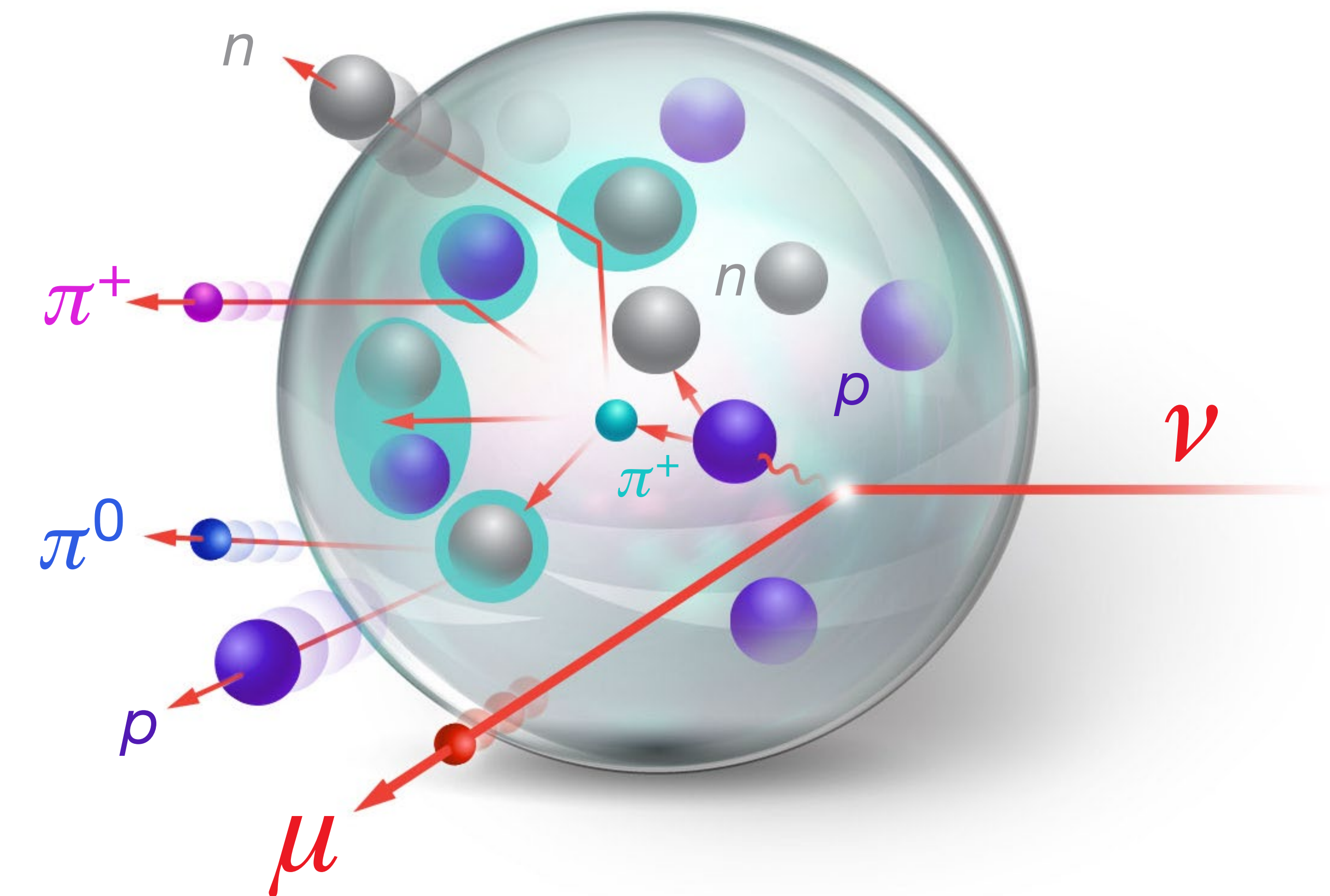


Theoretical tools for neutrino scattering: interplay between lattice QCD, EFTs, nuclear physics, phenomenology, and neutrino event generators



Steven Gardiner
HSF Generator WG Meeting

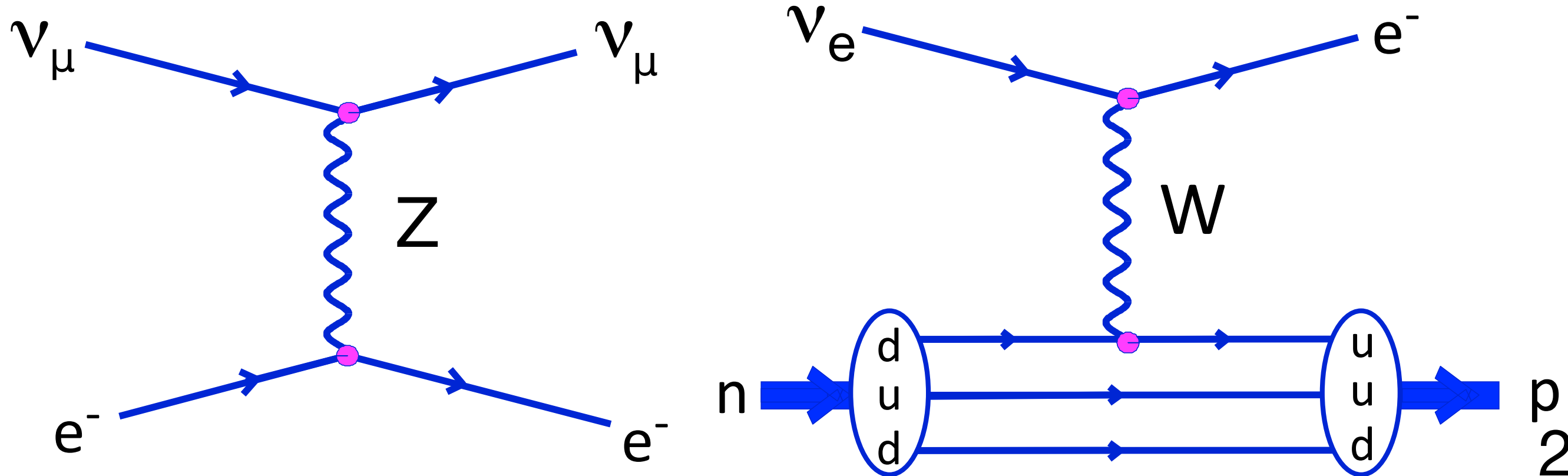
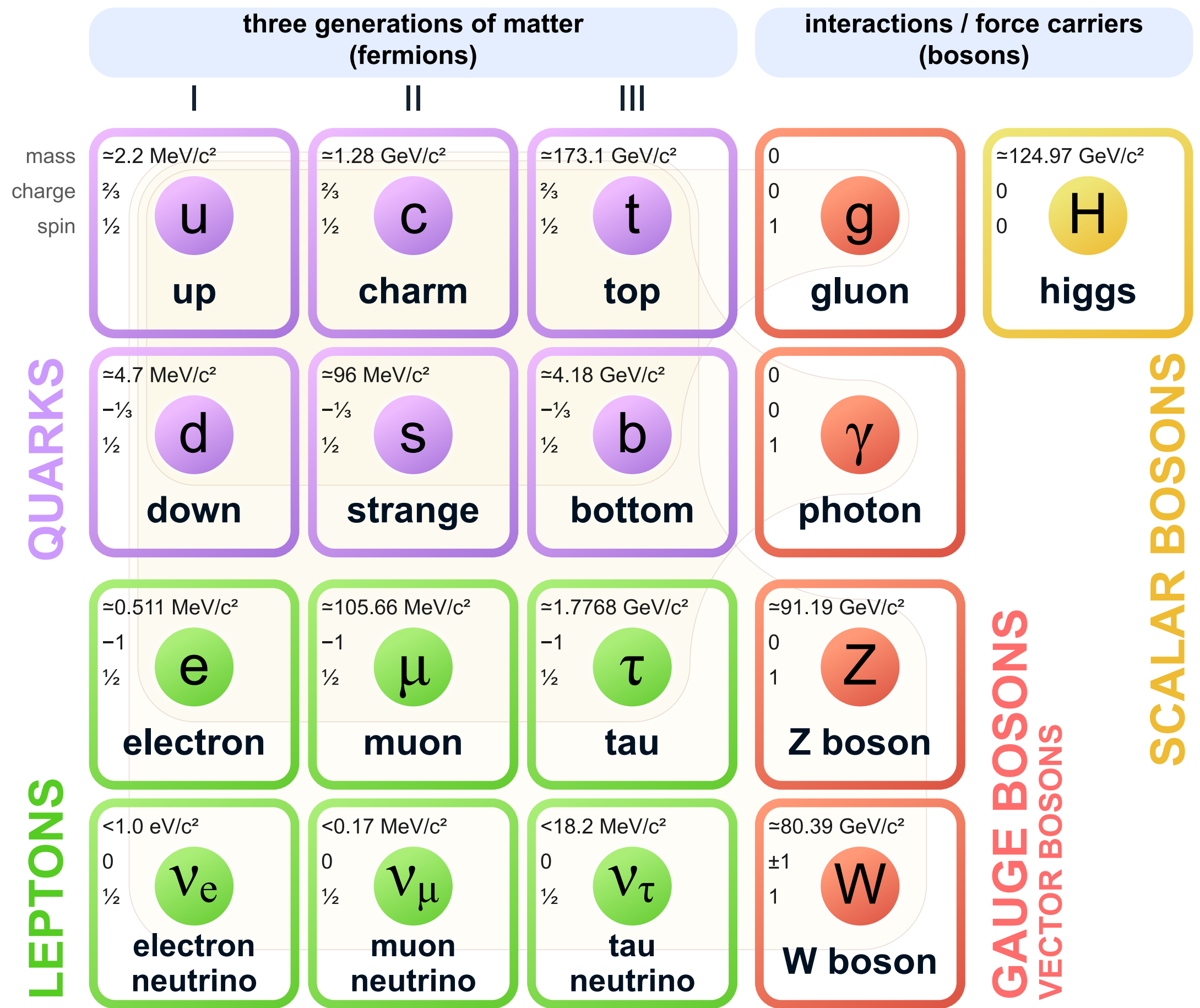
5 May 2022

Partially based on [arXiv:2203.09030](https://arxiv.org/abs/2203.09030)

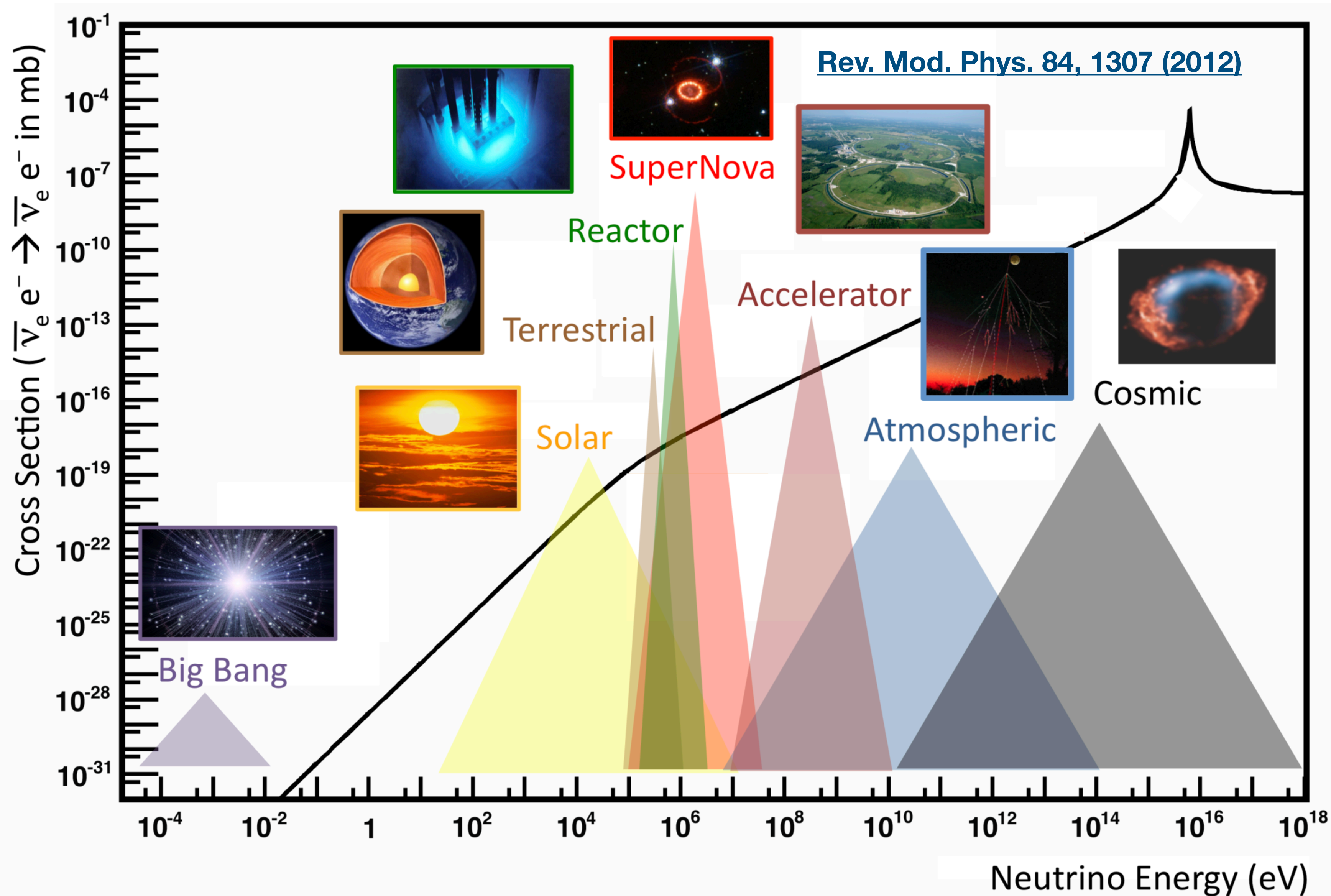
Neutrinos in the Standard Model

- Weakly interacting
 - W exchange = “charged current” (CC)
 - Z exchange = “neutral current” (NC)
- Detectors typically rely on **neutrino-nucleus** interactions
 - Far larger cross section than ν -e scattering
- Intense neutrino beams and massive targets still required to do the physics!

Standard Model of Elementary Particles



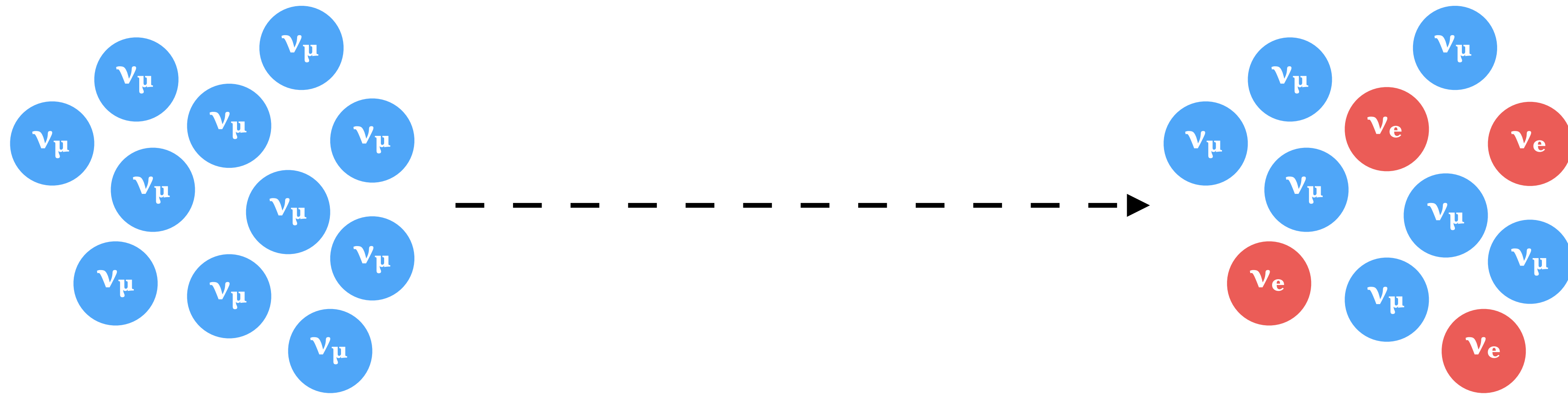
Neutrino physics across energy scales



- Many orders of magnitude in energy!
- **White paper** focuses on ~ 1 MeV to ~ 10 GeV region
- **MeV:** solar + supernova neutrinos, precision nuclear measurements
- **GeV:** oscillations, various exotic searches
- Very high energies also interesting, cross-section models sub-leading concern

Neutrino oscillations

- Flavor eigenstates (ν_e, ν_μ, ν_τ) \neq mass eigenstates (ν_1, ν_2, ν_3) \rightarrow mixing
- Leads to oscillations: flavor can change as neutrinos travel

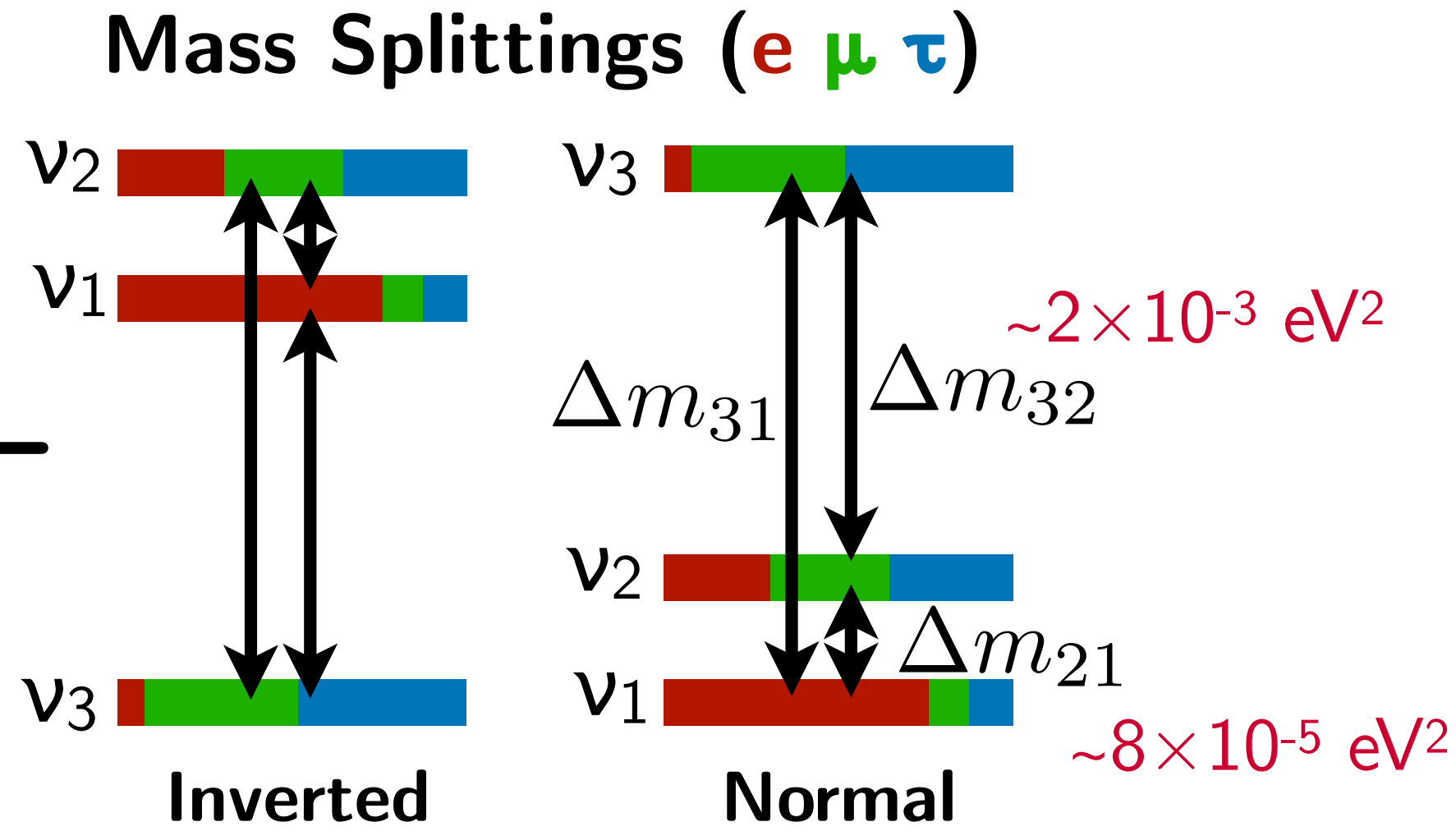


Oscillation probability: $P(\nu_\alpha \rightarrow \nu_\beta) \approx \sin^2 2\theta \sin^2 \left(\frac{\Delta m^2 L}{4E_\nu} \right)$
(two-neutrino case)

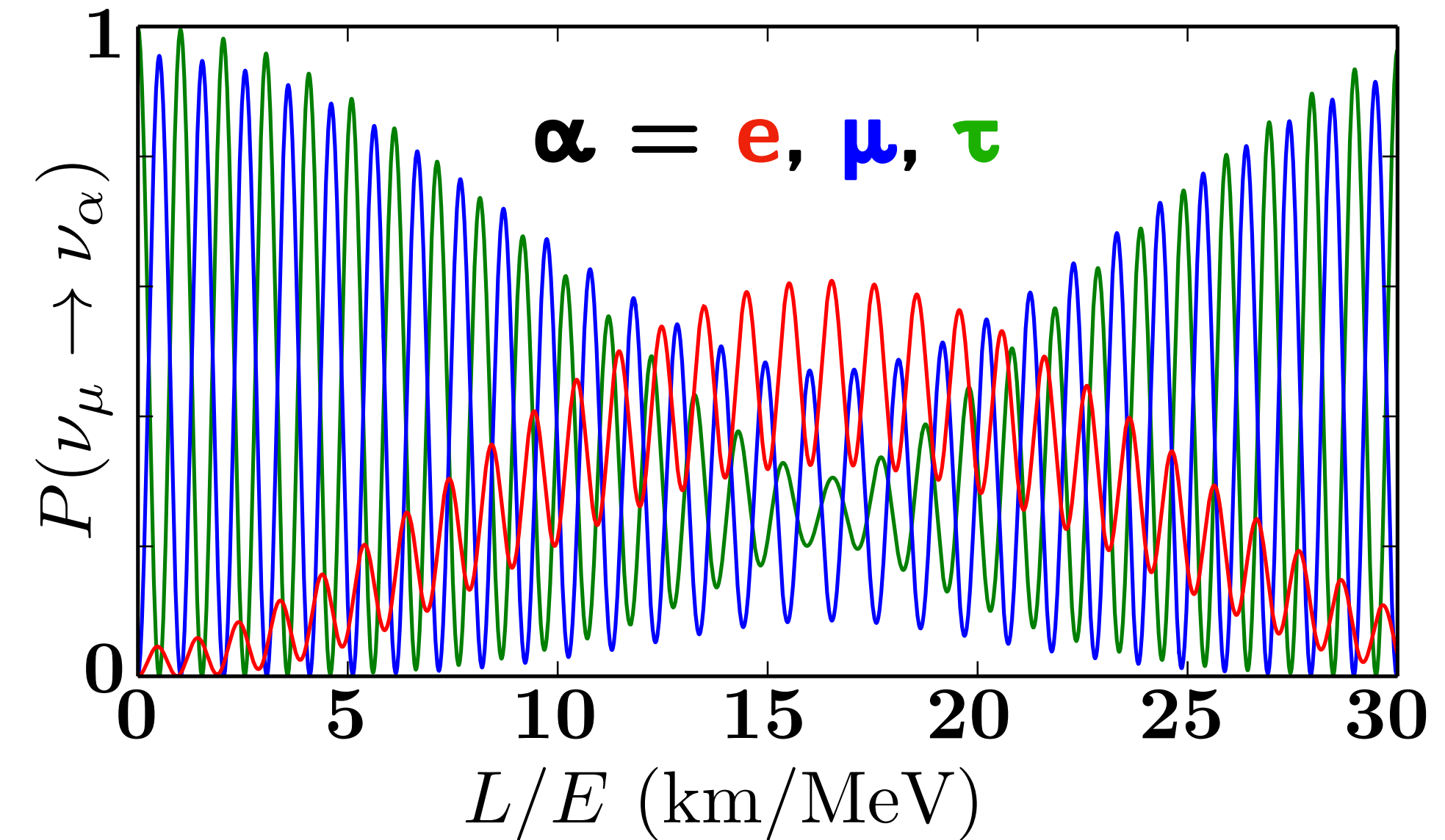
Neutrino oscillations

Three Neutrinos
with Mixing

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle +$$



Oscillation Probabilities



Mixing matrix

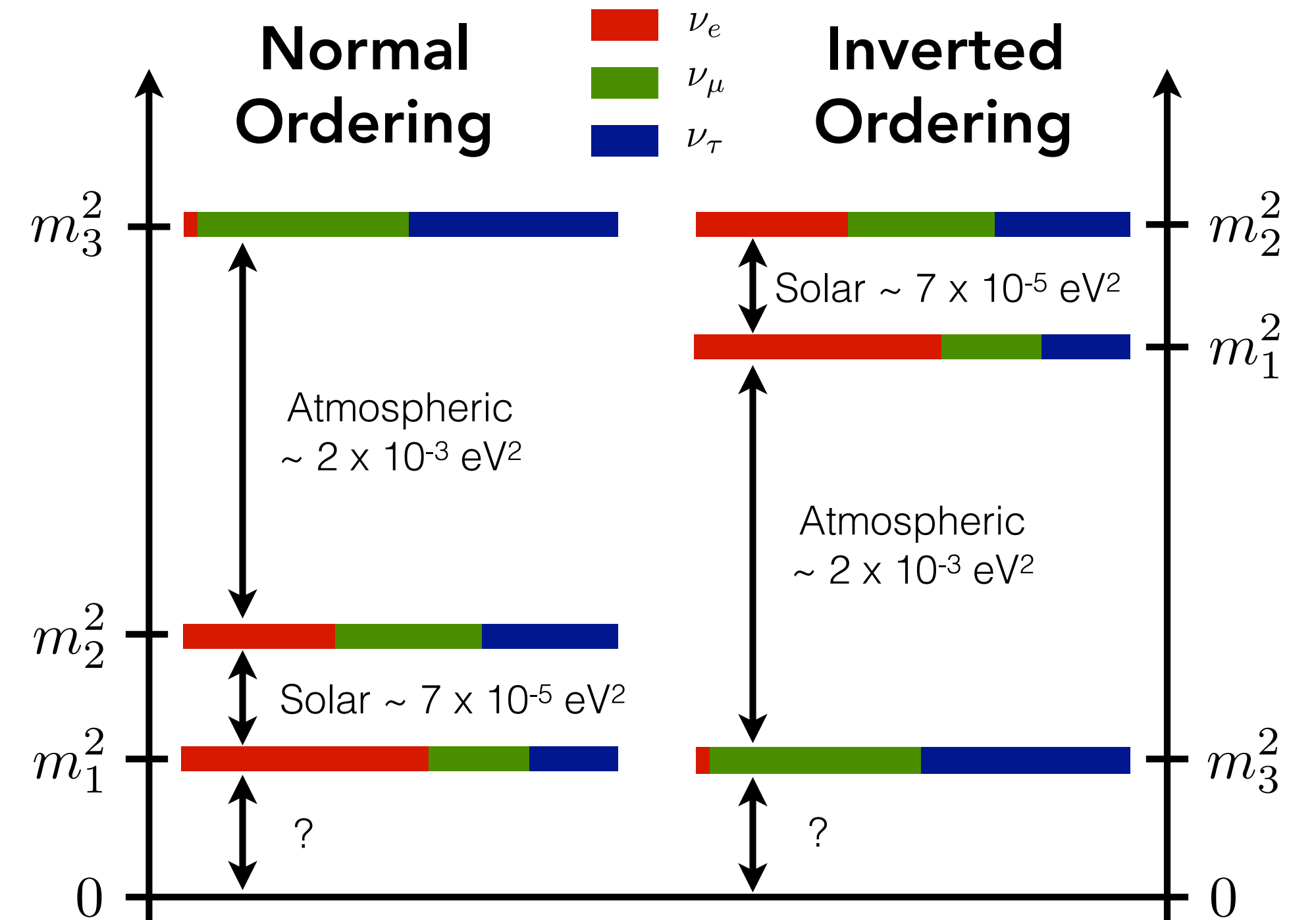
- 3 mixing angles $\theta_{12}, \theta_{23}, \theta_{13}$
- CP-violating complex phase δ^{CP}
 - If $\delta^{\text{CP}} \neq 0, \pi$, then neutrinos and antineutrinos oscillate differently: $P(\nu_\alpha \rightarrow \nu_\beta) \neq P(\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta)$

Key open questions for neutrino oscillation experiments

Is there CP violation in the lepton sector?
(Is $\delta^{\text{CP}} \neq 0, \pi$?)

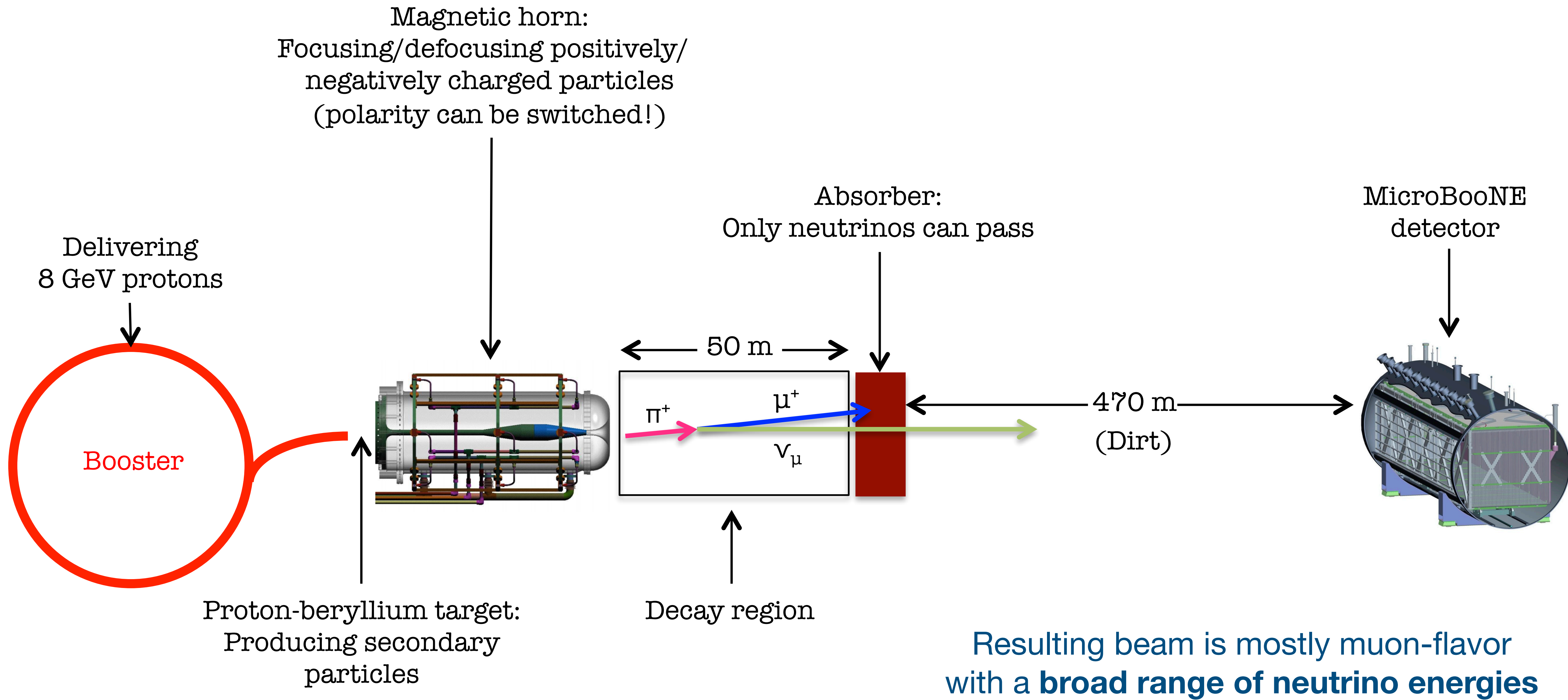
Are there more than 3 neutrinos?
(Sterile: do not participate in weak interactions)

Are there new interactions that we could discover using neutrinos?



What is the neutrino mass ordering?
(Is ν_3 the heaviest or lightest mass eigenstate?)

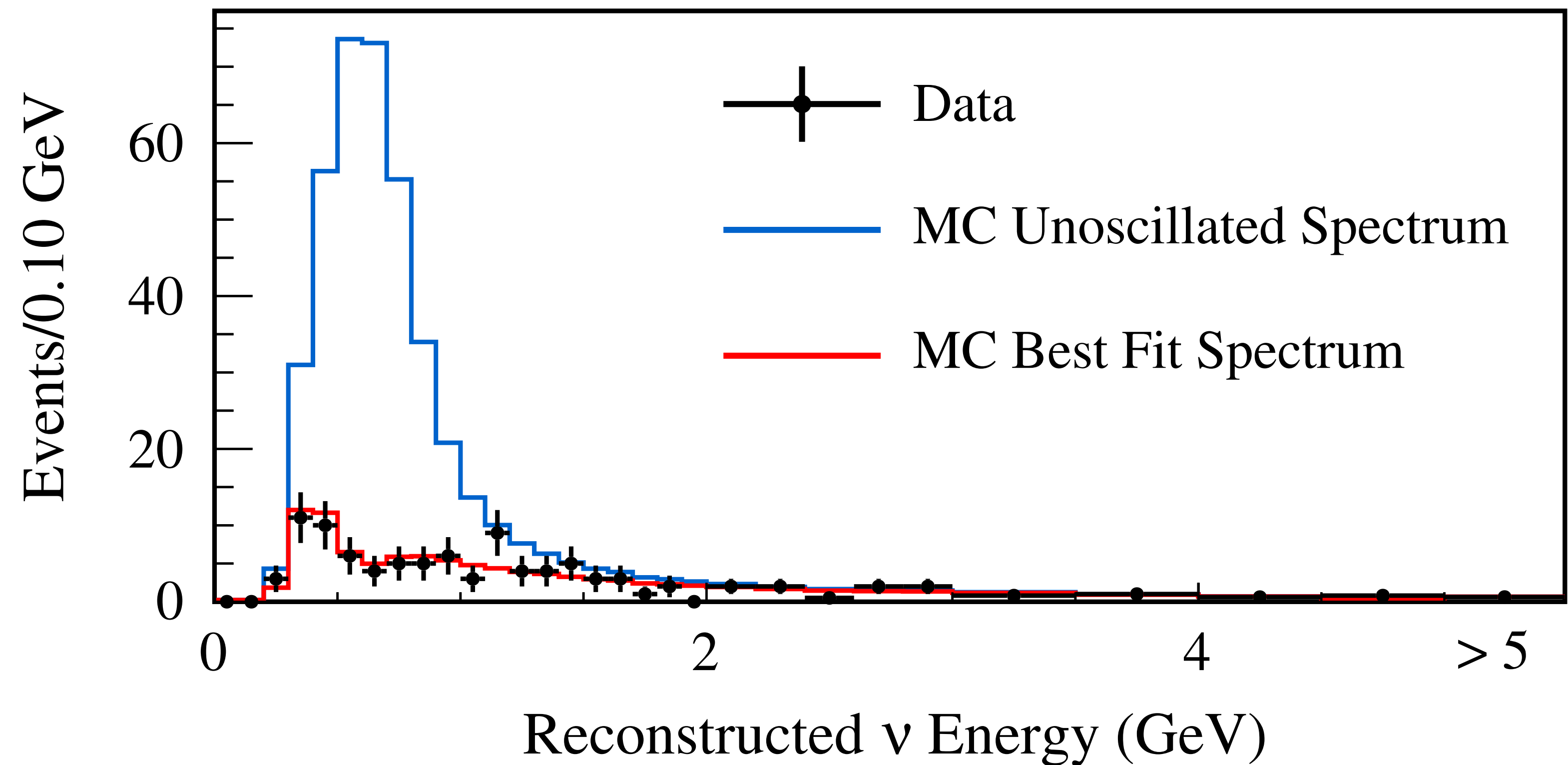
Neutrino production at the Booster Neutrino Beam



Measuring neutrino oscillations

T2K Collaboration, [Phys. Rev. D 91, 072010 \(2015\)](#)

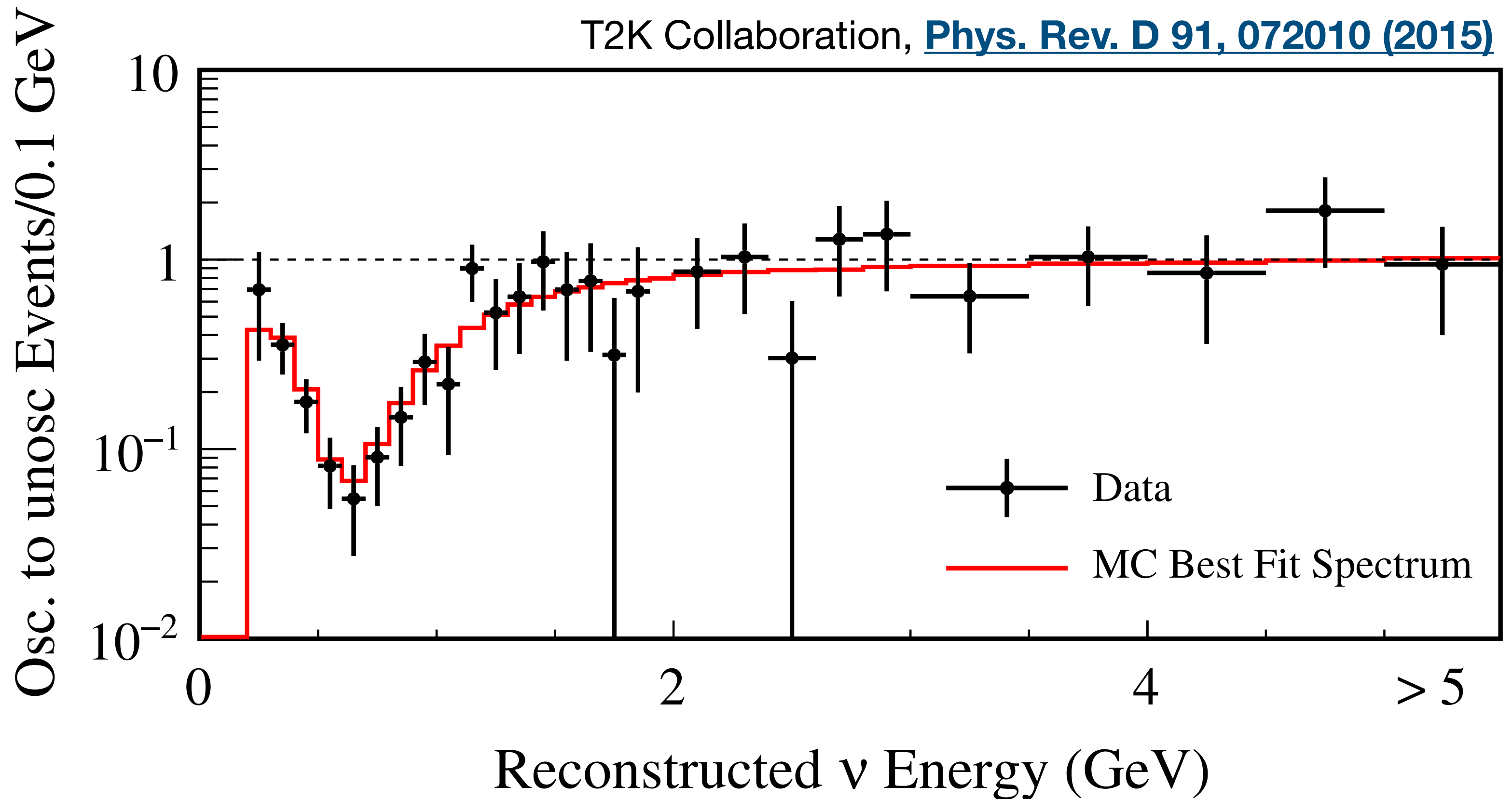
- Experiments typically seek to obtain $P_{\nu_\alpha \rightarrow \nu_\beta}$ from data
 - Measure parameters
 - Test non-standard scenarios
- Not directly observable
 - Compare measured event rate to a no-oscillation expectation
- **Example:** ν_μ disappearance at T2K



1. Count ν_μ as function of energy (**black**)
2. Predict expected result without oscillations (**blue**)
3. Multiply prediction by $P_{\nu_\mu \rightarrow \nu_\mu}$ and fit oscillation parameters (**red**)

Measuring neutrino oscillations

- Experiments typically seek to obtain $P_{\nu_\alpha \rightarrow \nu_\beta}$ from data
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- **Example:** ν_μ disappearance at T2K



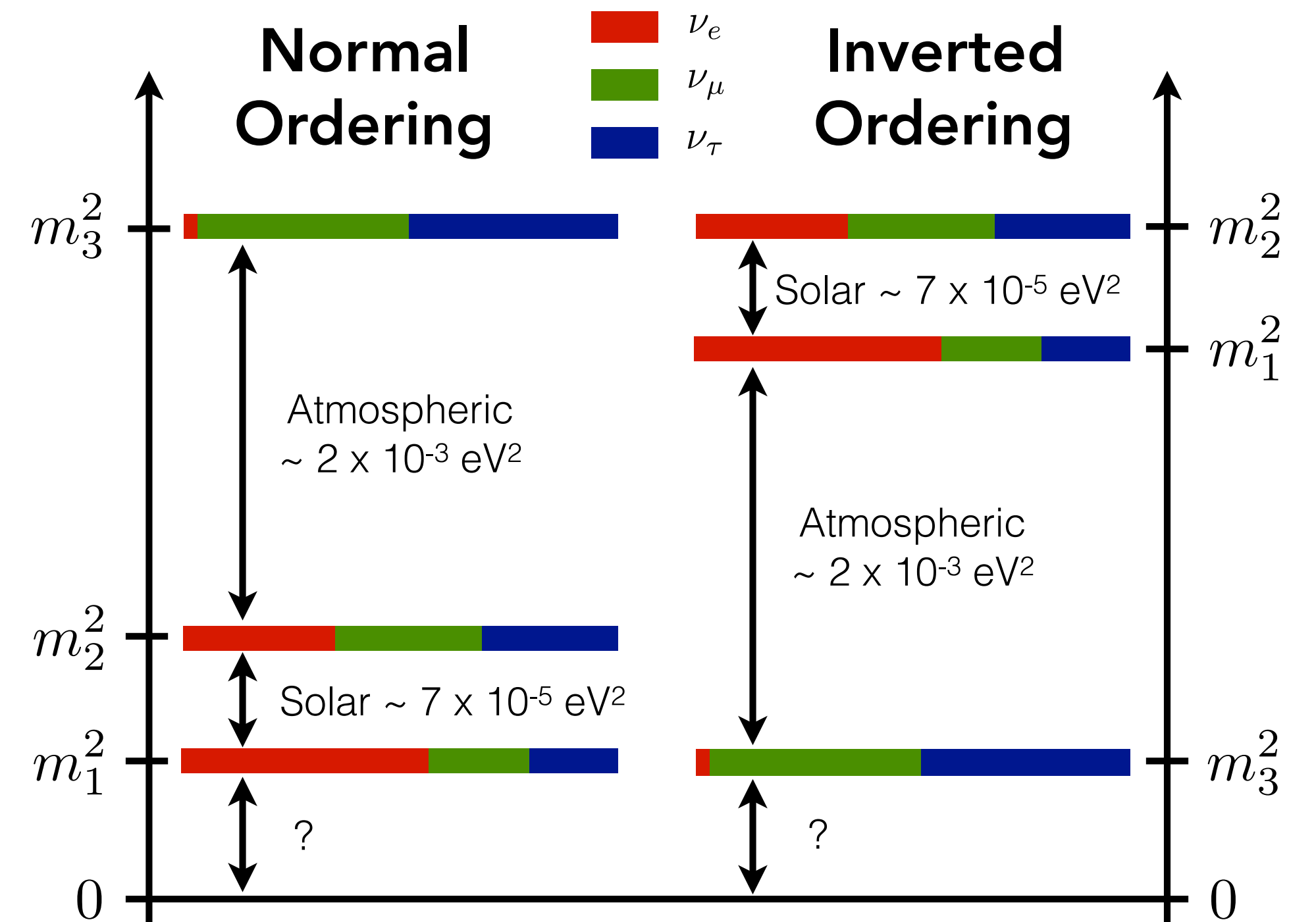
An accurate understanding of **neutrino energy reconstruction** and the **predicted event rate** is critical to
SUCCESS

Key open questions for neutrino oscillation experiments

Is there CP violation in the lepton sector?
(Is $\delta^{\text{CP}} \neq 0, \pi$?)

Are there more than 3 neutrinos?
(Sterile: do not participate in weak interactions)

Are there new interactions that we could discover using neutrinos?



What is the neutrino mass ordering?
(Is ν_3 the heaviest or lightest mass eigenstate?)

Opportunities beyond neutrino properties:

- Natural neutrino sources: solar, supernova, and atmospheric neutrinos
- Rare event searches: proton decay, dark matter, heavy neutral leptons, . . .

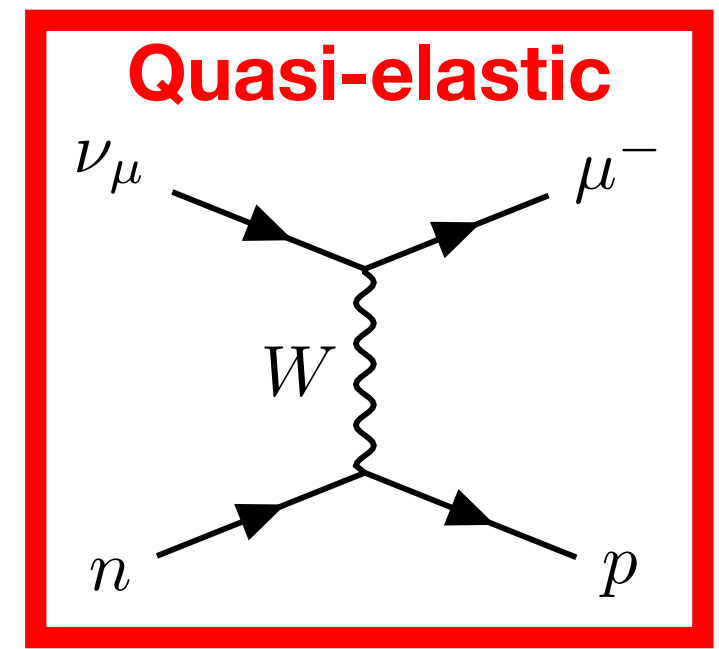
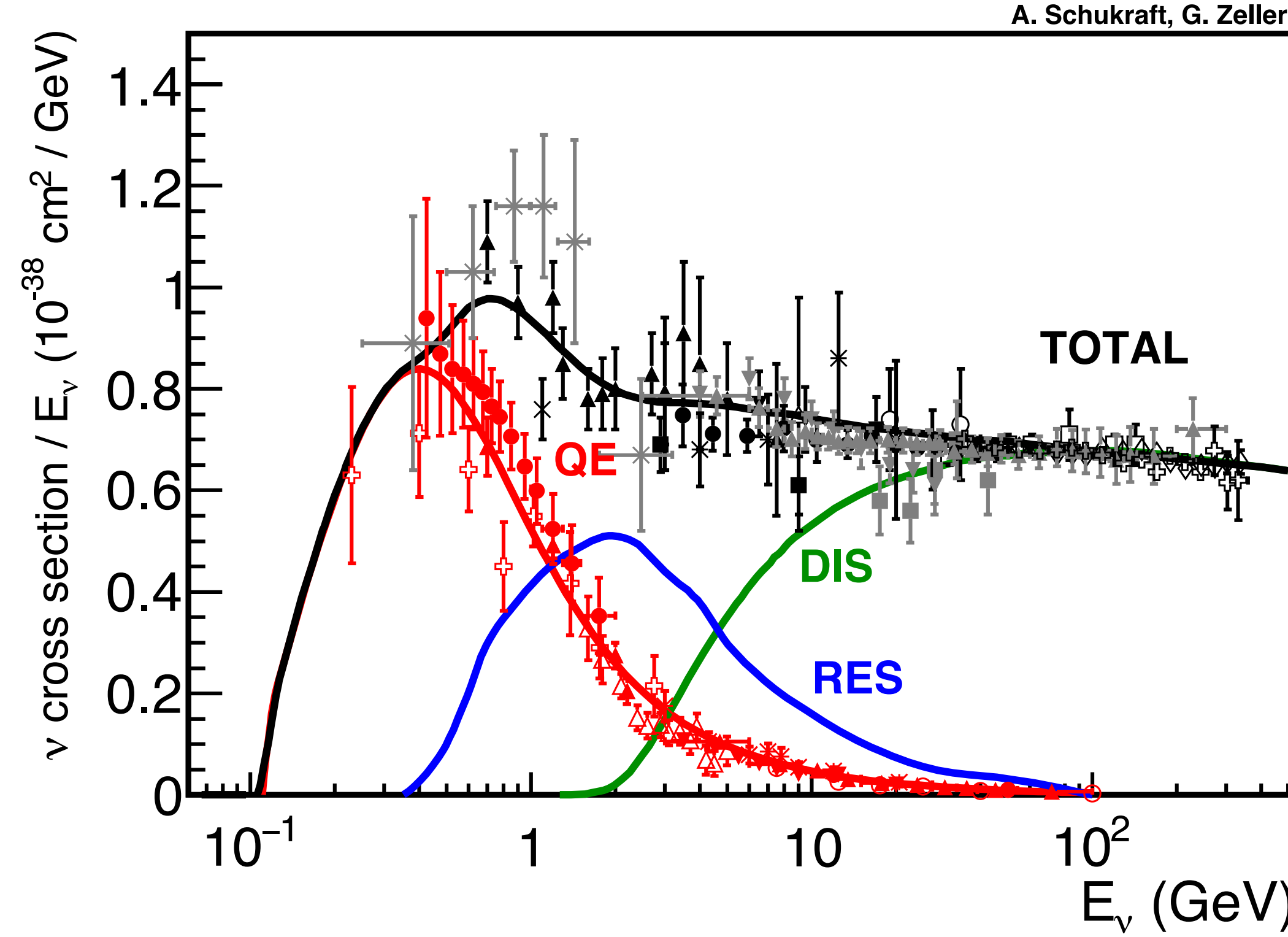
Modeling neutrino-nucleus interactions

- Experiments use cross-section models for critical tasks

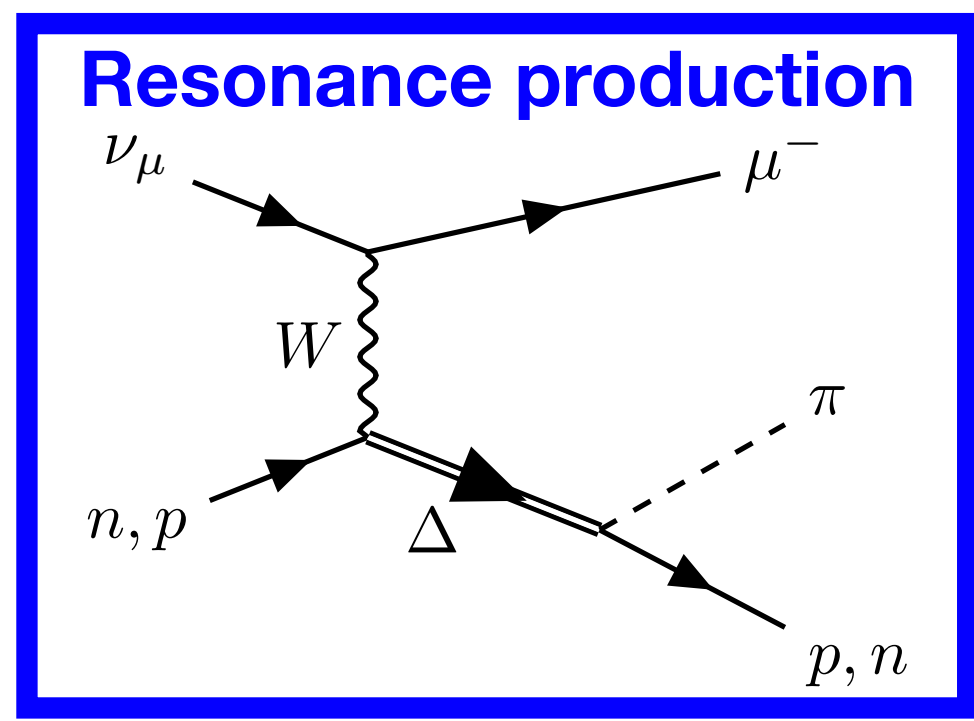
- **Neutrino energy reconstruction**

- Expected event rates
- Efficiency and background corrections
- Systematic uncertainty calculations

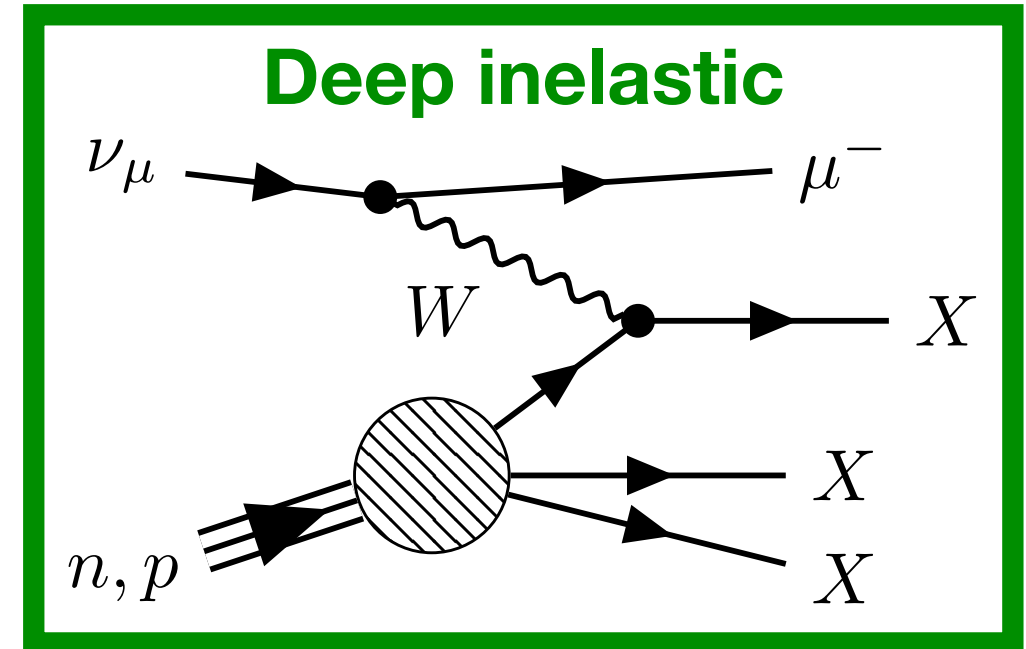
- Measurements essential to constrain and improve models



QE

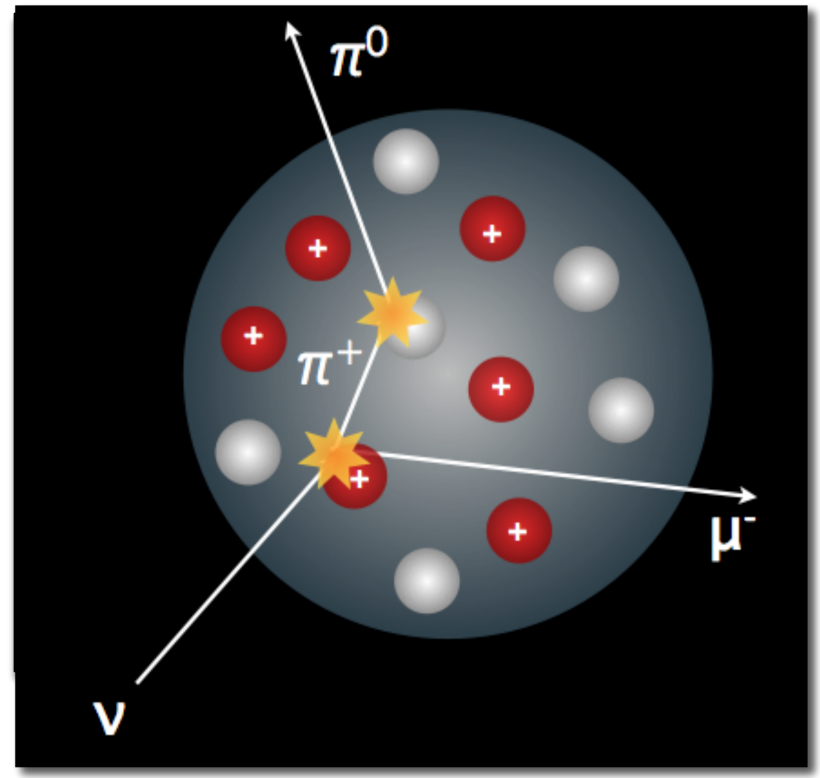


RES

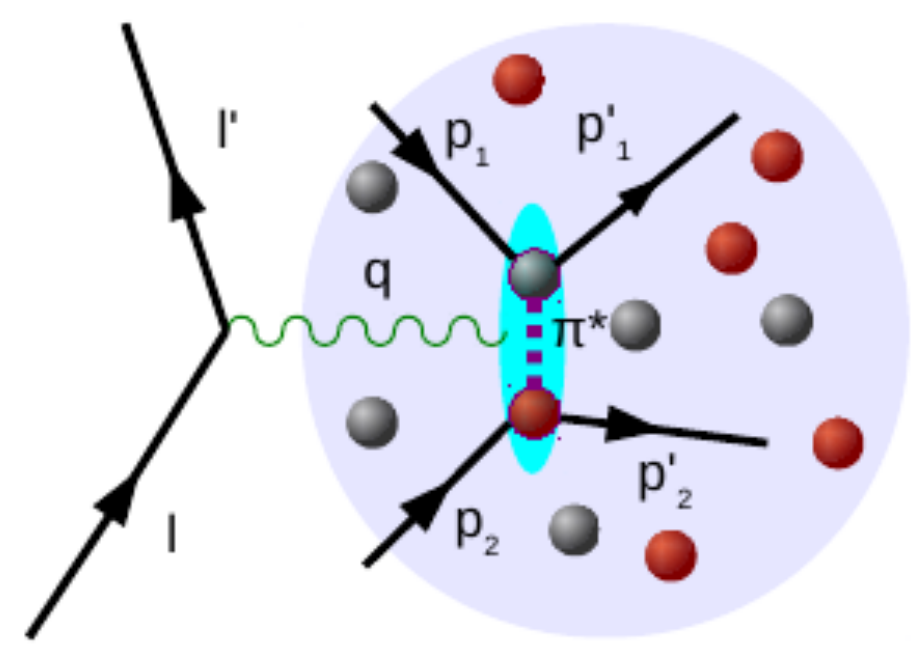


DIS

Final-state interactions (FSIs)



Two-particle two-hole (2p2h) interactions ("MEC")

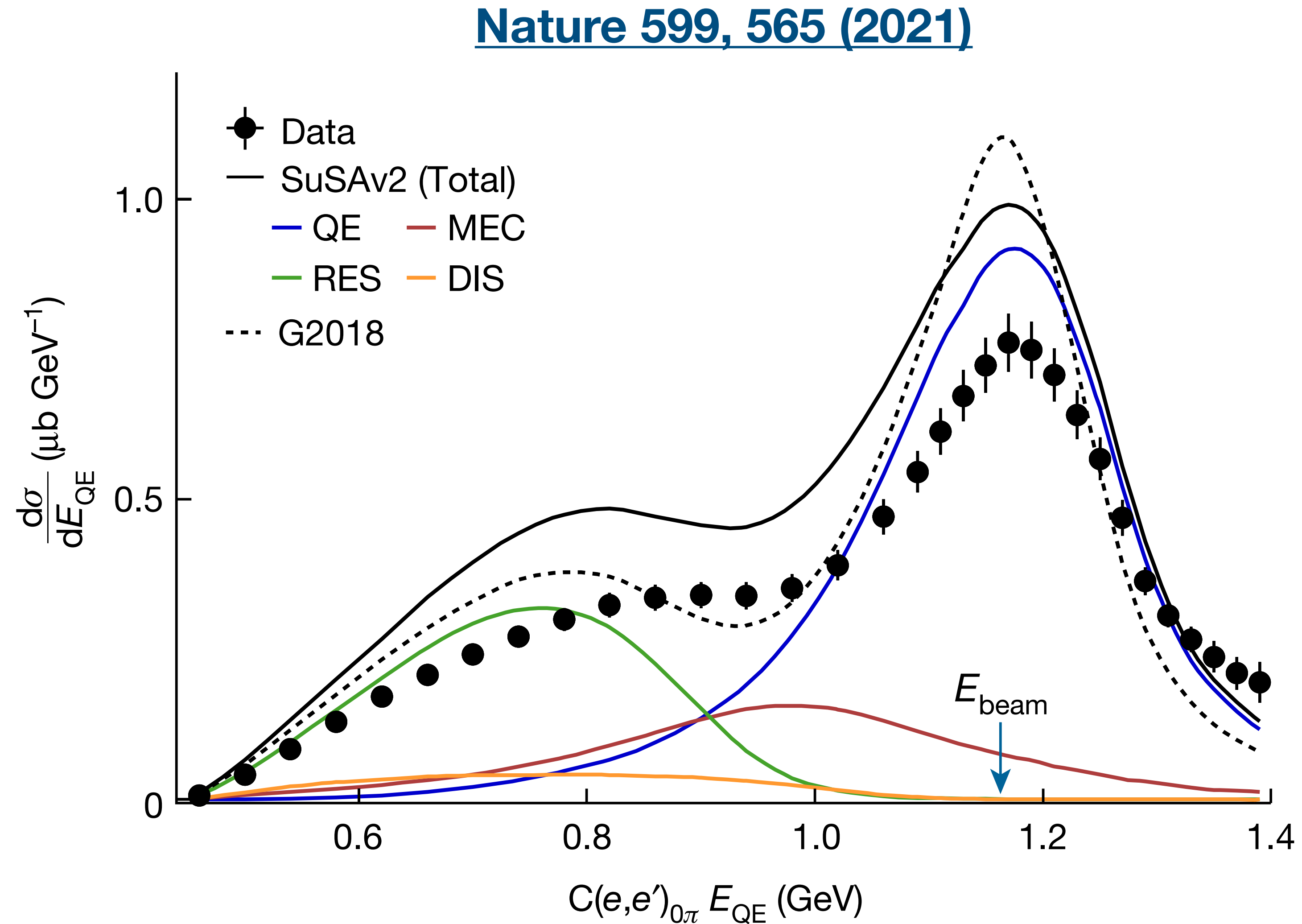


↑
Nucleon-level processes

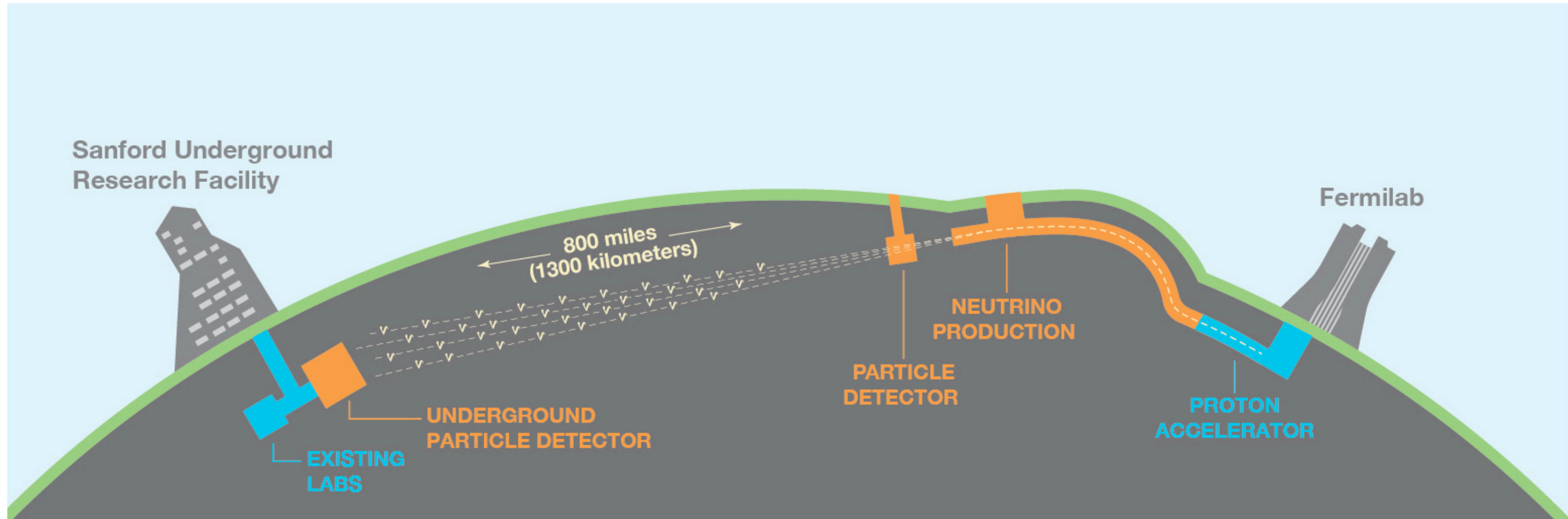
← Nuclear effects

Checking neutrino energy reconstruction with electrons

- Apply neutrino energy estimation methods to electron-nucleus data
 - Monoenergetic beam
 - “Simple” 0π case
- Large fraction of events are misreconstructed
- Current generator-based models describe the bias poorly
 - Clear need (and path) for improvements!

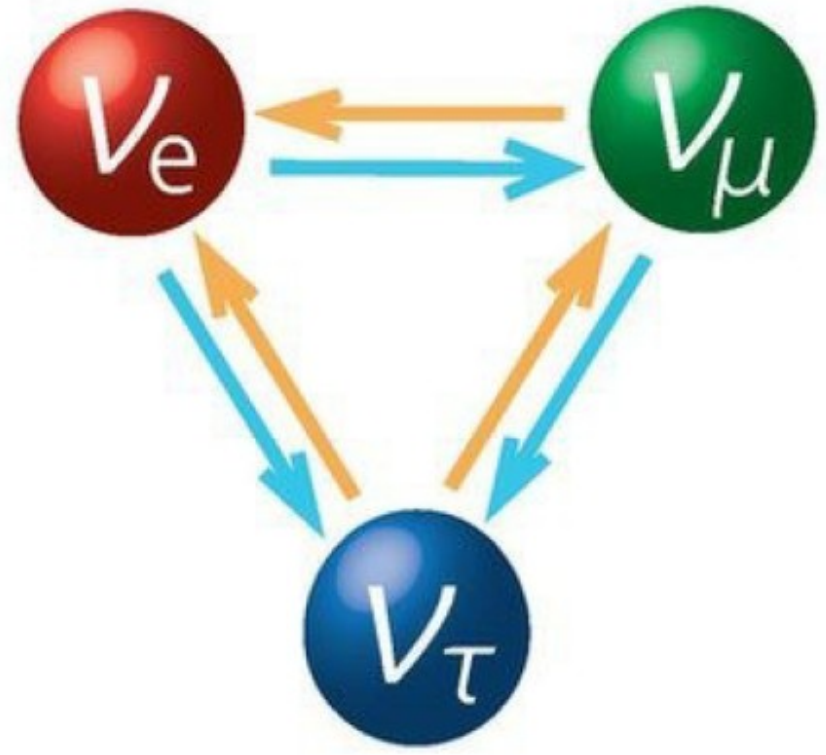


The Deep Underground Neutrino Experiment (DUNE)



- World's most powerful neutrino beam (1.2 MW+) and two groups of detectors
 - **Far detector:** 4 × 17 kton LArTPCs (40 kton total fiducial mass)
 - **Near detector:** Multi-component (including liquid and gaseous argon)
- Data taking to begin circa 2030

Primary science goals of DUNE



Accelerator neutrino oscillations

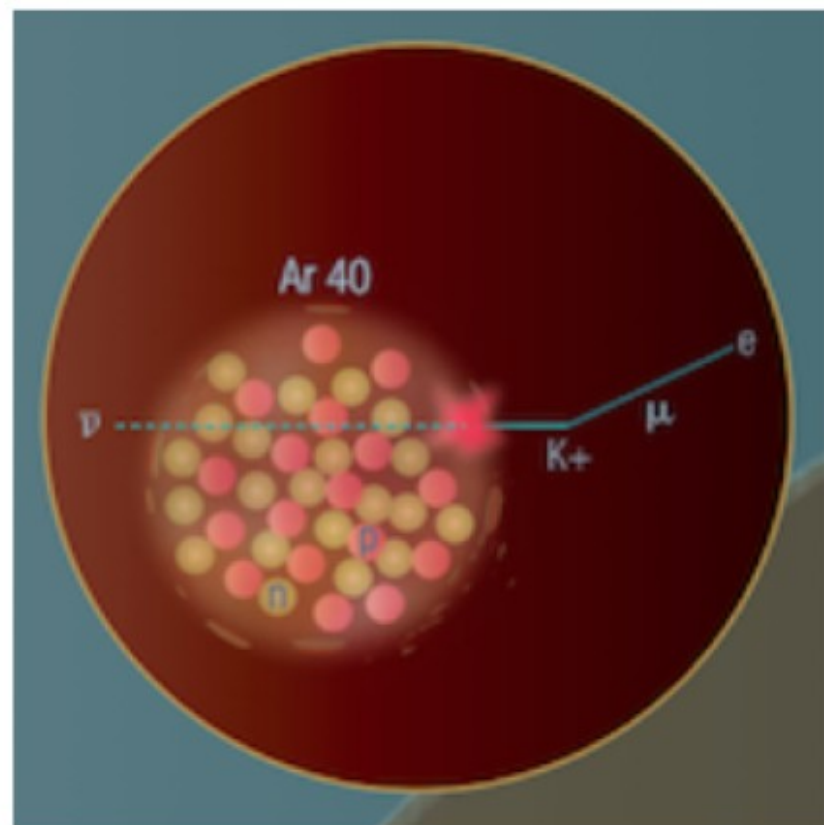
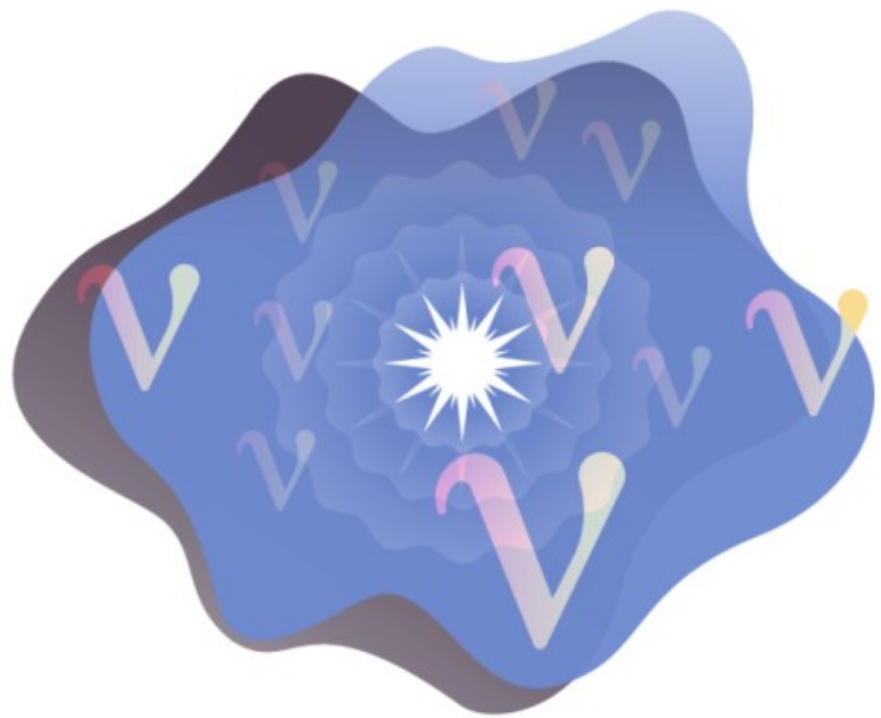
- Search for CP violation ($\delta^{\text{CP}} \neq 0, \pi$)
- Neutrino mass ordering
- Precision mixing parameters

Supernova physics

- Measure O(10 MeV) neutrinos from a galactic supernova
- Unique sensitivity to ν_e component, rich physics potential

Proton decay

- Prediction of many BSM theories
- LArTPC well-suited to some decay modes, e.g., $p \rightarrow K^+ + \bar{\nu}$
- Potential sensitivity to other violations of baryon number ($n \rightarrow \bar{n}$)



Simulating MeV-scale neutrino interactions

- ν -e, ν -p, and CEvNS are “easy”
(the last up to the nuclear form factor)

- Inelastic reactions on complex nuclei are hard

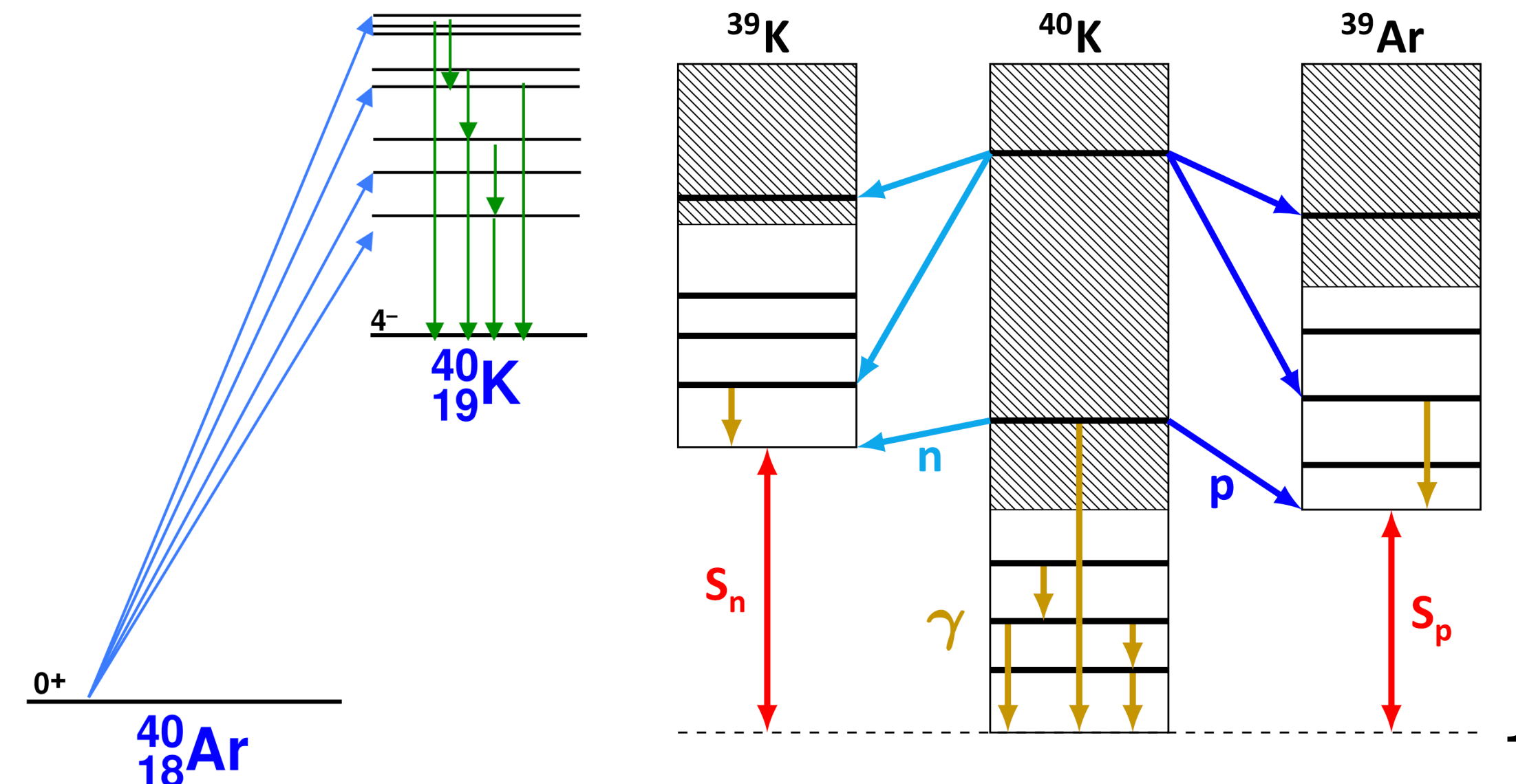
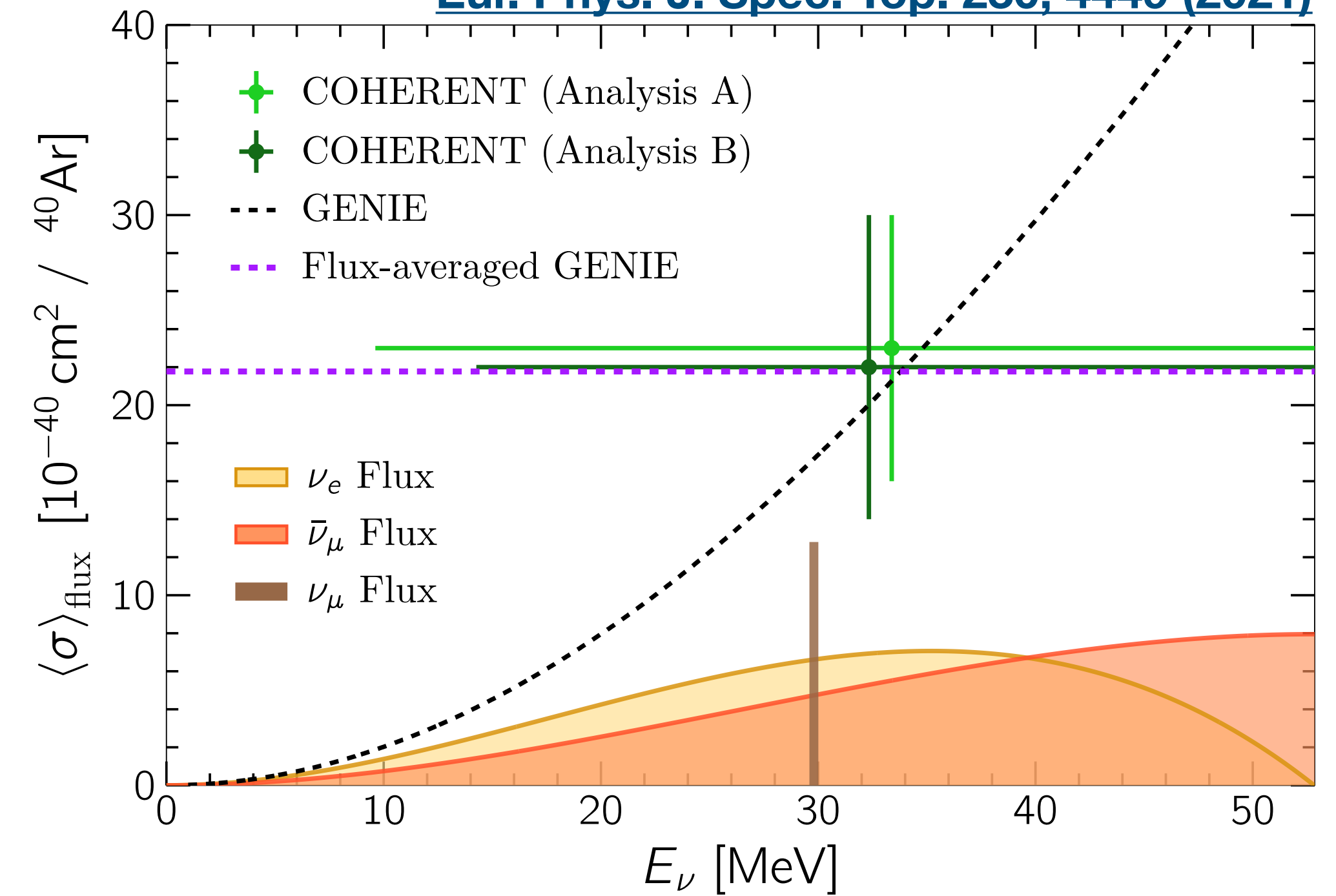
- **Example:** $\nu_e + {}^{40}\text{Ar}$ for supernova detection in DUNE

- Many competing pathways for nuclear (de-)excitation

- Very limited direct constraints from experiment

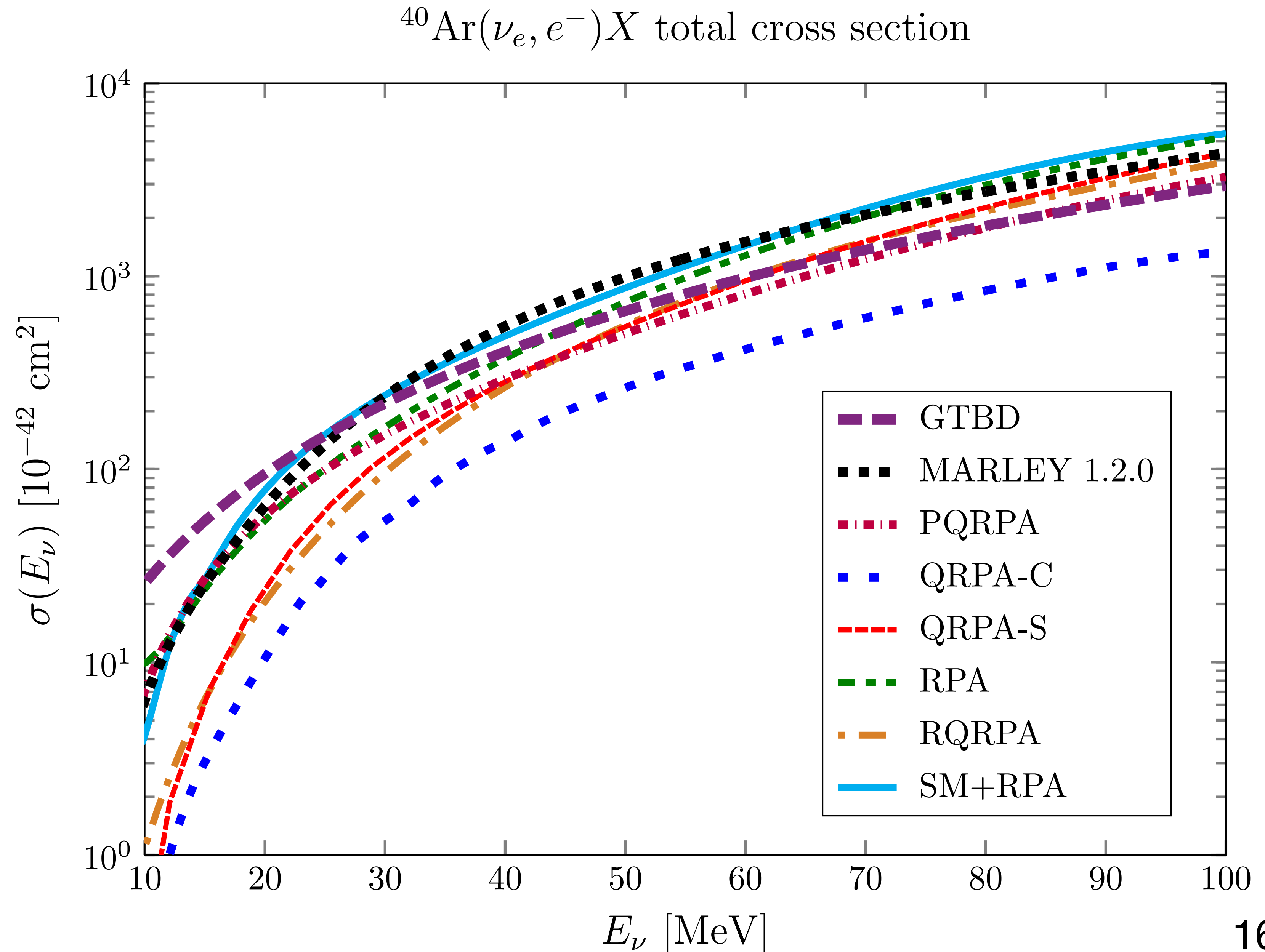
- More details: [Phys. Rev. C 103, 044604 \(2021\)](#)

[Eur. Phys. J. Spec. Top. 230, 4449 \(2021\)](#)



Low-energy CC ν -Ar cross-section uncertainties

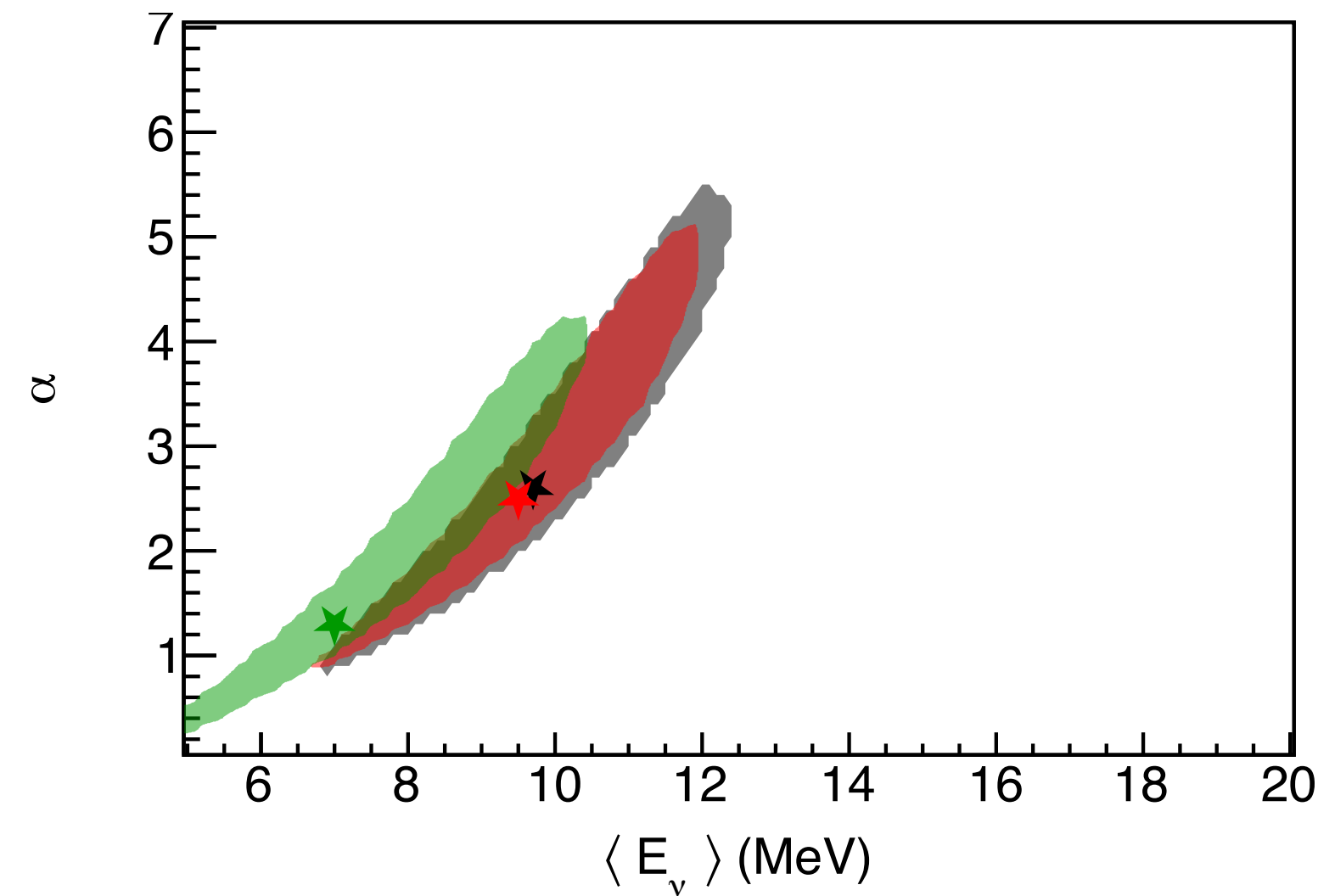
- Significant model disagreements
- No measurements this important channel below 100 MeV
- What is the impact on DUNE supernova physics?



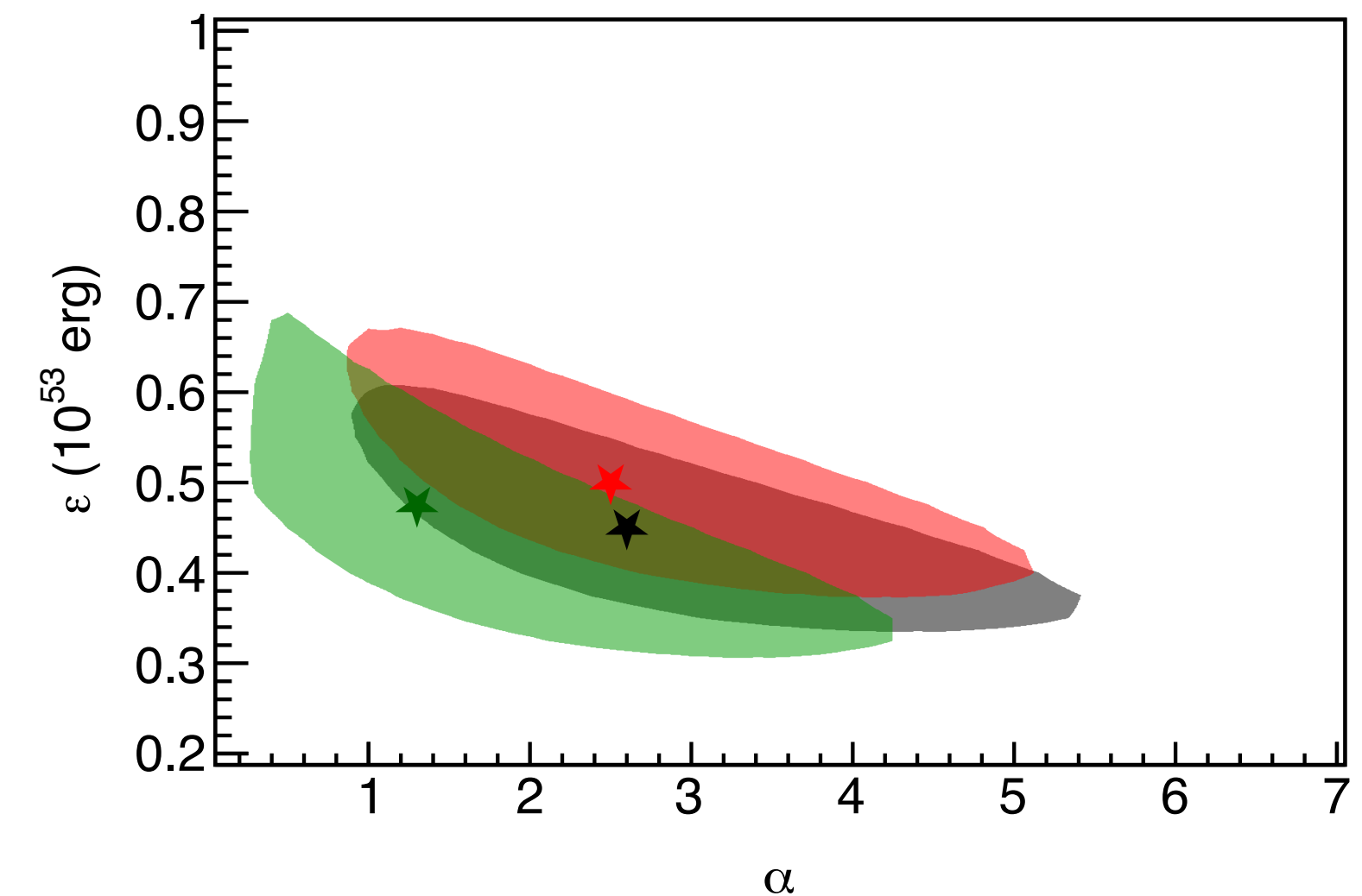
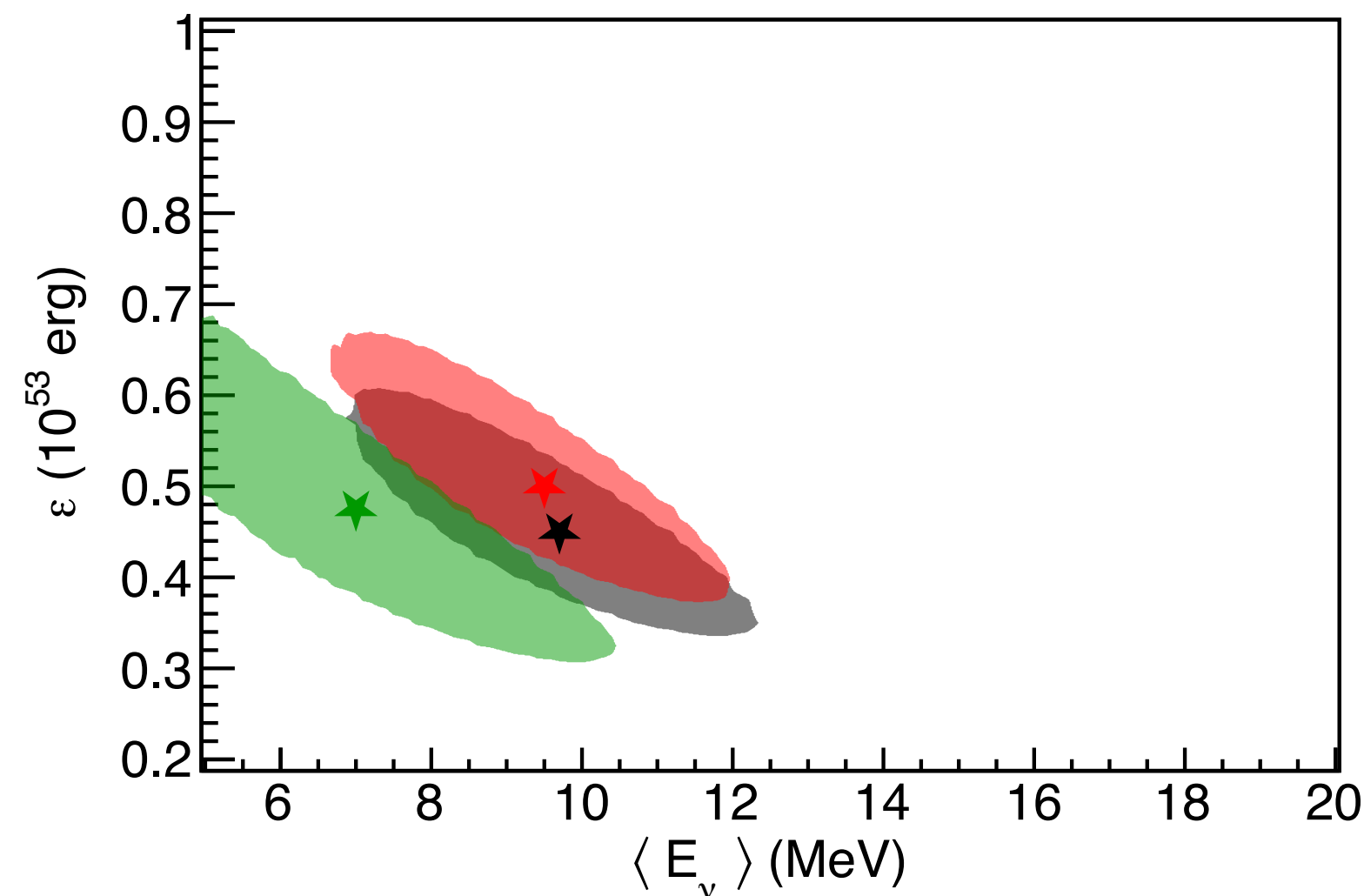
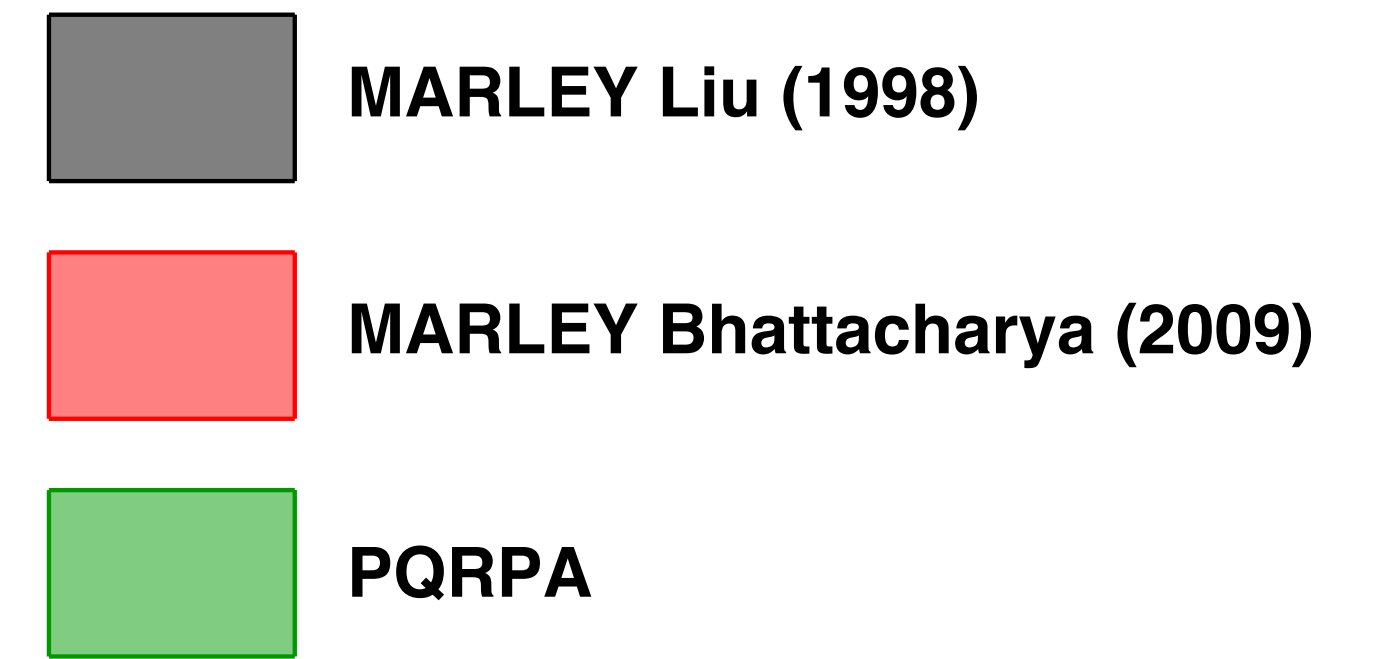
Low-energy CC ν -Ar cross-section uncertainties

E. Conley, S. Gardiner, *et al.*, in prep.

- **Toy analysis** seeks to extract flux parameters from simulated DUNE supernova neutrino data
- \mathcal{E} = energy release (erg)
- $\langle E_\nu \rangle$ = mean neutrino energy (MeV)
- α = shape parameter (dimensionless)

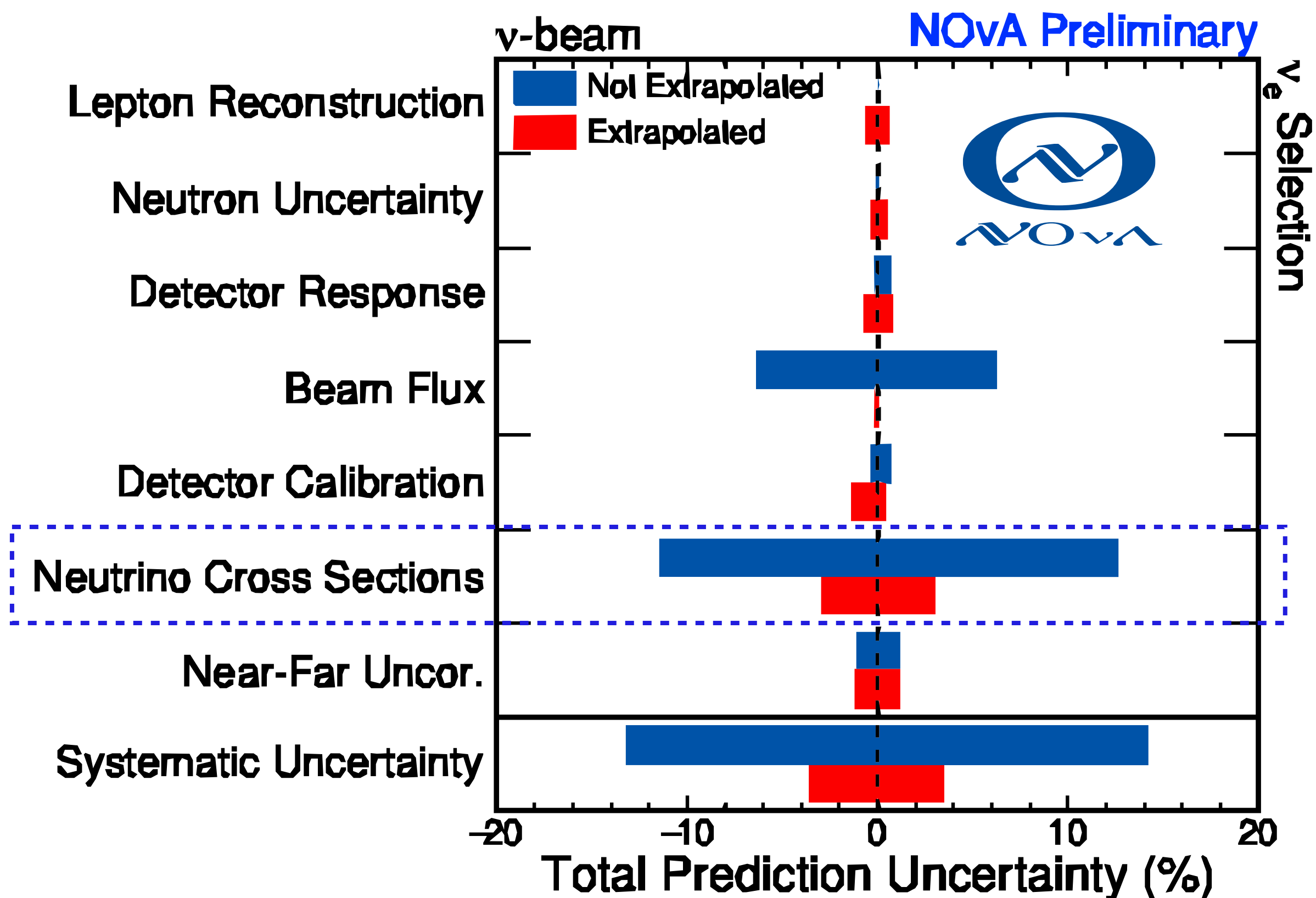


Assumed cross section: Bhattacharya (2009)
with different true scenarios

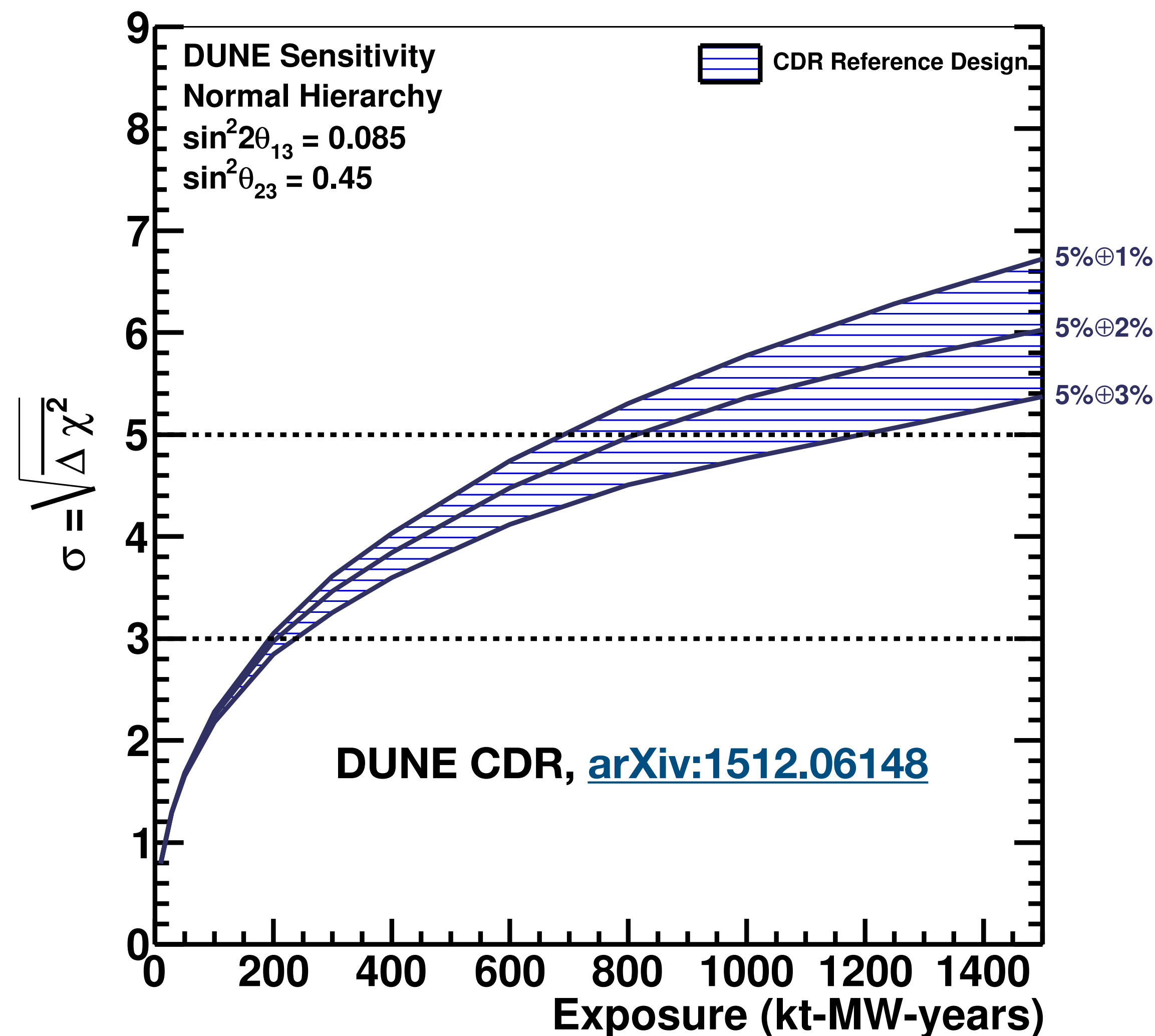


Cross-section systematic uncertainties

M. Elkins & T. Nosek (for NOvA), [Neutrino 2020 poster](#)



50% CP Violation Sensitivity



Typically among the leading uncertainties, and percent-level improvements matter!

Neutrino event generators

- **“Bridge” between theory and experiment:** model predictions are made easily usable
 - Essential for theory efforts to improve experimental precision
- Full final-state predictions needed
 - Efficiencies, backgrounds
- Systematic uncertainty quantification



Neutrino event generator landscape

Four major packages at accelerator energies (~100 MeV to ~20 GeV)

Experiment-focused generators

Meet the needs of current oscillation experiments



[Eur. Phys. J. Spec. Top. 230, 4449 \(2021\)](#)

C++. Primary generator for Fermilab experiments. Largest group (still just a handful of active developers). Ambitions to be the universal platform.

NEUT (no official logo)

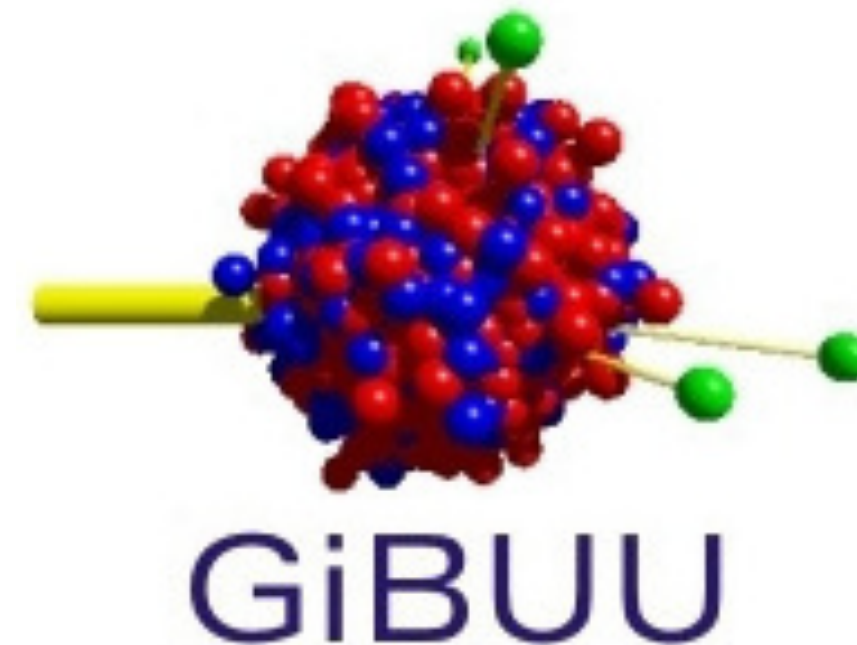


[Eur. Phys. J. Spec. Top. 230, 4469 \(2021\)](#)

C++/Fortran. Primary generator for J-PARC experiments (T2K, Super-K, Hyper-K). Not yet fully open source.

Theory-focused generators

Aid theoretical investigations of neutrino scattering



[J. Phys. G: Nucl. Part. Phys. 46 113001 \(2019\)](#)

Fortran. Supports neutrino projectiles as part of larger framework. Most sophisticated FSI model. Limited infrastructure (no geometry handling, unweighting, etc.)

NuWro



[Nucl. Phys. Proc. Suppl. 229-232, 499 \(2012\)](#)

C++. Many model options, often the first adopter of new theory developments from the literature.

Neutrino event generator landscape

Other notable generators

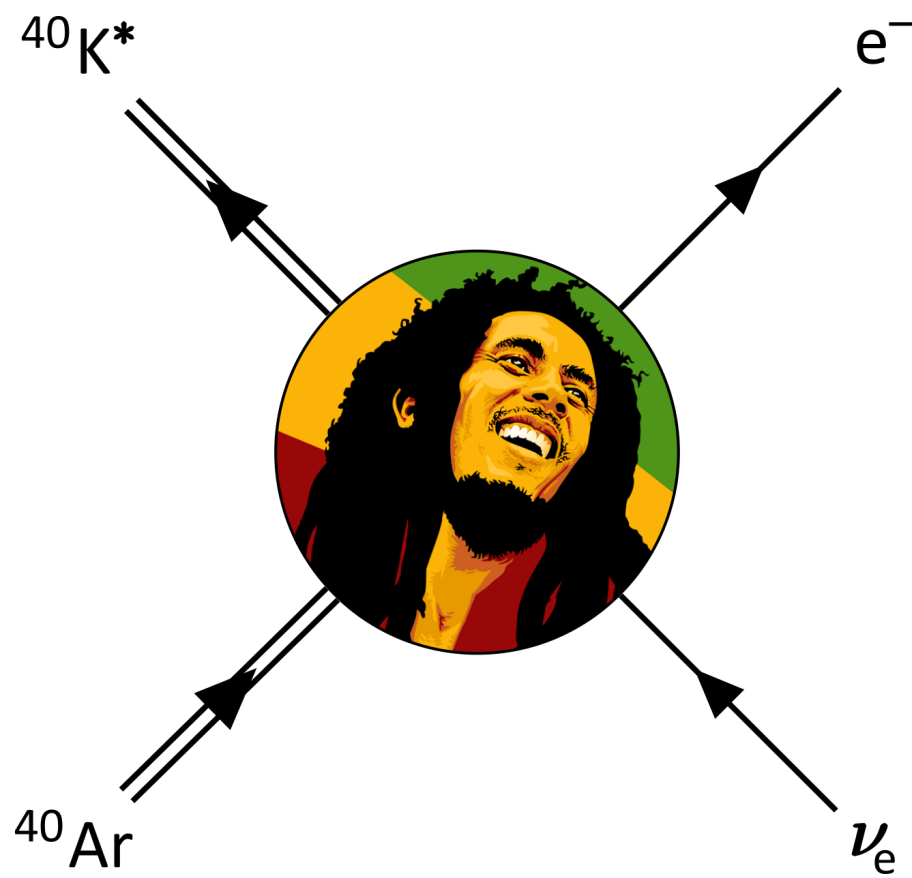
MARLEY

[Comput. Phys. Commun. 269, 108123 \(2021\)](#)

C++. Focus on inelastic ν -nucleus scattering at $O(10 \text{ MeV})$. Used by DUNE for supernova neutrino studies. Single author (for now).

LeptonInjector [Comput. Phys. Commun. 266, 108018 \(2021\)](#)

C++. Generator designed for very high-energy neutrino telescopes. Created by the IceCube Collaboration.



ACHILLES

(no official logo)

[arXiv:2110.15319](#)

C++. In early (but very interesting!) development. Applies techniques from LHC (e.g., n-body phase space, UFO files) to neutrinos for the first time. Emphasis on BSM modeling capabilities.



Coherent elastic neutrino-nucleus scattering (CEvNS)

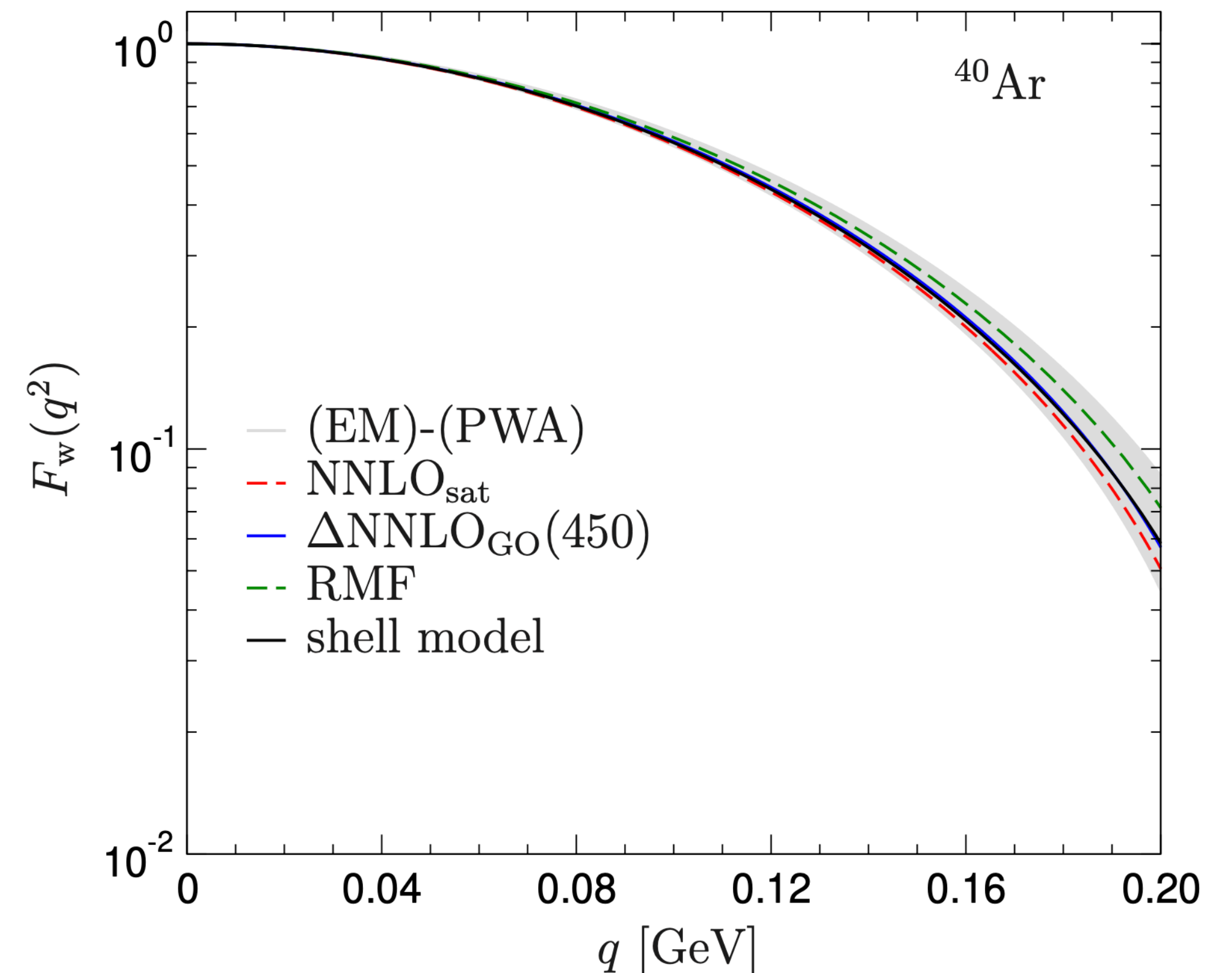
- Dominant nuclear scattering process at low neutrino energy
 - NC, leaves nucleus in ground state
 - First observed by COHERENT in 2017 at ORNL
- Nuclear form factor sensitive to proton/neutron densities
- Precise calculations will enable detailed searches for new physics

Differential cross section

$$\frac{d\sigma}{dT} = \frac{G_F^2 M}{4\pi} \left(1 - \frac{MT}{2E_\nu^2} \right) Q_w^2 [F_w(q^2)]^2$$

Weak nuclear charge

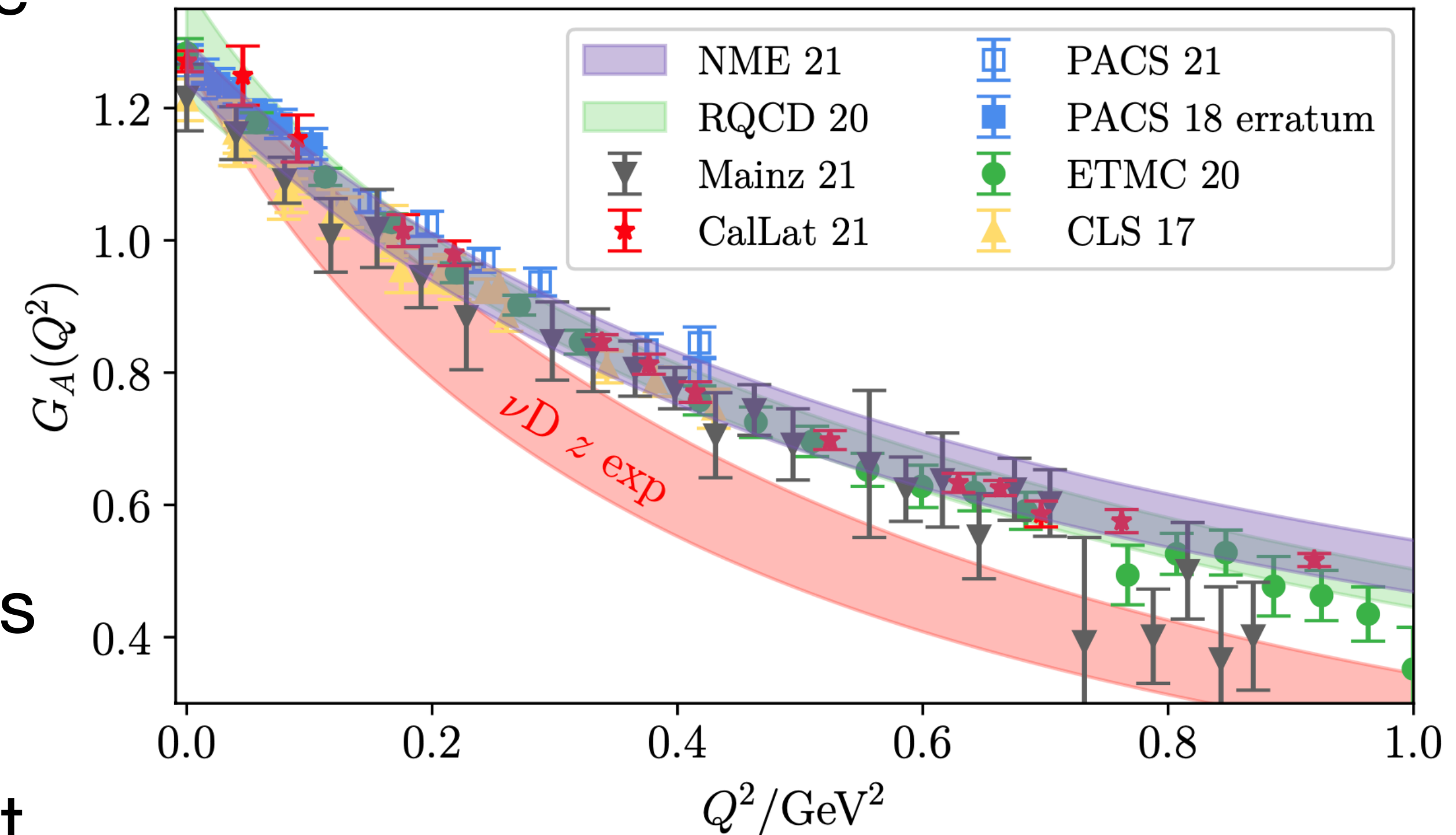
$$Q_w = Z(1 - 4 \sin^2 \theta_W) - N$$



Lattice QCD calculations

$$\langle N' | A_\mu^a | N \rangle = \bar{u}_{N'} \left[G_A(Q^2) \gamma_\mu + \tilde{G}_P(Q^2) \frac{q_\mu}{M_N} \right] \gamma_5 \tau^a u_N$$

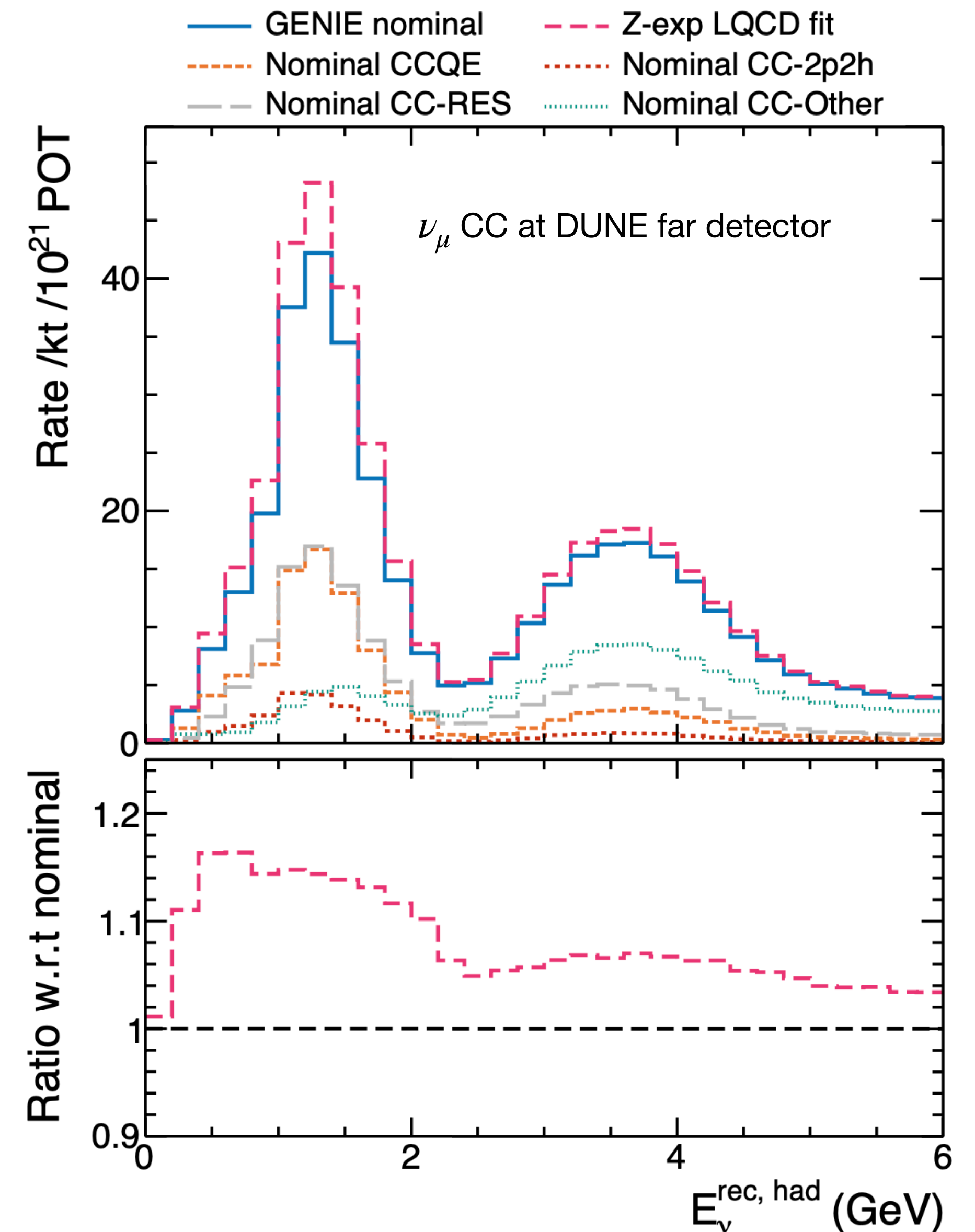
- One- and few-nucleon parameters calculable now (or in the foreseeable future) via lattice techniques
 - Complementary to other approaches
- Example: nucleon axial form factor G_A
 - Key for quasielastic ν scattering
- Tension seen between recent LQCD results and ν D bubble chamber data
 - Impact can be as much as a 10% effect for DUNE ([arXiv:2201.01839](https://arxiv.org/abs/2201.01839))
 - Possible motivation for new measurements



Lattice QCD calculations

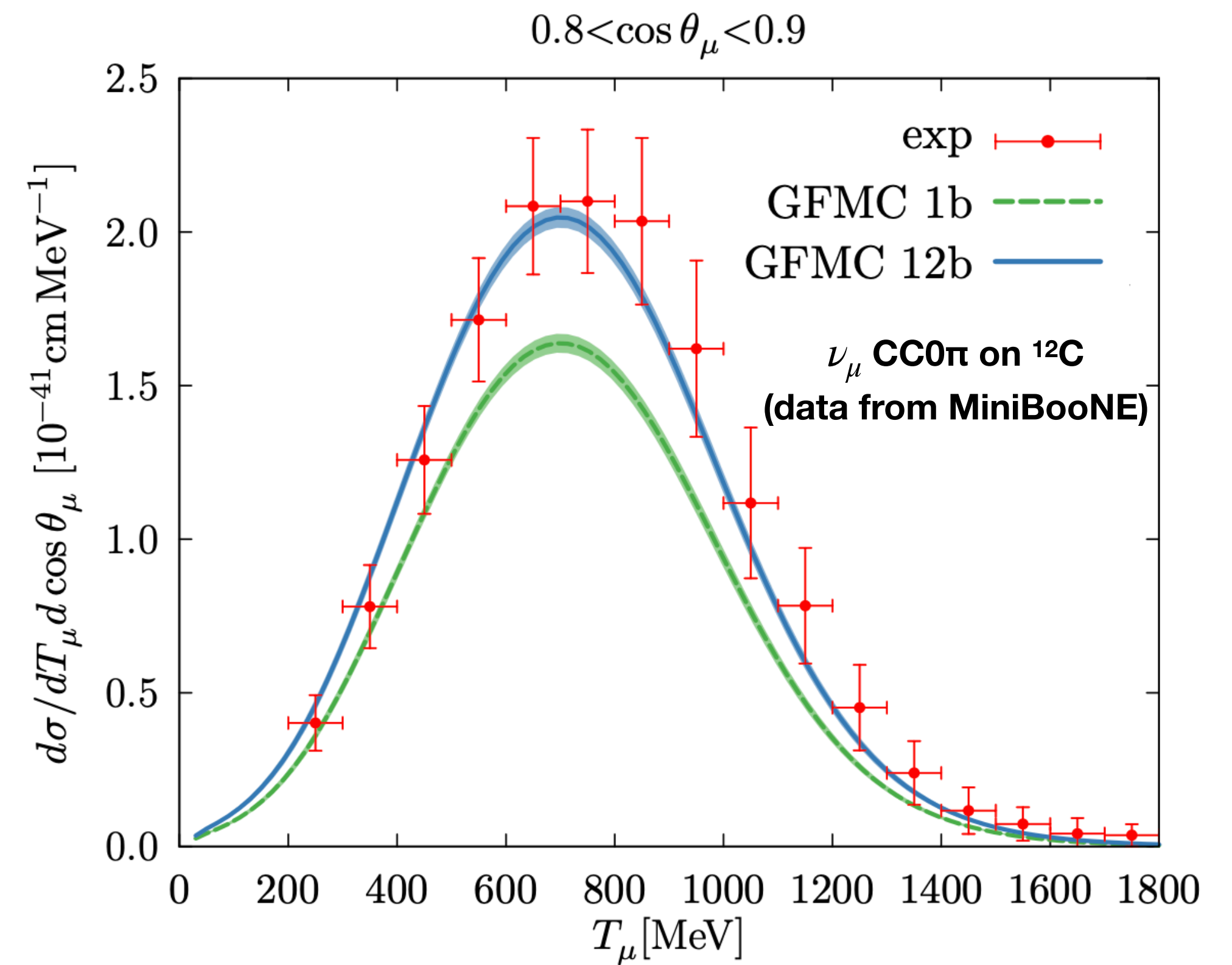
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$$\langle N' | A_\mu^a | N \rangle = \bar{u}_{N'} \left[G_A(Q^2) \gamma_\mu + \tilde{G}_P(Q^2) \frac{q_\mu}{M_N} \right] \gamma_5 \tau^a u_N$$

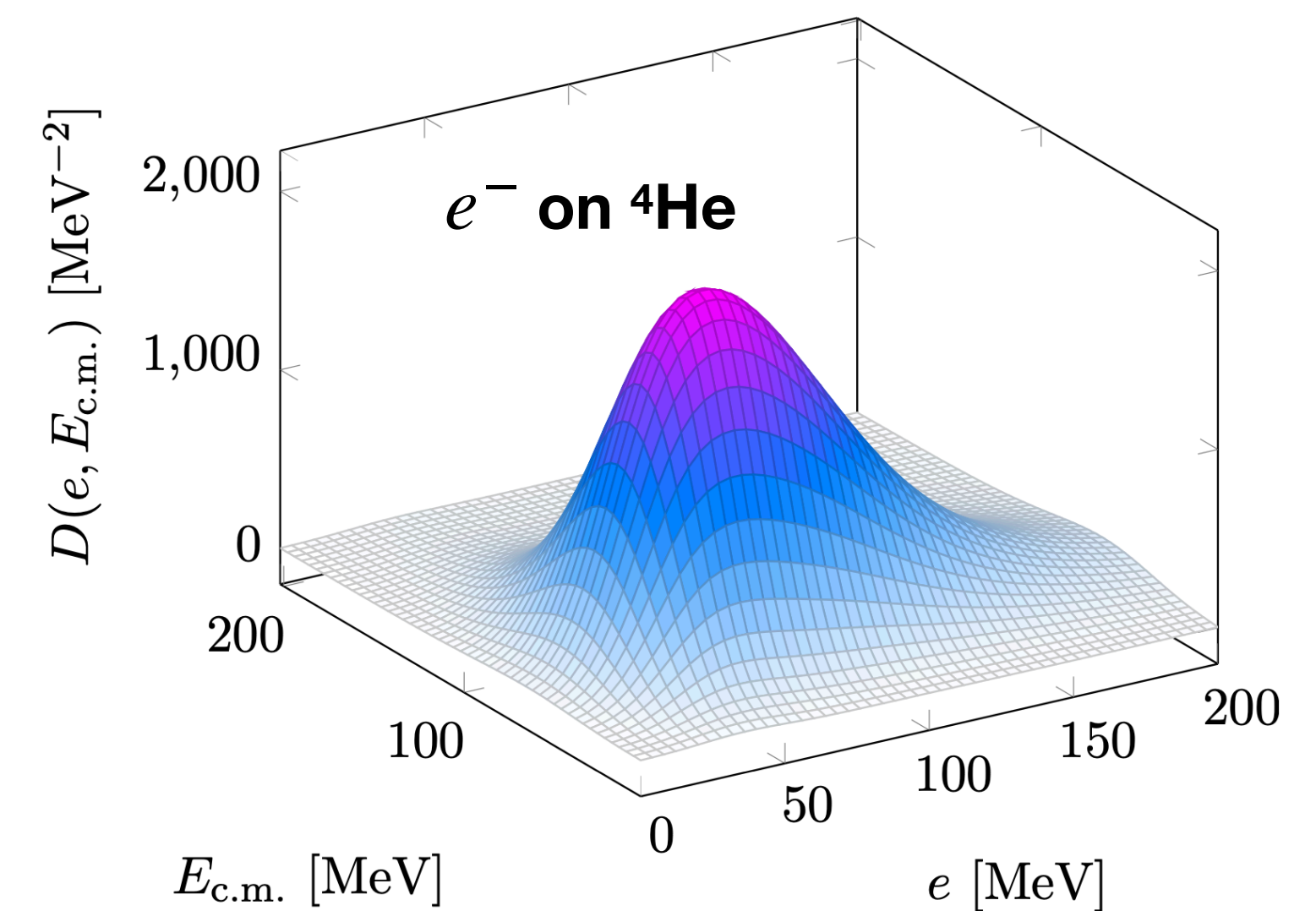


Many-body theory approaches

- Much exciting work on lepton-nucleus scattering
- Includes *ab initio* calculations performed via quantum Monte Carlo (QMC)
 - High-quality description of data
 - Computationally demanding
- Various observables calculable
 - “Response densities” for outgoing nucleon kinematics



Transverse Density $q = 500 \text{ MeV}/c$



GENIE hadronic tensor interface

Differential cross section built from contraction of two tensors

$$\frac{d^2\sigma}{dE'_\ell d\Omega'_\ell} \propto L_{\mu\nu} W^{\mu\nu}$$

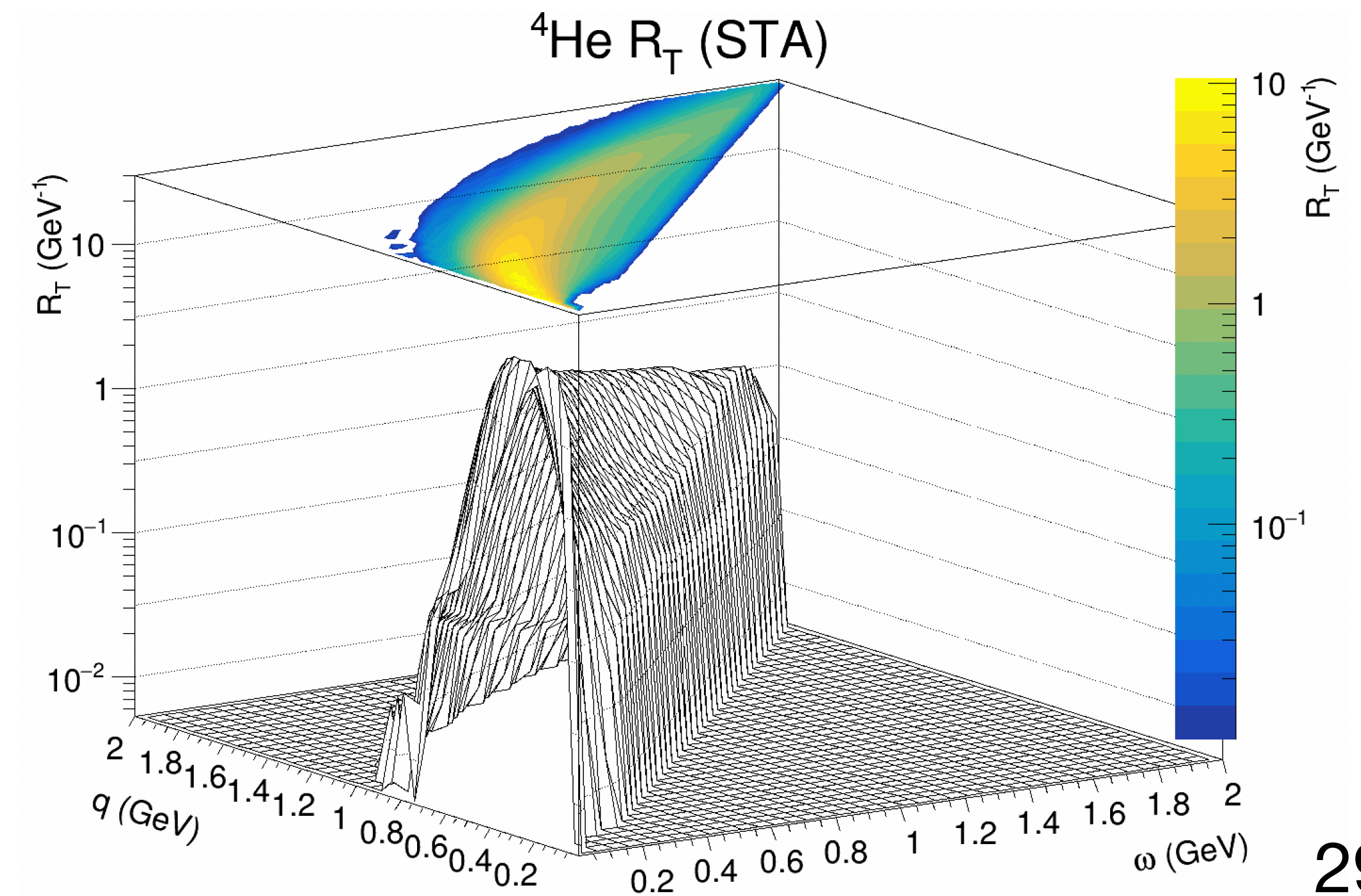
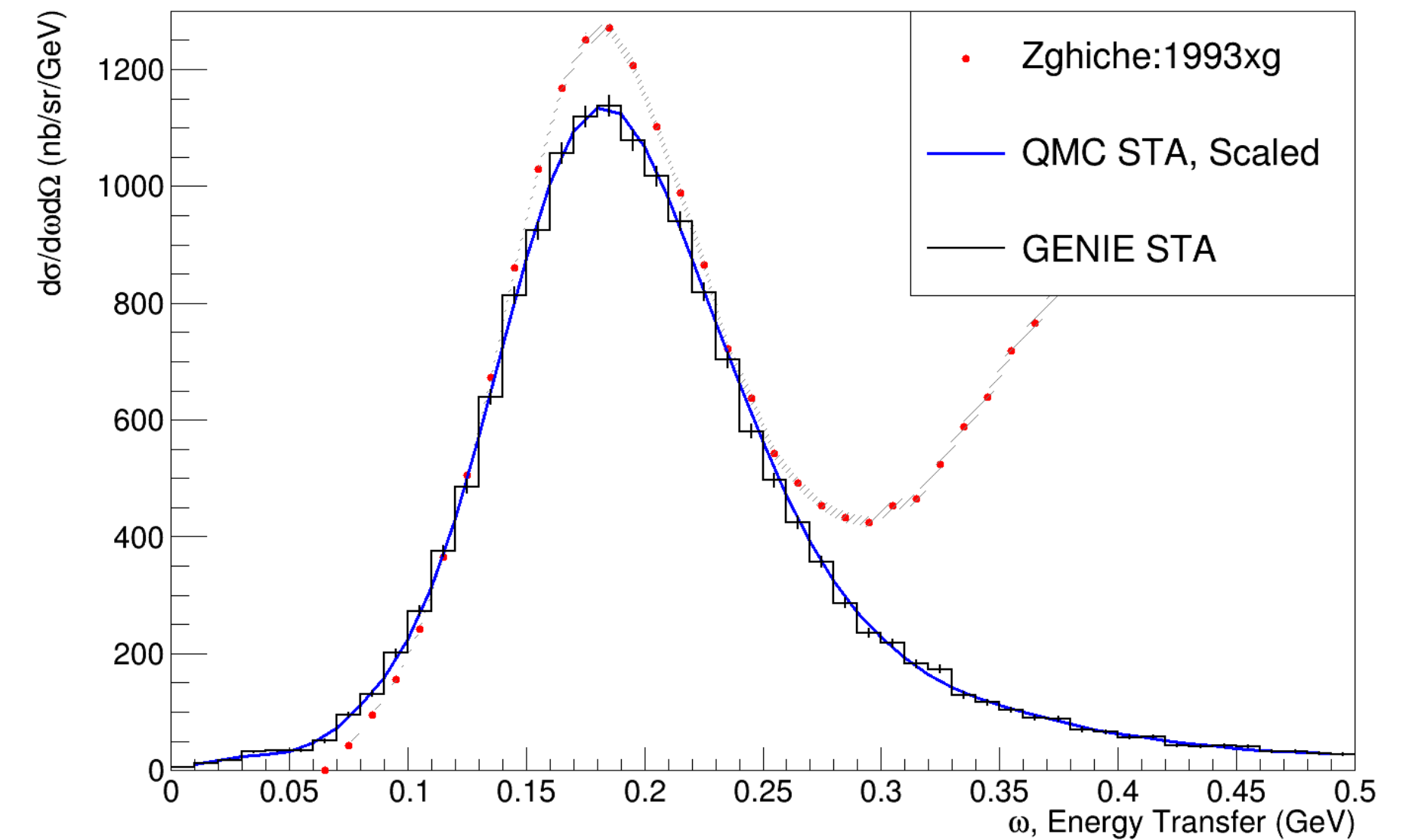
Exploit symmetries: only 5 components of $W^{\mu\nu}$ are needed for weak processes

Only two for EM: $R_L = W^{00}$ and $R_T = W^{11}$

Precomputed tables of these allow for **efficient interpolation**

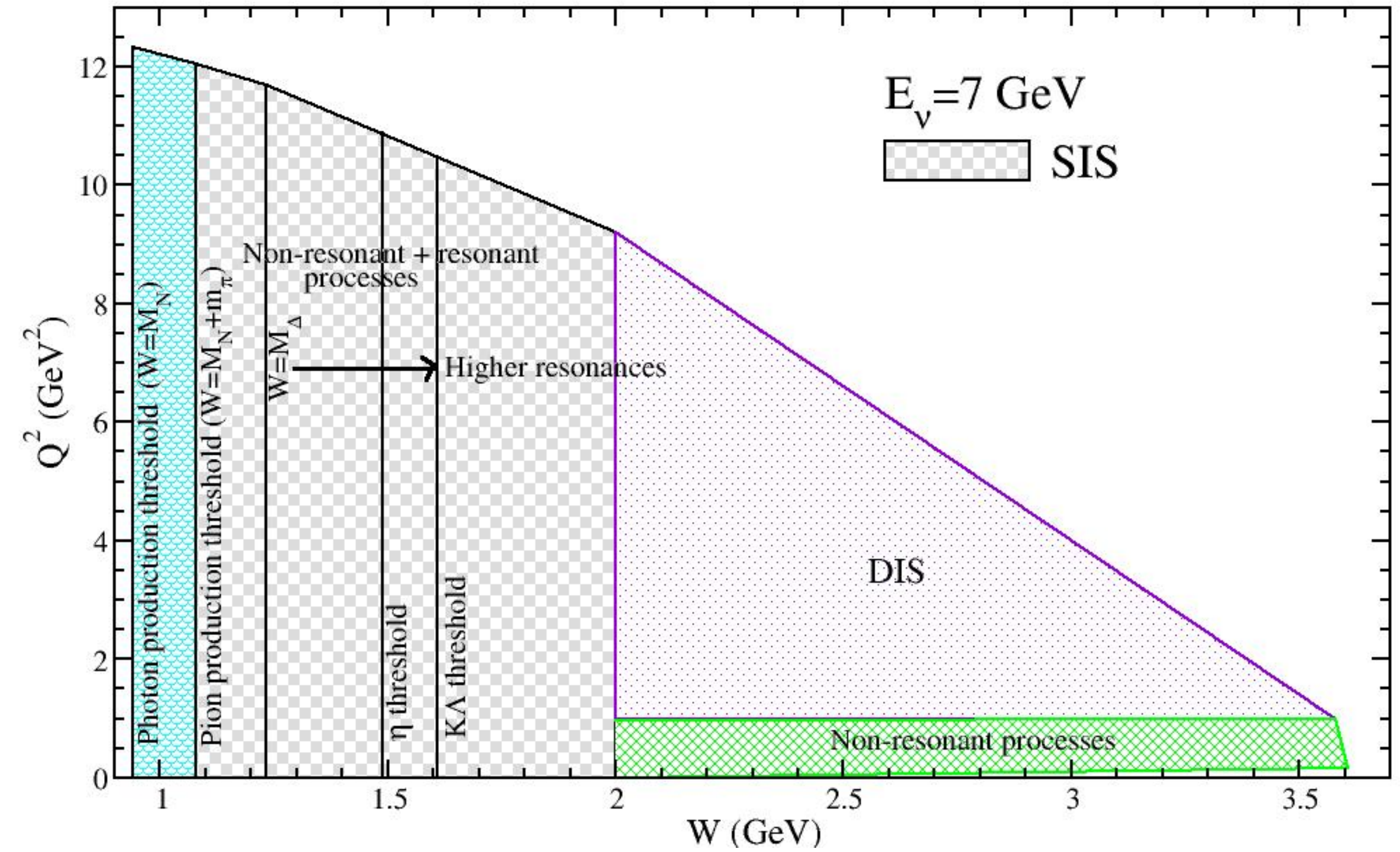
[Phys. Rev. D 103, 052001 \(2021\)](#)

Z = 2, A = 4, Beam Energy = 0.64 GeV, Angle = $60^\circ \pm 0.25^\circ$

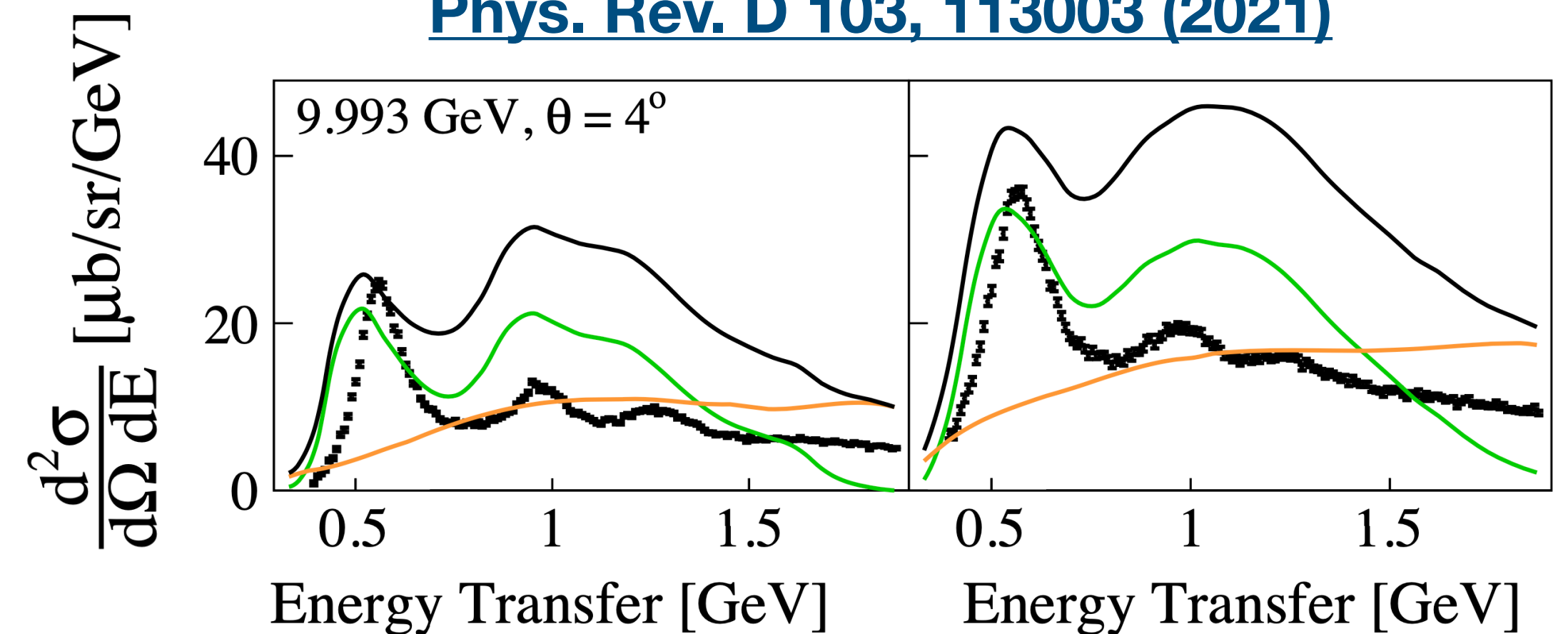


Shallow and deep inelastic scattering

- SIS = transition region between hadronic and quark + gluon representations
 - Poorly understood, but important for precision GeV-scale experiments
- Generators typically extrapolate from the DIS region
 - Checks of GENIE against electron data reveal major trouble
- Further theoretical & experimental attention to this region will be helpful!

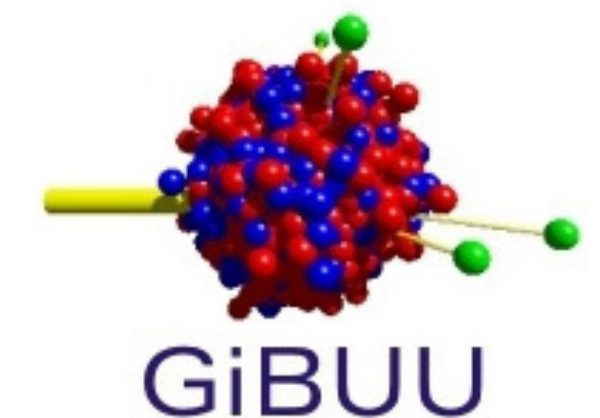


[Phys. Rev. D 103, 113003 \(2021\)](#)



Sociological & organizational issues for neutrino generators

- Mission critical, but in a “no man’s land” between theory & experiment
 - Currently poor career incentives, motivation for short-term solutions
 - Recruiting, training, and retaining junior scientists becomes difficult
- HEP motivation, but NP expertise needed for a solution
- No clear community leadership structure
 - GENIE authors, for example, typically have other responsibilities
- Priorities hard to establish without new infrastructure investment
 - Global tunes, apply model variations to expected DUNE sensitivity, etc.
- Likely some challenges in common with comparable LHC efforts



“We’re ~20 years behind the LHC folks”

- An assessment not original to me, but one that I agree with
- Many problems we’re beginning to face have known LHC solutions
 - High-multiplicity events (n-body phase space generation)
 - Generator interoperability (standardization, HepMC3)
 - Tuning & systematics (Professor)
- Continued dialog with you will be very helpful
 - In return, we can offer solidarity in advocating for the importance of HEP generator work (e.g., [arXiv:2203.11110](https://arxiv.org/abs/2203.11110)) to the whole community
- I look forward to future opportunities to learn and collaborate!