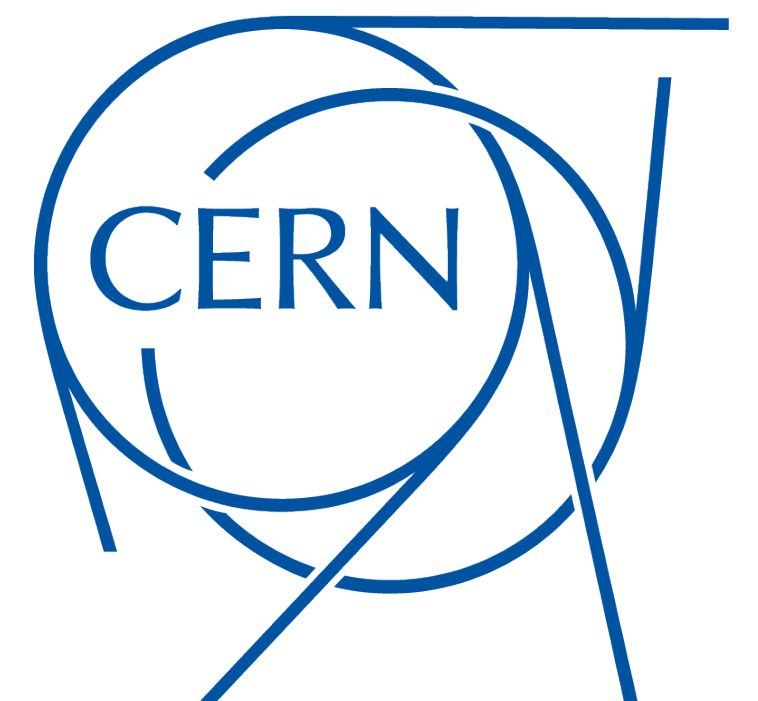




# Going off topics to demix quarks and gluons in $\alpha_s$ extractions

[arXiv:2206.10642](https://arxiv.org/abs/2206.10642) [hep-ph]

[M. LeBlanc \(CERN\)](#), [B. Nachman \(LBNL\)](#), [C. Sauer \(Heidelberg\)](#)

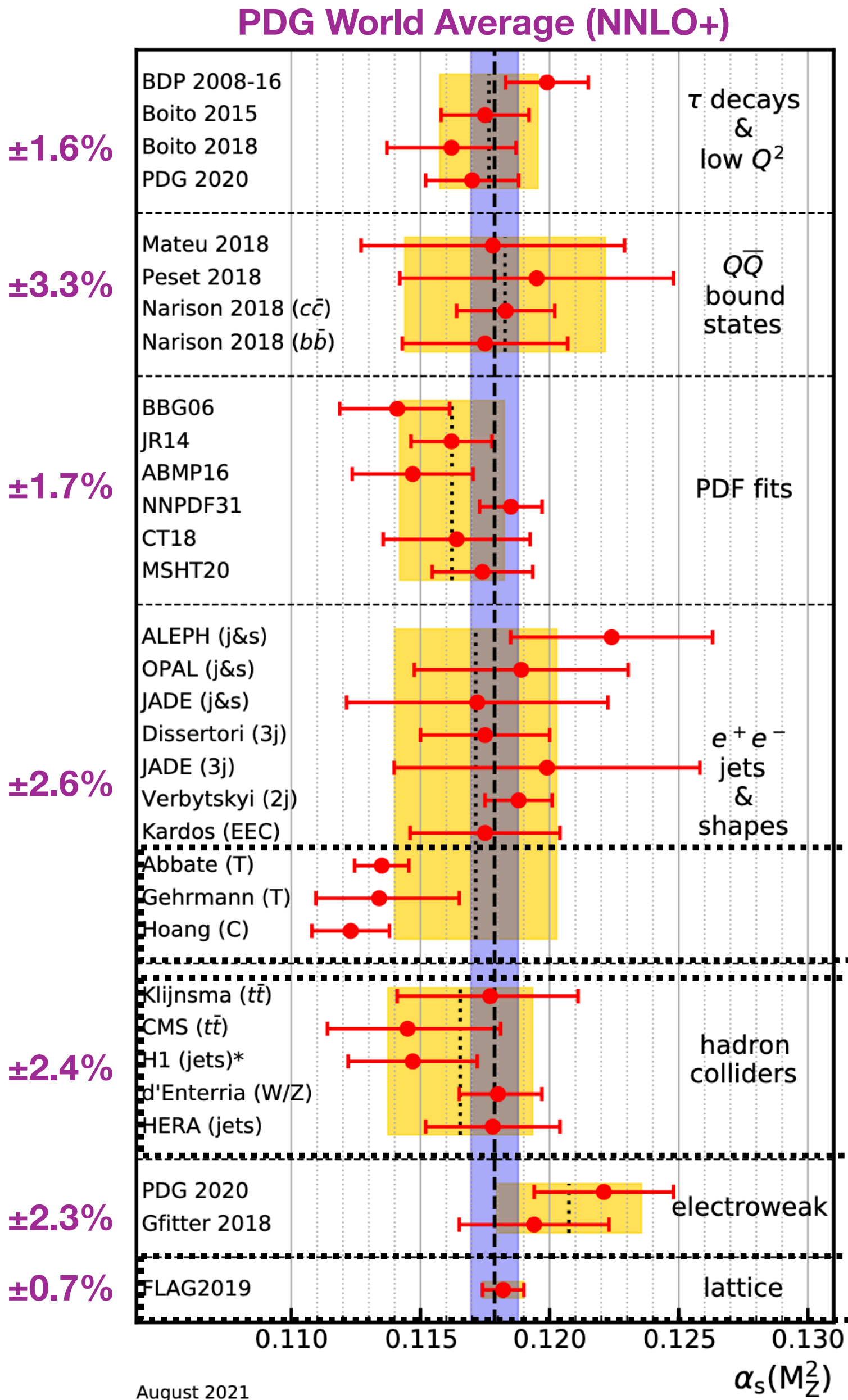
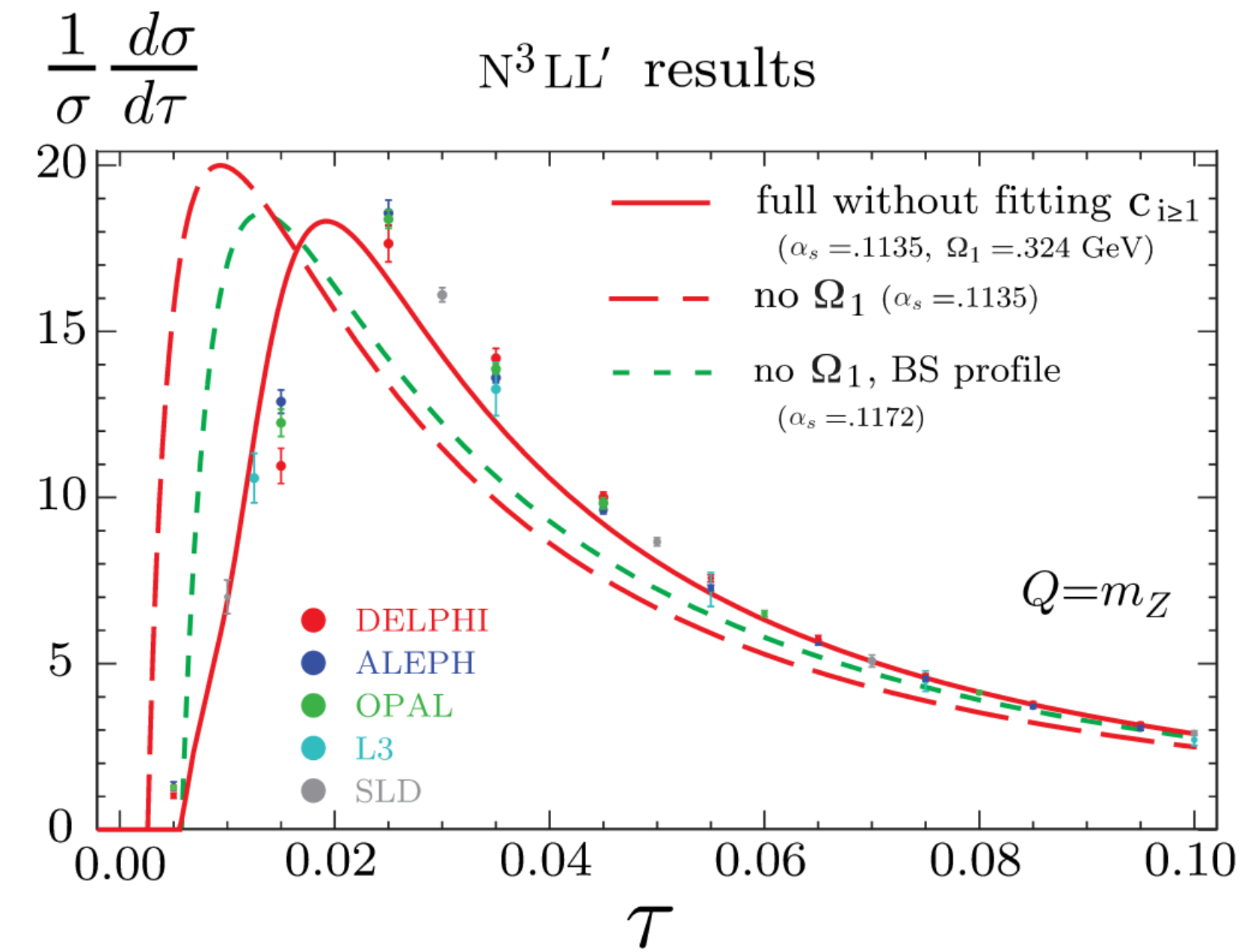


# Strong coupling

The QCD coupling,  $\alpha_s$ , is known with far less precision than the couplings of other gauge field theories.

$$\delta\alpha \sim 10^{-10} \ll \delta G_F \sim 10^{-7} \ll \delta G \sim 10^{-5} \ll \delta\alpha_s \sim 10^{-3}$$

This uncertainty is driven by tensions within the  $\alpha_s$  world average, and it is becoming increasingly relevant in predictions related to Higgs & top production, EWPOs, etc.



Most precise collider extractions (LEP) in tension with other results...

No LHC extraction from jet cross sections at NNLO+!

Lattice average very precise

$\alpha_s(M_Z) = 0.1135 \pm 0.0010$  ( $e^+e^-$  thrust)

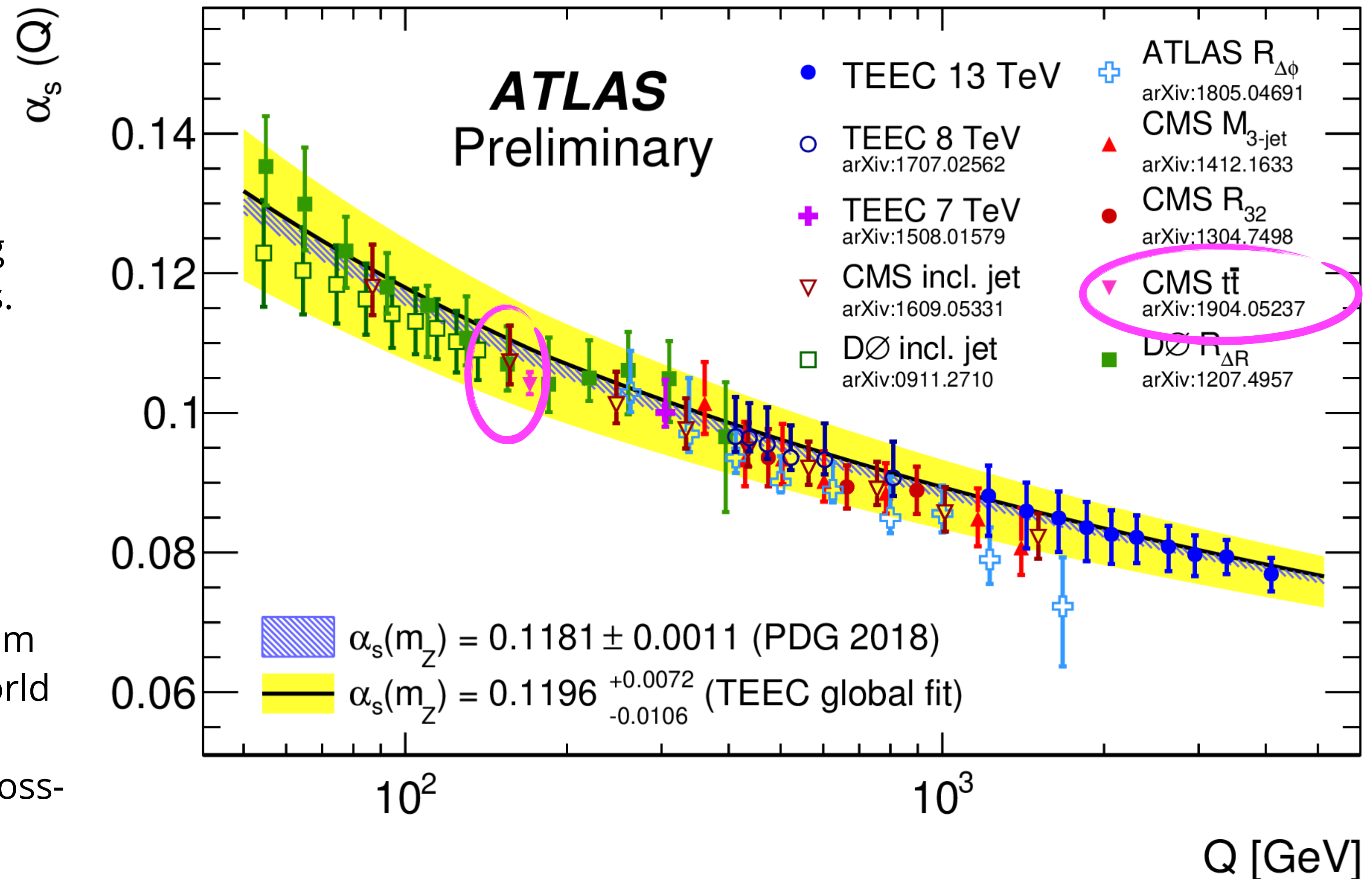
vs.

$\alpha_s(M_Z) = 0.1182 \pm 0.0008$  (lattice)

**Tension > 3 $\sigma$**

# $\alpha_s$ extractions from jets at the LHC

- Sensitivity to strong coupling at colliders from the **jet multiplicity** and **the jet rate** when performing extractions from jet cross-sections.
  - NNLO theory for 3-jet cross-section has only recently been computed at leading colour (Czakon *et al.* [2106.05331](#))
- The only test of asymptotic freedom at the LHC that enters the PDG world average so-far is the **single point** from CMS's top pair production cross-section measurement, at  $Q=m_t$





# How can we perform an extraction like the LEP thrust one at the LHC?

## LEP EXTRACTIONS

$e^+e^-$



Thrust extraction sensitive in resummation-dominated region

## LHC EXTRACTIONS

Underlying event / colour reconnection



Jet rate or cross-section ratio usually compared to fixed-order calculations



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## LHC EXTRACTIONS FROM JSS

soft-drop grooming  
→ mitigate soft/wide-angled contributions





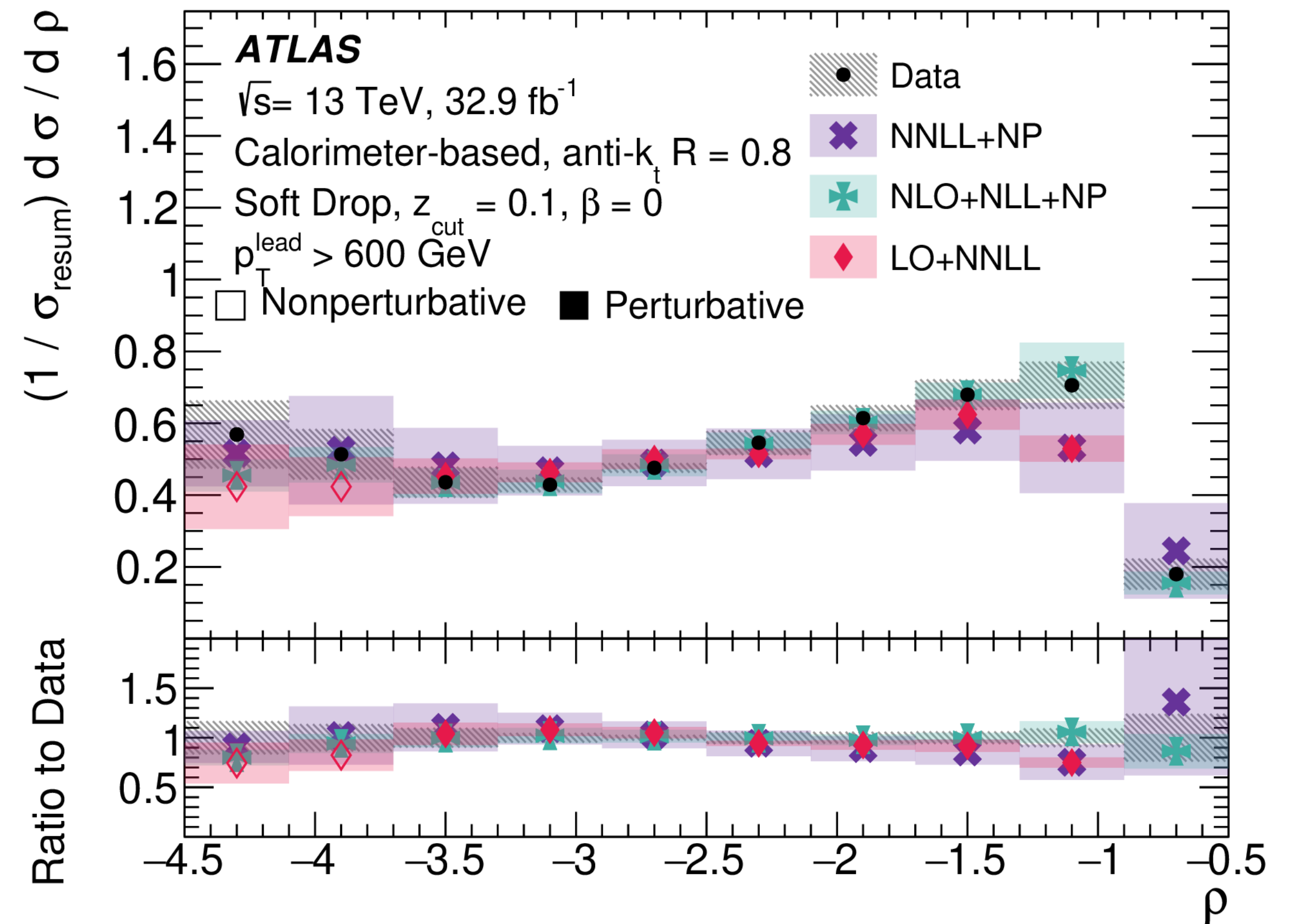
Soft-drop mass prediction  
→ precise resummation



# Soft-drop jet mass

## ATLAS, CMS references

- The soft-drop jet mass has been measured during Run 2 and compared to >LL theory.
  - Great experimental and theoretical precision in the resummation-dominated region of the observable.
- Leading behaviour:  $m_{SD} \sim C_i \alpha_S$ .
  -  Sensitive to the strong coupling.
  -  Also sensitive to the  $q/g$  colour factor  $C_i$ .

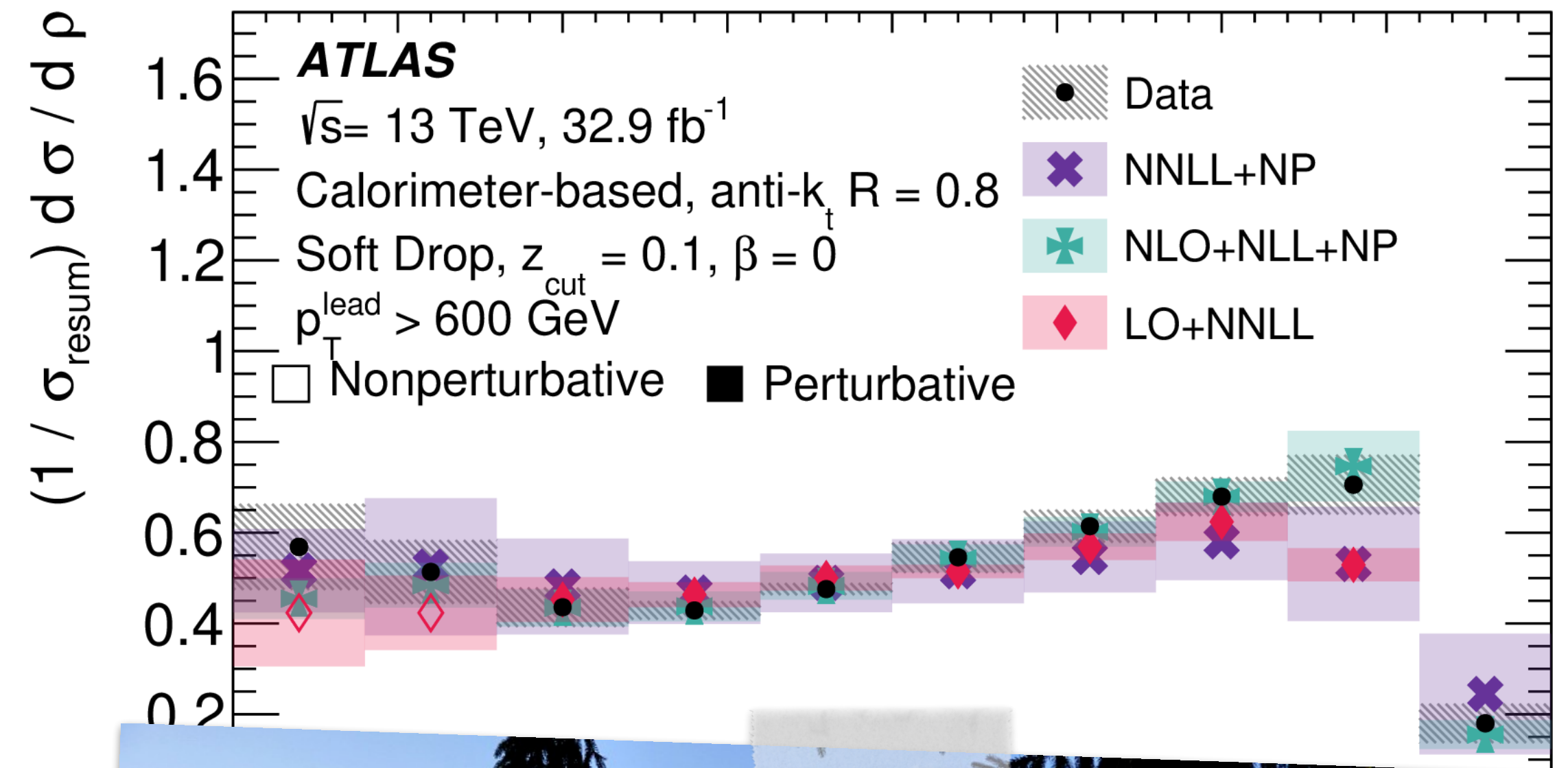




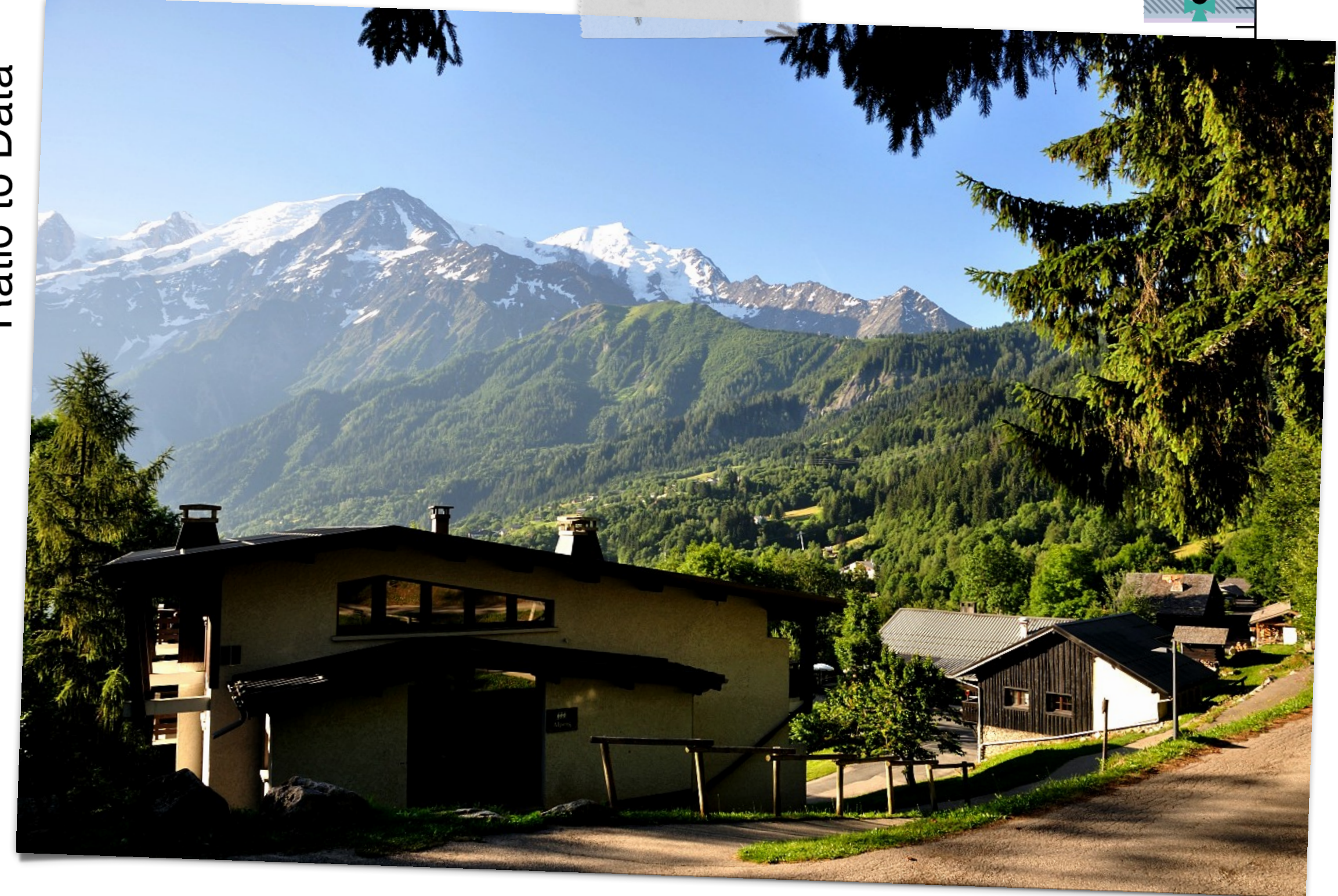
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- Sensitive to the strong coupling.
- Also sensitive to the  $q/g$  colour factor  $C_i$ .
- Detailed prospective study for  $\alpha_s$  extractions performed at Les Houches in 2017 ([1803.07977](https://arxiv.org/abs/1803.07977)).



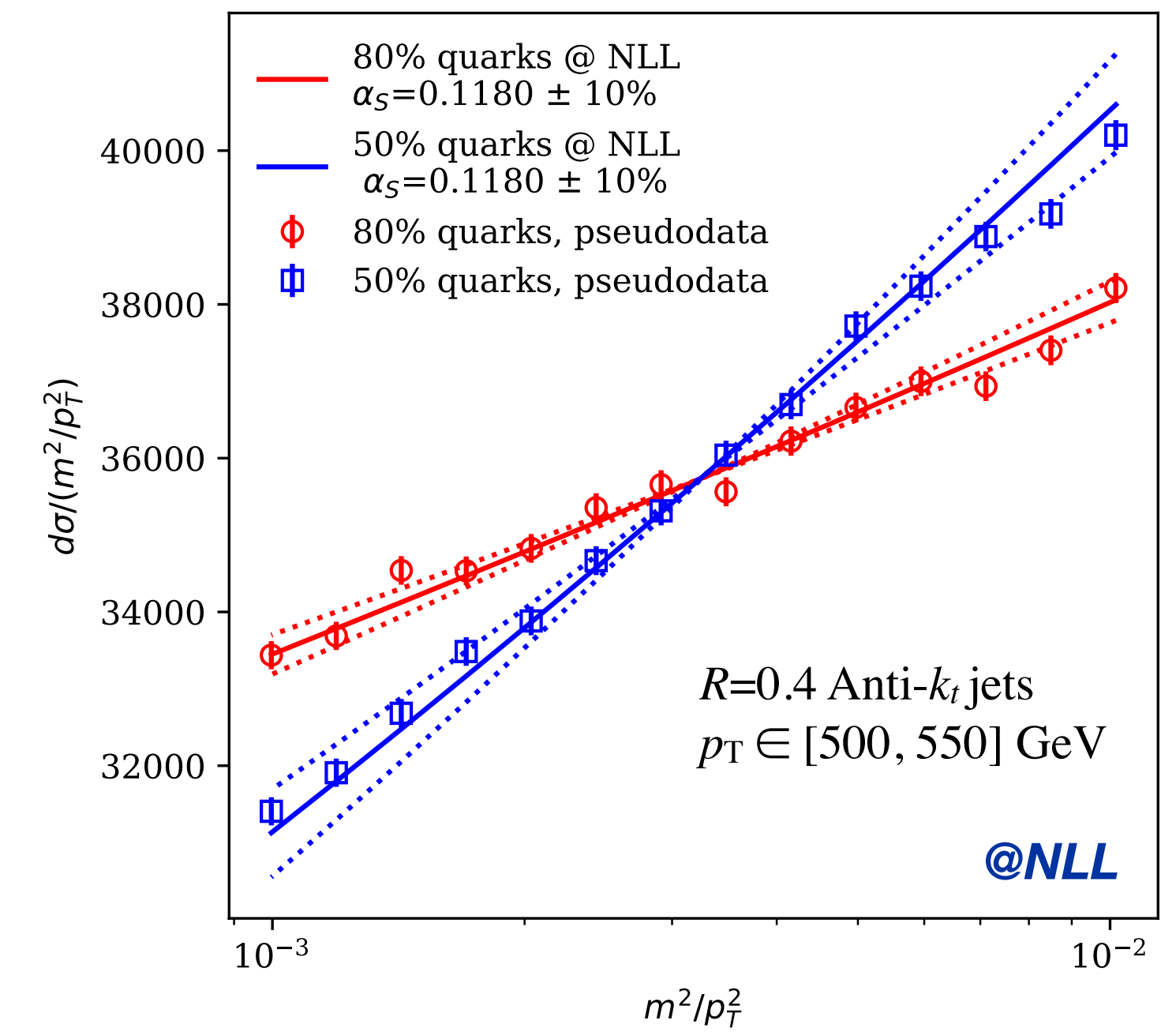
Ratio to Data





# Repeating the LH17 Fit

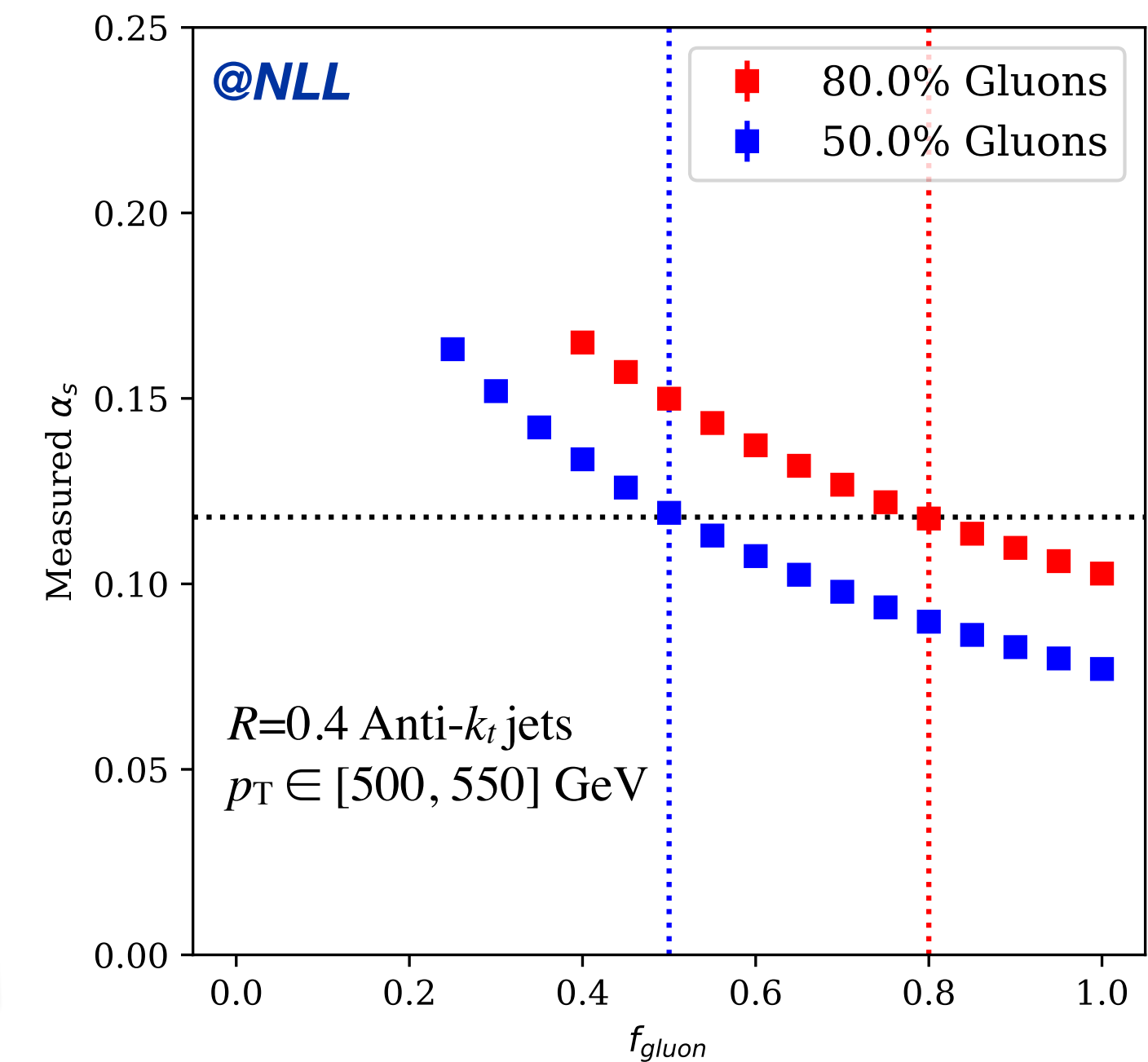
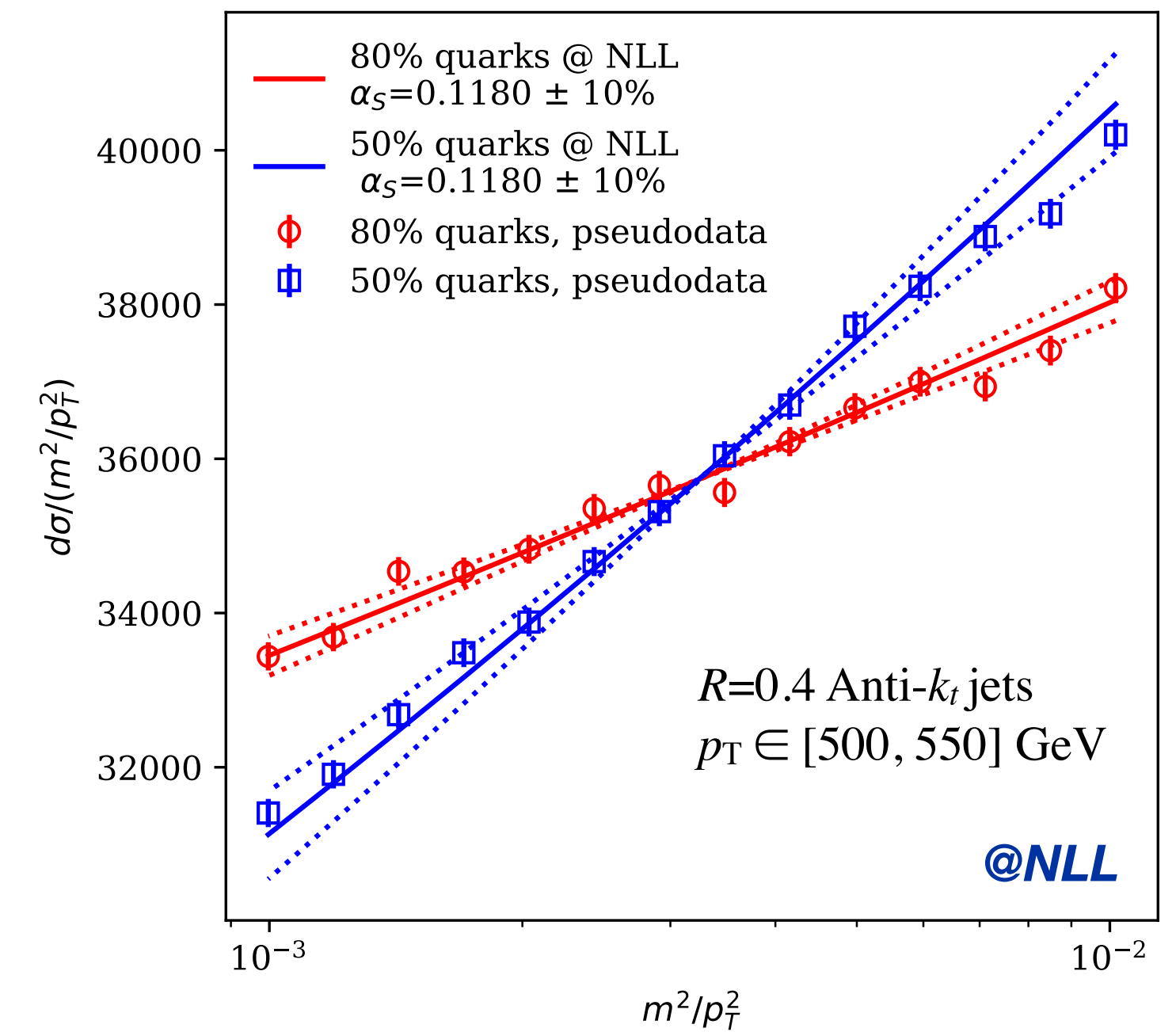
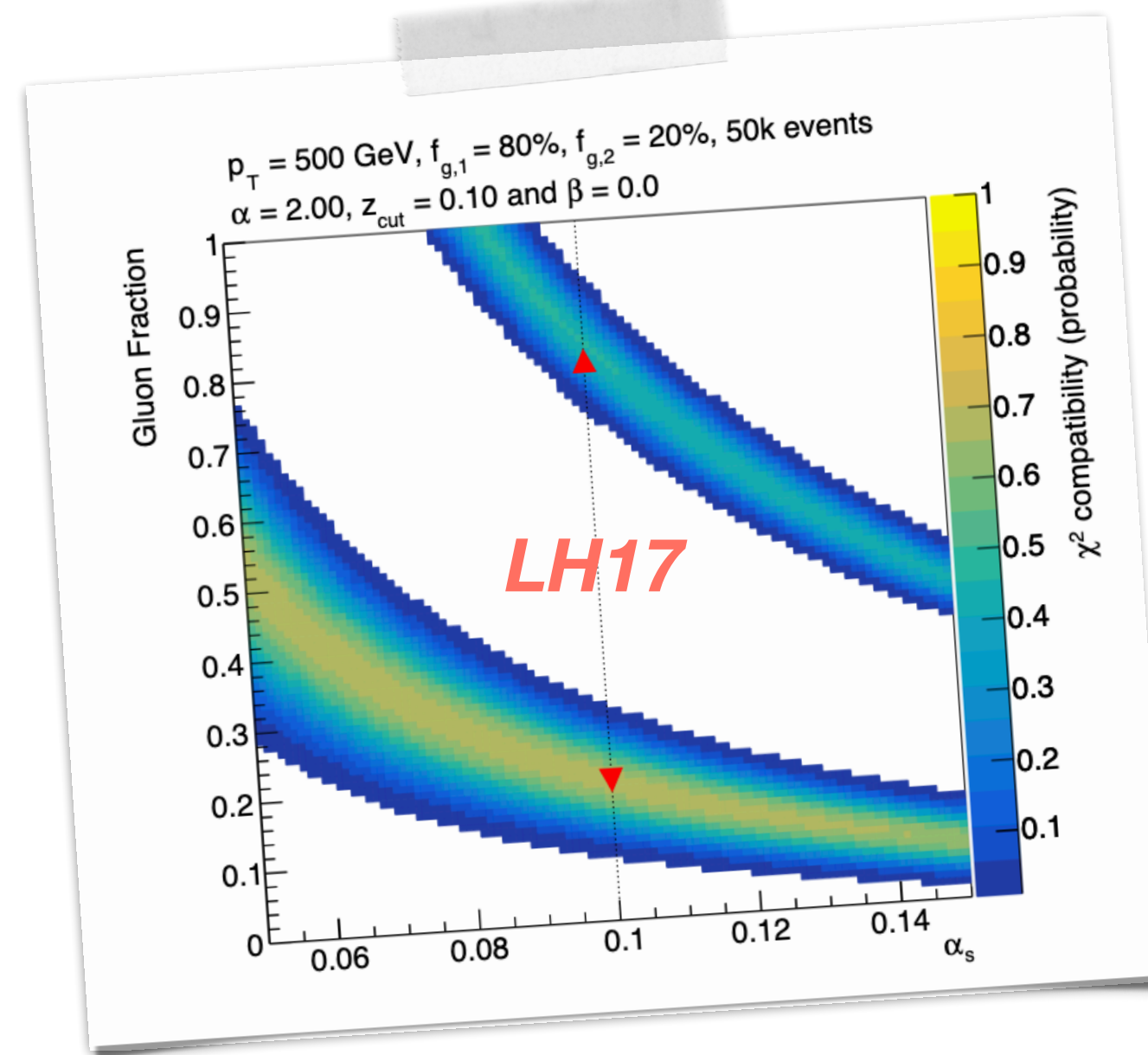
- Generate **pseudodata** from NLL prediction for quark- & gluon-initiated jets.





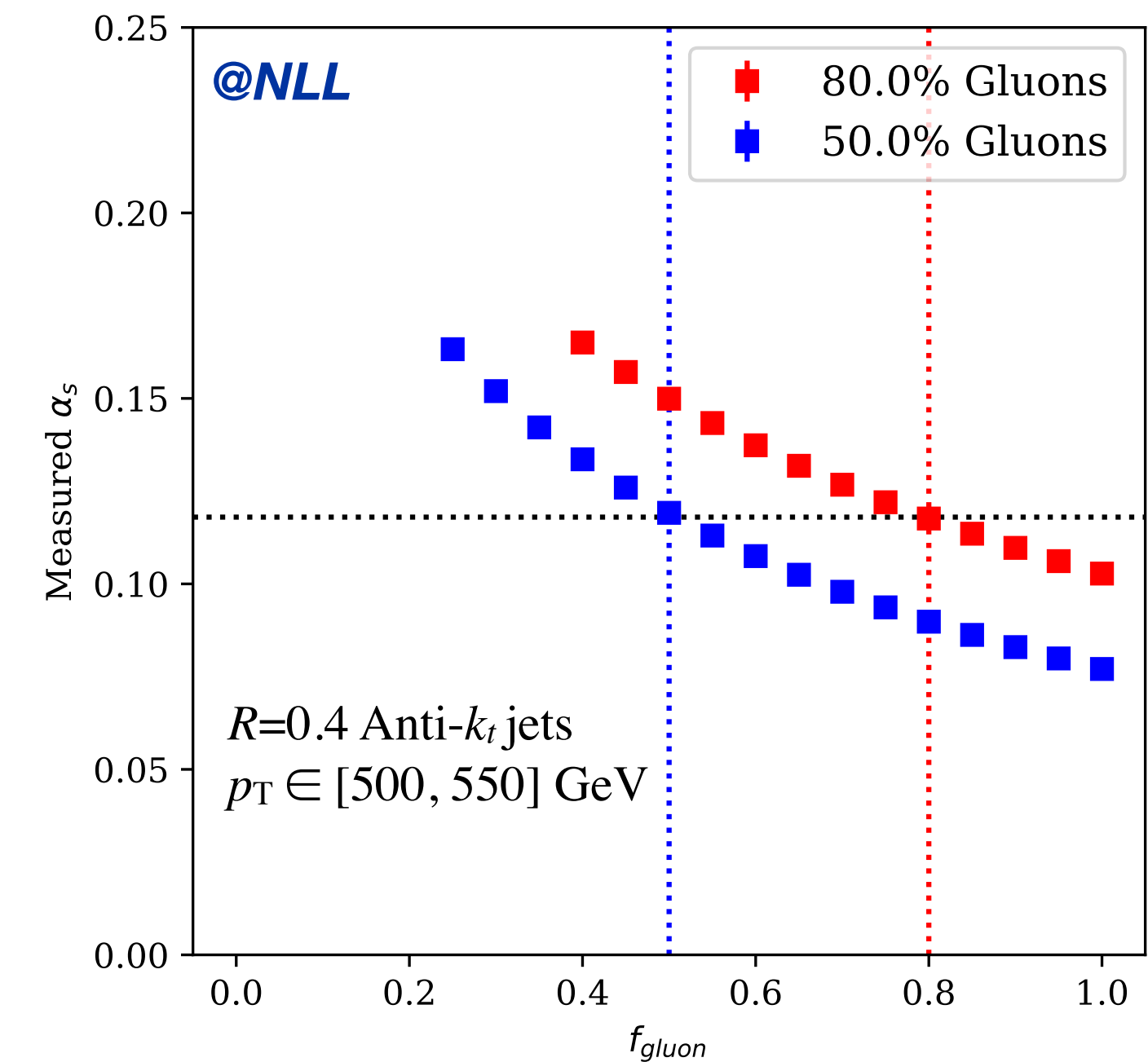
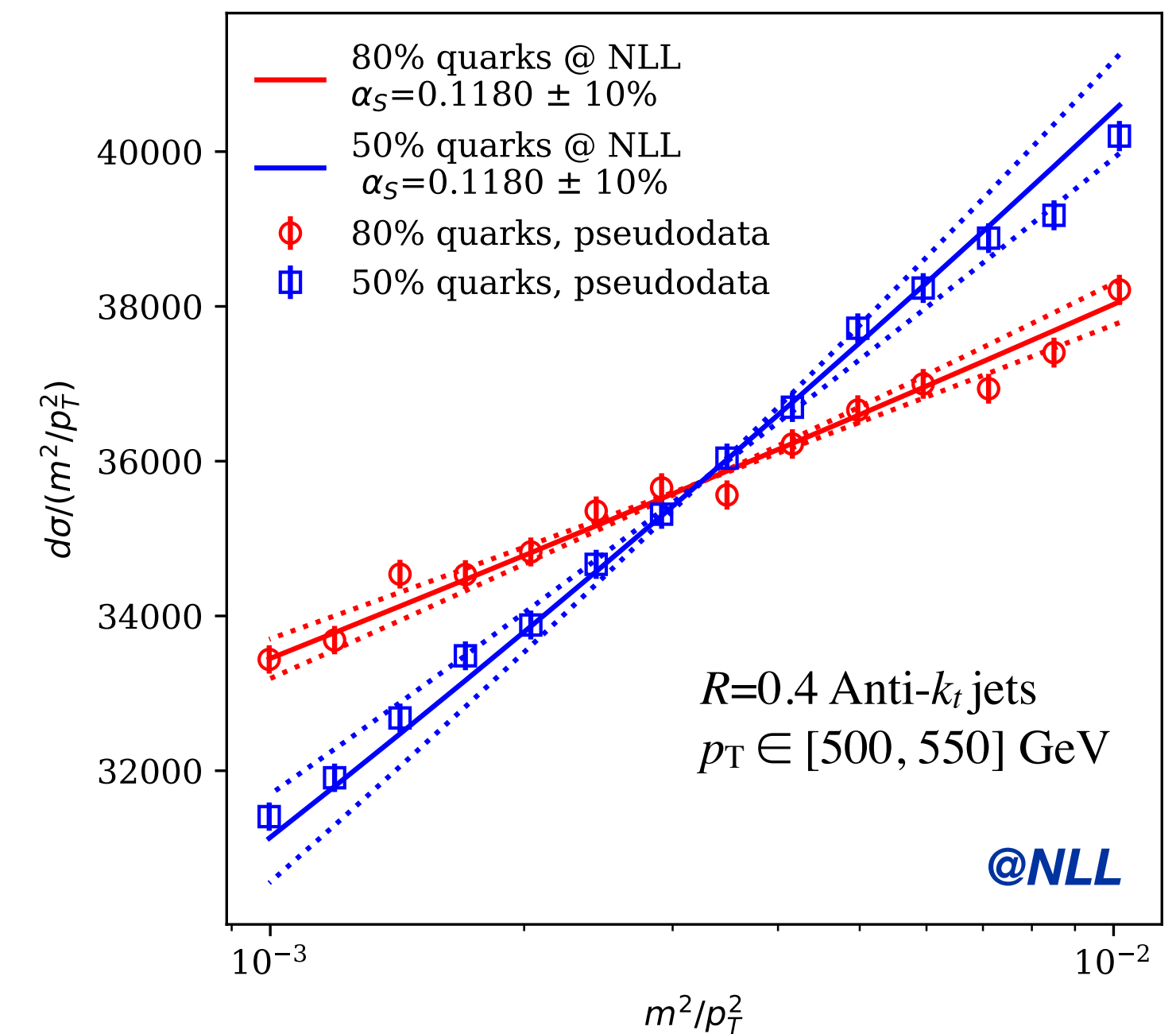
# Repeating the LH17 Fit

- Generate **pseudodata** from NLL prediction for quark- & gluon-initiated jets.
- Characteristic curve demonstrates degeneracy between  $f_{\text{gluon}}$  and  $\alpha_s$ .
  - Obtained by **altering the value of  $f_{\text{gluon}}$  in the fit for a given mixed sample and extracting  $\alpha_s$ .**



# Repeating the LH17 Fit

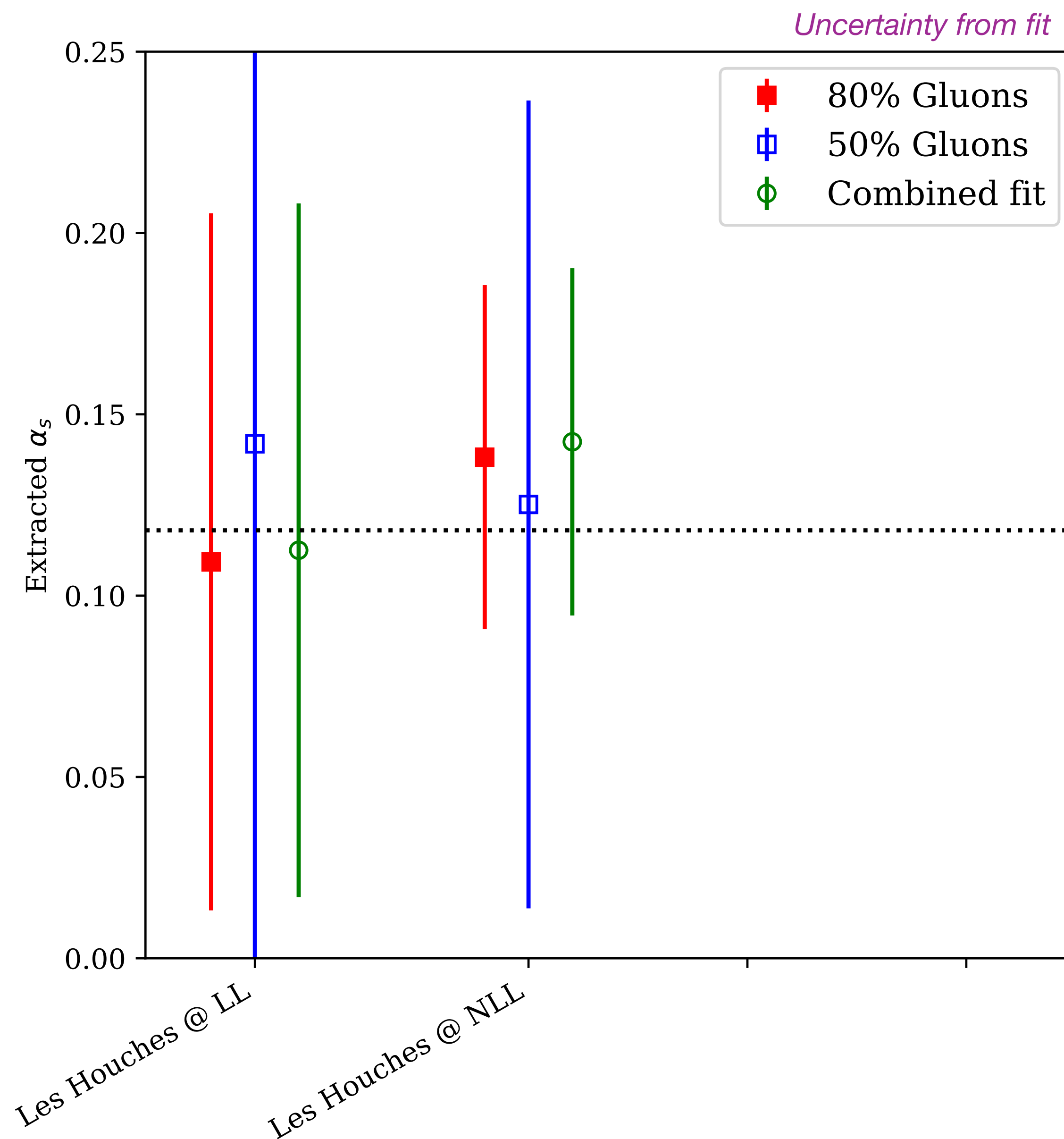
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  - Obtained by **altering the value of  $f_{\text{gluon}}$  in the fit for a given mixed sample and extracting  $\alpha_s$ .**
- Could break this degeneracy in a couple of ways:
  - Theoretical calculation of  $f_{\text{gluon}} \rightarrow$  sensitive to PDFs, **could fit PDFs at the same time** (more complex). X ?
  - Could **fit multiple higher-order correlators** simultaneously (degeneracy breaks beyond NLL).
    - *Requires simultaneous theoretical prediction of multiple JSS observables at very high precision ...* X





# Results: LH17 Approach

- When left unconstrained, this degeneracy results in large instabilities / uncertainties in the extracted  $\alpha_s$  value.
- Can fit both mixed samples at once to improve slightly, but errors still on the order of  $\sim 35\%$ .
- The LH Jets Working Group became a bit pessimistic ...



*“Without some kind of conceptual breakthrough, though, we expect that the quark/gluon fraction will be a limiting aspect of  $\alpha_s$  extractions from jet substructure at the LHC.”*

*— Les Houches Jets Working Group, [arXiv:1803.07977](https://arxiv.org/abs/1803.07977) [hep-ph]*



# How do we break this degeneracy?

Simultaneously fit  $\alpha_s$  and the  $q/g$  fractions —  
fractions —  
*explored in LH17*



Calculate the  $q/g$  fractions —  
*depends on PDFs*



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Calculate the  $q/g$  fractions —  
*depends on PDFs*



Demix underlying  $q/g$  distributions  
from data!





# Jet topics

- E. Metodiev & J. Thaler 1802.00008,
- P. Komiske, E. Metodiev & J. Thaler 1809.01140
- P. Komiske, S. Kryhin & J. Thaler 2205.04459

**Key idea:** statistically **demix** two samples of q/g jets by maximally subtracting the two mixtures from one another, such that the zeros of the subtracted distributions correspond to the anchor regions.

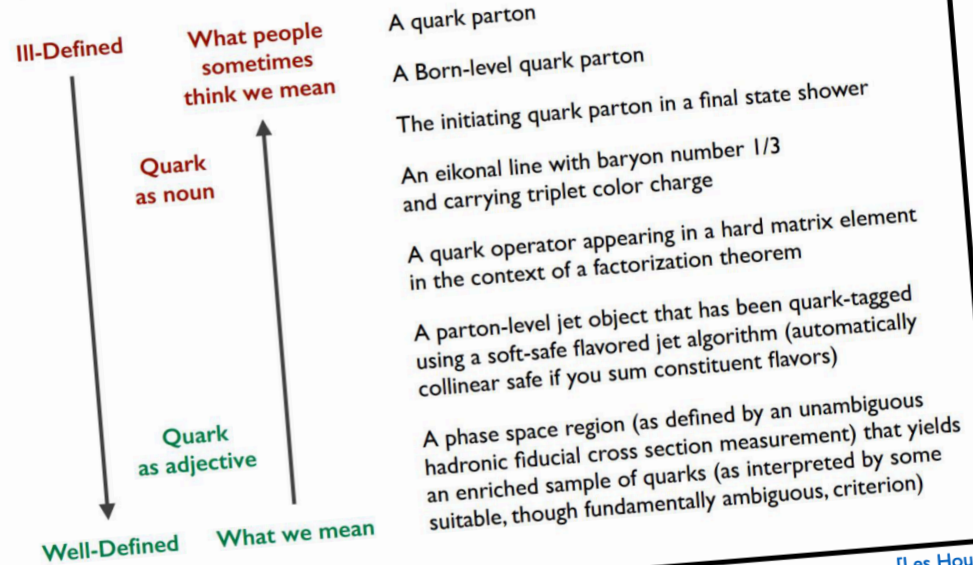
**Data-driven:** does not depend on predictions/labels!

## What are "Quark" and "Gluon" jets?

### What is a Quark Jet?

From lunch/dinner discussions

Word Count



[Les Houches 2015 Report]  
[P.Gras, et al., 1704.03878]

Eric M. Metodiev, MIT

On the Topic of Jets

## Our Plan: An operational definition of quark and gluon jets

### That definition:

[A quark jet is defined by:]  
A phase space region (as defined by an unambiguous hadronic fiducial cross section measurement) that yields an enriched sample of quarks (as interpreted by some suitable, though fundamentally ambiguous, criterion)

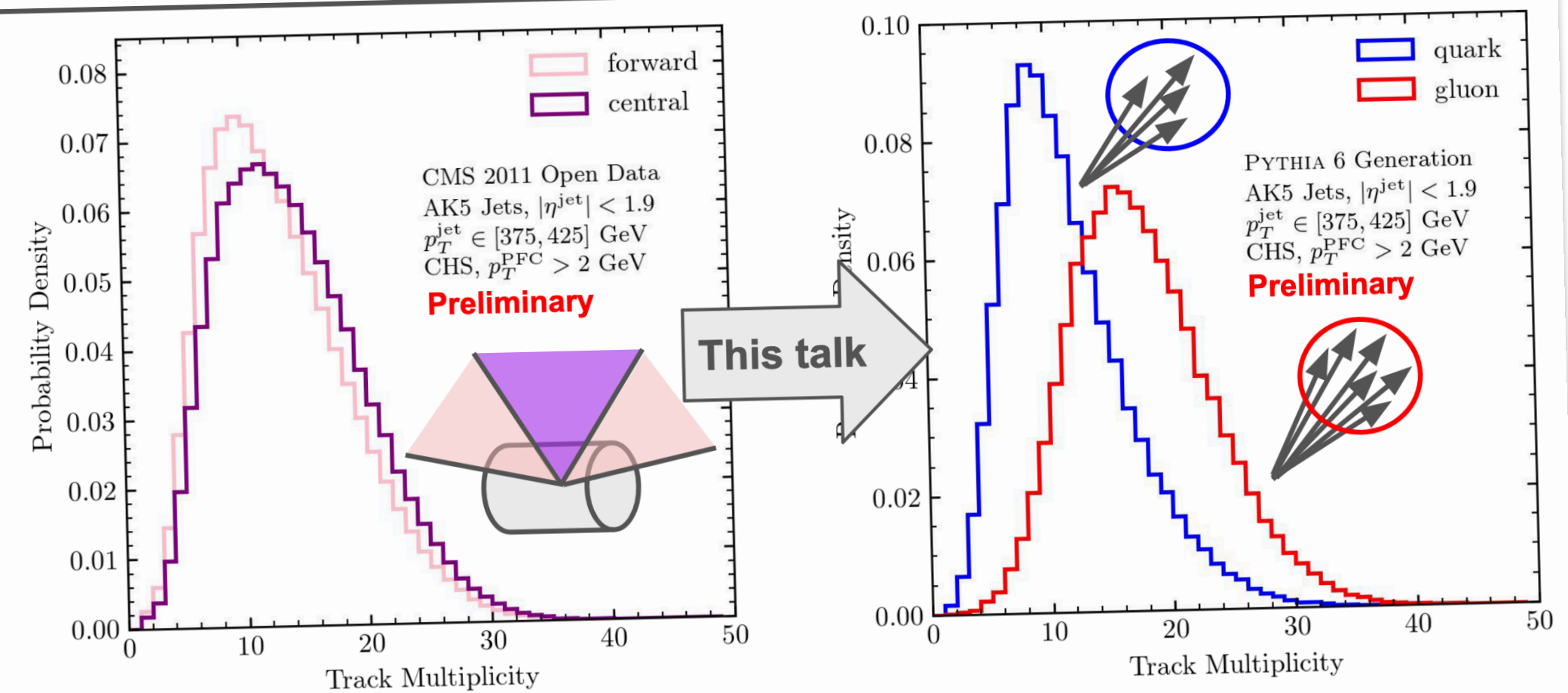
This talk: Translating those 30 words to these 2 equations:

$$p_{\text{quark}}(\mathbf{x}) \equiv \frac{p_A(\mathbf{x}) - \kappa_{AB} p_B(\mathbf{x})}{1 - \kappa_{AB}} \quad p_{\text{gluon}}(\mathbf{x}) \equiv \frac{p_B(\mathbf{x}) - \kappa_{BA} p_A(\mathbf{x})}{1 - \kappa_{BA}}$$

Eric M. Metodiev, MIT

On the Topic of Jets

## Can we decompose a measured sample of jets into its components?



Radha Mastandrea

BOSTON 2019

MIT MOD 2

ERIC @ BOOST 18

RADHA @ BOOST 19

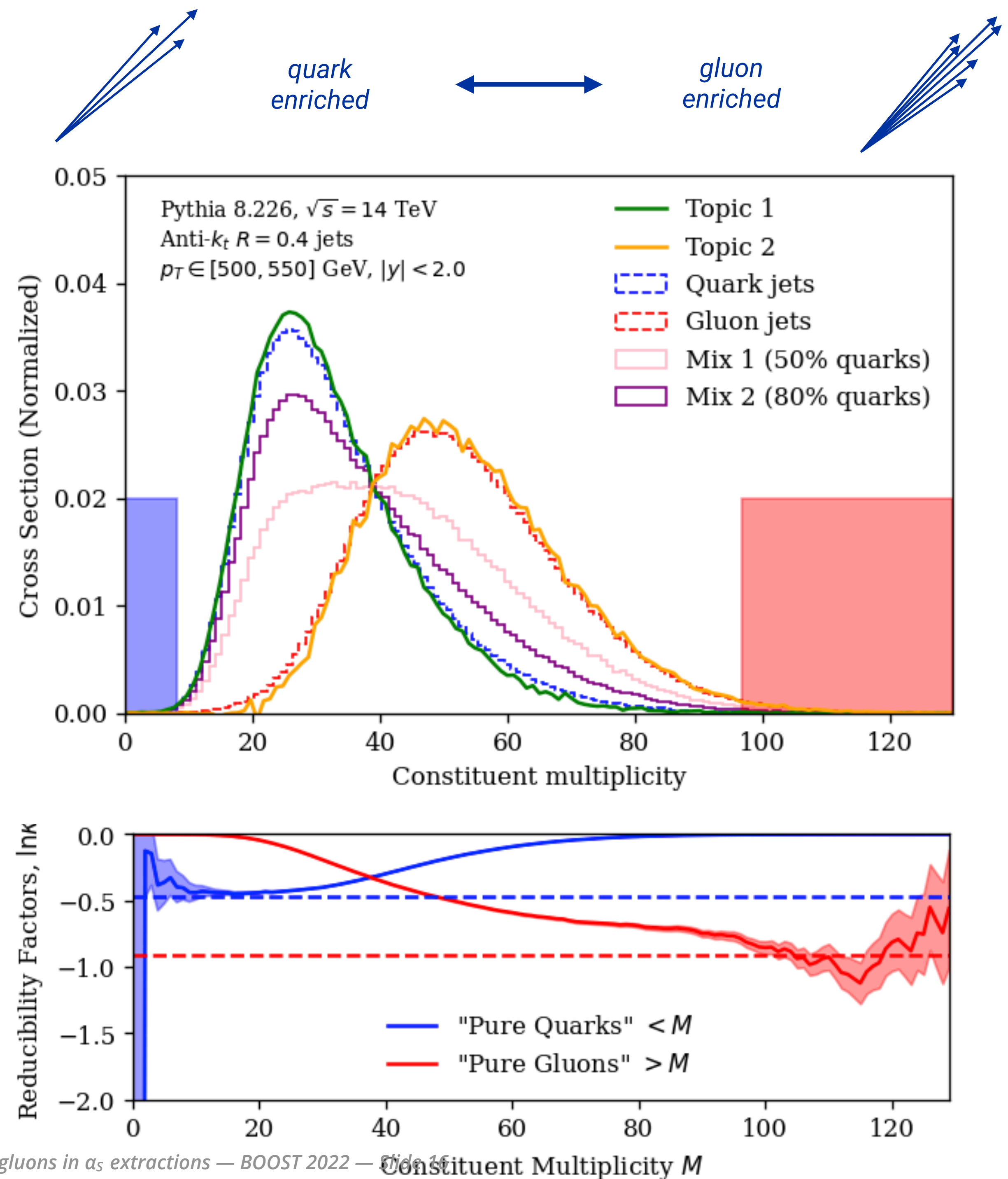
# Jet topics

- Obtain **jet topics** from likelihood ratios.

$$p_{\text{quark}}(\mathbf{x}) = \frac{p_A(\mathbf{x}) - \kappa_{AB} p_B(\mathbf{x})}{1 - \kappa_{AB}}$$

$$p_{\text{gluon}}(\mathbf{x}) = \frac{p_B(\mathbf{x}) - \kappa_{BA} p_A(\mathbf{x})}{1 - \kappa_{BA}}$$

- Here, using two mixed samples of 50% (~dijets) and 80% quarks (~gluons).
- Extracted **topic 1** and **topic 2** recover original **quark** and **gluon** distributions!
- Can use extracted topics to obtain the q/g fractions of the two mixed samples (next slide).

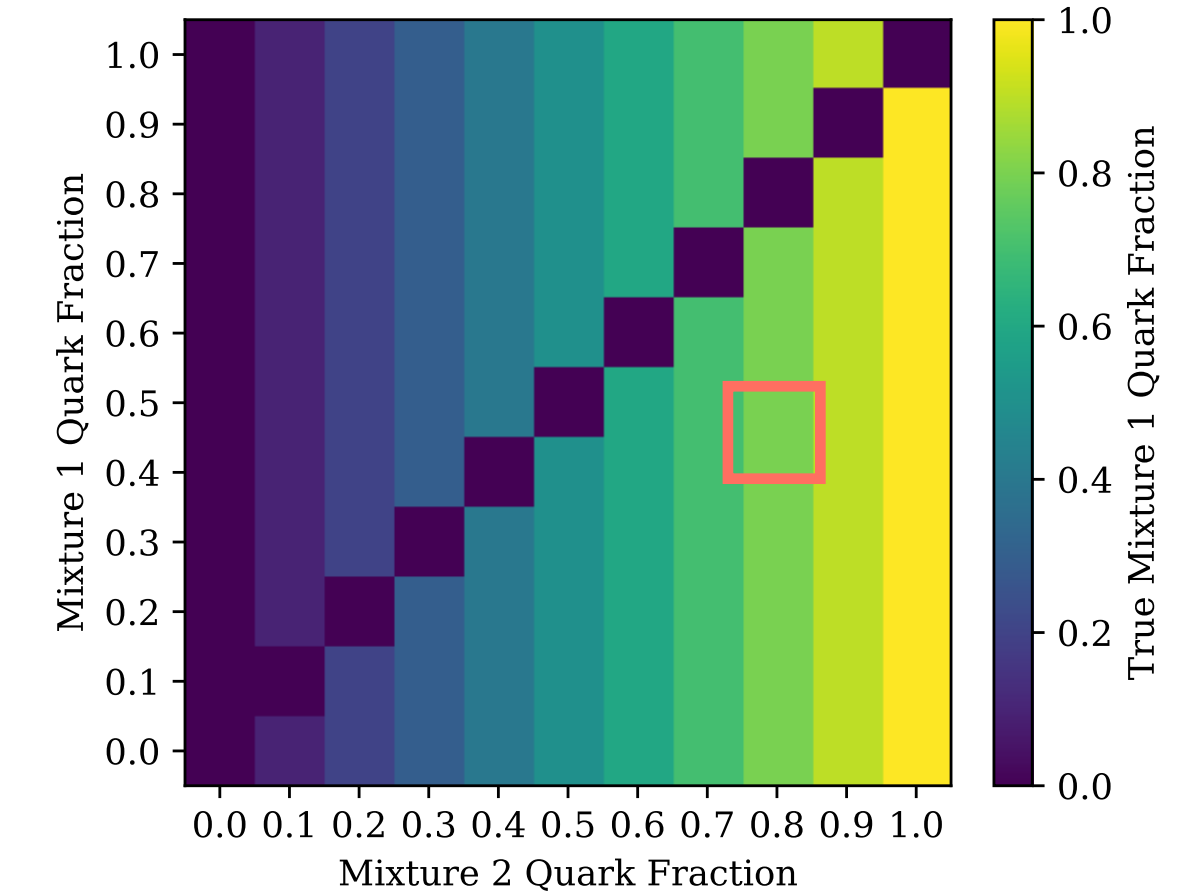
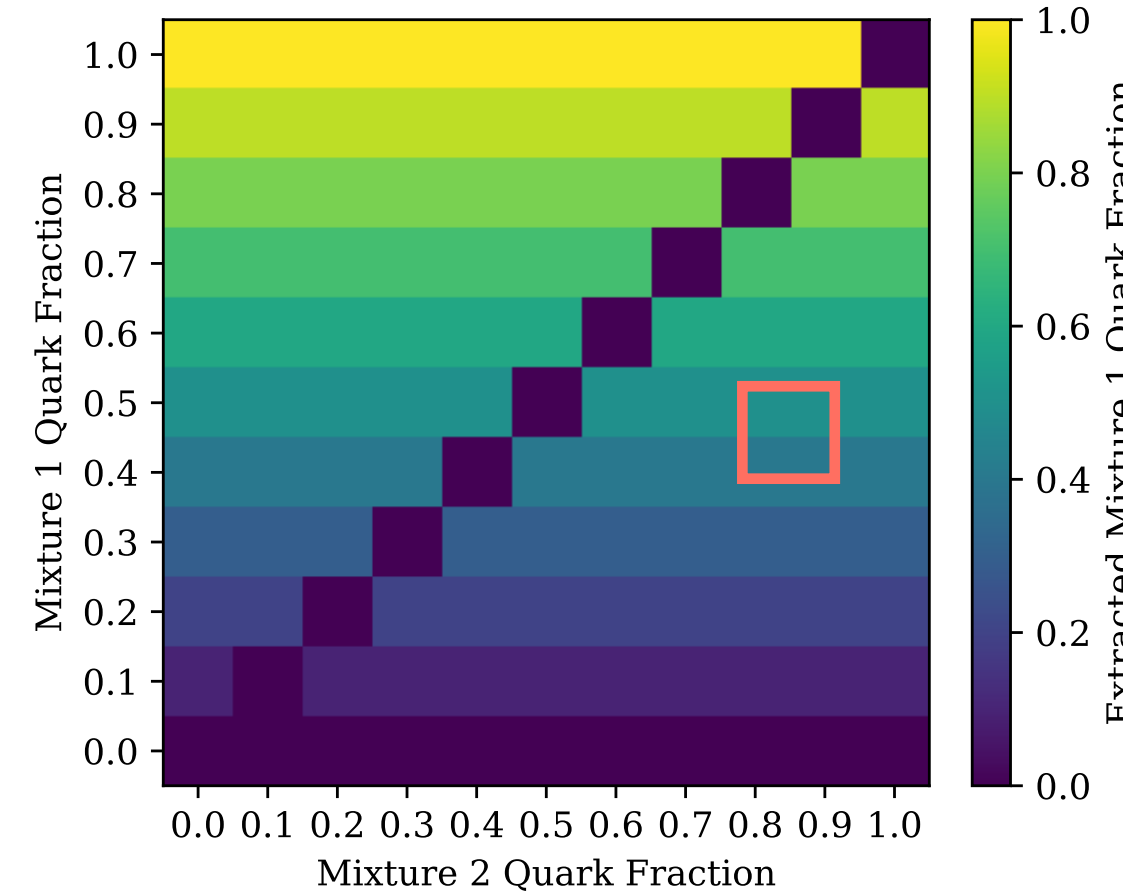




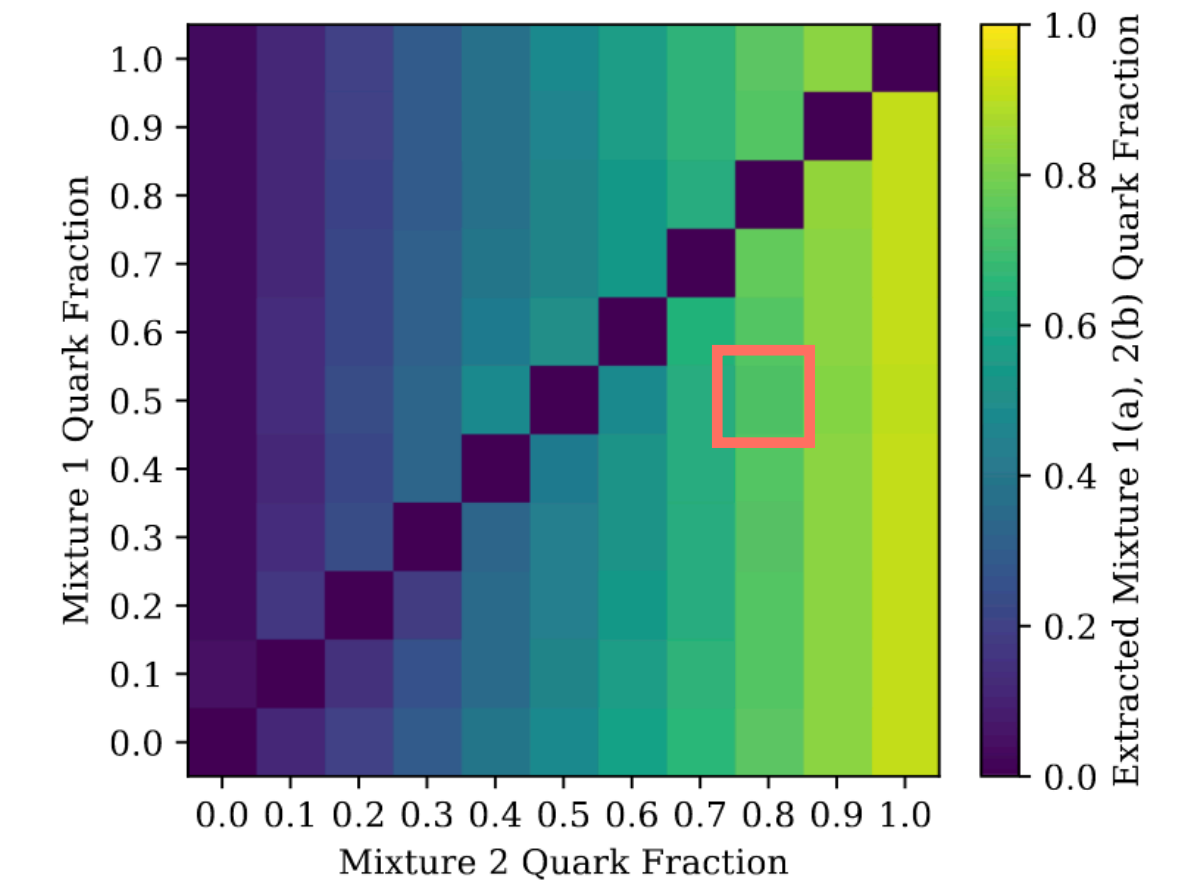
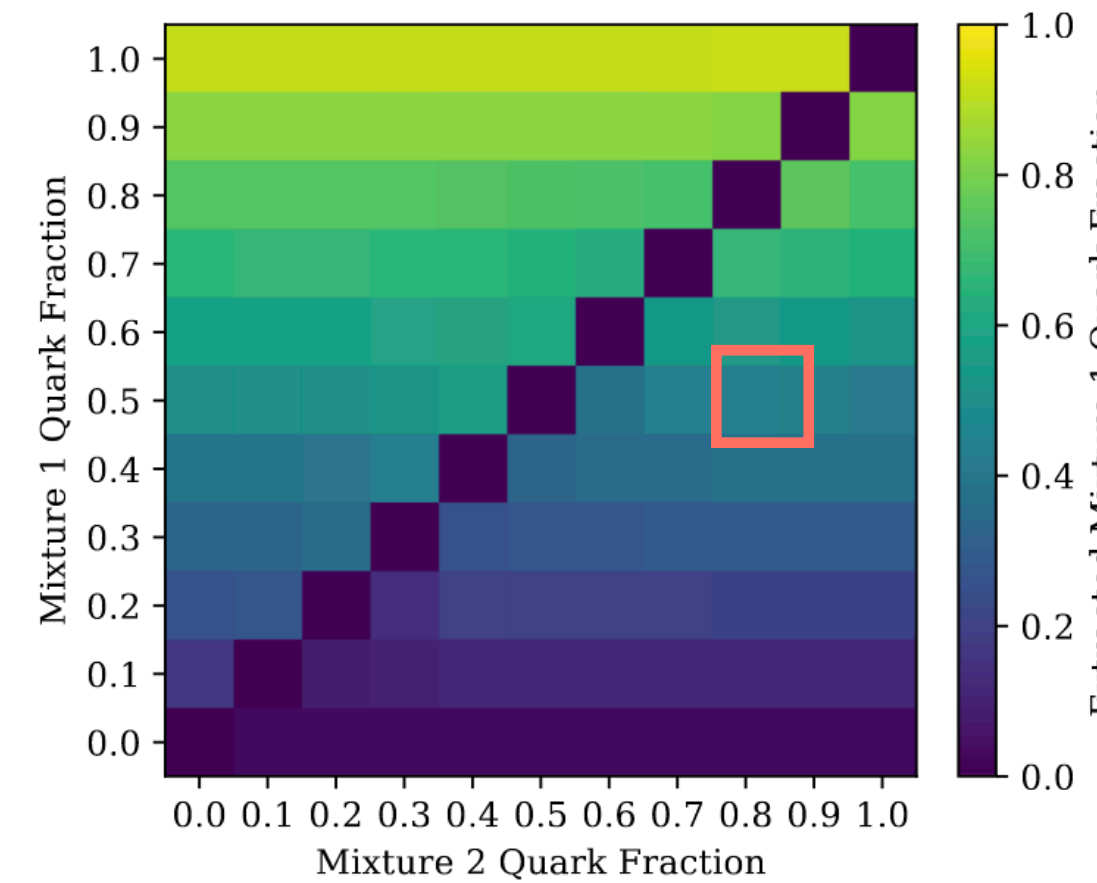
# q/g fractions

- Results of q/g fraction extraction using  $N_{\text{constituents}}$ .
  - Able to recover true fractions to within ~10-15%, performance worse for certain mixtures
    - e.g. pure in one flavour or degenerate.
- Using same anchor region for all bins — performance could probably be improved by someone patient.
- Better methodologies to select anchor regions proposed while we were finalising the study : Komiske *et al.* [2205.04459](#).

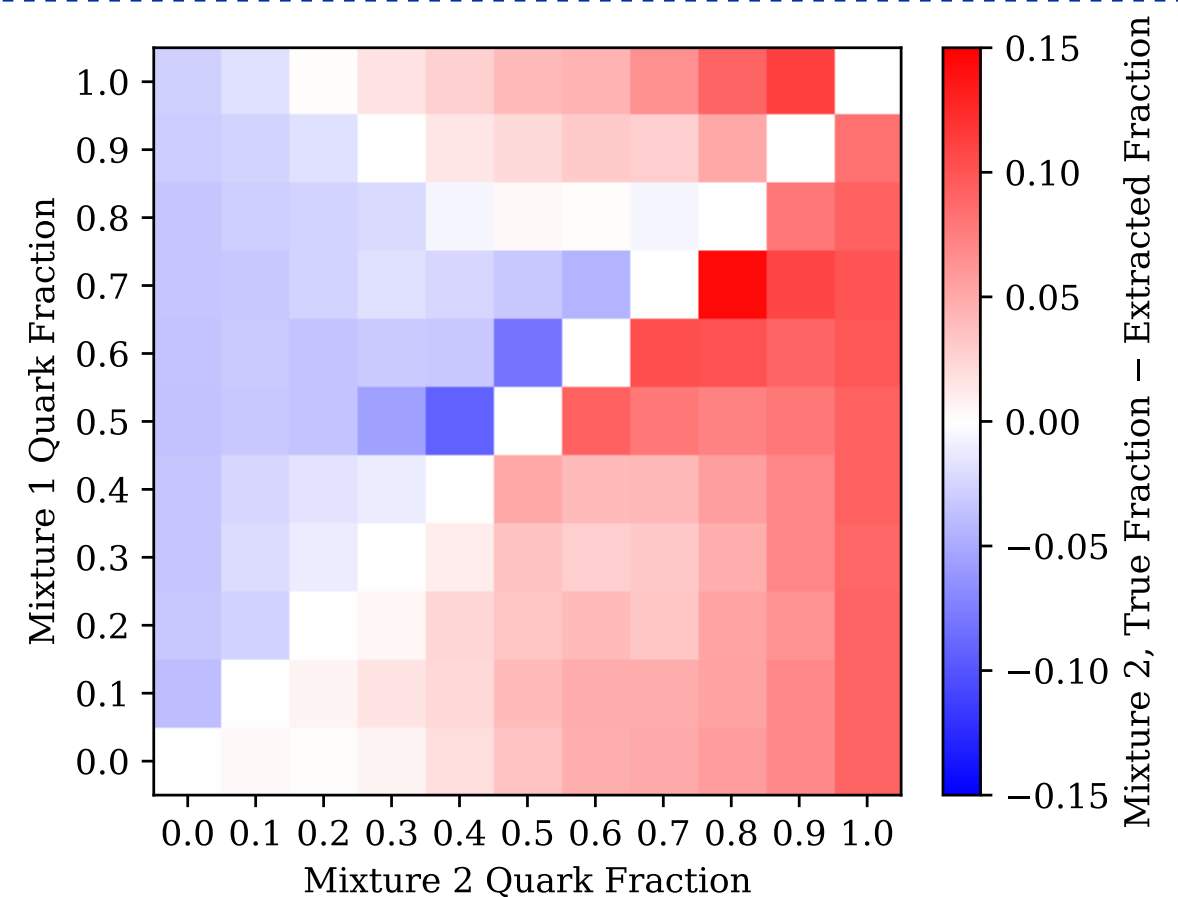
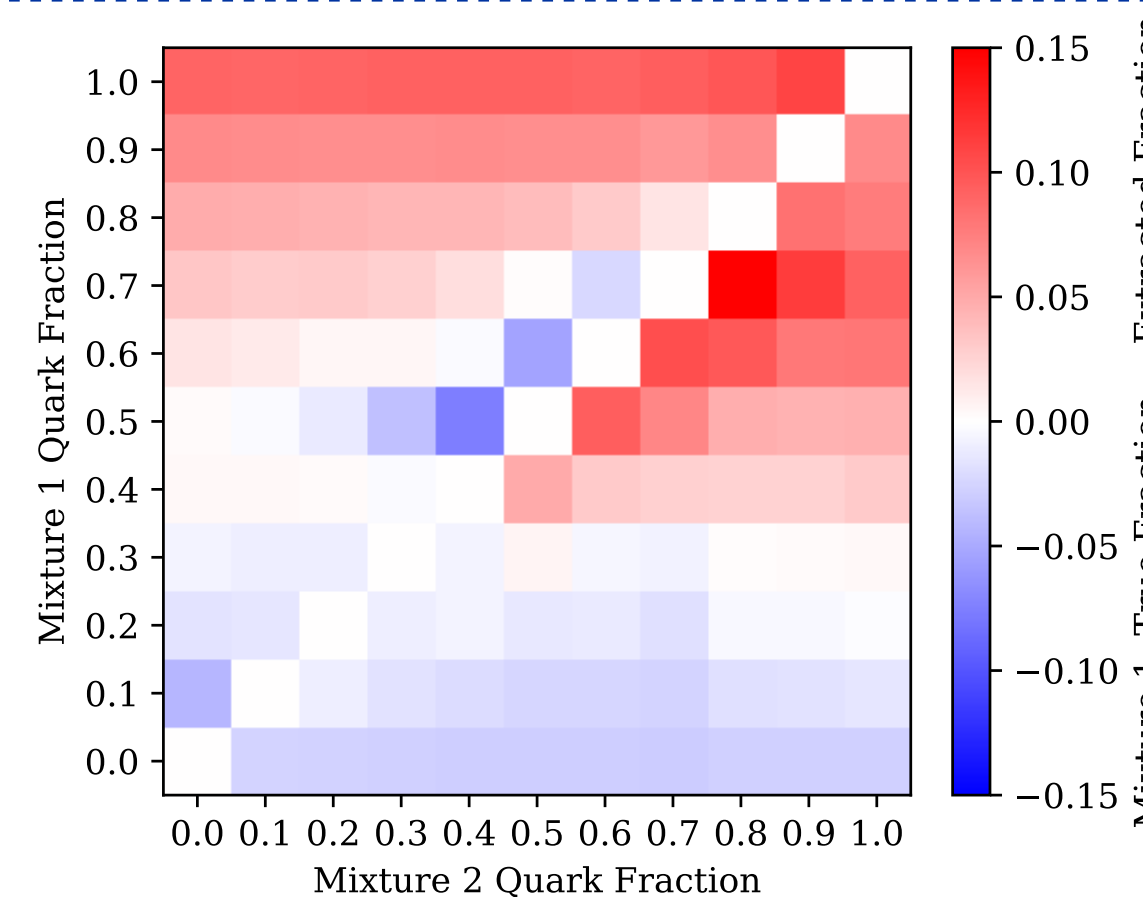
True fractions (trivial)



Extracted fractions (NConst.)

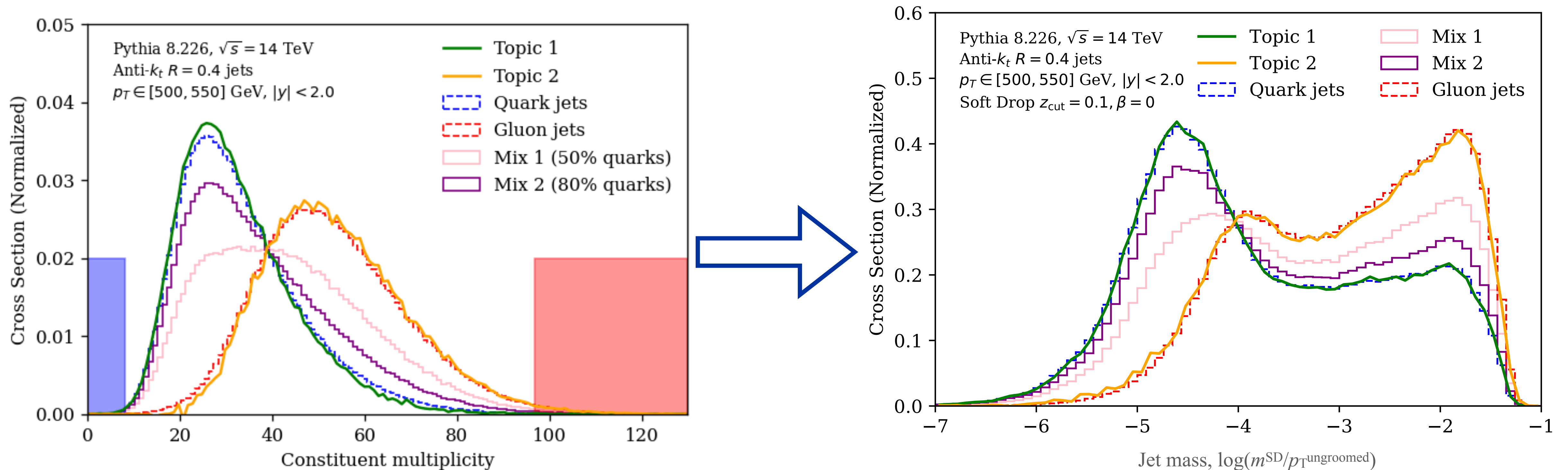


Non-closure (NConst.)





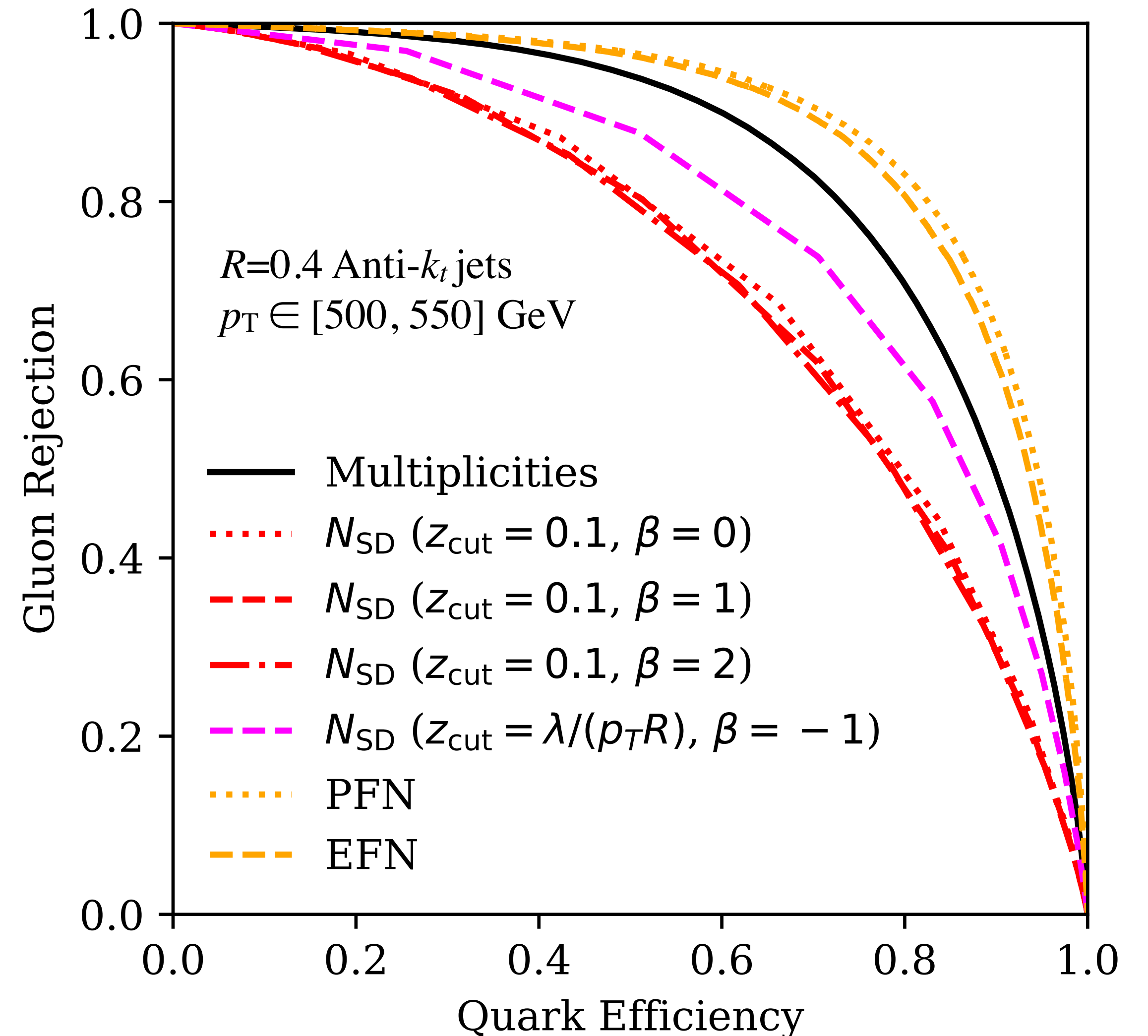
# Going 'off topics' (get it now?)



- Reducibility factors are a property of the ***event ensemble***, rather than the jet/event.
  - Once we extract them from a mutually-irreducible observable, we can apply them to obtain **topics for *non-mutually-irreducible* observables**.

# Other $q/g$ discriminants

- $N_{\text{constituents}}$  may not be a desirable observable experimentally.
  - Systematics may be difficult to define in a robust way (cluster efficiency, *etc.*)
- — but any mutually-irreducible observable can be used.
  - In practice, whatever observable allows for the most precise extraction is probably the best one to try.
- Studied a few other options, and repeated the study in-detail with a PFN  $q/g$  classifier.
  - Could design an ML/AI discriminant with correlated response at particle- and detector-level, better experimental precision than  $N_{\text{constituents}}$ .

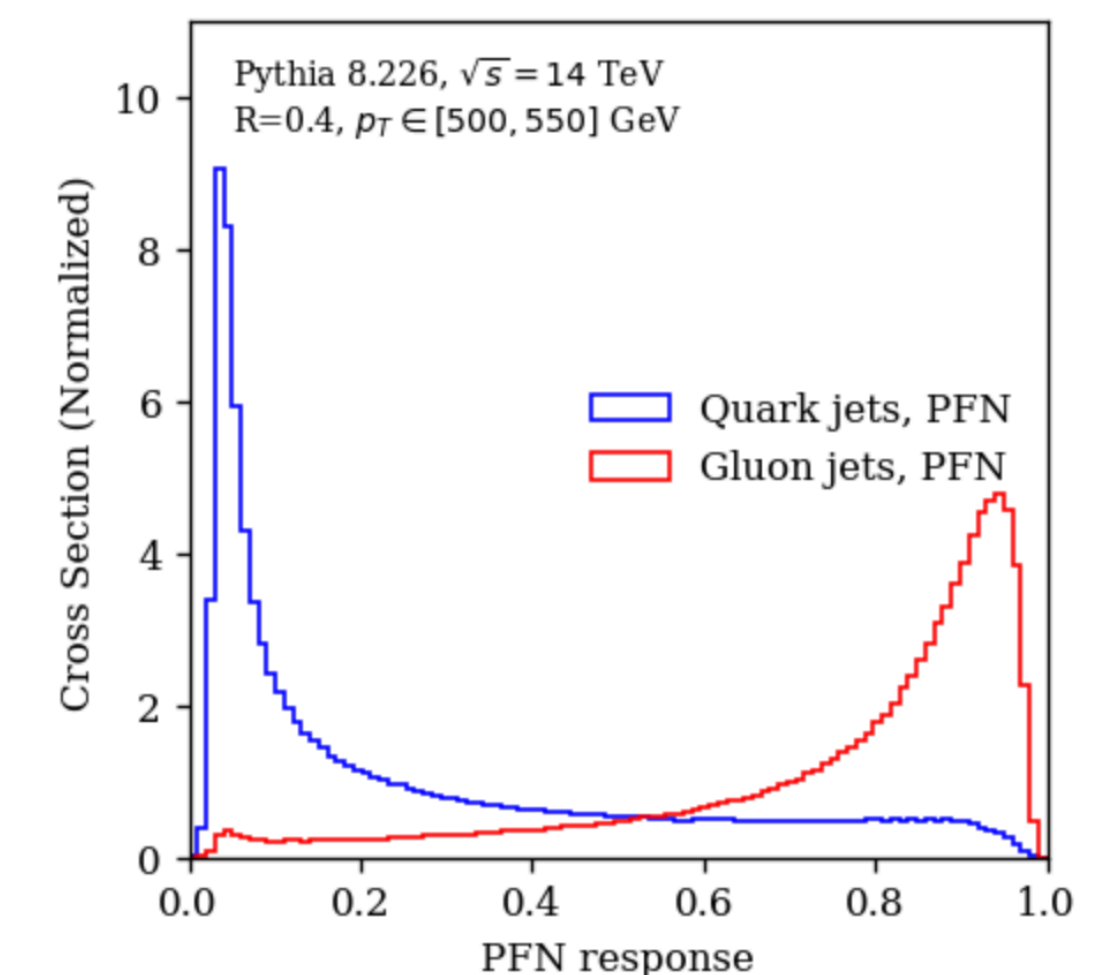
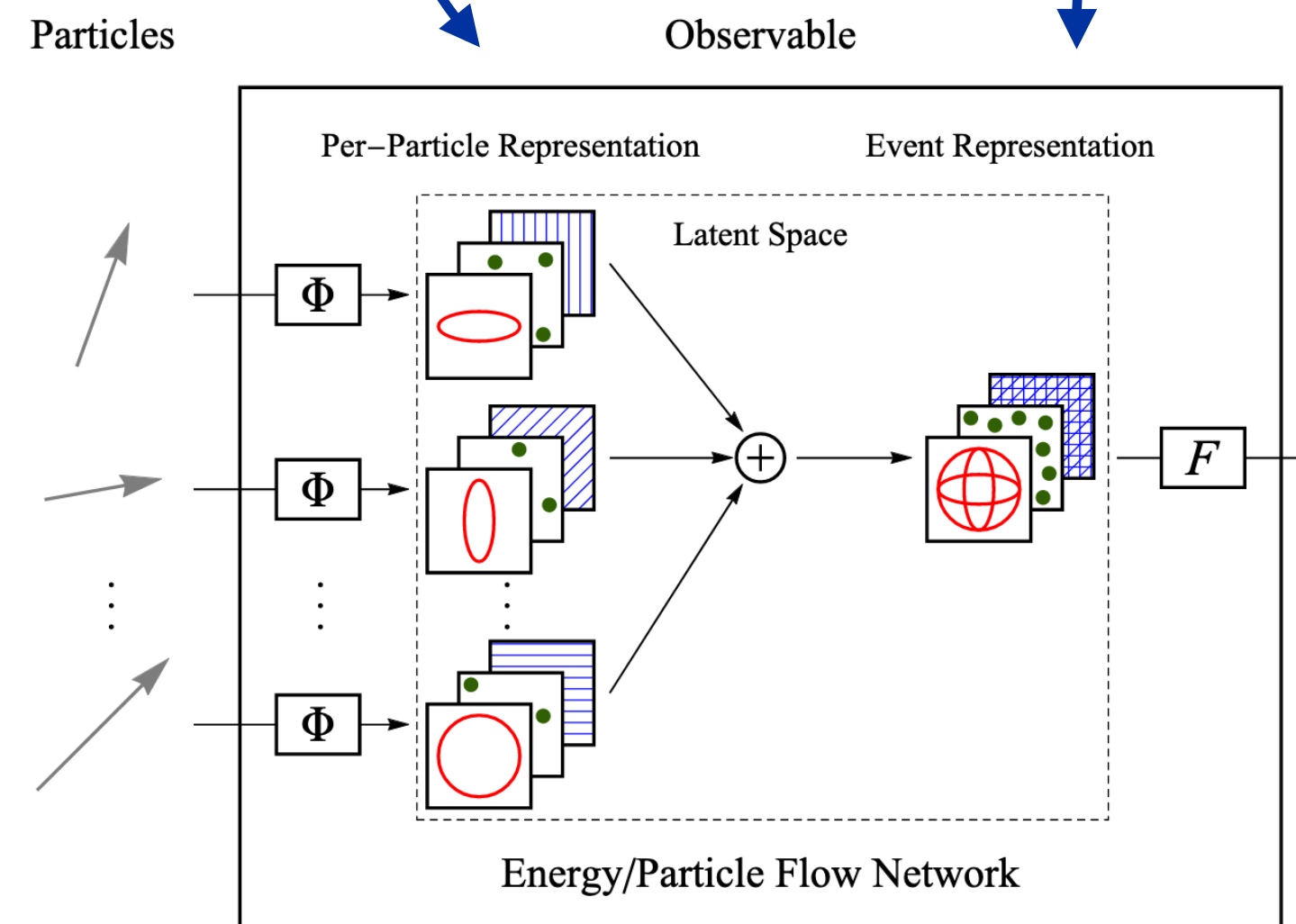
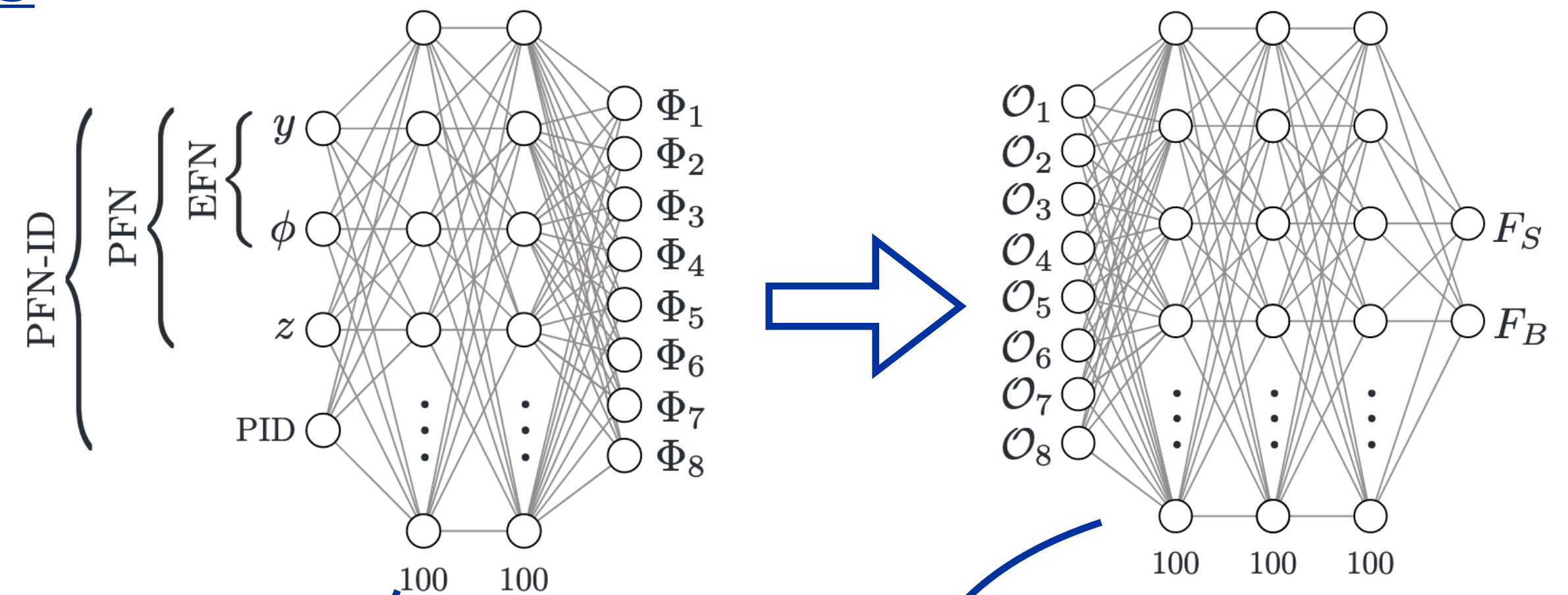


# Particle Flow Networks (Deep Sets)

[Komiske, Metodiev & Thaler 1810.05165](#)

[Zaher et al. 1703.06114](#)

- Jets are **unordered** particle sets of **variable length**.
  - Point-clouds are a natural representation for hadronic showers:
  - Deep sets framework is naturally permutation invariant due to internal sum layer.
- ***This approach has already been explained at BOOST, so we'll spare you the details this time.***

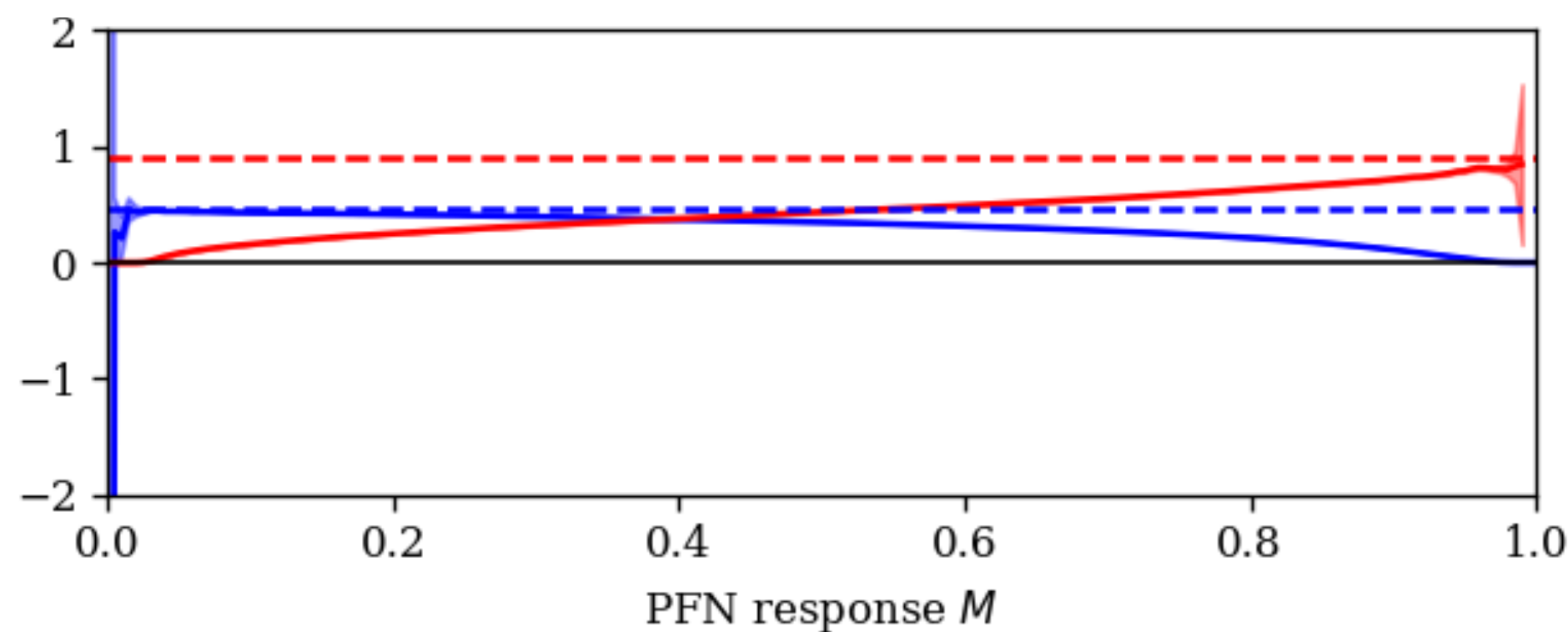
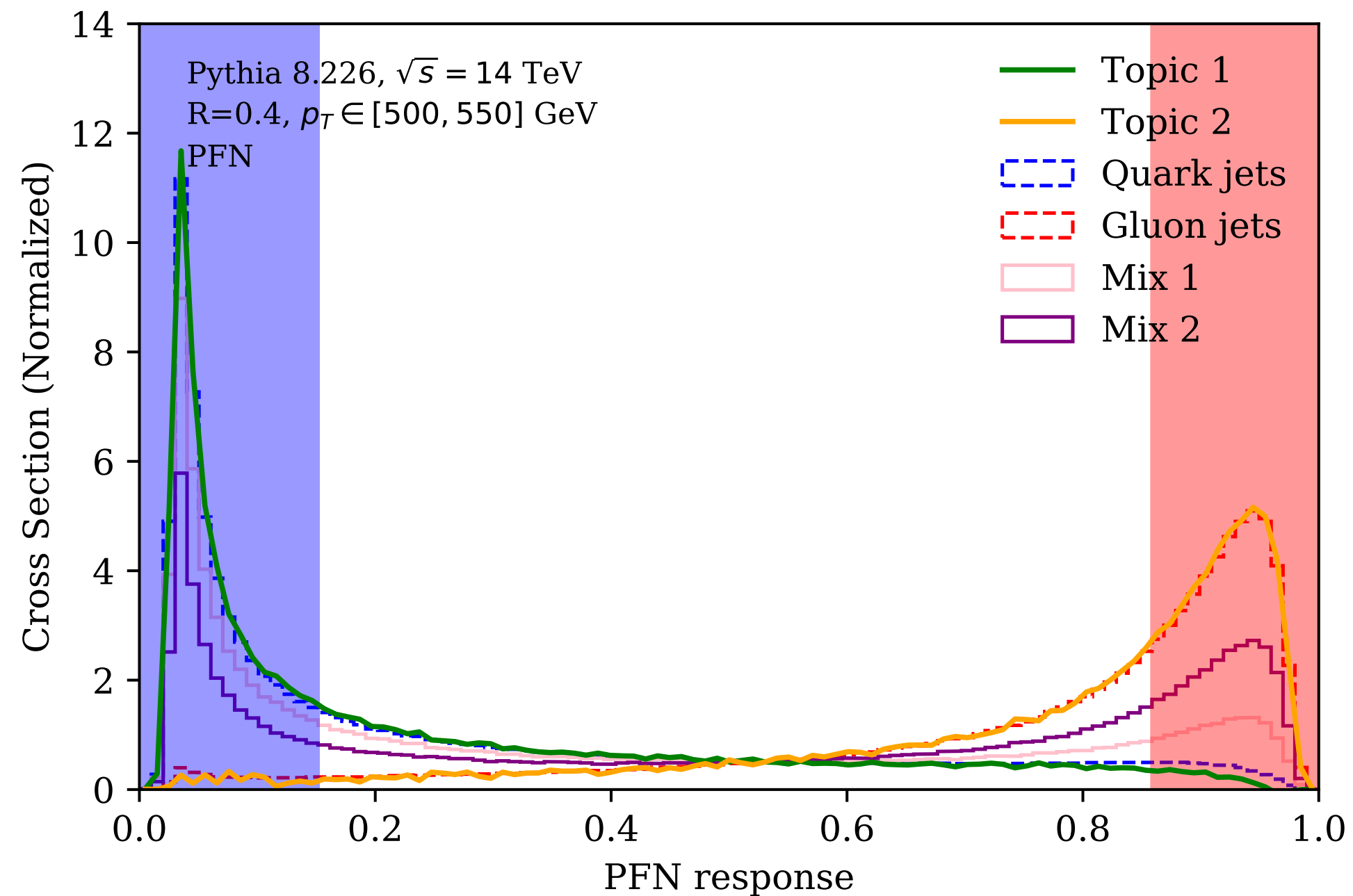




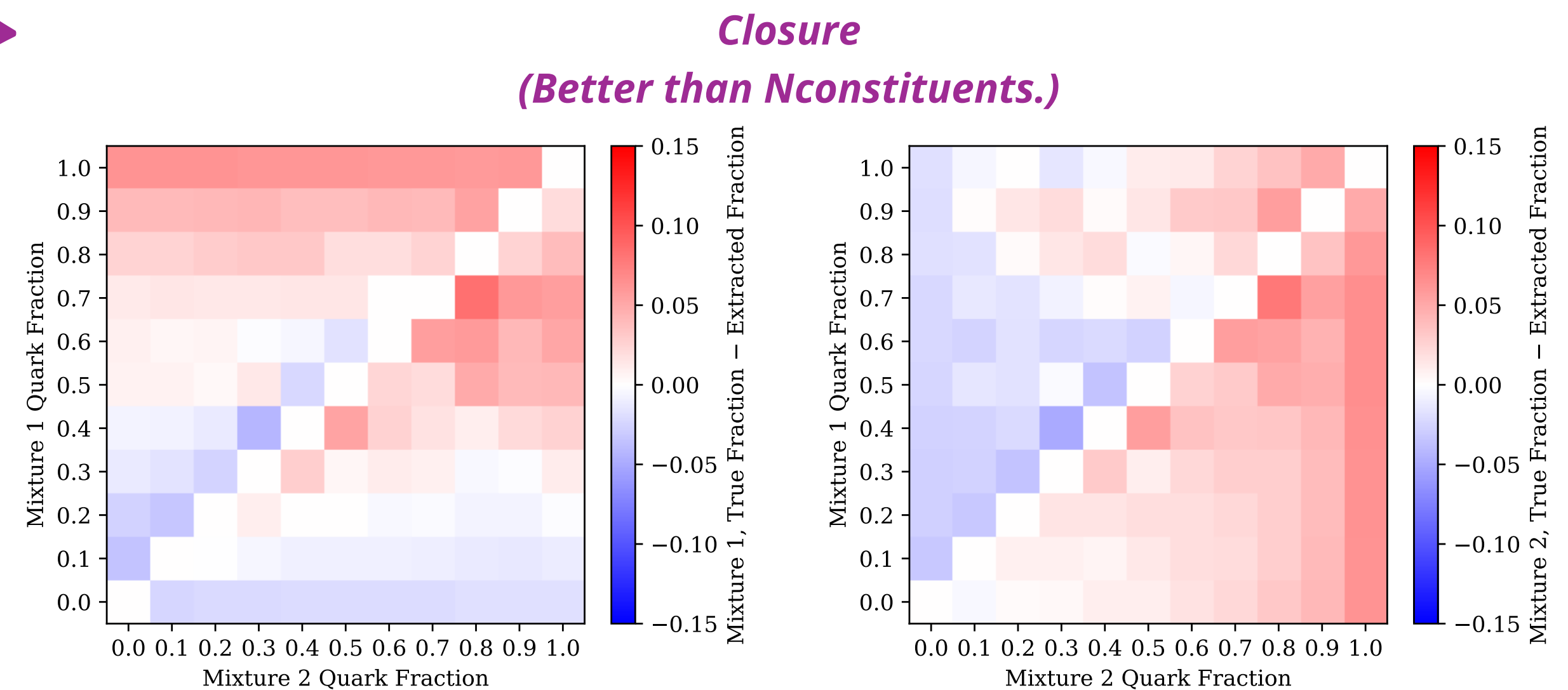
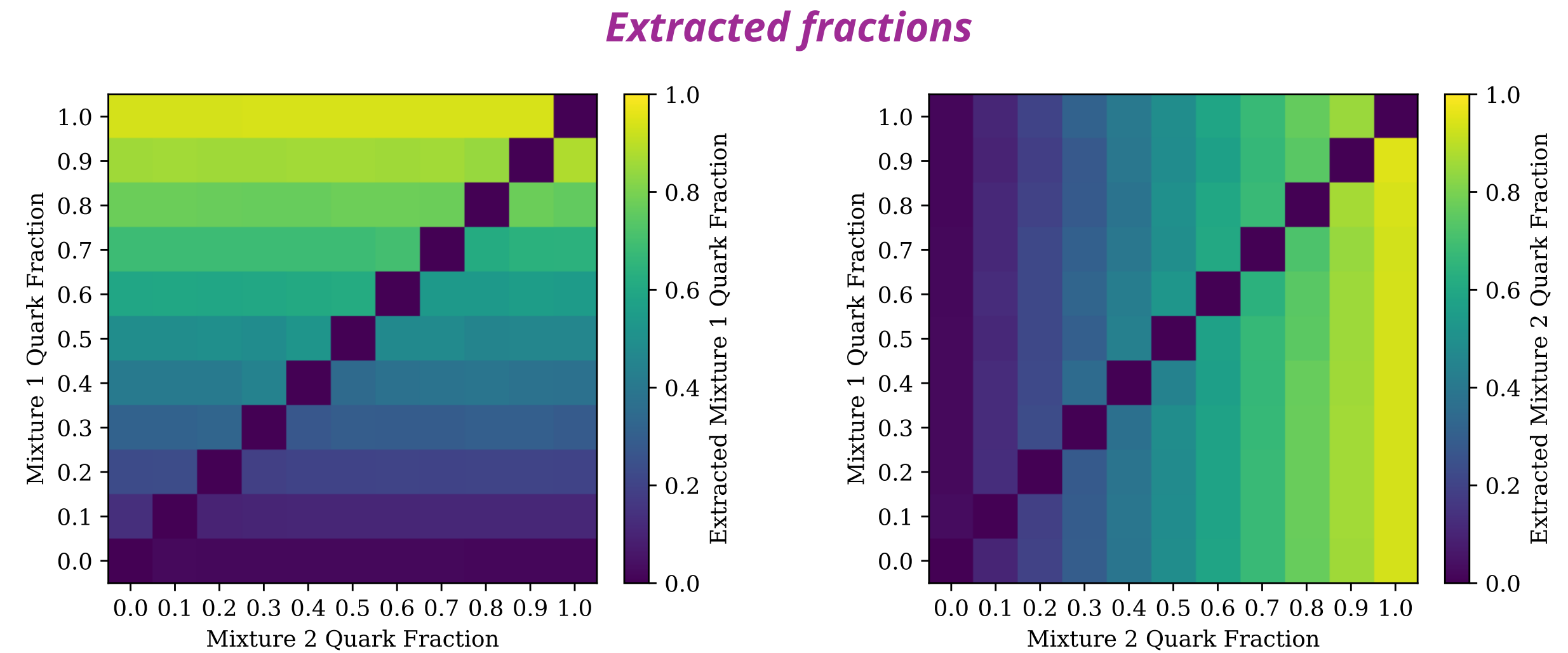
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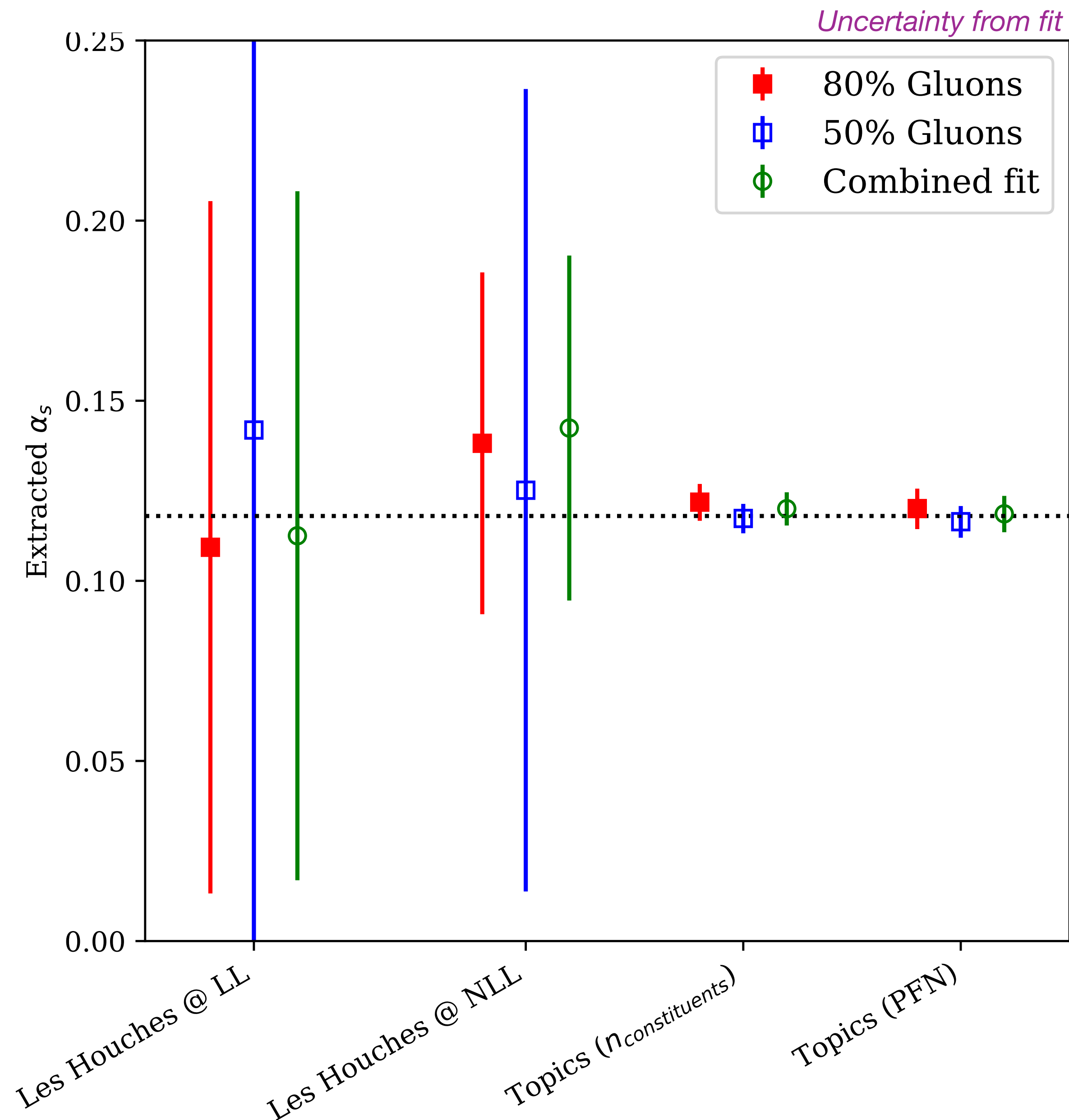


Follow  
same  
procedure



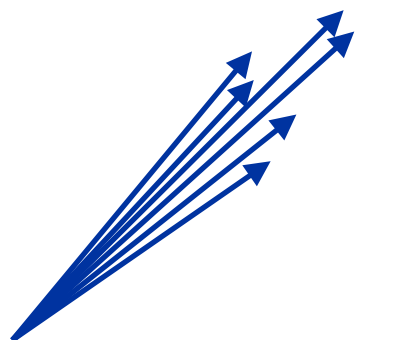
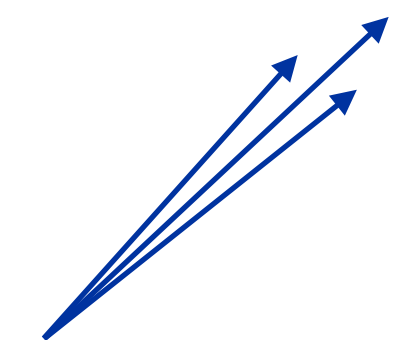
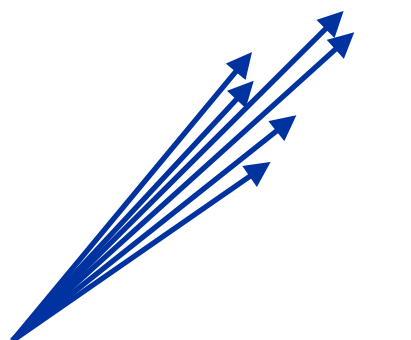
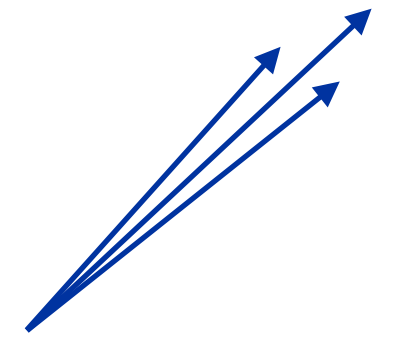
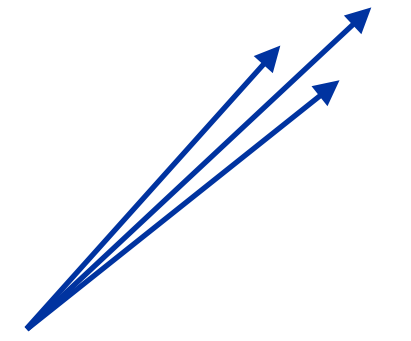
# Improved Results

- Repeat fitting procedure, fixing  $q/g$  fractions to the values extracted via topics.
  - Large covariances in fit essentially removed: remaining uncertainty is either statistical in nature or related to anchor bin selection.
- Relative uncertainty in this fit reduced to  $\sim 7\%$ .
  - Topics extractions can be further refined.
    - Anchor region selection still rudimentary here: better strategies in Komiske et al. [2205.04459](#).
- Other experimental & theoretical challenges remain, but this approach opens a new way forward toward the first extractions of  $\alpha_s$  from JSS.

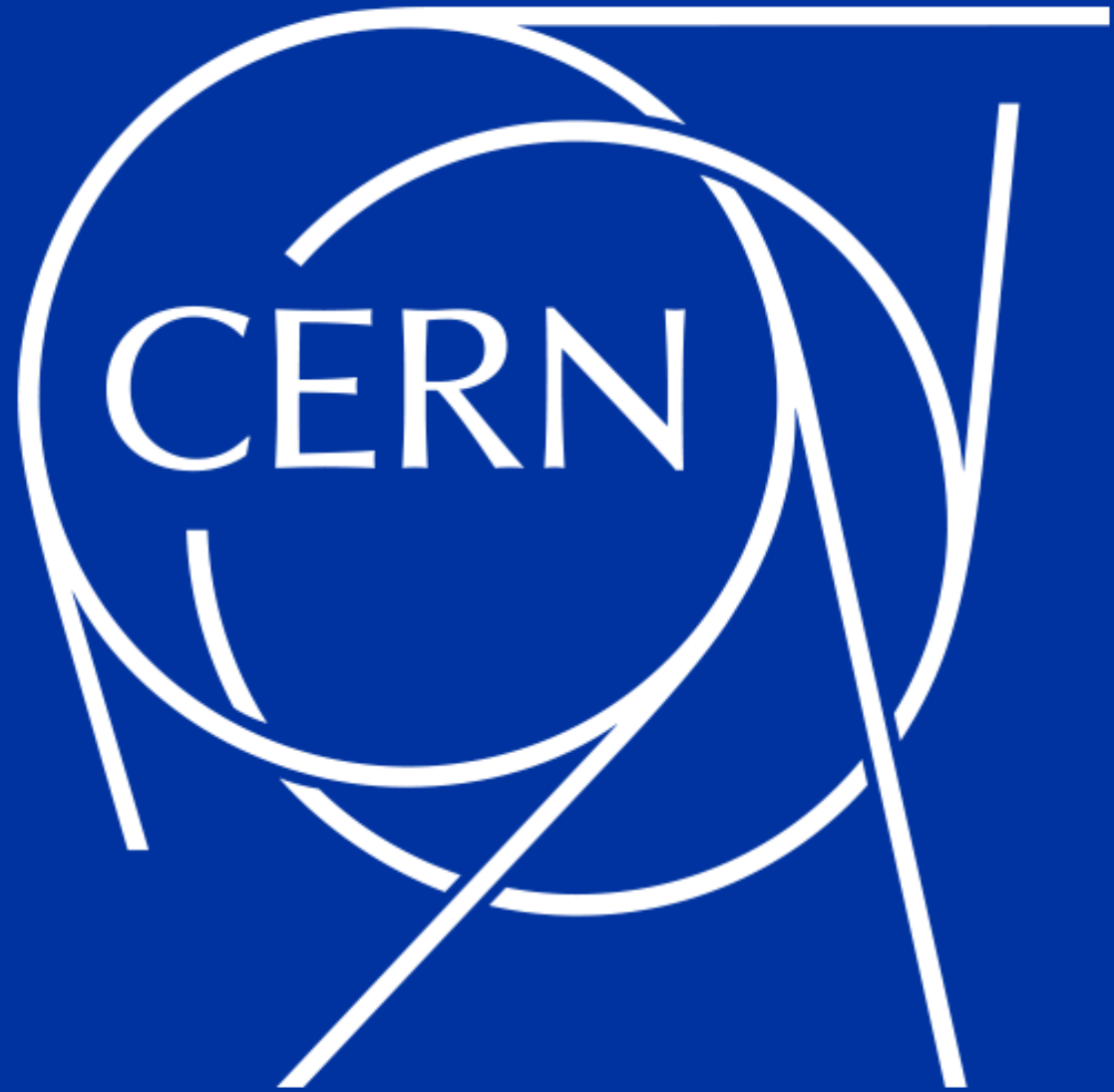


# Summary

- We have outlined a proposal to apply statistical demixing procedures in the context of  $\alpha_s$  extractions from groomed JSS observables.
  - This work builds upon the strategy outlined by the Jets working group at [LH'17 \(1803.07977\)](#).
  - Degeneracy between  $\alpha_s$  and sample  $q/g$  composition is broken by this method, removing the major source of methodological uncertainty.
- It is possible to use IRC-unsafe information to extract the sample  $q/g$  composition without compromising theoretical tractability.
  - *i.e.* we can incorporate **ML/AI-based observables** and **precision QCD!**
- Many experimental & theoretical steps to go before complete  $\alpha_s$  extractions from JSS are competitive.
  - *Can topics be identified as the “quarks” and “gluons” used in calculations?*







*Thanks for thinking  
about these topics!*

