

OCTANT SENSITIVITY RESTORED

In presence of a light sterile neutrino due to resonant matter effect

arXiv:2212.02949[hep-ph]

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OVERVIEW

1. Motivation
2. Analytical Study of Probabilities in 3+1 Framework
3. Octant Degeneracy in 3+1 Framework
4. Octant Sensitivity in Context of DUNE
5. Outlook

MOTIVATION

STANDARD NEUTRINO OSCILLATION FRAMEWORK

$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle$, $i\partial\nu_\alpha/\partial t = H|\nu_f\rangle$, $H = \frac{1}{2E} U M U^\dagger$, $H_m = H + H_{int}$, $\Delta_{ij} = m_i^2 - m_j^2$
 $A = 2\sqrt{2}G_F N_e E$ (CC interaction potential), G_F : Fermi Constant, N_e : e^- density

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \begin{bmatrix} c_{13} & 0 & s_{13} e^{-i\delta_{cp}} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta_{cp}} & 0 & c_{13} \end{bmatrix} \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}, M = \begin{bmatrix} m_1^2 & 0 & 0 \\ 0 & m_2^2 & 0 \\ 0 & 0 & m_3^2 \end{bmatrix}, H_{int} = \begin{bmatrix} \frac{A}{2E} & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{i>j}^N \text{Re}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin^2 \frac{1.27\Delta_{ij}L}{E} + 2 \sum_{i>j}^N \text{Im}(U_{\alpha i}^* U_{\beta i} U_{\alpha j} U_{\beta j}^*) \sin \frac{2 * 1.27\Delta_{ij}L}{E}$$

Two flavour oscillation

$$P_{e\mu} = \sin^2 2\theta \sin^2 \frac{1.27\Delta_{21}L}{E}, P_{e\mu}^m = \sin^2 2\theta_m \sin^2 \frac{1.27\Delta_{21m}L}{E}, \tan 2\theta_m = \frac{\Delta_{21} \sin 2\theta}{\Delta_{21} \cos 2\theta - A}$$

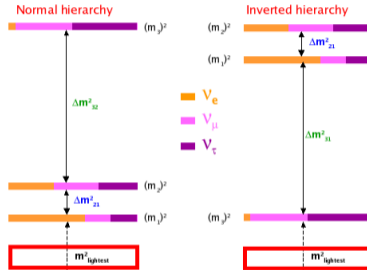
$$\theta_m = \pi/4: E_{res} = \frac{\Delta_{21} \cos 2\theta}{2V_{cc}}: \text{MSW Resonance energy (Mikheyev et al., Sov.J.Nucl.Phys. 42, 1985)}$$

CURRENT SCENARIO OF NEUTRINO OSCILLATION

$$\theta_{12} = 33.44^\circ, \theta_{13} = 8.57^\circ, \theta_{23} = 49.20^\circ, \Delta_{21} = 7.42e^{-5} eV^2, |\Delta_{31}| = 2.52e^{-3} eV^2 \text{ (JHEP,2020,178)}$$

Octant of θ_{23}

- $\theta_{23} : 39.6^\circ \rightarrow 51.8^\circ (3\sigma)$
- $\theta_{23} < 45^\circ$: Lower Octant (LO)
- $\theta_{23} > 45^\circ$: Higher Octant (HO)



Mass Hierarchy(antares.in2p3.fr)

CP Sensitivity

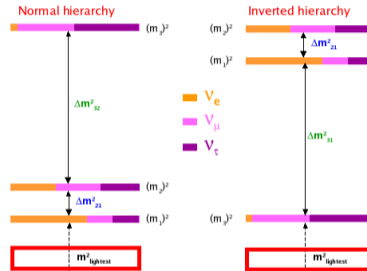
- $\delta_{CP} = 0, \pi$: CP Conservation;
- $\frac{\pi}{2}, \frac{3\pi}{2}$: CP Violation

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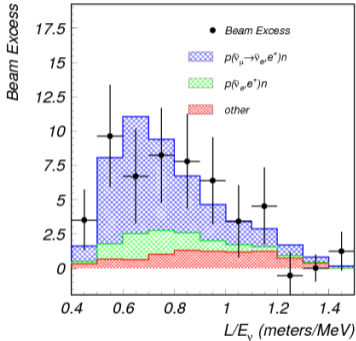
CP Sensitivity

- $\delta_{CP} = 0, \pi$: CP Conservation;
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Degeneracies in 3 flavor oscillation paradigm

- **octant- δ_{CP} degeneracy(fixed hierarchy):** $P_{\mu e}(HO, \delta_{CP}) = P_{\mu e}(LO, \delta'_{CP})$
- hierarchy- δ_{CP} degeneracy(fixed octant): $P_{\mu e}(NH, \delta_{CP}) = P_{\mu e}(IH, \delta'_{CP})$.
- Combined hierarchy- $\theta_{23} - \delta_{CP}$ degeneracy: $P_{\mu e}(NH, \theta_{23}, \delta_{CP}) = P_{\mu e}(IH, \theta'_{23}, \delta'_{CP})$.

STERILE NEUTRINO



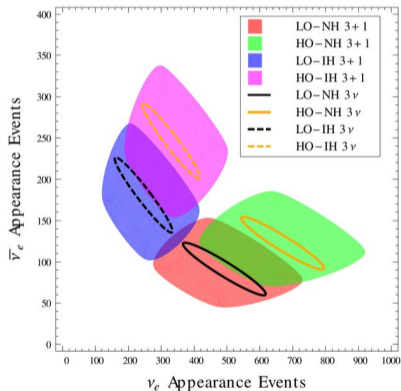
Beam excess at LSND

- LSND observed beam excess 3.8σ , hints $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ oscillation (Hill, PRL, 1995).
- Results of MiniBooNE has confirmed in 4.8σ (Aguilar-Arevalo et al, arXiv:2006.16883).
- Observation of ν_e deficit in SAGE and GALLEX (Phys.Rev.C83:065504,2011) has been reinforced with the recent results from BEST at 5σ (Barinov et al., 2021, arXiv:2109.11482).
- To solve these anomalies existence of an extra light sterile neutrino with mass $m_s \sim 1eV$ is proposed leading to 3+1 Oscillation framework,

$$U_s = \tilde{R}_{34}(\theta_{34}, \delta_{34}) R_{24}(\theta_{24}) \tilde{R}_{14}(\theta_{14}, \delta_{14}) R_{23}(\theta_{23}) \tilde{R}_{13}(\theta_{13}, \delta_{13}) R_{12}(\theta_{12})$$

$R_{ij}(\theta_{ij})$: Rotation matrices in i-j plane, $U_{ij}^\delta = \text{diag}(1, 1, 1, e^{i\delta_{ij}})$, δ_{ij} 's: CP phases.

STERILE NEUTRINO HINDERING THE OCTANT- δ_{CP} DEGENERACY?



Bi-event plot at DUNE

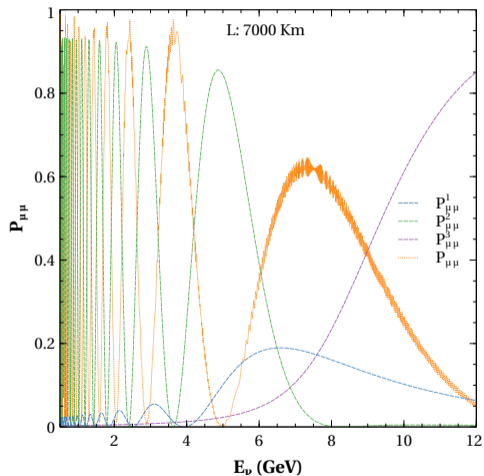
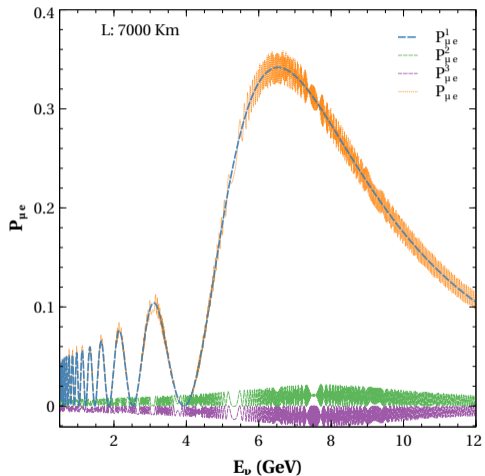
- Agarwalla et al, PRL, 2017 showed the presence of eV scale sterile neutrino jeopardize the octant discovery.
- Their results are for shorter baselines explained through vacuum oscillations.
- **We explore the octant sensitivity at beam+atmospheric baselines with ν_s where matter effect is important.**
- **We have derived the oscillation probabilities in 3+1 framework using: Two Mass Scale Dominance approximation.**

ANALYTICAL STUDY OF PROBABILITIES IN 3+1 FRAMEWORK

THE 3+1 OSCILLATION FRAMEWORK

- $\Delta_{21} \ll \Delta_{31} \ll \Delta_{41} \rightarrow \Delta_{21} = 0$: Two Mass Scale Dominance (TMSD) Approx.
- Vacuum Hamiltonian in mass basis: $H_M = \frac{1}{2E} \text{diag}(0, 0, \Delta_{31}, \Delta_{41})$
- Effective mixing matrix: $\tilde{U} = R_{24}(\theta_{24}) \tilde{R}_{14}(\theta_{14}, \delta_{14}) R_{23}(\theta_{23}) U_{\delta_{13}} R_{13}(\theta_{13})$
- Interaction Hamiltonian: $H_{int} = \text{diag}(V_{CC}, 0, 0, -V_{NC}) = \frac{1}{2E} \text{diag}(A, 0, 0, A/2)$
- Total Hamiltonian: $H = \frac{1}{2E} (U H_M U^\dagger + H_{int}) = (H_0 + H_p)$
- Eigenvalues of H_0 : $\frac{\Delta_{41}}{2E}, 0, 0, 0 \rightarrow$ **degenerate perturbation theory**

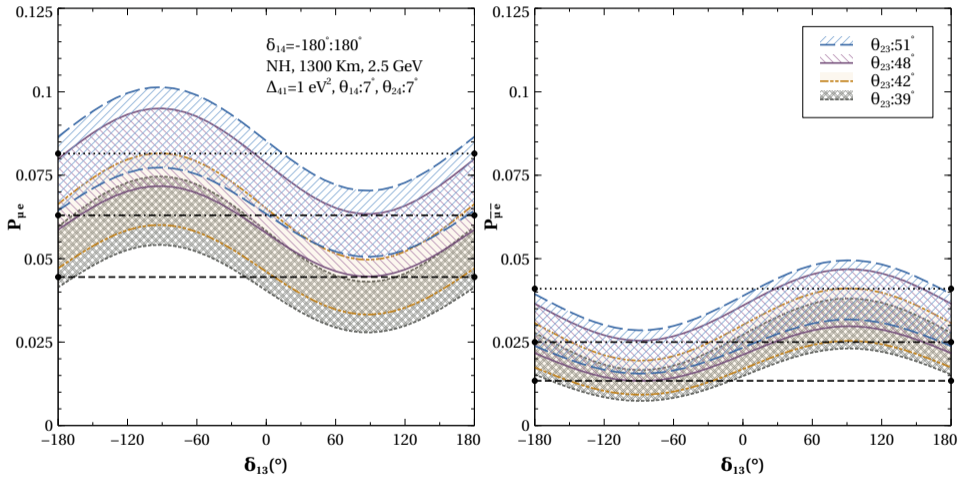
ANALYTIC PROBABILITIES



$$P_{\mu e}^1 \sim 4 \cos^2 \theta_{13m} \cos^2 \theta_{14m} \sin^2 \theta_{13m} \cos^2 \theta_{24m} \sin^2 \theta_{23} \sin^2 \frac{1.27 \Delta_{31}^m L}{E} \quad P_{\mu \mu}^1 \sim \cos^4 \theta_{24m} \sin^2 2\theta_{13m} \sin^4 \theta_{23} \sin^2 \frac{1.27 \Delta_{31}^m L}{E}$$

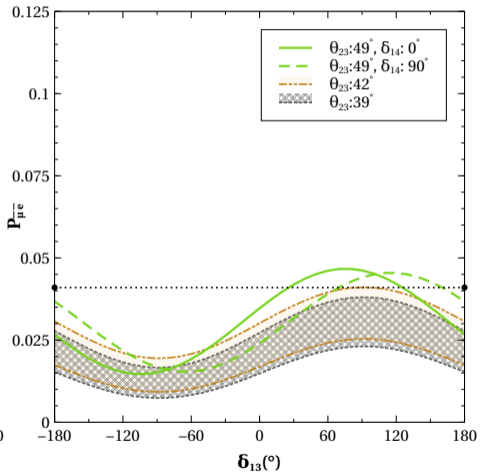
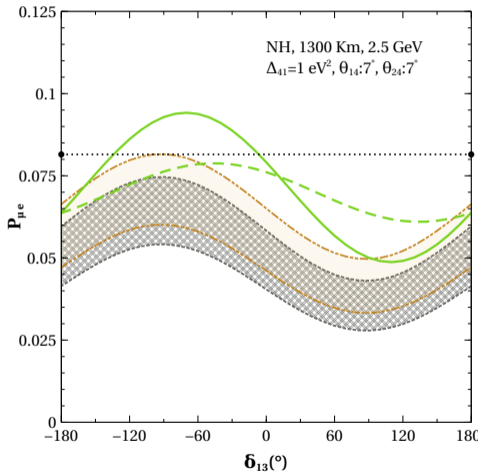
OCTANT DEGENERACY IN 3+1 FRAMEWORK

OCTANT DEGENERACY AT 1300 KM



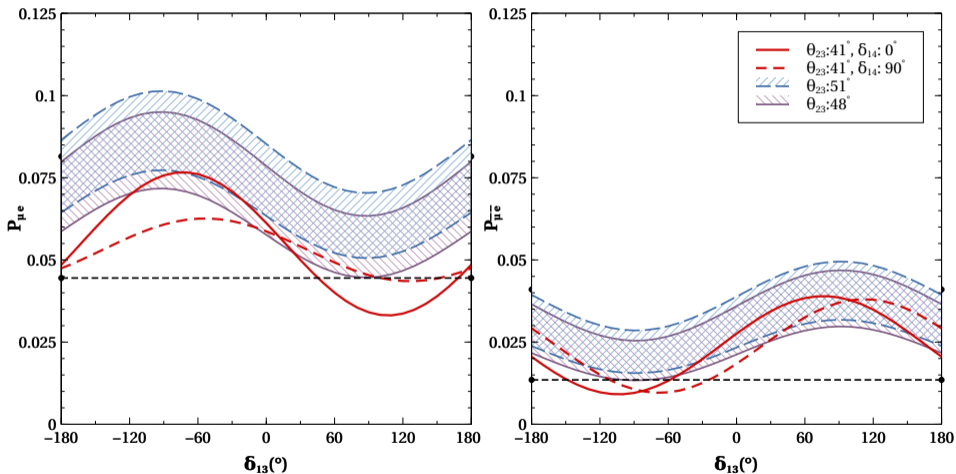
Degenerate solutions are observed for θ_{23} , δ_{14} variation in both octants.

OCTANT DEGENERACY AT 1300 KM



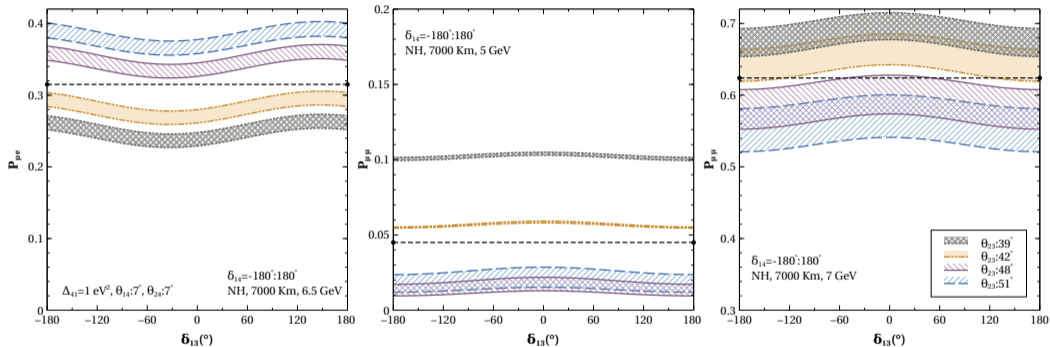
With θ_{23}, δ_{14} being fixed for one octant, the degeneracy gets lifted at certain δ_{13} values.

OCTANT DEGENERACY AT 1300 KM



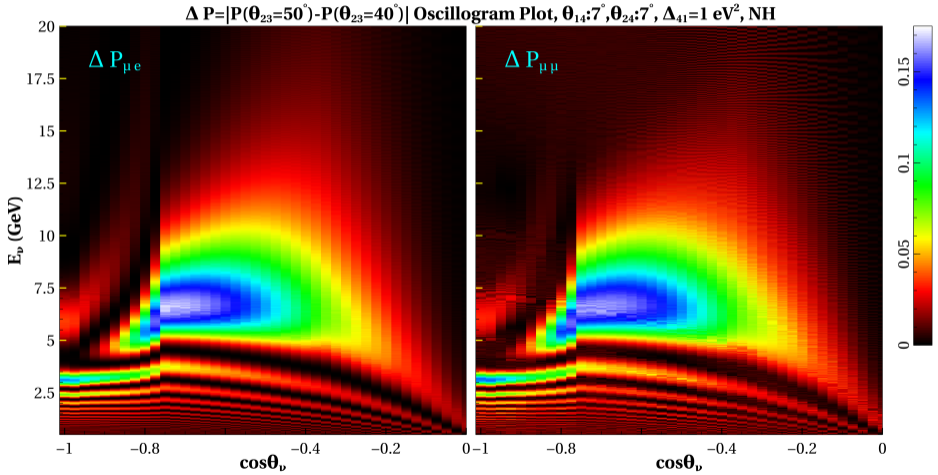
With θ_{23}, δ_{14} being fixed for one octant, the degeneracy gets lifted at certain δ_{13} values.

OCTANT DEGENERACY AT 7000 KM



- Clear removal of degeneracy at both $P_{\mu e}$, $P_{\mu\mu}$ channel.
- Higher baselines show promises of better octant sensitivity.

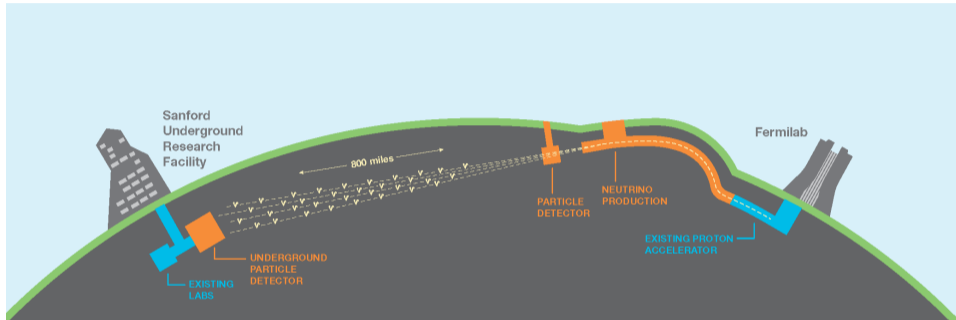
PROBABILITY OSCILLOGRAM SHOWING OCTANT DEGENERACY



Higher baselines of $(5 : 10) \times 10^3 \text{ km}$ show a significant difference in probabilities.

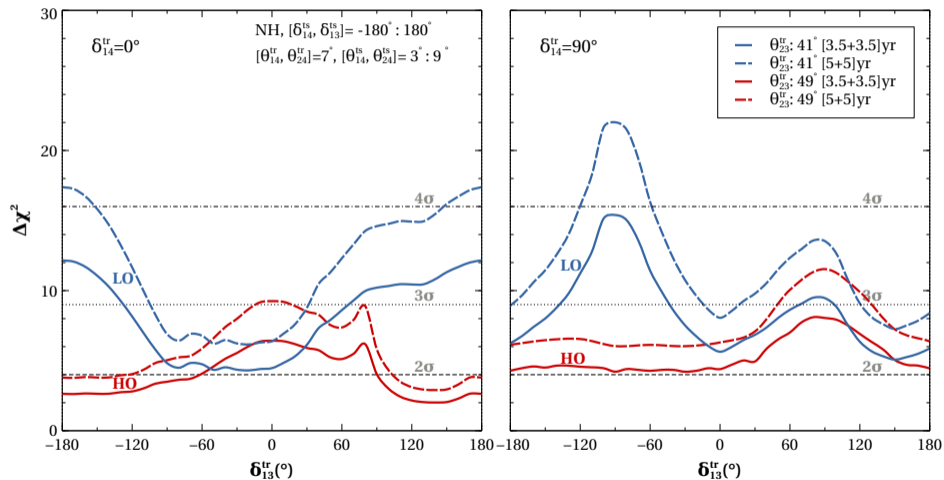
OCTANT SENSITIVITY IN CONTEXT OF DUNE

DEEP UNDERGROUND NEUTRINO EXPERIMENT (DUNE)



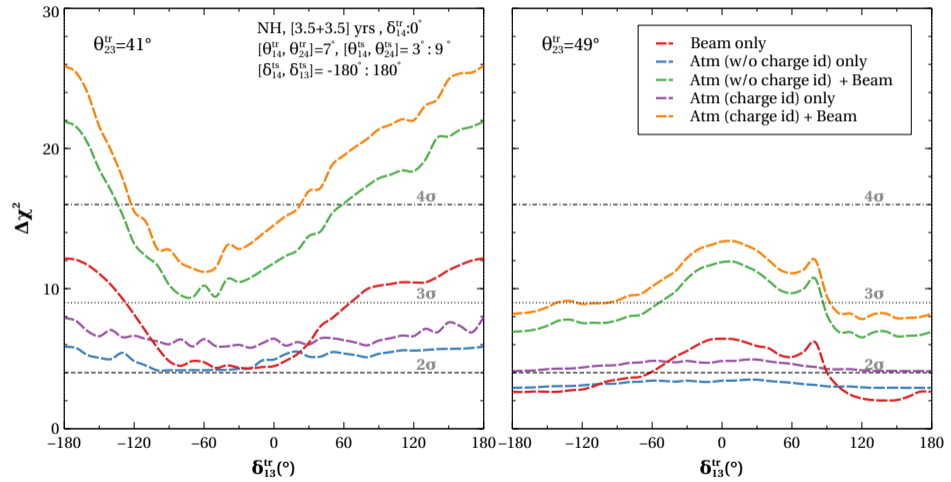
- Primary goals: testing CPV in lepton sector, finding mass hierarchy, θ_{23} octant.
- Long baseline experiment with the far detector at 1300 km with mean neutrino energy around 2 ~ 3 GeV using liquid argon time projection chamber of 40 kt.
- Anticipating data collection from 2026 for 7 years (3.5 years of $\nu/\bar{\nu}$ beam mode)
- Along with accelerator ν beam DUNE can study atmospheric neutrinos.

OCTANT SENSITIVITY FOR BEAM NEUTRINOS



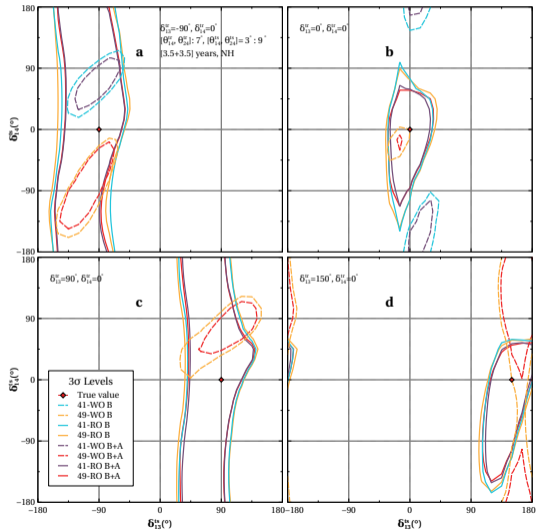
Sensitivity is over 2σ for most the δ_{13} values.

OCTANT SENSITIVITY FOR BEAM AND ATMOSPHERIC NEUTRINOS



The addition of atmospheric analysis lifts sensitivity over 3σ for most of the δ_{13} values.

CONTOUR PLOTS OF SENSITIVITY TO THE OCTANT



δ_{13}	δ_{14}	Present Degeneracies
-90°	0°	WO-R δ_{13} -W δ_{14}
0°	0°	WO-R δ_{13} -R δ_{14} (49°), WO-R δ_{13} -W δ_{14} (41°)
90°	0°	WO-R δ_{13} -W δ_{14} (49°)
150°	0°	WO-R δ_{13} -R δ_{14} (49°), WO-R δ_{13} -W δ_{14} (49°)

Table: The degeneracies for different true value of δ_{13} with true $\delta_{14} = 0^\circ$

- Inclusion of atmospheric analysis shrinks all the contours improving octant sensitivity.
- The precision of the RO true solutions along with the size and type of WO contours depend on $\delta_{13}^{\text{true}}$ for fixed $\delta_{14}^{\text{true}}$.

OUTLOOK

CONCLUSION

- Analytic probabilities using TMSD approximation shows good fit to the numerical probabilities especially in around the resonance energy.
- Combining the beam and the atmospheric neutrinos, we can obtain 3σ sensitivity in the entire true δ_{13} space for true values of $\theta_{23} = 41^\circ$, $\delta_{14} = 0^\circ$. In case of true values of $\theta_{23} = 49^\circ$, $\delta_{14} = 0^\circ$, 3σ sensitivity is achieved for 55% of the δ_{13}^{true} values.
- We also identify the extra degeneracies due to the presence of δ_{14} assuming the normal hierarchy at different true values of phases.



THANK YOU

ENERGIES FOR $\Delta_{21} = 0$ APPROXIMATION WITH ν_s

The modified energies in $\text{NH}(E_4^m > E_3^m > E_2^m > E_1^m)$ [$A' = A/2$]

$$\begin{aligned}
 E_1^m &: C[\Delta_{31} \sin^2(\theta_{13} - \theta_{13m}) + A'(1 + \cos^2 \theta_{14} + \cos^2 \theta_{14} \sin^2 \theta_{24}) \cos^2 \theta_{13m}]/2E \\
 E_2^m &: 0 \\
 E_3^m &: C[\Delta_{31} \cos^2(\theta_{13} - \theta_{13m}) + A'(1 + \cos^2 \theta_{14} + \cos^2 \theta_{14} \sin^2 \theta_{24}) \sin^2 \theta_{13m}]/2E \\
 E_4^m &: C[\Delta_{41} + A'(1 + \sin^2 \theta_{14} - \cos^2 \theta_{14} \sin^2 \theta_{24})]/2E
 \end{aligned} \tag{1}$$

$$\sin 2\theta_{13m} = \frac{\Delta_{31} s 2\theta_{13} + A \cos(\delta_{13} - \delta_{14}) s \theta_{14} s \theta_{23} s 2\theta_{24}}{f}$$

$$\sin \theta_{24m} = \sin \theta_{24} [1 - \frac{A}{\Delta_{41}} c^2 \theta_{14} c^2 \theta_{24}], \cos \theta_{24m} = \cos \theta_{24} [1 + \frac{A}{\Delta_{41}} c^2 \theta_{14} s^2 \theta_{24}],$$

$$\sin \theta_{14m} = \sin \theta_{14} [1 + \frac{A}{\Delta_{41}} c^2 \theta_{14} (1 + s^2 \theta_{24})], \cos \theta_{14m} = \cos \theta_{14} [1 - \frac{A}{\Delta_{41}} s^2 \theta_{14} (1 + s^2 \theta_{24})]$$

OSCILLATION/SURVIVAL PROBABILITIES IN PRESENCE OF STERILE NEUTRINO

$$P_{\mu e}^1 = 4 \cos^2 \theta_{13m} \cos^2 \theta_{14m} \sin^2 \theta_{13m} (\cos^2 \theta_{24m} \sin^2 \theta_{23} - \sin^2 \theta_{14m} \sin^2 \theta_{24m}) \sin^2 D_{31}^m \\ + 2 \cos^3 \theta_{13m} \cos^2 \theta_{14m} \sin \theta_{13m} \sin \theta_{14m} \sin 2\theta_{24m} \sin \theta_{23} \sin D_{31}^m \sin(D_{31}^m + \delta) \\ - 2 \cos \theta_{13m} \cos^2 \theta_{14m} \sin^3 \theta_{13m} \sin \theta_{14m} \sin 2\theta_{24m} \sin \theta_{23} \sin D_{31}^m \sin(D_{31}^m - \delta),$$

$$P_{\mu e}^2 = \cos^2 \theta_{14m} \sin 2\theta_{13m} \sin \theta_{14m} \sin \theta_{23} \sin 2\theta_{24m} \sin D_{41}^m \sin(D_{41}^m - \delta) + \sin^2 2\theta_{14m} \sin^2 \theta_{24m} \cos^2 \theta_{13m} \sin^2 D_{41}^m,$$

$$P_{\mu e}^3 = -\cos^2 \theta_{14m} \sin 2\theta_{13m} \sin \theta_{14m} \sin \theta_{23} \sin 2\theta_{24m} \sin D_{43}^m \sin(D_{43}^m - \delta) + \sin^2 2\theta_{14m} \sin^2 \theta_{24m} \sin^2 \theta_{13m} \sin^2 D_{43}^m$$

$$P_{\mu e}^{4\nu} = P_{\mu e}^1 + P_{\mu e}^2 + P_{\mu e}^3, \quad P_{\mu e}^{3\nu} = \sin^2 2\theta_{13m} \sin^2 \theta_{23} \sin^2 D_{31}^m$$

$$P_{\mu\mu}^1 = \cos^4 \theta_{24m} \sin^2 2\theta_{13m} \sin^4 \theta_{23} \sin^2 D_{31}^m + \sin^4 \theta_{24m} \sin^4 \theta_{14m} \sin^2 2\theta_{13m} \sin^2 D_{31}^m \\ + \sin 2\theta_{24m} \sin \theta_{14m} \sin 4\theta_{13m} \sin \theta_{23} \cos \delta (\cos^2 \theta_{24m} \sin^2 \theta_{23} - \sin^2 \theta_{24m} \sin^2 \theta_{13m}) \sin^2 D_{31}^m \\ + 4 \cos^2 \theta_{24m} \sin^2 \theta_{24m} \sin^2 \theta_{14m} \sin^2 \theta_{23} (1 - \frac{\sin^2 2\theta_{13m}}{2} - \sin^2 2\theta_{13m} \cos^2 \delta) \sin^2 D_{31}^m,$$

$$P_{\mu\mu}^2 = \cos^4 \theta_{24m} \cos^2 \theta_{13m} \sin^2 2\theta_{23} \sin^2 D_{32}^m + 4 \cos^2 \theta_{24m} \sin^2 \theta_{24m} \sin^2 \theta_{14m} \sin^2 \theta_{13m} \cos^2 \theta_{23} \sin^2 D_{32}^m \\ - 4 \cos^3 \theta_{24m} \sin \theta_{24m} \sin \theta_{14m} \sin 2\theta_{13m} \cos^2 \theta_{23} \sin \theta_{23} \cos \delta \sin^2 D_{32}^m,$$

$$P_{\mu\mu}^3 = \cos^4 \theta_{24m} \sin^2 \theta_{13m} \sin^2 2\theta_{23} \sin^2 D_{21}^m + 4 \cos^2 \theta_{24m} \sin^2 \theta_{24m} \sin^2 \theta_{14m} \cos^2 \theta_{13m} \cos^2 \theta_{23} \sin^2 D_{21}^m \\ + 4 \cos^3 \theta_{24m} \sin \theta_{24m} \sin \theta_{14m} \sin 2\theta_{13m} \cos^2 \theta_{23} \sin \theta_{23} \cos \delta \sin^2 D_{21}^m$$

$$P_{\mu\mu}^{4\nu} = 1 - P_{\mu\mu}^1 + P_{\mu\mu}^2 + P_{\mu\mu}^3, \quad P_{\mu\mu}^{3\nu} = 1 - \sin^2 2\theta_{13m} \sin^4 \theta_{23} \sin^2 D_{31}^m - \sin^2 2\theta_{23} (\cos^2 \theta_{13m} \sin^2 D_{32}^m + \sin^2 \theta_{13m} \sin^2 D_{21}^m)$$

$$D_{ij}^m = \frac{1.27 \Delta_{ij}^m L}{E}, \quad \Delta_{ij}^m: \text{modified mass-squared difference, } \delta = \delta_{13} - \delta_{14}: \text{effective phase, } \theta_{ijm}: \text{modified angles in matter}$$

ANALYTICAL OVERVIEW OF OCTANT- δ_{CP} DEGENERACY

- $\theta_{23} = \frac{\pi}{4} \pm \eta, \eta \sim 0.1 \xrightarrow{\text{lim}} \sin^2 \theta_{23} \simeq \frac{1}{2} \pm \eta, \sin \theta_{23} \simeq \frac{1}{\sqrt{2}}(1 \pm \eta)$
- $\Delta P \equiv P_{\mu e}^{HO}(\delta_{13}^{HO}, \delta_{14}^{HO}) - P_{\mu e}^{LO}(\delta_{13}^{LO}, \delta_{14}^{LO}) = \Delta P_0 + \Delta P_1 + \Delta P_2 + \Delta P_{fast}$
- $\Delta P < 0$ suggests degeneracy is absent

$$\Delta P_0 = 8\eta \cos^2 \theta_{13m} \cos^2 \theta_{14m} \cos^2 \theta_{24m} \sin^2 \theta_{13m} \sin^2 D_{31}^m$$

$$\Delta P_1 = X_1(1 + \eta) \sin(D_{31}^m + \delta^{HO}) - X_1(1 - \eta) \sin(D_{31}^m + \delta^{LO})$$

$$\Delta P_2 = -Y_1(1 + \eta) \sin(D_{31}^m - \delta^{HO}) + Y_1(1 - \eta) \sin(D_{31}^m - \delta^{LO})$$

$$\Delta P_f = \sum_{k=1,3} Z_k(1 + \eta) \sin(D_{4k}^m - \delta^{HO}) - Z_k(1 - \eta) \sin(D_{4k}^m - \delta^{LO})$$

$$X_1 = \sqrt{2} \cos^3 \theta_{13m} \cos^2 \theta_{14m} \sin \theta_{13m} \sin \theta_{14m} \sin 2\theta_{24m} \sin D_{31}^m$$

$$Y_1 = \sqrt{2} \cos \theta_{13m} \cos^2 \theta_{14m} \sin^3 \theta_{13m} \sin \theta_{14m} \sin 2\theta_{24m} \sin D_{31}^m$$

$$Z_1 = \cos^2 \theta_{14m} \sin 2\theta_{13m} \sin \theta_{14m} \sin 2\theta_{24m} \sin D_{41}^m / \sqrt{2},$$

$$Z_3 = -\cos^2 \theta_{14m} \sin 2\theta_{13m} \sin \theta_{14m} \sin 2\theta_{24m} \sin D_{43}^m / \sqrt{2}$$

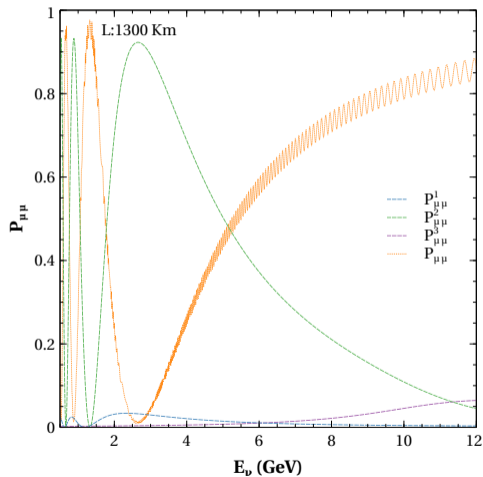
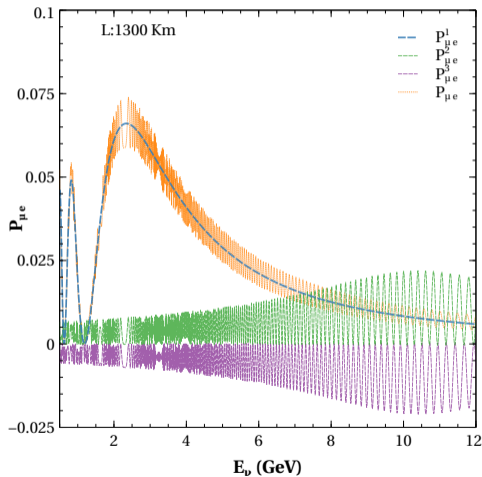
810 Km: $\Delta P_0 = 0.022, X_1 = 0.013, Y_1 = 0.0004, Z_1 = 0.0001, Z_3 = -0.0164$: ΔP will be zero for some phases

7000 Km:

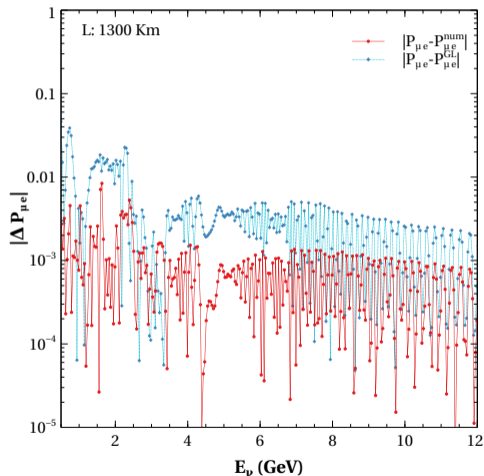
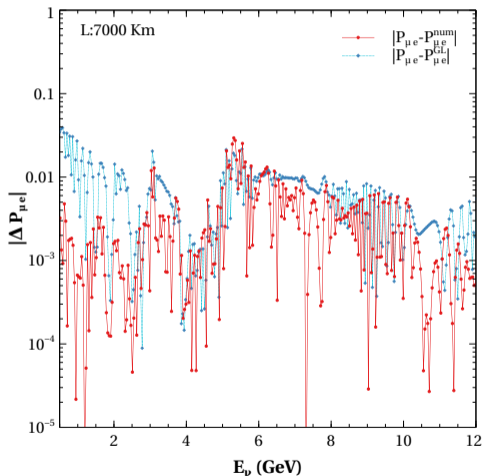
$\Delta P_0 = 0.136, X_1 = 0.026, Y_1 = 0.007, Z_1 = -0.0056, Z_3 = 0.0064 \equiv \Delta P < 0$:

degeneracy removed

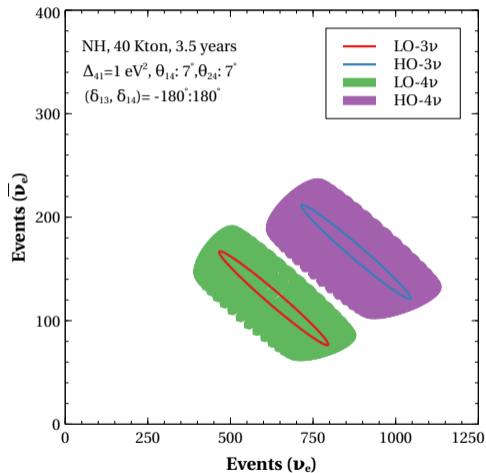
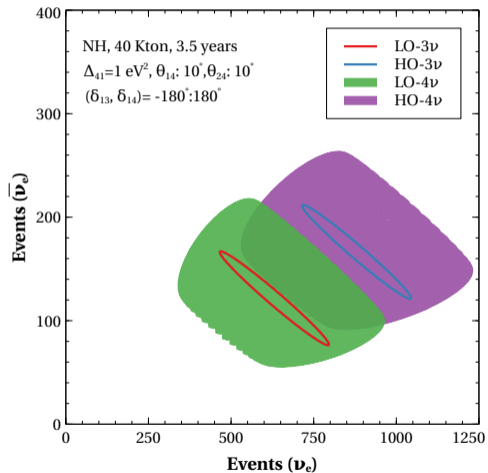
ANALYTIC PROBABILITIES AT 1300 KM



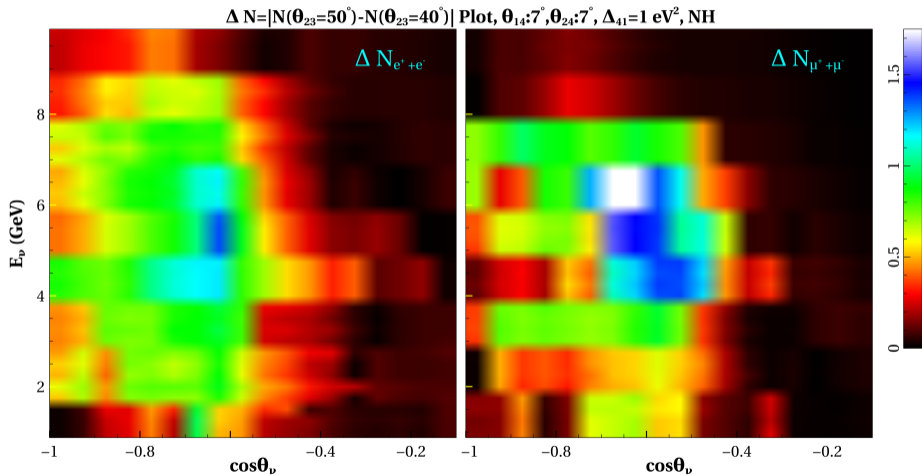
COMPARISONS OF ANALYTIC PROBABILITIES WITH NUMERICAL ONES



BI-EVENTS PLOT AT 1300 KM



EVENTS AT HIGHER BASELINES



OCTANT DEGENERACY IN $P_{\mu\mu}$ CHANNEL AT 1300 KM