



Measuring leptonic CP violation at the second neutrino oscillation maximum with ESSnuSB

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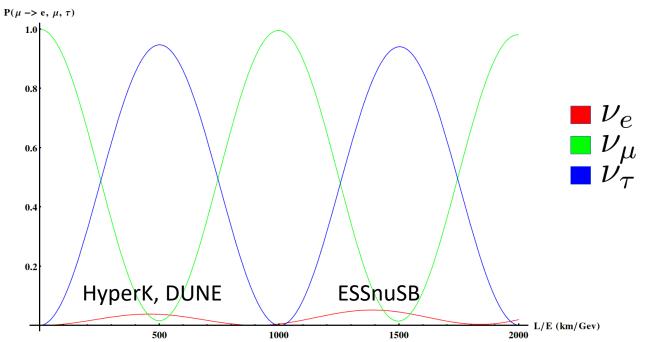


CERN EP Seminar 12 April 2022



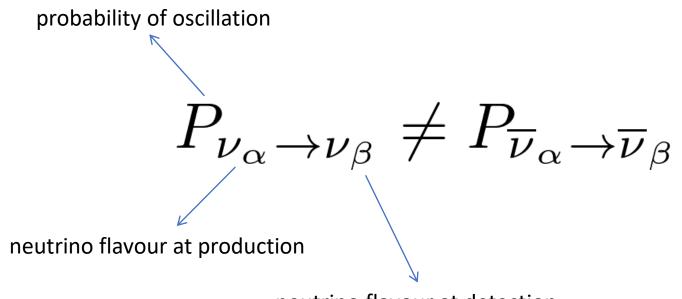
ESSnuSB

A design study for an experiment to measure CP violation at 2nd neutrino oscillation maximum.



CP violation in neutrino oscillations

Oscillation probability for neutrinos is different than oscillation probability for anti-neutrinos in vaccum.



neutrino flavour at detection

CP violation in ESSnuSB

$$P_{\nu_{\mu} \to \nu_{e}} \neq P_{\overline{\nu}_{\mu} \to \overline{\nu}_{e}}$$

We will study v_e and \overline{v}_e appearance in v_μ and \overline{v}_μ beam, respectively

The plan:

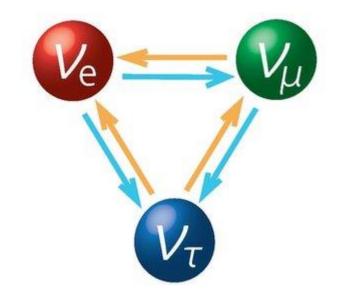
- 1. Run with ν_{μ} and look at ν_{e} appearance, then
- 2. Run with \overline{v}_{μ} and look at \overline{v}_{e} appearance

Why 2nd maximum?

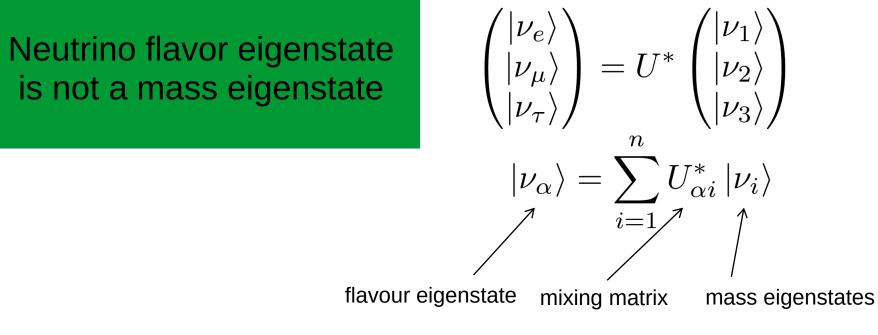
Large signal and small matter effects

Neutrino oscillations

Neutrino flavour can effectively change between its creation and interaction.



Neutrino oscillations



has a mass m_i

- $U_{\alpha i}$ is called the PMNS (Pontecorvo-Maki-Nakagawa-Sakata) matrix
- $U_{\alpha i}$ must be unitary for probability conservation
 - for *n* generations of neutrinos it is a *n* x *n* complex matrix
 - here we focus on standard 3 neutrino generations

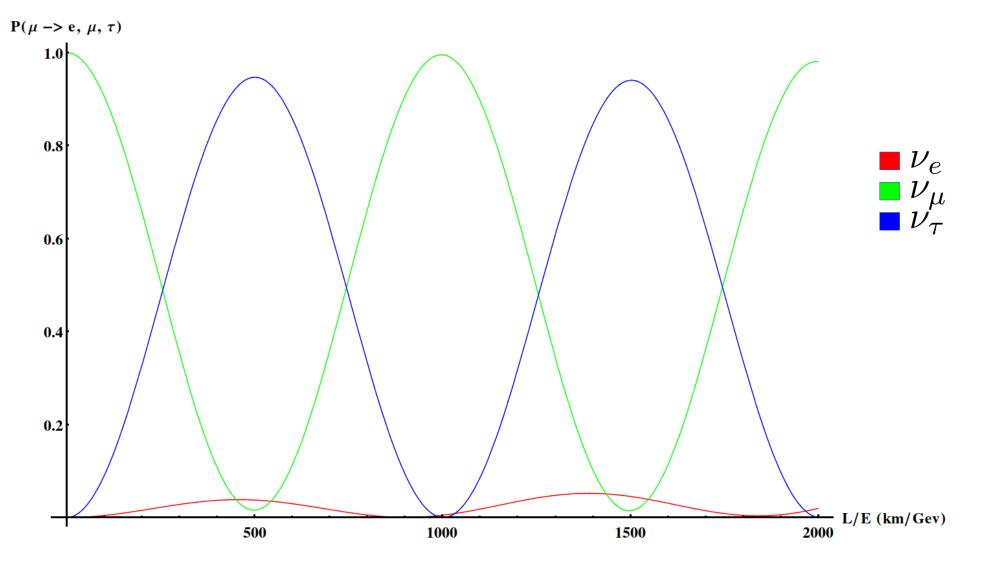
Neutrino oscillations (3 generations)

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{cp}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{cp}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{cp}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{cp}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{cp}} & c_{23}c_{13} \end{pmatrix} \begin{bmatrix} \mu \\ \mu \\ \tau \end{bmatrix}$$

$$P_{\nu_{\alpha} \to \nu_{\beta}} = \delta_{\alpha\beta} - 4\sum_{i>j} \operatorname{Re}\left(A_{ij}^{\alpha\beta}\right) \sin^{2}\frac{\Delta m_{ij}^{2}L}{4E} \pm 2\sum_{i>j} \operatorname{Im}\left(A_{ij}^{\alpha\beta}\right) \sin\frac{\Delta m_{ij}^{2}L}{4E}$$

Six parameters in total: $\Delta m_{21}^2, \Delta m_{32}^2, \theta_{12}, \theta_{13}, \theta_{23}, \delta_{cp}$

Neutrino oscillations



CP violation in vacuum

$$P_{\nu_{\alpha} \to \nu_{\beta}} = \delta_{\alpha\beta} - 4\sum_{i>j} \operatorname{Re}\left(A_{ij}^{\alpha\beta}\right) \sin^{2}\frac{\Delta m_{ij}^{2}L}{4E} \pm 2\sum_{i>j} \operatorname{Im}\left(A_{ij}^{\alpha\beta}\right) \sin\frac{\Delta m_{ij}^{2}L}{4E}$$

CP violationT violationCPT symmetry
$$P_{\nu_{\alpha} \rightarrow \nu_{\beta}} \neq P_{\overline{\nu}_{\alpha} \rightarrow \overline{\nu}_{\beta}}$$
 $P_{\nu_{\alpha} \rightarrow \nu_{\beta}} \neq P_{\nu_{\beta} \rightarrow \nu_{\alpha}}$ $P_{\nu_{\alpha} \rightarrow \nu_{\beta}} = P_{\overline{\nu}_{\beta} \rightarrow \overline{\nu}_{\alpha}}$

All three equations can be proven using the formula above.

CP violation "amplitude":

$$P_{\nu_{\alpha} \to \nu_{\beta}} - P_{\overline{\nu}_{\alpha} \to \overline{\nu}_{\beta}} = 4 \sum_{i>j} \operatorname{Im} \left(A_{ij}^{\alpha\beta} \right) \sin \frac{\Delta m_{ij}^2 L}{2E}$$

Jarlskog invariant



$$s_{ij} \equiv \sin \theta_{ij}$$

$$c_{ij} \equiv \cos \theta_{ij}$$

$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$$

$$A_{ij}^{\alpha\beta} \equiv U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*$$

Imaginary part of $A_{ij}^{\alpha\beta}$ is constant up to a sign for all $\alpha \neq \beta$ and $i \neq j$, else it is zero

• this is a "measure" of CP violation in 3-generation neutrino model

 $J = s_{12}c_{12}s_{13}c_{13}s_{23}c_{23}c_{13}\sin\delta_{\rm CP}$ - Jarlskog in 3-gen PMN

Jarlskog invariant in standard 3-gen PMNS parametrization

- J = 0 if any of the mixing angles θ_{ij} is 0 or $\pi/2$, or δ_{CP} is 0 or π
 - in that case there is no CP violation
- $J \sim -0.03$ assuming current PDG central values

CP violation "amplitude":

$$P_{\alpha \to \beta} - P_{\overline{\alpha} \to \overline{\beta}} = 4 \sum_{i>j} \operatorname{Im} \left(A_{ij}^{\alpha \beta} \right) \sin \frac{\Delta m_{ij}^2 L}{2E}$$

CP violation in ESSnuSB

General CP violation "amplitude":

$$P_{\nu_{\alpha} \to \nu_{\beta}} - P_{\overline{\nu}_{\alpha} \to \overline{\nu}_{\beta}} = 4 \sum_{i>j} \operatorname{Im} \left(A_{ij}^{\alpha\beta} \right) \sin \frac{\Delta m_{ij}^2 L}{2E}$$

ESSnuSB CP violation

$$P_{\nu_{\mu} \to \nu_{e}} - P_{\overline{\nu}_{\mu} \to \overline{\nu}_{e}} = 4J \left(\sin \frac{\Delta m_{31}^{2} L}{2E} - \sin \frac{\Delta m_{32}^{2} L}{2E} - \sin \frac{\Delta m_{21}^{2} L}{2E} \right)$$
$$= -16J \sin \frac{\Delta m_{31}^{2} L}{4E} \sin \frac{\Delta m_{32}^{2} L}{4E} \sin \frac{\Delta m_{21}^{2} L}{4E}$$
$$J = s_{12}c_{12}s_{13}c_{13}s_{23}c_{23}c_{13} \sin \delta_{\rm CP}$$

To have CP violation we must have $J \neq 0$, but also $\Delta m_{ij}^2 \neq 0$ --> all three masses must be different

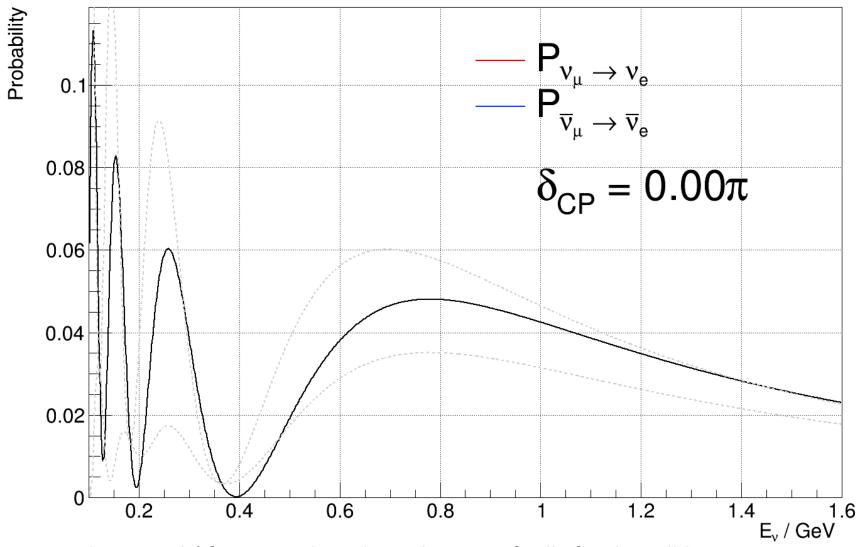
$$s_{ij} \equiv \sin \theta_{ij}$$

$$c_{ij} \equiv \cos \theta_{ij}$$

$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$$

$$A_{ij}^{\alpha\beta} \equiv U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*$$

Effect of δ_{CP} on oscillations in vacuum



Thanks to my student L. Halić for patiently making plots specifically for this talk!

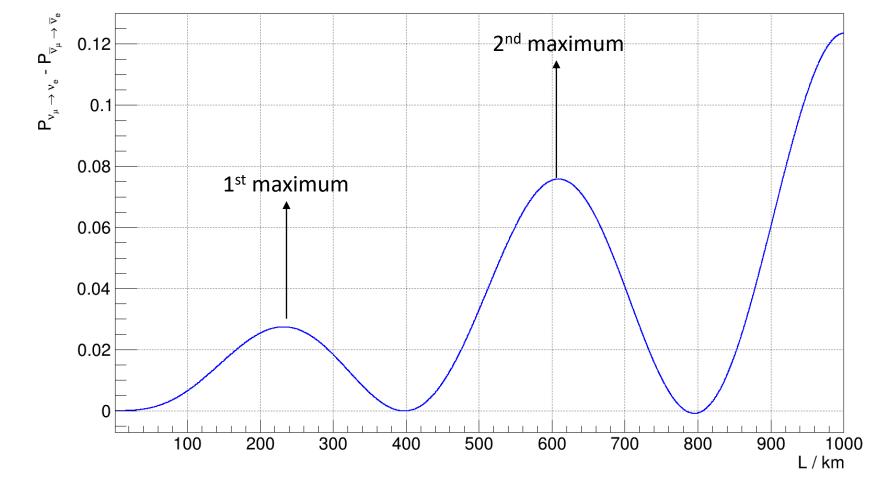
$\begin{aligned} & \mathsf{CP} \text{ violation in ESSnuSB} \\ & A_{CP} \equiv P_{\nu_{\mu} \to \nu_{e}} - P_{\overline{\nu}_{\mu} \to \overline{\nu}_{e}} = -16J \sin \frac{\Delta m_{31}^2 L}{4E} \sin \frac{\Delta m_{32}^2 L}{4E} \sin \frac{\Delta m_{21}^2 L}{4E} \\ & \mathsf{E} = 400 \text{ MeV} \end{aligned}$

$$s_{ij} \equiv \sin \theta_{ij}$$

$$c_{ij} \equiv \cos \theta_{ij}$$

$$\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$$

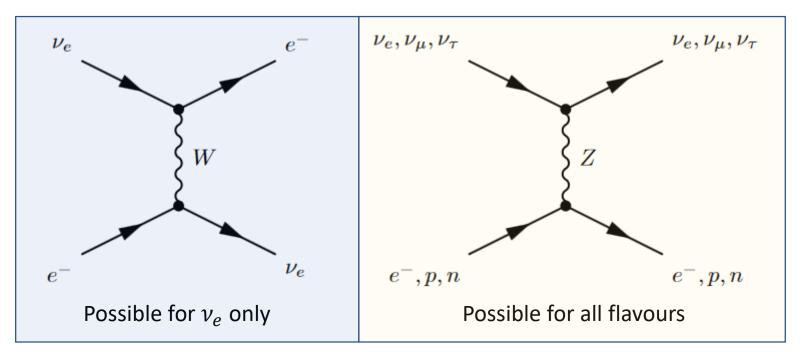
$$A_{ij}^{\alpha\beta} \equiv U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*$$



$$\frac{A_{CP} @ 2nd \max}{A_{CP} @ 1st \max} \sim 2.7$$

- Does not depend on *J*, i.e.
 PMNS matrix elements
- Depends only on mass splittings

Distortion of oscillation probabilities due to elastic scattering of neutrinos with matter



- Elastic neutrino scattering can proceed through:
 - NC interactions for all flavour/mass eigenstates
 - CC interactions with electrons for electron neutrinos
- Therefore electron neutrinos see a slightly different effective potential than muon and tau neutrinos
 - This modifies the evolution of flavour states in matter

• For uniform matter density, these effects can be included by replacing vacuum oscillation parameters with effective "matter parameters"

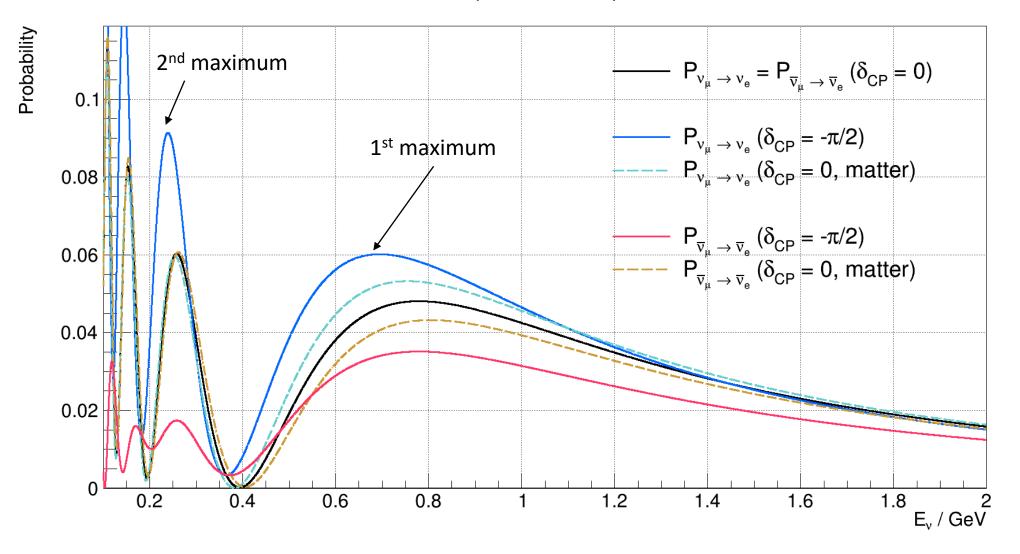
•
$$\theta_{ij} \to \theta_{ij}^{(m)}(E), \, \delta_{CP} \to \delta_{CP}^{(m)}(E) \text{ and } \Delta m_{ij}^2 \to \Delta M_{ij}^2(E)$$

• the effective parameters now depend on energy

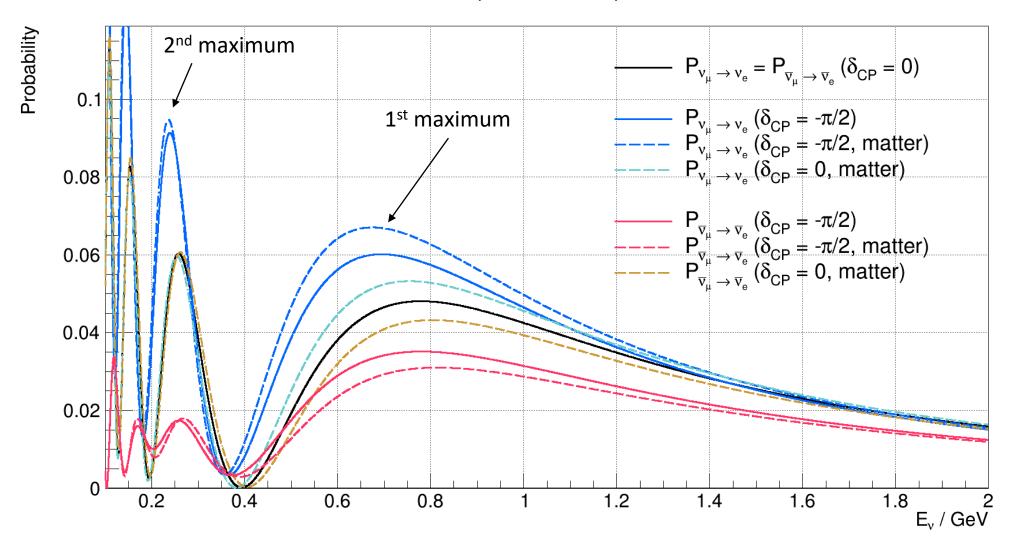
$$P_{\nu_{\alpha}\to\nu_{\beta}}^{(m)} = \delta_{\alpha\beta} - 4\sum_{i>j} \operatorname{Re}\left({}^{(m)}A_{ij}^{\alpha\beta}(E)\right) \sin^{2}\frac{\Delta M_{ij}^{2}(E)\ L}{4E} \pm 2\sum_{i>j} \operatorname{Im}\left({}^{(m)}A_{ij}^{\alpha\beta}(E)\right) \sin\frac{\Delta M_{ij}^{2}(E)\ L}{4E}$$

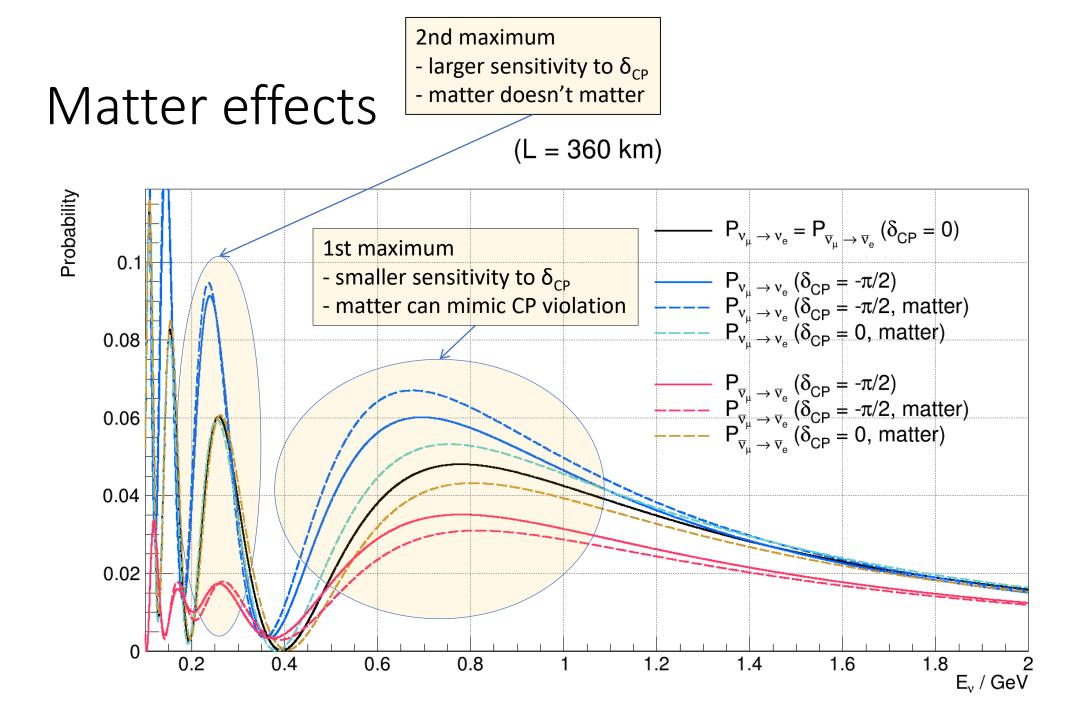
 For non-uniform densities it requires numerical calculation of probabilities

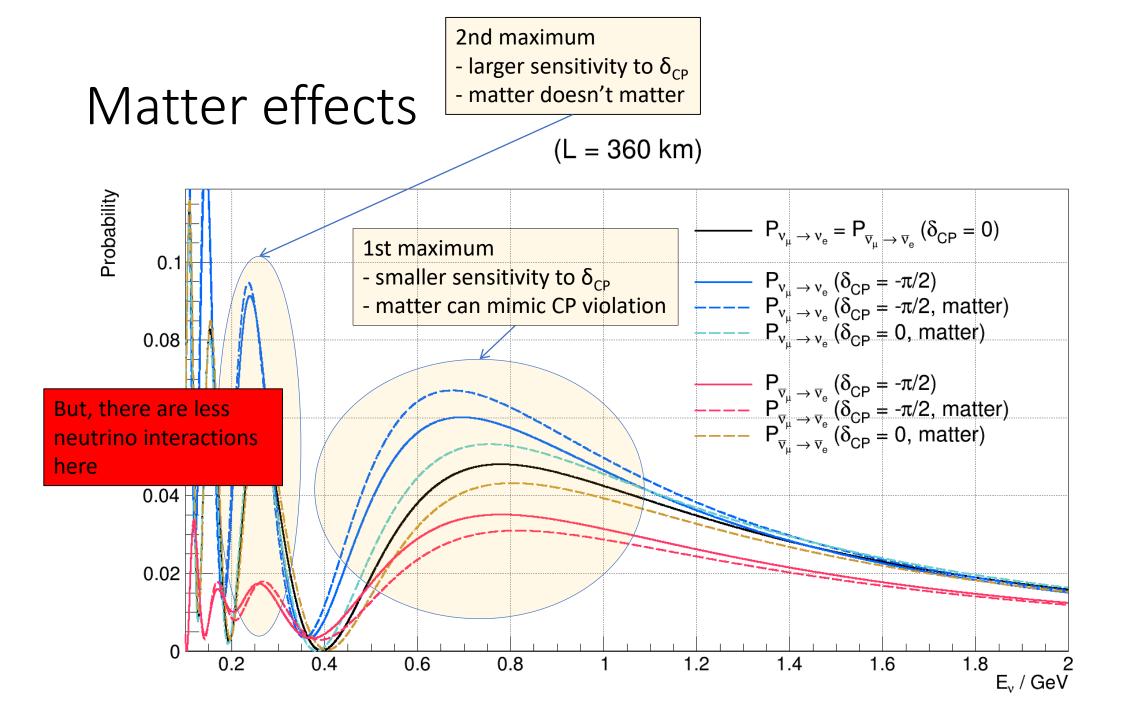
(L = 360 km)



(L = 360 km)







Why 2nd maximum? (summary)

| The good | Vacuum CPV signal 2.7 times larger than at 1 st max. Fake CPV signal from matter effects very small. | | | |
|--|--|--|--|--|
| | You get less statistics because you have to either: | | | |
| The bad | Move 3x further than 1st maximum - flux 9x smaller | | | |
| Reduce energy 3x – cross-section at least 3x smaller | | | | |
| The optima | • Depends on the systematic error and beam intensity | | | |
| • 3x signal | at 2nd osc. maximum is less obscured by systematics, but we have | | | |

- less statistics (measured appearance events).
 - If the signal at 2nd maximum is not obscured by larger statistical error, then 2nd maximum is better Intense beam is needed
- With no systematic error, first maximum is better
 - more statistics, even though the effect is smaller.

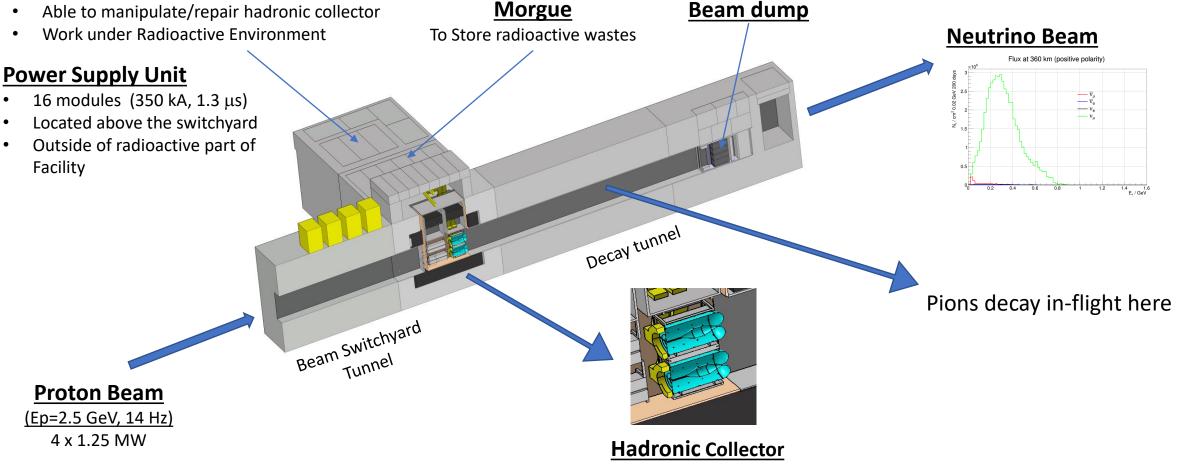
ESSnuSB project

How to observe the CP violation in the 2nd oscillation maximum

Neutrino beam production

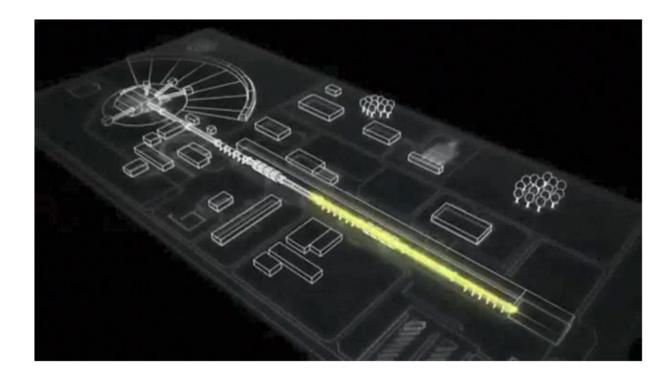
 $\pi^+ \to \mu^+ + \nu_\mu \qquad \pi^- \to \mu^- + \overline{\nu}_\mu$

Hot Cell

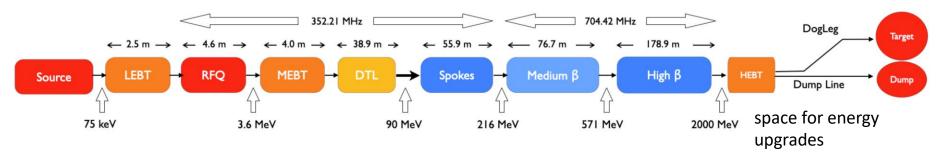


Can we go to 2nd maximum?

A very intense proton linac is in construction near Lund, Sweden.



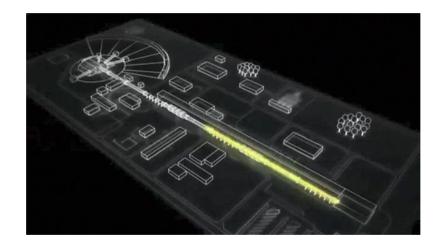
ESS proton linac

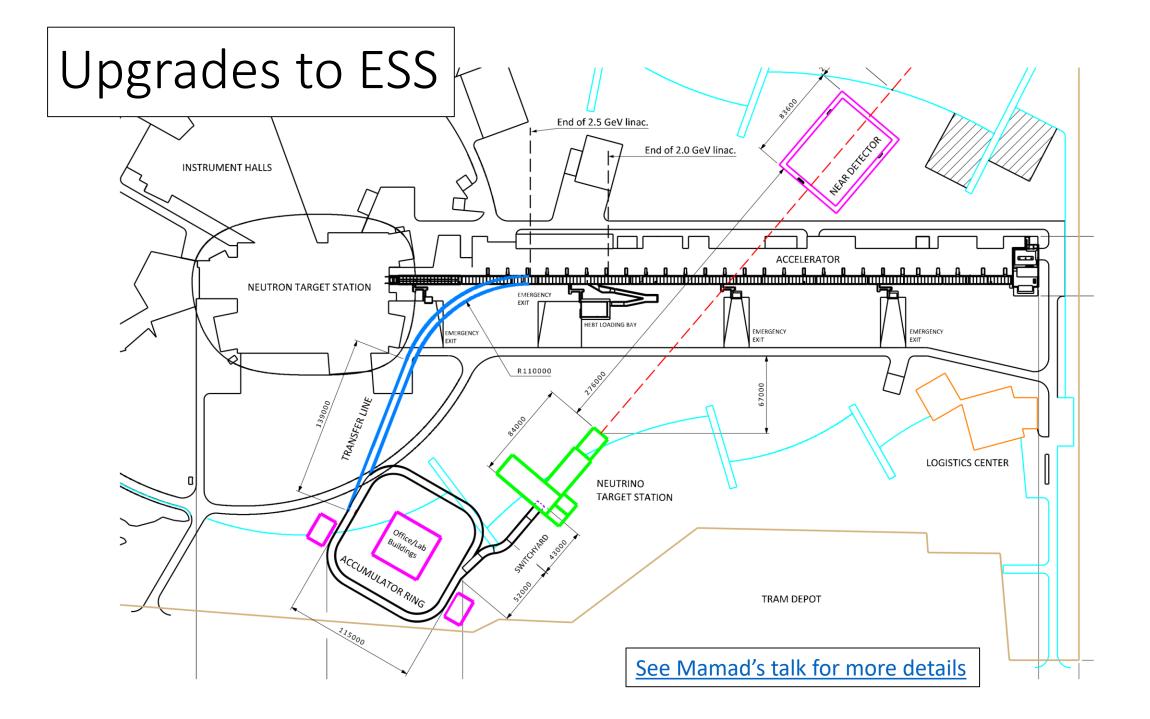


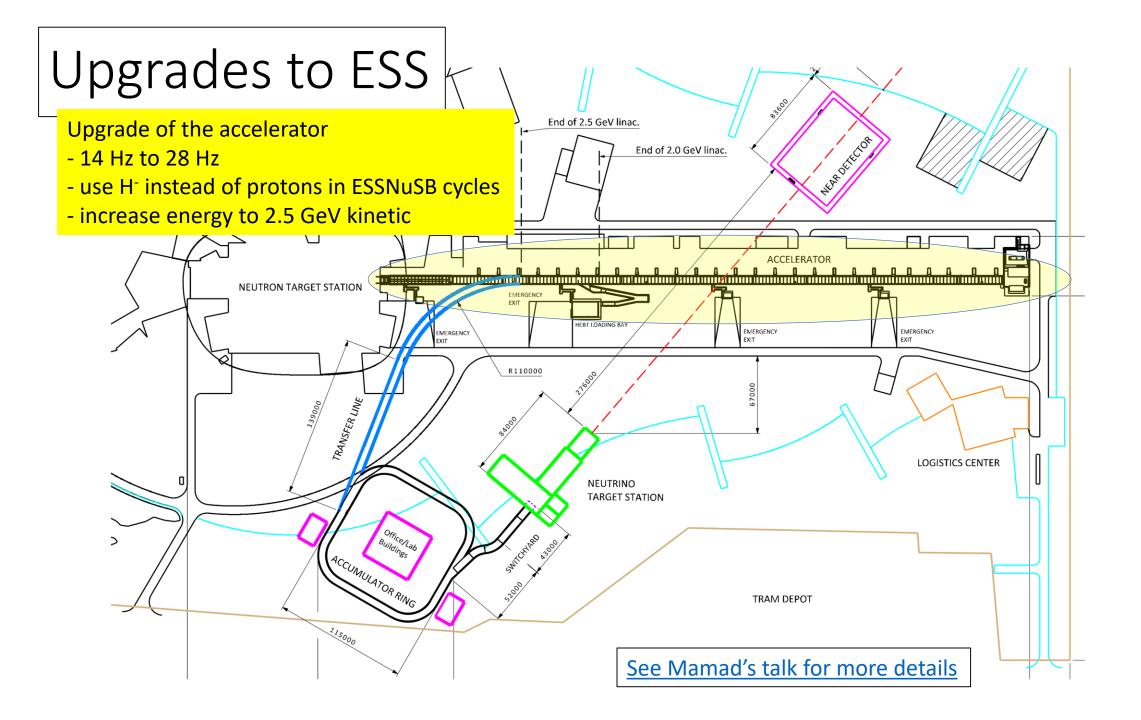
- The ESS will be a copious source of spallation neutrons.
- 5 MW average beam power.
- 125 MW peak power.
- 14 Hz repetition rate (2.86 ms pulse duration, 10¹⁵ protons).
- Duty cycle 4%.
- 2.0 GeV kinetic energy protons
 - $\circ~$ up to 3.5 GeV with linac upgrades
- >2.7x10²³ p.o.t/year.

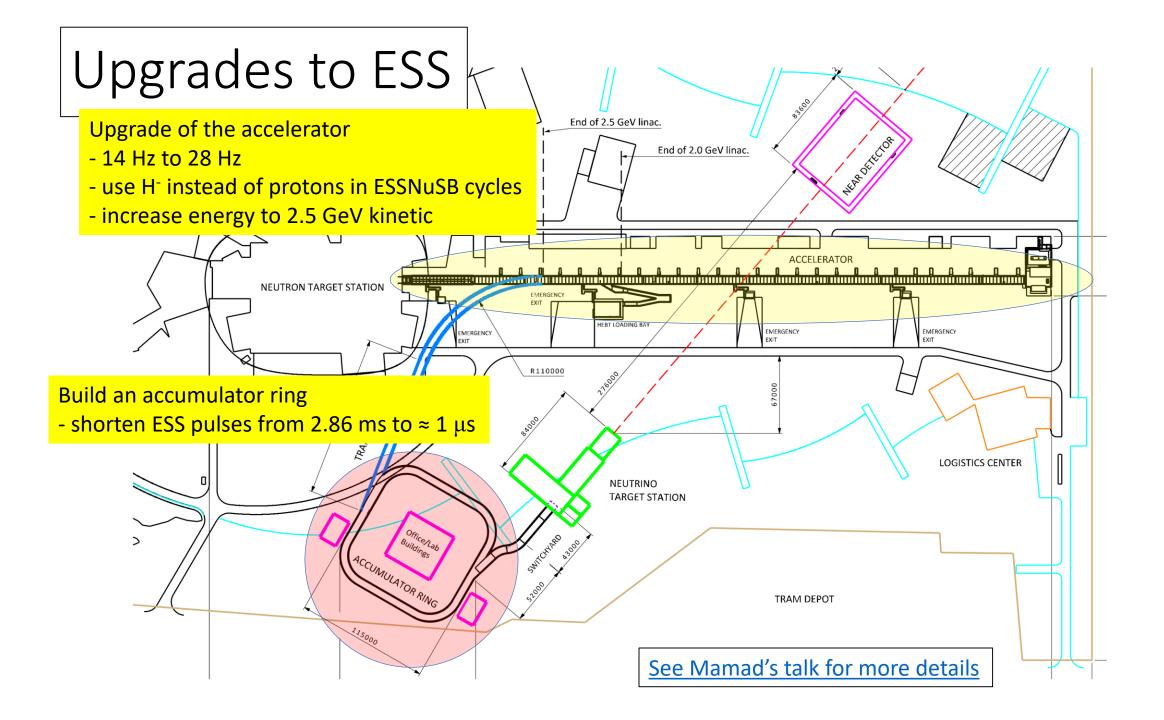
First beam on target expected in 2024.

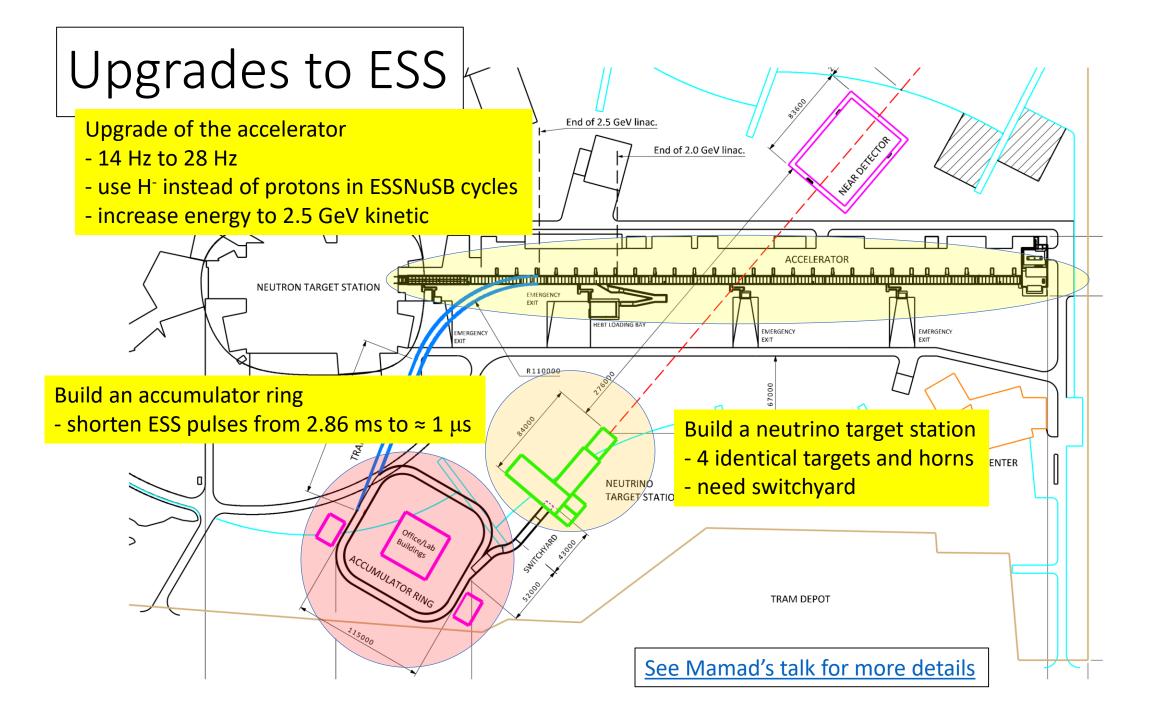
450 mg of protons/year at 95% speed of light!

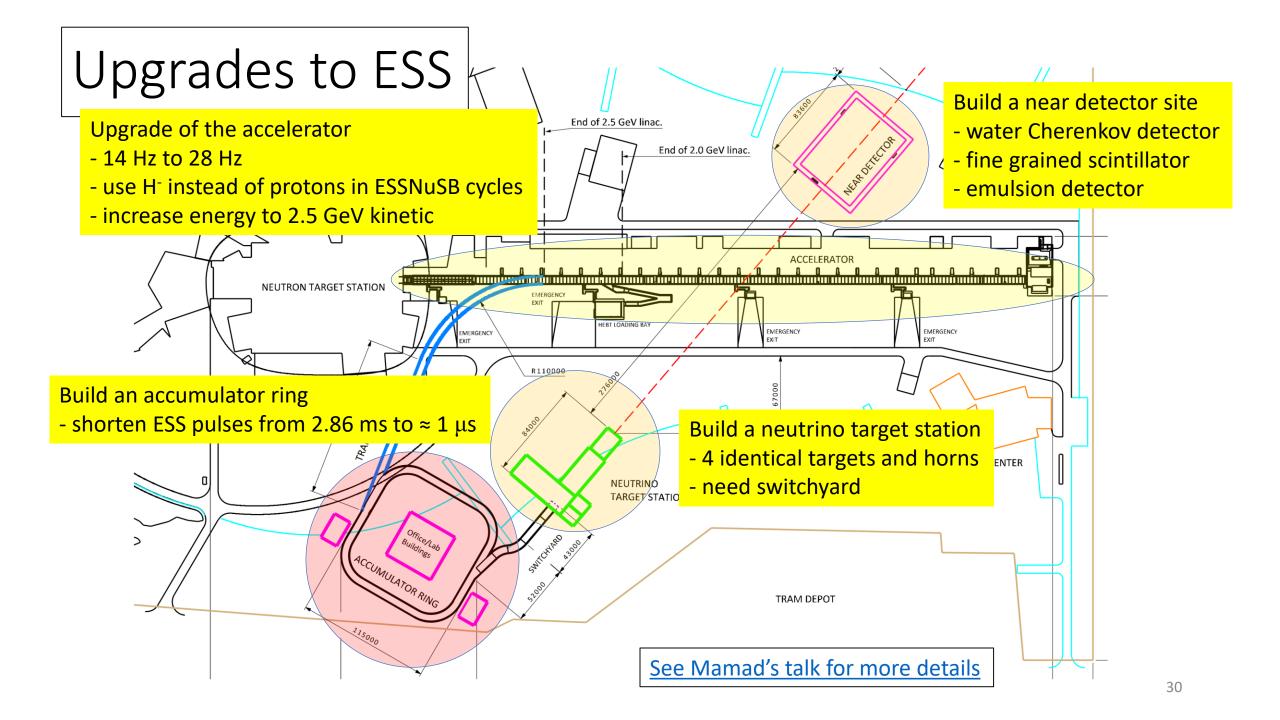






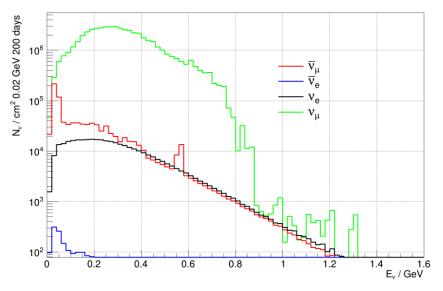






ESSvSB v energy distribution (after optimisation)

Flux at 360 km (positive polarity)



• almost pure v_{μ} beam

will be used to

measure v_e cross-

sections in a near

contamination which

• small v_e

detector

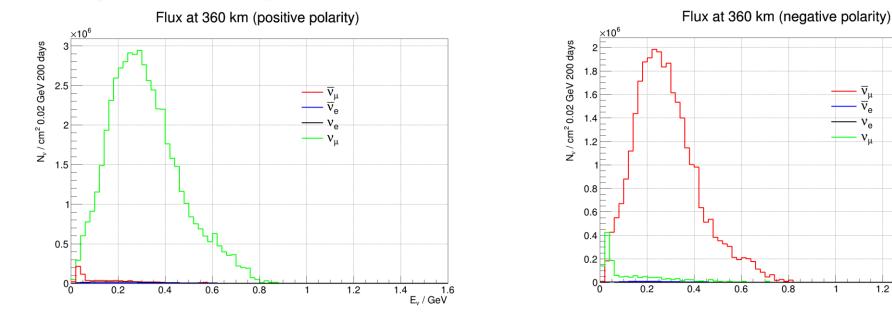
$N_{\rm v}\,/\,cm^2$ 0.02 GeV 200 days \overline{v}_{μ} չուր 10⁴ 10³ 10² 10 1 0 0.2 0.4 0.6 0.8 1.2 1.4 1 1.6 E, / GeV

Flux at 360 km (negative polarity)

Flavour v Mode $\overline{\boldsymbol{\nu}}$ Mode N_{ν} (10⁵/ cm²) N_{ν} (10⁵/ cm²) % % 520.06 97.6 15.43 4.7 ν_{μ} 0.67 3.67 0.10 0.03 v_e $\bar{\nu}_{\mu}$ 9.10 1.7 305.55 94.8 0.023 0.03 1.43 0.43 $\bar{\nu}_e$

at 360 km from the target and per year (in absence of oscillations)

ESSvSB v energy distribution (after optimisation)



• almost pure v_{μ} beam

• small v_e contamination which will be used to measure v_e crosssections in a near detector

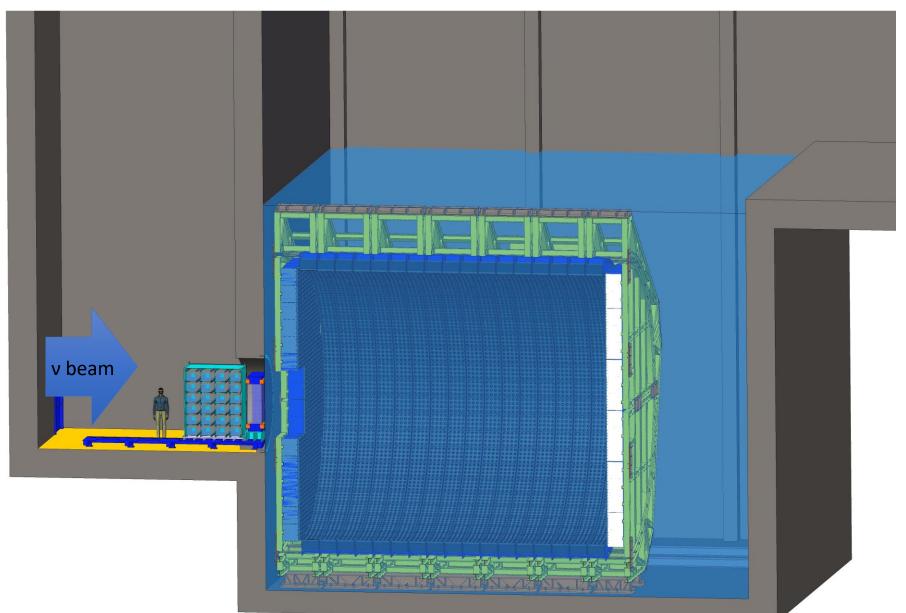
| Flavour | ν Mode | | $\overline{\nu}$ Mode $\overline{\overline{\nu}}$ Mode | | |
|----------------|--|------|--|------|--|
| | $N_{ m u}$ (10 ⁵ / cm ²) | % | $N_{ m u}$ (10 ⁵ / cm ²) | % | |
| $ u_{\mu}$ | 520.06 | 97.6 | 15.43 | 4.7 | |
| ν_e | 3.67 | 0.67 | 0.10 | 0.03 | |
| $ar{ u}_{\mu}$ | 9.10 | 1.7 | 305.55 | 94.8 | |
| $\bar{\nu}_e$ | 0.023 | 0.03 | 1.43 | 0.43 | |

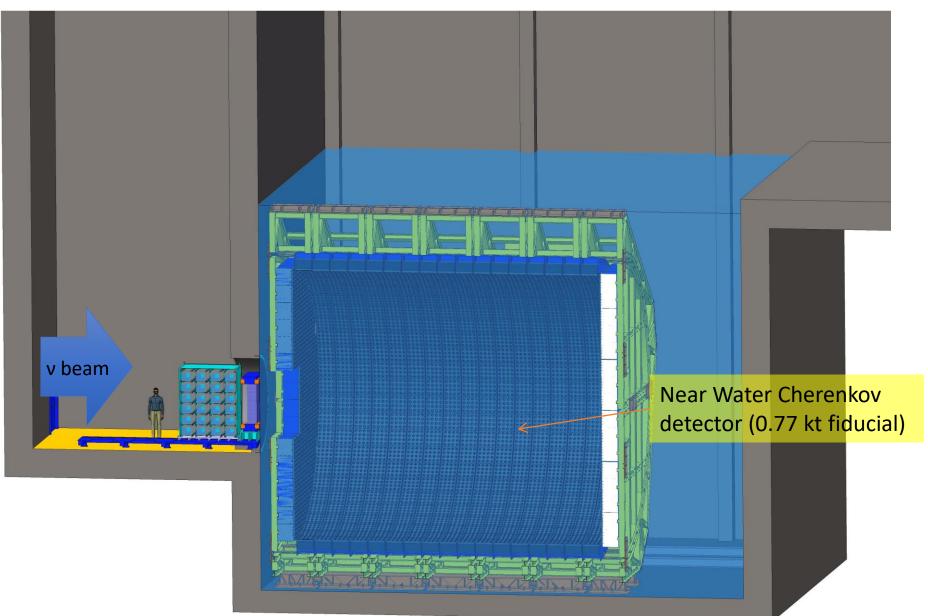
at 360 km from the target and per year (in absence of oscillations)

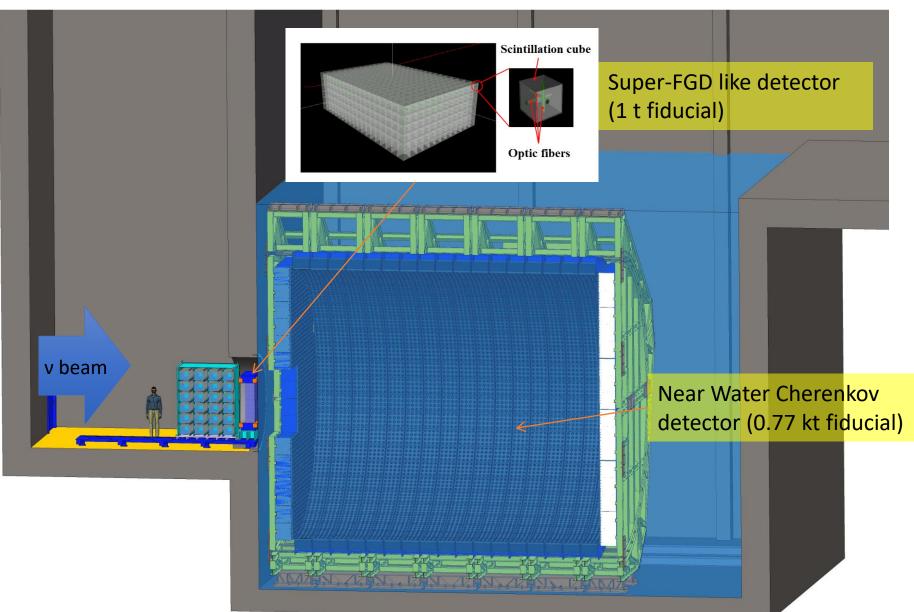
1.4 1.6 E_v / GeV

ν_e

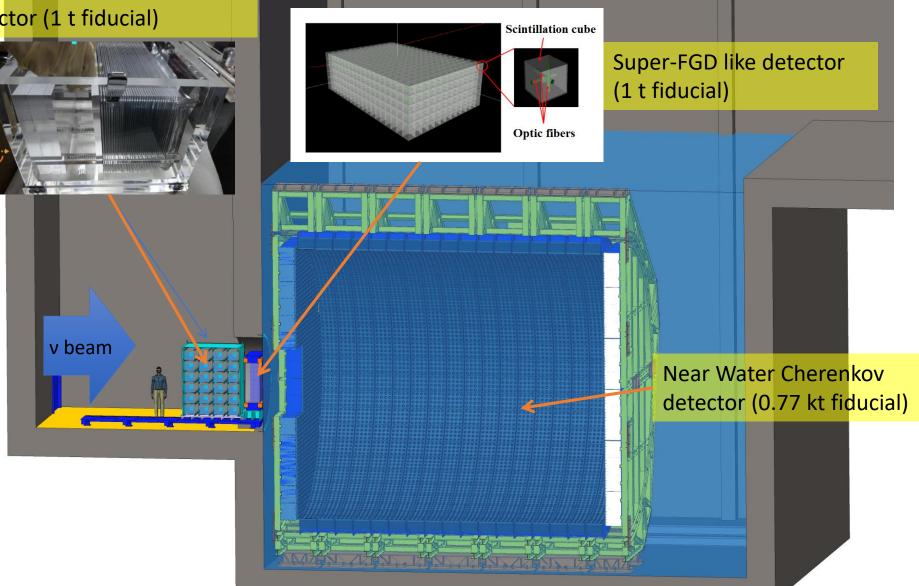
1.2







NINJA-like water-emulsion detector (1 t fiducial)





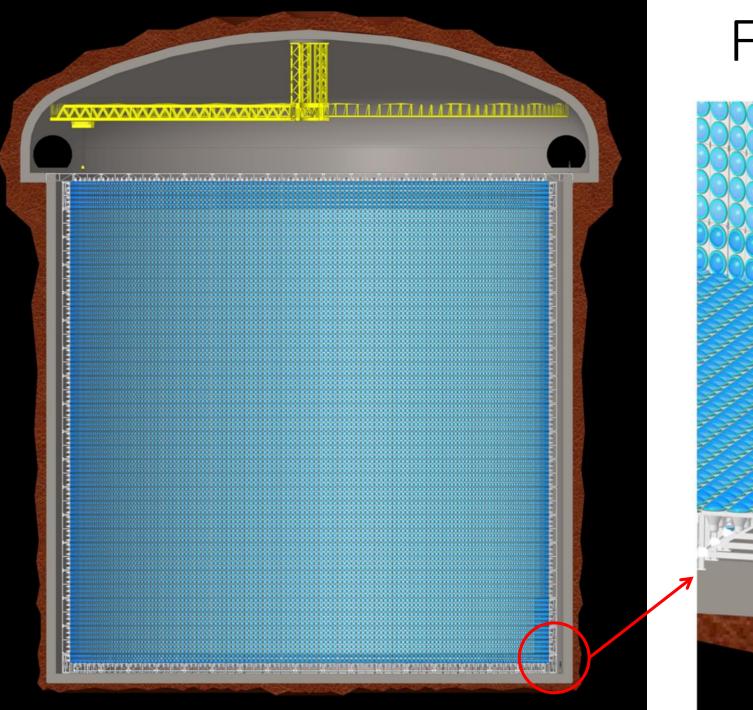
Far detector position

Selected baseline:

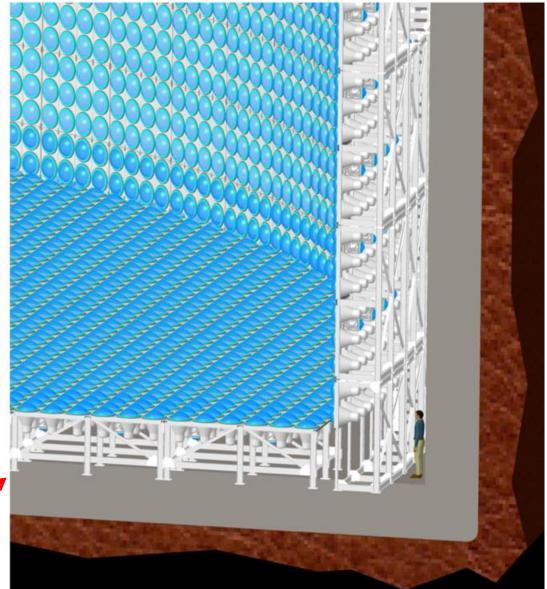
- Zinkgruvan mine, 360 km from the source, partly covernig 1st and 2nd maximum
 - Number of interactions at 2nd maximum similar to Garpenberg

Alternative (not selected)

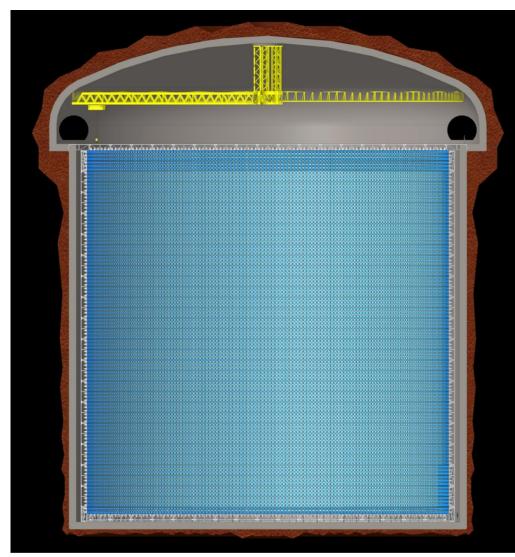
• Garpenberg mine, 540 km from the neutrino source, corresponding to 2nd oscillation maximum.



Far detector



Far detectors



Design

- 2 x 270 kt fiducial volume (~20xSuperK)
- Readout: 2 x 38k 20" PMTs
- 30% optical coverage
 - design here for 40% with an option that ¹/₄ PMTs will not be installed

Can also be used for other purposes:

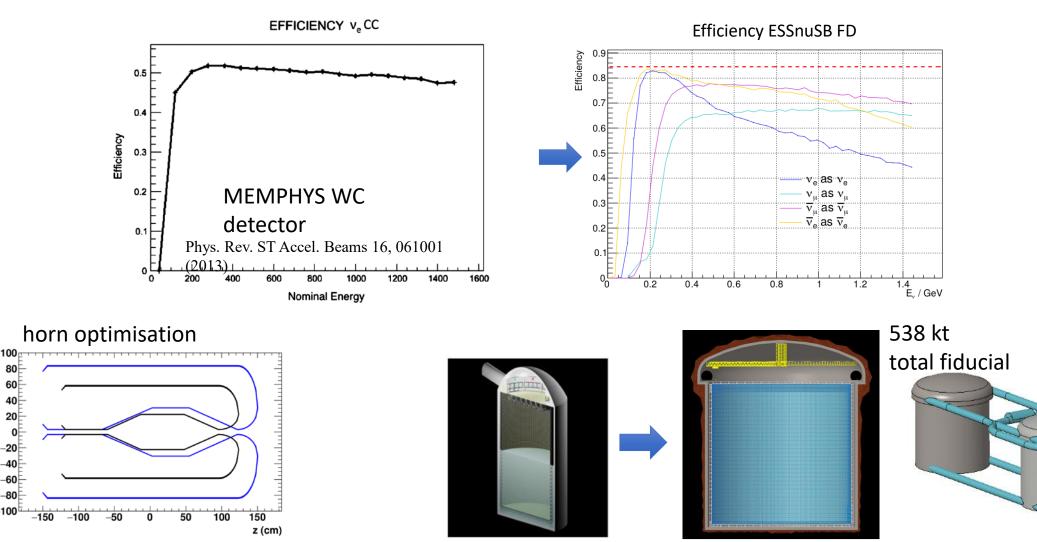
- Proton decay
- Astroparticles
- Galactic SN v
- Diffuse supernova neutrino background
- Solar Neutrinos
- Atmospheric Neutrinos

Improvements on sensitivity

- Near detectors optimized for flux and cross-section measurement 5% systematics within easy reach .
- Far detectors' response optimized for ESSnuSB flux very high efficiency and purity at ESSnuSB energies ٠
- Genetic Algorithm for Target Station optimization more neutrinos

r (cm)

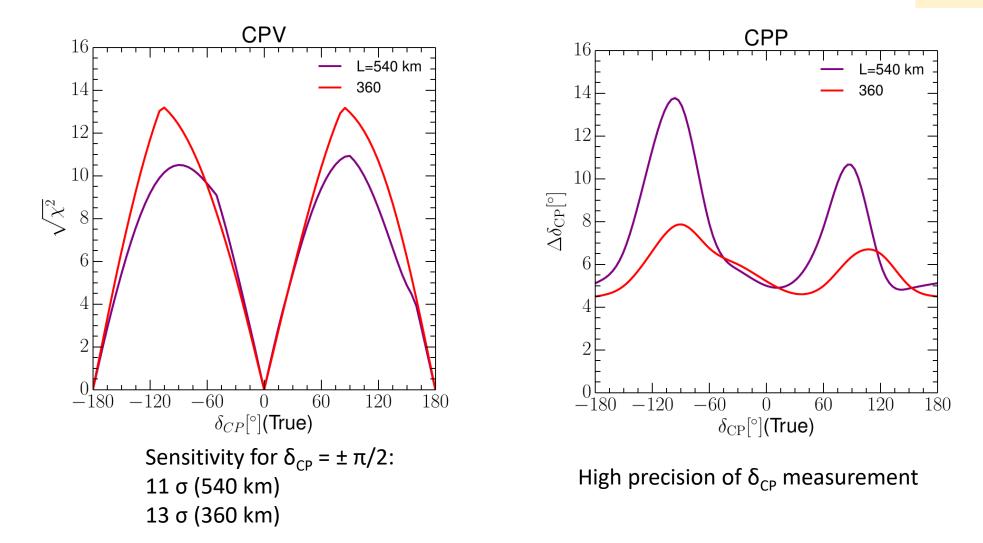
-60 -80 -100



Updated physics performance of the ESSnuSB experiment, Eur.Phys.J.C 81 (2021) 12, 1130

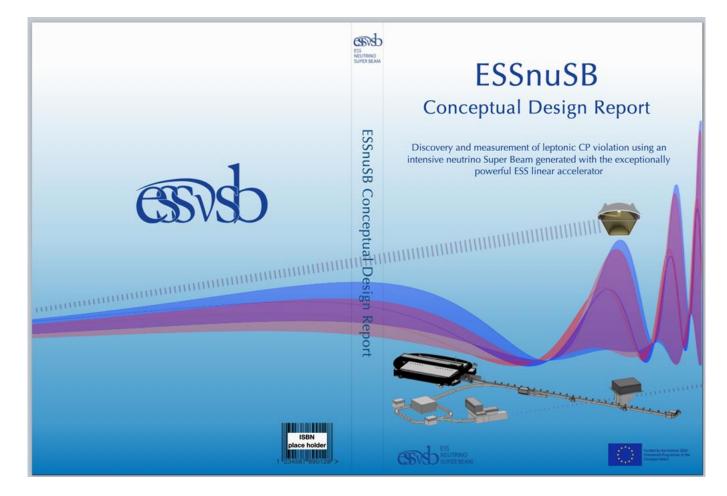
DOI:10.1140/epjc/s10052-021-09845-8, arXiv:2107.07585

State of analysis June 2021

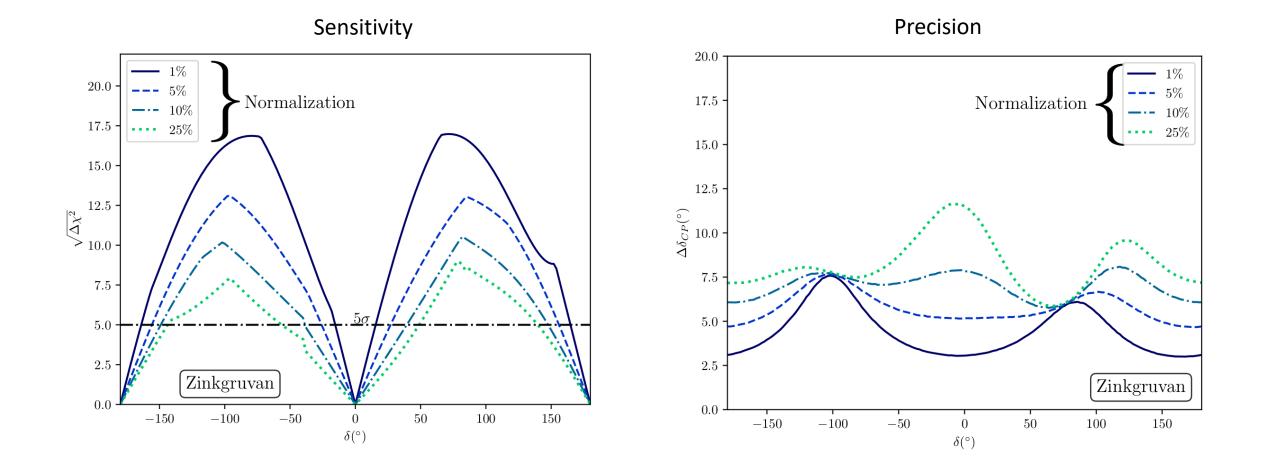


Latest physics reach

- Since our previous publication:
 - Improved flux simulation
 - Improved detector geometry simulation
 - Improved handling of systematic errors
- Will be published within the CDR soon

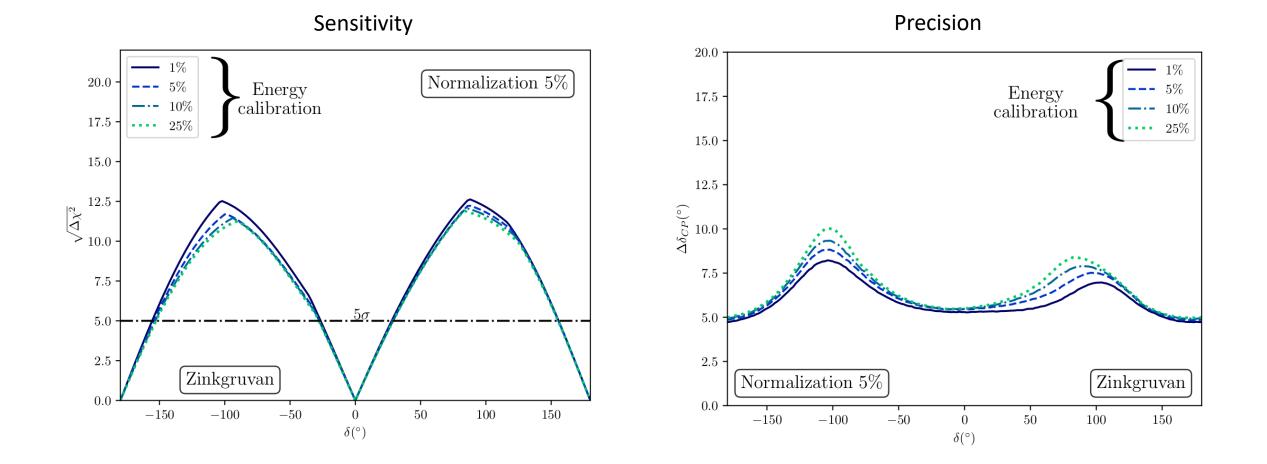


Effect of normalization uncertainty

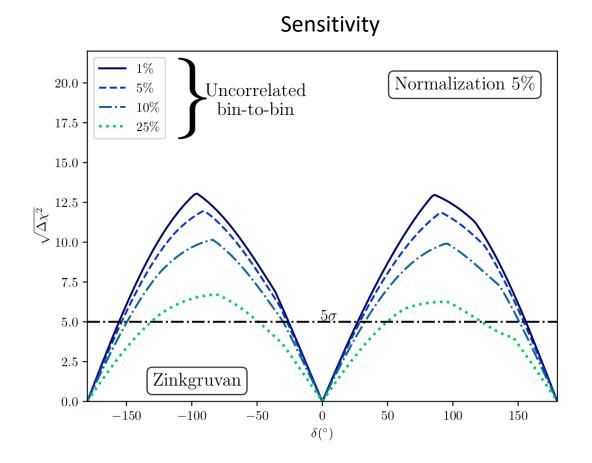


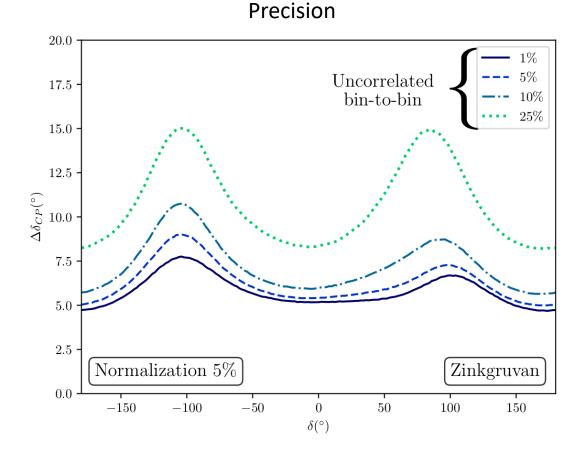
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Effect of energy calibration uncertainty

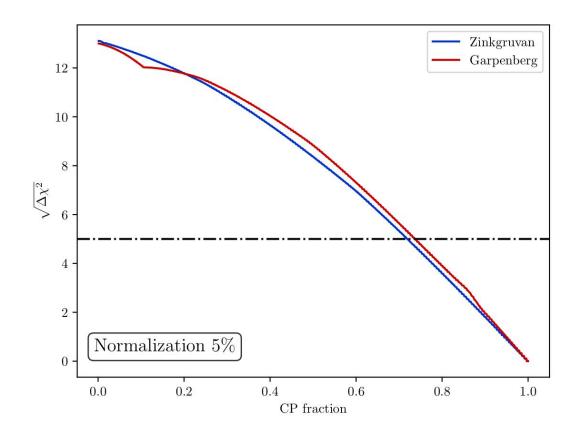


Effect of bin-to-bin uncorrelated uncertainty



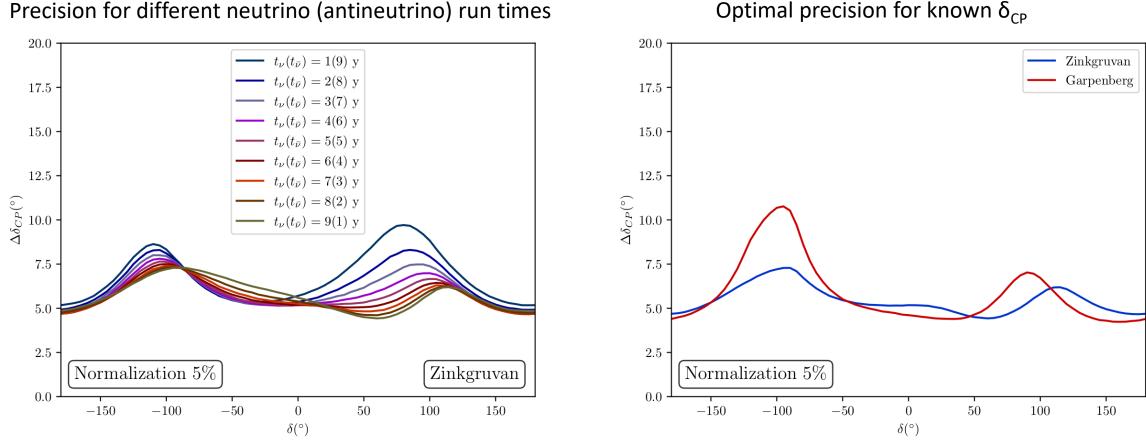


CP coverage



71% coverage of δ_{CP} range with more than 5 σ

Optimization for precision Supposing that value of δ_{CP} is roughly known at ESSnuSB time



ESSvSB at the European level

• A H2020 EU Design Study (Call INFRADEV-01-2017)



LBNO (2010-

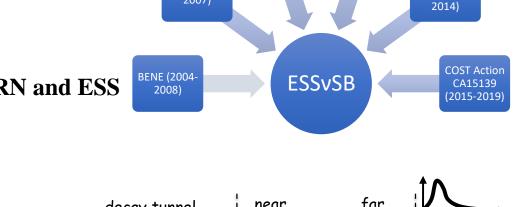
LAGUNA

(2008-2010)

- **Title of Proposal**: Discovery and measurement of leptonic CP violation using an intensive neutrino Super Beam generated with the exceptionally powerful ESS linear accelerator
- Duration: 4 years
- Total cost: 4.7 M€
- Requested budget: 3 M€

Approved end of August 2017

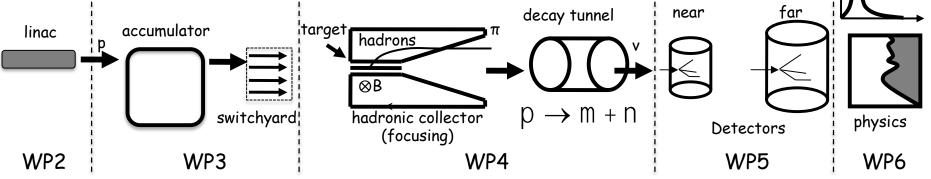
- 15 participating institutes from
 11 European countries including CERN and ESS
- 6 Work Packages



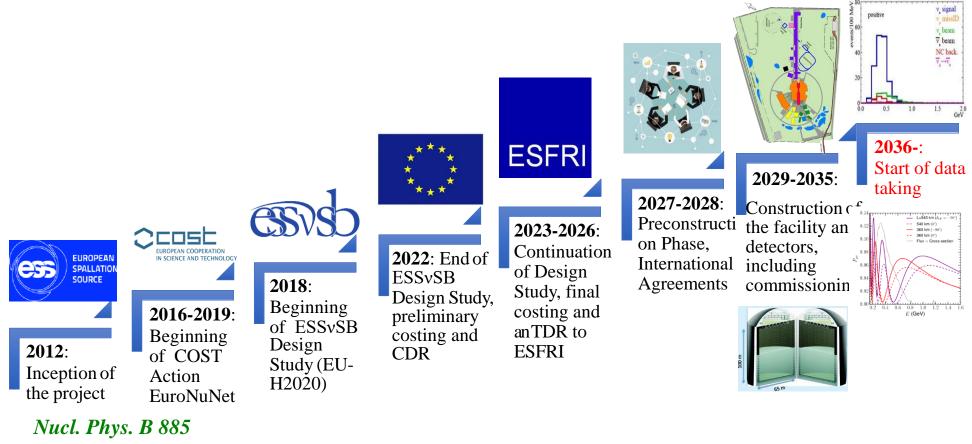
ISS (2005-

2007)

EUROv (2008-2012)



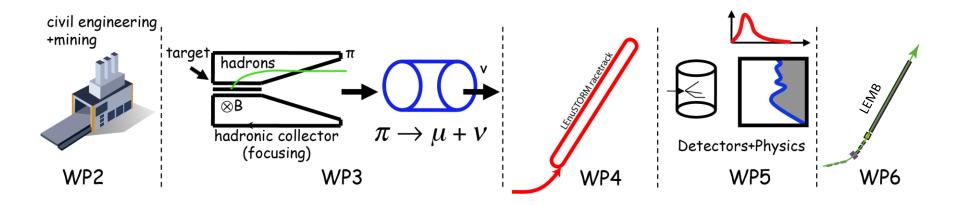
Schedule for a 2nd generation ESS-based neutrino Super Beam ESSnuSB



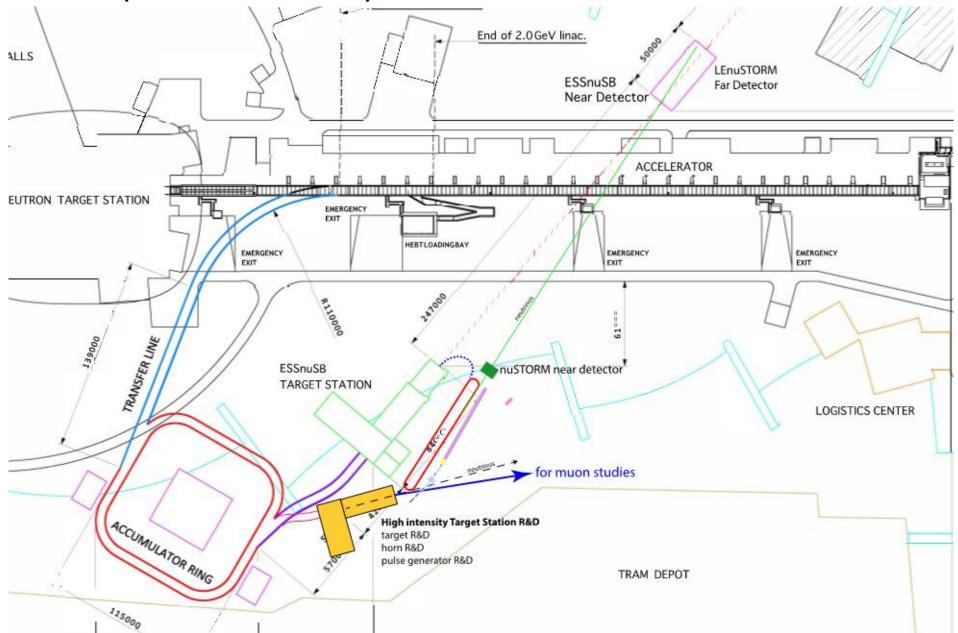
(2014) 127

The ESSnuSB+ project proposal

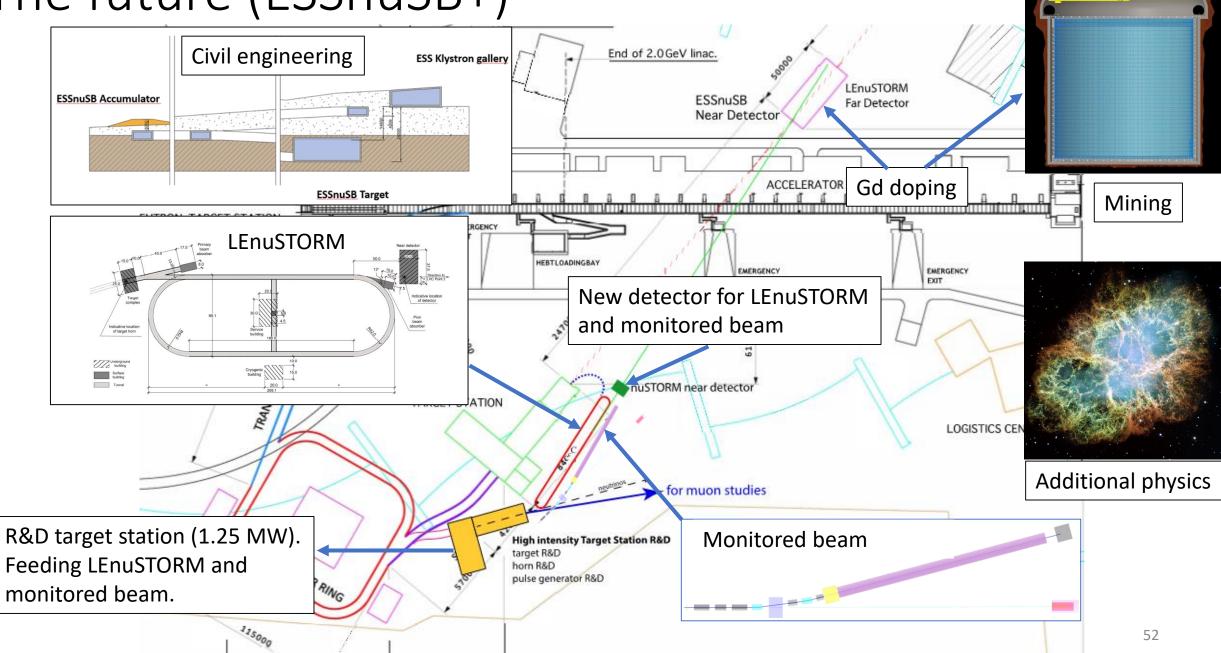
- Having finished the conceptual design of the facility for CP violation measurement, we need to take further steps
- Start with the civil engineering and infrastructure development
- Design prototyping facilities at ESS
- Design facilities for very precise neutrino cross-section measurement: low energy nuSTORM (LEnuSTORM) and monitored beam (LEMB)
- Explore additional physics opportunities offered by ESSnuSB with addition of LEnuSTORM and LEMB
- We have received strong support from the ESS management



The future (ESSnuSB+)



The future (ESSnuSB+)



ESSnuSB movies

https://www.youtube.com/watch?v=PwzNzLQh-Dw



https://www.youtube.com/watch?v=qAnvftOnAlg



Special thanks to my ESSnuSB colleagues!

The content presented here is a result of 4 years of collaborative effort of many people involved in ESSnuSB project.

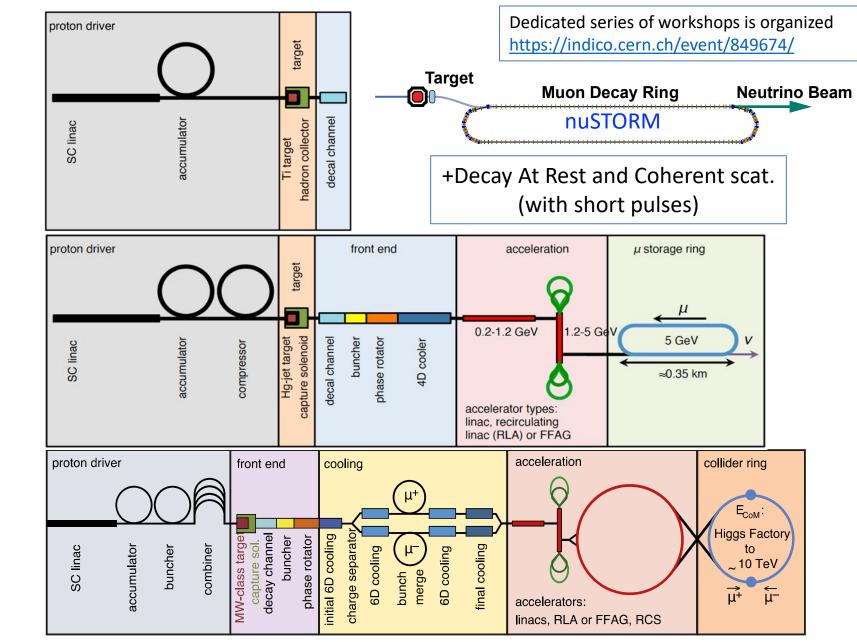
Thank you all for making this possible!

Conclusions

- ESSnuSB aims to observe CP violation in neutrino oscillations at the 2nd oscillation maximum using 538 kt WC detector
 - 2nd maximum makes the measurement resilient to systematic errors and matter effects
 - Recent optimizations predict that in 10 years of data taking ESSnuSB will be able to
 - reach 5 σ over 71% of δ_{CP} range
 - reach δ_{CP} resolution of less than 8°
 - determine neutrino mass hierarchy
- ESS linac will be most powerful proton accelerator in the world
 - can be used to generate intense neutrino beam to go to 2nd maximum
 - neutron user programme will start in 2025, decision on neutrino programme pending
 - proposed modifications would allow a rich additional physics programme at ESS
 - muon physics, DAR experiments, short neutron pulses, ...
- Large far detectors can also be used for rich astroparticle physics programme
- The ESSnuSB Design Study has been supported by EU-Horizon 2020 during the period 2018-2022.
- We are about to seek renewed support from EU-Horizon Europe for the period 2023-2026
 - ESSnuSB+ received in March 2022 a letter of strong support from the ESS Director General Helmut Schober

Thank you for your attention

ESSvSB and (R&D) synergies

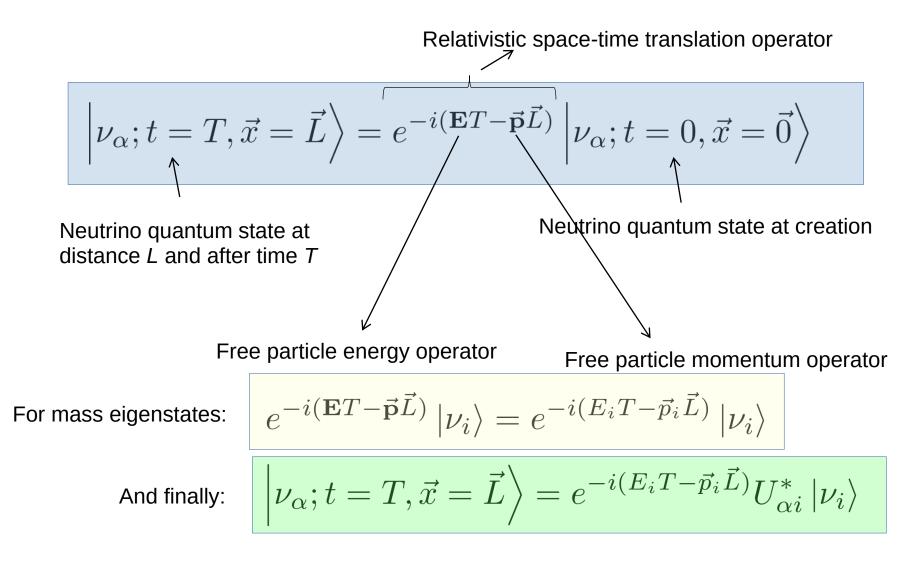


Super Beam

Neutrino Factory Muon Collider

Neutrino oscillations

Flavour state evolution



Neutrino oscillations

Oscillation probability in vacuum

Oscillation probability:

$$P_{\alpha \to \beta} = \left| \left\langle \nu_{\beta} \middle| \nu_{\alpha}; t = T, \vec{x} = \vec{L} \right\rangle \right|^2$$

Assuming:

$$\vec{L}$$
 parallel to $\vec{p_i}$
 $T = L/\beta \approx L$
 $E_i + p_i \approx 2E$
 $-$ neutrino travels in the direction of its momentum

One gets the final relation:

 $\Delta m_{ij}^2 \equiv m_i^2 - m_j^2$ $A_{ij}^{\alpha\beta} \equiv U_{\alpha i}^* U_{\alpha j} U_{\beta i} U_{\beta j}^*$

$$P_{\alpha \to \beta} = \delta_{\alpha\beta} - 4\sum_{i>j} \operatorname{Re}\left(A_{ij}^{\alpha\beta}\right) \sin^2 \frac{\Delta m_{ij}^2 L}{4E} \pm 2\sum_{i>j} \operatorname{Im}\left(A_{ij}^{\alpha\beta}\right) \sin \frac{\Delta m_{ij}^2 L}{2E}$$

PMNS matrix parametrization (Dirac neutrino)

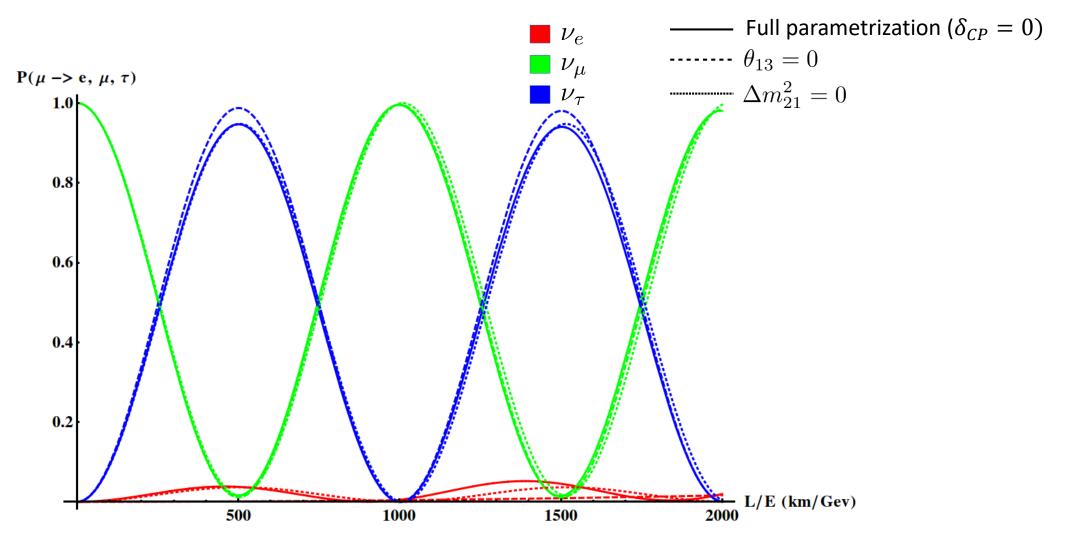
Standard parametrization used in modern literature:

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{cp}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{cp}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
$$s_{ij} \equiv \sin \theta_{ij}$$

 $c_{ij} \equiv \cos \theta_{ij}$

- Analogue to Euler matrices used for 3D rotations
- This is **not** the most general unitary matrix parametrization a 3x3 unitary matrix has 6 phases
 - 5 phases can be canceled by rephasing charged lepton and neutrino fields
- A single leftover phase is always present in the middle factor

Muon neutrino oscillations



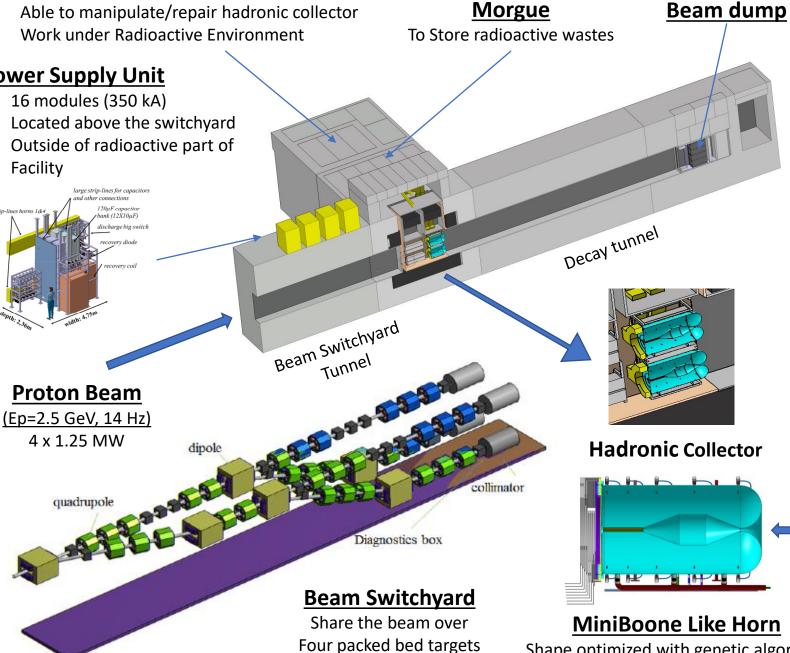
Hot Cell

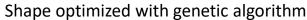
strin_lines horns 1.

- Able to manipulate/repair hadronic collector ٠
- Work under Radioactive Environment ٠

Power Supply Unit

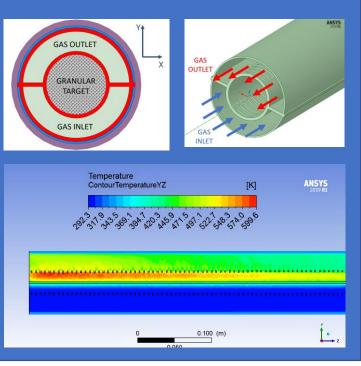
- 16 modules (350 kA)
- Located above the switchyard
- Outside of radioactive part of Facility

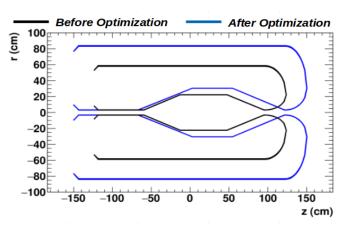




Granular Target Concept

Target made of 3 mm titanium spheres cooled by transverse helium gas cooling

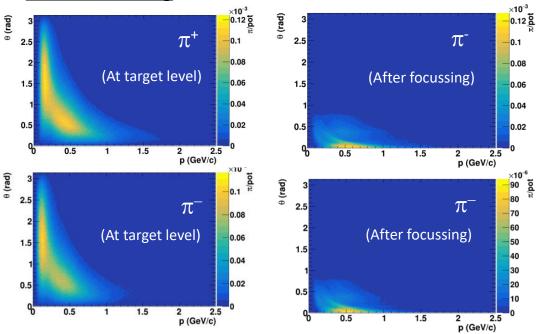




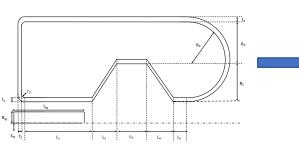
Neutrino beam production

| π^+ · | \rightarrow | $\mu^+ + \nu_\mu$ | (Positive polarity) |
|-----------|---------------|---------------------------|---------------------|
| π^- - | \rightarrow | $\mu^- + \bar{\nu}_{\mu}$ | (Negative polarity) |

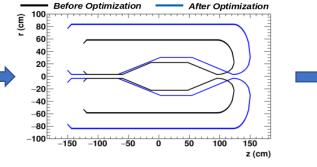
Horn focussing



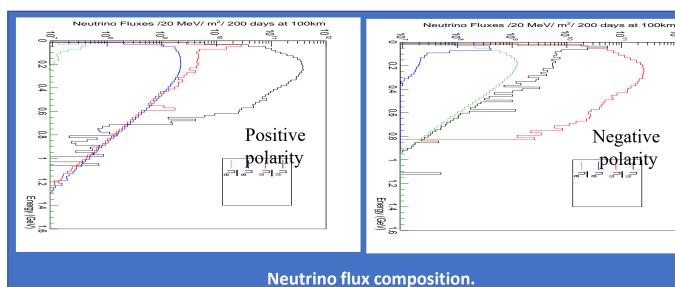
Horn optimisation procedure



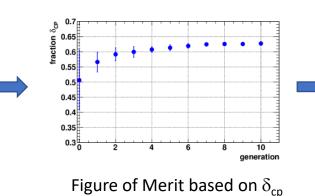
Horn parametrisation

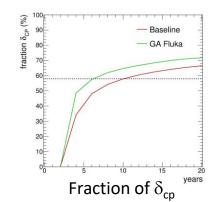


Optimisation based on Genetic Algorithm



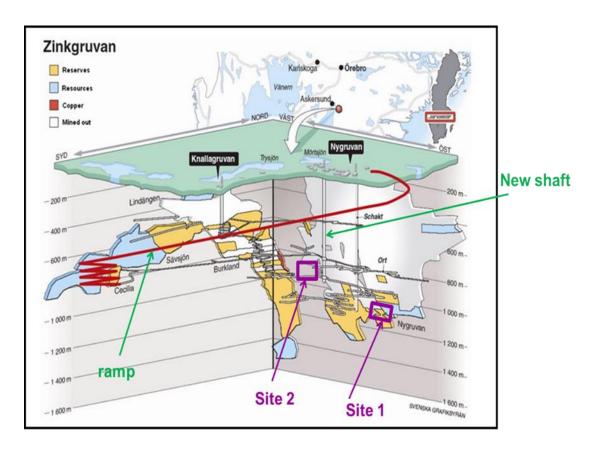
| | $\phi_{ u}$ 10 ¹⁰ .m ⁻² | % | $\phi_{ u}$ 10 ¹⁰ .m ⁻² | % | | | |
|----------------|---|------|---|------|--|--|--|
| $ u_{\mu}$ | 674 | 97.6 | 20 | 4.7 | | | |
| $ar{ u}_{\mu}$ | 11.8 | 1.7 | 396 | 94.8 | | | |
| ν_e | 4.76 | 0.67 | 0.13 | 0.03 | | | |
| $\bar{\nu}_e$ | 0.03 | 0.03 | 1.85 | 0.43 | | | |



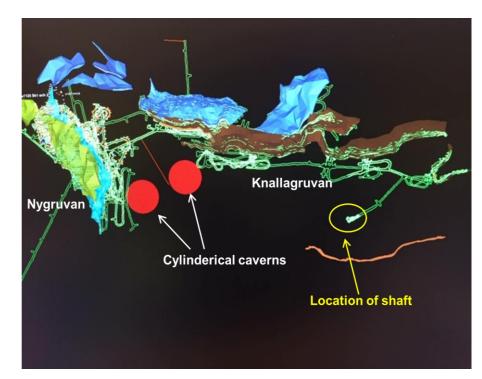


ð

Zinkgruvan mine

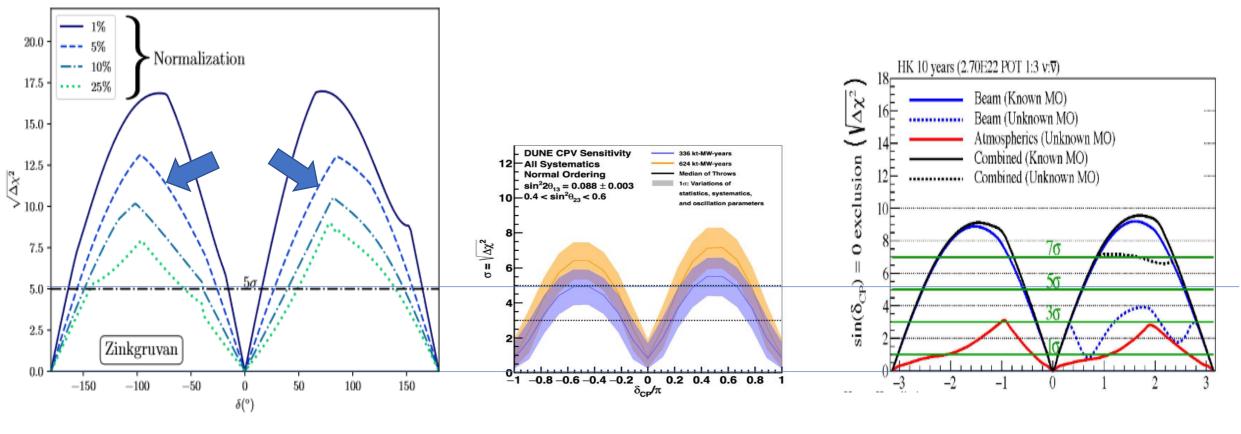


Potential location in Site 2



Site 2 is considered as best considering access to main transport infrastructure and located in an area less disturbed by mining activities

ESSnuSB in the international context – CPV discovery

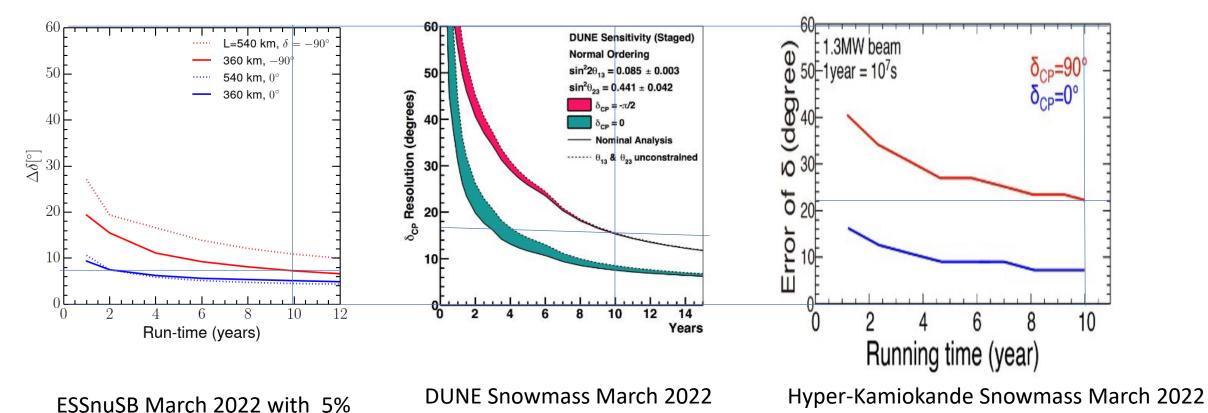


ESSnuSB March 2022 with 5% normalization error

DUNE Snowmass March 2022

Hyper-Kamiokande Snowmass March 2022

ESSnuSB in the international context – CPV resolution



normalization error

Table 5.5: The number of expected μ^{ID} events per running year, per level of the analysis, per flavour and interaction type, and per each horn polarity.

| Positive polarity | | | | | | | | |
|-------------------------------------|---|----------------------|---|---|---|---|---|---|
| | $\nu_{\mu} \operatorname{CC} \mu^{\mathrm{ID}}$ | $v_e CC \mu^{ID}$ | $\bar{\nu}_{\mu} \operatorname{CC} \mu^{\mathrm{ID}}$ | $\bar{\nu}_e \operatorname{CC} \mu^{\operatorname{ID}}$ | $\nu_{\mu} \operatorname{NC} \mu^{\mathrm{ID}}$ | $v_e \operatorname{NC} \mu^{\operatorname{ID}}$ | $\bar{\nu}_{\mu} \operatorname{NC} \mu^{\mathrm{ID}}$ | $\bar{\nu}_e \operatorname{NC} \mu^{\operatorname{ID}}$ |
| All interactions | 5.19×10^{7} | 2.88×10^{4} | 1.43×10^{5} | 19.7 | 2.29×10^{7} | 1.44×10^{5} | 8.44×10^{4} | 159 |
| Trigger | 5.13×10^{7} | 2.71×10^{4} | 1.42×10^{5} | 18.1 | 1.98×10^{6} | 1.36×10^{4} | 6150 | 10.2 |
| Sub-Cherenkov criterion | 3.10×10^{7} | 2.00×10^{4} | 1.06×10^{5} | 12.6 | 5.40×10^{4} | 678 | 179 | 0.2 |
| Reconstruction quality criteria | 2.59×10^{7} | 1.43×10^{4} | 9.29×10^{4} | 8.7 | 2.69×10^{4} | 407 | 111 | 0.1 |
| Cherenkov-ring resolution criterion | 2.12×10^{7} | 1.03×10^{4} | 7.69×10^{4} | 6.3 | 2.11×10^4 | 327 | 93.6 | 0.1 |
| Pion-like criteria | 2.12×10^{7} | 1.03×10^{4} | 7.69×10^{4} | 6.3 | 2.11×10^4 | 327 | 93.6 | 0.1 |
| Multi-subevent criterion | 2.10×10^{7} | 1.03×10^{4} | 7.69×10^{4} | 6.3 | 2.11×10^4 | 326 | 93.4 | 0.1 |
| Negative polarity | | | | | | | | |
| | $\nu_{\mu} \mathbf{CC} \mu^{\mathbf{ID}}$ | $v_e CC \mu^{ID}$ | $\bar{\nu}_{\mu} \operatorname{CC} \mu^{\mathrm{ID}}$ | $\bar{\nu}_e \operatorname{CC} \mu^{\operatorname{ID}}$ | $\nu_{\mu} \operatorname{NC} \mu^{\mathrm{ID}}$ | $v_e \operatorname{NC} \mu^{\operatorname{ID}}$ | $\bar{\nu}_{\mu} \operatorname{NC} \mu^{\mathrm{ID}}$ | $\bar{\nu}_e \operatorname{NC} \mu^{\operatorname{ID}}$ |
| All interactions | 5.17×10^{5} | 179 | 8.36×10^{6} | 2610 | 2.62×10^{5} | 983 | 5.05×10^{6} | 2.08×10^{4} |
| Trigger | 5.10×10^{5} | 168 | 8.31×10^{6} | 2400 | 2.20×10^{4} | 86.9 | 3.46×10^{5} | 1410 |
| Sub-Cherenkov criterion | 3.12×10^{5} | 125 | 5.55×10^{6} | 1690 | 799 | 4.9 | 5490 | 33.4 |
| Reconstruction quality criteria | 2.65×10^{5} | 89.0 | 4.71×10^{6} | 1170 | 456 | 3.1 | 3050 | 15.7 |
| Cherenkov-ring resolution criterion | 2.17×10^{5} | 65.5 | 3.87×10^{6} | 806 | 372 | 2.5 | 2720 | 12.8 |
| Pion-like criteria | 2.17×10^{5} | 65.5 | 3.87×10^{6} | 806 | 372 | 2.5 | 2720 | 12.8 |
| | | | | | | | | |

| Positive polarity | | | | | | | | |
|-------------------------------------|------------------------------|----------------------|--------------------------------------|---|--------------------------------|---------------------------------|--------------------------------------|---------------------------------------|
| | v_{μ} CC e^{ID} | $v_e CC e^{ID}$ | $\bar{\nu}_{\mu}$ CC e^{ID} | $\bar{v}_e \ \mathbf{CC} \ e^{\mathbf{ID}}$ | ν_{μ} NC e^{ID} | $v_e \text{ NC } e^{\text{ID}}$ | $\bar{\nu}_{\mu}$ NC e^{ID} | $\bar{v}_e \text{ NC } e^{\text{ID}}$ |
| All interactions | 1.50×10^{7} | 5.33×10^{5} | 4.28×10^{4} | 382 | 2.44×10^{7} | 1.65×10^{5} | 7.87×10^{4} | 142 |
| Trigger | 1.50×10^{7} | 5.33×10^{5} | 4.28×10^{4} | 382 | 2.44×10^{7} | 1.65×10^{5} | 7.87×10^{4} | 142 |
| Sub-Cherenkov criterion | 2.57×10^{6} | 5.14×10^{5} | 1.00×10^{4} | 359 | 8.93×10^{5} | 8570 | 3060 | 3.7 |
| Reconstruction quality criteria | 2.11×10^{6} | 4.69×10^{5} | 8380 | 327 | 7.62×10^{5} | 7360 | 2630 | 3.2 |
| Cherenkov-ring resolution criterion | 6.22×10^{5} | 3.70×10^{5} | 2190 | 256 | 6.55×10^{5} | 6390 | 2200 | 2.7 |
| Pion-like criteria | 9.63×10^{4} | 3.32×10^{5} | 209 | 234 | 7.19×10^{4} | 718 | 313 | 0.3 |
| Multi-subevent criterion | 3.95×10^{4} | 3.22×10^{5} | 80.9 | 234 | 7.09×10^{4} | 691 | 307 | 0.3 |
| Negative polarity | | | | | | | | |
| | v_{μ} CC e^{ID} | $v_e CC e^{ID}$ | \bar{v}_{μ} CC e^{ID} | $\bar{v}_e \ \mathbf{CC} \ e^{\mathbf{ID}}$ | v_{μ} NC e^{ID} | $v_e \text{ NC } e^{\text{ID}}$ | \bar{v}_{μ} NC e^{ID} | $\bar{v}_e \text{ NC } e^{\text{ID}}$ |
| All interactions | 1.66×10^{5} | 3260 | 2.49×10^{6} | 5.29×10^{4} | 2.68×10^{5} | 1070 | 4.61×10^{6} | 1.93×10^{4} |
| Trigger | 1.66×10^{5} | 3260 | 2.49×10^{6} | 5.29×10^{4} | 2.68×10^{5} | 1070 | 4.61×10^{6} | 1.93×10^{4} |
| Sub-Cherenkov criterion | 2.87×10^{4} | 3140 | 4.31×10^{5} | 5.09×10^{4} | 9860 | 53.2 | 1.22×10^{5} | 574 |
| Reconstruction quality criteria | 2.39×10^{4} | 2860 | 3.49×10^{5} | 4.66×10^{4} | 8500 | 45.8 | 1.06×10^{5} | 492 |
| Cherenkov-ring resolution criterion | 8000 | 2260 | 6.89×10^{4} | 3.66×10^4 | 7330 | 39.7 | 8.95×10^{4} | 426 |
| D' I'll i'l i'l | 1180 | 2020 | 9640 | 3.34×10^{4} | 940 | 4.5 | 1.14×10^{4} | 43.7 |
| Pion-like criteria | 1100 | 2020 | 20.0 | | | | | |

Table 5.4: The number of expected e^{ID} events per running year, per level of the analysis, per flavour and interaction type, and per each horn polarity.

Table 5.13: Expected number of neutrino interactions in 538 kt FD fiducial volume at a distance of 360 km (Zinkgruvan mine) in 200 days (one effective year). Shown for positive (negative) horn polarity.

| | Channel | Non oscillated | Oscillated | | | | | |
|----|---|-----------------------------|---|---|---|--|--|--|
| | Channel | Non oscillateu | $\delta_{CP} = 0$ | $\delta_{CP} = \pi/2$ | $\delta_{CP} = -\pi/2$ | | | |
| | $\nu_{\mu} \rightarrow \nu_{\mu}$ | 22 630.4 (231.0) | 10 508.7 (101.6) | 10 430.6 (5.8) | 10 430.6 (100.9) | | | |
| | $\nu_{\mu} \rightarrow \nu_{e}$ | 0 (0) | 768.3 (8.6) | 543.8 (5.8) | 1 159.9 (12.8) | | | |
| | $v_e \rightarrow v_e$ | 190.2 (1.2) | 177.9 (1.1) | 177.9 (1.1) | 177.9 (1.1) | | | |
| CC | $v_e \rightarrow v_\mu$ | 0 (0) | $5.3(3.3 \times 10^{-2})$ | $7.3 (4.5 \times 10^{-2})$ | $3.9(2.4 \times 10^{-2})$ | | | |
| cc | $\overline{\nu}_{\mu} \rightarrow \overline{\nu}_{\mu}$ | 62.4 (3 640.3) | 26.0 (1 896.8) | 26.0 (1 898.9) | 26.0 (1 898.9) | | | |
| | $\overline{v}_{\mu} \rightarrow \overline{v}_{e}$ | 0 (0) | 2.6 (116.1) | 3.5 (164.0) | 1.4 (56.8) | | | |
| | $\overline{\nu}_e \to \overline{\nu}_e$ | $1.3 \times 10^{-1} (18.5)$ | $1.3 \times 10^{-1} (17.5)$ | $1.3 \times 10^{-1} (17.5)$ | $1.2 \times 10^{-1} (17.5)$ | | | |
| | $\overline{\nu}_e \rightarrow \overline{\nu}_\mu$ | 0 (0) | $3.0 \times 10^{-3} (4.0 \times 10^{-1})$ | $1.5 \times 10^{-3} \ (2.1 \times 10^{-1})$ | $4.1 \times 10^{-3} (5.6 \times 10^{-1})$ | | | |
| | ν_{μ} | 16 015.1 (179.3) | | | | | | |
| NC | ve | 103.7 (0.7) | | | | | | |
| NC | $\overline{\nu}_{\mu}$ | 55.2 (3 265.5) | | | | | | |
| | $rac{\overline{ u}_{\mu}}{\overline{ u}_{e}}$ | $1 \times 10^{-1} (13.6)$ | | | | | | |

| | Channel | L = 540 km | L = 360 km |
|------------|---|---------------|-----------------|
| Signal | $ u_{\mu} \rightarrow \nu_e \ (\bar{\nu}_{\mu} \rightarrow \bar{\nu}_e) $ | 272.22(63.75) | 578.62 (101.18) |
| | $ u_{\mu} \to \nu_{\mu} \ (\bar{\nu}_{\mu} \to \bar{\nu}_{\mu}) $ | 31.01 (3.73) | 67.23 (11.51) |
| Background | $\nu_e \to \nu_e \ (\bar{\nu}_e \to \bar{\nu}_e)$ | 67.49(7.31) | 151.12 (16.66) |
| | $\nu_{\mu} \text{ NC } (\bar{\nu}_{\mu} \text{ NC})$ | 18.57(2.10) | 41.78 (4.73) |
| | $\bar{\nu}_{\mu} ightarrow \bar{\nu}_{e} \ (\nu_{\mu} ightarrow \nu_{e})$ | 1.08(3.08) | 1.94 (6.47) |

Table 1: Signal and major background events for the appearance channel corresponding to positive (negative) polarity per year for $\delta_{CP} = 0^{\circ}$.

| | Channel | L = 540 km | L = 360 km |
|------------|---|------------------|-------------------|
| Signal | $ \nu_{\mu} \to \nu_{\mu} \ (\bar{\nu}_{\mu} \to \bar{\nu}_{\mu}) $ | 4419.69 (733.31) | 7619.16 (1602.02) |
| | $\nu_e \to \nu_e \ (\bar{\nu}_e \to \bar{\nu}_e)$ | 7.77(0.02) | 17.08 (0.05) |
| Background | $\nu_{\mu} \text{ NC } (\bar{\nu}_{\mu} \text{ NC})$ | 69.23(8.24) | 155.77 (18.54) |
| | $ \nu_{\mu} \to \nu_{e} \ (\bar{\nu}_{\mu} \to \bar{\nu}_{e}) $ | 14.68(0.06) | 61.30 (0.17) |
| | $\bar{\nu}_{\mu} \to \bar{\nu}_{\mu} \ (\nu_{\mu} \to \nu_{\mu})$ | 12.35 (41.00) | 21.39 (72.59) |

Table 2: Signal and major background events for the disappearance channel corresponding to positive (negative) polarity per year for $\delta_{CP} = 0^{\circ}$.