



First measurement of anti- $k_T$  jet  
spectra and jet substructure using  
the archived ALEPH  $e^+e^-$  data at  
91.2 GeV

Yi Chen (MIT)  
BOOST 2022, Aug. 16

In collaboration with Y.-J. Lee,  
A. Badea, A. Baty, P. Chang,  
Y.-T. Chien, G.M. Innocenti, M. Maggi,  
C. McGinn, D. V. Perepelitsa, M. Peters,  
T.-A. Sheng, J. Thaler

The MITHIG's work is supported by DOE-NP





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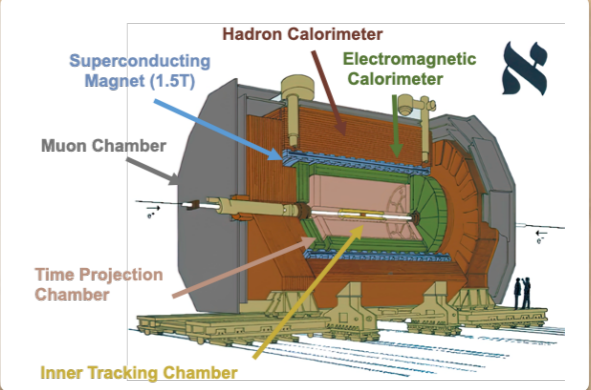
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energy and  
substructure

# anti-“ $k_T$ ” jet in $e^+e^-$ with ALEPH

$\sqrt{s} = 91.2 \text{ GeV}$



Presented by Yi



with friends

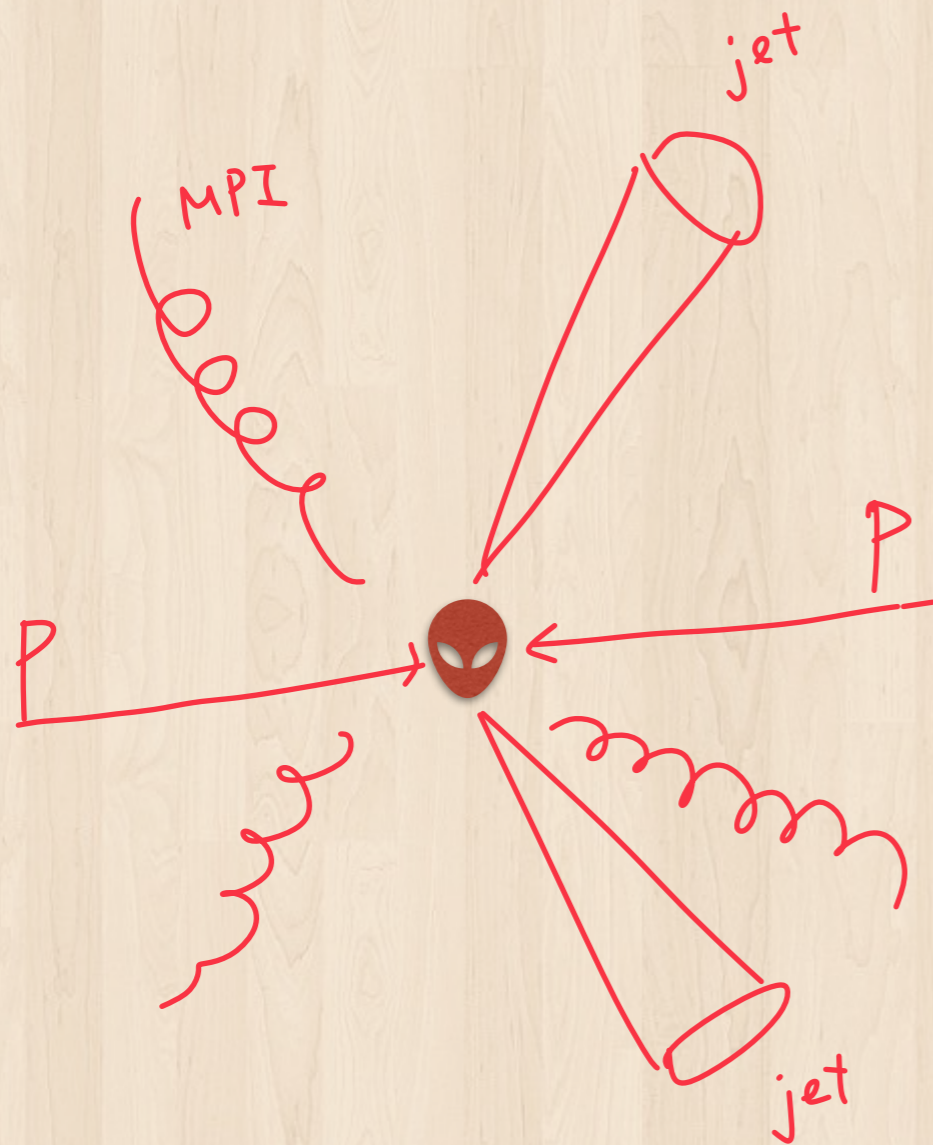
ALEPH, LEP



Why jet in LEP  $e^+e^-$ ?



# It's clean

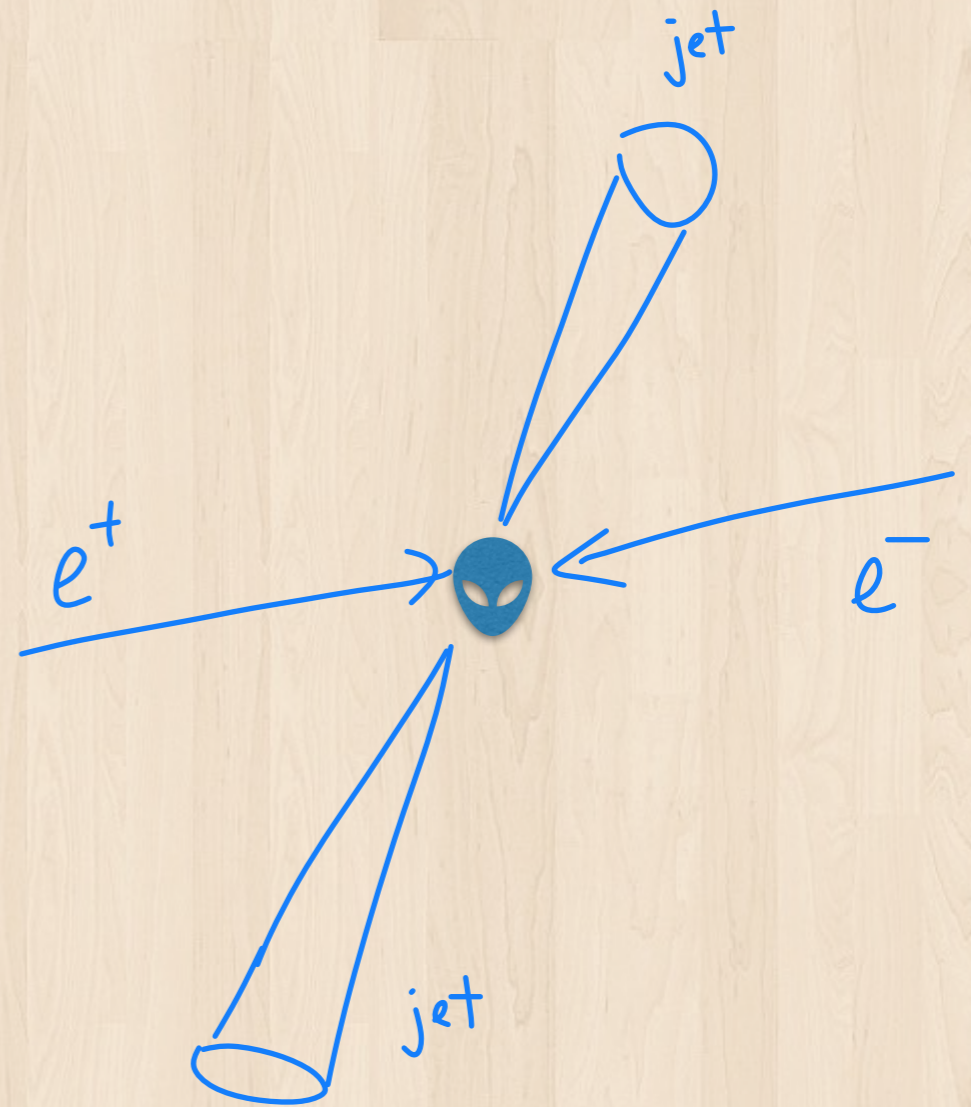


~~PDF~~

~~MPI~~

~~Beam  
remnant~~

...

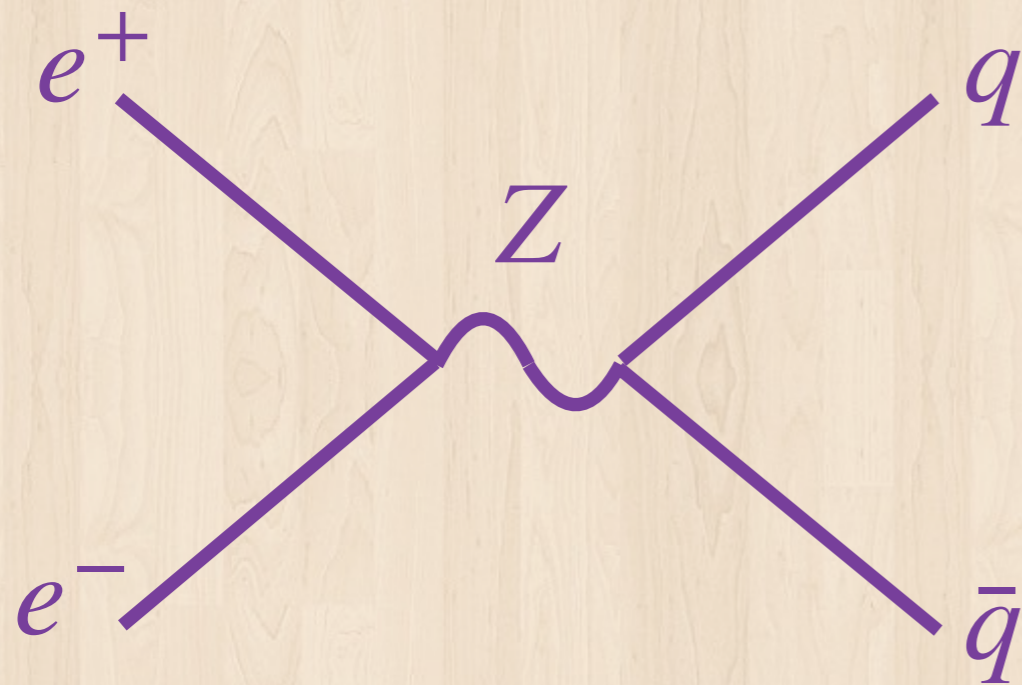


Cleanest test of QCD

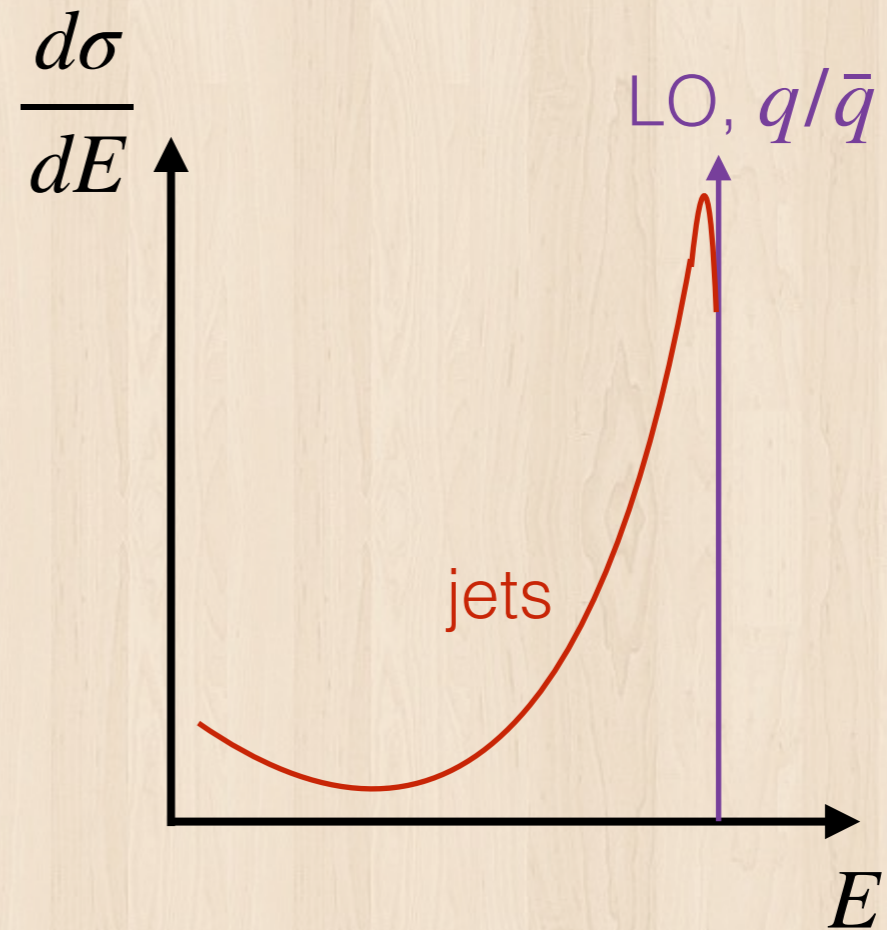


# It's peaked and quark dominated

91.2 GeV collisions



Dominant jet diagram

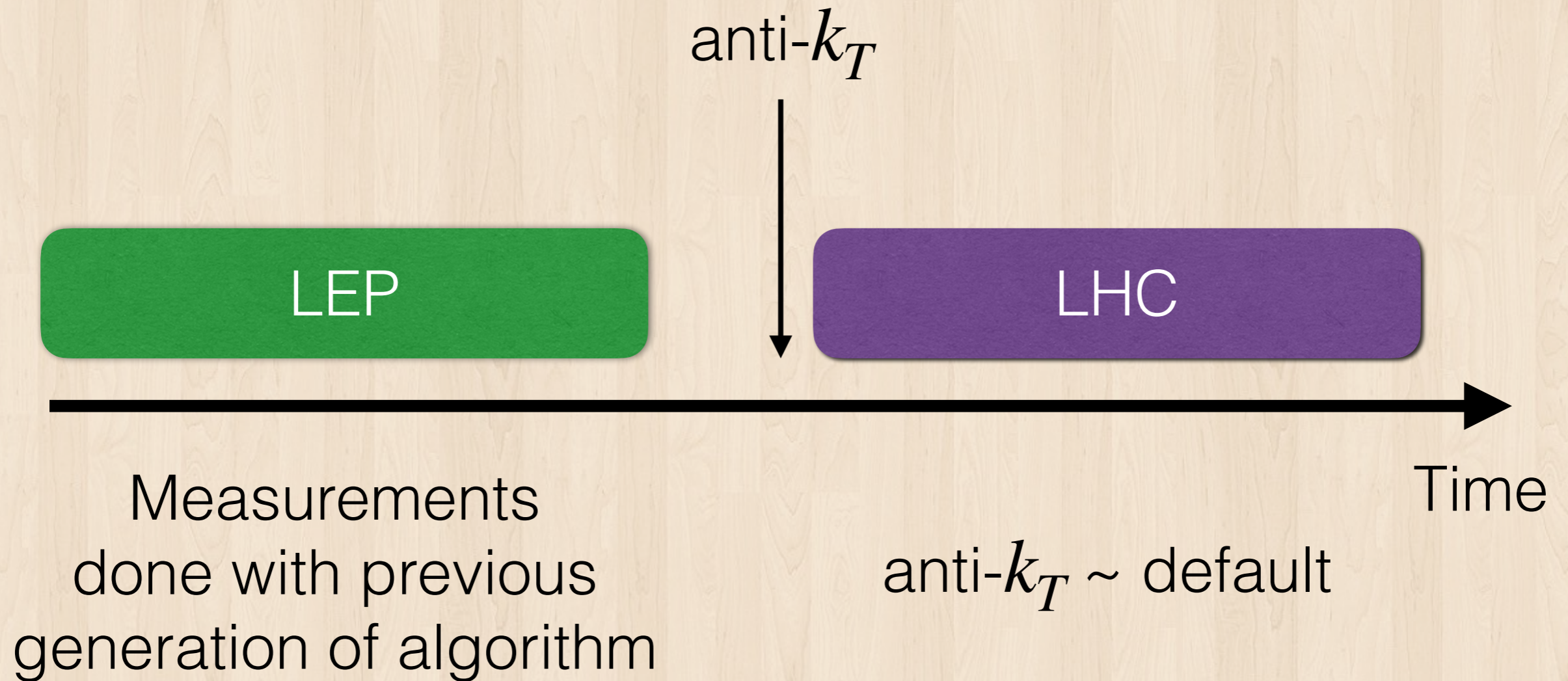


Peaked structure is useful for studying jets

Out-of-cone energy  $\rightarrow$  "energy loss"



# It predates anti- $k_T$

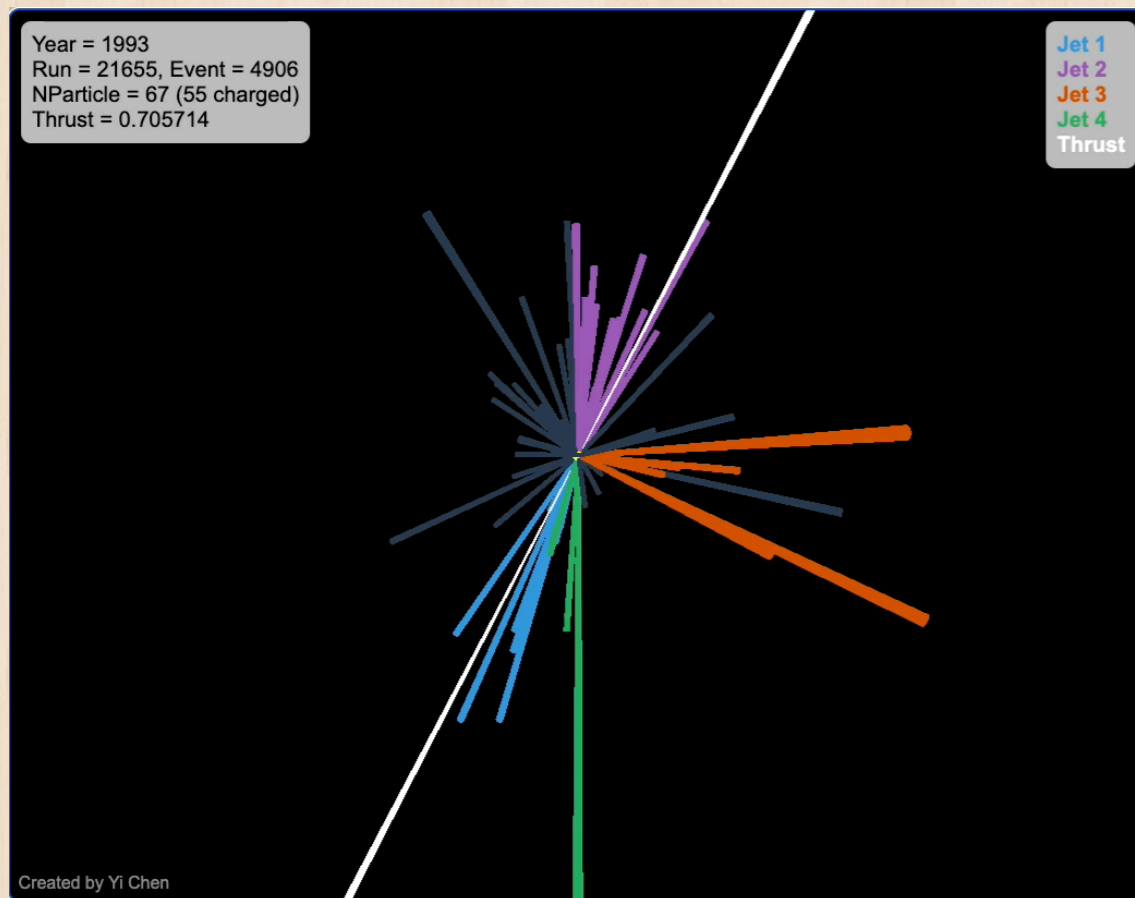


Excellent opportunity for re-analysis

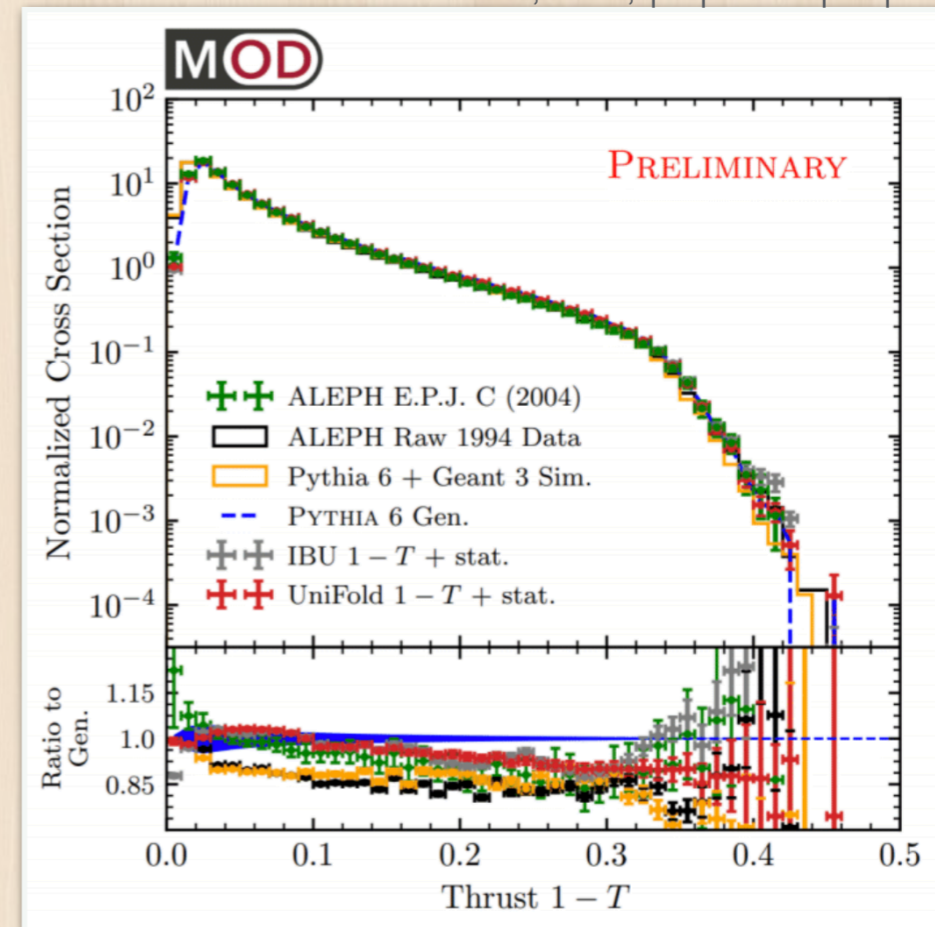


# High quality archived data

Badea, Komiske, Metodiev, Thaler,  
Nachman, Lee, paper in preparation



[\(link to animation\)](#)



Published results can be reproduced

Big thanks to ALEPH collaboration and MIT open data



Anti-“ $k_T$ ” Jets



# Jets are well calibrated

Energy flow object

Jet clustering

MC-based calibration

Data/MC residual calibration

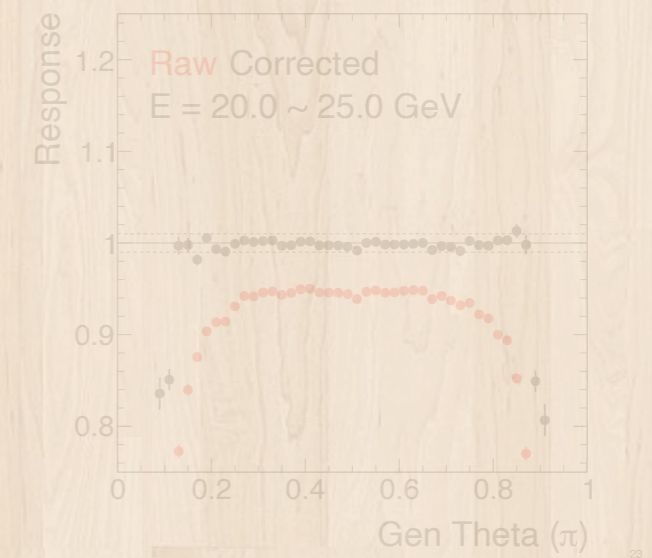
Data/MC resolution

Cluster with  $e^+e^-$  version of anti- $k_T$

$$d_{ij} = \min \left( E_i^{-2}, E_j^{-2} \right) \frac{1 - \cos \theta_{ij}}{1 - \cos R}$$

Two-steps:  
+/- side difference  
Multi jet mass

Up to 5% difference (relative)





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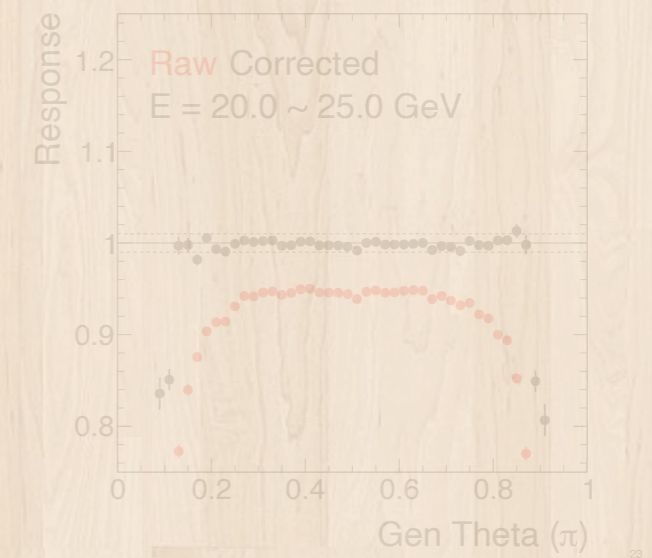
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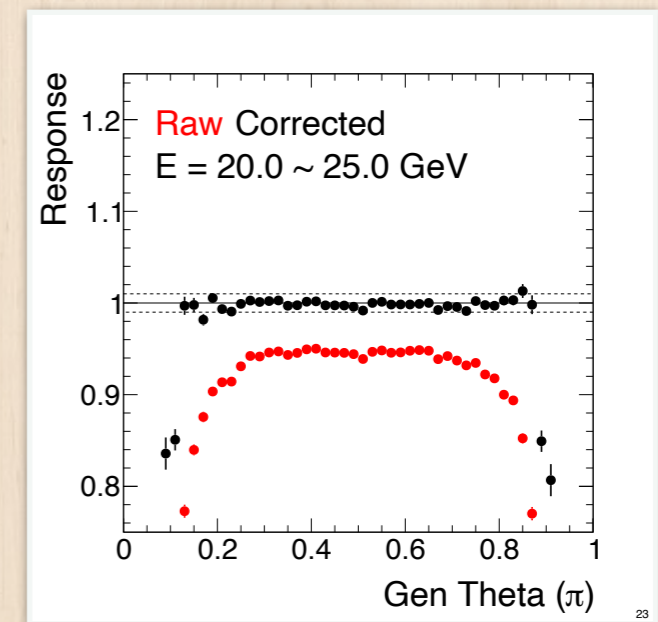
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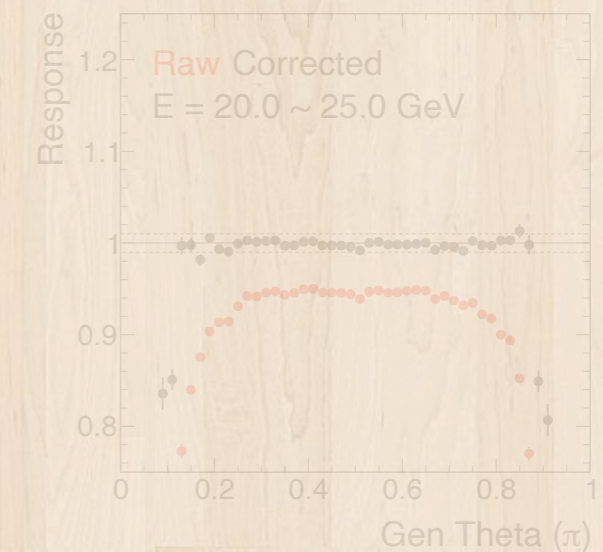
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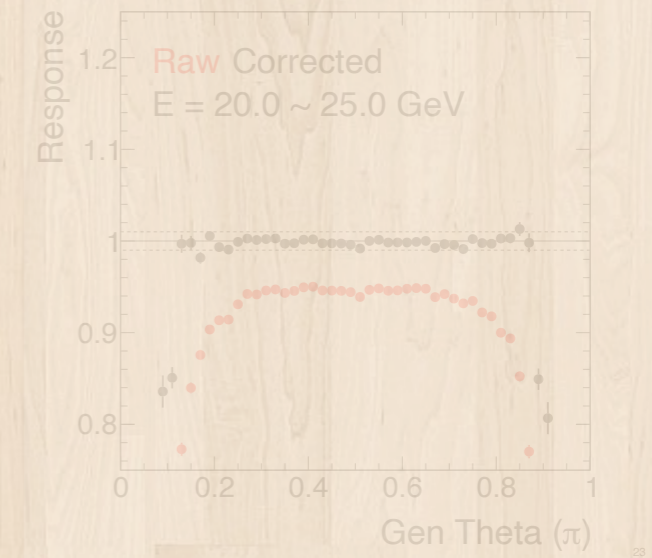
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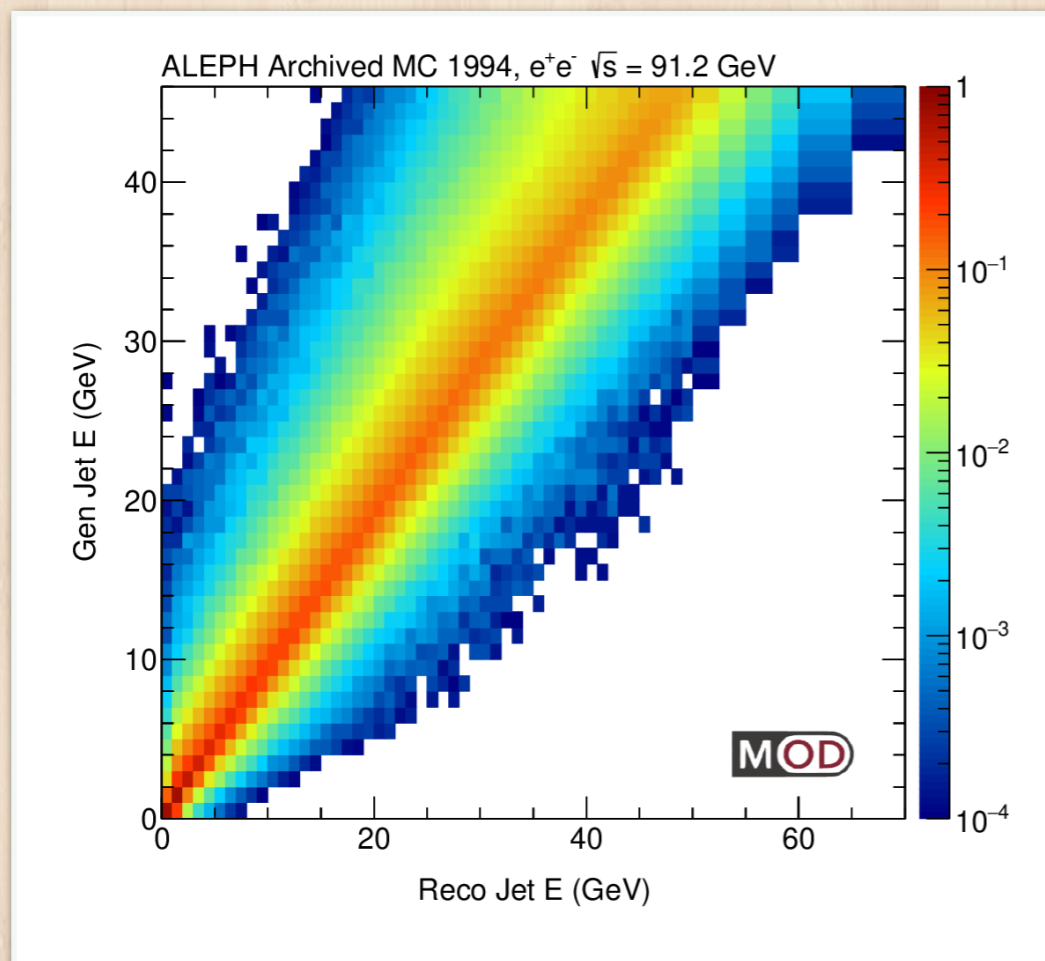
Two-steps:  
+/- side difference  
Multi jet mass



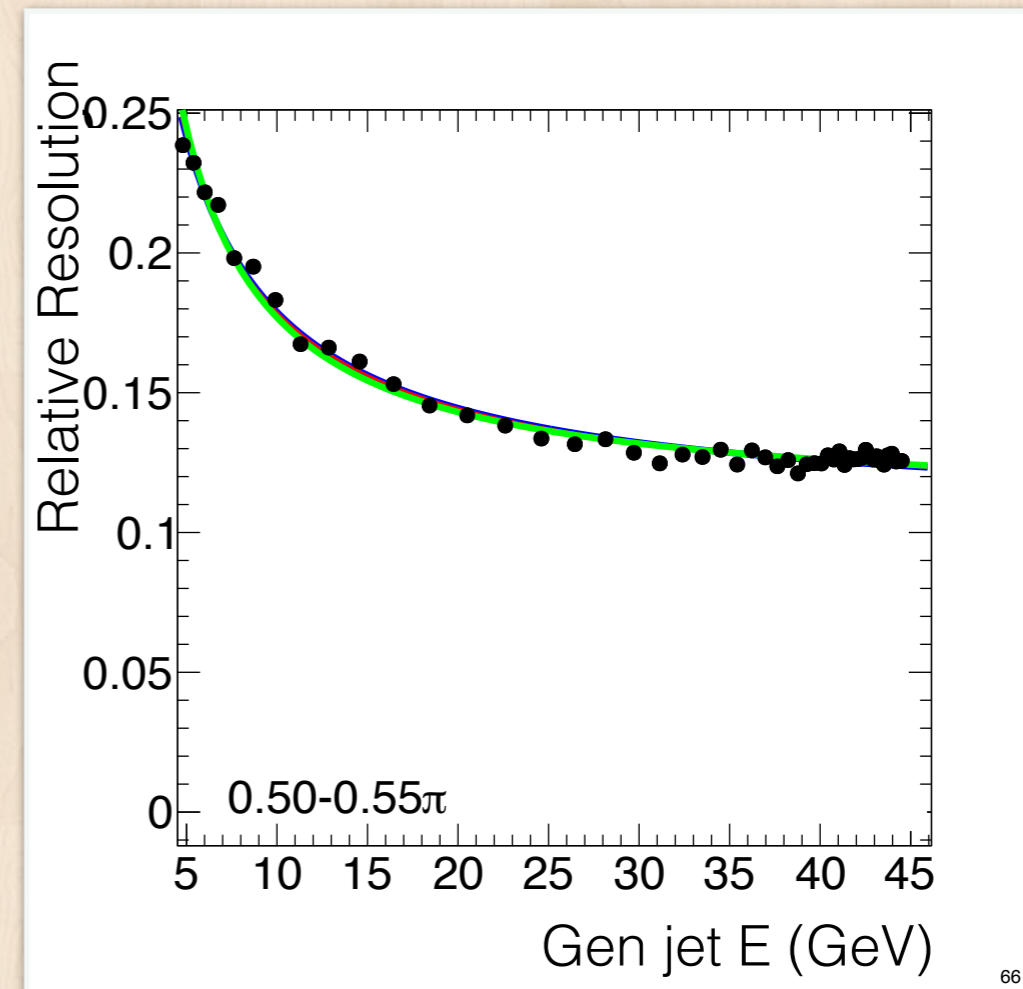
Up to 5% difference (relative)



# Performance



Good correlation  
No weird structure



Decent resolution  
10-20% in the  
range we measure



# List of measurements (so far)

anti-“ $k_T$ ” jet,  $R = 0.4$

$0.2\pi < \theta_{\text{jet}} < 0.8\pi$  ← acceptance (avoid beam pipe)

Inclusive jets

Energy spectra

Full jet mass

Groomed jet angle

Energy sharing

Groomed jet mass

Leading dijets

Energy spectra

Energy sum

Soft drop grooming



Inclusive jet spectrum



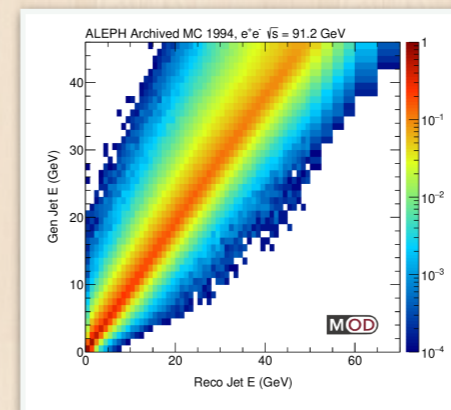
# Analysis overview

Raw spectrum

Corrected spectrum

Unfolded spectrum

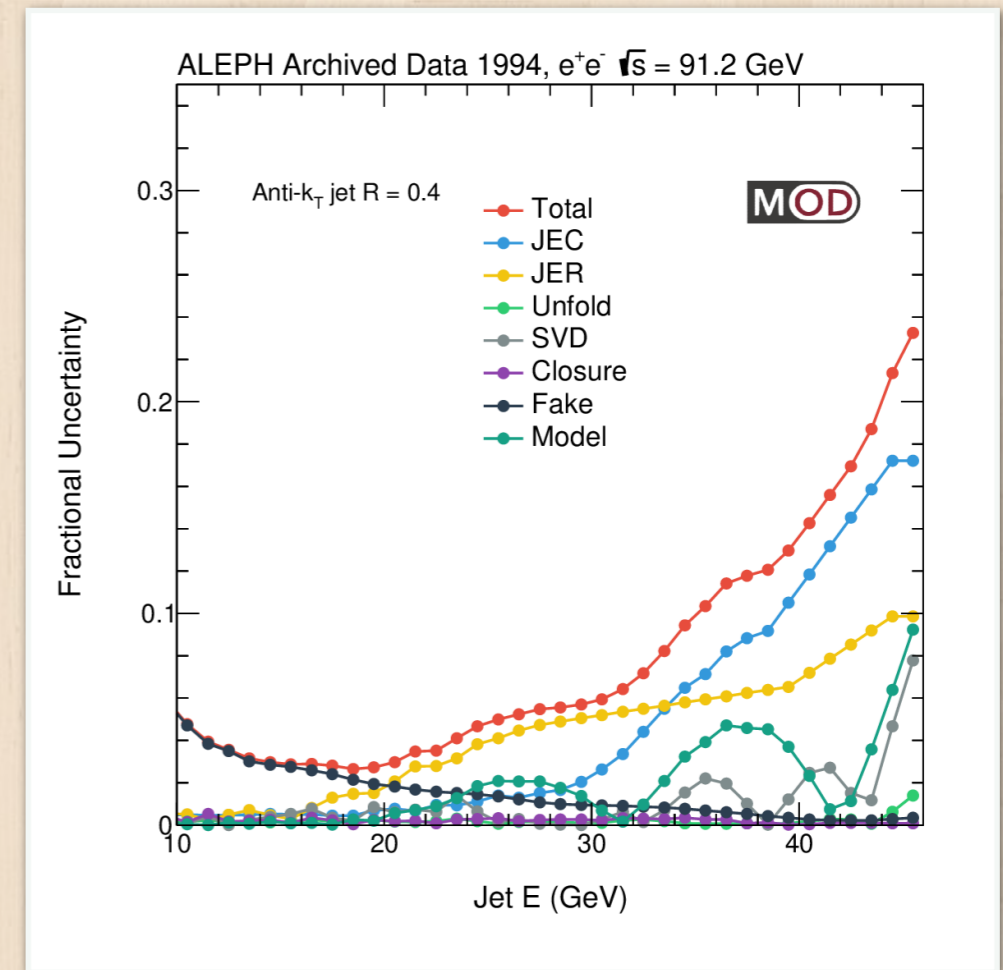
Jet calibration





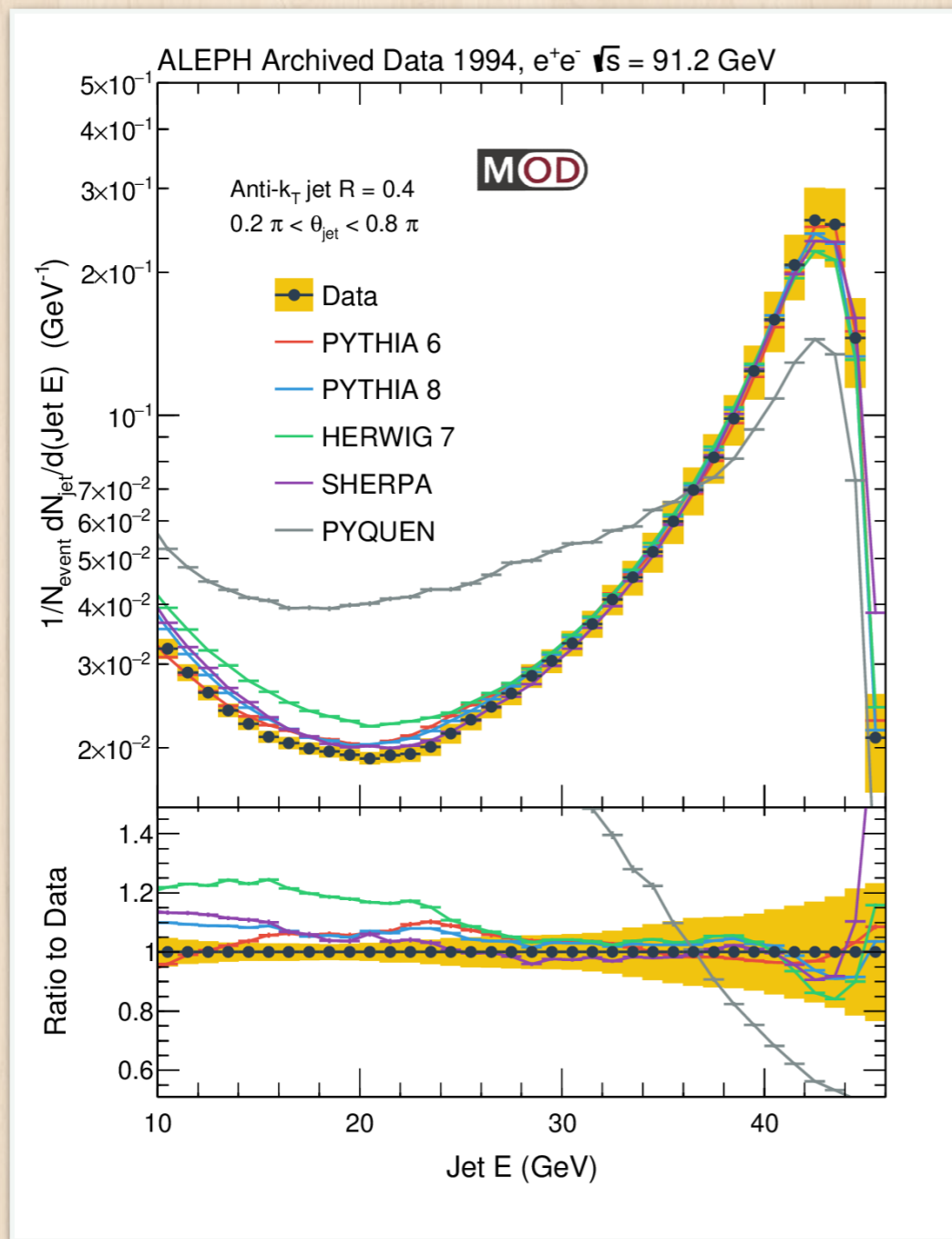
# Systematic uncertainties

- Jet-related
  - scale: change energy scale
  - resolution: vary jet smearing
- Unfolding
  - Prior & regularization
  - Different unfold method
- Fake (combinatorial jet)
  - generator jet matching studies
- Modeling





# Energy spectrum



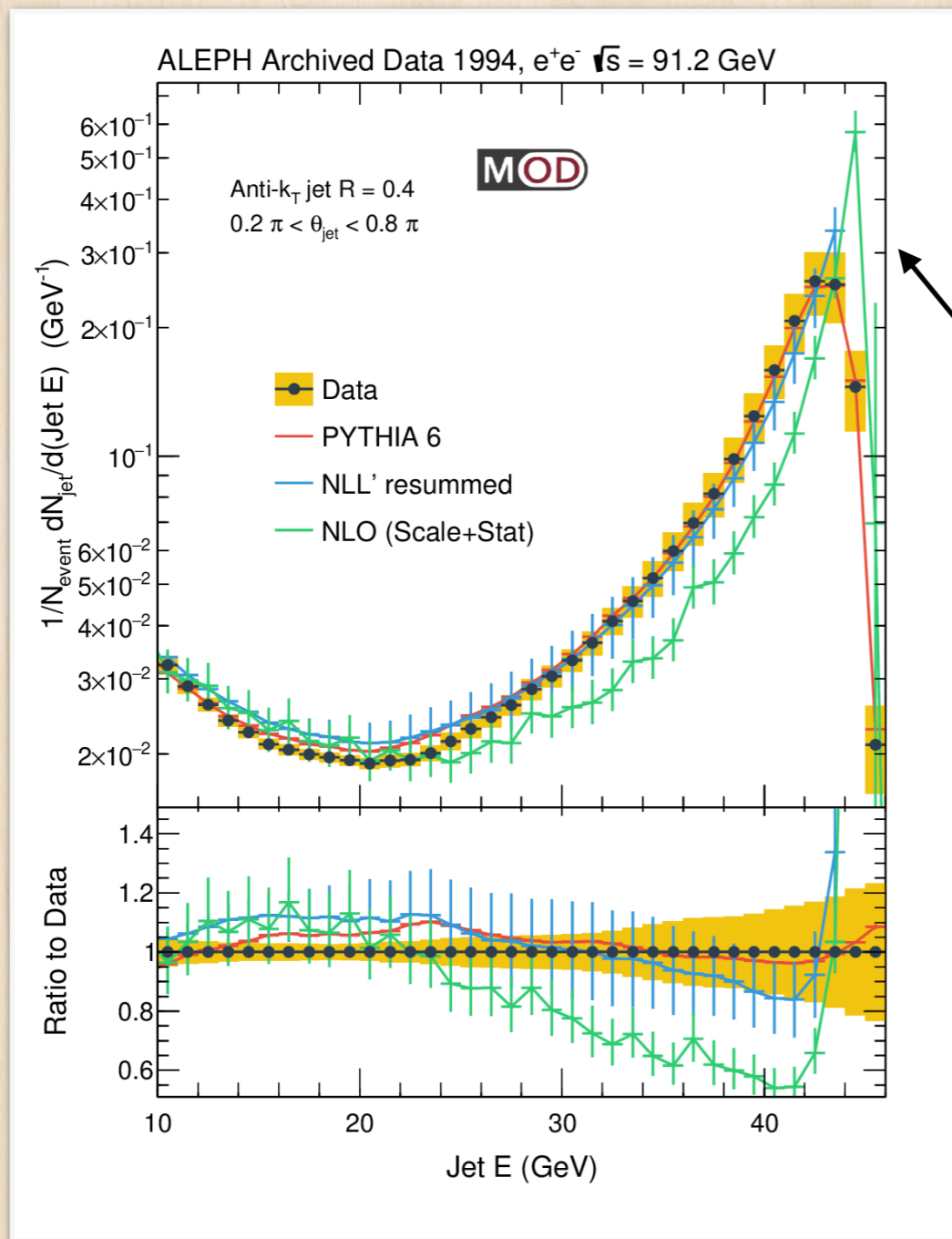
Comparison to MC and theory calculations (not shown in this plot)

Most generators can describe the peak region

Up to 10-20% disagreement at low E  
→ out-of-cone energy, wide angle emission, ...



# Energy spectrum



LO parton level  
= delta function at 45 GeV  
not too interesting to plot

NLO parton level sharper  
than measured data

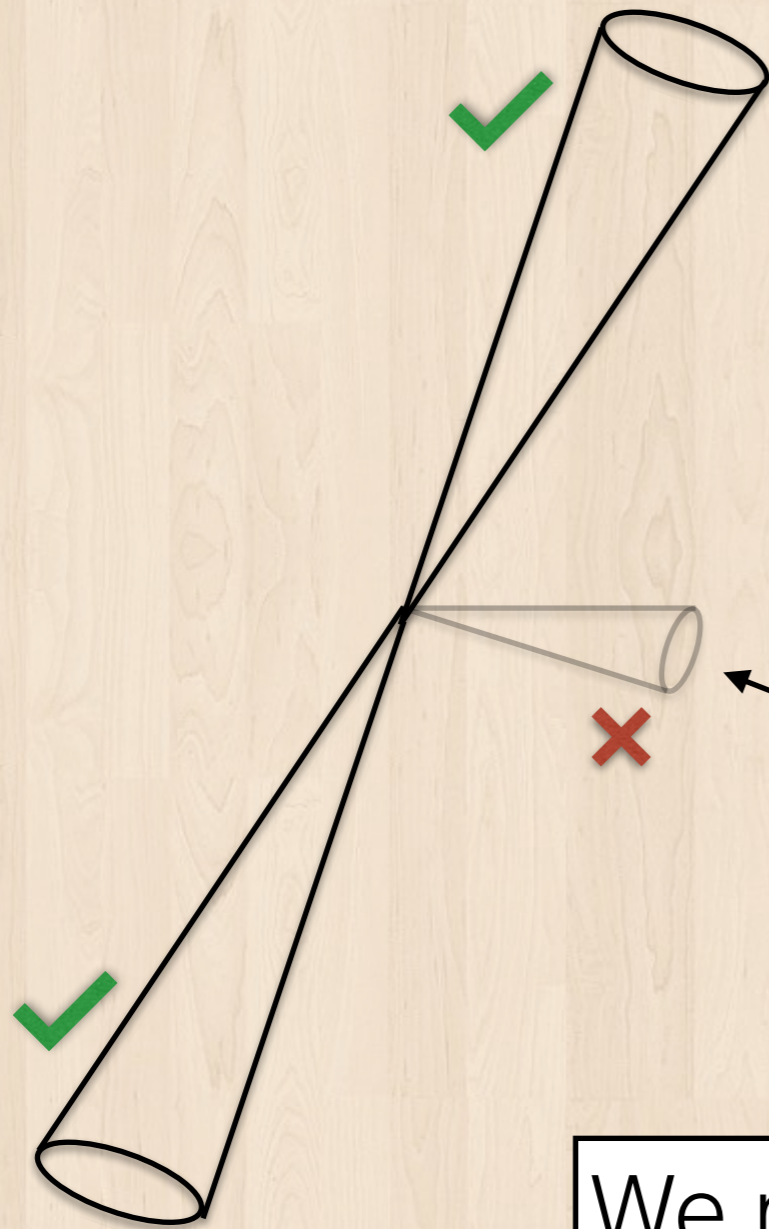
NLL' resummed generally  
describe data



Leading dijet



# Leading dijet



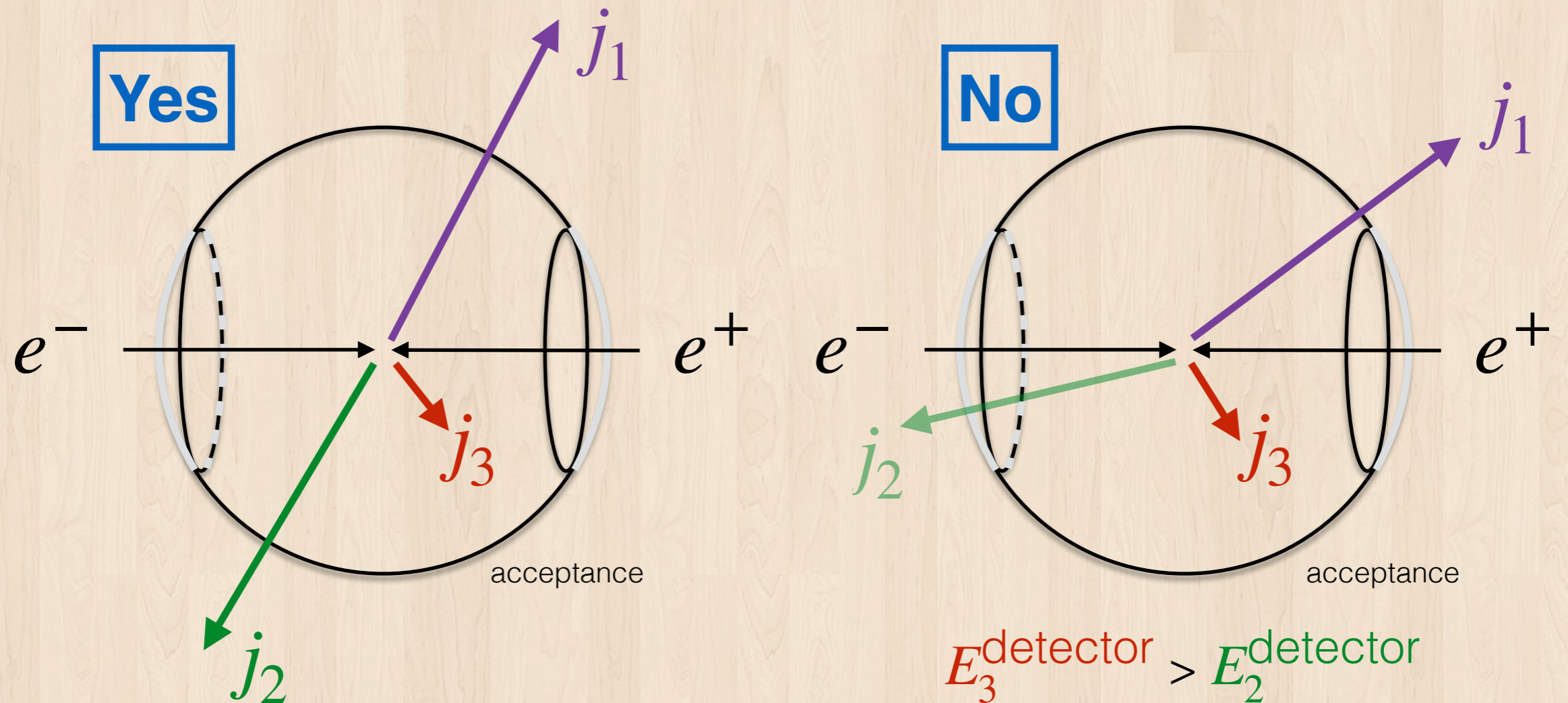
Better quantify the in-cone energy by limiting to only the leading dijet

Ignore the mini-jets

We measure the “global” leading dijet



# Global leading dijet

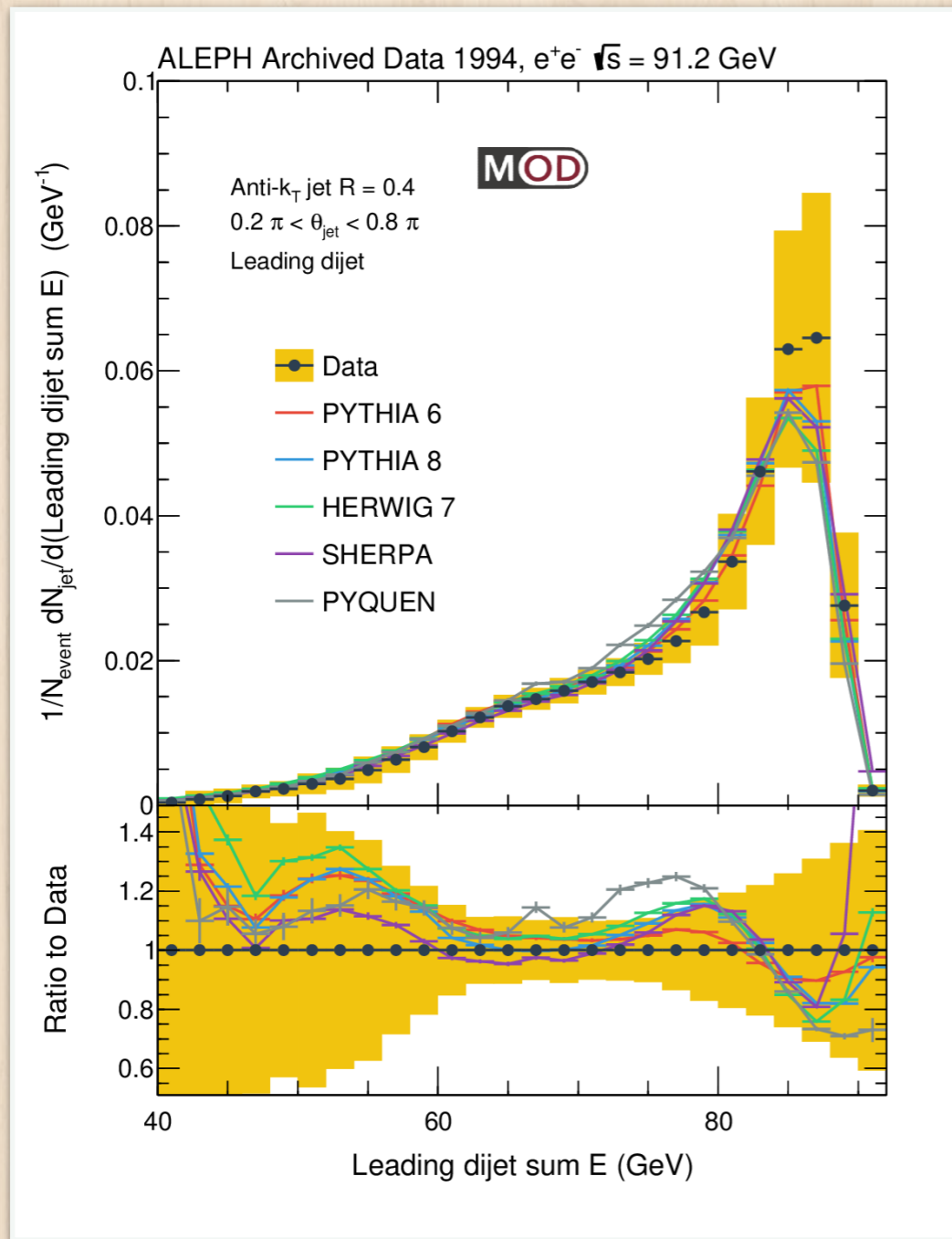


We want to measure global leading dijet

But: out-of-acceptance jets appear lower in energy  
→ selection + correction



# Energy sum



Total in-cone energy  
in the leading two jets

Most generators can  
describe data within  
(large-ish) uncertainty

Dominated by  
modeling uncertainty

(Leading di-jet energy: not shown)



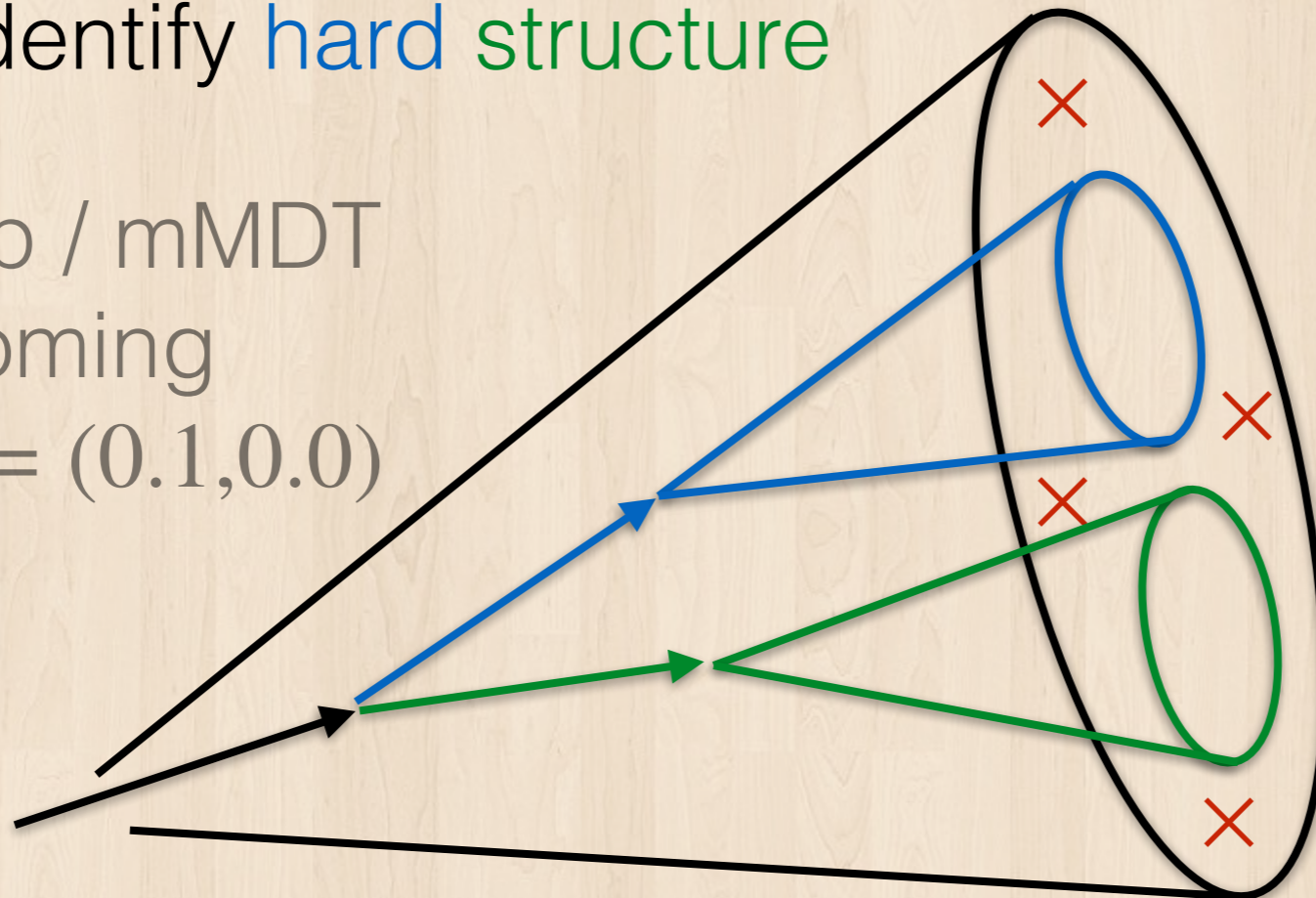
# Inclusive jet structure & substructures



# Jet substructure

Identify **hard structure**

Soft drop / mMDT grooming  
 $(z_{\text{cut}}, \beta) = (0.1, 0.0)$



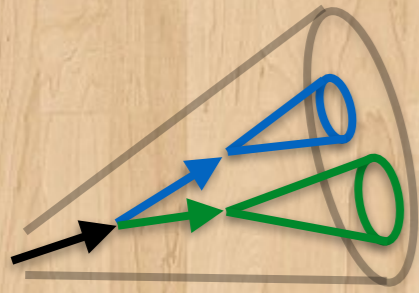
Clean up  
**wide-angle**  
soft energy

Not shown due to time

Adapt to use energy and opening angle for  $e^+e^-$

$R_g$  = opening angle  
 $z_g$  = energy sharing  
 $M_g$  = invariant mass

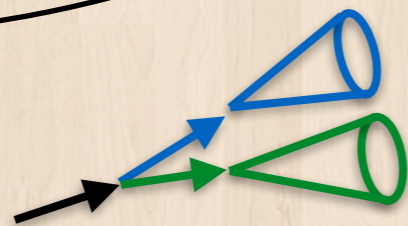
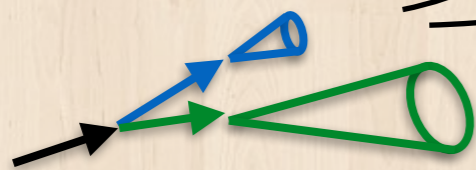
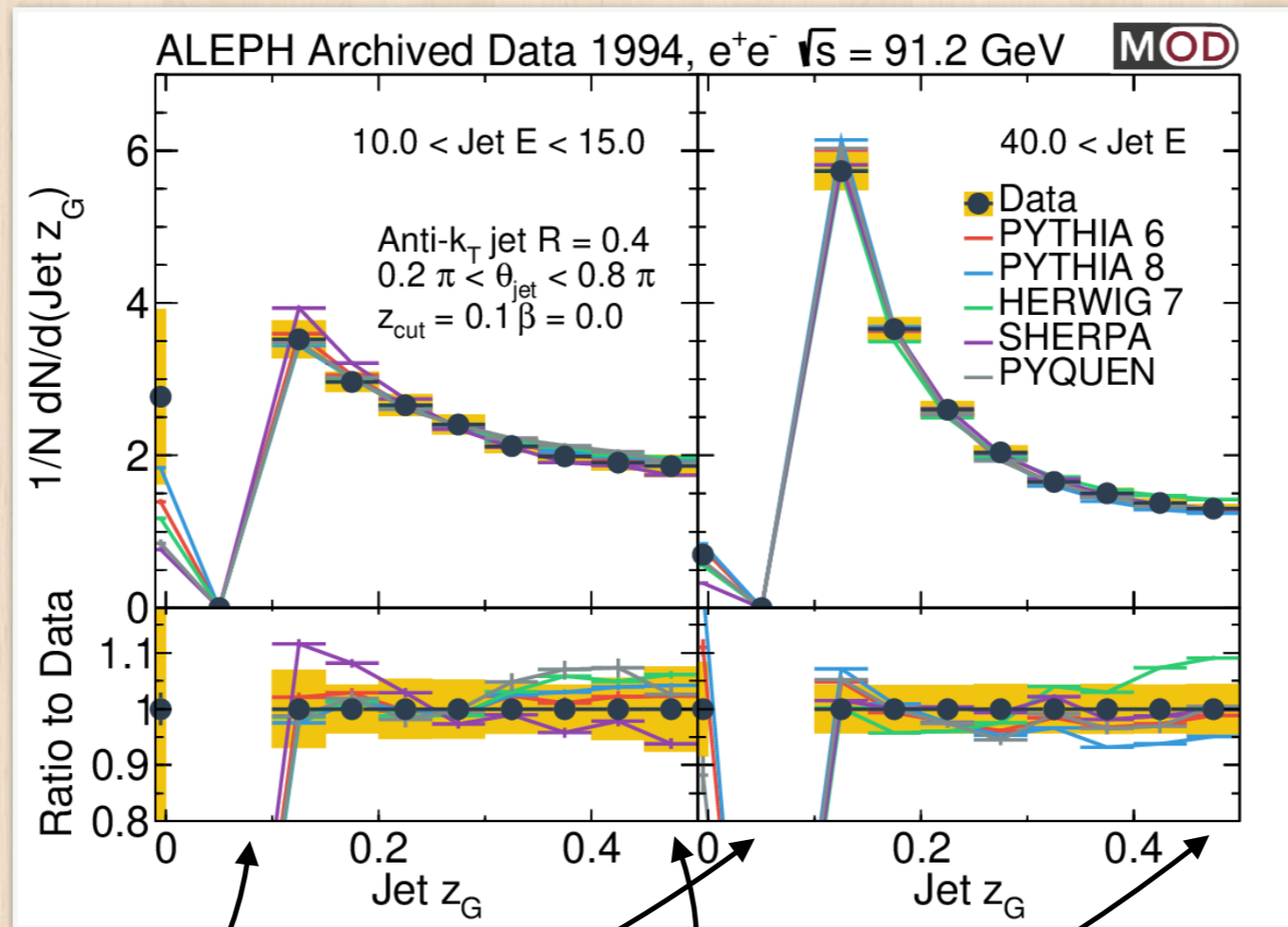




# Energy sharing $z_G$

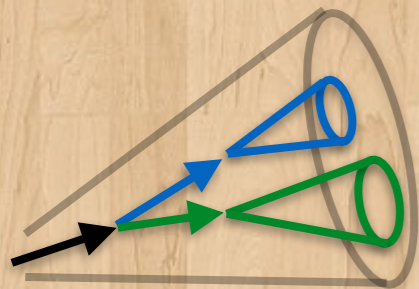
$$\frac{\min(\text{blue cone}, \text{green cone})}{\text{blue cone} + \text{green cone}}$$

Measurement binned in energy (most not shown)



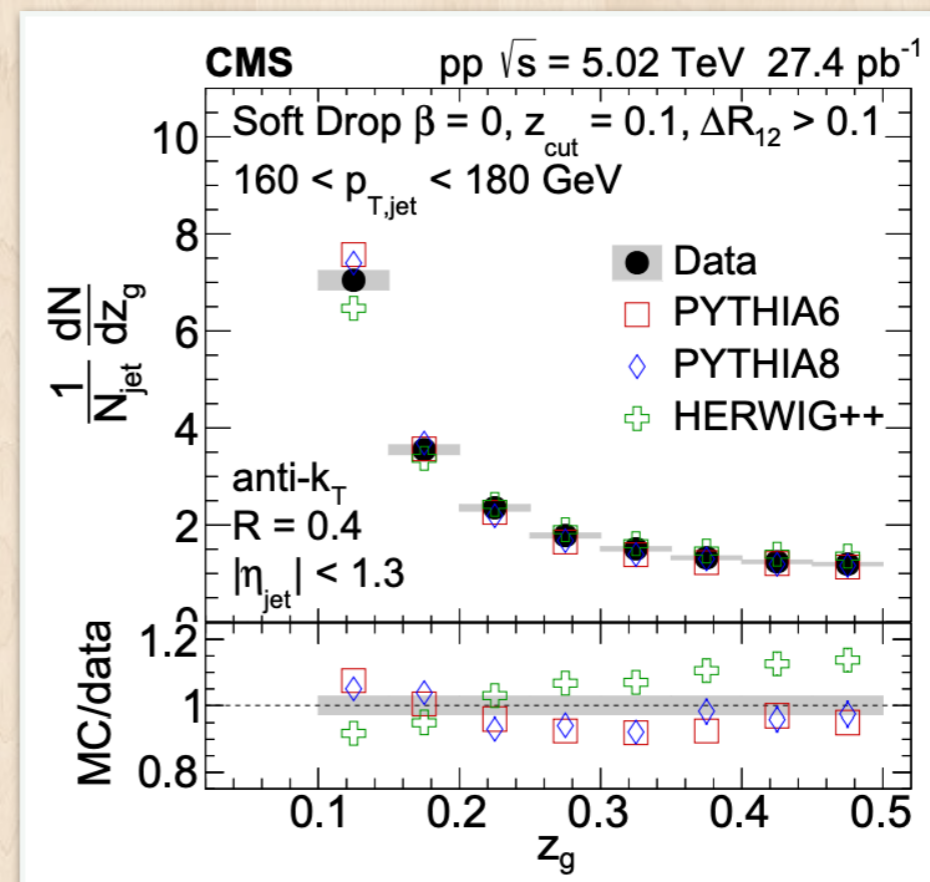
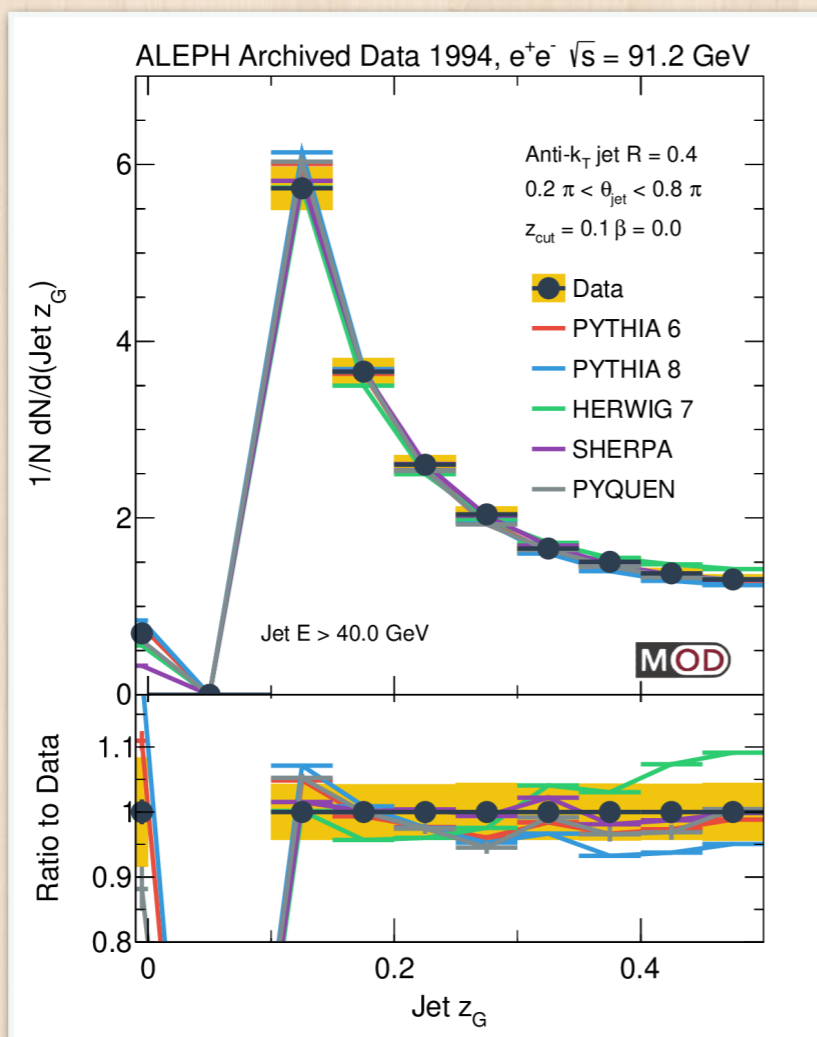
High energy  
More similar to the  $1/z$   
from splitting function





# Energy sharing $z_G$

$$\frac{\min(\text{blue cone}, \text{green cone})}{\text{blue cone} + \text{green cone}}$$

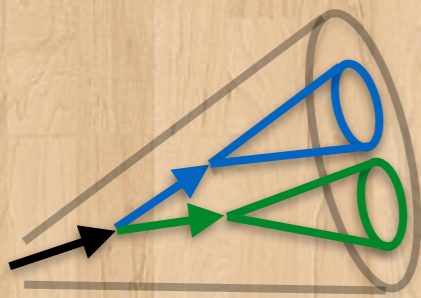


At high energy similar to LHC results

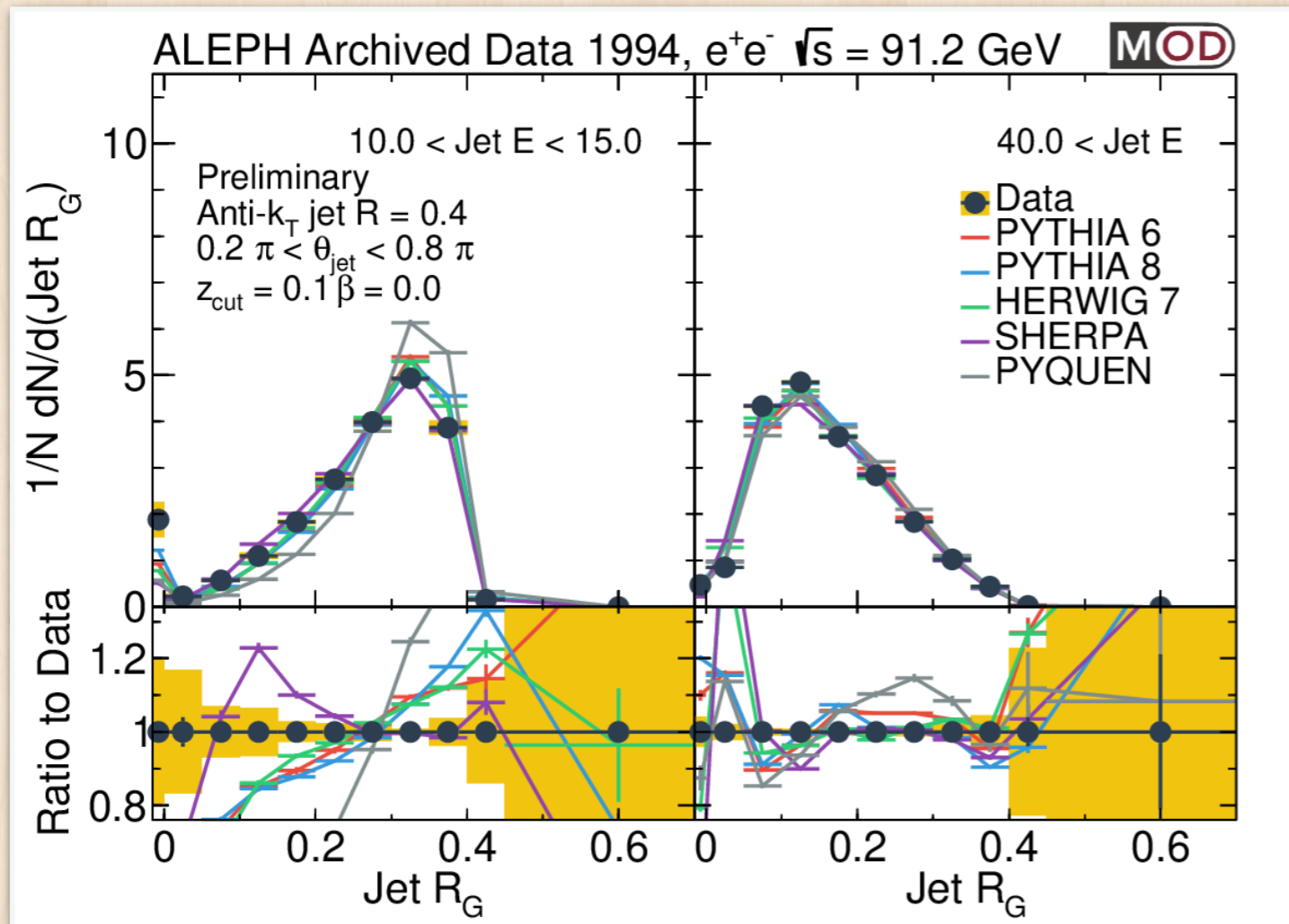
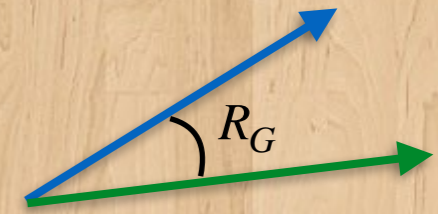
Comparison to **PYTHIA** and **HERWIG** also similar

Disagreement in LHC can be improved by  $e^+e^-$  input





# Groomed $R_G$

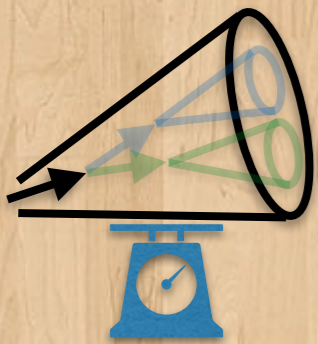


Much higher  $R_G$   
 for low energy jets  
 $\Rightarrow$  soft radiation &  
 combinatorial

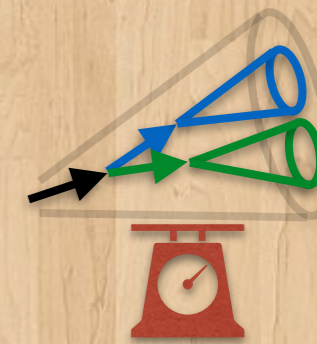
High energy jets  
 more similar to  
 LHC/RHIC

Very distinct behavior between low and high energy  
 Worse data/generator agreement at low energy

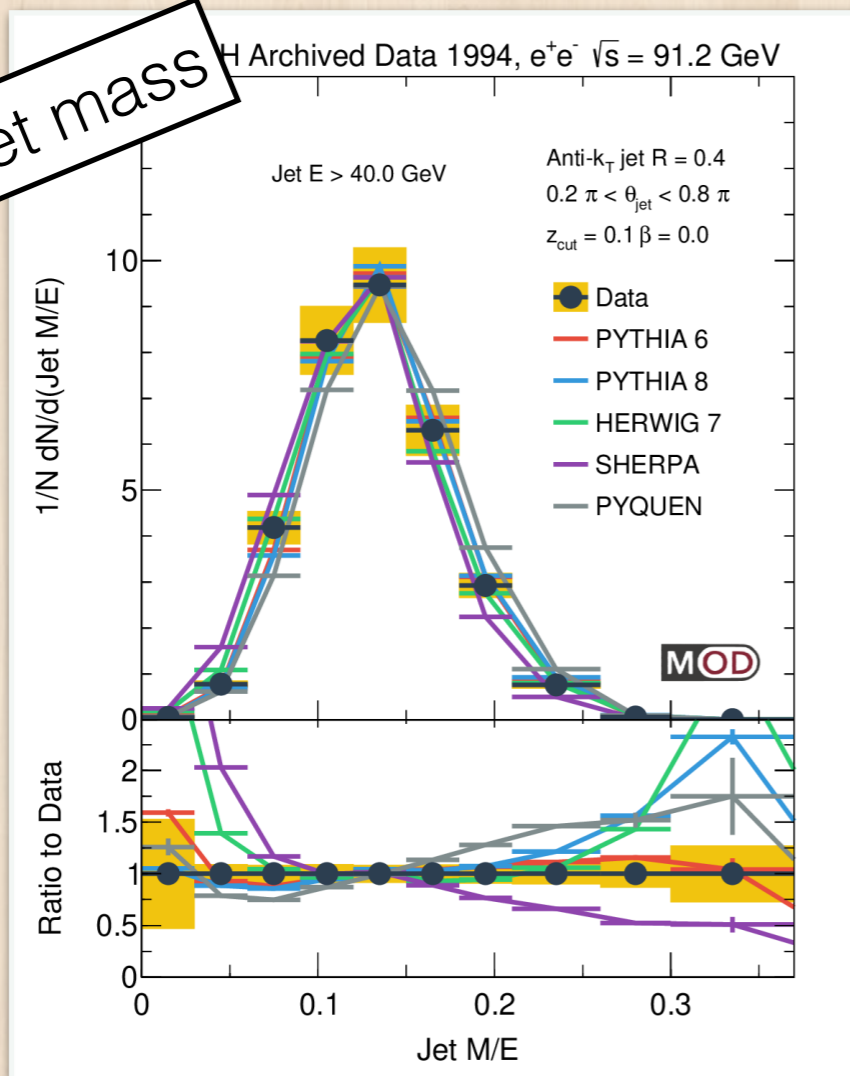




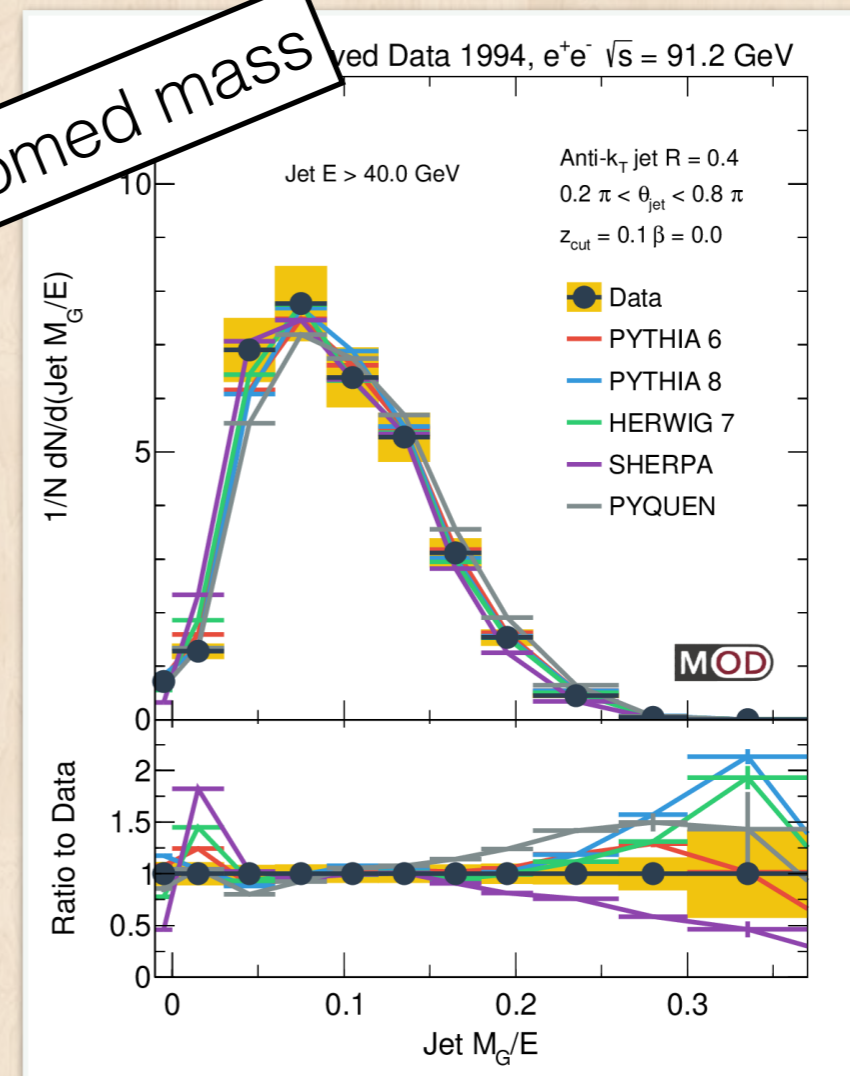
# Jet mass



Full jet mass



Groomed mass



General shape vs tail  
Explicit  $(M - M_G)/E$

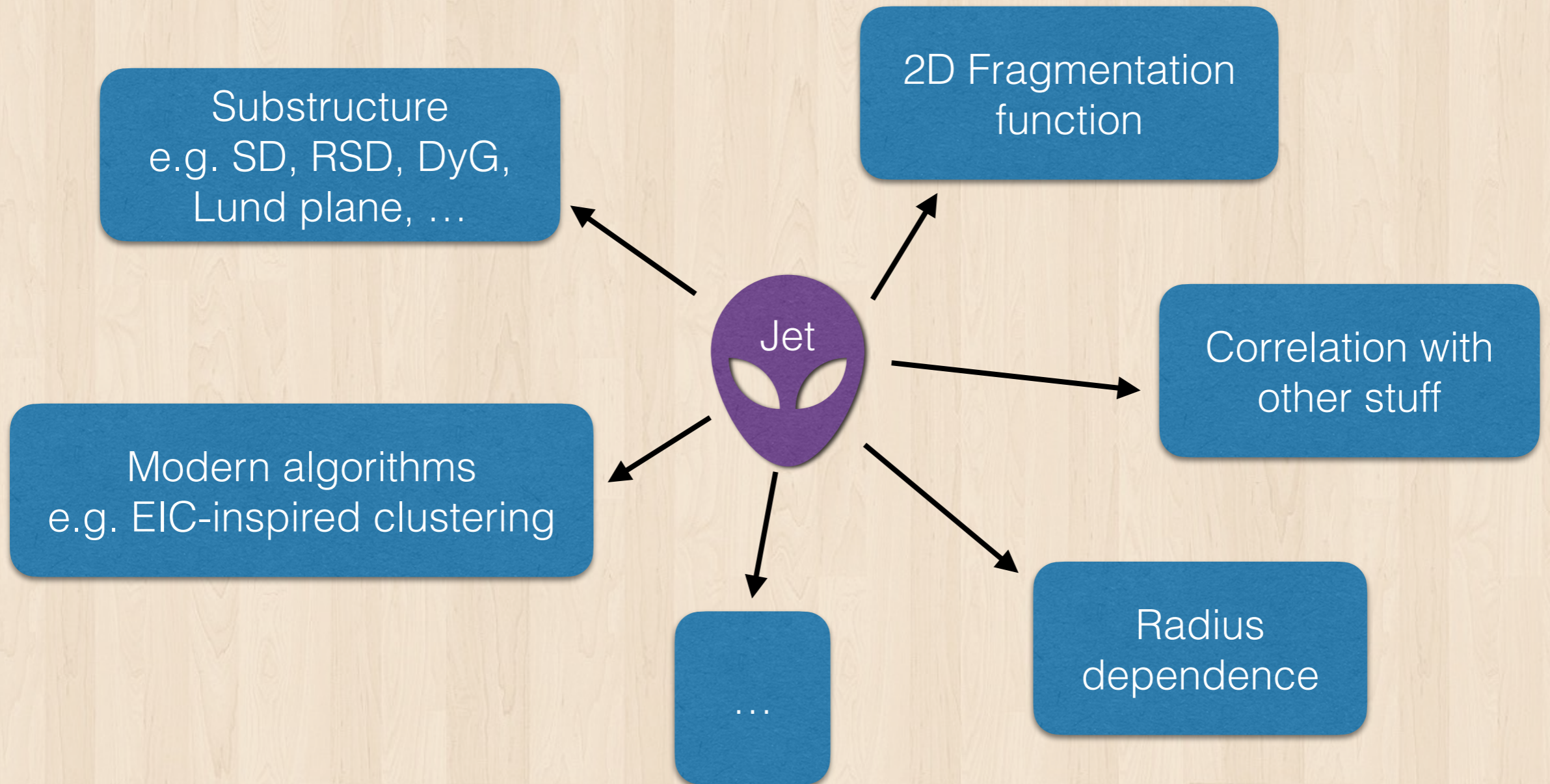
Interesting to compare to  
higher order generators



Looking into the future



# Many future possibilities



Testing ground for new algorithm developments

Provide reference measurements

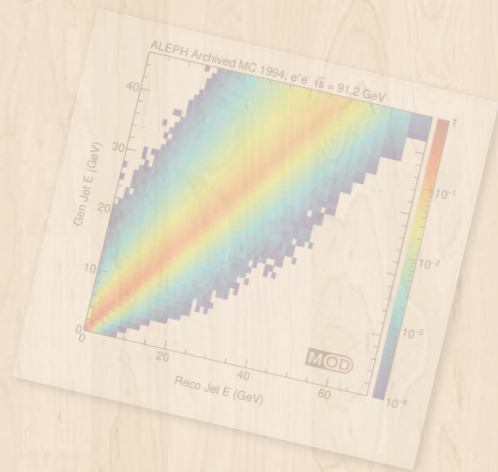
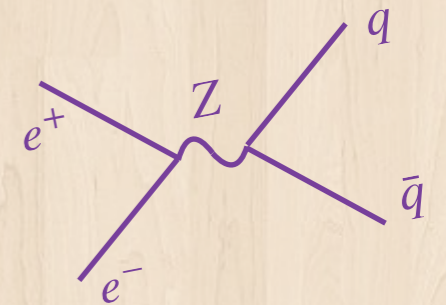


Concluding remarks



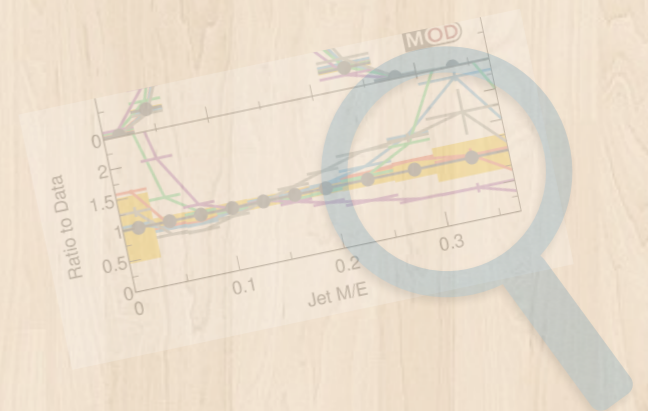
# Jets in LEP $e^+e^-$ data

$e^+e^-$  is the cleanest system to test QCD



Calibrated and measured jet spectra and substructure using the ALEPH archived data

Input for MC generators  
+ reference result

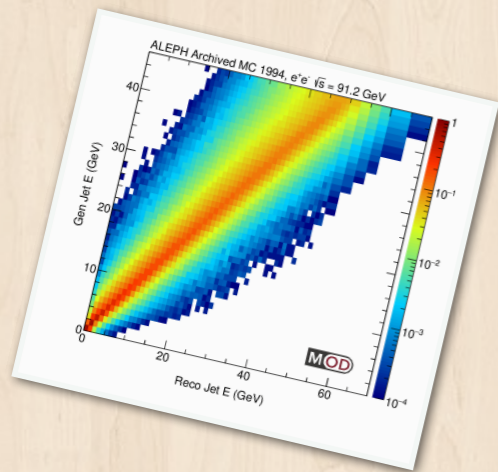


Numerous future possibilities



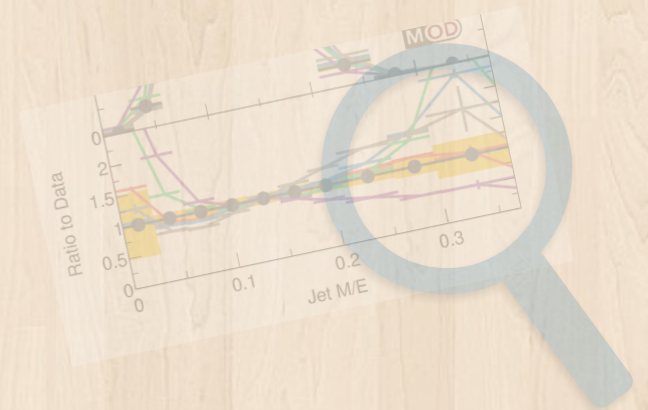
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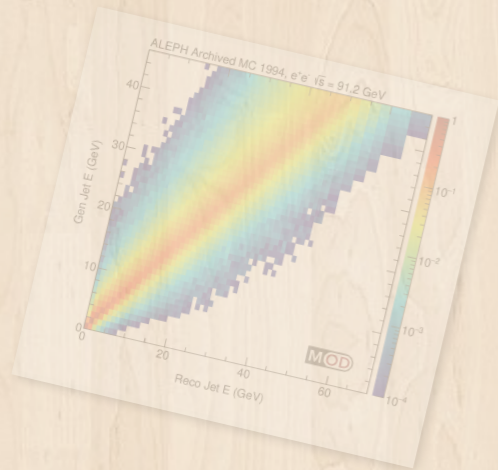


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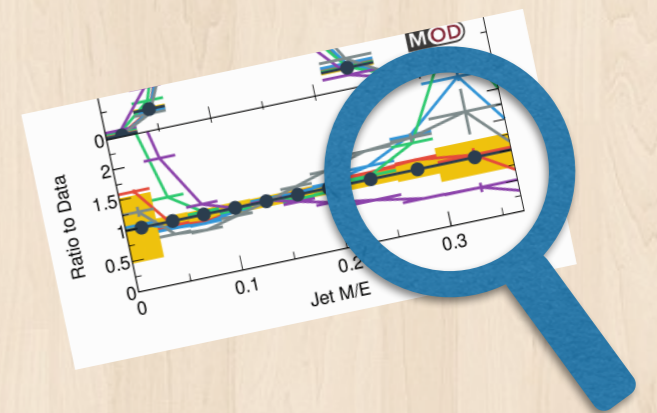
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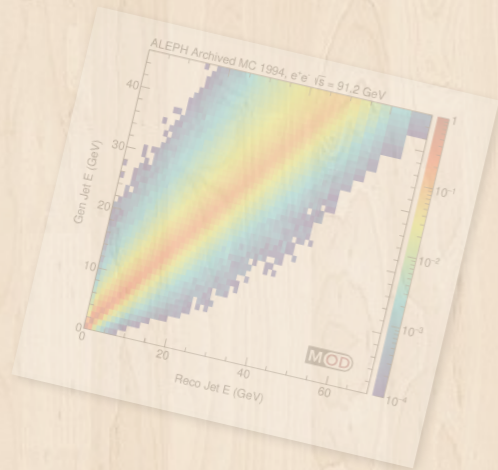


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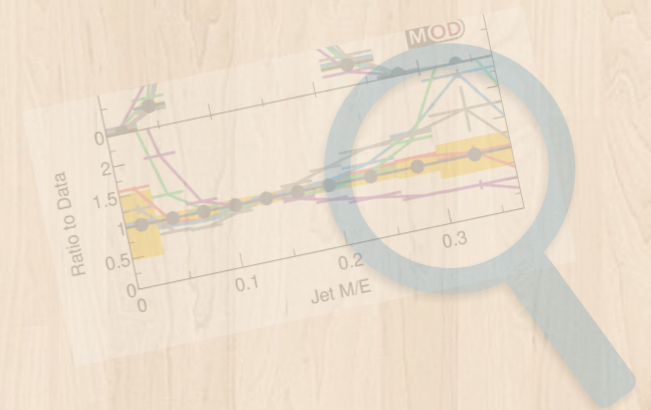
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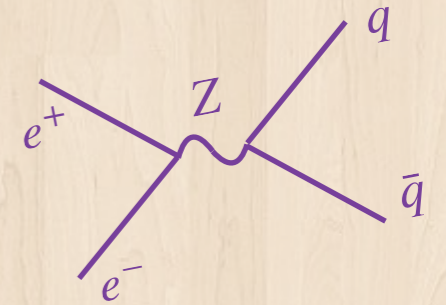
# Thank you!

- We would like to thank Roberto Tenchini and Guenther Dissertori from the ALEPH collaboration for the useful comments and suggestions on the use of ALEPH archived data
- We would like to thank Felix Ringer, Jesse Thaler, Andrew Larkoski, Liliana Apolinário, Ben Nachman, Camelia Mironov, Jing Wang for the useful discussions on the analysis

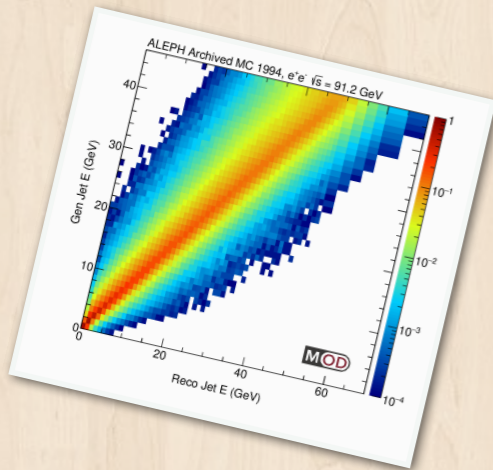


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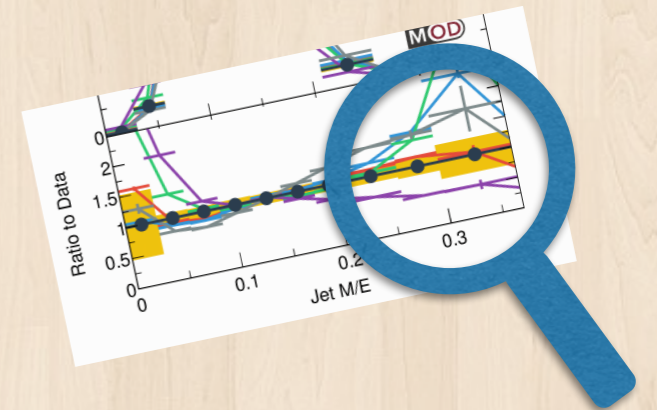
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Input for MC generators  
+ reference result



Numerous future possibilities



Backup Slides Ahead

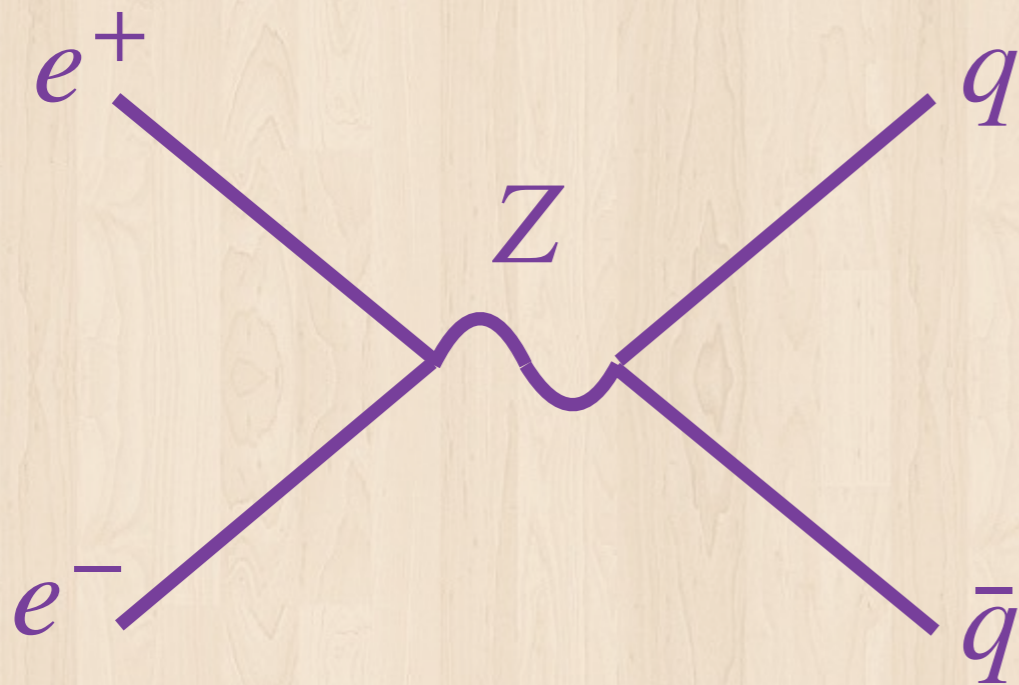




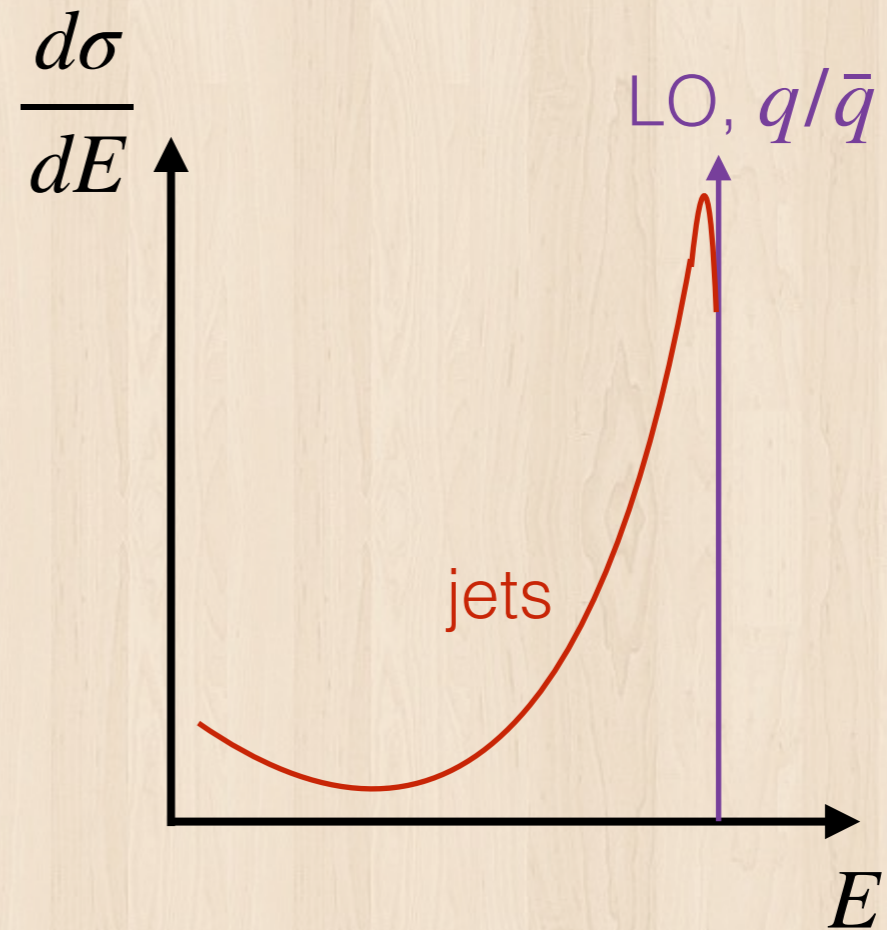


# Peaked structure

91.2 GeV collisions



Dominant jet diagram



Peaked structure is useful for studying jets

Out-of-cone energy => "energy loss"

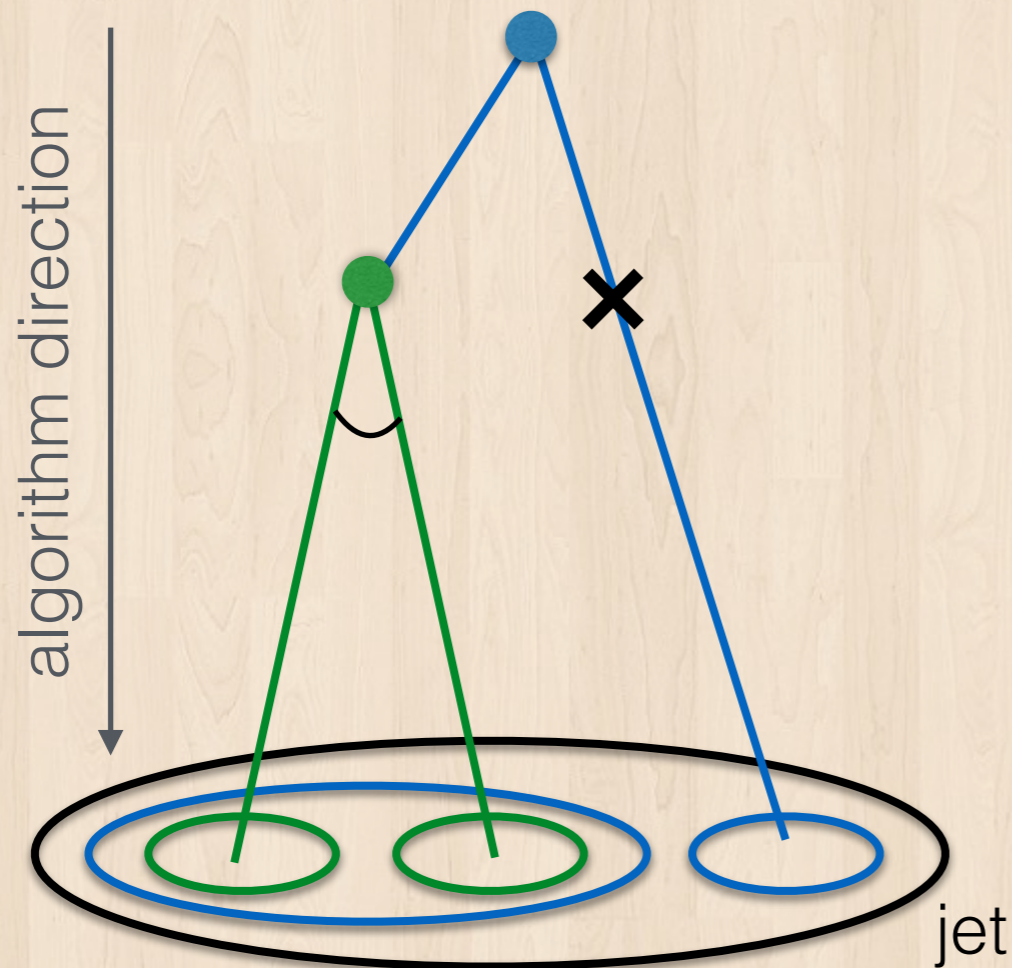


# Jet grooming

Soft drop/mMDT grooming

Recluster jet constituents with C/A algorithm

Sequentially open up jet until condition is met



$$(z_{\text{cut}}, \beta) = (0.1, 0.0)$$

$$z \equiv \frac{\min(E_1, E_2)}{E_1 + E_2} > z_{\text{cut}} \left( \frac{\theta_{12}}{R} \right)^\beta$$

*E* instead of  $p_T$                        $\theta_{12}$  = real angle

$r_g$  = opening angle

$z_g$  = momentum sharing

$M_g$  = invariant mass



# Jet calibration

$$\begin{array}{ccc} \text{Jet energy scale in data} & = & \text{Jet energy scale in simulation} \times \frac{\text{Jet energy scale in data}}{\text{Jet energy scale in simulation}} \\ \text{Inclusive} & & \text{Selection } O(1\%) \end{array}$$

“MC calibration”

“Residual”

Strategy: first go 99% of the way there with simulation  
Then data and MC difference in restricted phase spaces

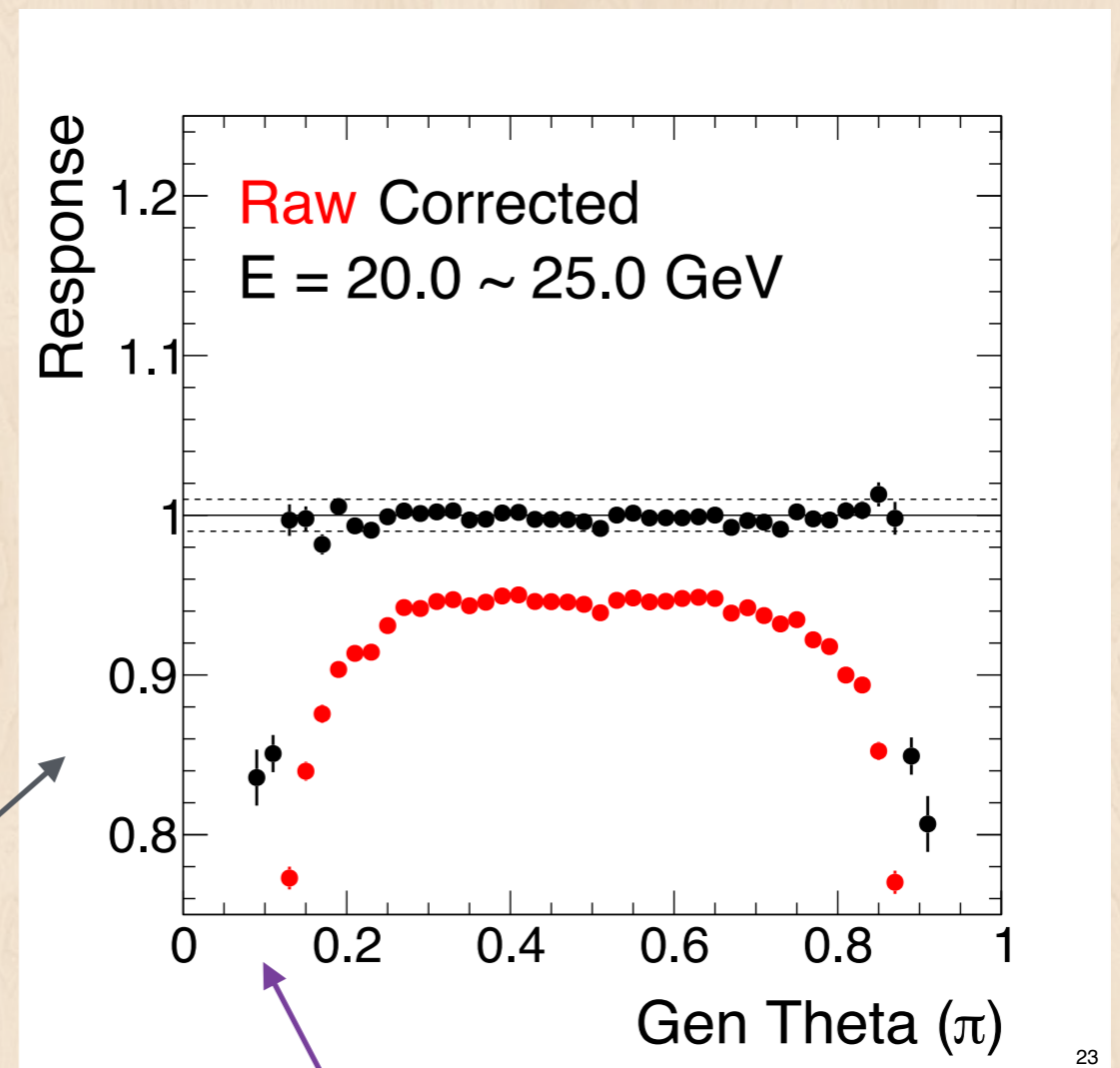


# Simulated energy scale

Correct detector jet energy  
in bins of jet direction ( $\theta_{\text{jet}}$ )

Good closure with  
 $E > 10 \text{ GeV}$   
 $0.2\pi < \theta_{\text{jet}} < 0.8\pi$

Example raw and  
corrected response  
(= reconstructed/generated)

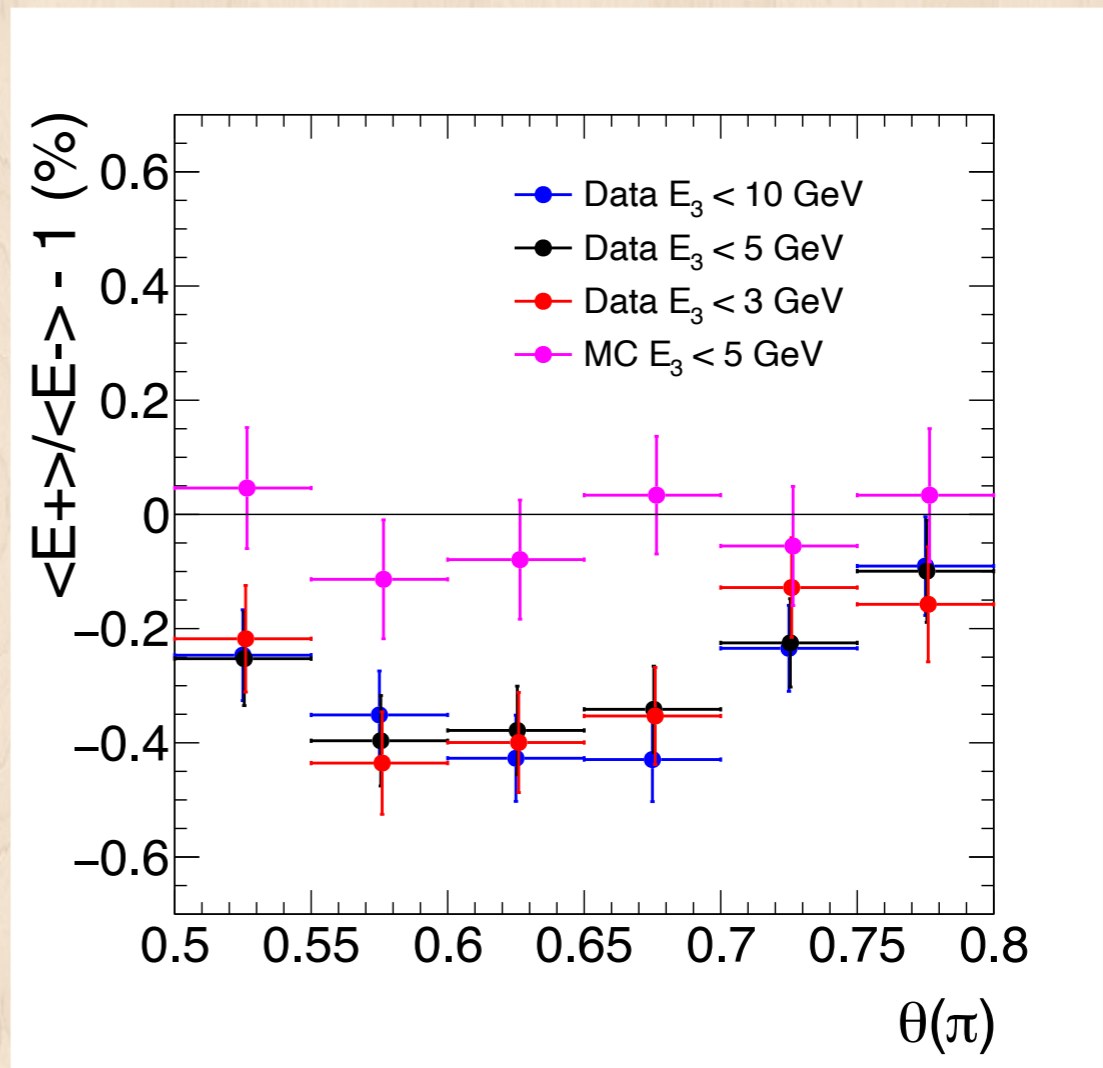
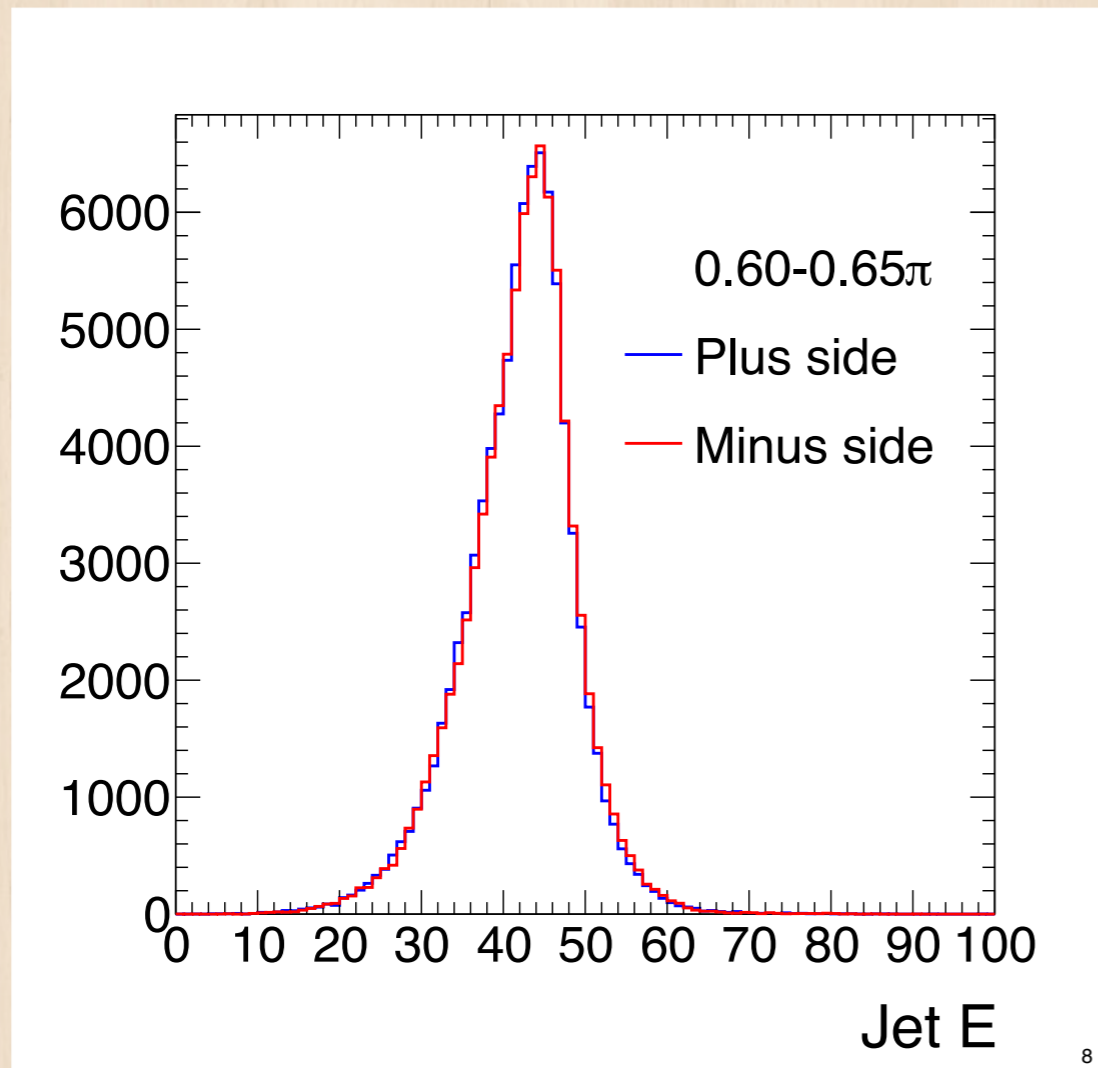


Energy leaking out  
around beam direction



# Residual calibration: step 1

Fiducial dijet, two sides of the detector

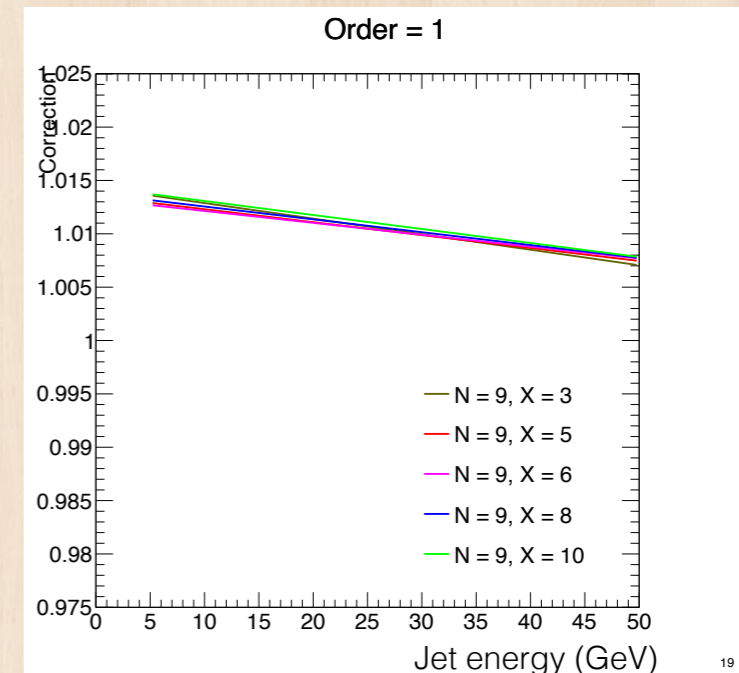
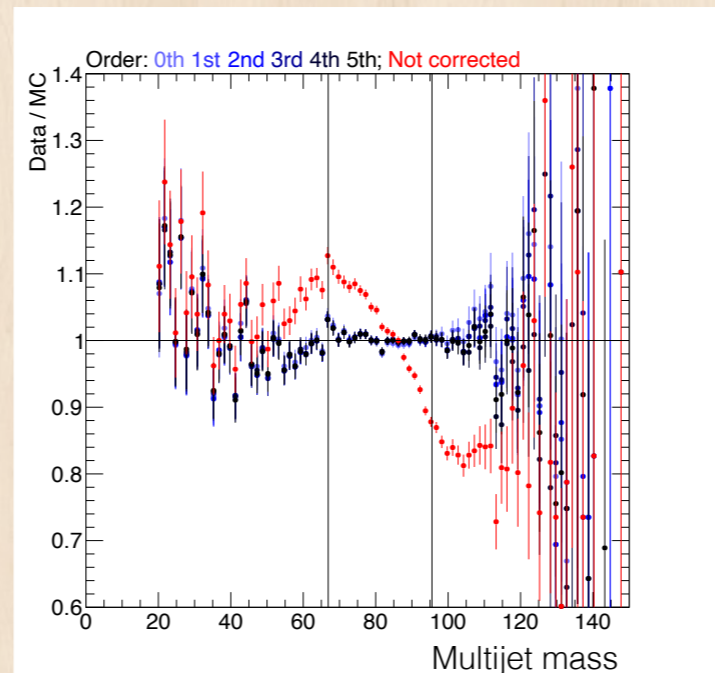
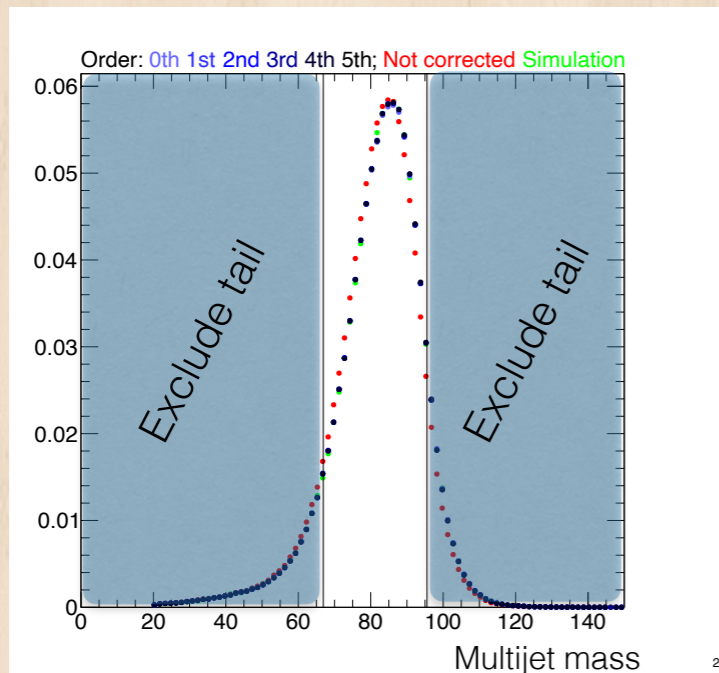


Look at data only, and calibrate out the difference between  $e^{-}$ - and  $e^{+}$ -going sides



# Residual calibration: step 2

Fiducial multijet invariant mass



Take up to leading N jet above X GeV

Vary N and X for systematics

Fit jet energy correction function parameters

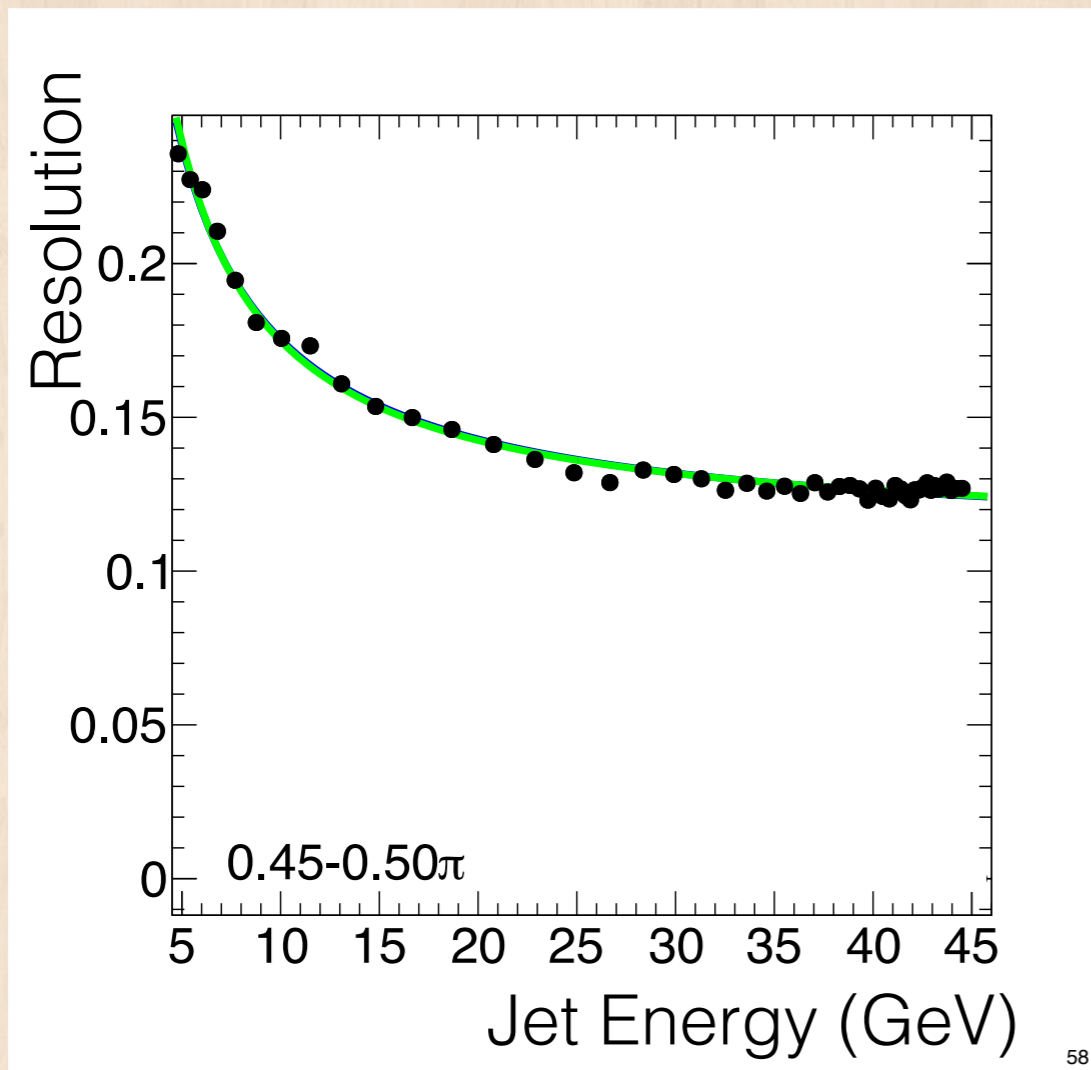
Minimize “quantile difference” ( $\sim$ KS) between data and MC curves

Nominal: linear correction as a function of energy



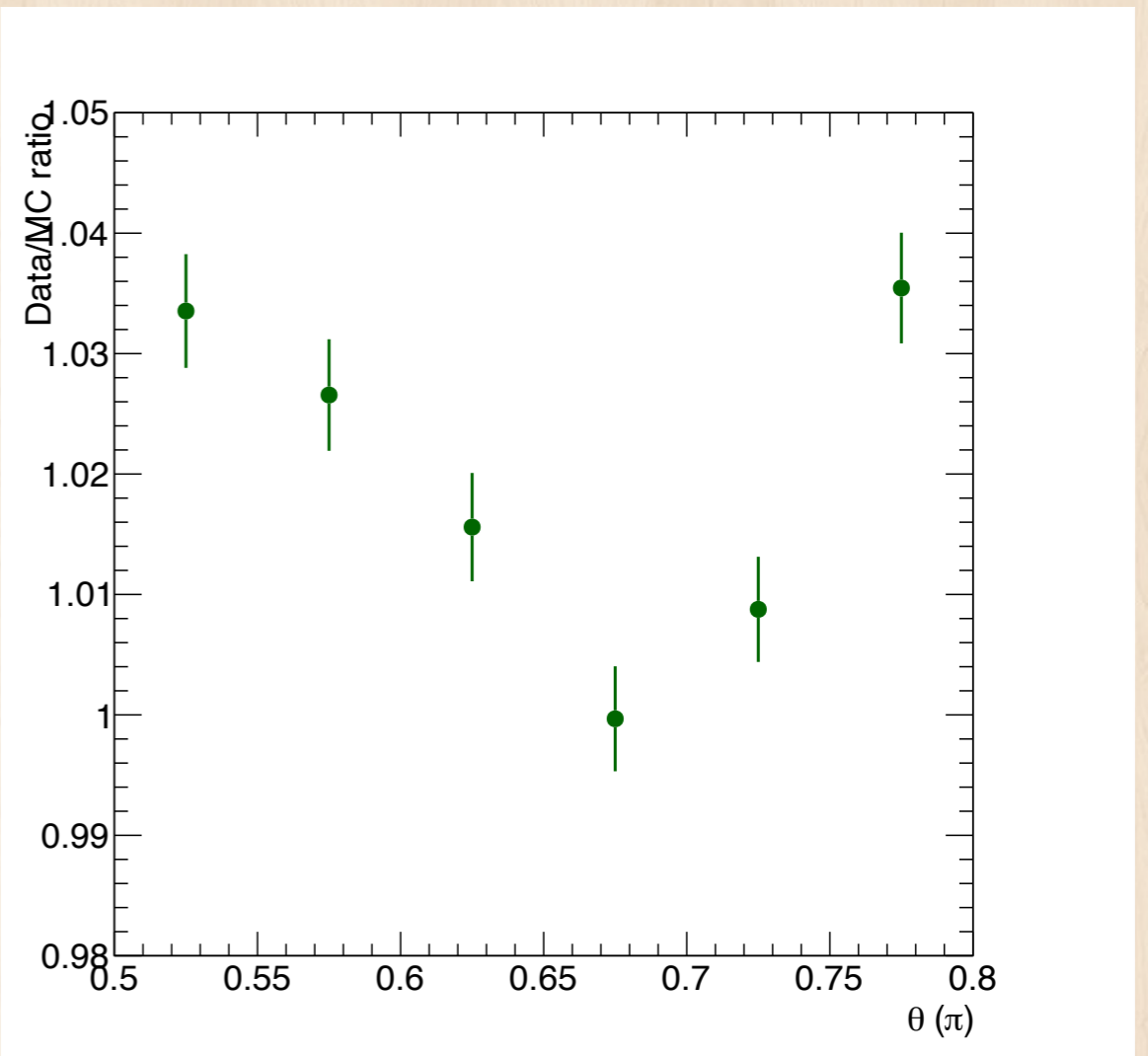
# Jet resolution

Jet resolution in simulation



Energy resolution: 10-25%  
(Angular resolution: 0.01-0.05)

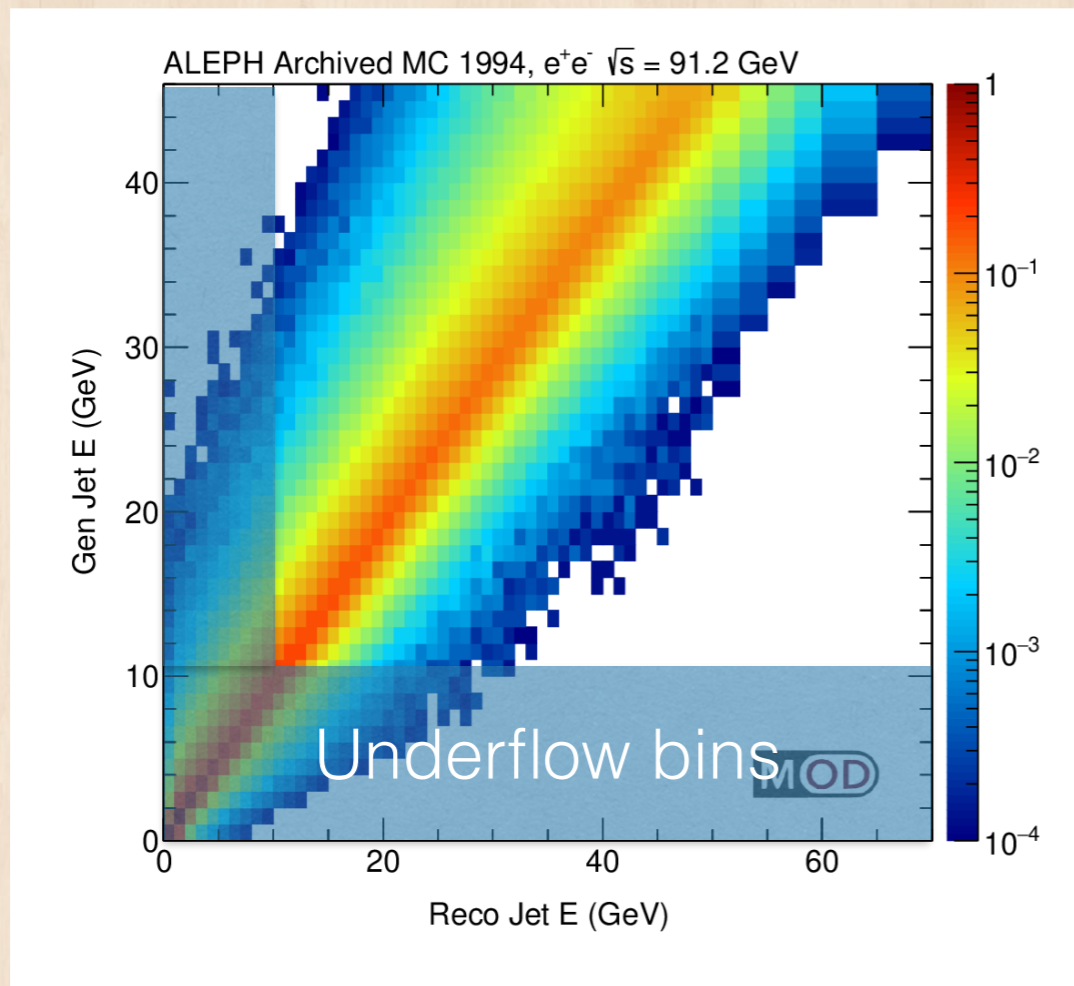
$\frac{\text{Data resolution}}{\text{MC resolution}}$



0-5% difference in energy  
resolution between data and MC



# Unfolding



Example: inclusive jet energy

Unfolding performed using the **BayesUnfold** method implemented in **RooUnfold** package

SVD unfold as systematic check

Flat prior as nominal

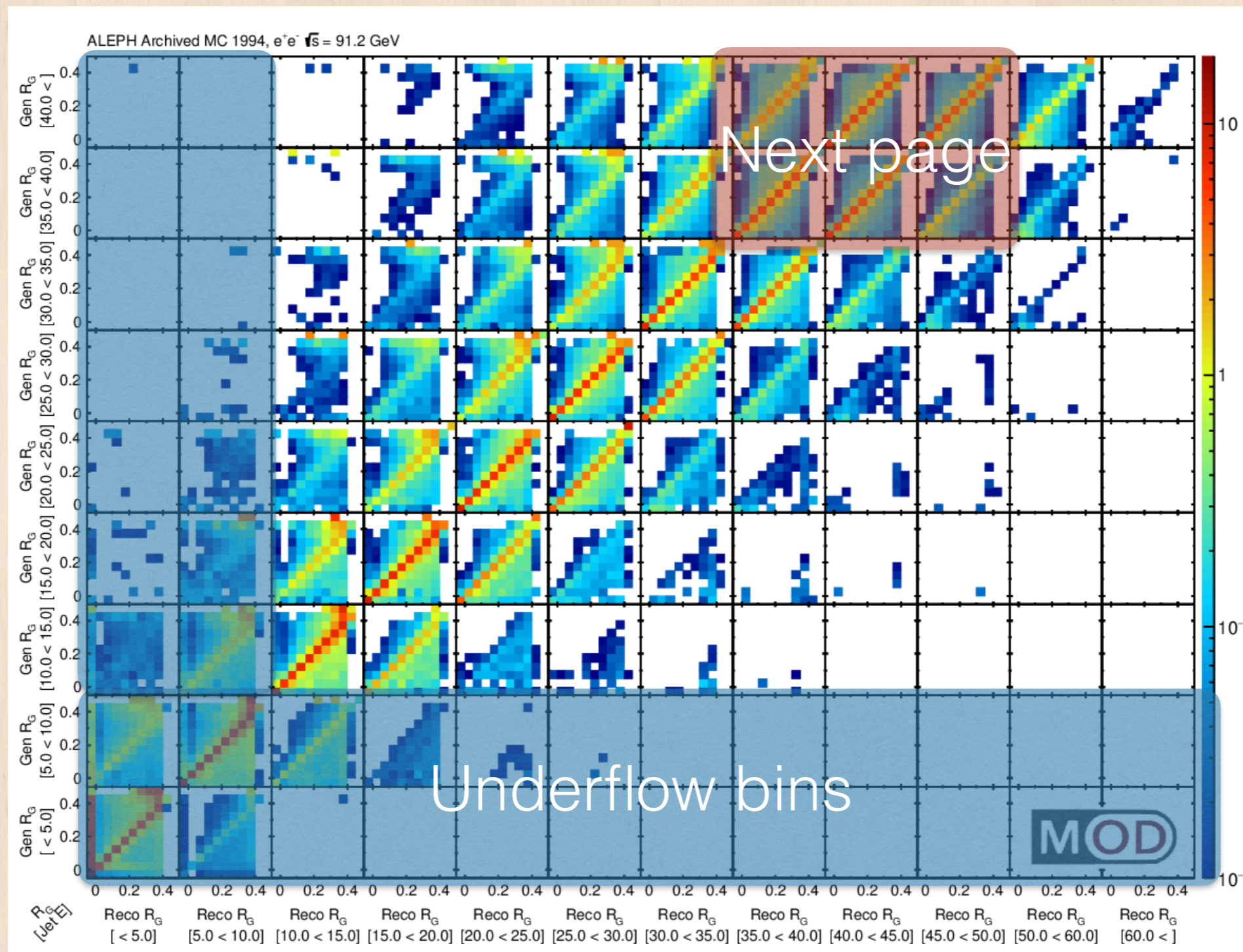
MC prior as systematic check

2D unfold for mass & groomed quantities

Due to energy migration



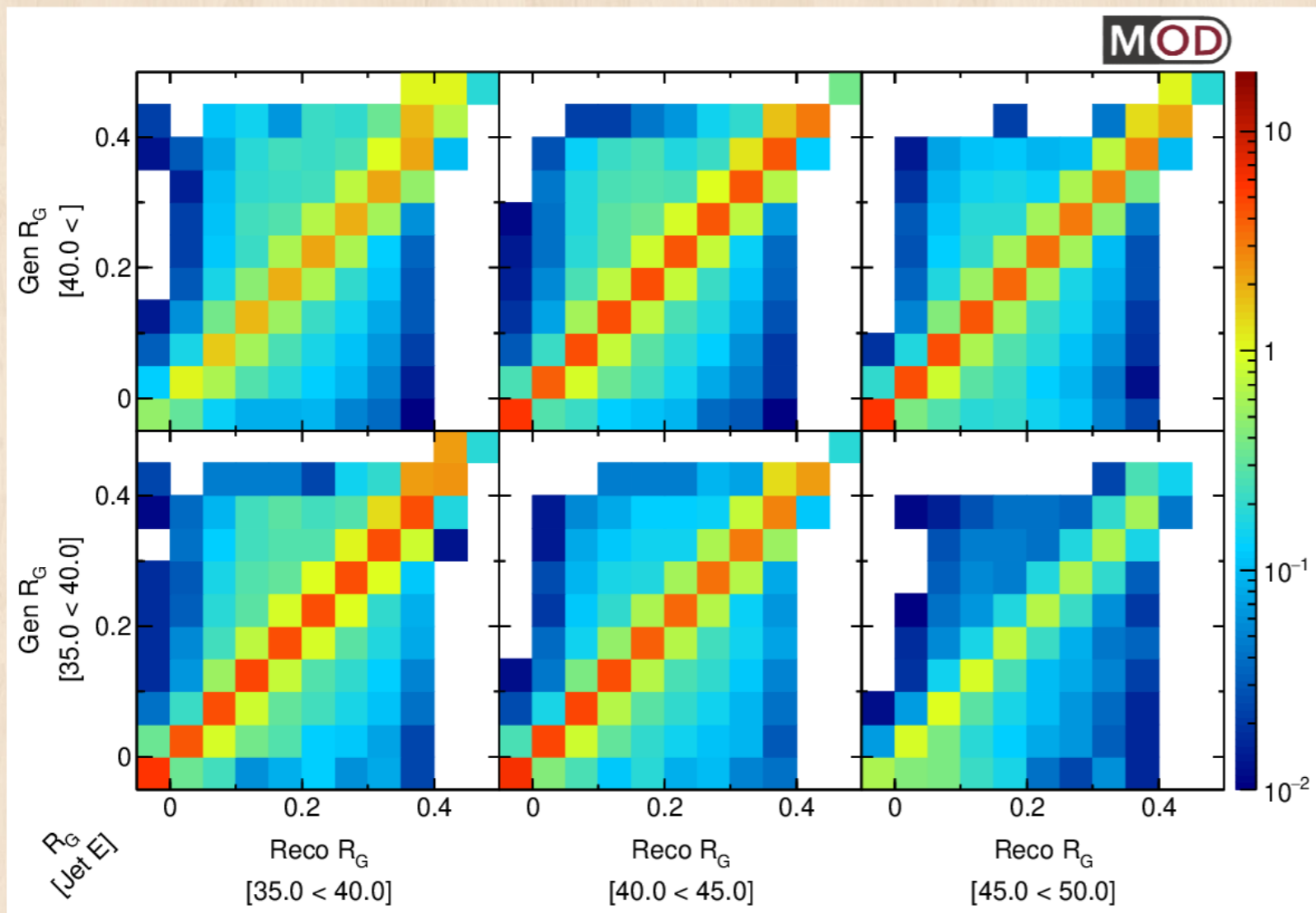
# 2D smearing matrix





# 2D smearing matrix

## Partial smearing matrix



Each block:  
different jet E

Generally  
well-behaved

Percent-level  
off-diagonal

Example: jet  $R_G$



# Leading dijet selection

Solution: require minimal total visible energy

Total visible energy = total energy of...

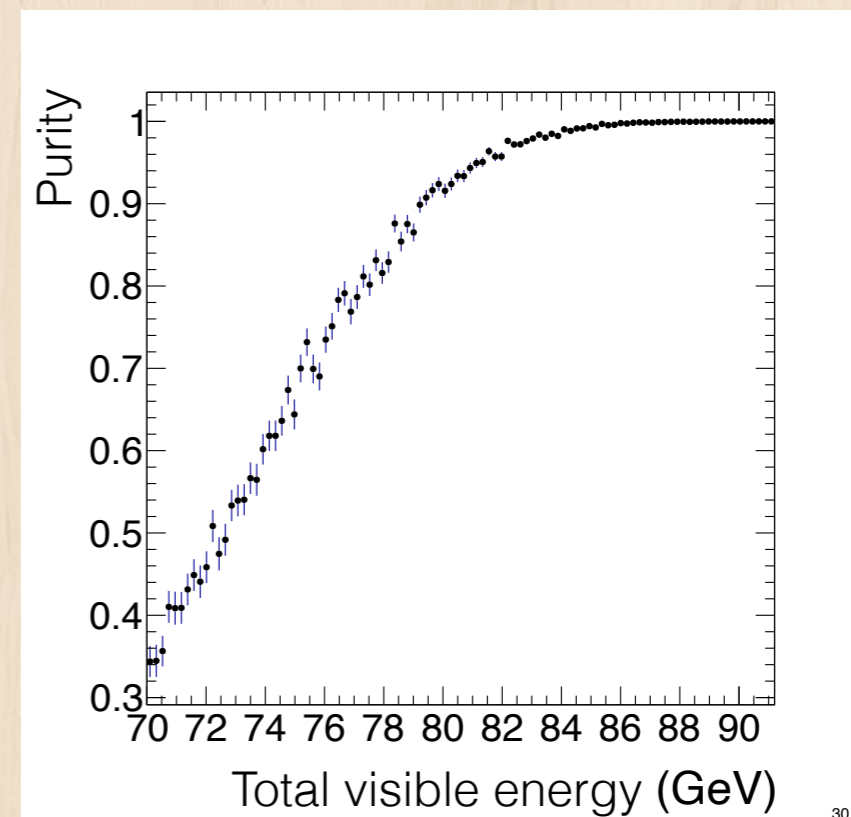
{Particles inside acceptance}  $\cup$

{Particles close to a jet with 5 GeV in acceptance}

Nominal working point: 99%

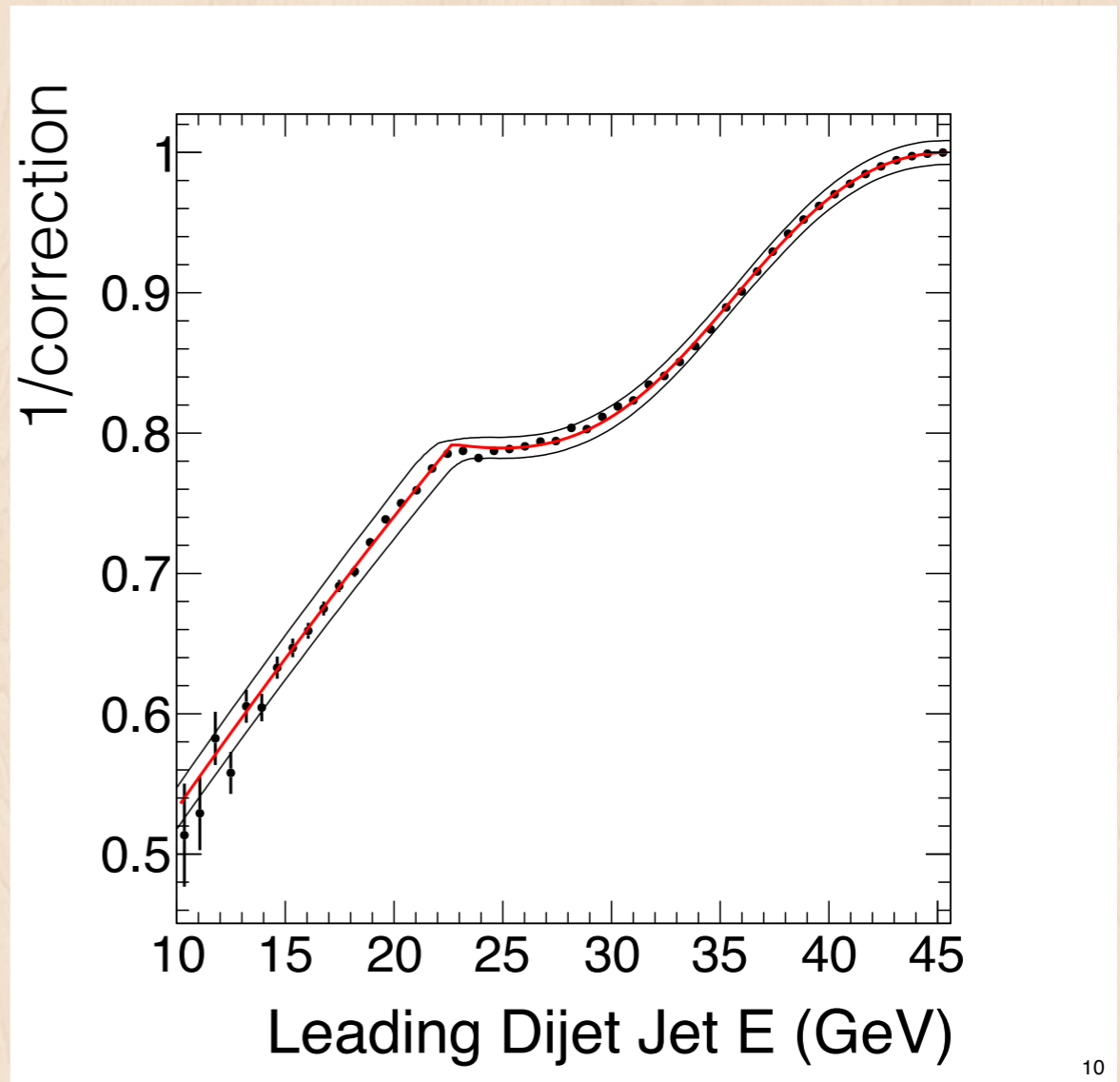
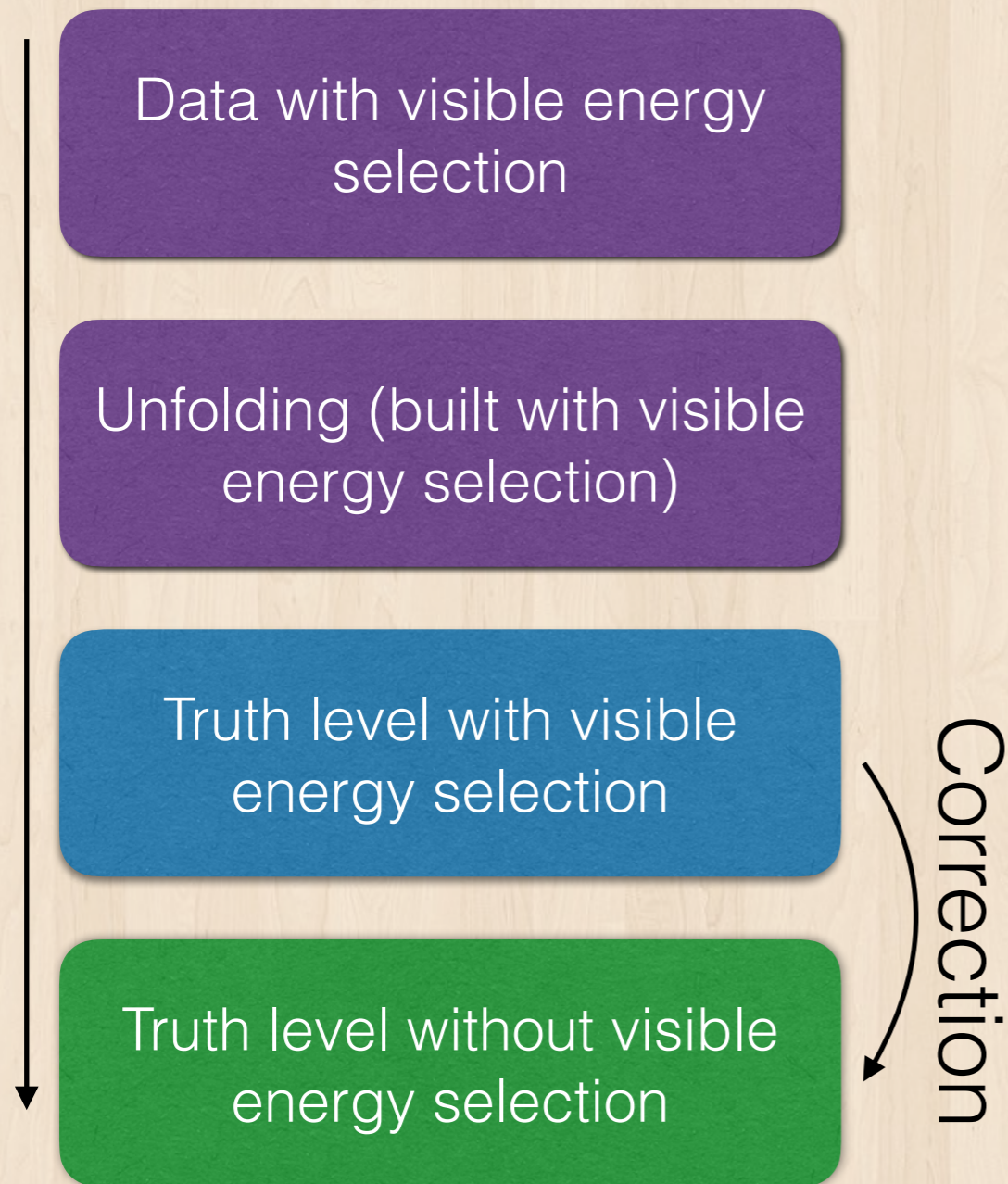
ie., >99% of events have global leading dijet within acceptance

Apply correction on measured spectra





# Leading dijet correction



Correction derived from simulation



# Leading dijet energy

Focus on the peak  
part of the spectrum

Most generators can  
describe data within  
(large-ish) uncertainty

Uncertainty  
dominated by  
modeling uncertainty

