

# Fingerprints of MeV scale secluded dark matter at CMB

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- PLANCK SATELLITE measures the number of effective relativistic degrees ( $N_{\text{eff}}$ ) of freedom at CMB.

$$N_{\text{eff}}^{\text{CMB}} = 2.99_{-0.33}^{+0.34} \quad \text{at 95\% CL}$$

[arXiv: 1807.06209]

This constitutes a fundamental probe of thermal history of early Universe.

**Q : How do you define  $N_{\text{eff}}$ ?**

$$\Rightarrow N_{\text{eff}} = 3 \times \left( \frac{11}{4} \right)^{4/3} \left( \frac{T_{\nu}^{\text{CMB}}}{T_{\gamma}^{\text{CMB}}} \right)^4$$

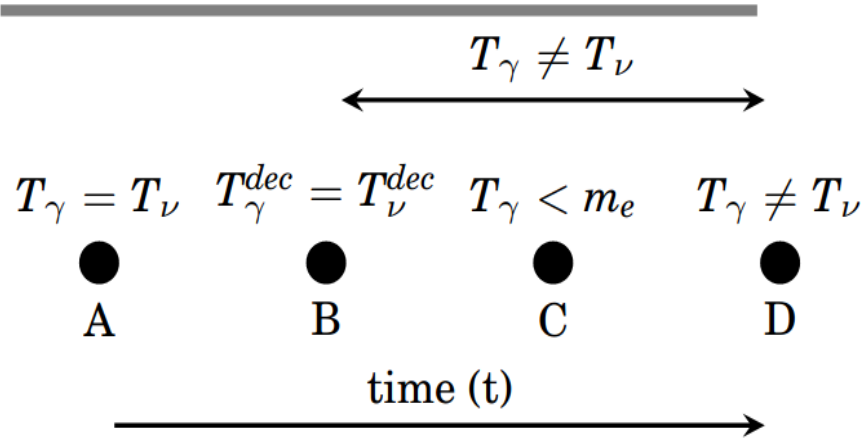
- Consider the change in effective number of degrees of freedom in entropy of the photon bath

$$g_{*s_\gamma} = \begin{cases} 2 + \frac{7}{8} \times 4 = \frac{11}{2}, & T \gtrsim m_e \\ 2 & T \lesssim m_e \end{cases}$$

The effective number of degrees of freedom in the neutrino bath entropy density remains same

$$g_{*s_\nu} = 3 \times 2 \times \frac{7}{8}$$

## Time Scale



- Apply conservation of comoving entropy density

$$s_\gamma(T_d) a(T_d)^3 = s_\gamma(T_\gamma^{\text{CMB}}) a(T_\gamma^{\text{CMB}})^3$$

$$s_\nu(T_d) a(T_d)^3 = s_\nu(T_\nu^{\text{CMB}}) a(T_\nu^{\text{CMB}})^3$$

Using  $s_\gamma = \frac{2\pi^2}{45} g_{*s_\gamma} T_\gamma^3$  and  $s_\nu = \frac{2\pi^2}{45} g_{*s_\nu} T_\nu^3$

We obtain,

$$\frac{T_\nu^{\text{CMB}}}{T_\gamma^{\text{CMB}}} = \left( \frac{4}{11} \right)^{1/3}$$

Hence in SM of particle physics

$$N_{\text{eff}} = 3$$

**Instantaneous decoupling approximation !!**

- If the neutrinos decoupling is instantaneous, we find  $N_{\text{eff}} = 3$ . But in practice this is not the case.

To obtain a clear prediction of  $N_{\text{eff}}$  in SM, one should correctly track the temperature evolutions for both neutrino bath and photon bath

$$\frac{dT_\nu}{dt} = \frac{C_{\text{inel.}}(T_\gamma, T_\nu) + C_{\text{el}}(T_\gamma, T_\nu) - 4H\rho_\nu}{\frac{\partial\rho_\nu}{\partial T_\nu}},$$

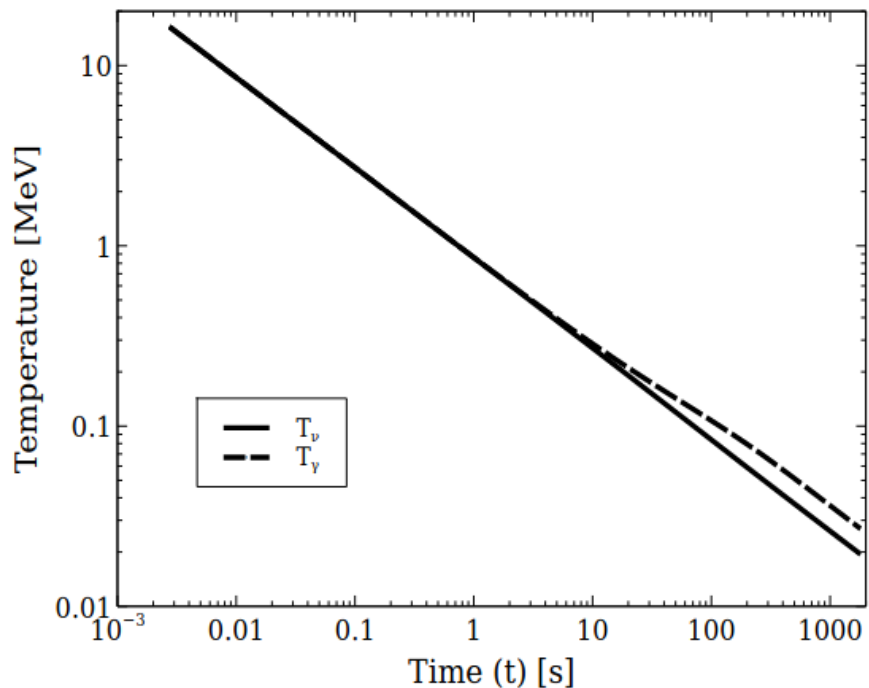
$$\frac{dT_\gamma}{dt} = \frac{-C_{\text{inel.}}(T_\gamma, T_\nu) - C_{\text{el}}(T_\gamma, T_\nu) - 3H(\rho_e + \rho_\gamma) - 3H(p_e + p_\gamma)}{\frac{\partial\rho_\gamma}{\partial T_\gamma} + \frac{\partial\rho_e}{\partial T_\gamma}}.$$

The relevant processes are

$$e^+e^- \leftrightarrow \bar{\nu}_i\nu_i, \quad e^\pm\nu_i \leftrightarrow e^\pm\nu_i, \quad e^\pm\bar{\nu}_i \leftrightarrow e^\pm\bar{\nu}_i,$$

$$\nu_i\nu_j \leftrightarrow \nu_i\nu_j, \quad \nu_i\bar{\nu}_j \leftrightarrow \nu_i\bar{\nu}_j, \quad \text{and} \quad \bar{\nu}_i\nu_i \leftrightarrow \bar{\nu}_j\nu_j$$

## N<sub>eff</sub> in SM of particle physics



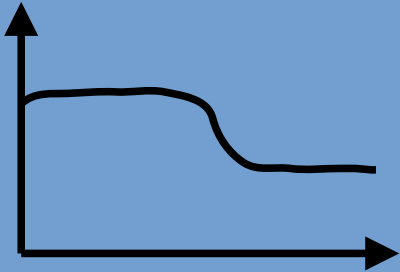
Neutrino Decoupling in the SM	$T_\gamma/T_\nu$	$N_{\text{eff}}$
Instantaneous decoupling	1.4010	3
Instantaneous decoupling + QED	1.3998	3.011
MB collision term	1.3961	3.042
MB collision term + QED	1.3949	3.053

The most precise evaluation predicts  $N_{\text{eff,SM}}^{\text{CMB}} = 3.045$ .

$N_{\text{eff}}$  in BSM: role of dark matter

Dark Matter  
Production

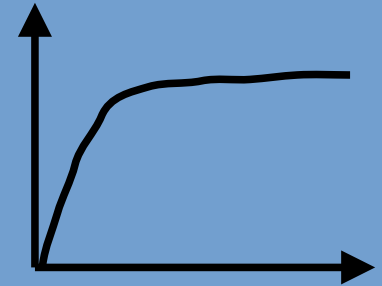
Thermal dark  
matter



Nucl.Phys.B 360 (1991) 145-179

Secluded dark  
matter

Non-thermal dark  
matter



JHEP 03 (2010) 080

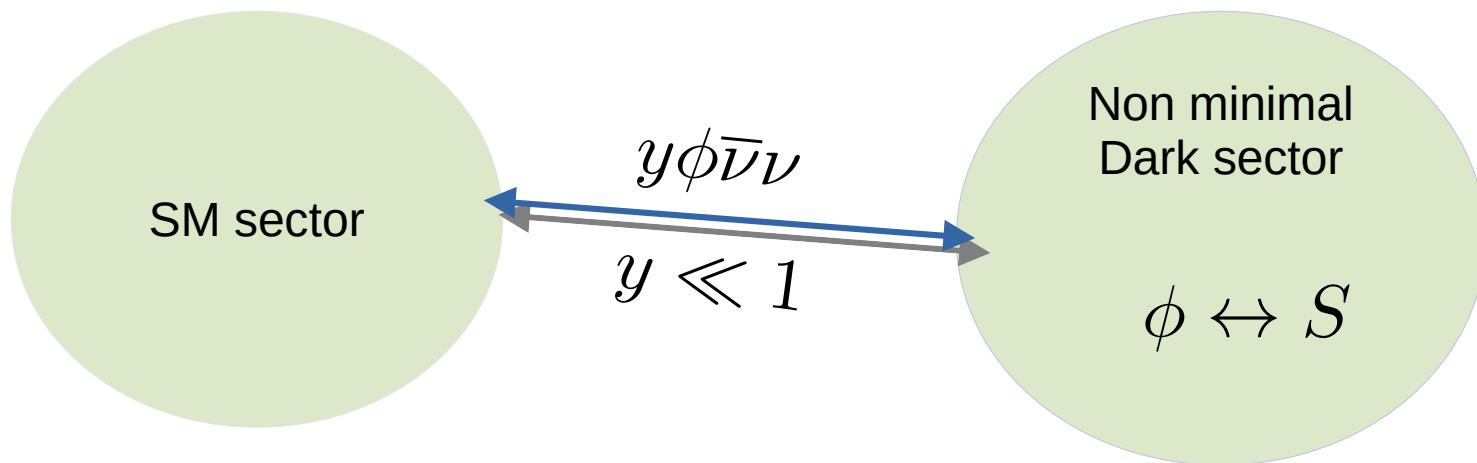
Dark Matter			
Particle	g-Spin	Planck+BAO	
		> 2.66	< 3.33
Majorana DM- $\nu$	2-F	-	8.5
Dirac DM- $\nu$	4-F	-	11.2
$\phi$ DM- $\nu$	1-B	-	5.7
$\phi^*$ DM- $\nu$	2-B	-	8.5
$Z'$ DM- $\nu$	3-B	-	10.1
Majorana DM- $e$	2-F	6.4	-
Dirac DM- $e$	4-F	9.2	-
$\phi$ DM- $e$	1-B	3.5	-
$\phi^*$ DM- $e$	2-B	6.5	-
$Z'$ DM- $e$	3-B	8.1	-

[arXiv: 1812.05605]

Lower bounds on the masses of various thermal dark matter particles (in MeV) at 95% CL.



Neutrino decoupling and  $N_{\text{eff}}$  in BSM: role of non-thermal secluded dark matter

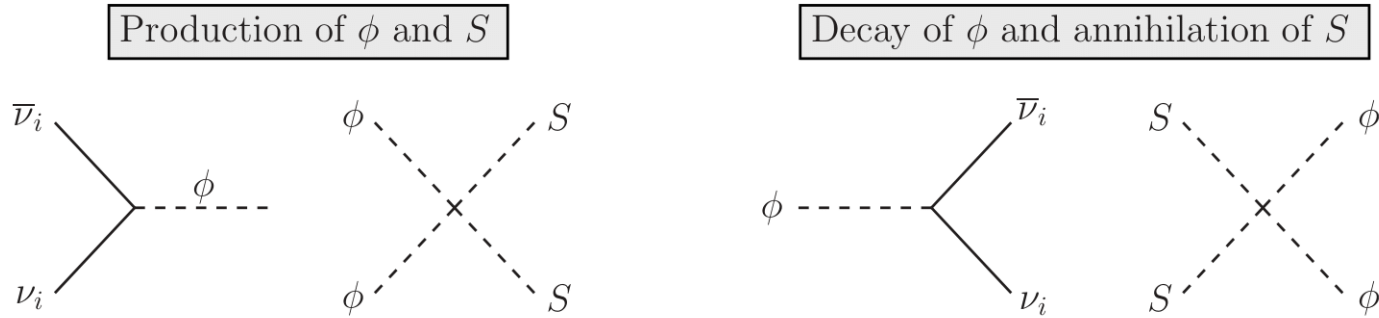


$$-\mathcal{L} \supset \frac{1}{2}m_S^2 S^2 + \frac{1}{2}m_\phi^2 \phi^2 + \frac{\lambda}{4}S^2\phi^2 + \frac{\kappa}{2}\phi\bar{\nu}_i\nu_i$$

Motivation:

(i) Imprint of such an MeV scale hidden dark sector on  $N_{\text{eff}}$  at CMB

(ii) Contribution of dark matter  $S$  on  $N_{\text{eff}}$



Model free parameters:  $\{m_S, m_\phi, \lambda, y\}$  where  $y^2 = \sum_{i=1}^3 \kappa^2$

- The DS remains secluded, this imposes constraint on  $y$ .

This can be quantified by

$$\sum_{i=1}^3 n_{\nu_i}^{\text{eq}} \langle \sigma v \rangle_{\bar{\nu}_i \nu_i \rightarrow \phi} < H$$

- We are interested in a situation where the dark sector is in internal thermal equilibrium and it has its own temperature

$$n_S^{\text{eq}} \langle \sigma v \rangle_{SS \rightarrow \phi\phi} > H$$

Hubble parameter :

$$H = \sqrt{\frac{8\pi}{3M_{PL}^2} (\rho_\gamma + \rho_\nu + \rho_S + \rho_\phi)}$$

New physics contribution to  $T_\nu$

$$\frac{dT_\nu}{dt} = \frac{C_{inel.}(T_\gamma, T_\nu) + C_{el}(T_\gamma, T_\nu) + \overbrace{C_{\phi \rightarrow \bar{\nu}\nu} - C_{\bar{\nu}\nu \rightarrow \phi}(T_\nu)}^{\text{New physics contribution to } T_\nu} - 4H\rho_\nu}{\frac{\partial \rho_\nu}{\partial T_\nu}},$$

$$\frac{dT_\gamma}{dt} = \frac{-C_{inel.}(T_\gamma, T_\nu) - C_{el}(T_\gamma, T_\nu) - 3H(\rho_e + \rho_\gamma) - 3H(p_e + p_\gamma)}{\frac{\partial \rho_\gamma}{\partial T_\gamma} + \frac{\partial \rho_e}{\partial T_\gamma}}.$$

$$\begin{aligned} \frac{dY_\phi}{dx} &= \frac{h_{\text{eff}} s_\gamma}{xH} \langle \sigma v_{\text{rel}} \rangle_{SS \rightarrow \phi\phi}^{T_D} \left[ Y_S^2 - \left( \frac{Y_S^{\text{eq}}(T_D)}{Y_\phi^{\text{eq}}(T_D)} \right)^2 Y_\phi^2 \right] \\ &+ \frac{h_{\text{eff}}}{xH} \left( \langle \Gamma_\phi \rangle_{T_\nu} Y_\phi^{\text{eq}}(T_\nu) - \langle \Gamma_\phi \rangle_{T_D} Y_\phi \right) \end{aligned}$$

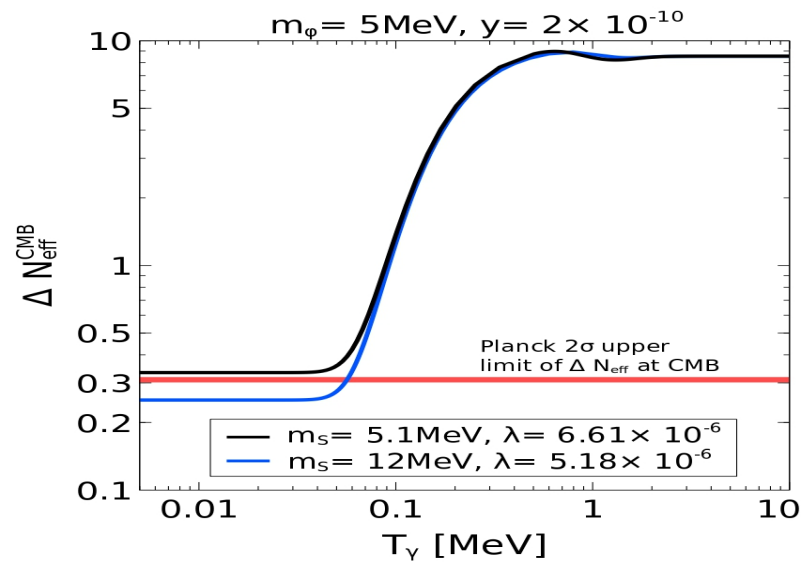
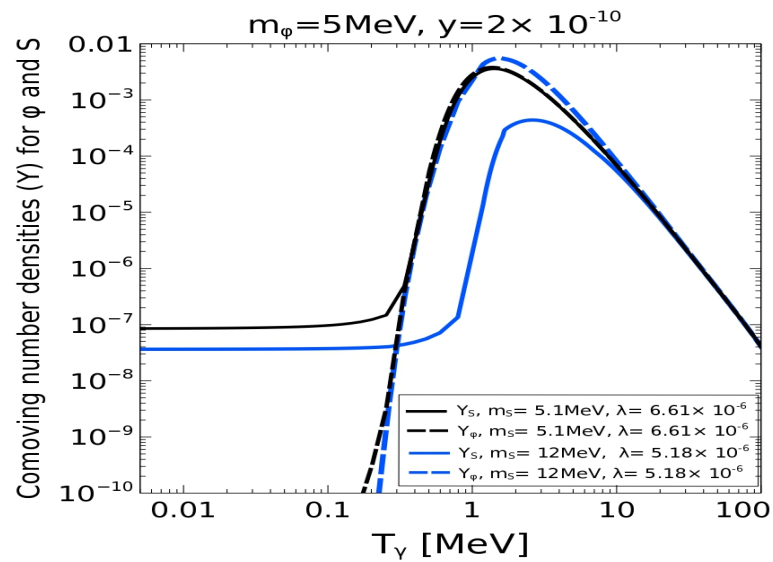
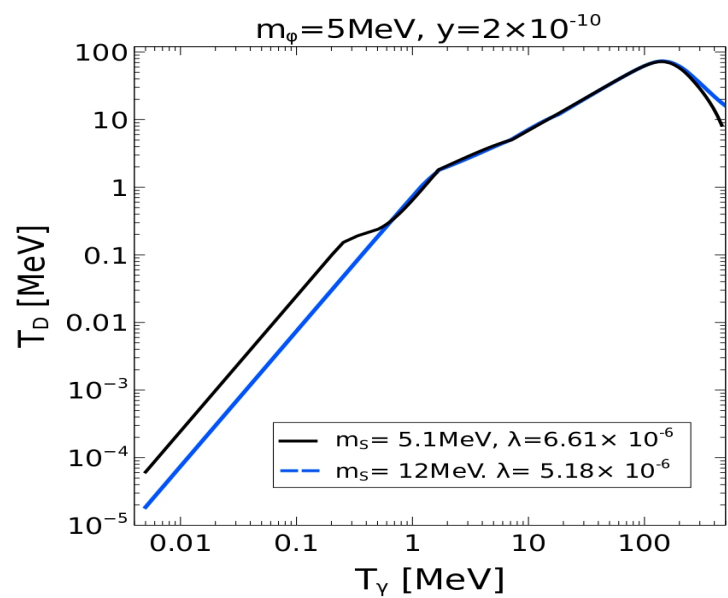
Where we define,  $x = \frac{m_S}{T_\gamma}$ ,

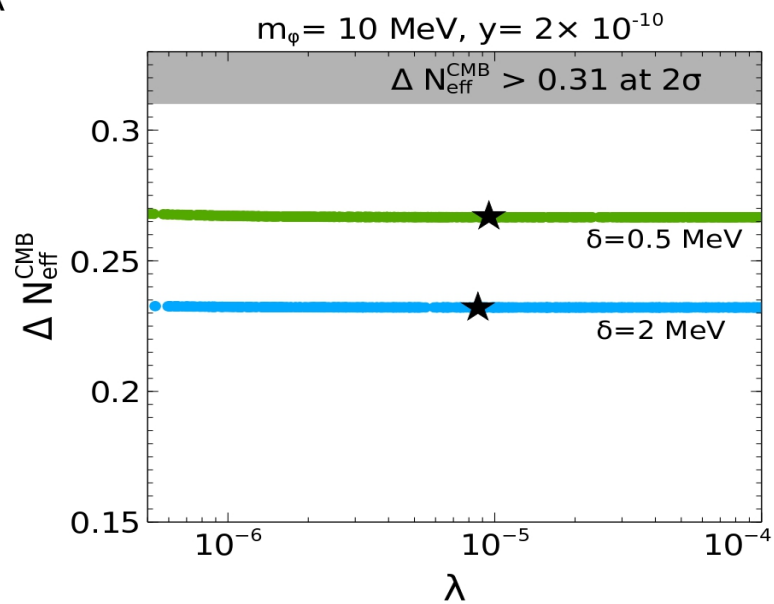
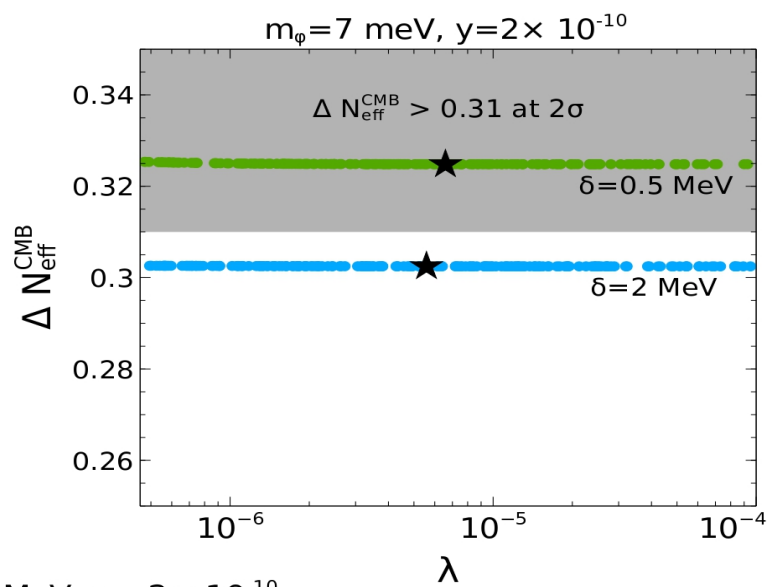
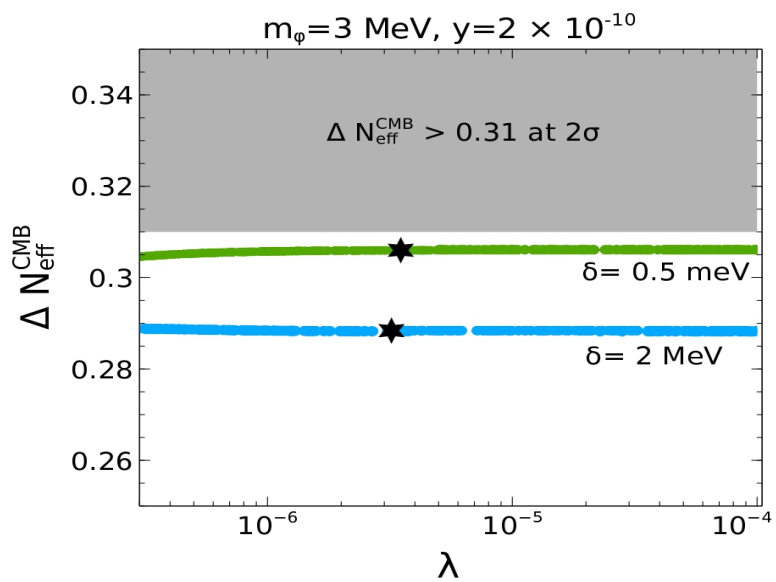
$$\frac{dY_S}{dx} = -\frac{h_{\text{eff}} s_\gamma}{xH} \langle \sigma v_{\text{rel}} \rangle_{SS \rightarrow \phi\phi}^{T_D} \left[ Y_S^2 - \left( \frac{Y_S^{\text{eq}}(T_D)}{Y_\phi^{\text{eq}}(T_D)} \right)^2 Y_\phi^2 \right]$$

$$F_1 = s_\gamma \langle \sigma v \rangle_{SS \rightarrow \phi\phi}^{T_D} \left[ Y_S^2 - \left( \frac{Y_S^{\text{eq}}(T_D)}{Y_\phi^{\text{eq}}(T_D)} \right)^2 Y_\phi^2 \right] \left( \rho_S^{\text{eq}} Y_\phi^{\text{eq}} - \rho_\phi^{\text{eq}} Y_S^{\text{eq}} \right),$$

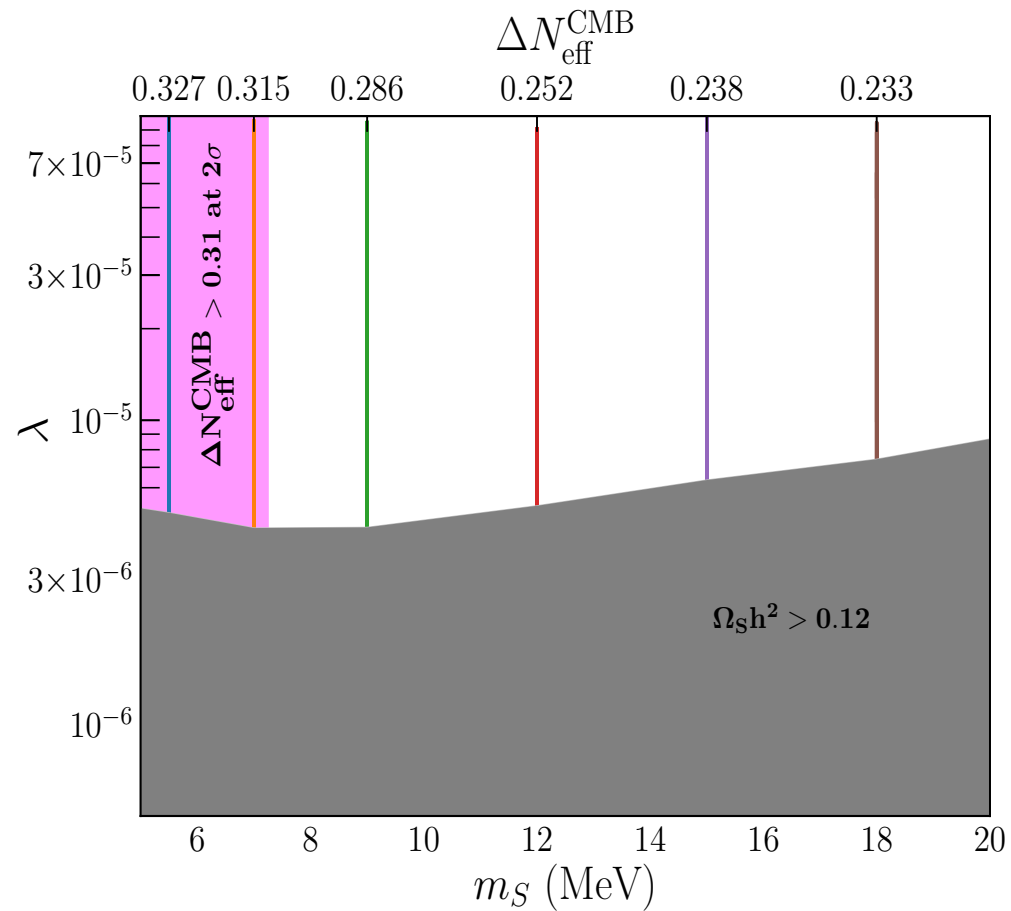
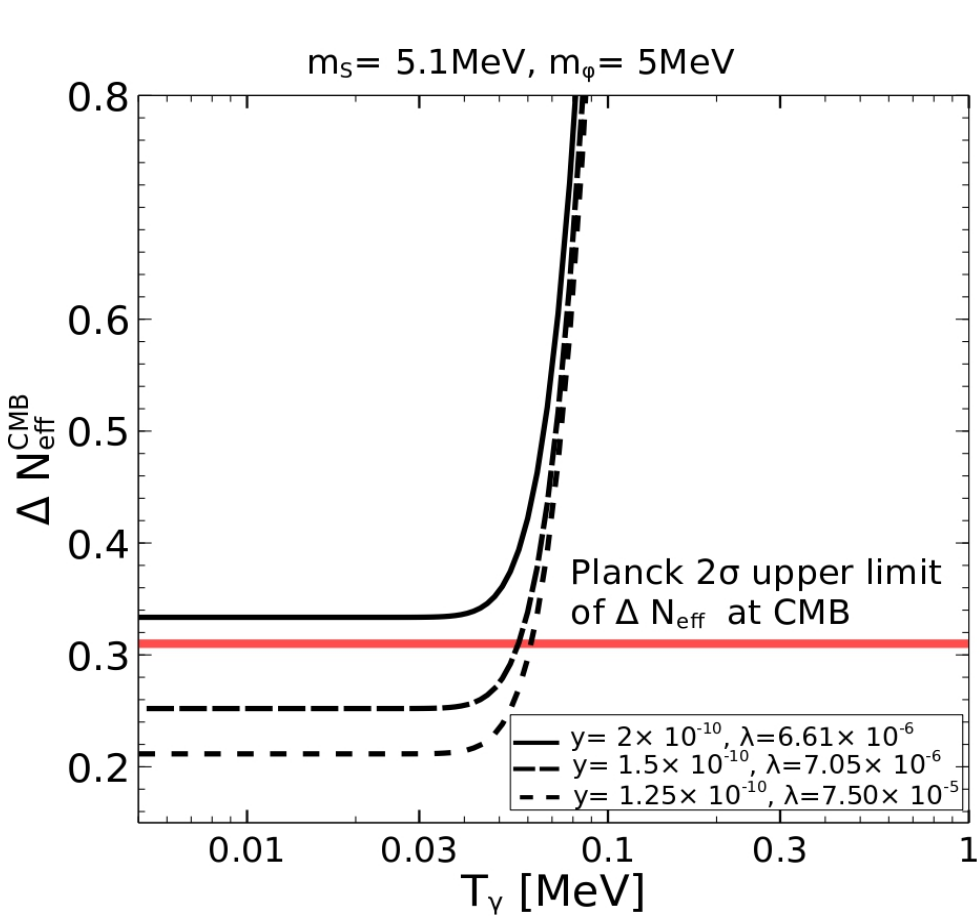
$$F_2 = -\rho_\phi^{\text{eq}}(T_D) Y_\chi^{\text{eq}}(T_D) \left[ \langle \Gamma_{\phi \rightarrow \nu\nu} \rangle_{T_\nu} Y_\phi^{\text{eq}}(T_\nu) - \langle \Gamma_{\phi \rightarrow \nu\nu} \rangle_{T_D} Y_\phi \right].$$

$$\frac{dT_D}{dx} = \frac{s_\gamma Y_\phi^{\text{eq}}(T_D) Y_S^{\text{eq}}(T_D) \left\{ \frac{1}{s_\gamma} C_{\nu\nu \leftrightarrow \phi} - 3H(Y_\phi + Y_S) T_D \right\} + F_1 + F_2}{xH \sum_{i \neq j} Y_i Y_j^{\text{eq}} \left\{ \frac{d\rho_i^{\text{eq}}}{dT_D} - \frac{1}{n_i^{\text{eq}}(T_D)} \frac{dn_i^{\text{eq}}(T_D)}{dT_D} \rho_i^{\text{eq}}(T_D) \right\}},$$





$$\delta = m_S - m_\phi$$



## Conclusions

1. We obtain unique predictions for the  $\Delta N_{\text{eff}}$  for a particular DM mass that satisfies the relic density bound with suitable value of  $\lambda$ , provided mass of the other scalar and its coupling strength with the SM neutrinos are fixed.
2. The dark matter mass has a nontrivial role on the prediction of  $\Delta N_{\text{eff}}$ . The predictions for  $\Delta N_{\text{eff}}$  turns out to be maximum in the nearly degenerate spectrum of dark sector particles and consideration of an increased hierarchy CMB between the dark sector particles reduces the impact of dark matter mass on  $\Delta N_{\text{eff}}$ . We also find that prediction CMB for  $\Delta N_{\text{eff}}$  is insensitive to the dark sector interaction rate, provided the dark thermal equilibrium is reached.
3. Increasing  $m_\phi$  upto a certain value keeping other parameters ( $y$ ,  $\lambda$  and  $\delta$ ) fixed, enhances  $\Delta N_{\text{eff}}$  hence restricted by the present Planck limit. When  $m_\phi$  is too large, the effect on  $\Delta N_{\text{eff}}$  of  $\phi$  diminishes.
4. For a particular  $m_\phi$  with a constant  $y$ , we are able to impose a lower bound on the DM mass from the Planck  $2\sigma$  CMB data on  $\Delta N_{\text{eff}}$ . As an example we find  $m_s \gtrsim 7$  MeV when  $m_\phi = 5$  MeV and  $y = 2 \times 10^{-10}$ . Additionally, a lower bound on  $\lambda$  can be derived such that the DM relic abundance remain below 0.12 as experimentally favored.
5. Finally, the upcoming CMB stage-IV experiment with improved sensitivity can probe the allowed region of model parameter space.