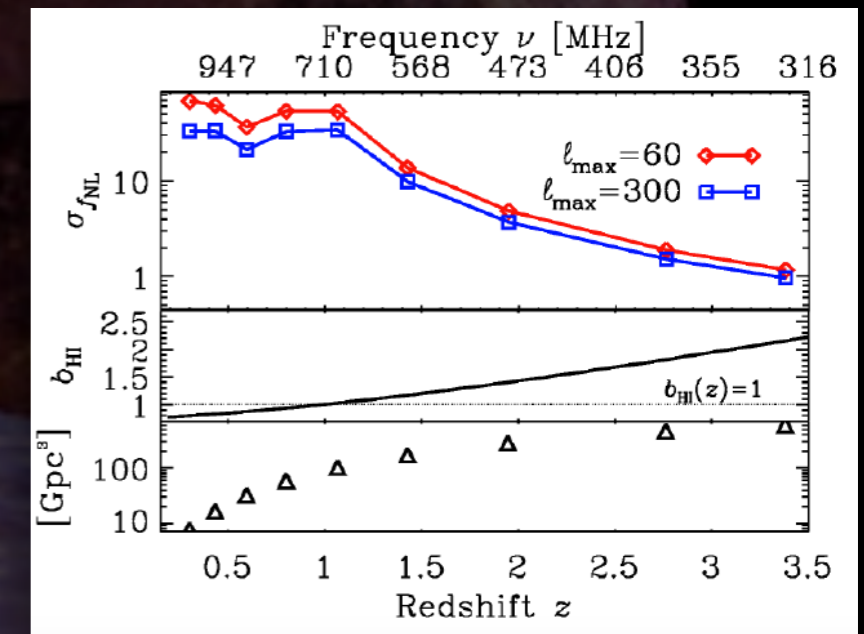
- Primordial Non-Gaussianity (PNG) is used to **discriminate** between different inflation models.
- Planck has shown that PNG is **not large**.
- In order to further and detect small PNG, we need larger **galaxy surveys**.



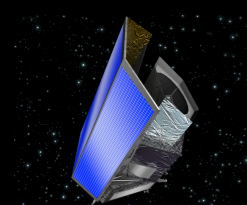
Forecast for SKA continuum surveys, Ferramacho et al. 2014



Forecast for SKA HI galaxy redshift surveys, Camera et al. 2014



Forecast for SKA HI intensity mapping surveys, Camera et al. 2013



LSS_(EUCLID, SKA, ..)

$\Lambda + \text{CDM}$

vs

$\beta(\phi + \text{CDM}) + \text{fNL}$

likelihood analysis

$$f_{obs} \rightarrow f_{thr}(p_i = \{H_0, \Omega_m, \Lambda, \dots, n_s, A_s, \dots\}) \approx f'_{thr}(p_i = \{H_0, \Omega_m, \phi, \dots, w_\phi, \beta, n_s, A_s, \text{fNL}, \dots\})$$

Observational Probes

Background

Angular diameter distance; BAO
Distance Modulus; SNIa, ...

Perturbed

nonlinear(N-Body) linear(LPT)

Linear Power Spectrum Bispectrum?

Halo Statistics Nonlinear Power Spectrum
Halo Structural Properties Halo Bias

$$\rho'_A + 3(1 + w_A)\rho_A = \frac{aQ_A}{\mathcal{H}} \quad Q_x = -Q_m.$$

$$Q_x = \Gamma\rho_x = -Q_m.$$

Continuity Equation

Energy Transfer

Interaction term

$$\nabla^2\Phi = \frac{3}{2}\mathcal{H} \sum_A \Omega_A [\delta_A - 3\mathcal{H}(1 + w_A)v_A],$$

Poisson Equation

Interaction perturbation source term

$$\Delta_A = \delta_A + \frac{\rho'_A}{\rho_A} v_A.$$

$$\nabla^2\Phi = \frac{3}{2}\mathcal{H}^2 \left(\sum_A \Omega_A \Delta_A - Q^\Phi \right),$$

$$Q^\Phi = \frac{a}{\rho_t} \sum_A Q_A v_A = \frac{a}{\rho_t} Q_x (v_x - v_m).$$

$$D_m(k, a) = \frac{\Delta_m(k, a)}{\Delta_{md}(k)} a_d,$$

Matter Growth factor

$$D_m = \frac{\Omega_{md}}{\Omega_m(1 + \mu)} \left[\frac{a_d \mathcal{H}_d^2}{a \mathcal{H}^2} D_\Phi - \mu \frac{\Omega_x}{\Omega_{xd}} D_x - B \frac{a_d \mathcal{H}_d^2}{T(k) k^{n_s/2}} Q^\Phi \right],$$

$$Q^\Phi = a \Gamma \Omega_x (v_x - v_m).$$

Dark Energy
source term

Scale-dependent interaction
source term



Linear Perturbation Theory

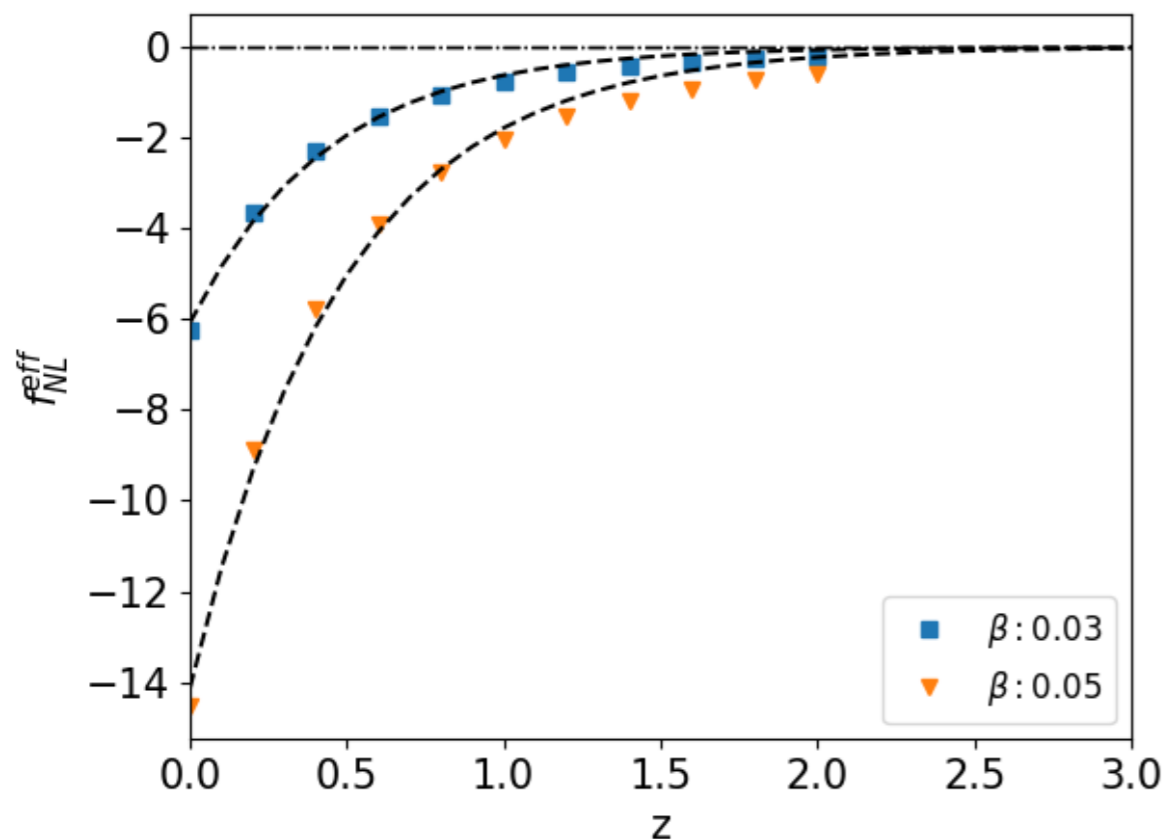
$\Lambda + \text{CDM}$

vs

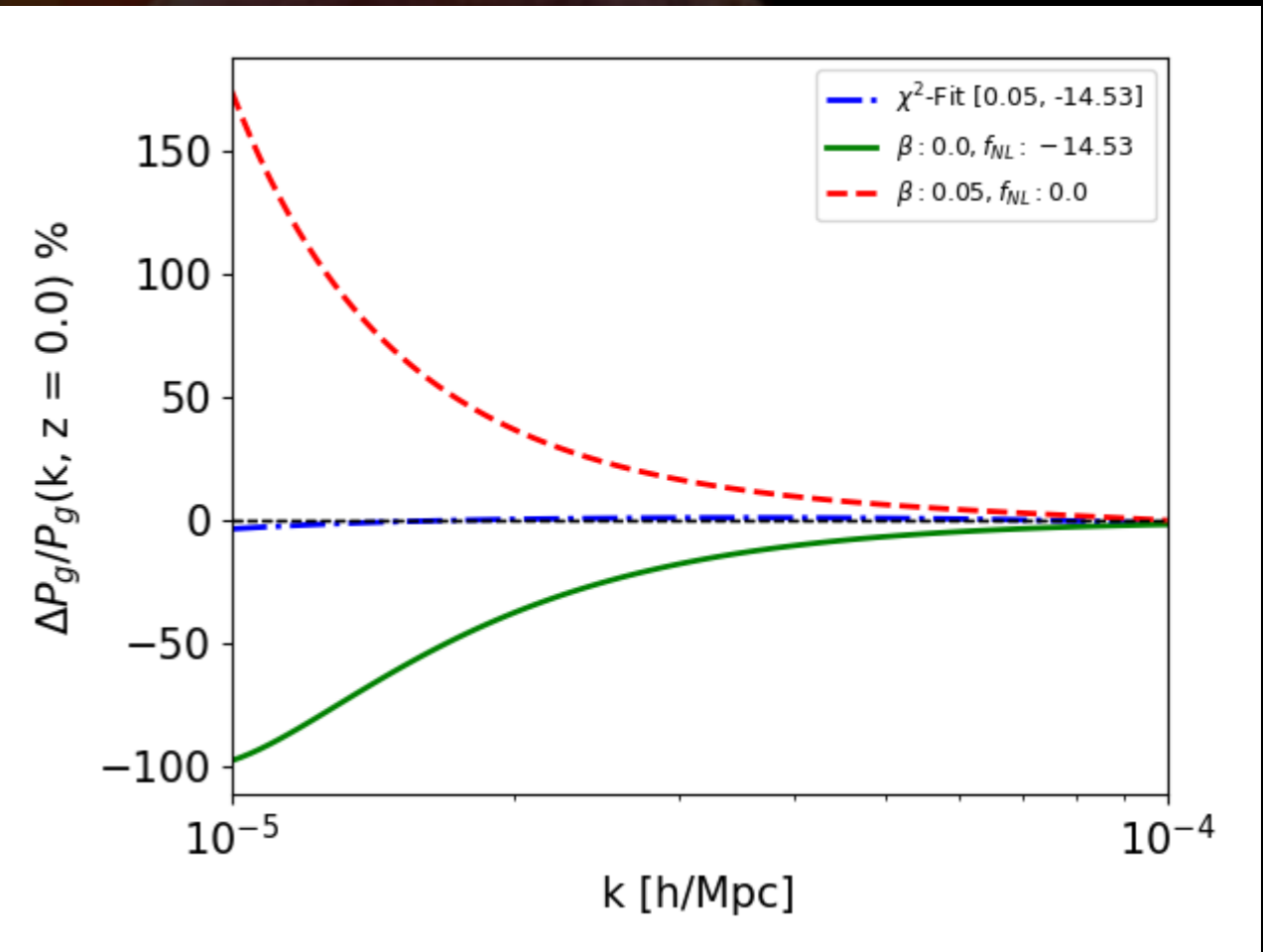
$\beta(\phi + \text{CDM}) + \text{fNL}$

$$b(k, z) = b_g(z) + \Delta b(k, z),$$

$$\Delta b = 3f_{\text{NL}}(b - 1) \frac{\delta_c H_0^2 \Omega_{m0}}{k^2 T D_m},$$

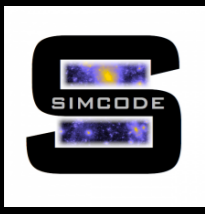


$$f_{\text{NL}}^{\text{eff}} = a e^{-bz} \beta,$$



$$P_g(k, a) = b^2 P_m(k, a),$$

$$P_m(k, a) = \frac{9A^2}{50\pi^3 H_0^n} k^n T(k)^2 \left[\frac{D_m(k, a)}{D_{\Phi 0}(k)} \right]^2.$$



$\Lambda + \text{CDM}$

vs

$\beta(\phi + \text{CDM}) + \text{fNL}$

Initial Conditions

Gaussian particle distribution.

Add non-Gaussianity

$$\Phi = \phi + f_{\text{NL}}(\phi^2 - \langle \phi^2 \rangle),$$

Structure Formation

Initial power spectrum.

Modified amplitude but same shape.

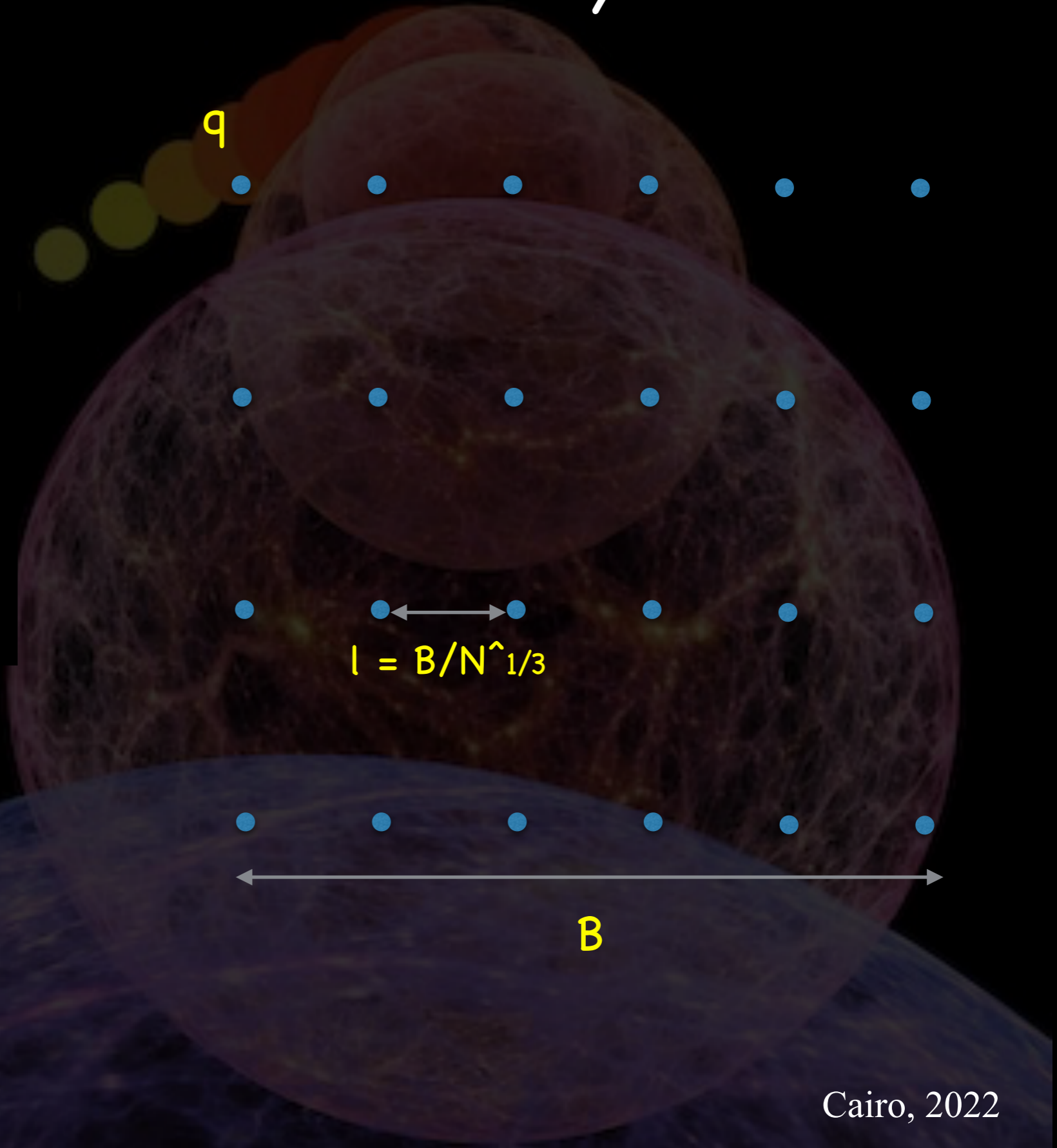
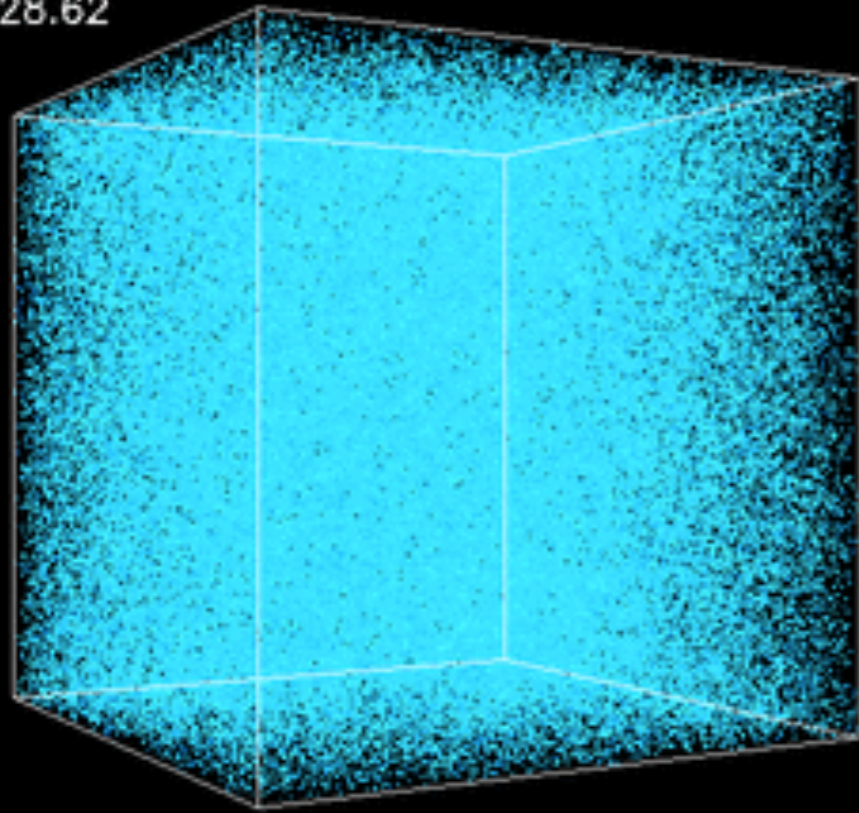
- Modified expansion rate.
- Mass variation.
- Extra velocity-dependent acceleration.
- Fifth force.

$$\tilde{H} \equiv H \left(1 - \frac{\beta(\phi)}{M} \frac{\dot{\phi}}{H} \right) \quad f(a) \sim \Omega_M^\gamma \left(1 + \gamma \frac{\Omega_{\text{CDM}}}{\Omega_M} \epsilon_c \beta_c^2 \right)$$

$$\tilde{G}_c = G_N [1 + 2\beta^2(\phi)], \quad \tilde{M}_c \equiv M_c e^{-\int \beta(\phi) \frac{d\phi}{da} da}$$

N-Body Simulation

$z=28.62$

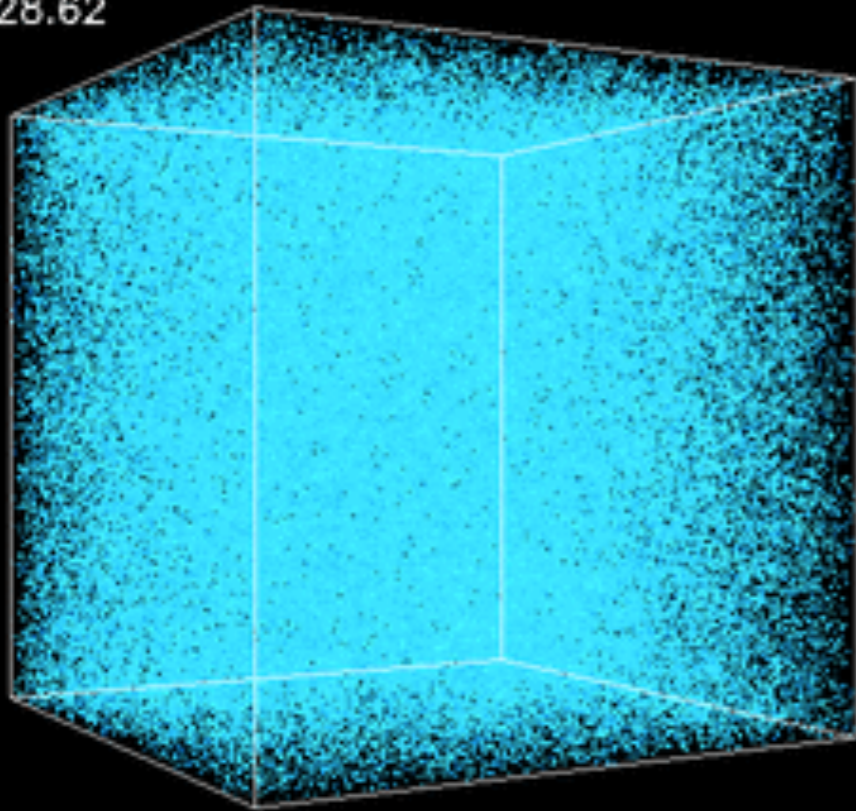


$$l = B/N^{1/3}$$

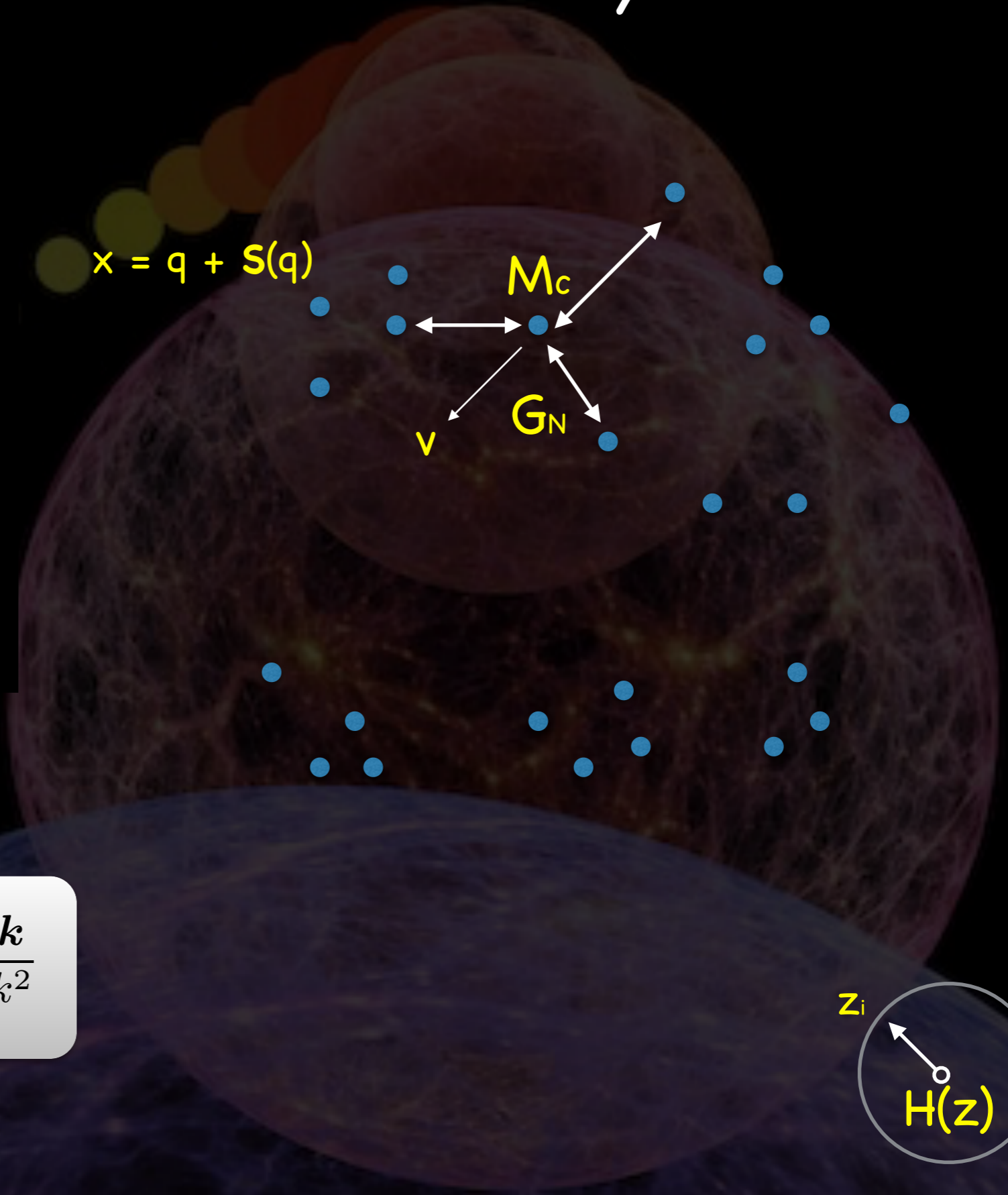
B

N-Body Simulation

$z=28.62$

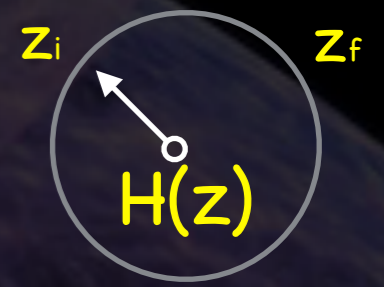


$$\mathbf{x} = \mathbf{q} + \mathbf{S}(\mathbf{q})$$

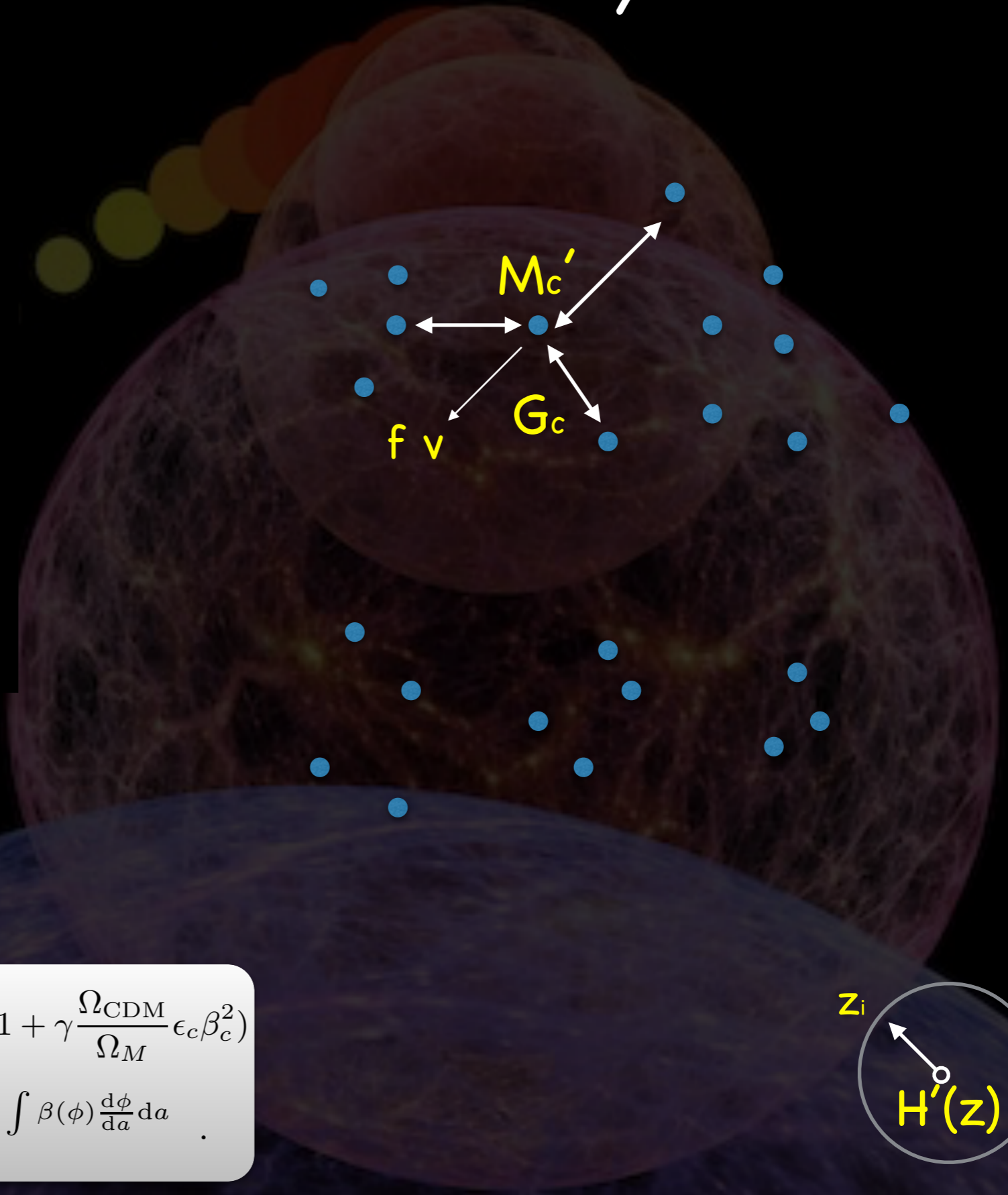
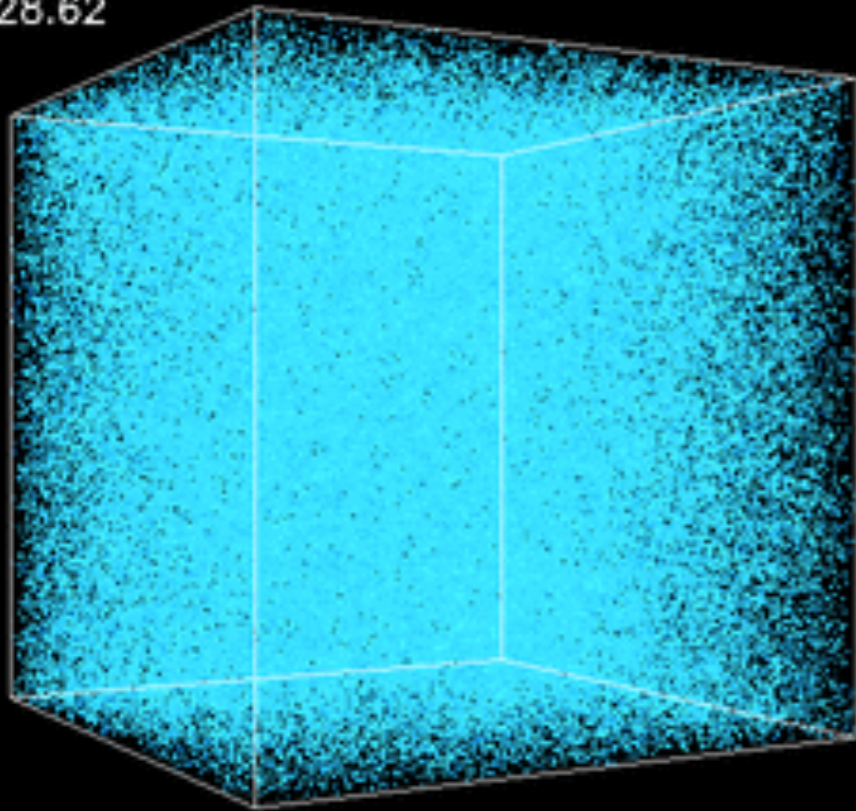


+ ICs (ZA, 2LPT)

$$\mathbf{v}(\mathbf{k}, a) = if(a)aH\delta(\mathbf{k}, a)\frac{\mathbf{k}}{k^2}$$



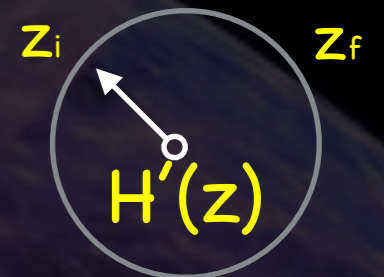
$z=28.62$



+ ICs (ZA, 2LPT)
+ Interaction

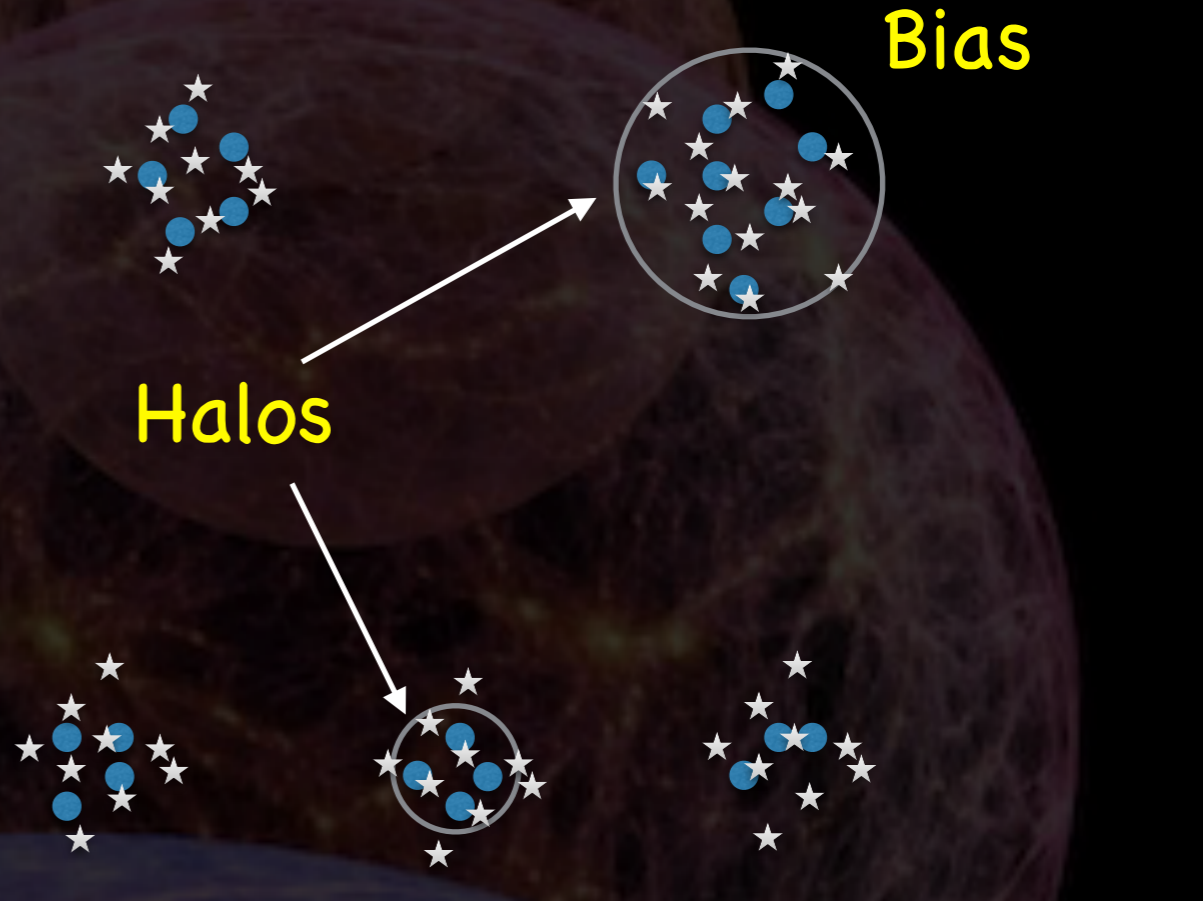
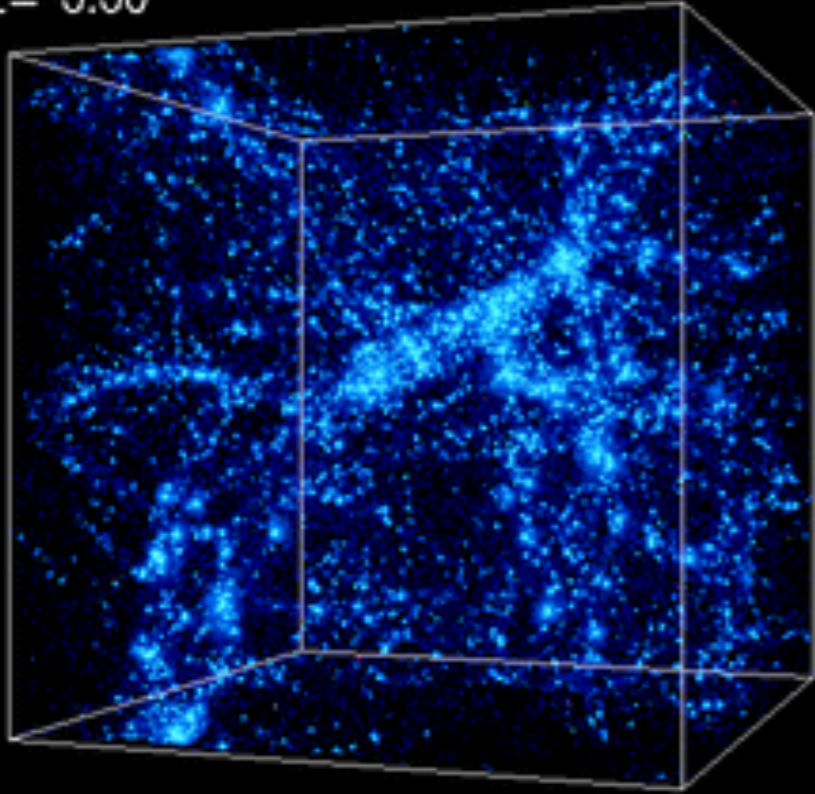
$$\tilde{H} \equiv H \left(1 - \frac{\beta(\phi)}{M} \frac{\dot{\phi}}{H} \right) \quad f(a) \sim \Omega_M^\gamma (1 + \gamma \frac{\Omega_{\text{CDM}}}{\Omega_M} \epsilon_c \beta_c^2)$$

$$\tilde{G}_c = G_N [1 + 2\beta^2(\phi)], \quad \tilde{M}_c \equiv M_c e^{-\int \beta(\phi) \frac{d\phi}{da} da} .$$



N-Body Simulation

$z = 0.00$

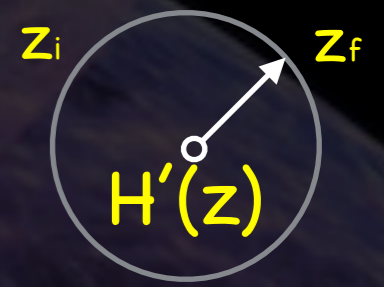


+ ICs (ZA, 2LPT)

+ Interaction

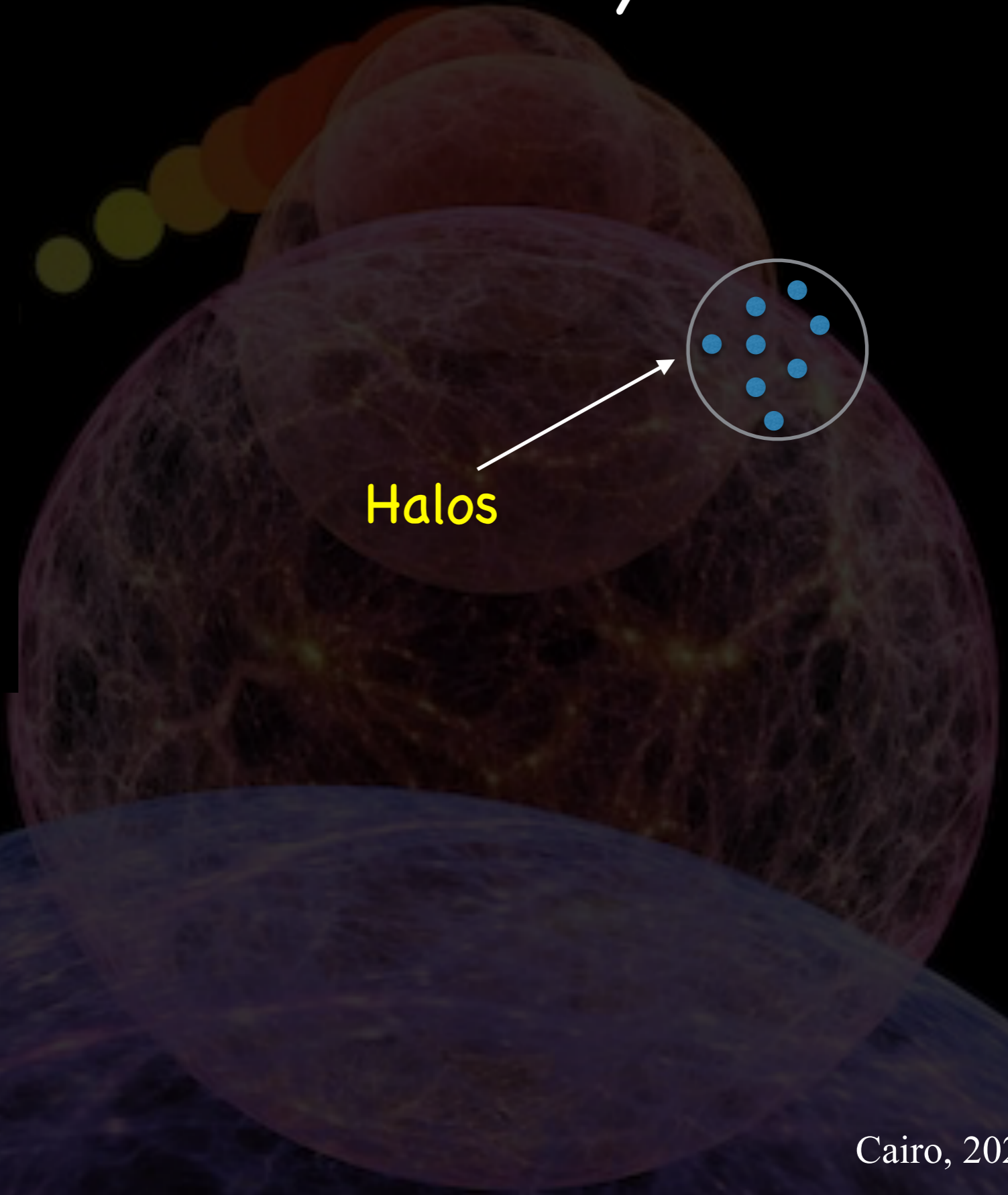
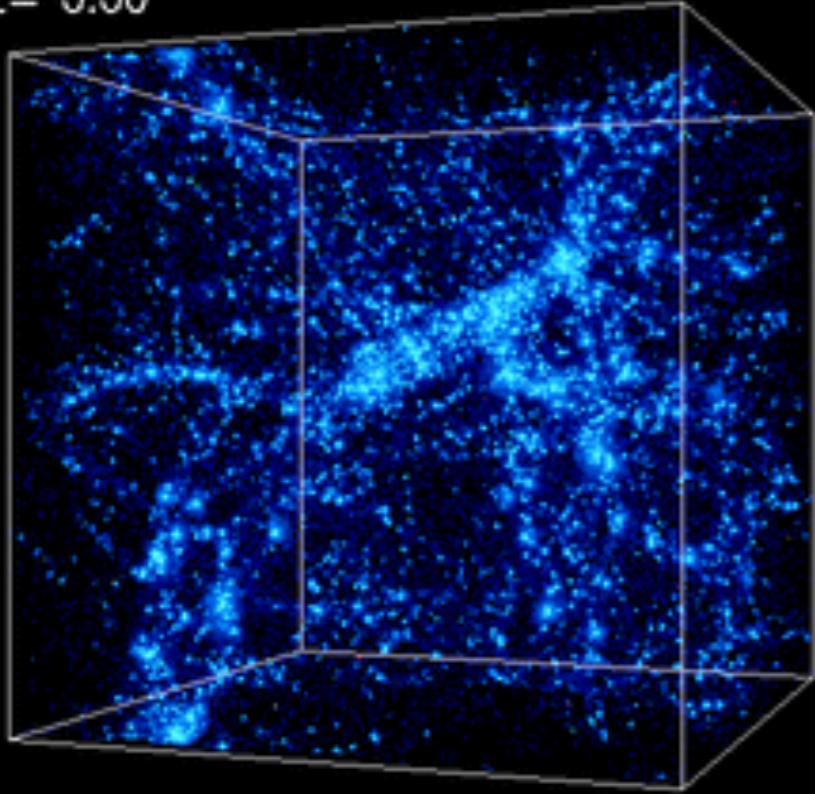
+ Evolution

$$\dot{\rho}_c + 3H\rho_c = -\sqrt{\frac{2}{3}}\beta_c(\phi)\frac{\rho_c\dot{\phi}}{M_{\text{Pl}}}$$



N-Body Simulation

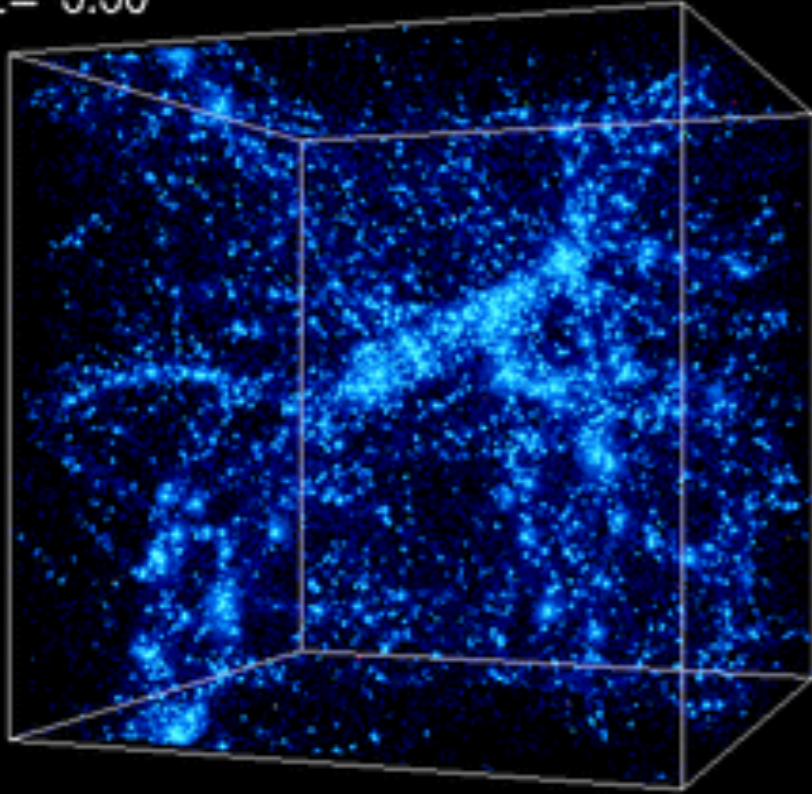
$Z = 0.00$



Halos

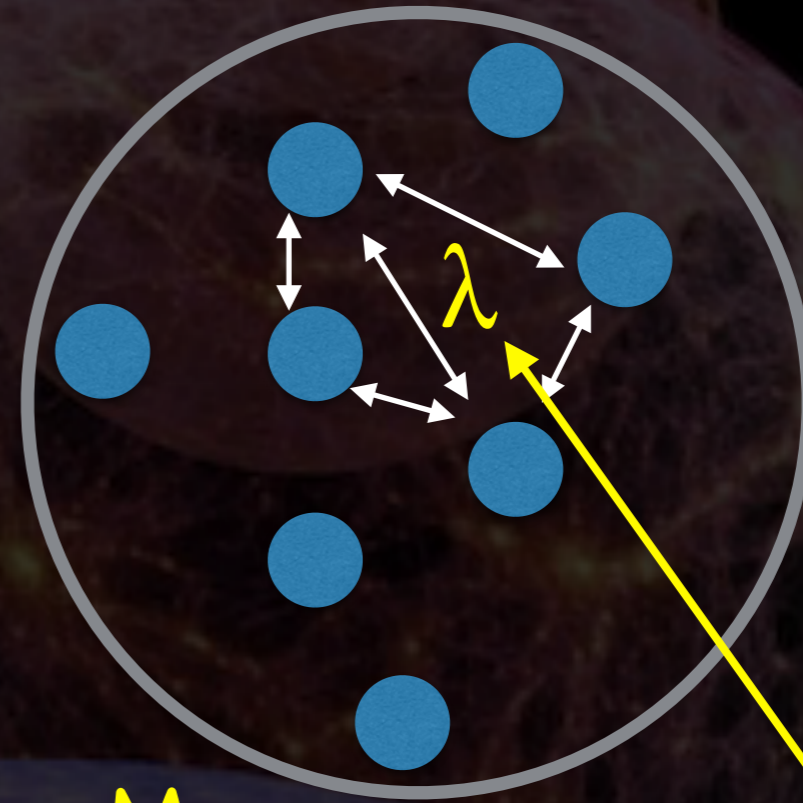
N-Body Simulation

$Z = 0.00$



Halos (HMF)

$$\frac{dn}{d \log M} = \frac{M}{L^3} \frac{\Delta N}{\Delta \log M}$$



FoF

M

$$\lambda \equiv \mathbf{b} \cdot l$$

CosmoSuite v.1

Perturbative Cosmology | CAMB

Data File Loading

Local Directory: /Users/mahmoud/Desktop | select | log file

Run Name: RUN02 | Results: Snaps | Data Files: XYZSnapPos.dat

File Preview | Set Header | File Update

File Preview

597.230408	5.392182	8.143722
596.924866	5.702603	8.552315
596.820068	5.724774	8.229371
597.333252	5.634561	10.778337
597.725342	6.399818	13.514186
598.038757	7.049821	15.493662
597.949402	7.465845	16.814236
598.048889	7.523783	17.863222
598.175659	6.559597	21.405462
597.445435	5.770187	24.260609
596.461487	5.855588	27.751532
595.744141	7.287629	34.002625
596.289490	8.032180	36.809811
596.541077	7.889088	36.163857
596.222961	8.166137	36.556633

xyz | xyz | Add file

Data Plots

- LCDM_fNL_250_005.0000.z2
- LCDM_fNL_500_005.0000.z2
- LCDM_fNL_1000_005.0000.z2
- XYZSnapPos.dat

Plot Options

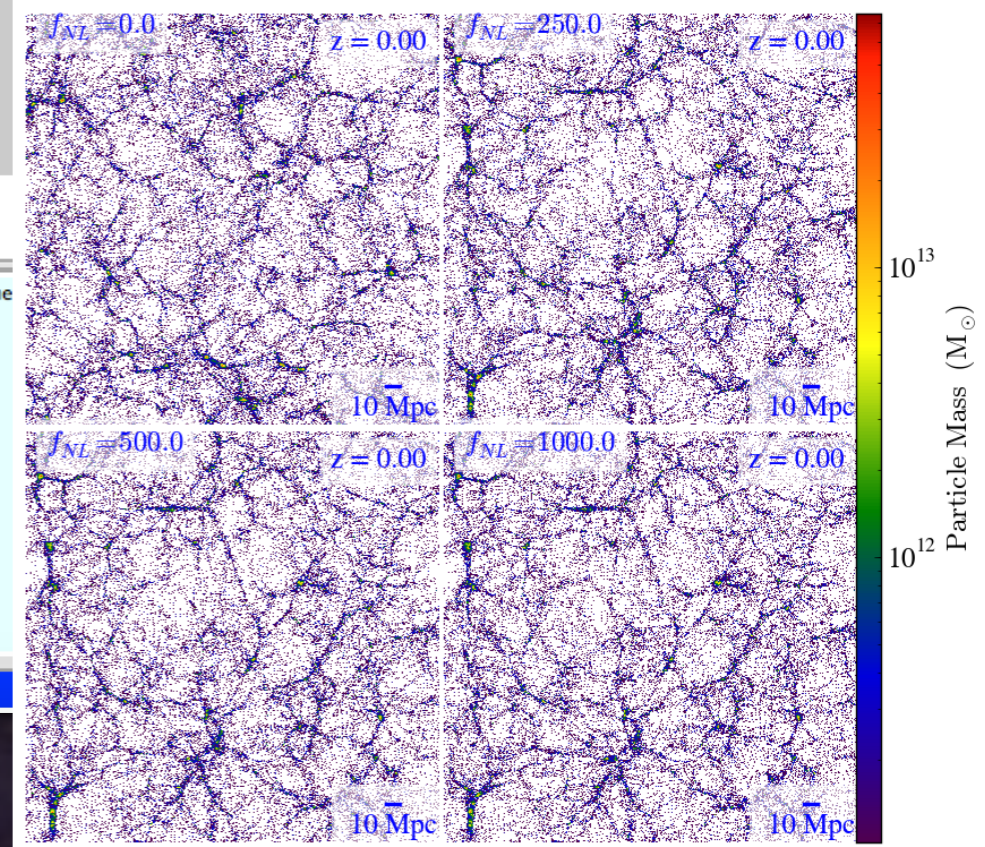
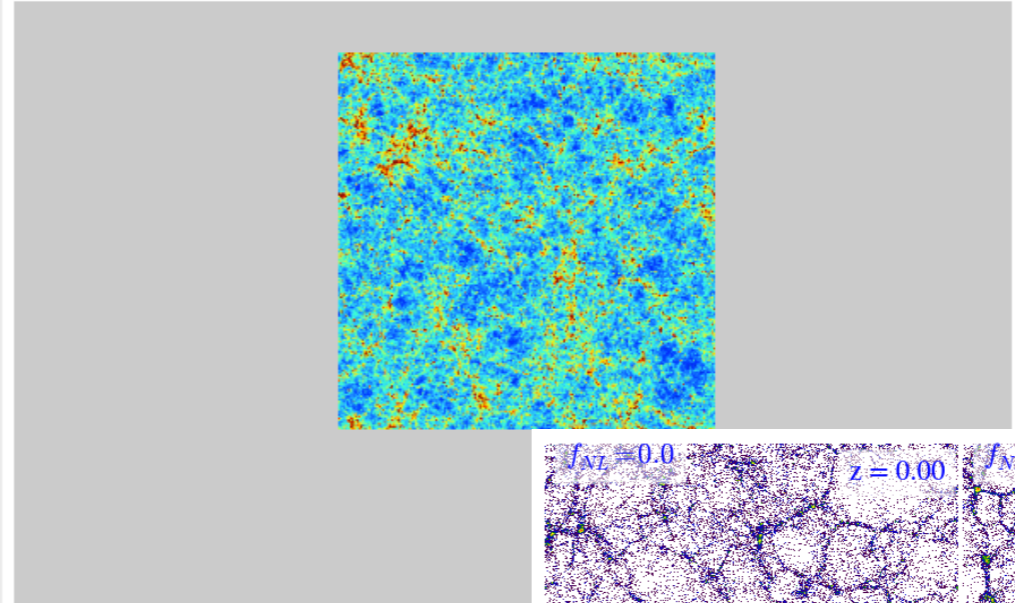
x-axis: x | y-axis: y | z-axis: z

Snap View | Map Bins: 256

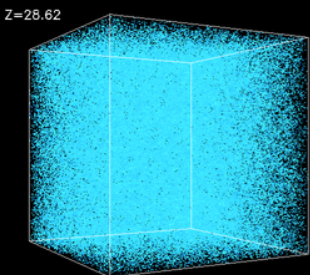
Depth: 71

Plot Refresh

Welcome to CosmoSuite

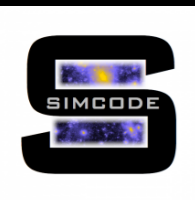


CosmoSuite



GADGET - 2

A code for cosmological simulations of structure formation



Nonlinear power spectrum

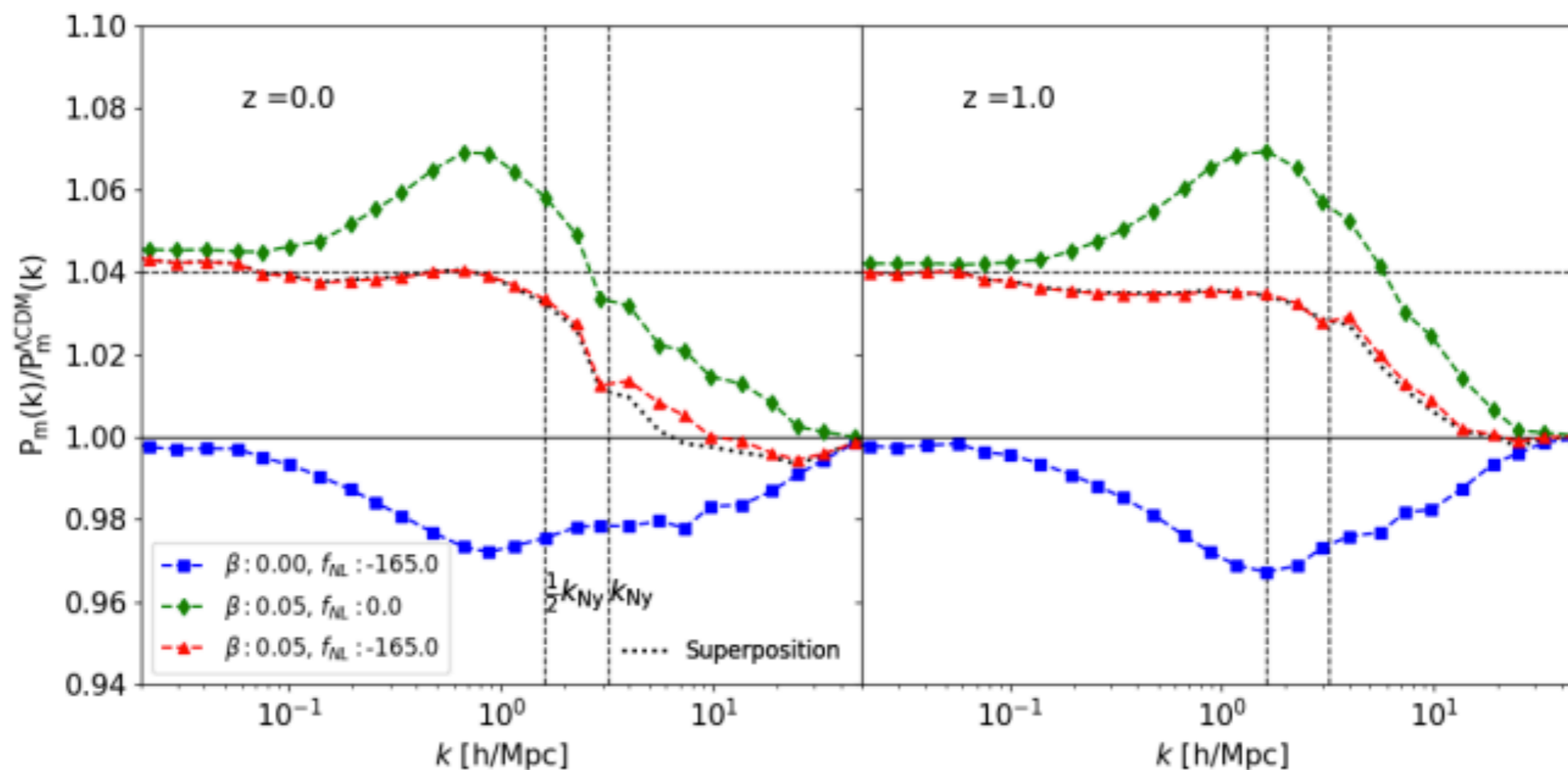


Figure 3. The non-linear matter power spectrum with IDE, PNG and their combination, relative to the reference ACDM spectrum, at $z = 0$ (left panel) and $z = 1$ (right panel). The dotted black curve shows the superposition spectra (IDE-only + PNG-only). The black dashed vertical lines show the Nyquist frequency and half of it.

[arXiv:1806.02356](https://arxiv.org/abs/1806.02356)

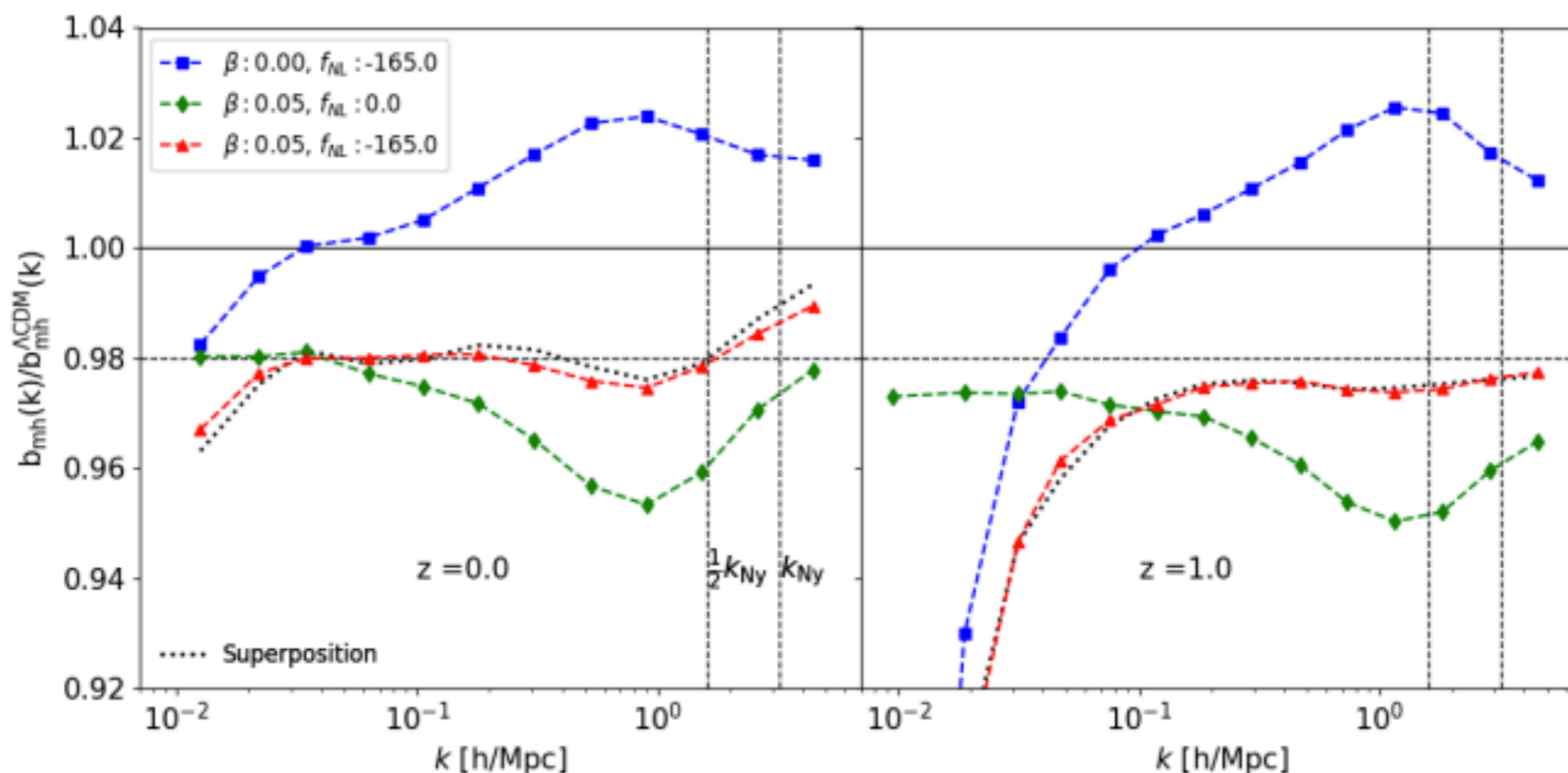


Figure 4. As in Fig. 3, for the halo-matter bias. Clearly, IDE shows no sign of scale-dependence on large scales.

$$b_{hm}(k) = \frac{P_{hm}(k)}{P_{mm}(k)}.$$

[arXiv:1806.02356](https://arxiv.org/abs/1806.02356)

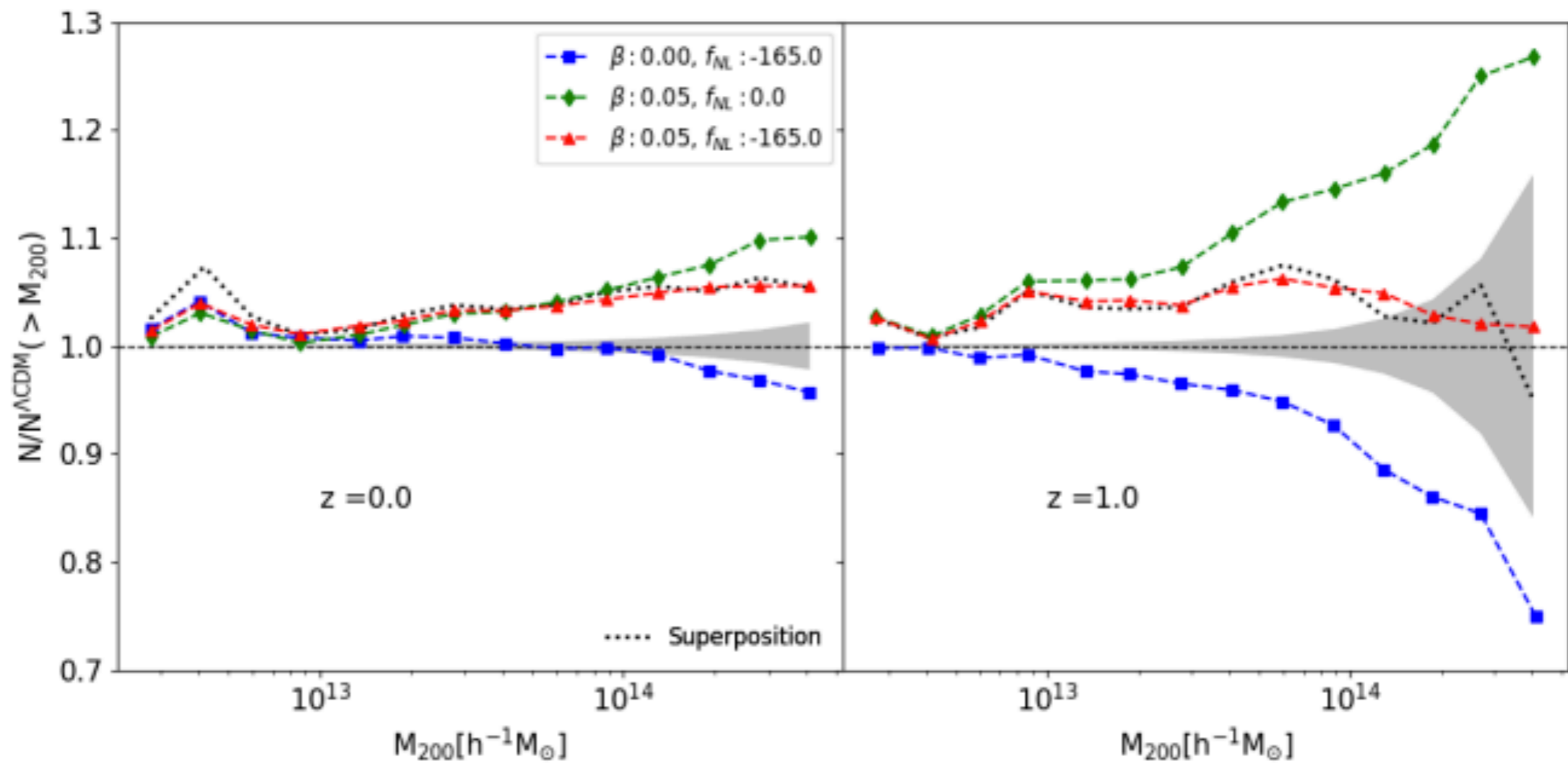


Figure 5. As in Fig. 3, for the halo mass function. The grey region represents the propagated Poissonian error of the number counts of halos in each bin.

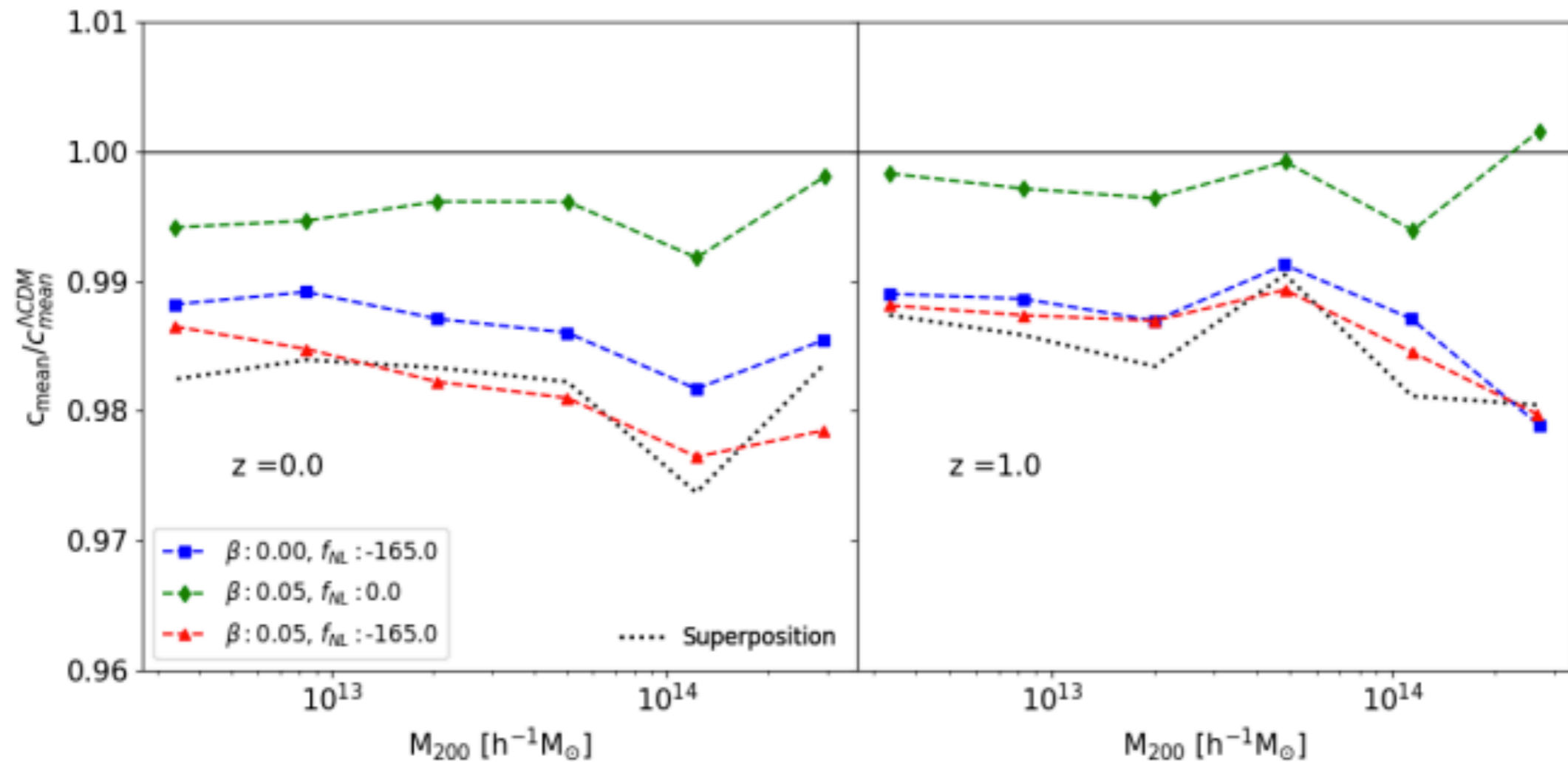
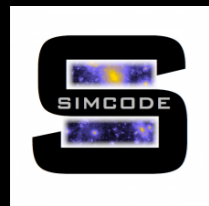


Figure 7. As in Fig. 3, for the concentration-mass relation.

$$\delta_c = \frac{200}{3} \frac{c^3}{\ln(1+c) - c/(1+c)} = 14.426 \left(\frac{V_{\text{max}}}{H_0 r_{\text{max}}} \right)^2$$



sub-Halo mass function

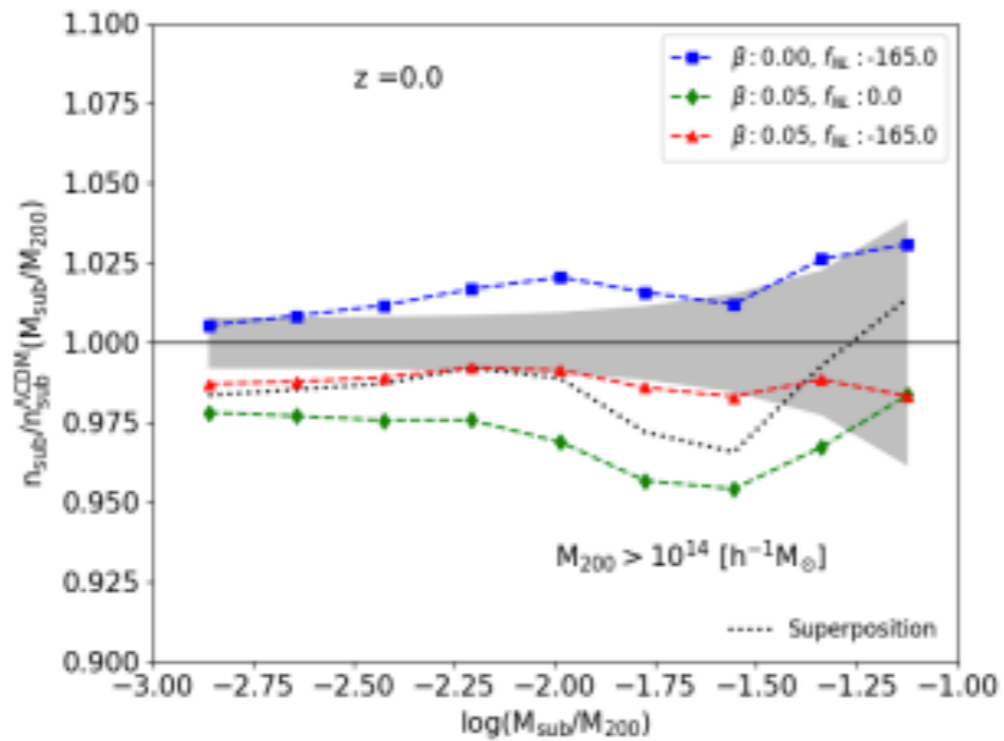


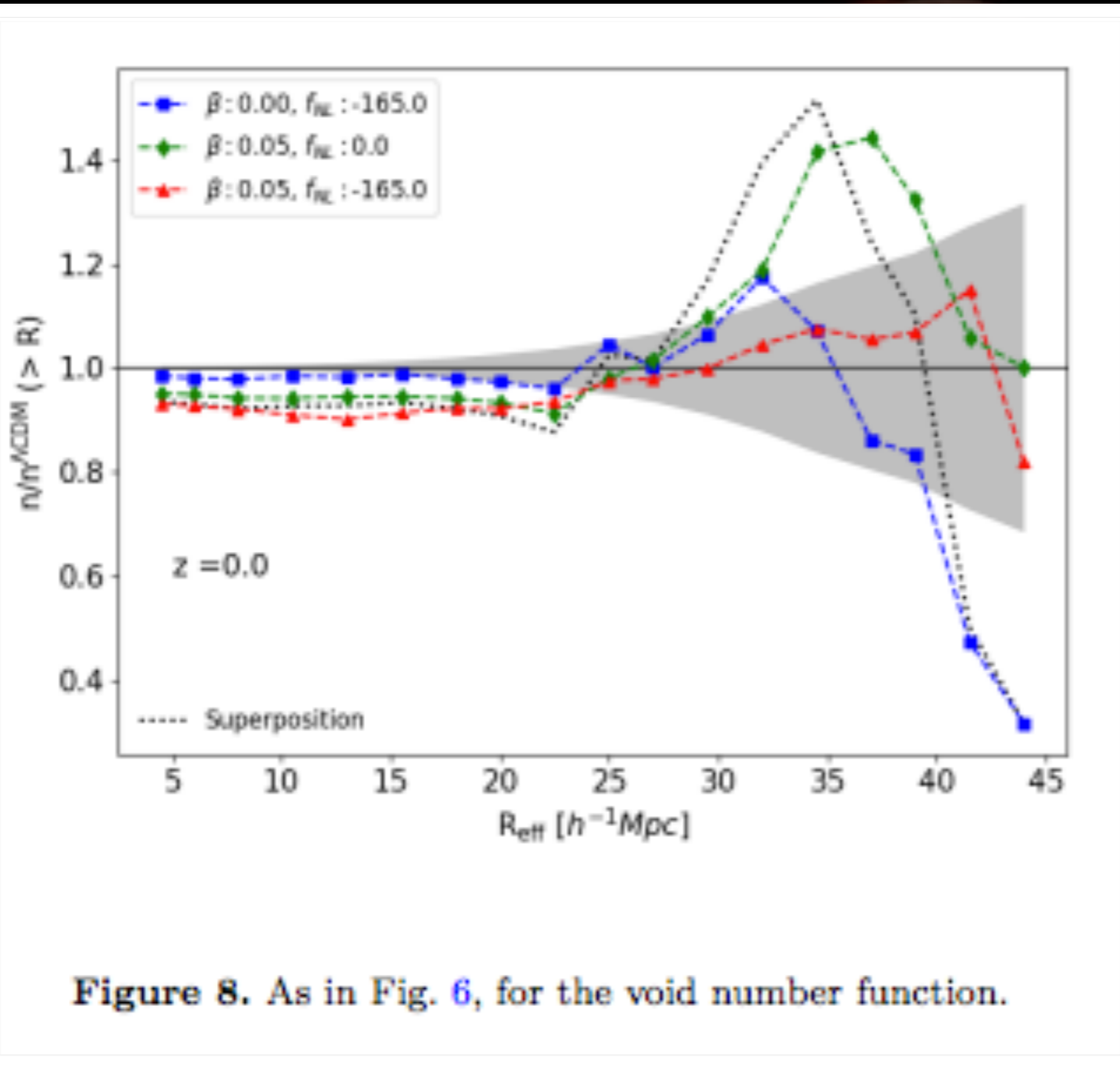
Figure 6. The subhalo mass function for the cosmologies under investigation at $z = 0$. The grey region represents the propagated Poissonian error of the number counts of subhalos in each bin and the dotted black line represents the superposition of IDE and PNG models.

[arXiv:1806.02356](https://arxiv.org/abs/1806.02356)

Cairo, 2022



void number function



[arXiv:1806.02356](https://arxiv.org/abs/1806.02356)

Conclusions

- IDE is not ruled out by current observations.
- LPT shows degeneracy on very large scales of the power spectrum between PNG and IDE.
- According to N-Body simulations, PNG and IDE also show some degeneracy on nonlinear power spectrum, halo mass function and nonlinear halo bias however it defies on halos structure properties such as Concentration.
- Disentangling PNG-IDE degeneracy could be done either by measuring degenerate observables at higher redshifts or by considering non-degenerate observables such as halo Concentration.