

PRIMORDIAL BLACK HOLES AS DARK MATTER FROM INFLATION

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PBHs

binary BH mergers

100 Hz



Courtesy
Caltech/MIT/LIGO Laboratory

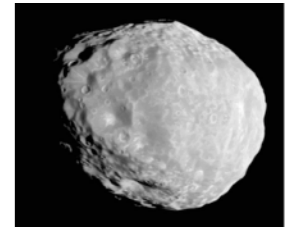
$100 M_{\odot}$

M_{\odot}

$$r_s = \frac{2GM}{c^2}$$

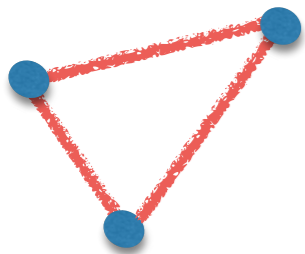
300 km

3 km



0.03 Hz – 3 Hz

e.g. LISA



100% DM

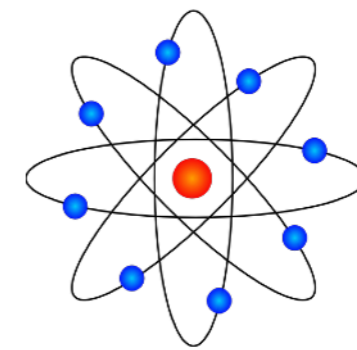
asteroid
mass
window

stochastic
background
of GWs

$10^{-12} M_{\odot}$



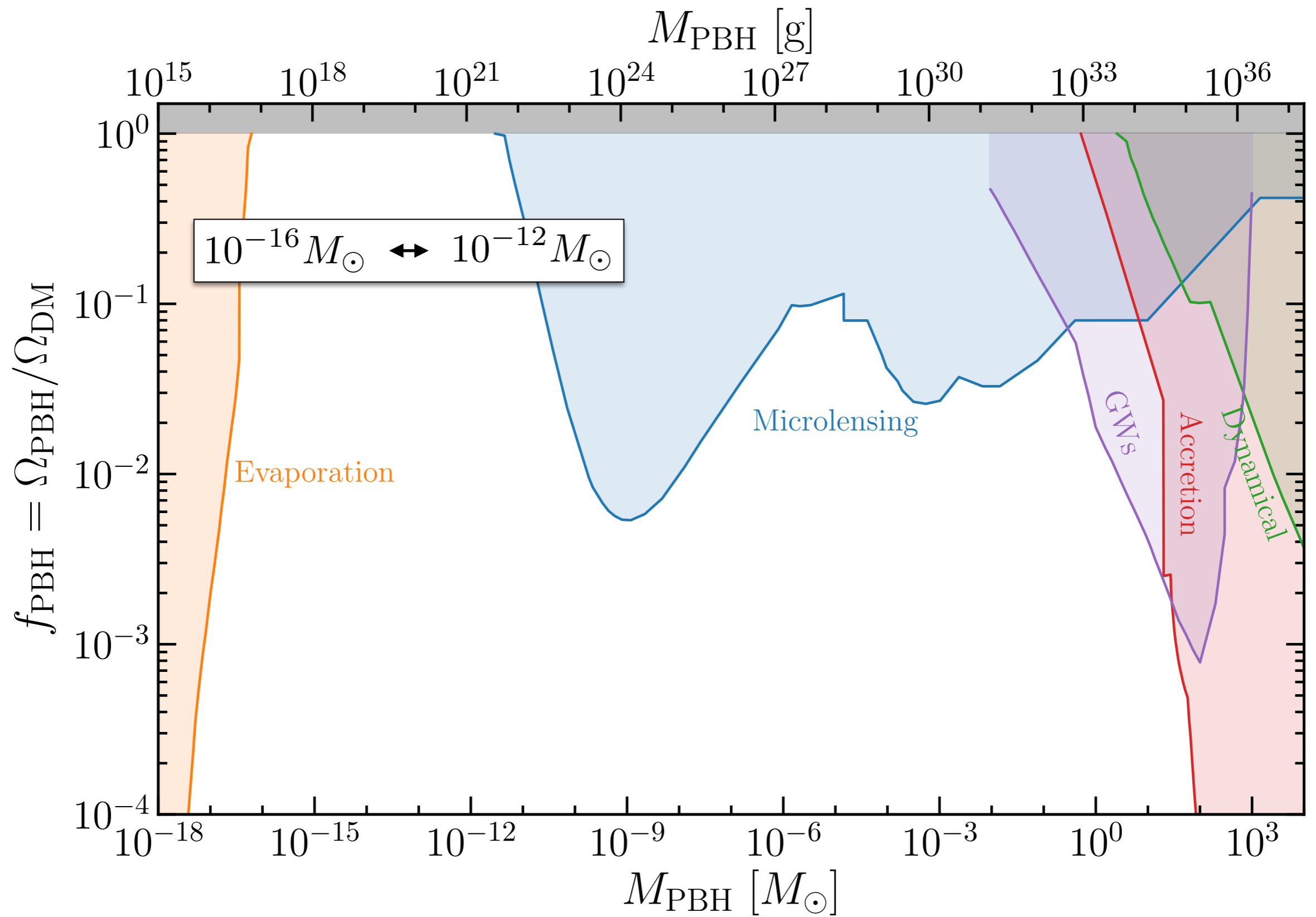
3 nm



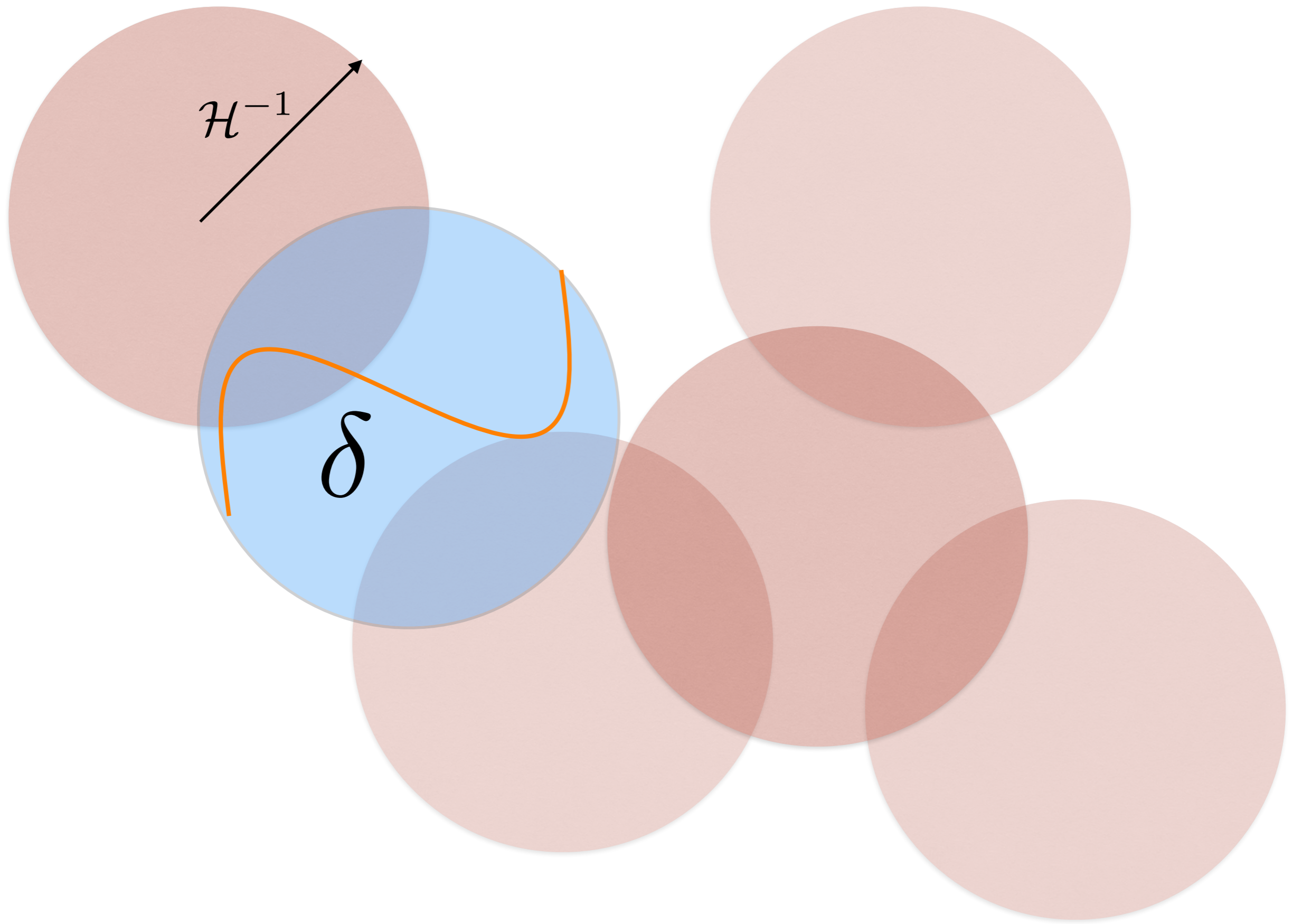
~ 0.1 nm

$10^{-16} M_{\odot}$

3×10^{-4} nm

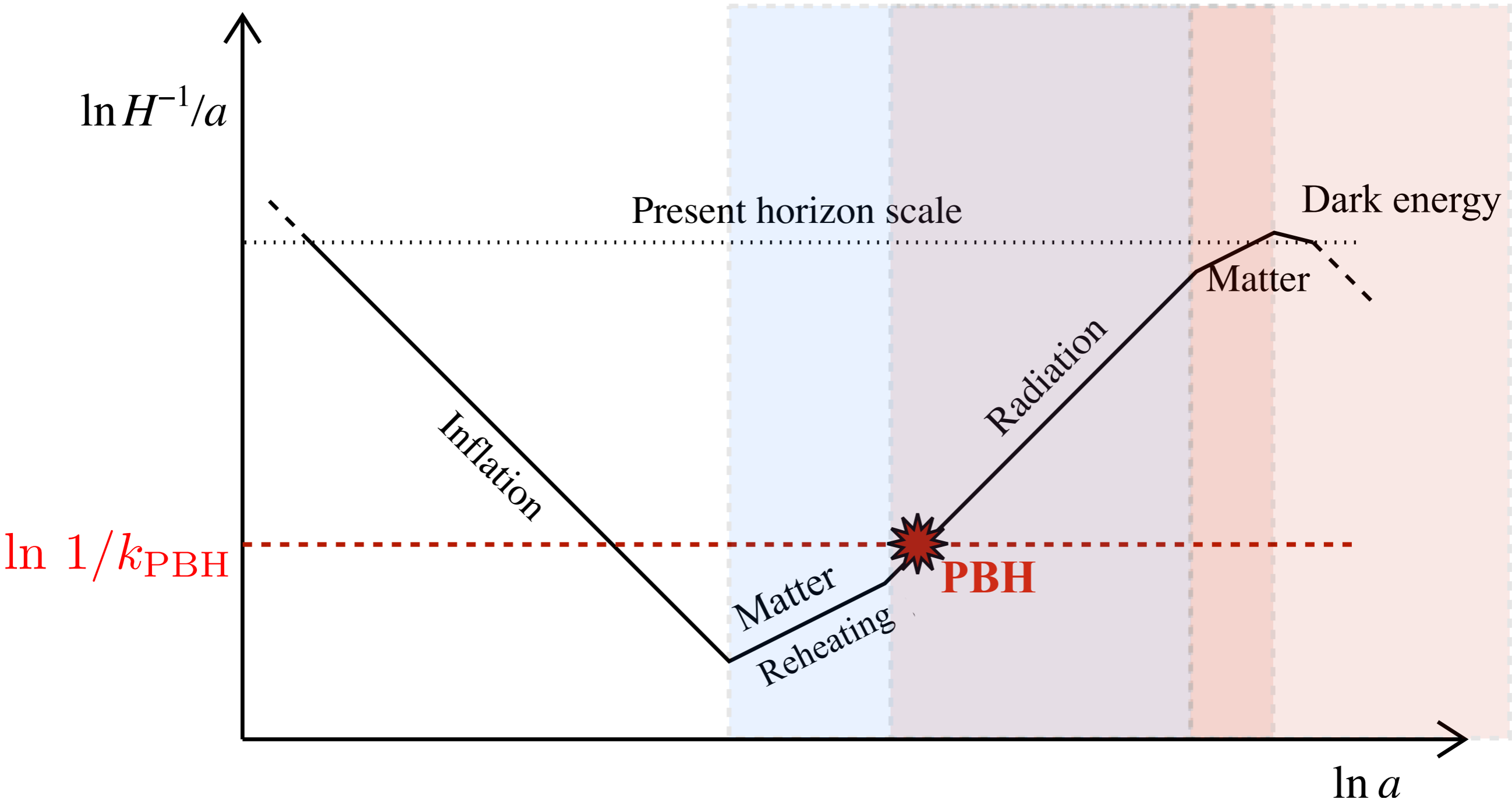


Primordial black hole formation from single-field inflation

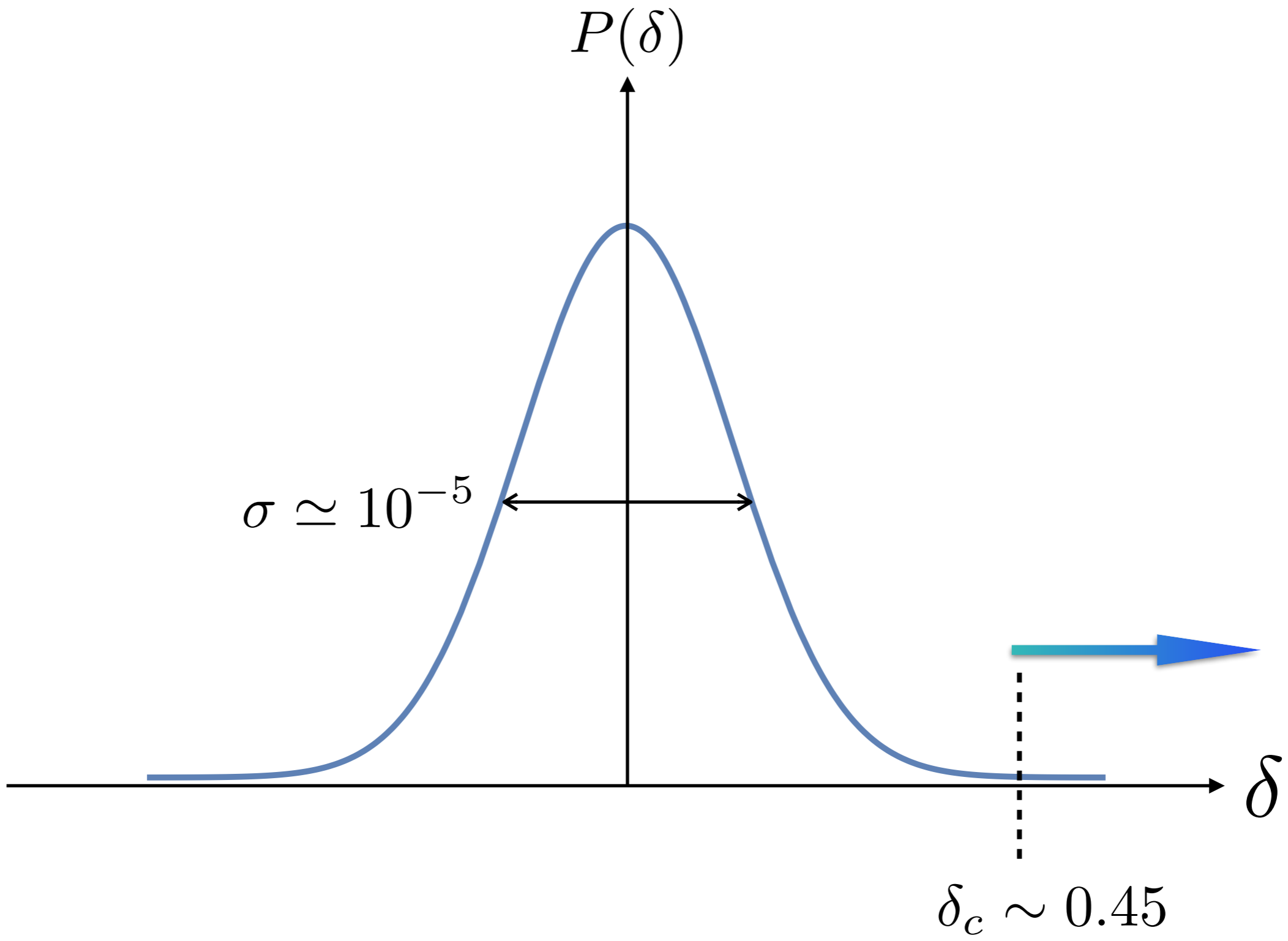




PBH



Adapted from Liddle and Leach, 2003



Individual masses

$$M \sim \frac{4}{3}\pi \rho H^{-3} \sim 10^{-14} \left(\frac{10^{13} \text{ Mpc}^{-1}}{k} \right)^2 M_{\odot}$$

$$N_e \simeq 18 - \frac{1}{2} \log \frac{M}{M_{\odot}}$$

Abundance

$$\beta(M) = \frac{1}{\sqrt{2\pi\sigma^2(M)}} \int_{\delta_c}^{\infty} d\delta \exp\left(\frac{-\delta^2}{2\sigma^2(M)}\right)$$

$$\sigma^2 \sim \mathcal{P}_{\mathcal{R}}$$

$$\sigma^2(M) = \frac{16}{81} \int \frac{dq}{q} (qR)^4 \mathcal{P}_{\mathcal{R}} W(qR)^2$$

$$\frac{\Omega_{\text{PBH}}(M)}{\Omega_{\text{DM}}} \simeq \frac{\beta}{10^{-16}} \left(\frac{M}{5 \cdot 10^{-16} M_{\odot}} \right)^{-1/2}$$

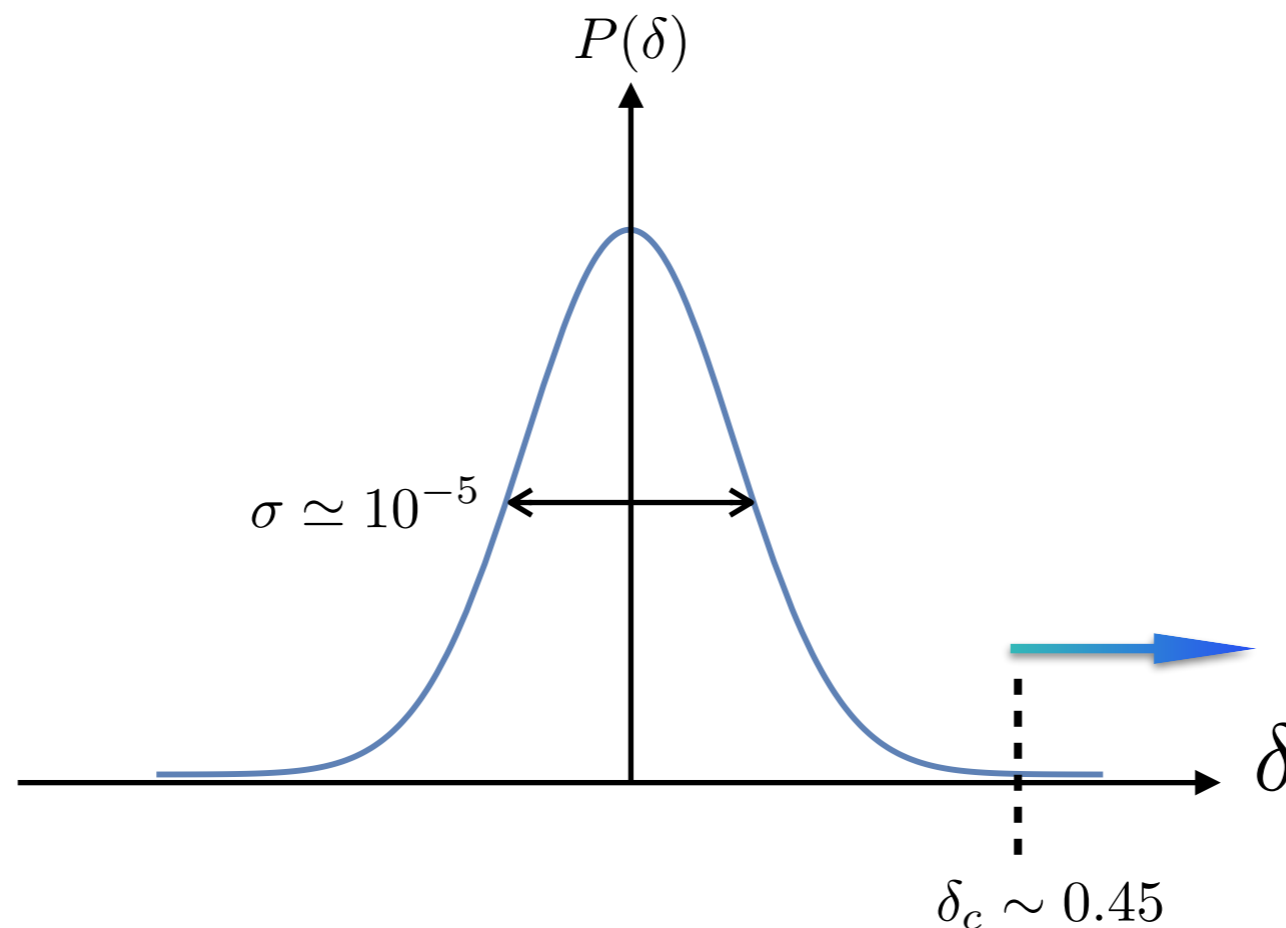
$$\mathcal{P}_{\mathcal{R}} \sim 10^{-2} \implies \frac{\Omega_{\text{PBH}}}{\Omega_{\text{DM}}} \sim 1$$

Is the Gaussian approximation reliable?

$$\delta(\vec{x}, t) = -\frac{4(1 + \omega)}{5 + 3\omega} \left(\frac{1}{aH} \right)^2 e^{-5\mathcal{R}(\vec{x})/2} \Delta e^{\mathcal{R}(\vec{x})/2}$$

Intrinsic non-Gaussianities in \mathcal{R}

NG $\sim \mathcal{O}(1)$ change in $\mathcal{P}_{\mathcal{R}}$ Taoso, Urbano 2021



How do the tails of the PDF of \mathcal{R} look like?

There are several indications that they are not Gaussian, specifically if slow-roll is broken or if interactions are important

$$q \dot{\mathcal{R}}^4 \implies P(\mathcal{R}) \sim \exp\left(-\frac{\mathcal{R}^{3/2}}{q^{1/4}}\right) \quad \text{for large } \mathcal{R}$$

Celoria, Creminelli, Tambalo, Yingcharoenrat 2021

How do the tails of the PDF of \mathcal{R} look like?

There are several indications that they are not Gaussian, specifically if slow-roll is broken or if interactions are important

Quantum diffusion

classical roll: $\frac{\dot{\phi}}{H} \gg \frac{H}{2\pi} \longrightarrow \mathcal{P}_{\mathcal{R}} \ll 1$

Stochastic inflation

Starobinsky

$$\text{USR} \implies P(\mathcal{R}) \sim \exp(-\kappa R) \quad \text{for large } \mathcal{R}$$

Ezquiaga, García-Bellido, Vennin 2019

Figueroa, Raatikainen, Rasanen, Tomberg 2020

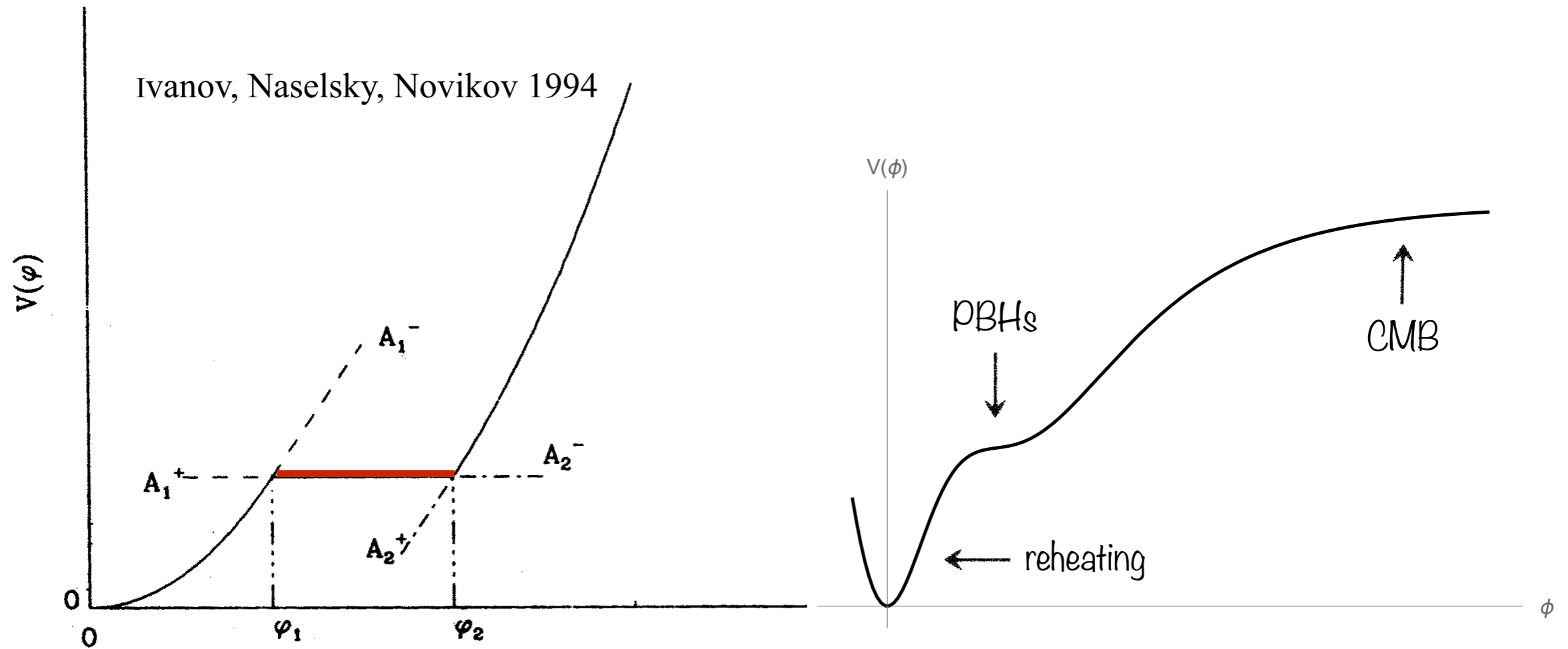
Pattison, Vennin, Wands, Assadullahi 2021

Modelling PBH formation from inflation

Requirements for PBH DM from inflation

- Enough inflation
- Agreement with the CMB and LSS
- Successful reheating
- $\frac{\Omega_{\text{PBH}}}{\Omega_{\text{DM}}} \sim 1$ (implies a large primordial spectrum...)
- $10^{-16} M_{\odot} \leftrightarrow 10^{-12} M_{\odot}$ (...at a specific scales)

Inflation and primordial black holes as dark matter



$$V(\phi) = \begin{cases} V_0 + A_+(\phi - \phi_0) & \text{for } \phi > \phi_0 \\ V_0 + A_-(\phi - \phi_0) & \text{for } \phi < \phi_0 \end{cases} \quad \text{Starobinsky 1994}$$

$$\mathcal{P}_{\mathcal{R}} \sim \left(\frac{H}{m_P} \right)^2 \left(\frac{H}{\dot{\phi}} \right)^2 \sim \frac{1}{m_P^2} \left(\frac{V}{V'} \right)^2 \frac{V}{m_P^4}$$

$V(\phi)$

$$\lambda \phi^4 + \xi \phi^2 R$$

(*“flatter”*)

PBHs



$$\mathcal{P}_{\mathcal{R}} \sim 10^{-2}$$



reheating

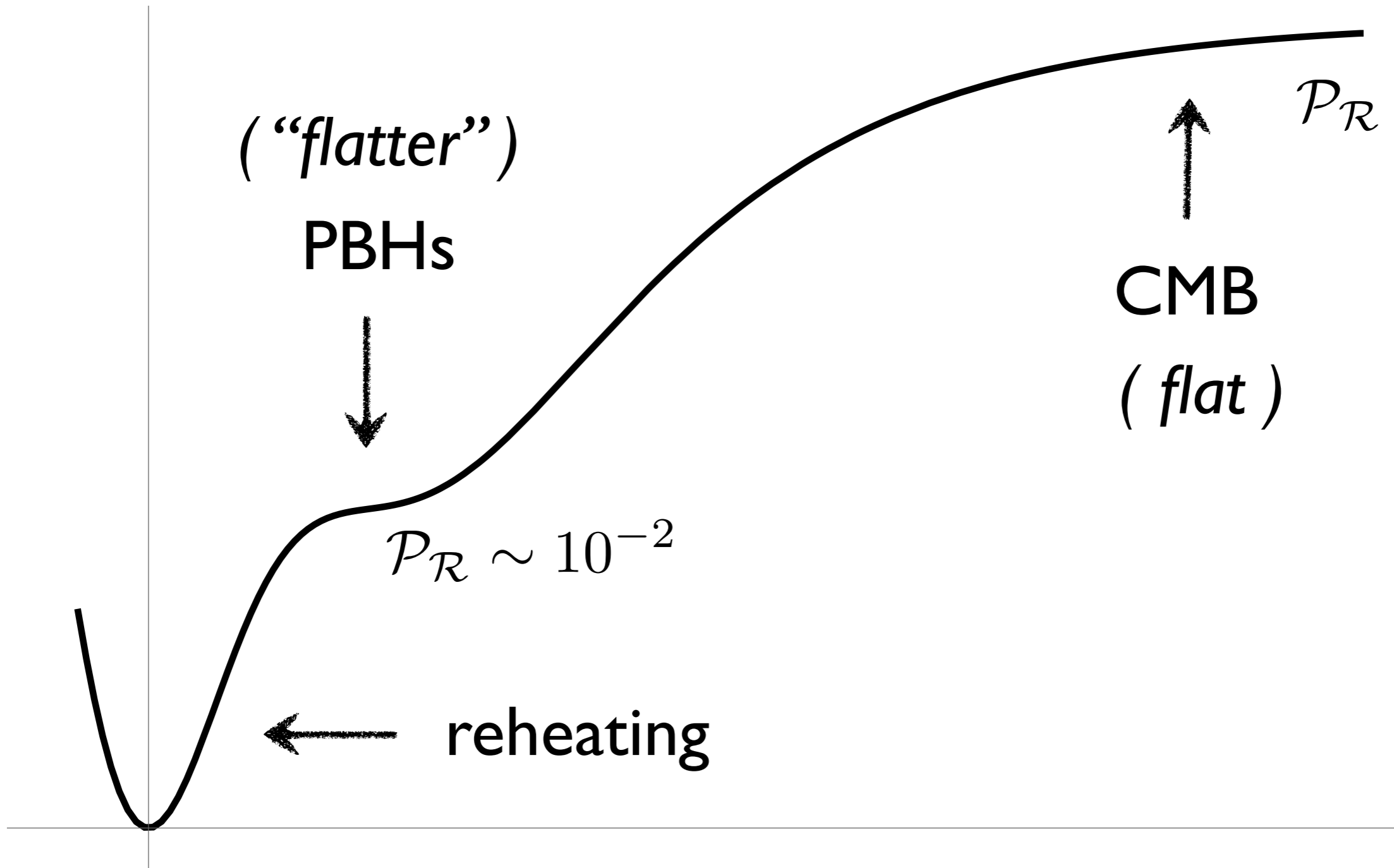


CMB

(*flat*)

$$\mathcal{P}_{\mathcal{R}} \sim 10^{-9}$$

ϕ



$$V(\phi) = a_2\phi^2 + a_3\phi^3 + a_4\phi^4$$

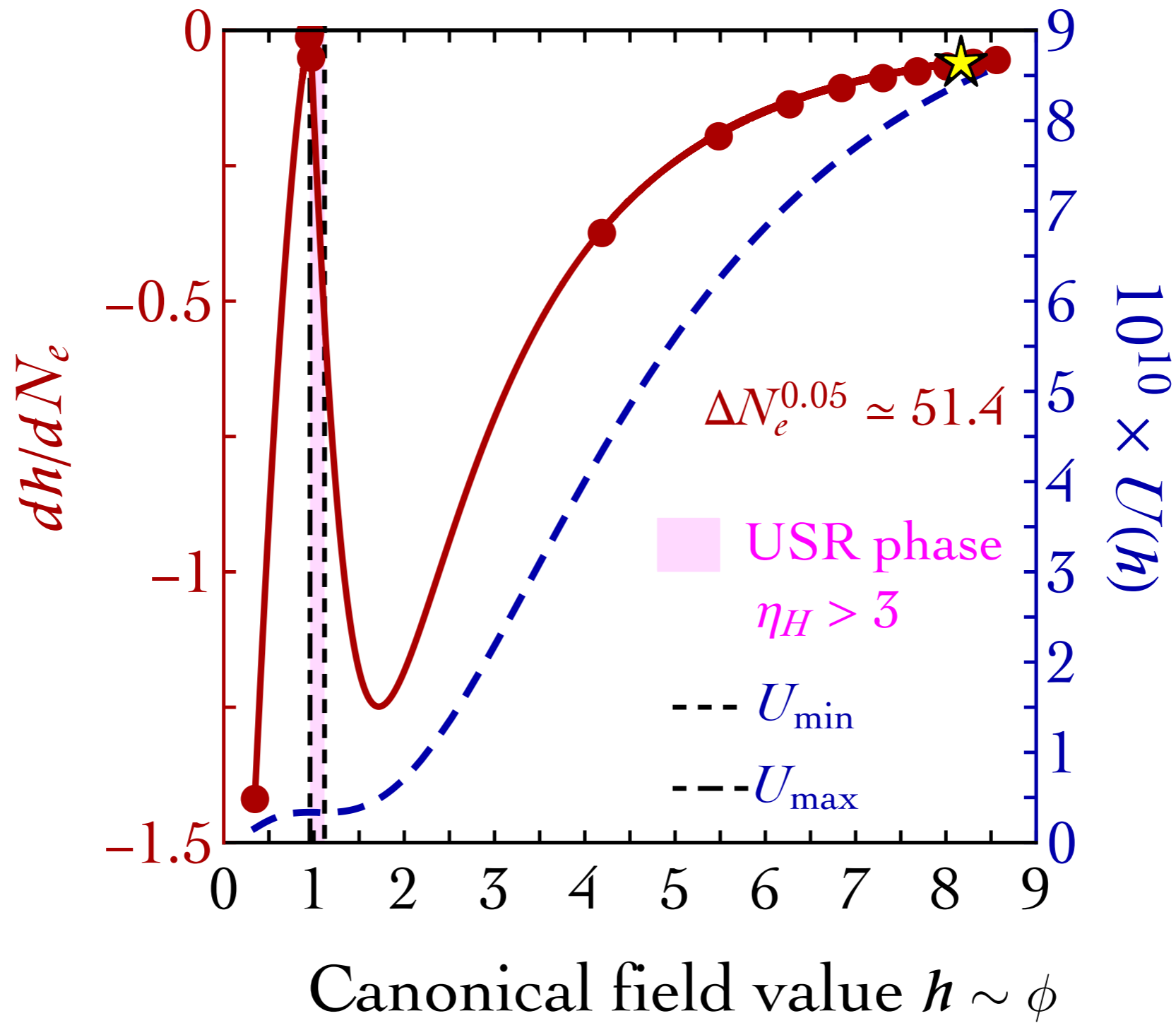


$$V = \lambda(\phi) \phi^4$$

$$\lambda(\phi) = \lambda(\phi_0) + \frac{1}{2}\beta_\lambda(\phi_0) \log \frac{\phi^2}{\phi_0^2} + \frac{1}{8}\beta'_\lambda(\phi_0) \left(\log \frac{\phi^2}{\phi_0^2} \right)^2 + \dots$$

$$\lambda(\mu_0) \sim |\beta_\lambda(\mu_0)| \sim \beta'_\lambda(\mu_0)$$

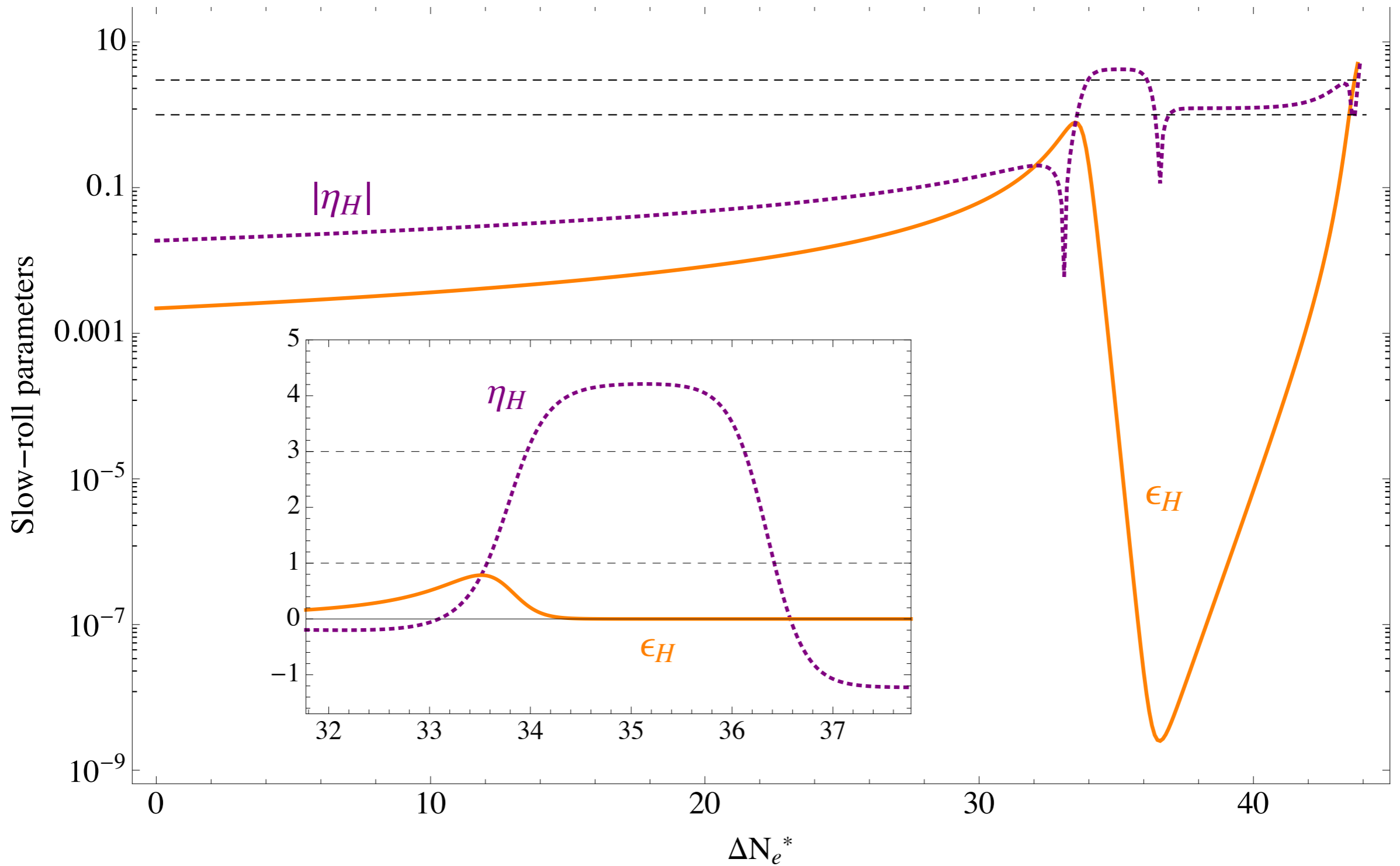
$$\xi(\phi) = \xi_0 \left(1 + b_3 \log \frac{\phi^2}{\phi_0^2} \right)$$



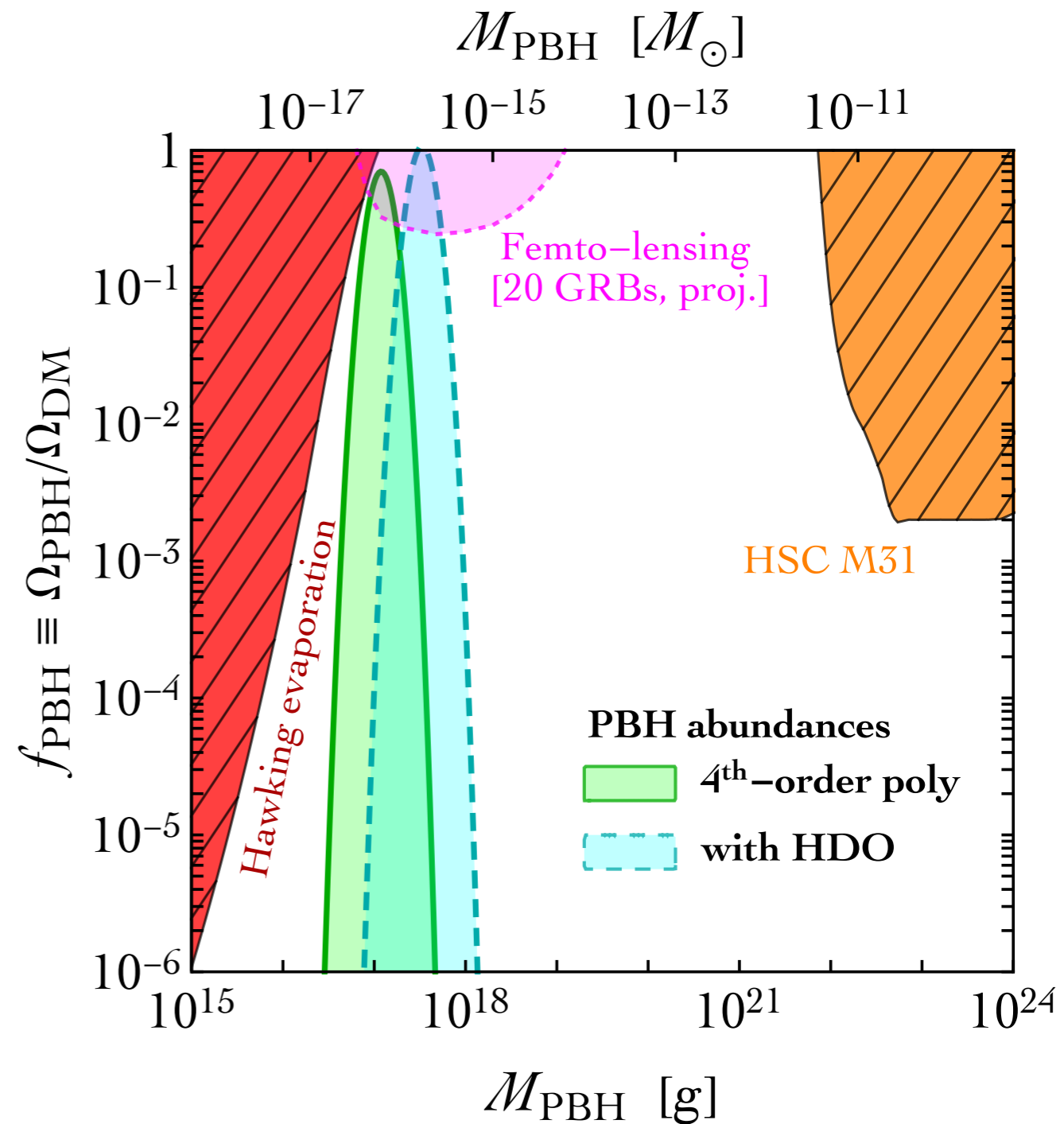
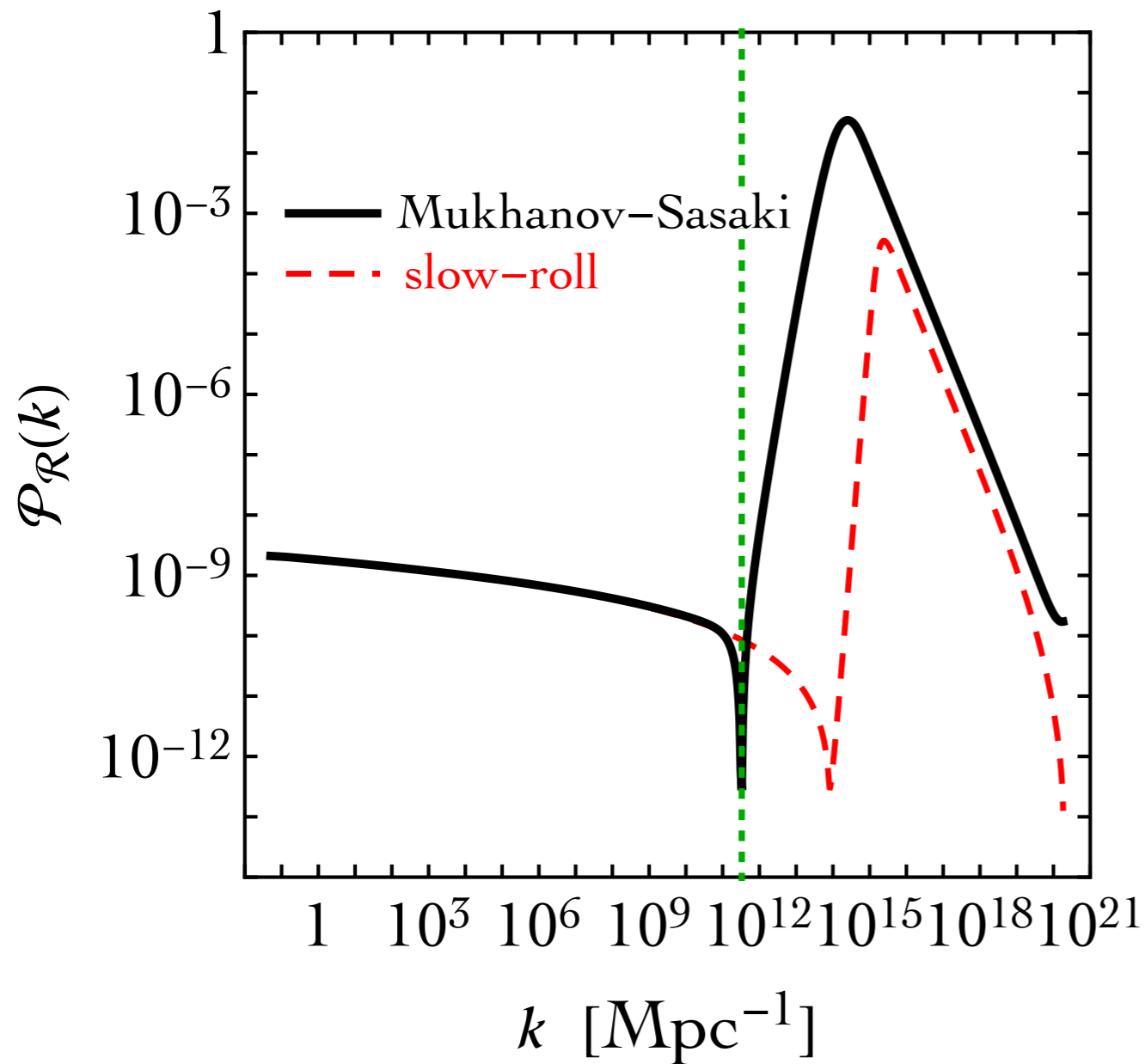
$$V(\phi) = a_2\phi^2 + a_3\phi^3 + a_4\phi^4$$

GB, Rey, Taoso, Urbano, 2020

$$\frac{d^2 \mathcal{R}_{\mathbf{k}}}{dN_e^2} + (3 + \epsilon_H - 2\eta_H) \frac{d\mathcal{R}_{\mathbf{k}}}{dN_e} + \frac{k^2}{a^2 H^2} \mathcal{R}_{\mathbf{k}} = 0$$



$$V(\phi) = a_2\phi^2 + a_3\phi^3 + a_4\phi^4$$



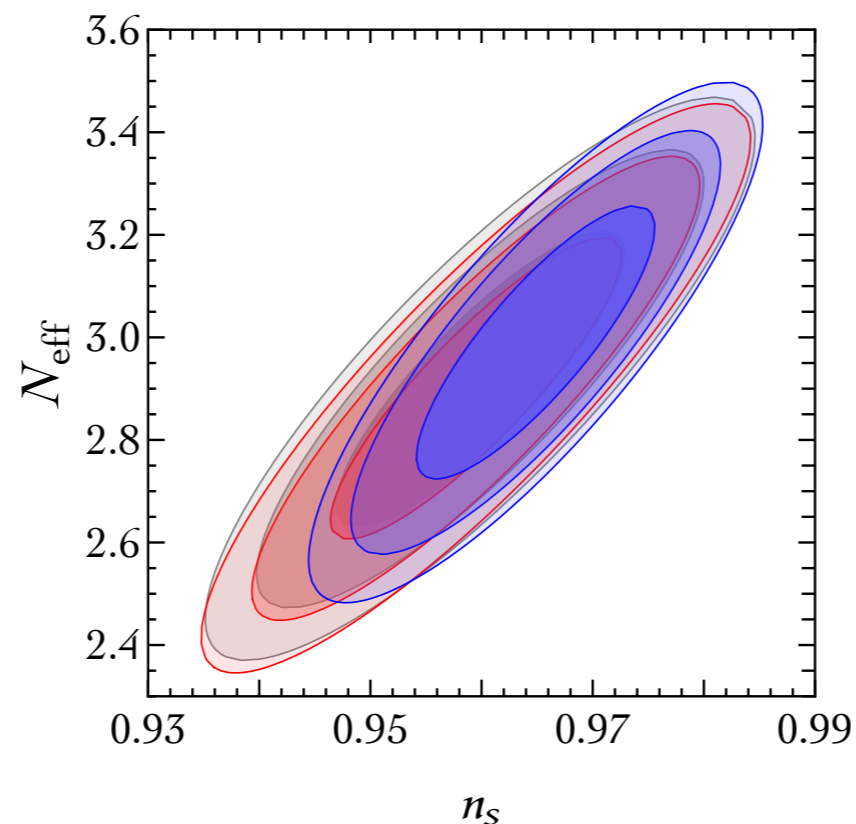
The scalar spectral index

$$\text{Base } \Lambda\text{CDM} : \quad n_s = 0.9649 \pm 0.0042$$

[68% CL, Planck TT, TE, EE + lowE + lensing]

‘simple’ models tend to predict $n_s \simeq 0.95$

$$V(\phi) = a_2\phi^2 + a_3\phi^3 + a_4\phi^4 + \sum_{n \geq 5} a_n\phi^n$$



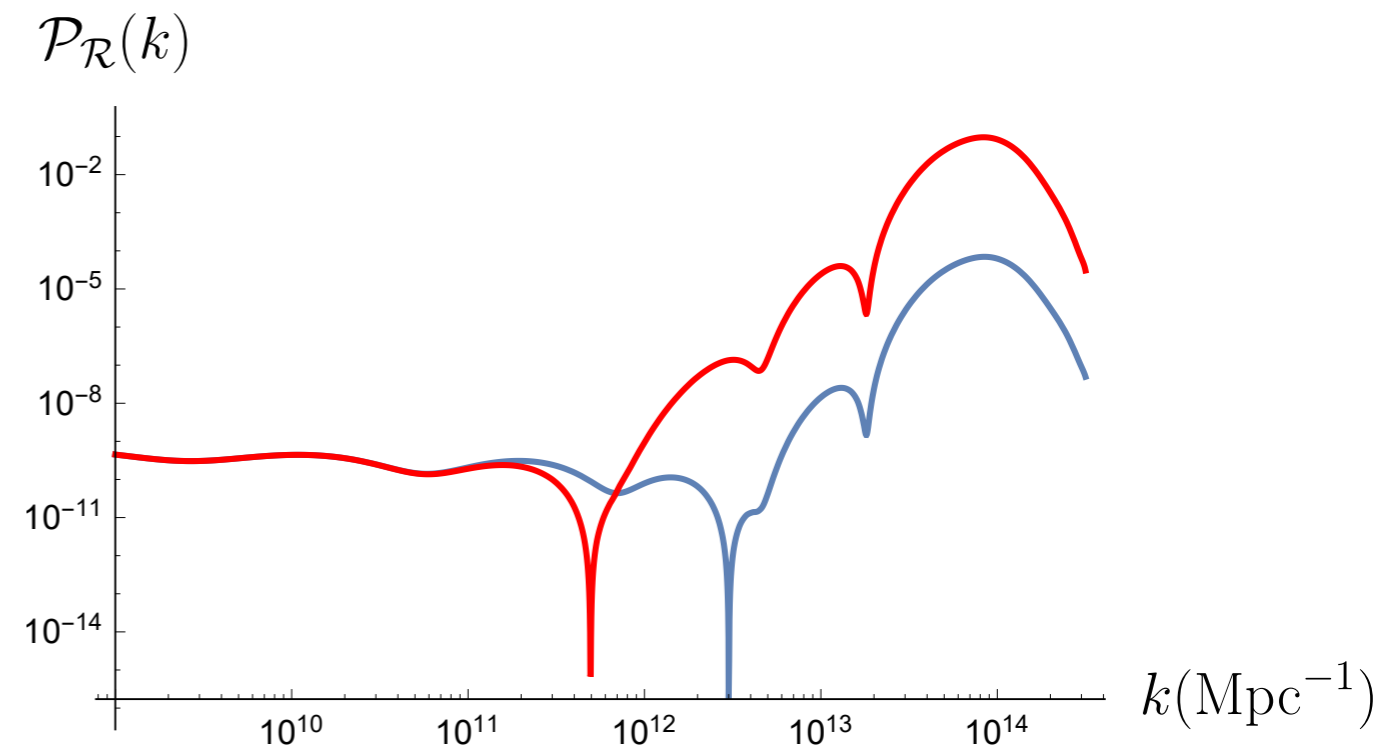
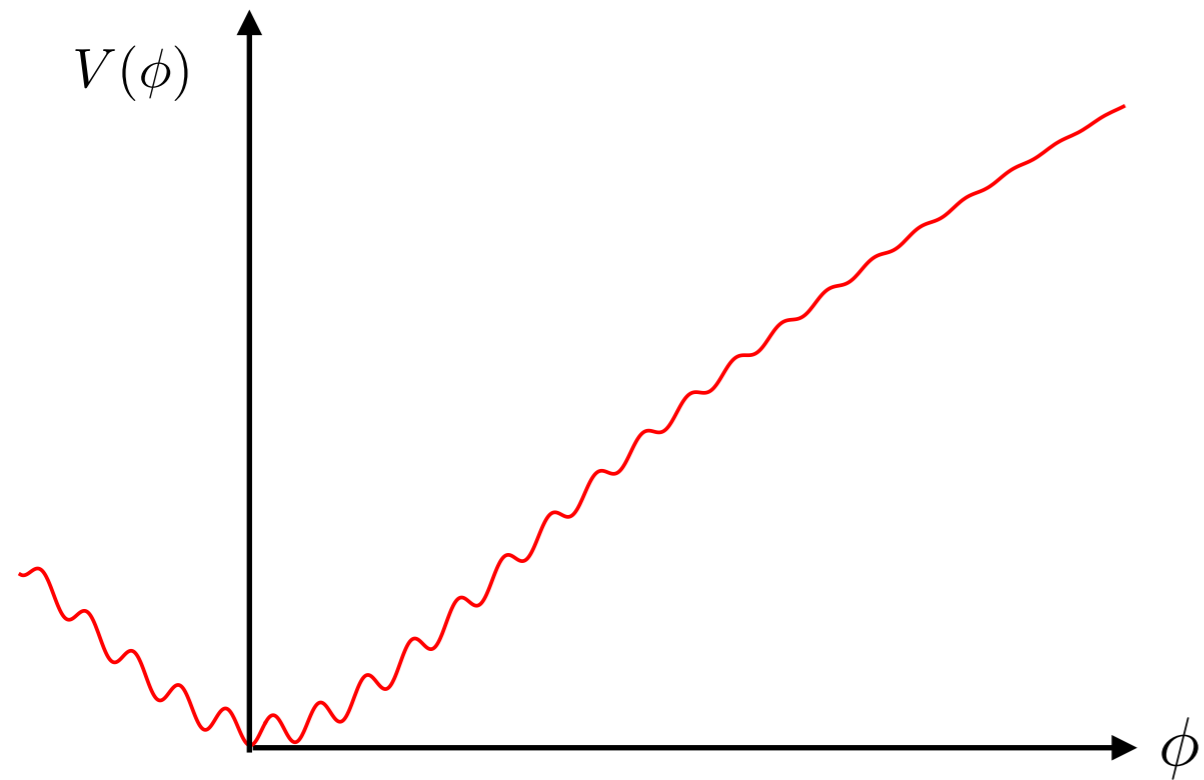
Exponential sensitivity of the abundance to the size of the primordial fluctuations

$$\beta(M) = \frac{1}{\sqrt{2\pi\sigma^2(M)}} \int_{\delta_c}^{\infty} d\delta \exp\left(\frac{-\delta^2}{2\sigma^2(M)}\right)$$

$$\sigma^2 \sim \mathcal{P}_{\mathcal{R}}$$

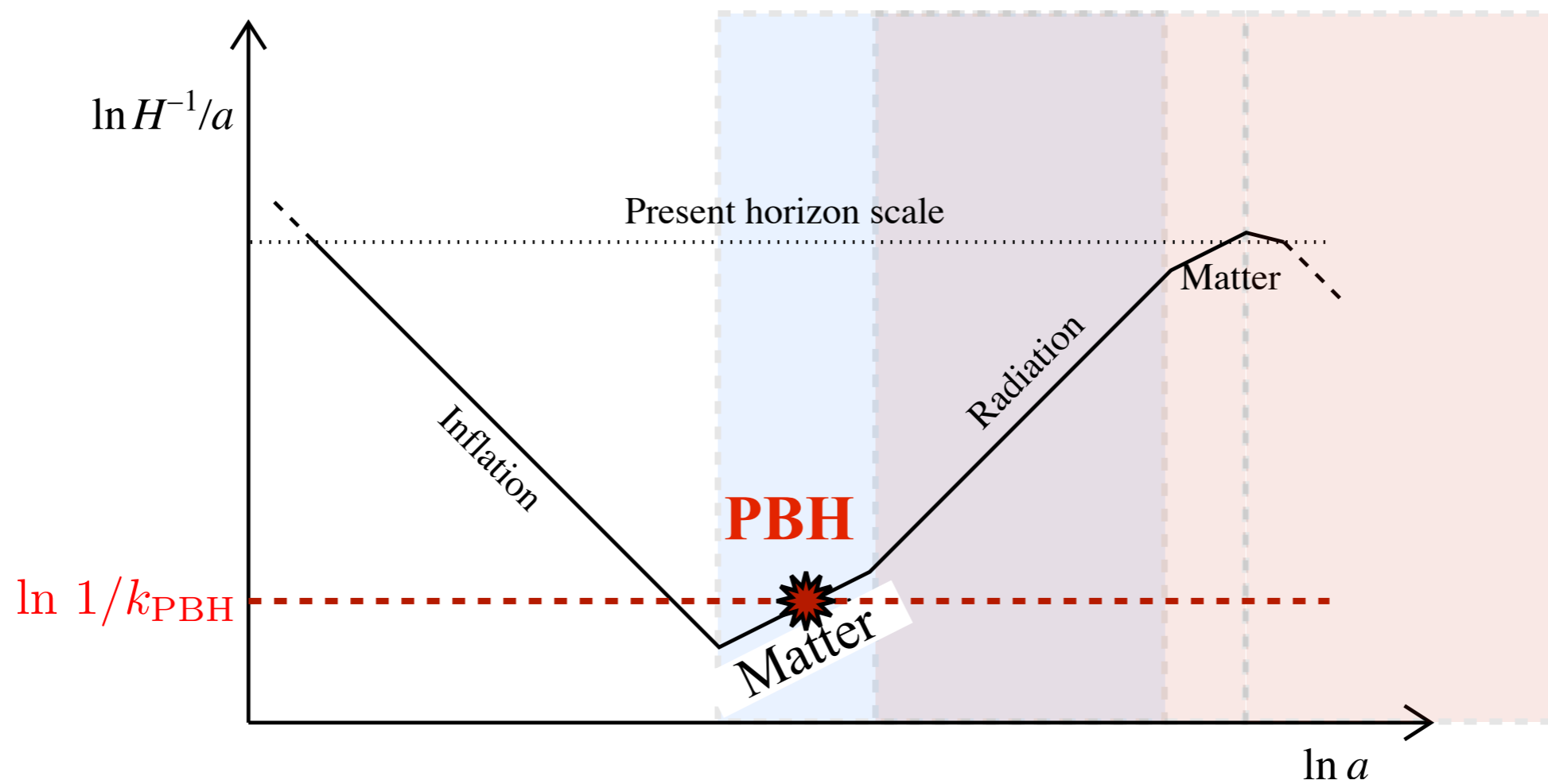
Tuning of parameters in the potential

Modulation + Matter domination



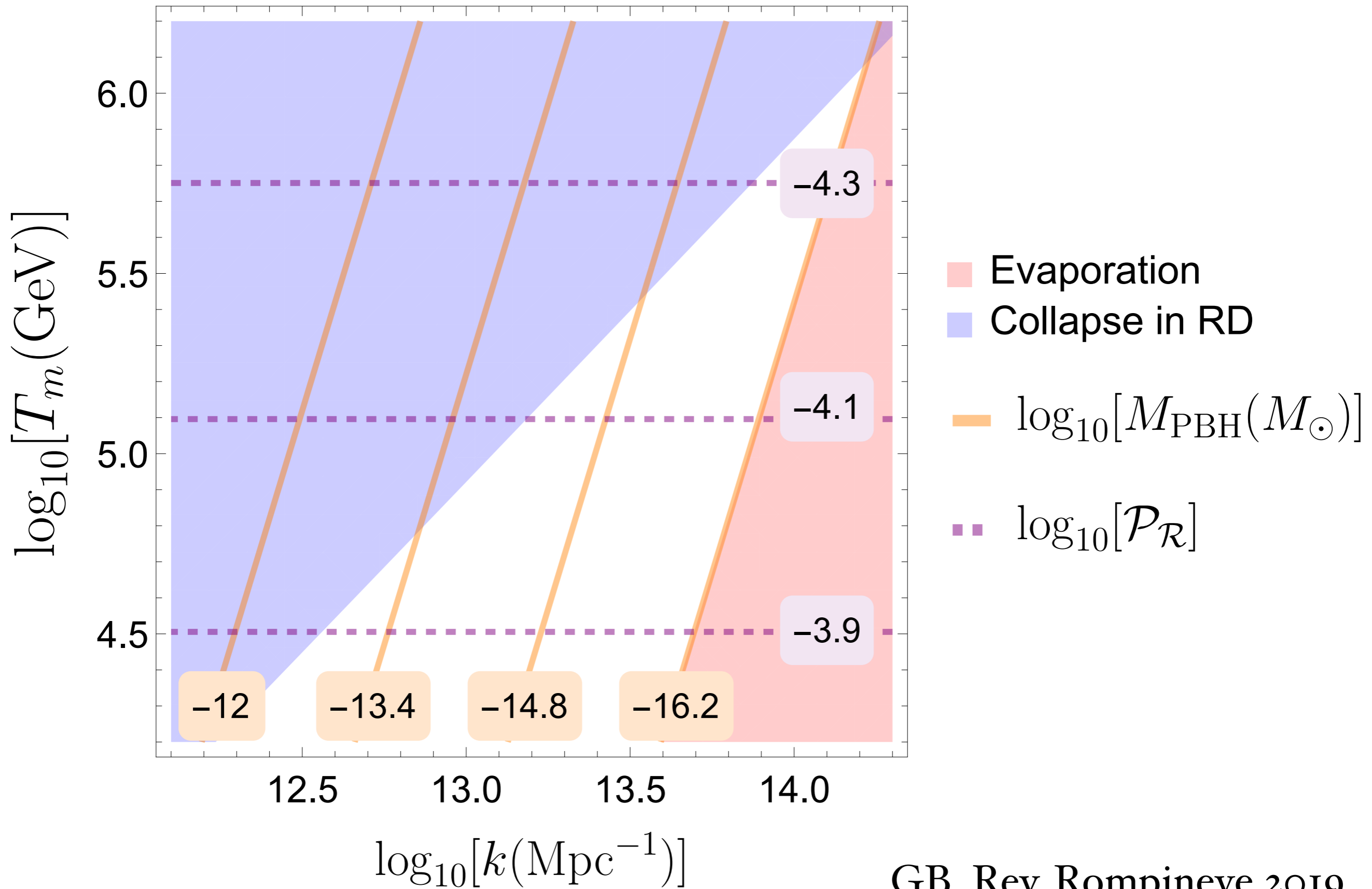
Axion monodromy inspired

GB, Rey, Rompineve 2019



$$\Omega_{\text{PBH}} \propto \begin{cases} \frac{e^{-\delta_c^2/\mathcal{P}_{\mathcal{R}}}}{\sqrt{\mathcal{P}_{\mathcal{R}}}} & \text{(Radiation)} \\ \mathcal{P}_{\mathcal{R}}^{5/2} & \text{(Matter)} \end{cases}$$

$$\gamma = 1 \quad f_{\text{PBH}} = 1$$



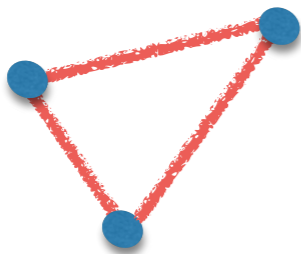
**A stochastic background of GWs
induced at second order in cosmological perturbation theory**

A stochastic background of GWs induced at second order in cosmological perturbation theory

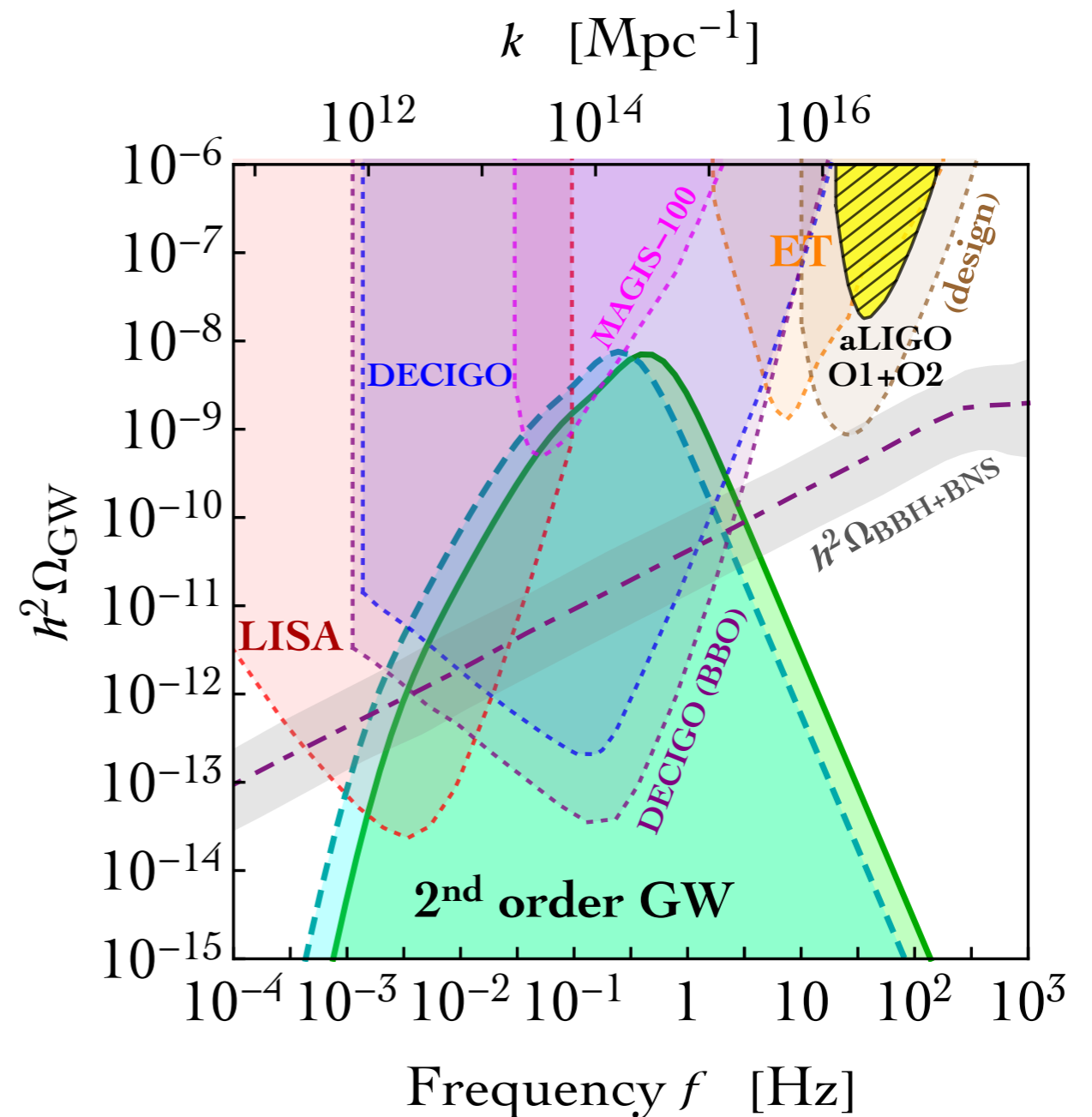
$$\text{GWs: } \left(\frac{M_{\text{PBH}}}{10^{17} \text{ g}} \right)^{-1/2} \simeq \frac{k}{2 \cdot 10^{14} \text{ Mpc}^{-1}} \simeq \frac{f}{0.3 \text{ Hz}}$$

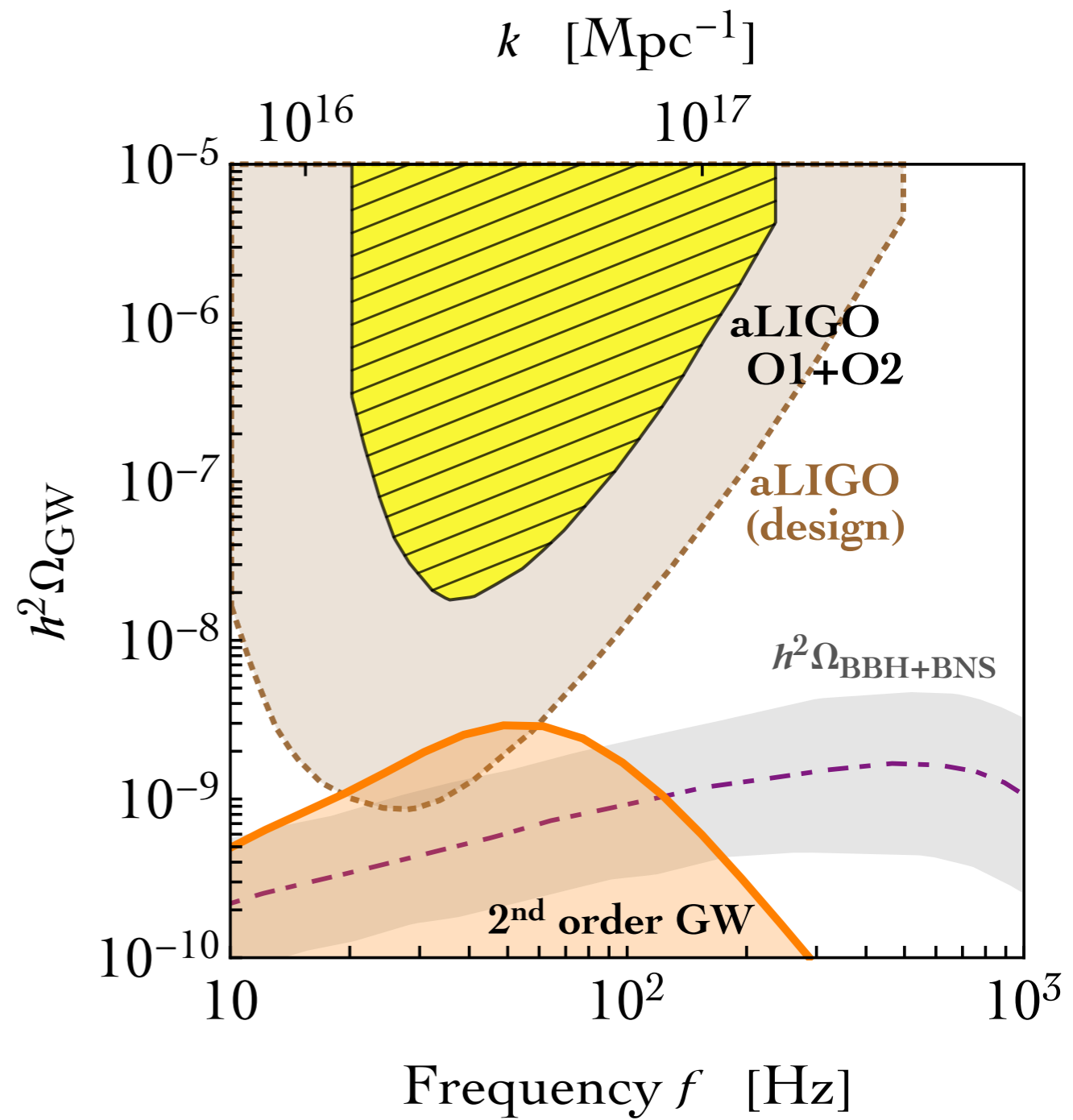
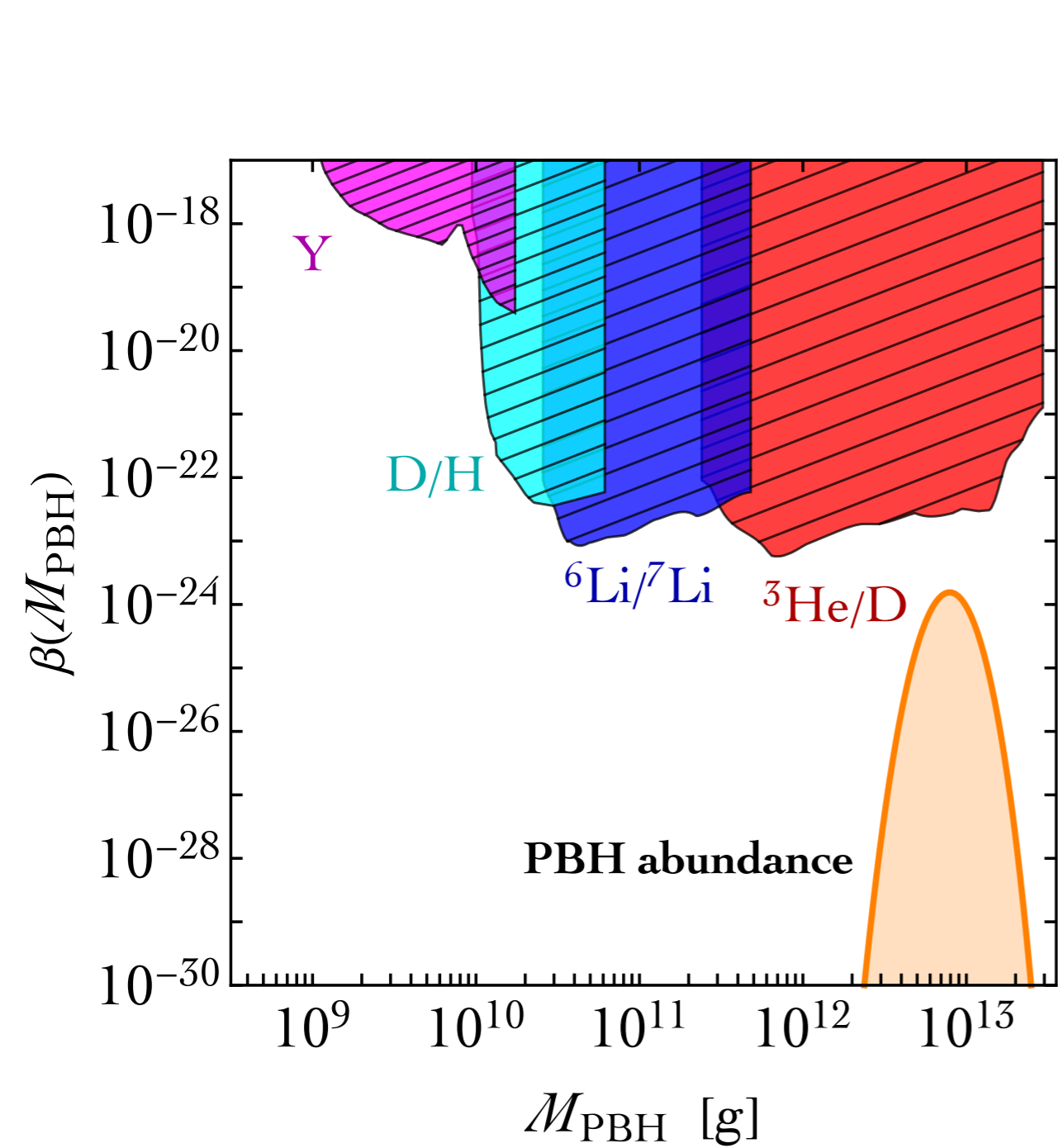
$$\Omega_{\text{GW}} \sim \mathcal{P}_h \sim (\mathcal{P}_{\mathcal{R}})^2$$

e.g. LISA (if PBHs are DM)



NANOGRAB Sept 2020: 10^{-8} Hz
Other PTA experiments as well





The EFT approach

$$\mathcal{S} = \int dt d^3x M^2 \frac{a^3 \epsilon}{c_s^2} \left[\dot{\mathcal{R}}^2 - \frac{c_s^2}{a^2} |\vec{\nabla} \mathcal{R}|^2 - m^2 \mathcal{R}^2 \right]$$

$$d\tilde{\tau} = c_s d\tau = \frac{c_s}{a} dt. \quad z^2 \equiv \frac{2M^2 a^2 \epsilon}{c_s}, \quad m = 0$$

$$\mathcal{S} = \frac{1}{2} \int d\tilde{\tau} d^3x z^2 \left[(\mathcal{R}')^2 - |\vec{\nabla} \mathcal{R}|^2 \right] \quad \mathcal{R}_k'' + 2 \frac{z'}{z} \mathcal{R}_k' + k^2 \mathcal{R} = 0.$$

$$\mathcal{P}_{\mathcal{R}} \propto \frac{H^2}{\epsilon c_s M^2} \quad \leftarrow \quad \mathcal{R} \simeq C_{1,k} + C_{2,k} \int \frac{c_s^2}{a^3 M^2 \epsilon H} dN$$

$$\frac{d\mathcal{R}}{dN_e} = C_{2,k} \exp \left[- \int (3 + \epsilon_H - 2\eta_H - 2s + \mu) \right] dN_e$$

Example: The EFT of inflation (slow-roll)

$$m = 0, \quad M = M_P$$

Unitarity: $\Lambda^4 \sim 16\pi^2 M_P^2 H^2 \epsilon \frac{c_s^5}{1 - c_s^2} \gg H^4$ Cheung et al 2007

$$c_s^4 \gg \mathcal{P}_{\mathcal{R}} \implies \epsilon_{\text{PBH}} \ll \Delta_{\zeta \text{CMB}}^2 c_{s \text{CMB}} \left(\frac{r_{\text{CMB}}}{0.07} \right) \left(\frac{\Delta_{\zeta \text{PBH}}^2}{0.01} \right)^{-5/4}$$

GB, Beltran-Jimenez, Pieroni 2018

Ghost condensate: $\mathcal{P}_{\mathcal{R}} \sim 0.01 \left(\frac{H}{M} \right)^{5/2}$

Arkani-Hamed, et al 2003

$$\omega^2 = c_s^2 k^2 + \alpha \frac{k^4}{a^2 H^2}$$

Example: The EFT of inflation (slow-roll)

$$S_{\mathcal{R}}^{(2)} = \int d^4x A a^3 \left[\dot{\mathcal{R}}^2 - c_s^2 \frac{(\nabla \mathcal{R})^2}{a^2} - \alpha \frac{(\nabla^2 \mathcal{R})^2}{H^2 a^4} \right],$$

$$\Lambda_3 \sim \varepsilon^{1/6} (M_{\text{Pl}} H^2)^{1/3}$$

Enhancement with respect to CMB scales:

$$c_s^2 \rightarrow 0 \quad : \quad (\Lambda_3/H)^{3/2}$$

$$c_s^2 < 0 \quad : \quad e^{2|c_s|^2} \Lambda_3/H$$

Weakly broken galilean symmetry

GB, Céspedes, Santoni, 2021

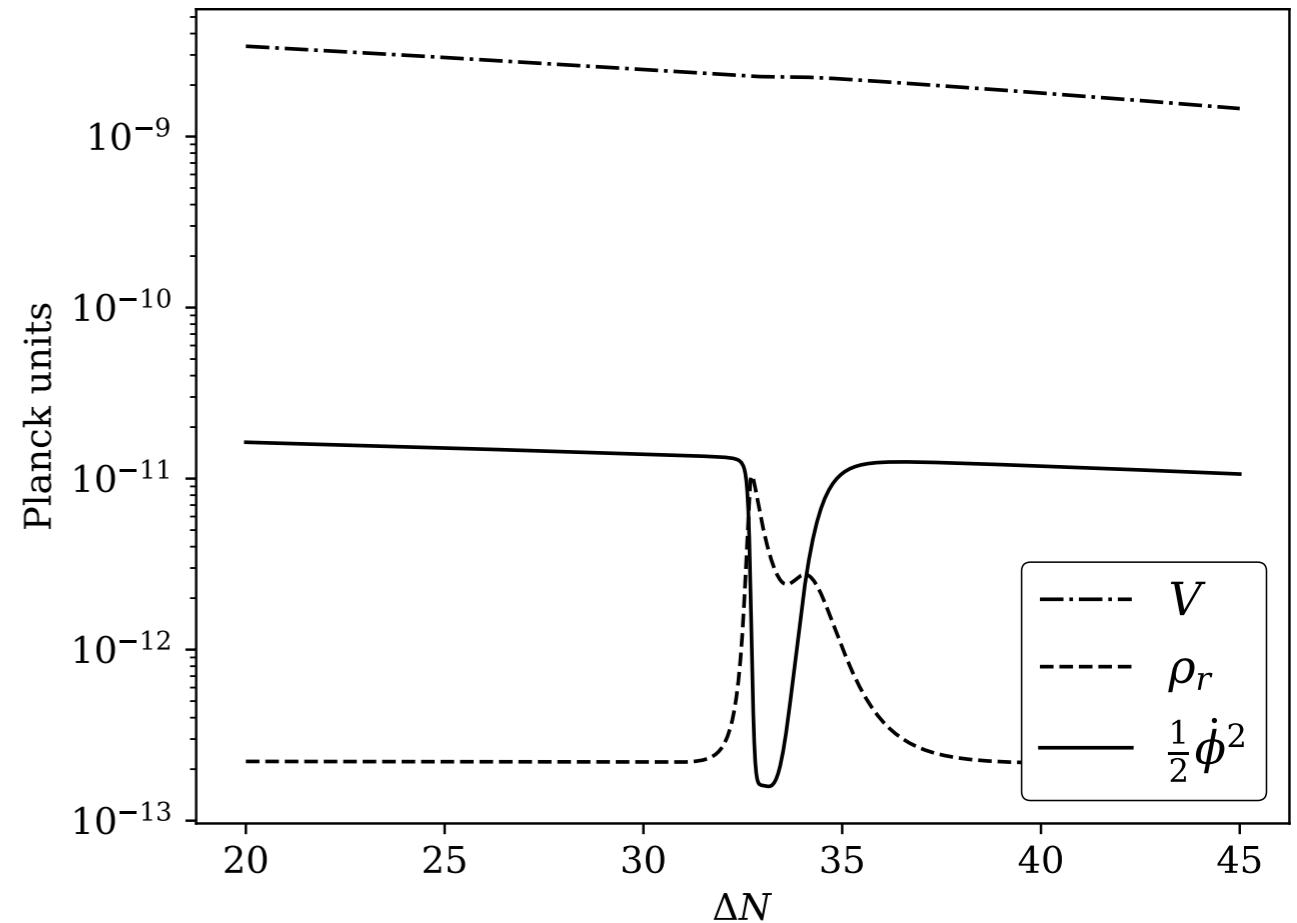
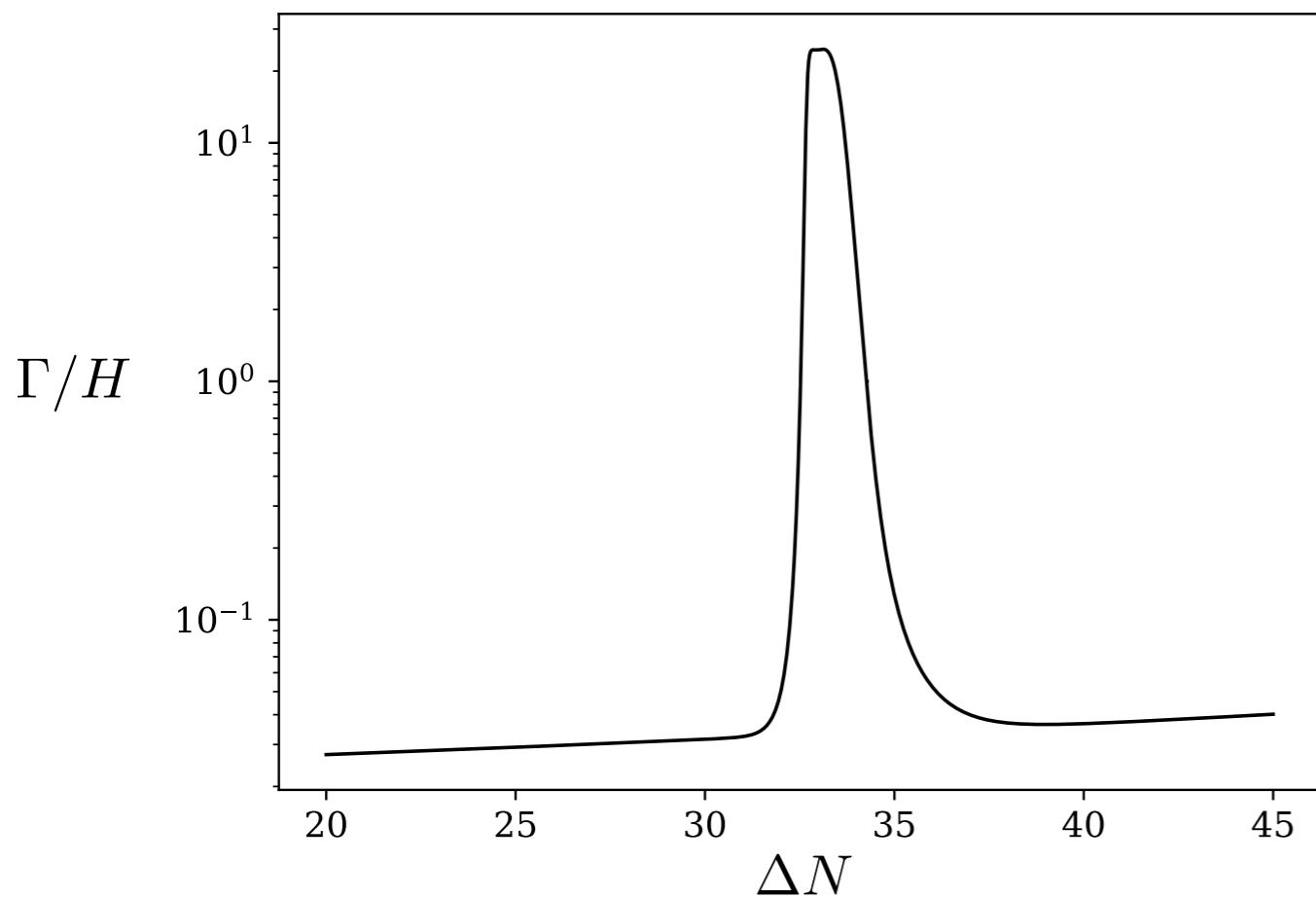
PBHs from dissipation during inflation

PBHs from dissipation during inflation

$$\ddot{\phi} + (3H + \Gamma)\dot{\phi} + \partial_{\phi}V = 0$$

$$\dot{\rho}_r + 4H\rho_r = \Gamma\dot{\phi}^2$$

$$\delta\ddot{\phi}_k + (3H + \Gamma)\delta\dot{\phi}_k + \left(\frac{k^2}{a^2} + \dot{\Gamma}\right)\delta\phi_k = \sqrt{\frac{2\Gamma T}{a^3}}\xi(t)$$

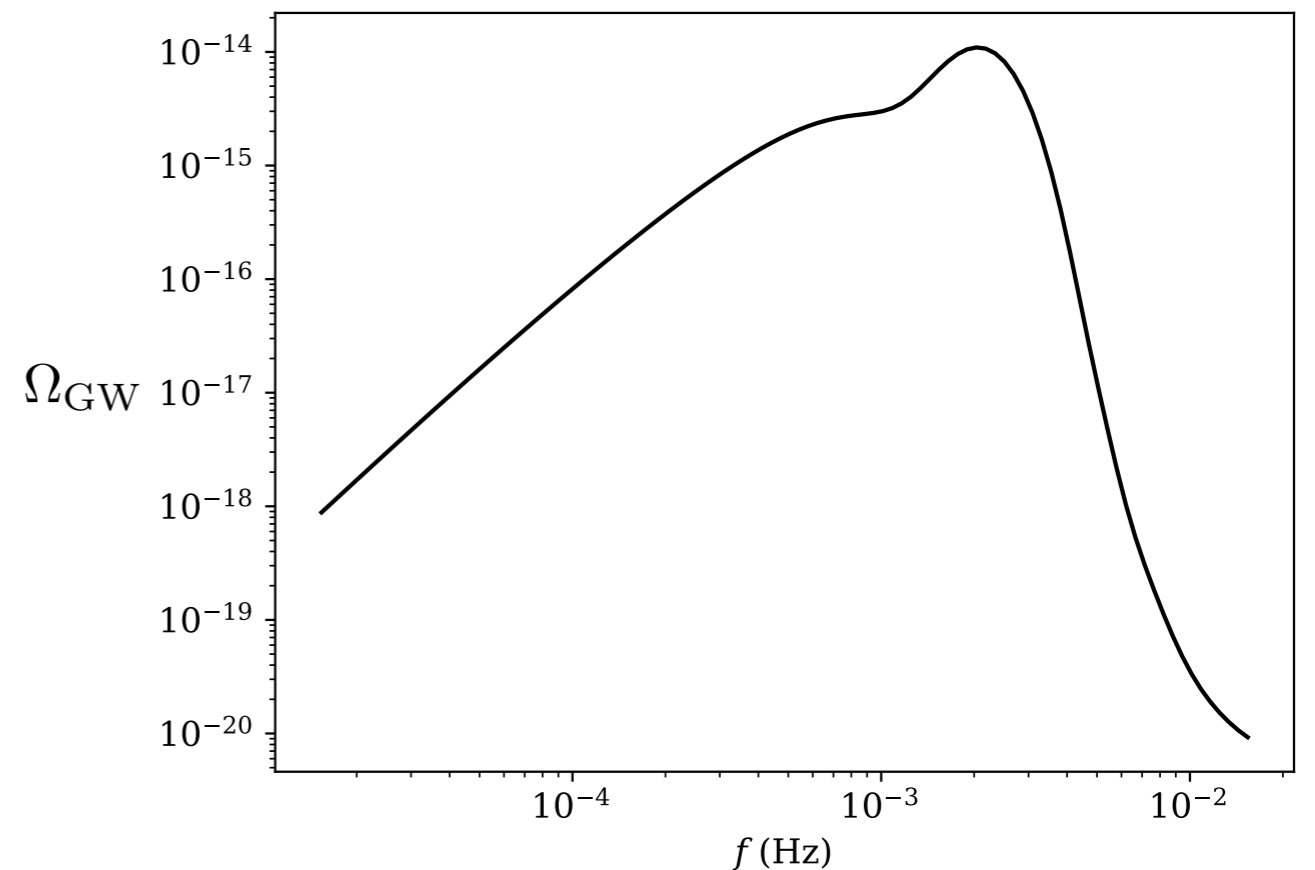
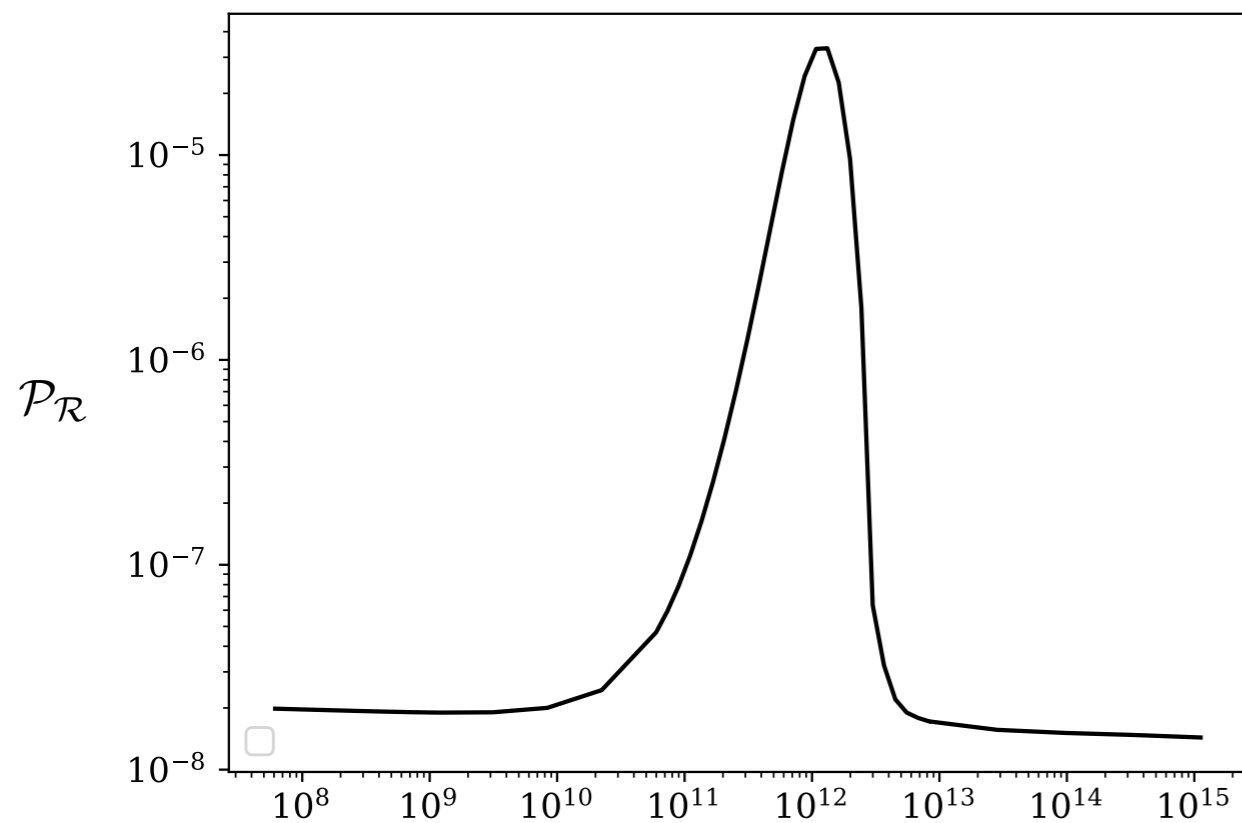


PBHs from dissipation during inflation

$$\ddot{\phi} + (3H + \Gamma)\dot{\phi} + \partial_{\phi}V = 0$$

$$\dot{\rho}_r + 4H\rho_r = \Gamma\dot{\phi}^2$$

$$\delta\ddot{\phi}_k + (3H + \Gamma)\delta\dot{\phi}_k + \left(\frac{k^2}{a^2} + \dot{\Gamma}\right)\delta\phi_k = \sqrt{\frac{2\Gamma T}{a^3}}\xi(t)$$



Summary

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Bounds have evolved during the last 5 years

PBH DM:

$$10^{-16} M_{\odot} \leftrightarrow 10^{-12} M_{\odot}$$

Rich phenomenology of inflationary and early universe cosmology: validity of perturbation theory, non-Gaussianities, quantum diffusion, dissipation, early matter domination, etc

And very interesting perspectives for GW experiments