

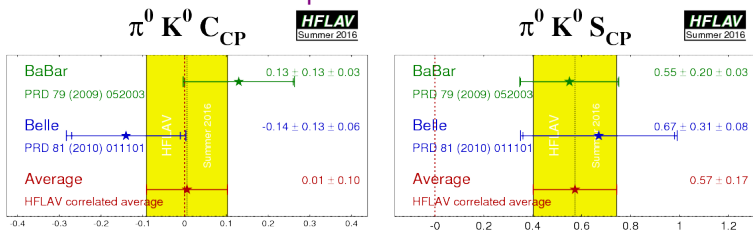
Motivation

- The sum-rule relation proposed by Gronau for $B \rightarrow K\pi$ provides a stringent test of SM

$$\mathcal{A}_{K^+\pi^-} + \mathcal{A}_{K^0\pi^+} \frac{\mathcal{B}(K^0\pi^+)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} = \mathcal{A}_{K^+\pi^0} \frac{\mathcal{B}(K^+\pi^0)}{\mathcal{B}(K^+\pi^-)} \frac{\tau_{B^0}}{\tau_{B^+}} + \mathcal{A}_{K^0\pi^0} \frac{\mathcal{B}(K^0\pi^0)}{\mathcal{B}(K^+\pi^-)}$$

- Predicted $\mathcal{A}_{K^0\pi^0} = -0.17 \pm 0.06$, Phys.Lett. B627 (2005) 82-8
- The limiting factor is $\mathcal{A}_{K^0\pi^0}$ precision. Need to push on this measurement, where Belle II is the key player.
- $B^0 \rightarrow K^0\pi^0$ is a golden mode at Belle II

Current Experimental status



B meson reconstruction

Selection criteria

$$B^0 \rightarrow K_S^0(\rightarrow \pi^+\pi^-)\pi^0(\rightarrow \gamma\gamma)$$

- π^0 reconstructed from a pair of photons
- K_S^0 reconstructed from two oppositely charged tracks, assumed to be pions

$$B^0 \rightarrow J/\psi(\rightarrow \mu^+\mu^-)K_S^0(\rightarrow \pi^+\pi^-) \text{ [control channel]}$$

- K_S^0 selection criteria are same like the signal mode
- Only K_S^0 used for B^0 vertexing to mimic the signal decay
- J/ψ reconstructed from dimuons

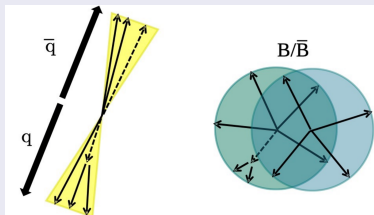
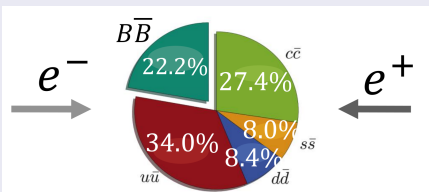
- Following two kinematic variables used to select B meson

$$M_{bc} = \sqrt{E_{beam}^{*2} - \vec{p}_B^{*2}}$$

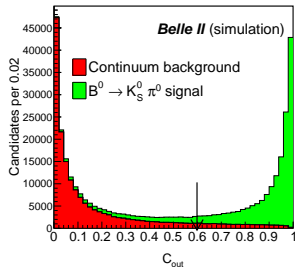
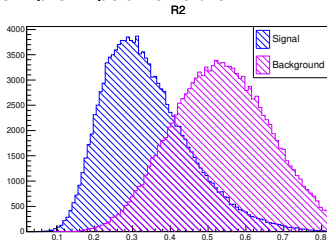
$$\Delta E = E_{beam}^* - E_B^*$$

Background study

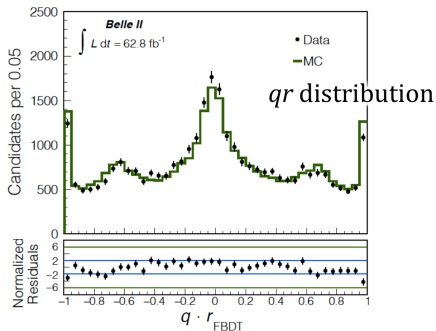
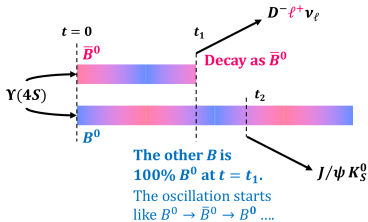
Continuum suppression



- Use a BDT to suppress the $e^+e^- \rightarrow q\bar{q}$ background
- An example input variable



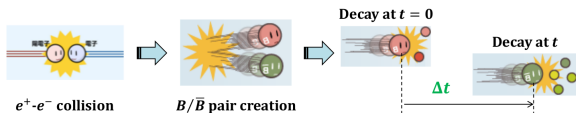
Flavor tagging



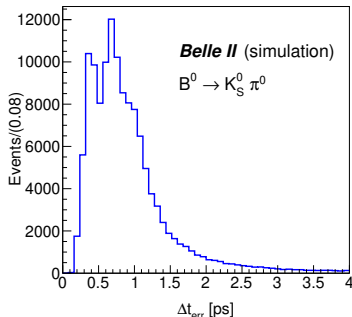
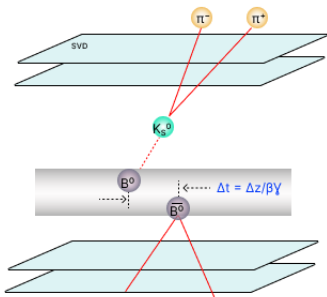
- $q = +1$ for B^0 and $q = -1$ for \bar{B}^0 tag
- $r = 0$ for no flavor information
- $r = 1$ for unambiguous flavor assignment
- Wrong tagging probability

$$w = \frac{1-r}{2}$$

Going for time-dependent analysis



- **Challenge:** For $K_S^0\pi^0$, no primary charge track to help in vertexing, which leads to a poor decay time resolution
- B^0 vertex position is determined by projecting the K_S^0 trajectory to the interaction region



TDCPV fitter preparation

- Divide the dataset into 7 $q \cdot r$ bins for a simultaneous maximum likelihood fit:

Compt.	Treatment during the fit
Signal	PDF shapes fixed from a $q \cdot r$ binned signal MC fit Floating parameters are the signal yield and \mathcal{A}_{CP} Fix the \mathcal{S}_{CP} value to the world-average of 0.57 [1]
$B\bar{B}$	PDF shapes are fixed from integrated $q \cdot r$ bin MC fit $B\bar{B}$ yield is floated with Gauss-constraint.
$q\bar{q}$	PDF shape parameters are floated over the $q \cdot r$ bin

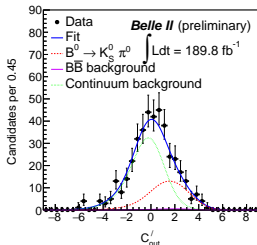
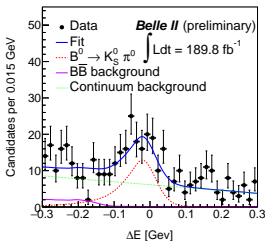
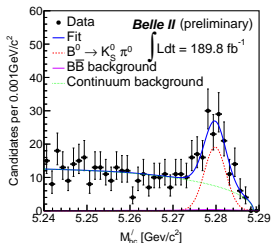
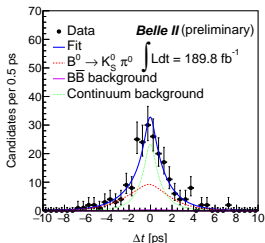
- Signal and background modelled with an empirical PDF determined from MC
- **Challenge:** Perform a four-dimensional simultaneous fit in seven $q \cdot r$ bins
- Validate the framework with $B^0 \rightarrow J/\psi K_S^0$ control channel.

1] <https://hflav-eos.web.cern.ch/hflav-eos/triangle/pdg2021>

Projection of the fit result

- Signal enhanced region: $5.27 < M_{bc} < 5.29 \text{ GeV}/c^2$, $-0.15 < \Delta E < 0.1 \text{ GeV}$ and $C'_{out} > 0$

Shown fit projections are for the candidates with integrated $q \cdot r$ bin



Preliminary

Final results

Preliminary

Dominant systematic uncertainties

Source	$\delta\mathcal{B}$ (%)	$\delta\mathcal{A}_{CP}$
π^0 reconstruction efficiency	7.5	–
Resolution function	–	0.050

Observable	Fitted value	World-average[1]
$\mathcal{B}(B^0 \rightarrow K^0\pi^0) \times 10^{-6}$	$11.0 \pm 1.2(stat) \pm 1.0(syst)$	9.9 ± 0.5
\mathcal{A}_{CP}	$-0.41^{+0.30}_{-0.32}(stat) \pm 0.09(syst)$	-0.01 ± 0.1

$$N_{\text{sig}} = 135.0^{+16.0}_{-15.0}$$

- \mathcal{B} and \mathcal{A}_{CP} are consistent with PDG values within uncertainty

1] <https://hflav-eos.web.cern.ch/hflav-eos/triangle/pdg2021>

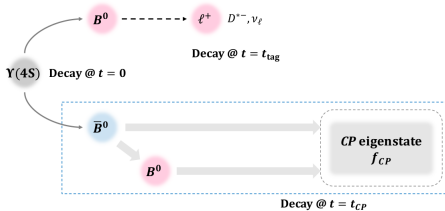
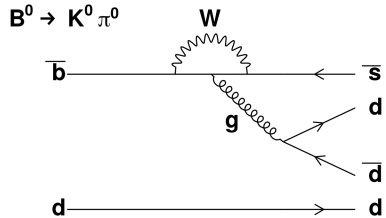
Summary and Plans

- Studied the 189.8fb^{-1} data to measure \mathcal{B} and \mathcal{A}_{CP}
- \mathcal{B} and \mathcal{A}_{CP} are consistent with PDG values within uncertainty
- The Belle II public result is available online:
<https://arxiv.org/abs/2206.07453>
- Work underway to have a journal paper soon with 361.5fb^{-1} dataset

Thank You

Motivation

- In the SM, the decay $B^0 \rightarrow K^0 \pi^0$ proceeds via $b \rightarrow s$ loop diagrams.
- Such FCNC transitions are highly suppressed in the SM and sensitive to non-SM particles appearing in the loops.



- τ_{B^0} = lifetime of B^0 ,
- $\Delta m_d = B^0 - \bar{B}^0$ mixing frequency
- $\Delta t = t_{CP} - t_{tag}$ (decay time diff.)
- $A_{CP} = \frac{\Gamma(\bar{B}^0 \rightarrow f_{CP}) - \Gamma(B^0 \rightarrow f_{CP})}{\Gamma(\bar{B}^0 \rightarrow f_{CP}) + \Gamma(B^0 \rightarrow f_{CP})} =$
- S_{CP} = mixing induced CPV
- In SM, $A_{CP} \approx 0$ & $S_{CP} = \sin 2\beta$

$$\mathcal{P}(\Delta t) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} [1 + q\{\mathcal{A}_{CP} \cos(\Delta m_d \Delta t) + \mathcal{S}_{CP} \sin(\Delta m_d \Delta t)\}]$$

Outline

- Motivation
- Development of time-dependent CPV fit
- Systematic uncertainties
- First measurement of \mathcal{B} and A_{CP}
- Summary and Plans

Analysis overview

Selection

- baseline selection cut optimised on simulation followed by optimisation of continuum suppression cut.

Efficiencies and corrections

- efficiencies from simulation, validated on data

Signal extraction

- develop fit model from simulation, adjusted on control mode
- determine selection efficiencies for \mathcal{B} calculation

Systematic uncertainties

- toy studies and control mode analyses

Validation & unblinding

- validate the full analysis on control on data
- apply full analysis to data

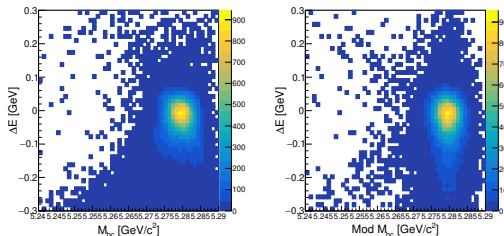
Modified M_{bc}

- π^0 in the final state causes correlation between ΔE and M_{bc} .

- $$M_{bc} = \sqrt{E_{beam}^{*2} - p_B^{*2}}$$

- $$p_B^* = p_{K_S^0}^* + p_{\pi^0}^*$$

- $$p_B^* = p_{K_S^0}^* + \frac{p_{\pi^0}^*}{|p_{\pi^0}^*|} \cdot \sqrt{(E_{beam}^* - E_{K_S^0}^*)^2 - m_{\pi^0}^2}$$

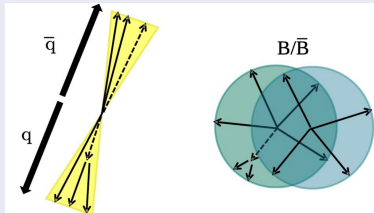
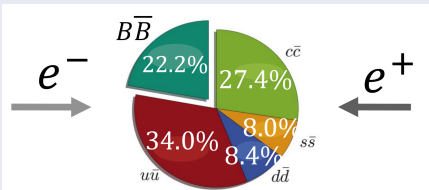


Comp.	Before	After
Signal	18.9%	-0.7%
$B\bar{B}$	-6.4%	4.4%
$q\bar{q}$	-0.4%	0.4%

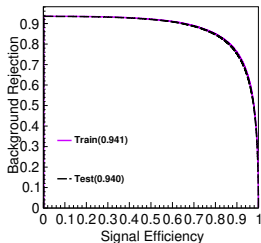
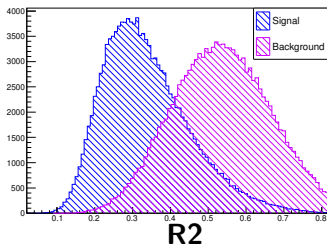
Following M_{bc} referred as modified M'_{bc}

Background study

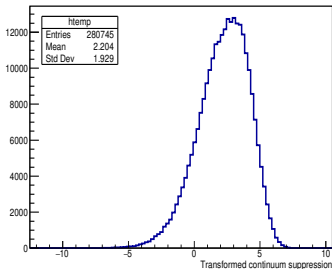
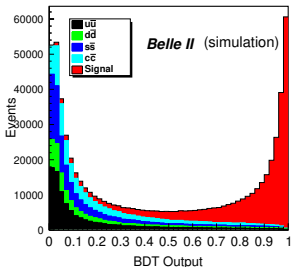
Continuum suppression



- $$R_2 = \frac{H_2}{H_0} = \frac{\sum_i^N \sum_j^N [|\vec{p}_i| |\vec{p}_j| \cdot (3 \cos^2 \theta_{ij} - 1)]}{2 \sum_i^N \sum_j^N [|\vec{p}_i| |\vec{p}_j|]}, \text{ for } q\bar{q} \text{ events } \cos \theta_{ij} \approx 1$$



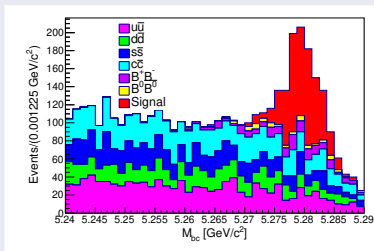
Log-transform of continuum output



- We transform the BDT classifier output (C_{out}) to (C'_{out}) in order to parametrize using a simple PDF
- Transform continuum suppression variable is defined as

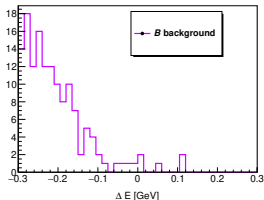
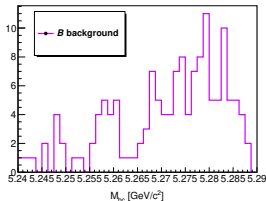
$$C'_{out} = \log\left(\frac{C_{out} - C_{out_{min}}}{C_{out_{max}} - C_{out}}\right) \quad (1)$$

where $C_{out_{max}}=0.99$ and $C_{out_{min}}=0.60$



Background study continued

- We do not find any $B\bar{B}$ events peaking in the ΔE signal region.
- There is non-negligible $B\bar{B}$ combinatorial background present.

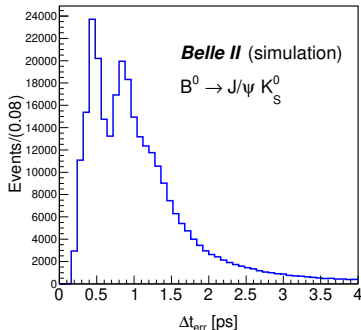
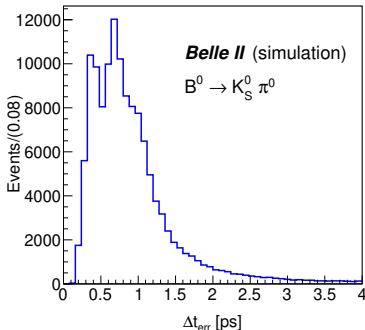


Correlation among fit variables

Category	$\Delta E - \Delta t$	$M_{bc} - C'_{out}$	$M_{bc} - \Delta t$	$\Delta E - C'_{out}$	$\Delta t - C'_{out}$
Signal	-0.01%	0.8%	0.7%	0.2%	0.3%
$B\bar{B}$	-0.1%	2.1%	-0.6%	-3.7%	-3.2%
$q\bar{q}$	-0.3%	-0.5%	0.5%	0.2%	0.6%

Decay-time uncertainty and time resolution

- Double peak observed in Δt_{err} distribution.
- Feature reproduced in the control channel.
- Considering contributions from both the peaks.
- Sum of two Gaussian use for the resolution function.



- Removing poor decay time resolution by applying $\sigma_{\Delta t_{err}} < 2.5$ ps.
- Signal efficiency = 12.3% ($N_{sig}^{expt} = 122$)

Validation results

- Check consistency with 1000 experiment
 - Pure toys: generate data from the PDFs and fit back.
 - GSIM toys: signal are sampling from simulated data, $B\bar{B}$ and $q\bar{q}$ are generated from PDFs

Pure toy

Parameter	Pull mean	Pull width	Fit value	Expected
Signal yield	0.06 ± 0.03	1.06 ± 0.03	124 ± 15	122
Continuum yield	0.02 ± 0.04	1.02 ± 0.03	2501 ± 53	2509
$B\bar{B}$ yield	gauss-cons.	gauss-cons.	43 ± 4	43
\mathcal{A}_{CP}	0.02 ± 0.04	1.08 ± 0.03	0.02 ± 0.33	0.0

GSIM toy

Parameter	Pull mean	Pull width	Fit value	Expected
Signal yield	0.03 ± 0.04	1.03 ± 0.03	123 ± 14	122
Continuum yield	-0.03 ± 0.04	1.02 ± 0.03	2506 ± 49	2509
$B\bar{B}$ yield	gauss-cons.	gauss-cons.	43 ± 4	43
\mathcal{A}_{CP}	-0.07 ± 0.04	0.98 ± 0.03	-0.01 ± 0.30	0.0

- There is no significant bias!

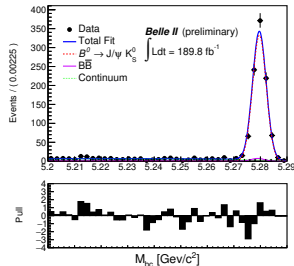
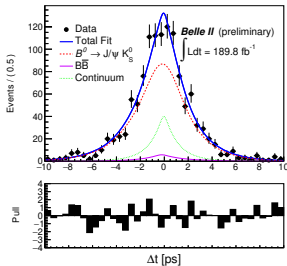
Control channel modelling

“Yesterday’s discovery is today’s calibration” – R.Feynman

- Want to perform the full analysis on the $B^0 \rightarrow J/\psi(\rightarrow \mu^+\mu^-)K_S^0$ decay as a validation. Compare with known values, a measurement of $\rightarrow B^0$ lifetime, A_{CP} and S_{CP}
- Only K_S^0 used for B^0 vertexing
- First, develop the analysis on simulation, as done for the rare decay
- Simplified fit: since $B^0 \rightarrow J/\psi K_S^0$ is much cleaner, don’t need CS. Fit M_{bc} and Δt only (details in backup).
- Same approach for flavour-tagging and time-dependent PDF:
 $\rightarrow 7 q \cdot r$ bin fit. \rightarrow cut a $\Delta t_{err} < 2.5$ ps, and resolution function (sum of two Gaussian)

B Lifetime fit(Data)

- 189.8 fb^{-1} Data



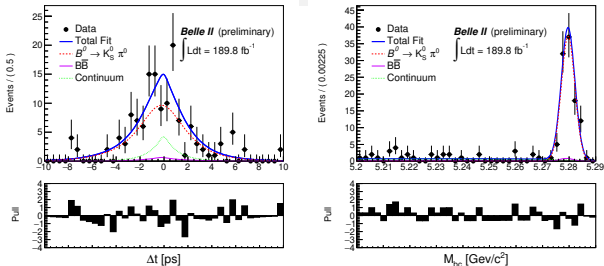
Preliminary !

Parameter	Fitted value	WA[1] value
Lifetime (ps)	$1.59^{+0.09}_{-0.08}$	1.519 ± 0.004

- Lifetime is consistent within uncertainty.

1] <https://hflav-eos.web.cern.ch/hflav-eos/triangle/pdg2021>

Example of fit projection (Data)



Preliminary !

Figure: 4th-bin fit projection in Data

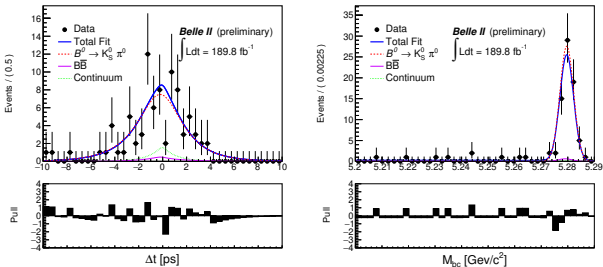


Figure: 5th-bin fit projection in Data

- Rest of the bin fit projection shown in backup slide

Results for $B^0 \rightarrow J/\psi K_S^0$

Preliminary !

- Sample size corresponding to 189.8 fb^{-1}

Parameter	Fitted value	WA[1]
\mathcal{A}_{CP}	$0.031^{+0.099}_{-0.098}$	0.000 ± 0.020
\mathcal{S}_{CP}	$0.818^{+0.156}_{-0.164}$	0.695 ± 0.019

- \mathcal{A}_{CP} and \mathcal{S}_{CP} are consistent within uncertainty.

1] <https://hflav-eos.web.cern.ch/hflav-eos/triangle/pdg2021>

Systematic uncertainty

Preliminary !

Table: List of systematic uncertainties contributing to the measured branching fraction.

Source	$\delta\mathcal{B}(\%)$
Tracking efficiency	0.6
K_S^0 reconstruction efficiency	4.2
π^0 reconstruction efficiency	7.5
Cont. supp. efficiency (see backup)	1.6
Number of $B\bar{B}$ events	3.2
Signal model	1.0
Continuum background model	0.9
Possible fit bias	2.0
Physics parameters	0.4
Total	9.6

Systematic uncertainty

Preliminary !

Table: List of systematic uncertainties contributing to \mathcal{A}_{CP} .

Source	$\delta\mathcal{A}_{CP}$
Flavor tagging	0.040
Resolution function	0.050
Physics parameter	0.021
B decay background asymmetry	0.002
Possible fit bias	0.010
Tag-side interference[1]	0.038
Background modeling	0.004
Signal modeling	0.015
Total	0.086

1] I. Adachi et al. (Belle Collaboration), Phys. Rev. Lett. **108**, 171802 (2012)

CKM Matrix

- The CKM matrix is a unitary matrix:
$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}^\dagger \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \equiv \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

From the unitarity condition, 6 equations are derived.

$$\begin{aligned} \text{(a)} \quad & V_{ud}V_{us}^* + V_{cd}V_{cs}^* + V_{td}V_{ts}^* = 0 & \text{(d)} \quad & V_{cd}V_{td}^* + V_{cs}V_{ts}^* + V_{cb}V_{tb}^* = 0 \\ \text{(b)} \quad & V_{ud}V_{cd}^* + V_{us}V_{cs}^* + V_{ub}V_{cb}^* = 0 & \text{(e)} \quad & V_{ud}V_{td}^* + V_{us}V_{ts}^* + V_{ub}V_{tb}^* = 0 \\ \text{(c)} \quad & V_{us}V_{ub}^* + V_{cs}V_{cb}^* + V_{ts}V_{tb}^* = 0 & \text{(f)} \quad & V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0 \end{aligned}$$

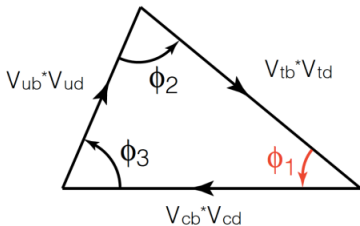
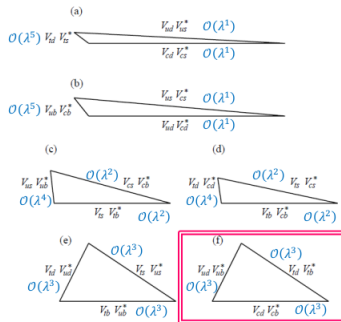
- From physics discussion, the Wolfenstein parameterization is obtained:

$$V_{\text{CKM}} \equiv \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

- You need to remember that V_{td} and V_{ub} are complex.
- You need to remember $\lambda \approx 0.2$ plus the order of λ for each element.
- You need to remember $A \approx 0.8$.

CKM Triangle

- Each of the equation forms a triangle on the complex plane.
- The bottom right triangle, which is associated to the equation $V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$ is moderately large.
- By assuming $V_{ud}V_{ub}^*$, $V_{cd}V_{cb}^*$, and $V_{td}V_{tb}^*$ are vectors, we can draw a triangle associated to the equation on the complex plane, which is called "CKM triangle".



Interior angle definition

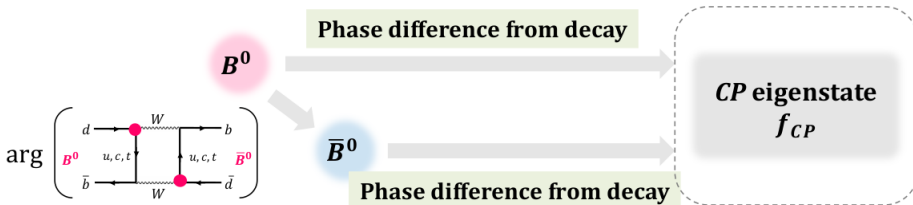
$$\phi_1 \equiv \arg\left(-\frac{V_{cd}V_{cb}^*}{V_{td}V_{tb}^*}\right) = \pi - \arg(V_{td})$$

$$\phi_2 \equiv \arg\left(-\frac{V_{td}V_{tb}^*}{V_{ud}V_{ub}^*}\right)$$

$$\phi_3 \equiv \arg\left(-\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*}\right)$$

If the KM theory is correct, $\phi_1 \neq 0, \pi$.

Mixing-Induced CP Violation



$$\arg \left(\begin{array}{c} d \xrightarrow{\quad} W \xrightarrow{\quad} b \\ u, c, t \uparrow \quad \downarrow u, c, t \\ \bar{b} \xrightarrow{\quad} W \xrightarrow{\quad} \bar{d} \end{array} \right)$$

Phase difference from the mixing $\pm 2\phi_1$

$$B^0 \rightarrow J/\psi K_S^0$$

$\left(\begin{array}{c} \bar{c} \\ c \end{array} \right) J/\psi$

$\left(\begin{array}{c} \bar{s} \\ s \end{array} \right) K^0 \rightarrow K_S$

$\left(\begin{array}{c} \bar{b} \\ d \end{array} \right) B^0$

V_{cb}^* W V_{cs}

$$\arg(B^0 \rightarrow J/\psi K_S^0) = \arg(V_{cb}^* V_{cs}) = 0$$

$$\bar{B}^0 \rightarrow J/\psi K_S^0$$

$\left(\begin{array}{c} c \\ \bar{c} \end{array} \right) J/\psi$

$\left(\begin{array}{c} s \\ \bar{s} \end{array} \right) \bar{K}^0 \rightarrow K_S$

$\left(\begin{array}{c} b \\ \bar{d} \end{array} \right) \bar{B}^0$

V_{cb} W V_{cs}^*

$$\arg(\bar{B}^0 \rightarrow J/\psi K_S^0) = \arg(V_{cb} V_{cs}^*) = 0$$

Remember only $\arg(V_{td})$ and $\arg(V_{ub})$ are non zero.

We can extract ϕ_1 by analyzing the $B \rightarrow J/\psi K^0$ and other $(c\bar{c})K^0$ modes.

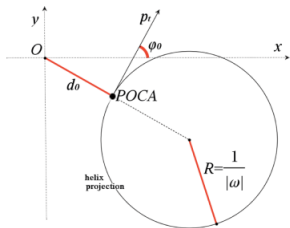
Determination of the B -Decay Position

- Charged particle trajectory in a magnetic field = **helix**

helix parameter $\equiv (d_0, \phi_0, \omega, z_0, \tan \lambda)$

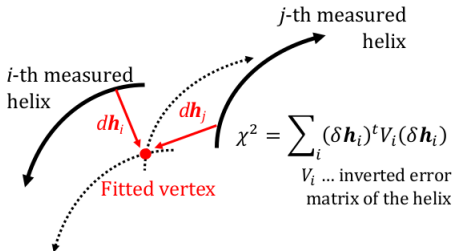
Belle II (BELLE2-NOTE-TE-2018-003)

$(x^P, y^P, z^P, p_x^P, p_y^P, p_z^P)$ at
POCA = Point of Closest Approach



$$\begin{aligned} x^P &= d_0 \sin \phi_0 & p_x^P &= \cos \phi_0 / \alpha \omega \\ y^P &= -d_0 \cos \phi_0 & p_y^P &= \sin \phi_0 / \alpha \omega \\ z^P &= z_0 & p_z^P &= \tan \lambda / \alpha \omega \end{aligned}$$

- The decay position (called vertex) is determined with the χ^2 -minimizing method.



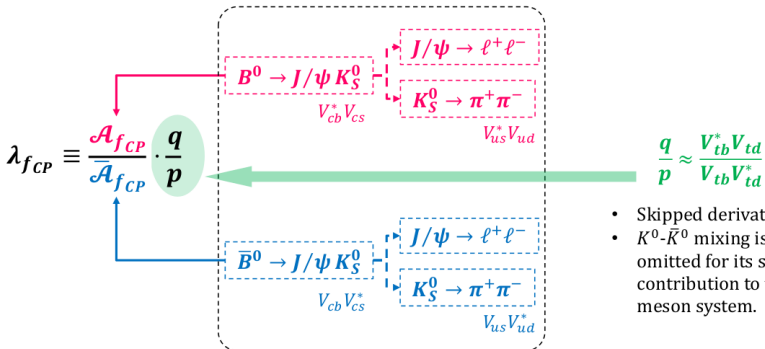
The vertex that gives the minimum χ^2 is taken as the fitted vertex (KFit).

When the “IP constraint” is applied to KFit, $\chi^2 + \chi_{IP}^2$ is minimized where χ_{IP}^2 accounts for the IP spread.

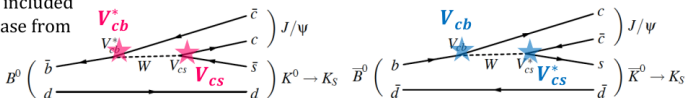
Typical vertex resolution: $\delta z \approx 50 \mu\text{m}$

The Last Piece, $\lambda_{f_{CP}}$

- Assume we use the golden mode for the test of the Kobayashi-Maskawa theory, where $B^0 \rightarrow J/\psi K_S^0$ and $\bar{B}^0 \rightarrow J/\psi K_S^0$.



- No V_{td} or V_{ub} included
 \rightarrow no CKM phase from the decay.



Application: CPV in B Decays at Belle (II)

- For $B^0(\bar{B}^0) \rightarrow J/\psi K_S^0$, $\lambda_{J/\psi K_S^0} \equiv \frac{\mathcal{A}_{f_{CP}}}{\bar{\mathcal{A}}_{f_{CP}}} \cdot \frac{q}{p} = \xi_{J/\psi K_S^0} \frac{V_{cb}^* V_{cs} V_{us}^* V_{ud}}{V_{cb} V_{cs}^* V_{us} V_{ud}^*} \cdot \frac{V_{ub}^* V_{td}}{V_{ub} V_{td}^*}$

Since only V_{td} and V_{ub} are complex, $\lambda_{J/\psi K_S^0} = \xi_{J/\psi K_S^0} \cdot e^{-2i\phi_1}$.

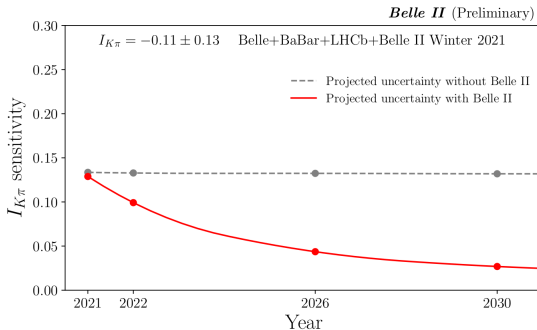
$$\mathcal{I}m(\lambda_{J/\psi K_S^0}) = -\xi_{J/\psi K_S^0} \sin 2\phi_1 = \sin 2\phi_1.$$

$$P(t; \ell^\pm) = \frac{1}{2\tau_{B^0}} e^{-\frac{|\Delta t|}{\tau_{B^0}}} (1 \pm \sin 2\phi_1 \sin \Delta m_d \Delta t)$$

- $\mathcal{I}m(\lambda_{f_{CP}})$ depends on the $\mathcal{A}_{f_{CP}}$ and $\bar{\mathcal{A}}_{f_{CP}}$, which are determined by the chosen $B^0(\bar{B}^0) \rightarrow f_{CP}$ mode. For example, if one chooses $B^0(\bar{B}^0) \rightarrow \pi^+ \pi^-$, he/she obtains the $P(t; \ell^\pm)$ equation with $\sin 2\phi_2$.

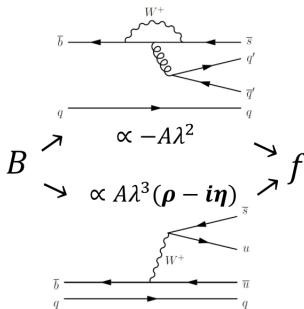
$\mathcal{B}[10^{-6}]$		
Mode	BaBar	Belle
$K^+\pi^-$	$19.1 \pm 0.6 \pm 0.6$ [16]	$20.00 \pm 0.34 \pm 0.60$ [17]
$K^+\pi^0$	$13.6 \pm 0.6 \pm 0.7$ [18]	$12.62 \pm 0.31 \pm 0.56$ [17]
$K^0\pi^+$	$23.9 \pm 1.1 \pm 1.0$ [19]	$23.97 \pm 0.53 \pm 0.71$ [17]
$K^0\pi^0$	$10.1 \pm 0.6 \pm 0.4$ [20]	$9.68 \pm 0.46 \pm 0.50$ [17]

\mathcal{A}_{CP}				
Mode	BaBar	Belle	LHCb	CDF
$K^+\pi^-$	$-0.107 \pm 0.016^{+0.006}_{-0.004}$ [20]	$-0.069 \pm 0.014 \pm 0.007$ [17]	$-0.084 \pm 0.004 \pm 0.003$ [21]	$-0.083 \pm 0.013 \pm 0.004$ [22]
$K^+\pi^0$	$0.030 \pm 0.039 \pm 0.010$ [18]	$0.043 \pm 0.024 \pm 0.002$ [17]	$0.025 \pm 0.015 \pm 0.006 \pm 0.003$ [23]	
$K^0\pi^+$	$-0.029 \pm 0.039 \pm 0.010$ [19]	$-0.011 \pm 0.021 \pm 0.006$ [17]	$-0.022 \pm 0.025 \pm 0.010$ [24]	
$K^0\pi^0$	$-0.13 \pm 0.13 \pm 0.03$ [25]	$0.14 \pm 0.13 \pm 0.06$ [26]		



CP Violation

- Physical laws not invariant under charge conjugation + parity inversion (mirror flip)
- Consequence of interference when a physical process can proceed in different ways
- CP violation in mixing: $B^0 \rightarrow \bar{B}^0 \neq \bar{B}^0 \rightarrow B^0$
- Indirect CP violation: asymmetry due to interference between mixing and decay amplitudes
- Direct CP violation:** $B \rightarrow f \neq \bar{B} \rightarrow \bar{f}$ due to interference in decay amplitudes
 - Requires non-zero relative weak and strong phase between amplitudes

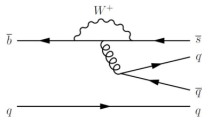


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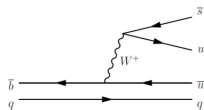
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The $B \rightarrow K\pi$ System

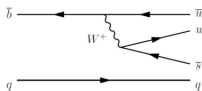
- $B^0 \rightarrow K^+\pi^-, B^0 \rightarrow K^0\pi^0,$
 $B^+ \rightarrow K^+\pi^0, B^+ \rightarrow K^0\pi^+$
- Dominated by QCD penguin diagrams
 - Suppressed by loop
 - Tree suppressed by V_{ub}
- Different $K\pi$ decays have contributions from different diagrams
- Potentially sensitive to new physics through massive virtual particles in loops



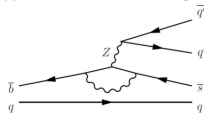
(a) $B \rightarrow K\pi$ penguin diagrams



(b) $B \rightarrow K^+\pi$ colour-favored tree diagrams



(c) $B \rightarrow K\pi^0$ color-suppressed tree diagrams

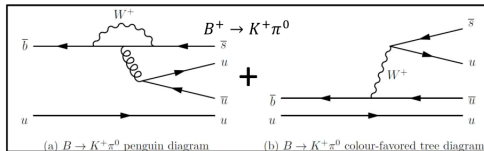
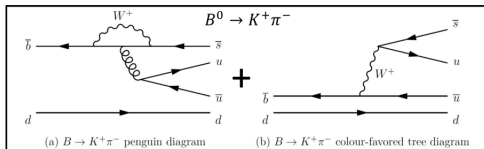


(d) $B \rightarrow K\pi^0$ electroweak penguin diagrams

The $K\pi$ Puzzle

- CP asymmetry in $B^0 \rightarrow K^+\pi^-$ and $B^+ \rightarrow K^+\pi^0$ from interference between tree and penguin diagrams
- Expected to be equal from isospin arguments
- Differs by more than 5σ according to current measurements

$$A_{CP}(B^+ \rightarrow K^+\pi^0) - A_{CP}(B^0 \rightarrow K^+\pi^-) = 0.124 \pm 0.021$$



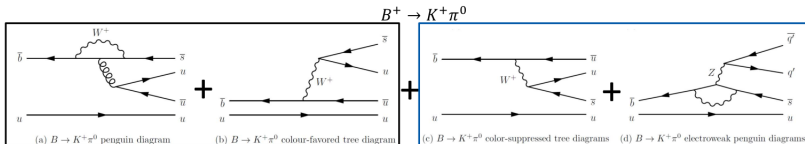
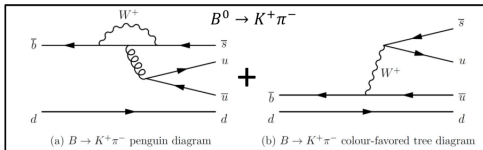
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The $K\pi$ Puzzle

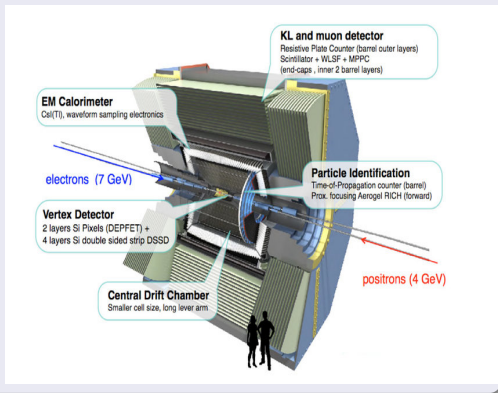
$$A_{CP}(B^+ \rightarrow K^+\pi^0) - A_{CP}(B^0 \rightarrow K^+\pi^-) = 0.124 \pm 0.021$$

- Color-suppressed tree and electroweak penguin diagrams contribute to $K^+\pi^0$ but not $K^+\pi^-$



SuperKEKB and Belle II Detector

- Asymmetric collider: e^- to 7 GeV and e^+ to 4 GeV
→ clean experimental environment
- World record peak luminosity:
 $3.1 \times 10^{34} \text{cm}^{-2}\text{s}^{-1}$
- New tracking system and improved vertexing
- Improved particle identification
- Better time resolution at calorimeter



Goal:

- Collect more than 50ab^{-1} data ($5 \times 10^{10} B\bar{B}$ pairs)
- 700 $B\bar{B}$ pairs/second

Currently:

- 216fb^{-1} data are collected. Today: results on $\approx 63\text{fb}^{-1}$

Selection criteria

$B^0 \rightarrow K_S^0 \pi^0$ selection

- $120 < m_{\pi^0} < 145$ MeV and $|\cos \theta_H| < 0.98$
- Barrel $E_\gamma > 30$, Backward $E_\gamma > 60$ and Forward $E_\gamma > 80$ MeV
- $482 < m_{K_S^0} < 513$ MeV
- $5.24 < M_{bc} < 5.3$ GeV and $-0.3 < \Delta E < 0.3$ GeV

$B^0 \rightarrow J/\psi K_S^0$ selection

- Criterias are taken from BELLE2-NOTE-PH-2020-038.
- $dr < 0.5$ cm, $|dz| < 3$ cm, for muon tracks.
- $\text{muonID}(\mu^+) \text{ or } \text{muonID}(\mu^-) > 0.2$
- $2.80 < M_{J/\psi} < 3.40$ GeV and $482 < M_{K_S^0} < 513$ MeV
- $5.2 < M_{bc} < 5.3$ GeV and $|\Delta E| < 0.05$ GeV
- For CP-side: IP constraint and only K_S^0 vertexing
- For tag-side : IP constraint
- $\sigma_{\Delta t} < 2.5$ ps

Rare components investigation

2D (M_{bc} , ΔE) Extended Fit (Cont'd)

- Rare background contributing to the analysis region:

expected @ 62.8 fb⁻¹

$$N = \int \mathcal{L} dt \cdot \sigma \cdot f^{+-} \cdot 2 \cdot \mathcal{B} \cdot \epsilon$$

Mode	$\mathcal{B}[10^{-6}]$ (PDG2020 Avg. [3])	$\epsilon[\%]$	Yield
$\rho^+ K^0$	$7.3^{+1.0}_{-1.2}$	1.05	5.5 ± 0.8
$K^*(892)^+ \pi^0$	6.8 ± 0.9	0.85	4.1 ± 0.5
$X_{s,u} \gamma$	349 ± 19	<0.01	0.7 ± 0.0
$a_1(1260)^+ K^0$	35 ± 7	<0.01	0.1 ± 0.0
$f_2(1270) K^0$	$2.7^{+1.3}_{-1.2}$	0.52	1.0 ± 0.4
$f_0(980) K^0$	4.1 ± 0.4	0.19	0.5 ± 0.1
$X_{s,d} \gamma$	349 ± 19	<0.01	0.5 ± 0.0
$K_S^0 K_S^0$	0.61 ± 0.08	0.50	0.2 ± 0.0
$K^0 \eta'$	66 ± 4	<0.01	0.1 ± 0.0
Sum			12.7 ± 1.1

dominant processes
 $B \rightarrow K^0 \pi^+ \pi^0$
 (PDG; PRD)

$$N = \int \mathcal{L} dt \cdot \sigma \cdot f^{00} \cdot 2 \cdot \mathcal{B} \cdot \epsilon$$

- Finally assign a Gauss($\mu=12.7$, $\sigma=1.1$) constraint on the normalization of rare background

Thrust

- **Thrust:** For a collection of N momenta \vec{p}_i ($i=1, \dots, N$), the thrust axis \vec{T} is defined as the unit vector along which their total projection is maximal.
- $T = \max \frac{\sum_i^N |\hat{T} \cdot \vec{p}_i|}{\sum_i^N |\vec{p}_i|}$

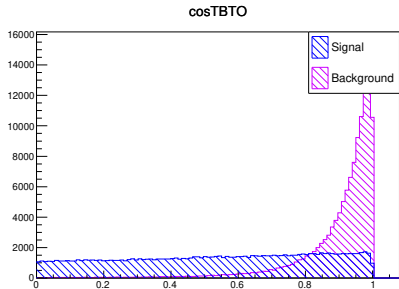
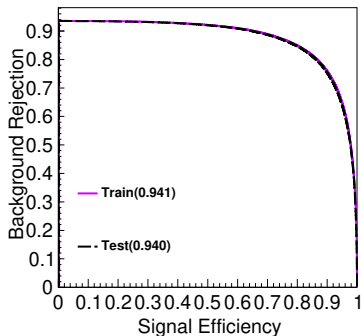
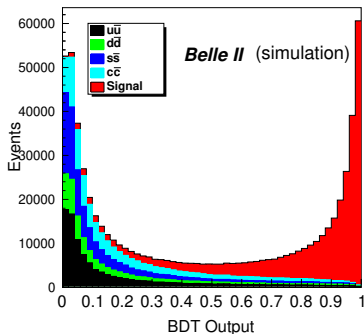


Figure: Cosine angle between signal B -meson and ROE (rest of the events)

Continuum suppression

- FatBDT as the multivariate classifier.
- Same number of signal and background events.
- 600 fb^{-1} for training and 400 fb^{-1} for testing.
- Same classifier input used(BELLE2-NOTE-PH-2020-046,BELLE2-NOTE-PH-2020-007).

Classifier Output



Background rejection comparison

Using our CS weight file

1) generic BKG to train CS

Cut	BKG rej.	# $u\bar{u}$	# $d\bar{d}$	# $s\bar{s}$	# $c\bar{c}$	# $B^0\bar{B}^0$	# B^+B^-	# signal
0.0		5434	2287	4180	4280	109	22	98
0.9	98.33 %	80	46	52	90	58	11	53

2) Continuum BKG to train CS

Cut	BKG rej.	# $u\bar{u}$	# $d\bar{d}$	# $s\bar{s}$	# $c\bar{c}$	# $B^0\bar{B}^0$	# B^+B^-	# signal
0.0		5434	2287	4180	4280	109	22	98
0.9	98.25 %	90	49	58	84	54	9	48

Using BELLE2-NOTE-PH-2020-046 CS weight file

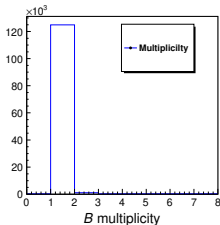
https://stash.desy.de/projects/B2B2C/repos/btohadronscripts/browse/BToCharmless_WithCorr_CSFBDT.root

Cut	BKG rej.	# $u\bar{u}$	# $d\bar{d}$	# $s\bar{s}$	# $c\bar{c}$	# $B^0\bar{B}^0$	# B^+B^-	# signal
0.0		5434	2287	4180	4280	109	22	98
0.9	98.39 %	74	45	52	88	54	11	48

- Now we use the common **BToCharmless weight file** for CS

Best candidate selection

- Found some events with more than one B candidate in an event.

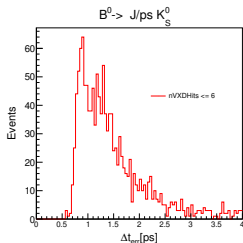
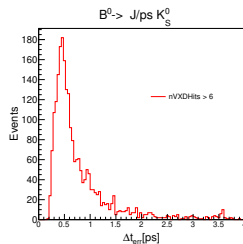
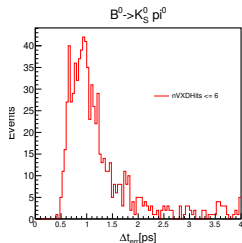
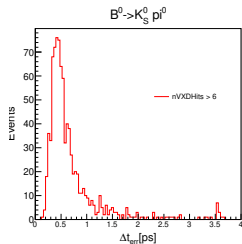


- Multiplicity=1.009
- π^0 multiplicity is severe than that of K_S^0 .
 - First selection based fit π^0 chiProb (p-value) ($\epsilon = 73\%$)
 - If the candidate has the same chiProb (p-value) on π^0 , then we do the K_S^0 chiProb (p-value) check ($\epsilon = 99\%$)

$$\epsilon_{\text{bcs}} = \frac{\text{No. of truth mathed events after BCS}}{\text{No. of truth matched events with multiplicity} > 1} = 74\% \quad (2)$$

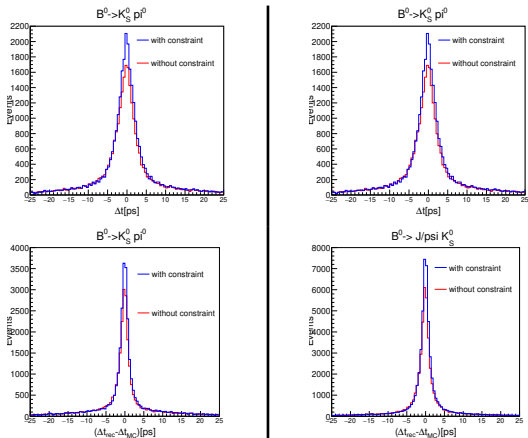
- Self-crossfeed fraction=1.5 %.
- Self-crossfeed component is taken into the signal PDF.

Δt_{err} double peak



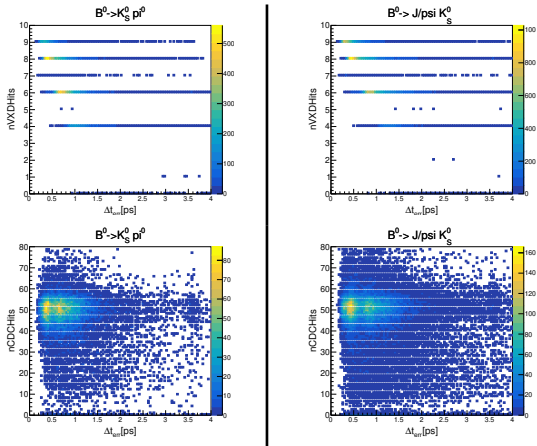
- We observe the second peak due to fewer hits in VXD.

Effect of IP constraint



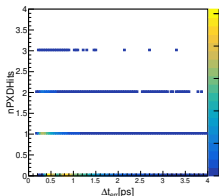
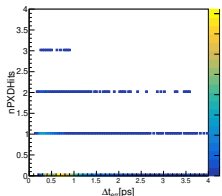
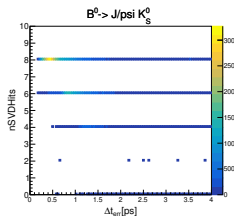
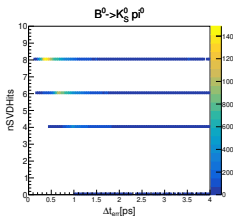
- After applying IP constraint in tag side Δt resolution improves.
- Similar trend is seen in the control channel .

Δt_{err} vs. Hits



- We plots number of hits in VXD and CDC to find out the double peak structure in the Δt_{err} distribution.

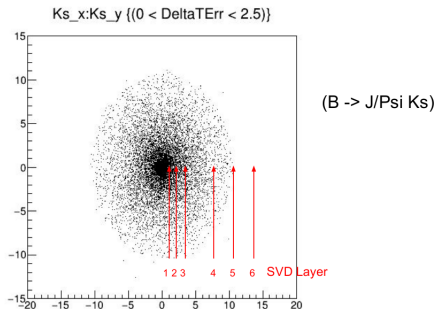
Δt_{err} vs. Hits



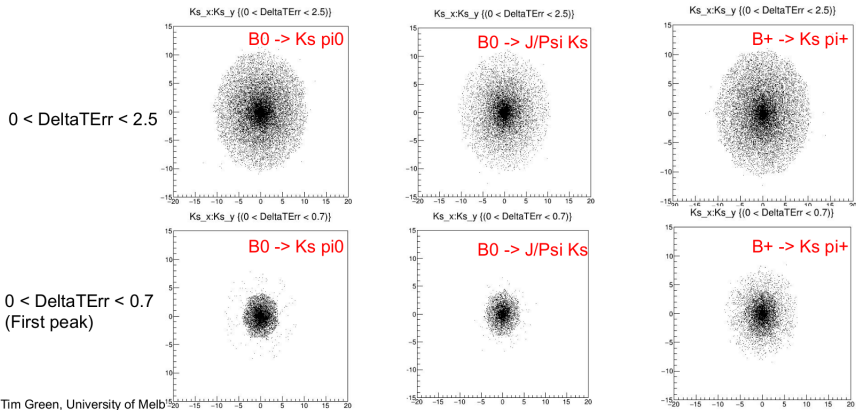
- We plot number of hits in VXD and CDC to find out the double peak structure in the Δt_{err} distribution.

DeltaTErr and Ks Vertex Position

- Location of Ks vertex on x-y plane
- Cut of 2.5 on DeltaTErr corresponds to the 5th layer of the SVD
- This means the cut requires two hits in the SVD



DeltaTErr and Ks Vertex Position



Signal mode

\mathcal{B} calculation

The \mathcal{B} is calculated as

$$\mathcal{B} = \frac{N_{sig}}{\epsilon \cdot f^{00} \cdot 2 \cdot \mathcal{B}_s \cdot N_{B\bar{B}}} \quad (3)$$

- $\mathcal{B}_s = 0.5$, probability of $K^0 \rightarrow K_S^0/K_L^0$
- $\mathcal{B}(B^0 \rightarrow K^0\pi^0) = 9.93 \times 10^{-6}$ (PDG value 2020)
- Signal efficiency=12.3 % (all selection + loose cont. supp. cut + $\sigma_{\Delta t}$)

Signal Modeling

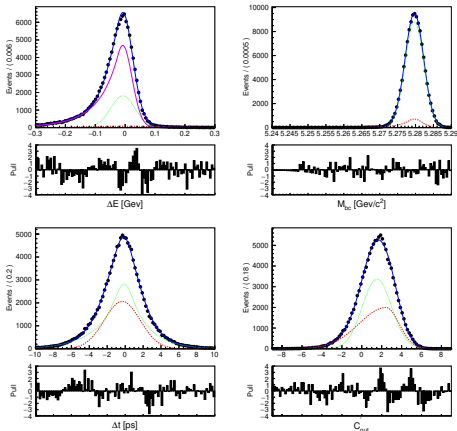
- Δt : RooBCPGenDecay PDF PDF convolved with double Gaussian:

$$P_{sig}(\Delta t, q) = \frac{\exp^{-|\Delta t|/\tau_{B^0}}}{4\tau_{B^0}} ([1 - q\Delta w + q\mu_i(1 - 2w)] + [q(1 - 2w) + \mu_i(1 - q\Delta w)](A_{CP} \cos(\Delta m_d \Delta t) - S_{CP} \cos(\Delta m_d \Delta t)))$$

Core and tail Gaussian, $\tau_{B^0} = 1.520$ ps and $\Delta m_d = 0.507/\text{ps}$

- ΔE : Crystal Ball + double Gaussian with common mean
- M_{bc} : Crystal Ball + Gaussian, C'_{out} : Bifurcated + Gaussian

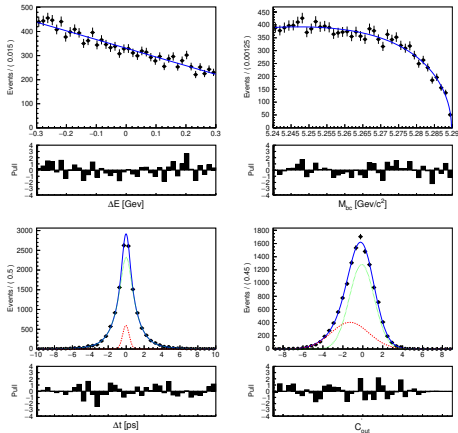
Example plot of integrated $q \cdot r$ bin



- In same way performed $7 q \cdot r$ bin fit to extract the PDFs parameters

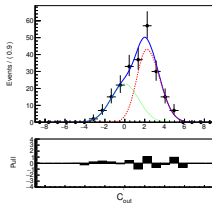
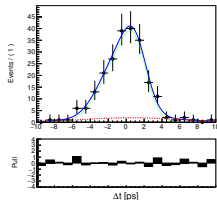
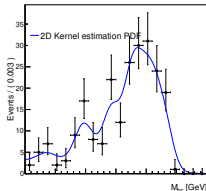
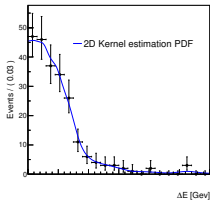
Continuum bkg modeling

- Δt : RooDecay PDF convolved with double Gaussian : $e^{-|t|/\tau}$
Core and tail Gaussian
- ΔE : Linear function
- M_{bc} : ARGUS function, C'_{out} : Bifurcated + Gaussian



$B\bar{B}$ bkg Modeling

- Δt : RooDecay PDF convolved with double Gaussian : $e^{-|t|/\tau}$
Core and tail Gaussian
- 2D Kernel estimation PDF used for $\Delta E - M_{bc}$ modeling
- C'_{out} : Bifurcated + Gaussian



$M_{bc} - \Delta E$ distribution between bad and good tag

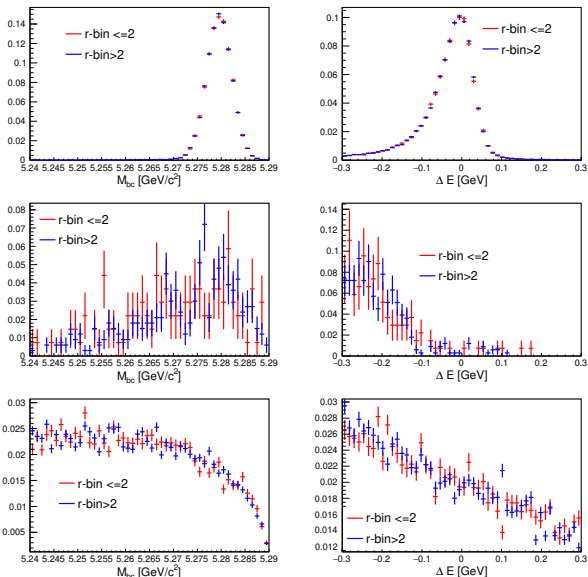


Figure: Signal (top), $B\bar{B}$ (middle) and $q\bar{q}$ (bottom)

$B\bar{B}$ normalisation sideband study

- Sideband region ($-0.3 < \Delta E < -0.2$)
- Optimised $CS > 0.9$ to reduce the continuum contribution.

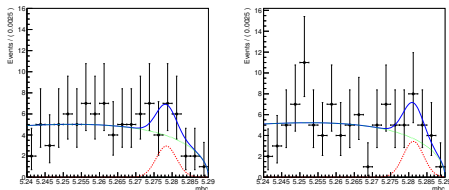


Figure: Sideband M_{bc} fit results in MC (left) and data (right) events.

Parameter	MC	Data
N_{peak}	8 ± 5	10 ± 5
N_{comb}	87 ± 10	90 ± 10

- We have confirmed this hypothesis in the case of MC events.
- Therefore, the uncertainty in the $B\bar{B}$ background yield is 5.

Control mode

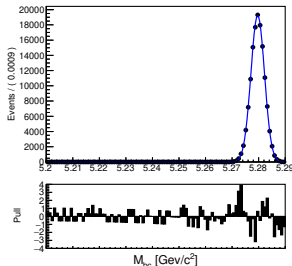
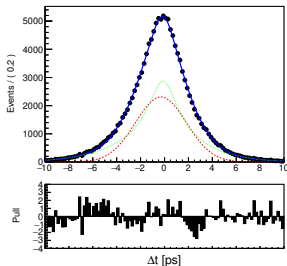
Signal Modeling

- Δt : RooBCPGenDecay PDF convolved with double Gaussian:

$$P_{sig}(\Delta t, q) = \frac{\exp(-|\Delta t|/\tau_{B^0})}{4\tau_{B^0}} ([1 - q\Delta w + q\mu_i(1 - 2w)] + [q(1 - 2w) + \mu_i(1 - q\Delta w)](A_{CP} \cos(\Delta m_d \Delta t) - S_{CP} \cos(\Delta m_d \Delta t)))$$

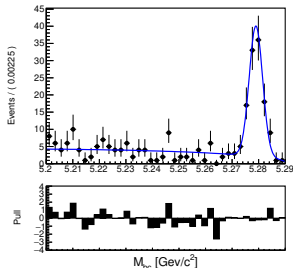
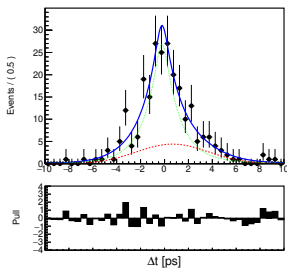
Core and tail Gaussian

- M_{bc} : Crystal Ball function



$B\bar{B}$ modeling

- Peaking component peaking at the true B mass (2 – 3% of signal events)
- Δt : RooDecay PDF convolved with double Gaussian : $e^{-|t|/\tau}$
Core and tail Gaussian
- M_{bc} : ARGUS + Gaussian function



$q\bar{q}$ modeling

- Δt : RooDecay PDF convolved with double Gaussian : $e^{-|t|/\tau}$
Core and tail Gaussian
- M_{bc} : ARGUS function

