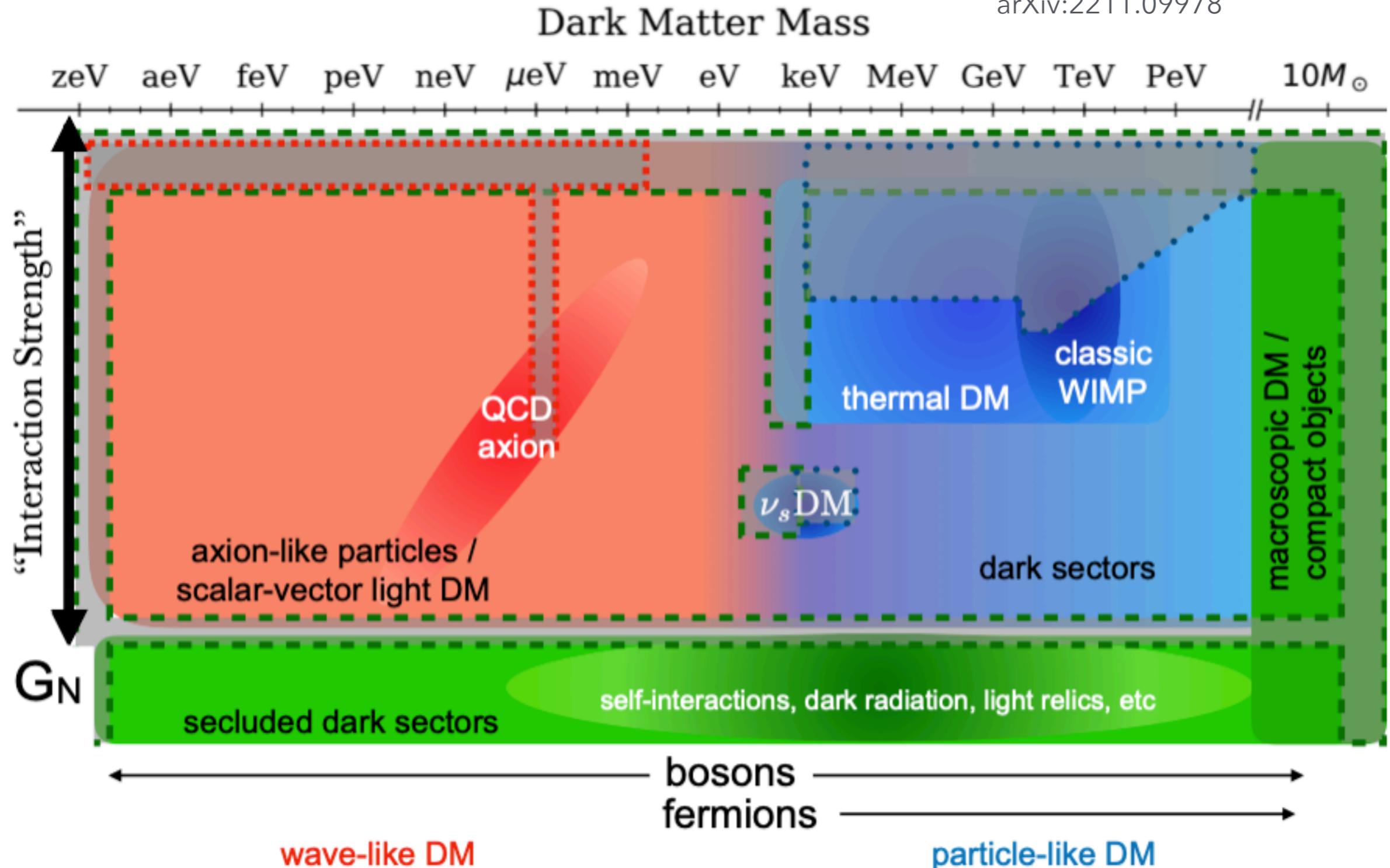


# Dark matter: theoretical status

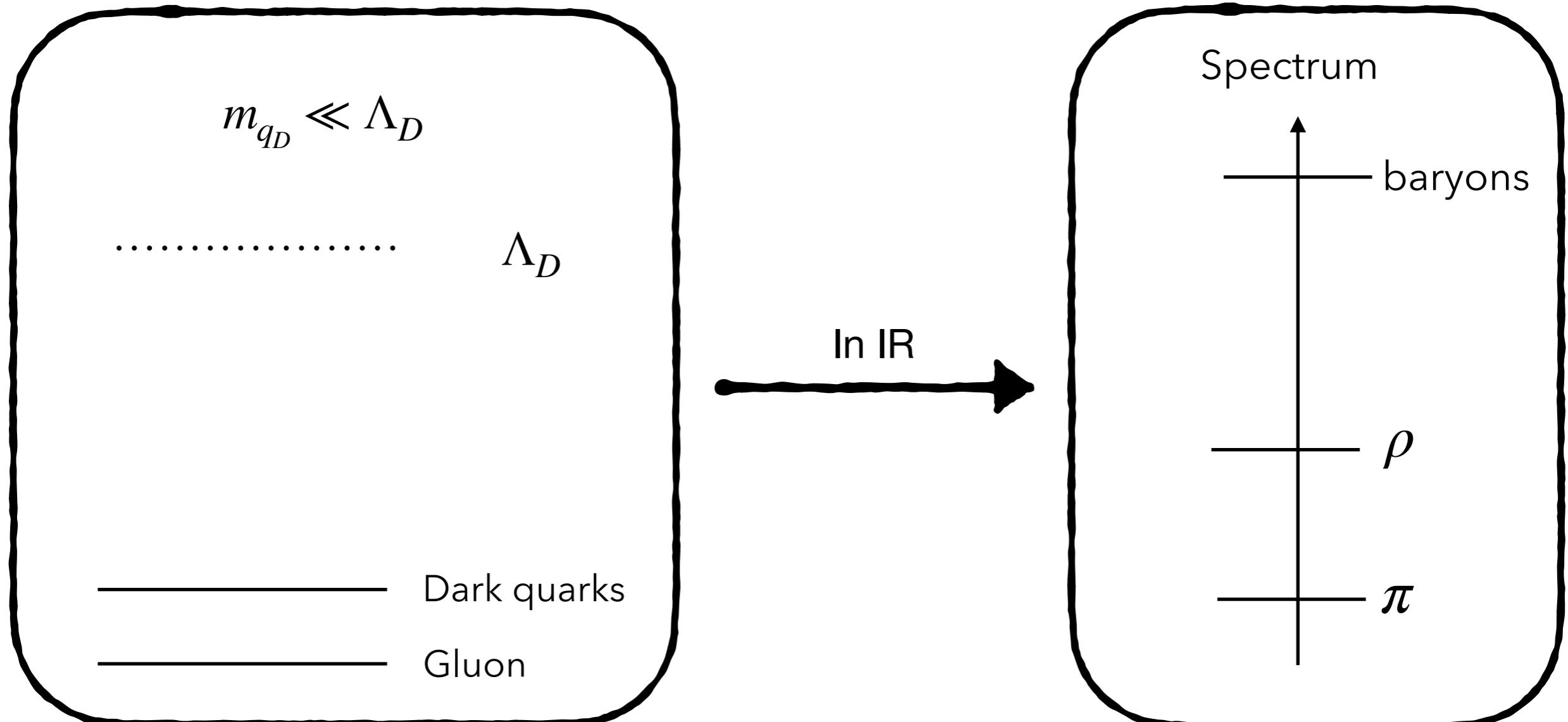
Suchita Kulkarni (she/her)  
Junior group leader  
[suchita.kulkarni@uni-graz.at](mailto:suchita.kulkarni@uni-graz.at)

# Dark matter: where are we?

Snowmass cosmic frontier  
arXiv:2211.09978



# Can dark matter be composite instead of elementary?



- UV and IR dynamics are correlated with each other; learning about UV can teach us about IR and vice-versa

# Can dark matter be composite instead of elementary?

- Composite Higgs: dark sector (DS) scale related to the SM

Nussinov Phys.Lett.B 165 (1985) 55-58, Chivakula et al,  
Nucl.Phys. B329 (1990) 445, Hietanen et al.,  
arXiv:1308.4130, Cacciapaglia et al arXiv:2002.04914

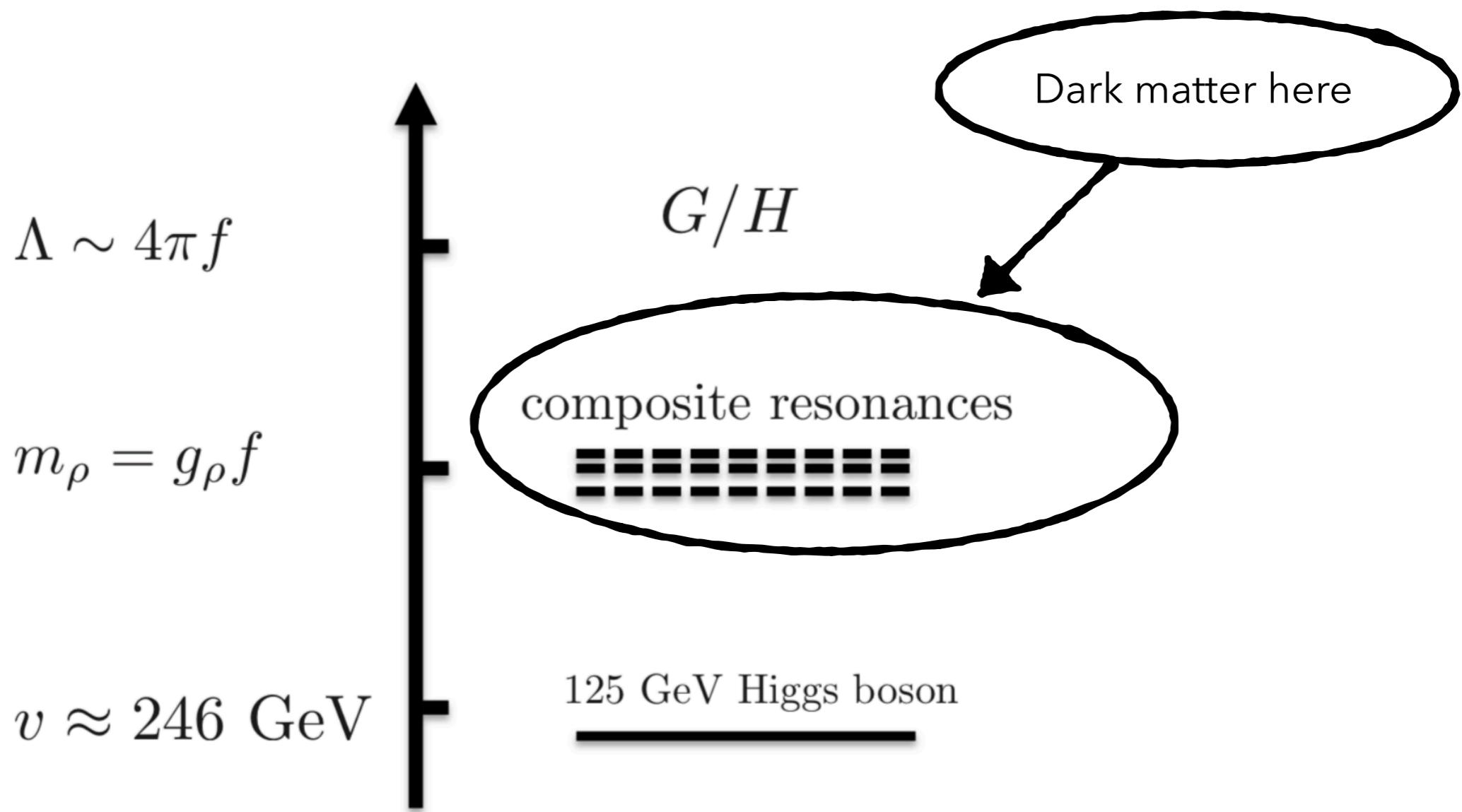


Figure from Liu et. al. arXiv:1904.00026

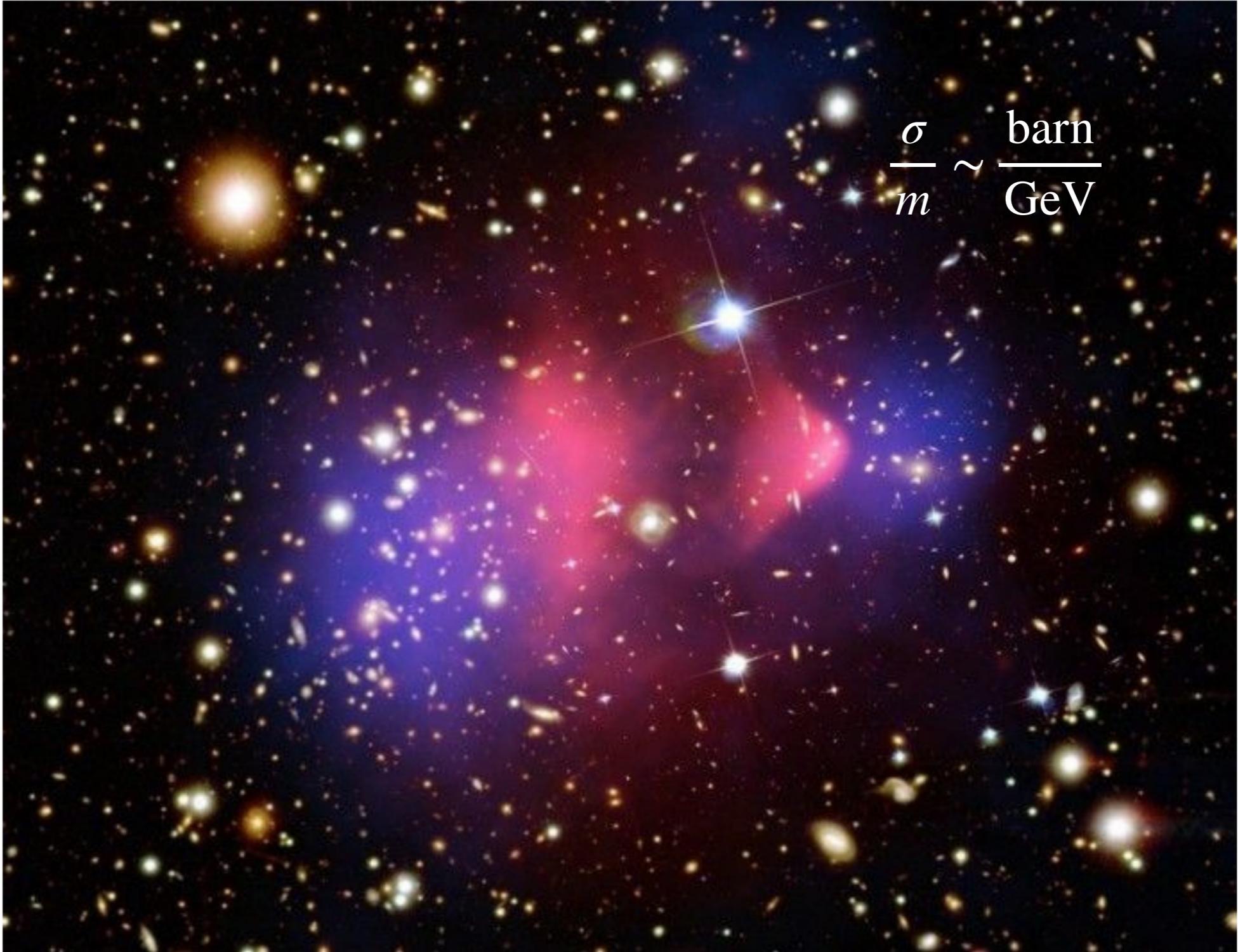
# Why strongly interacting dark matter

Why not!

That's a reason but let's explore a bit more

# Large self-interactions possible

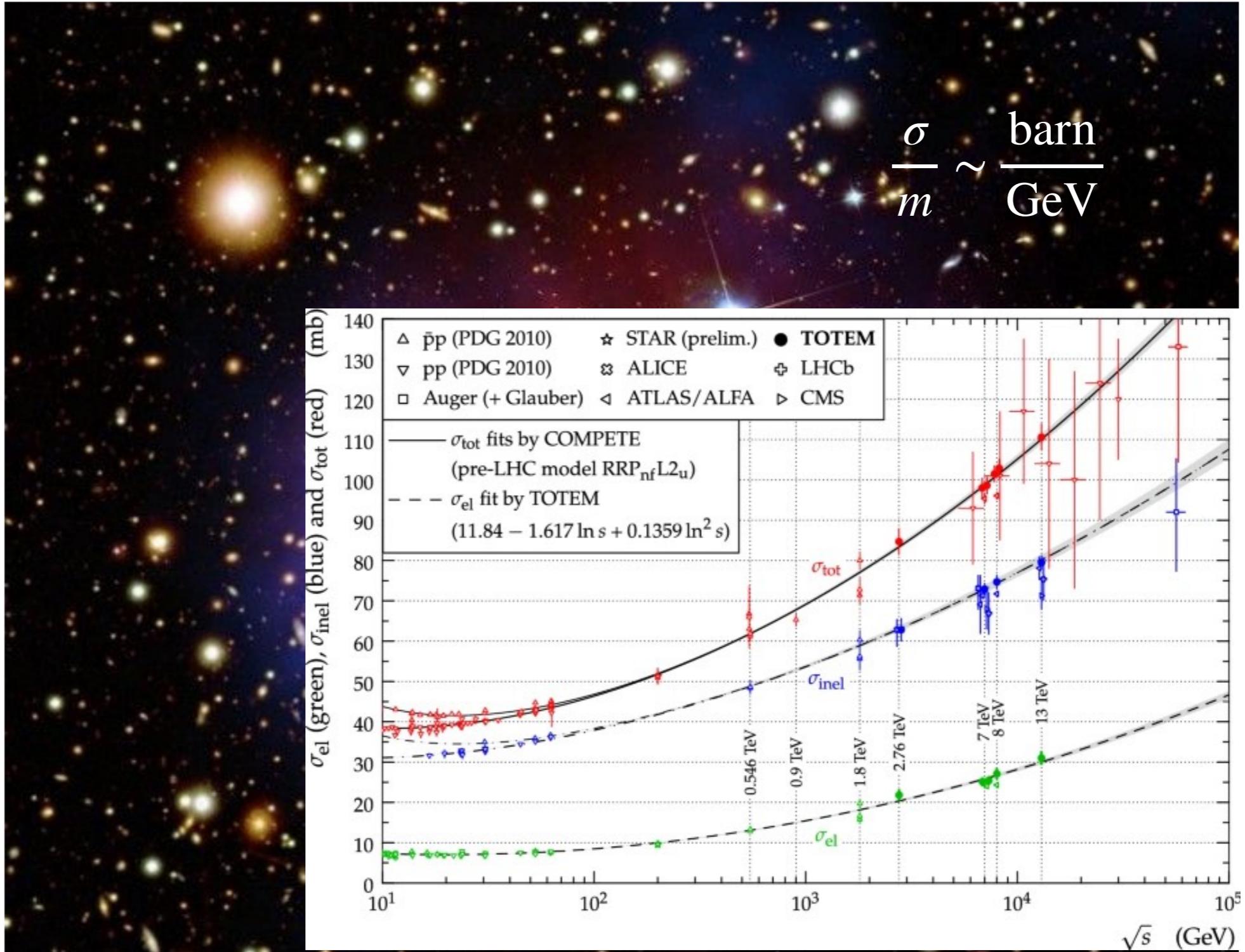
See also review talk by J. Bagla



$$\frac{\sigma}{m} \sim \frac{\text{barn}}{\text{GeV}}$$

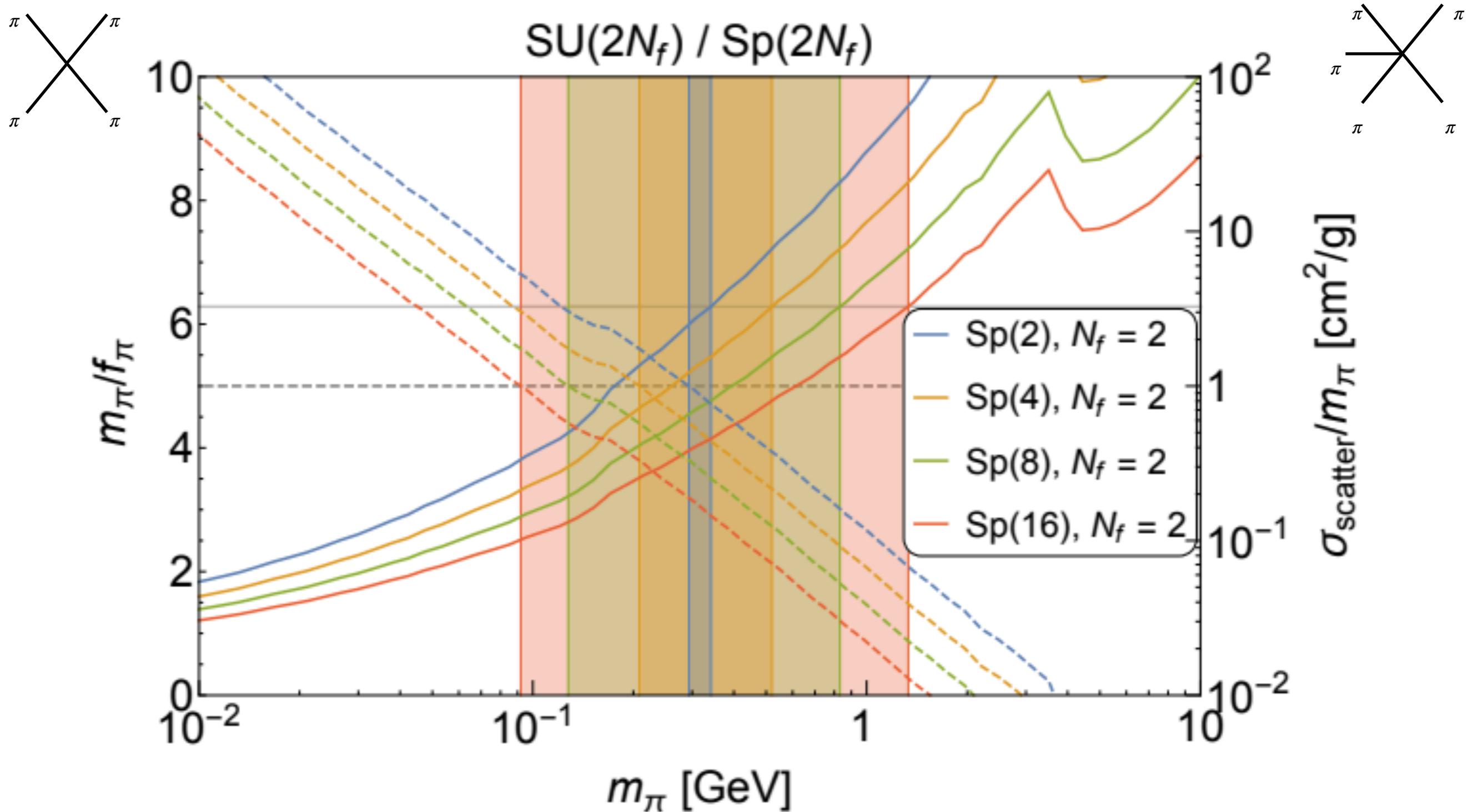
# Large self-interactions possible

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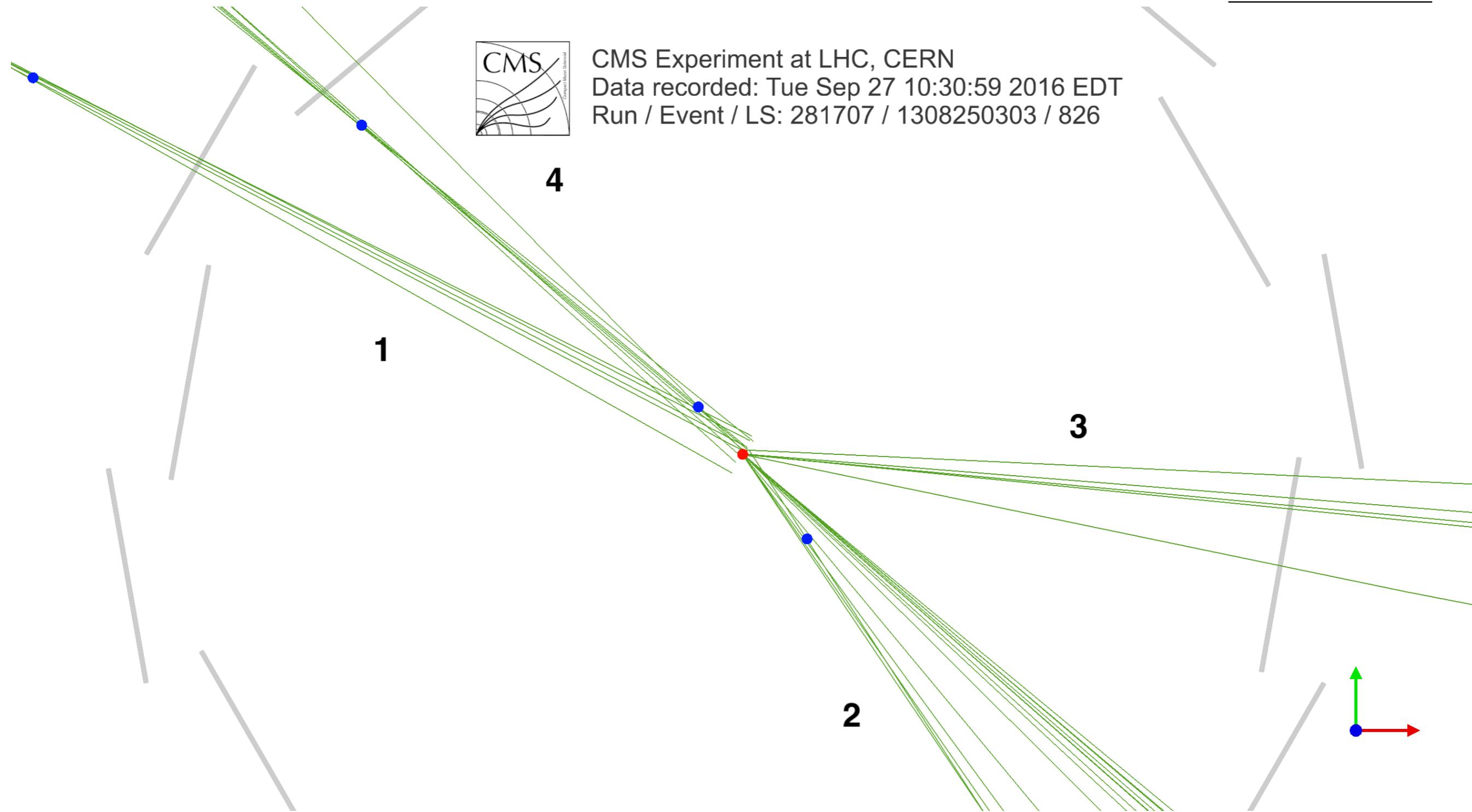
# Can also generate relic

Hochberg et al arXiv:1411.3727



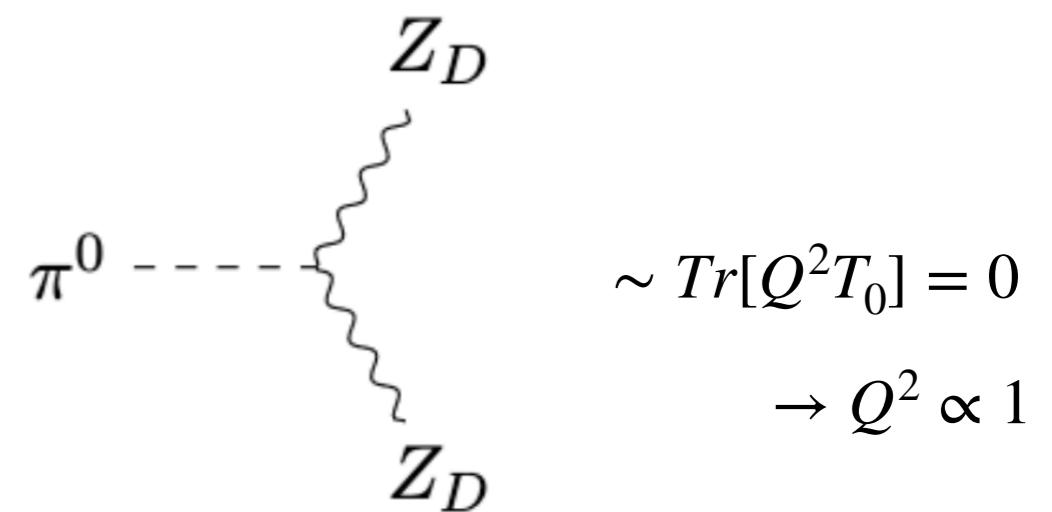
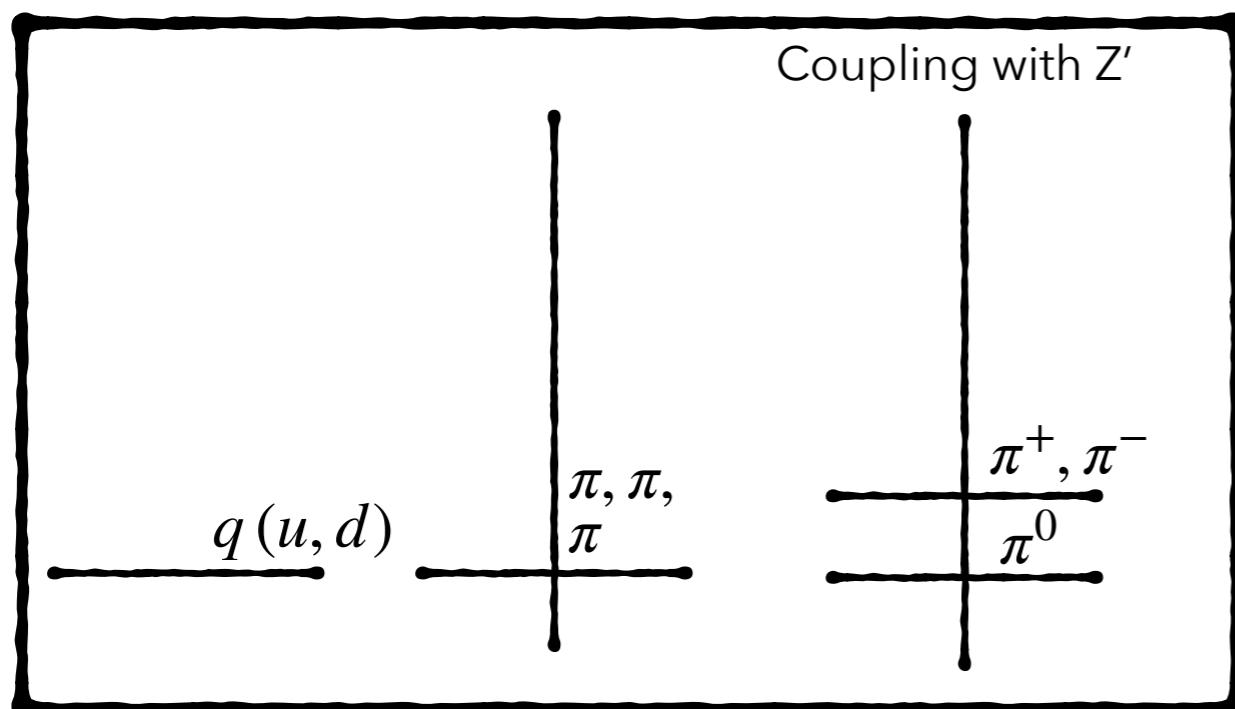
# Lead to new experimental signatures

arXiv:1810.10069



# Primary obstacles in theory constructions

- DM longevity needs to be ensured
  - Impose external symmetries
  - Use accidental symmetries e.g. lightest baryon (proton) is stable in the SM due to baryon number conservation
  - Engineer models to ensure stability



- Quantitative estimates from genuine non-perturbative physics are needed (Oida!)

# Oida

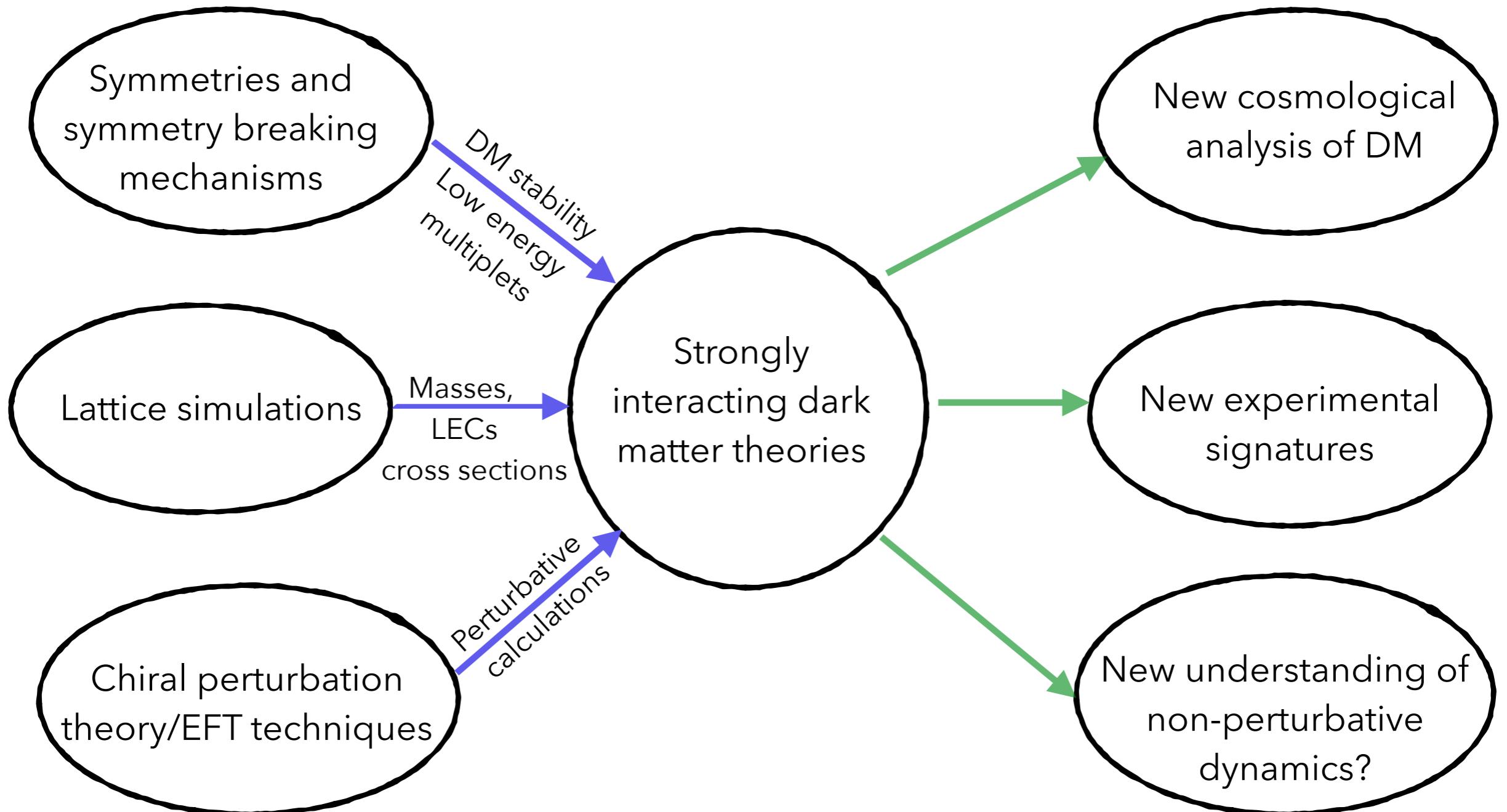
German/Austrian/Bavarian expression

Literal meaning: Old one (dude/mate)

Can be used to pretty much express any emotion (see [here](#))

# Strongly interacting theories: pathways

How to make systematic progress in the landscape of strongly interacting dark matter?

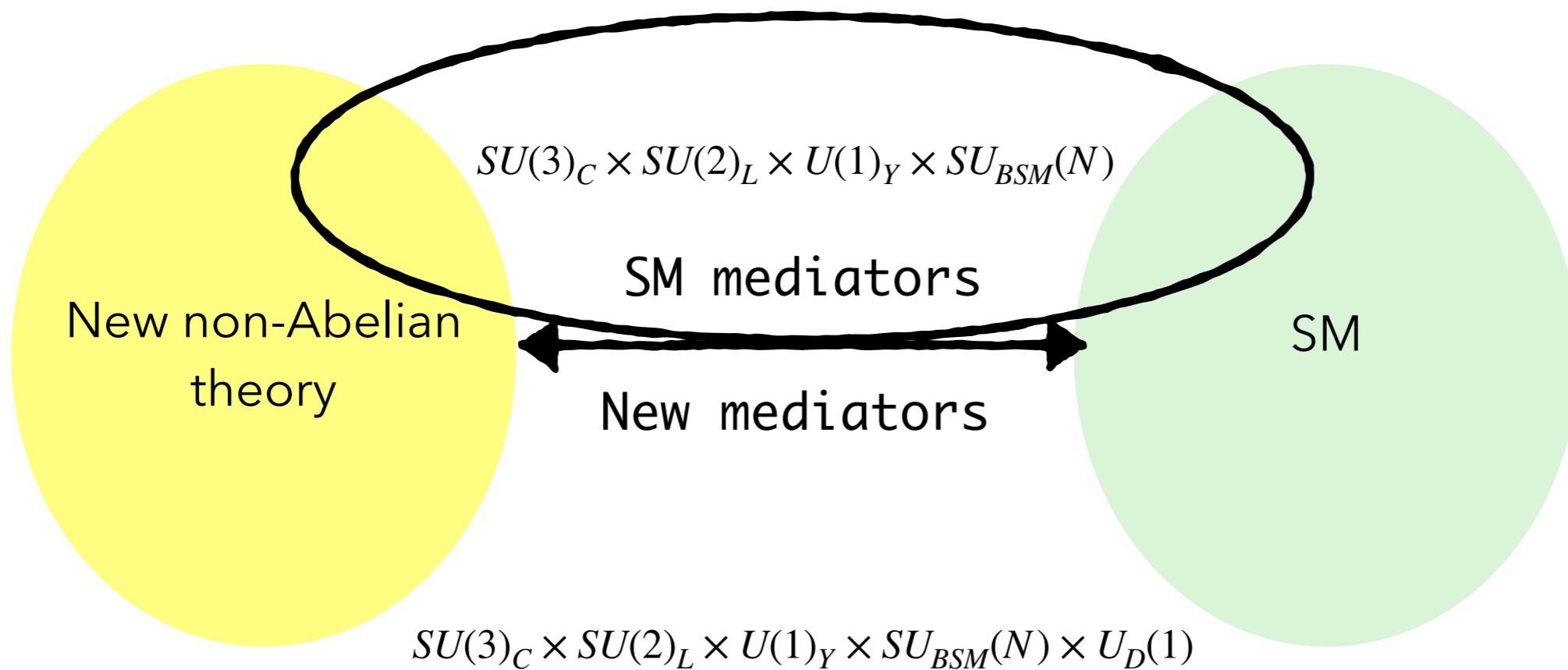


N.B. All calculations can be done on lattice, but they are expensive,  
perturbative analysis is pragmatic way out



New non-Abelian  
theory

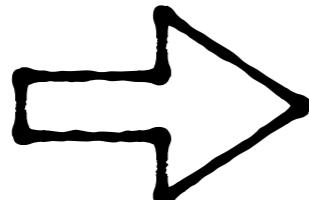
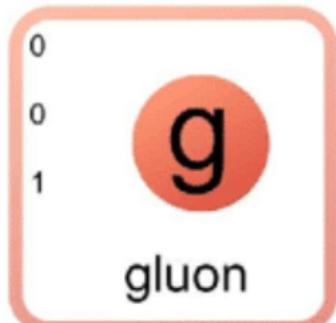
# Portal phenomenology - I



J. Butterworth, L. Corpe, **SK.**, X. Kong, M. Thomas arXiv:2105.08494

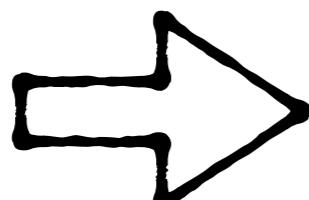
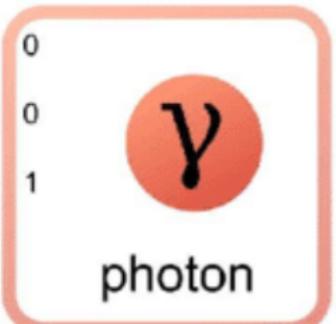
# SM mediators

Appelquist et al arXiv:1402.6656  
Bagnasco et. al. hep-ph/9310290



Relevant if DS has SM color charges

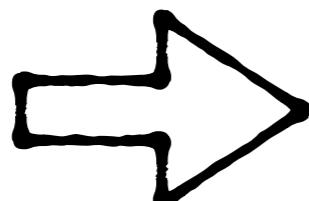
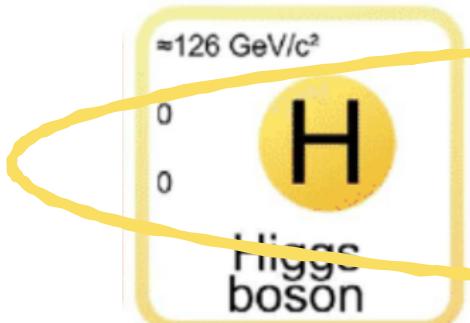
See: Chivukula et. al. hep-ph/9210274; Godbole et. al. 1506.01408; Bay and Osborne 1506.07110



Lowest dimensional operators:

- magnetic dipole (5)
- charge radius (6)
- polarizability (7)

Similar considerations for W/Z mediators, suppressed by masses

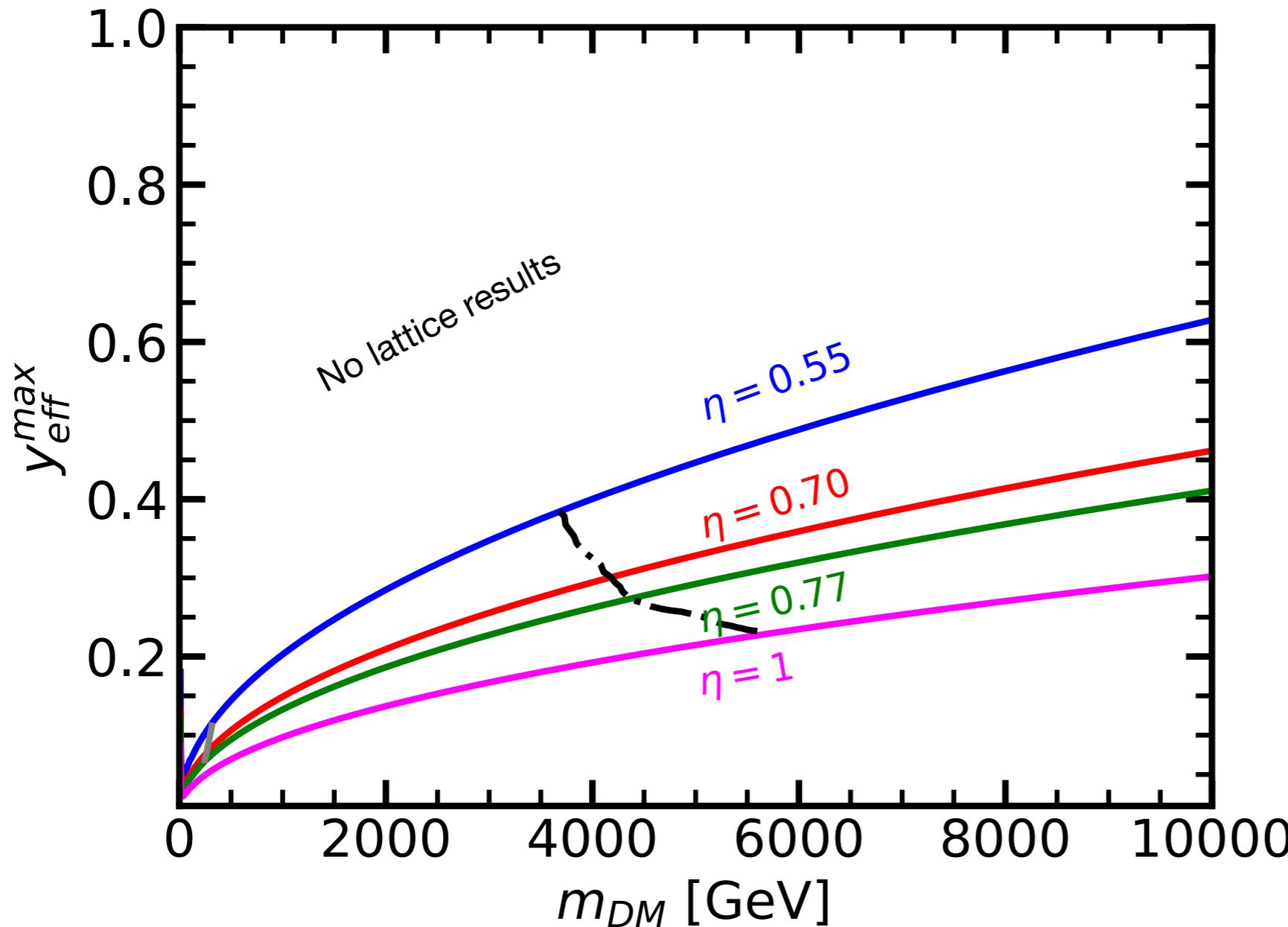


Most relevant interaction if constituents have Yukawa couplings

- Focus on Higgs mediated interactions
- Theory with  $N_{c_D} = 4, N_{f_D} = 4$ ; contains scalar baryon
- Dark quarks get part of their masses from EWSB and partly vector-like

# Higgs mediators

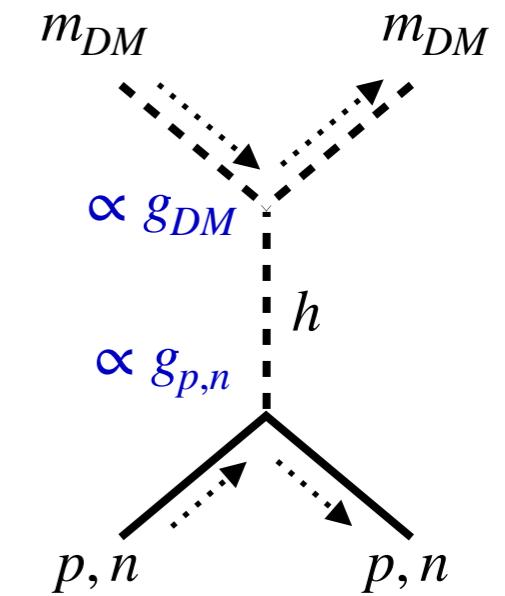
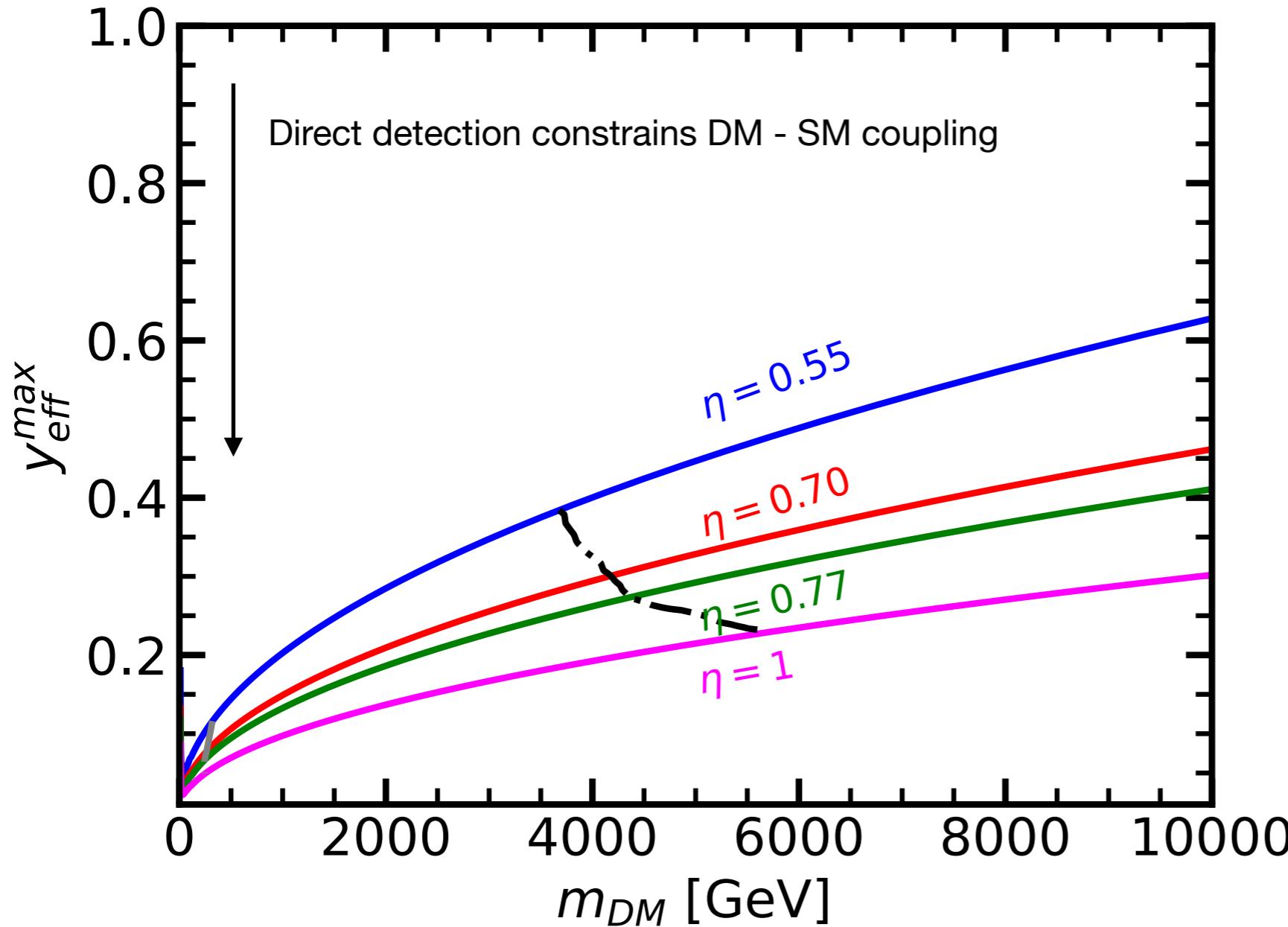
J. Butterworth, L. Corpe, S.K. et. al. arXiv:2105.08494



Either require low values of Higgs - dark quark effective Yukawa coupling or require very heavy dark matter

# Higgs mediators

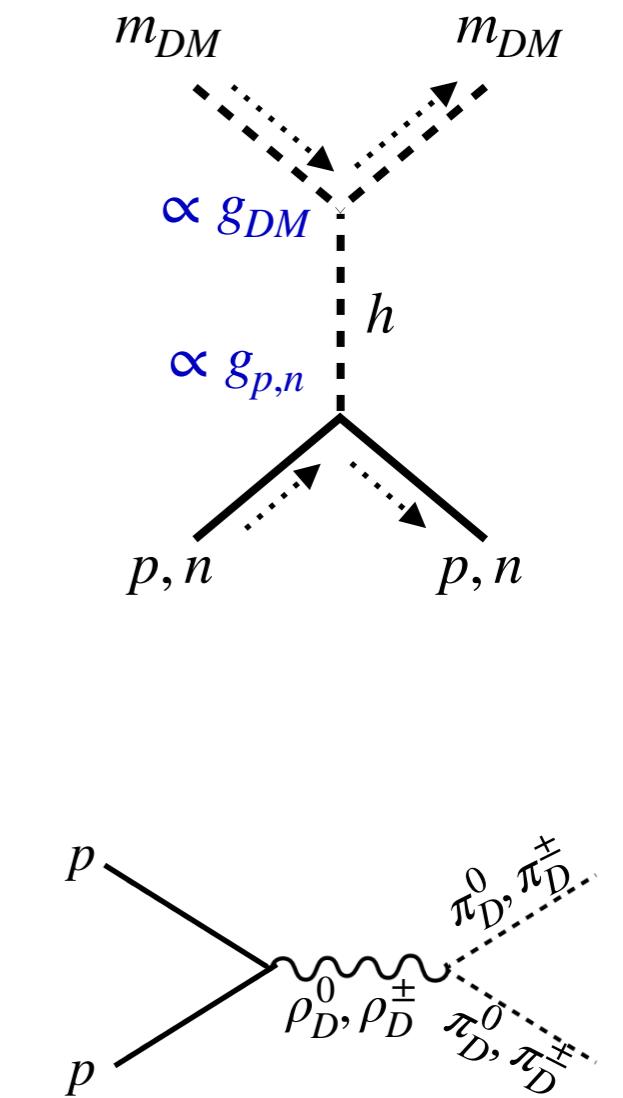
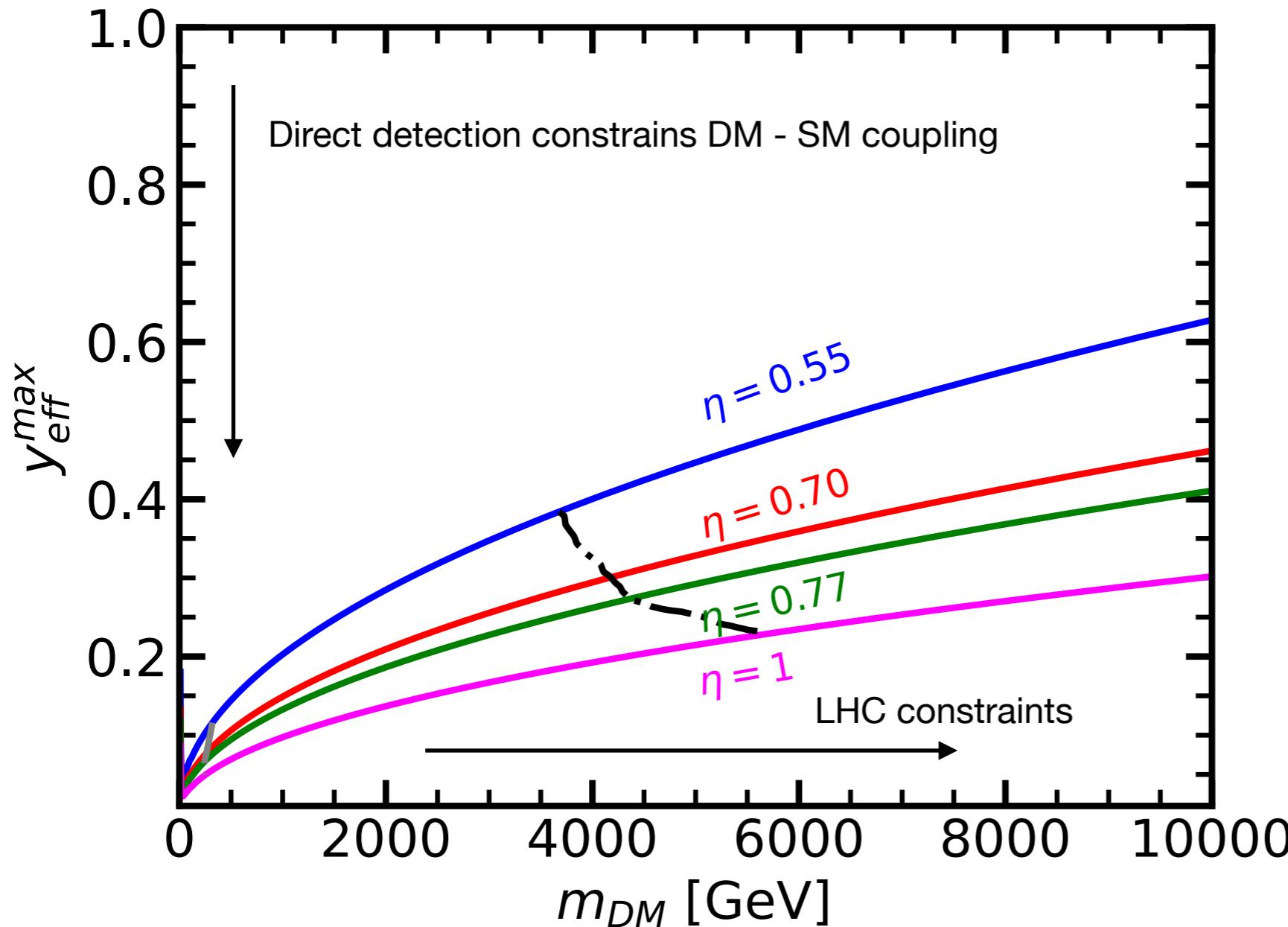
J. Butterworth, L. Corpe, S.K. et. al. arXiv:2105.08494



Either require low values of Higgs - dark quark effective Yukawa coupling or require very heavy dark matter

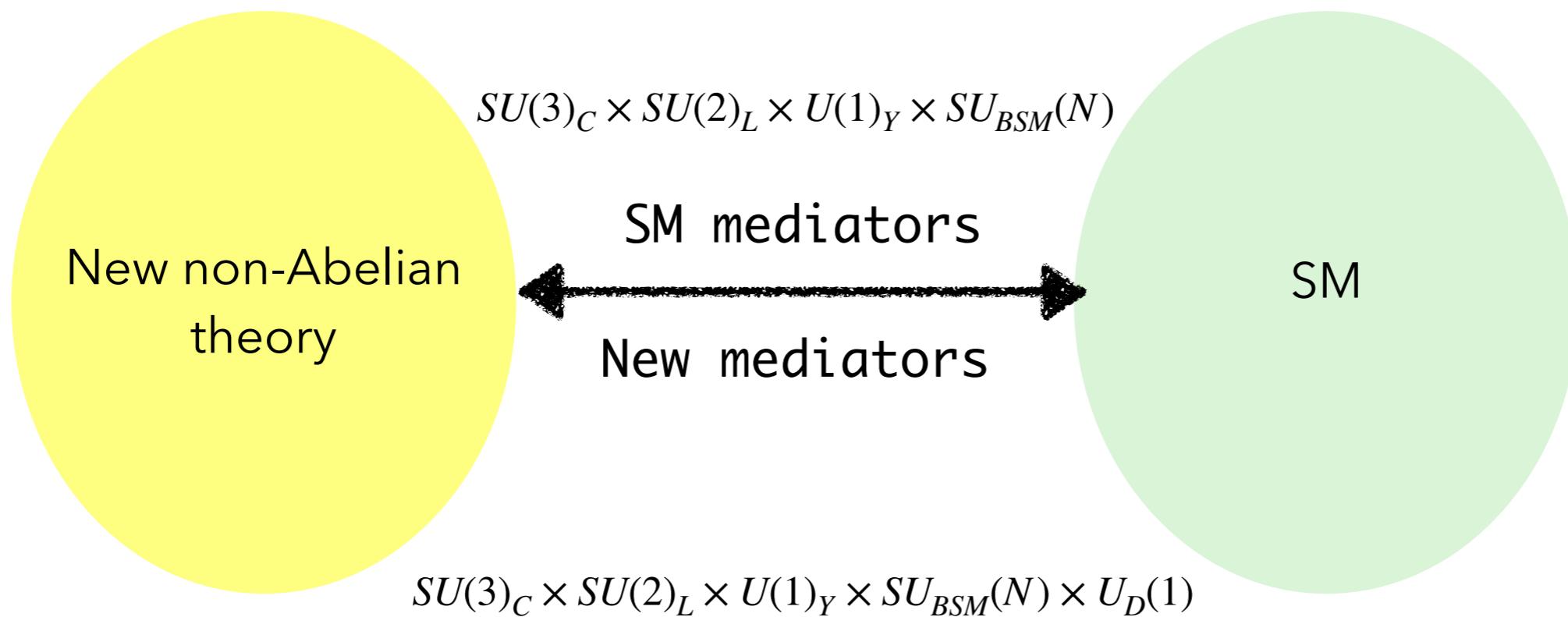
# Higgs mediators

J. Butterworth, L. Corpe, S.K. et. al. arXiv:2105.08494



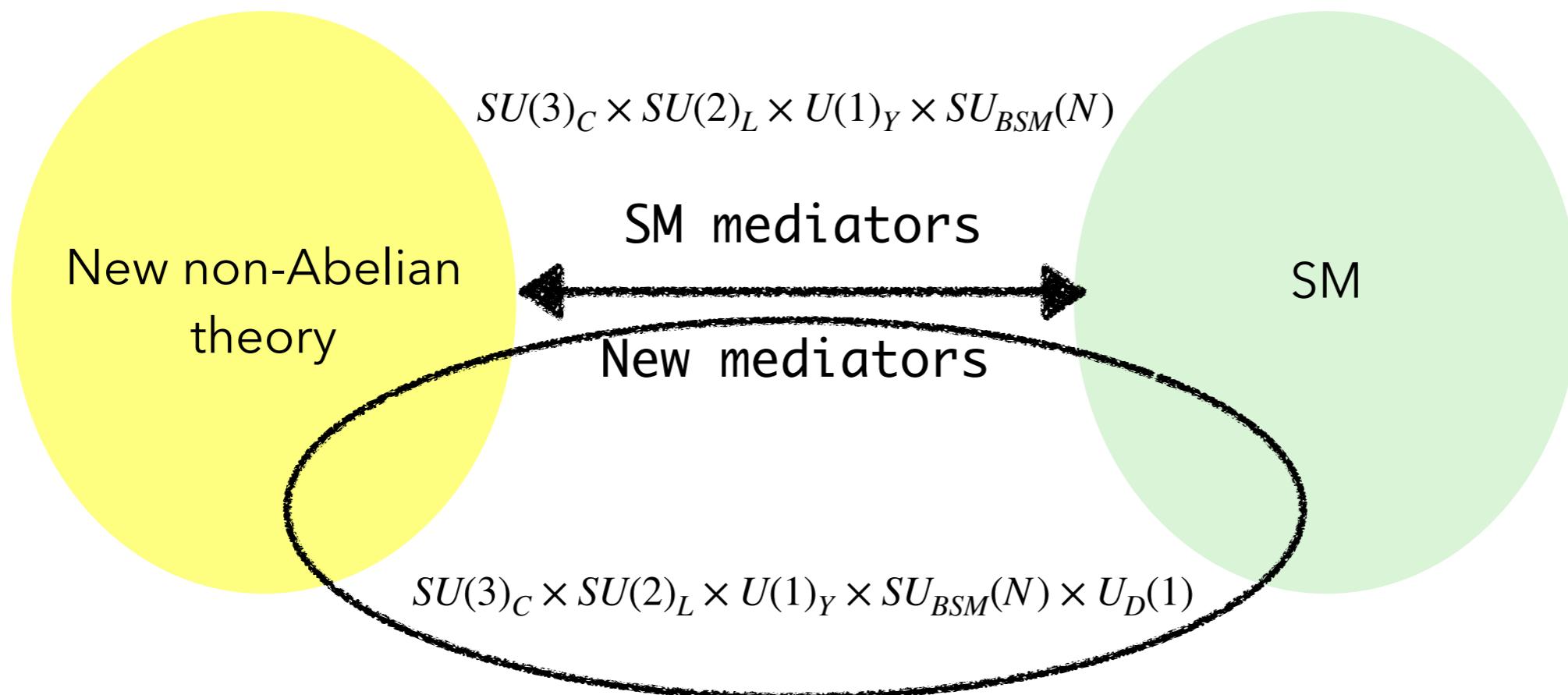
Either require low values of Higgs - dark quark effective Yukawa coupling or require very heavy dark matter

# Portal phenomenology - II



Snowmass darkshowers (incl. **S.K.**, S. Mee, M. Strassler) arXiv:2202.05191

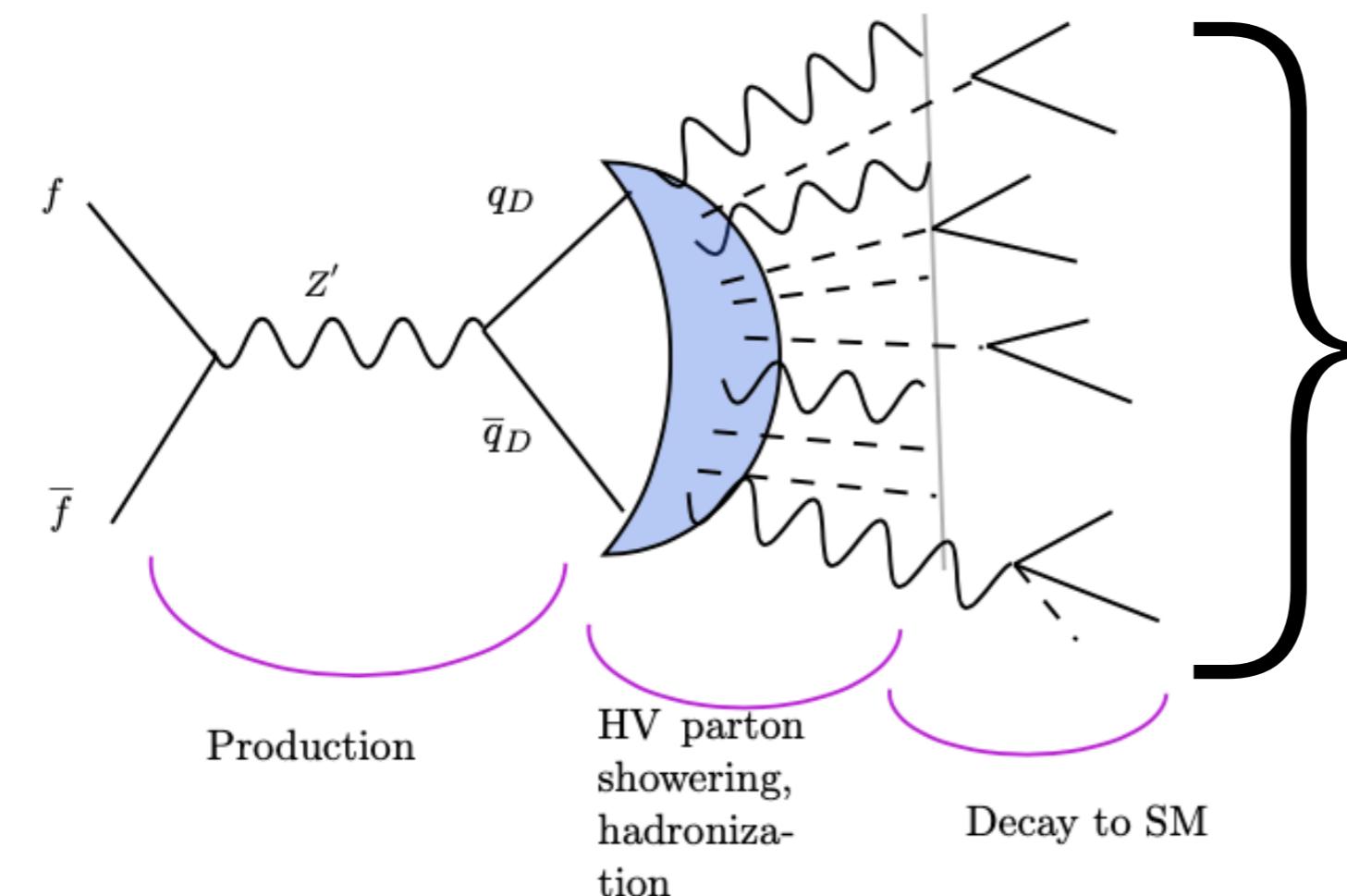
# Portal phenomenology - II



Snowmass darkshowers (incl. **S.K.**, S. Mee, M. Strassler) arXiv:2202.05191

# Theory setup

$$\mathcal{L}_{\text{int}} \subset -e_D Z'_\mu \sum_i \bar{q}_{Di} Q_i \gamma^\mu q_{Di} - g_q Z'_\mu \sum_r \bar{q}_{SM,r} \gamma^\mu q_{SM,r}$$



Strassler et al hep-ph/0604261  
 Cohen et al arXiv:1503.00009  
 Schwaller et al arXiv:1502.05409  
 LLP community report arXiv:1903.04497  
 Kahlhoefer et.al. arXiv:1907.04346  
 Hofman et al arXiv:0803.1467  
 Strassler arXiv:0801.0629  
 Knapen et al arXiv:1612.00850

- Jets with large MET inside
- Jets with displaced vertices
- Jets with too many or too few tracks

- $m_{q_D} \ll \Lambda_D \ll m_{Z'} \rightarrow$  production of dark quarks followed by rapid parton showering and hadronization  $\rightarrow$  jets
- $Z'$  coupling leads to decay of some of the dark hadrons back to the SM; details coupling dependent

# Lattice inputs

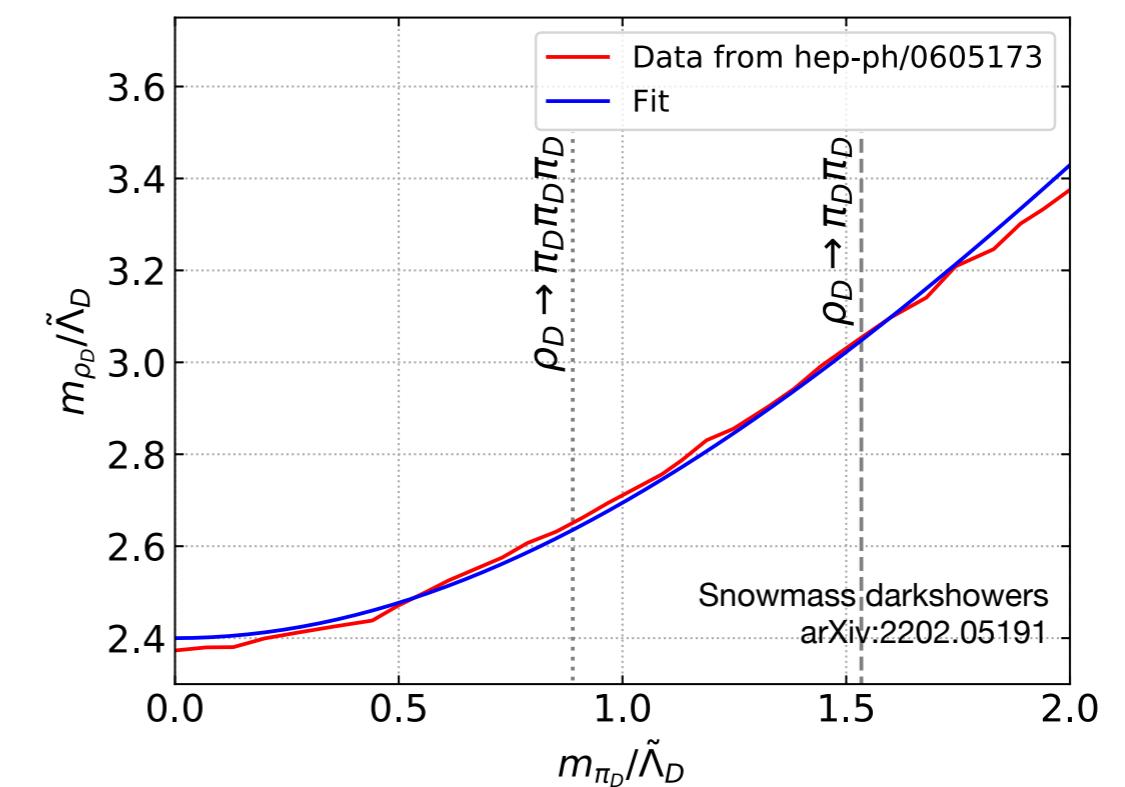
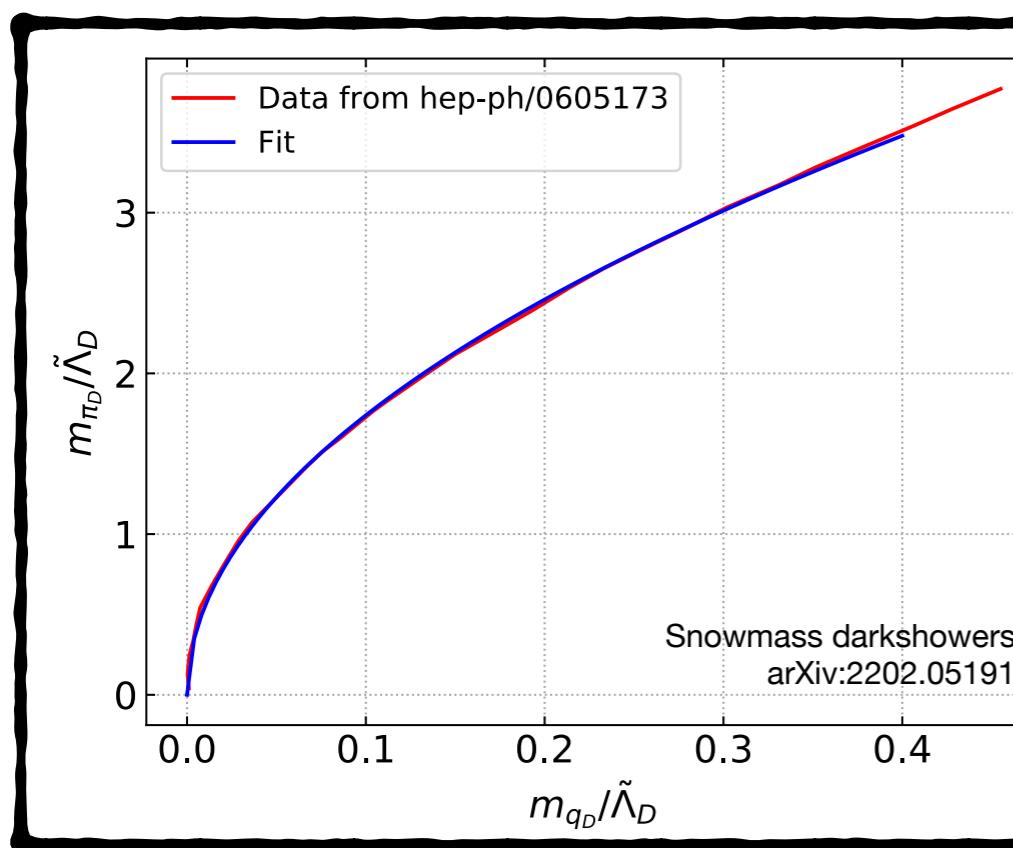


Snowmass darkshowers arXiv:2202.05191

- Effects due to  $N_{c_D}, N_{f_D}$  can be ignored for now
- Dark meson mass fits from lattice results

$$\frac{m_{\pi_D}}{\tilde{\Lambda}_D} = 5.5 \sqrt{\frac{m_{q_D}}{\tilde{\Lambda}_D}}$$

$$\frac{m_{\rho_D}}{\tilde{\Lambda}_D} = \sqrt{5.76 + 1.5 \frac{m_{\pi_D}^2}{\tilde{\Lambda}_D^2}}$$



# Beyond SU(N) groups

Needs "durchhiaseln"

## durchhiaseln

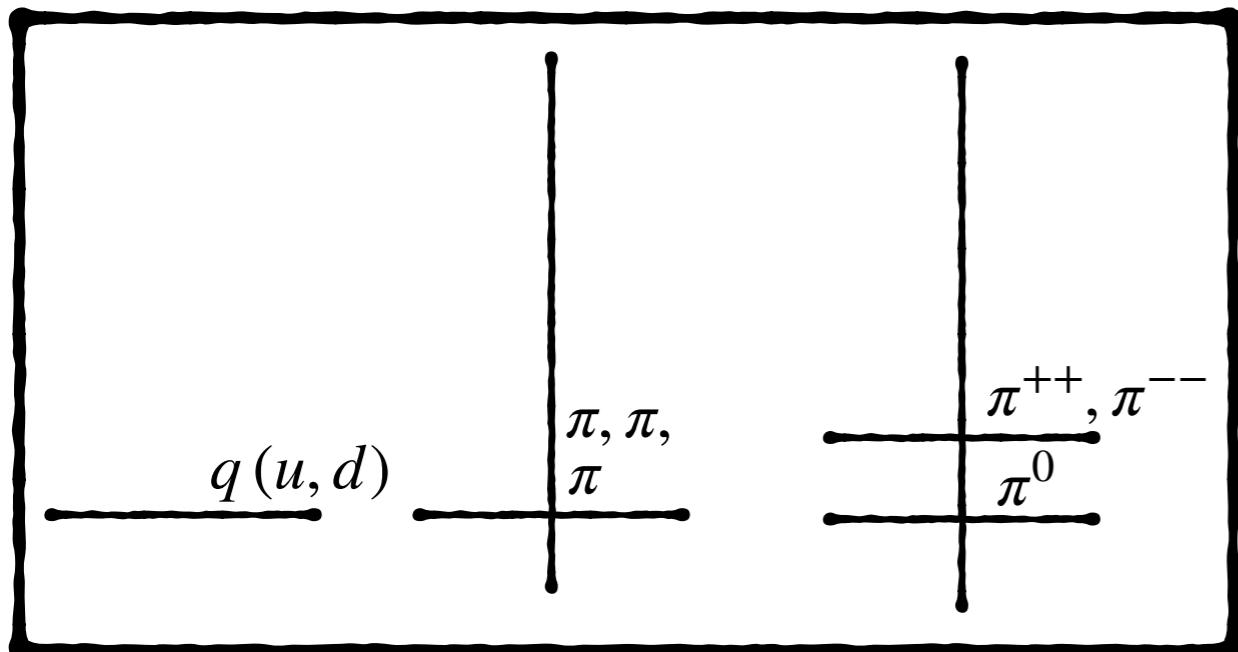
Used in rural Austria, particular in upper Murtal region  
A long and tedious calculation

# Number of pions can be very different - I

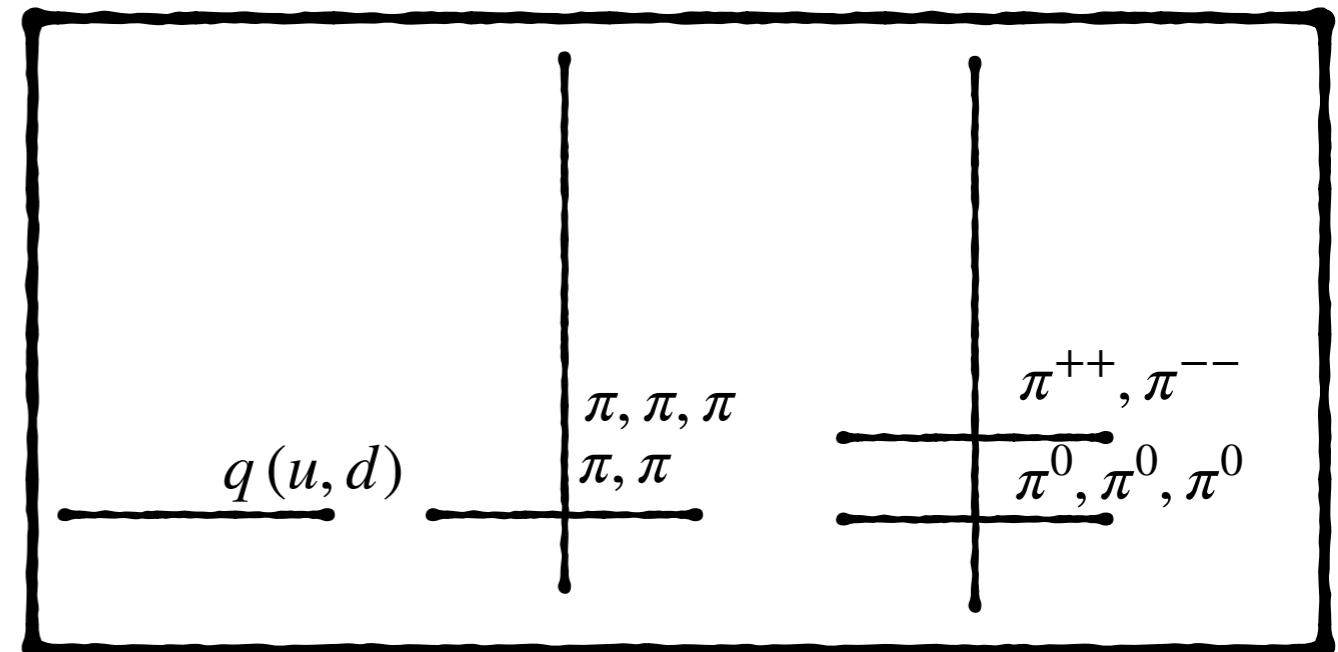
S.K., A. Maas, S. Mee, M. Nikolic, J. Pradler, F. Zierler arXiv:2202.05191

- SU(N) gauge groups: need three fermions in fundamental representation to get at least five pions
- Sp(N) gauge group: Need two fermions in fundamental representation to get five pions  
 $SU(2N_f)/Sp(2N_f)$  coset space contains  $(2N_f + 1)(N_f - 1)$  broken generators
- Coupling with  $Z'$  preserves DM stability

SU(N): 2 fermions in fundamental



Sp(N): 2 fermions in fundamental

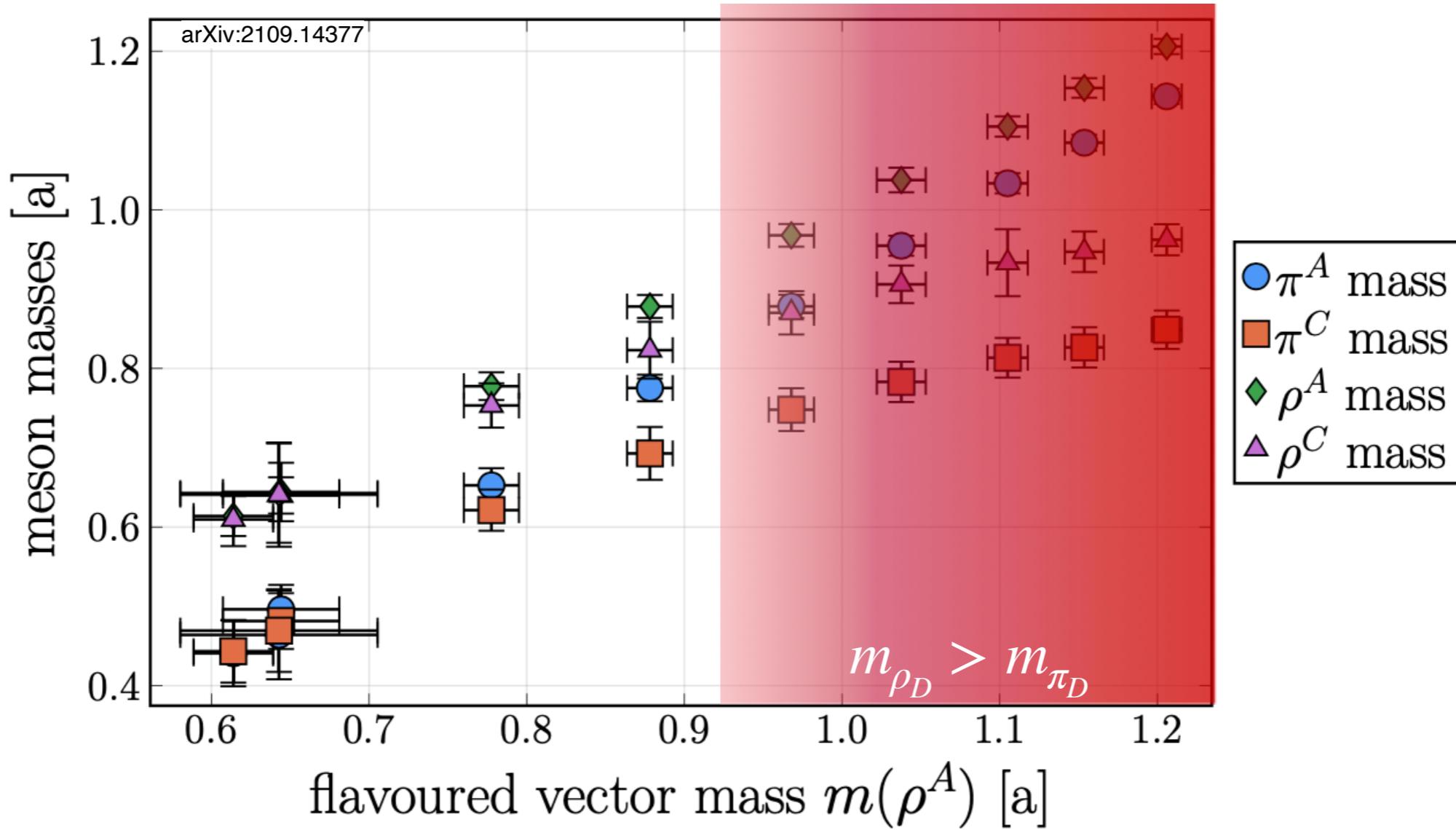


- $Z'$  charged for quarks +1, -1

# Lattice calculations $m_u \neq m_d$

S.K., A. Maas, S. Mee, M. Nikolic, J. Pradler, F. Zierler arXiv:2202.05191

( $\beta = 6.9$ ,  $m(\rho^{deg})/m(\pi^{deg}) = 1.41$ ): meson masses

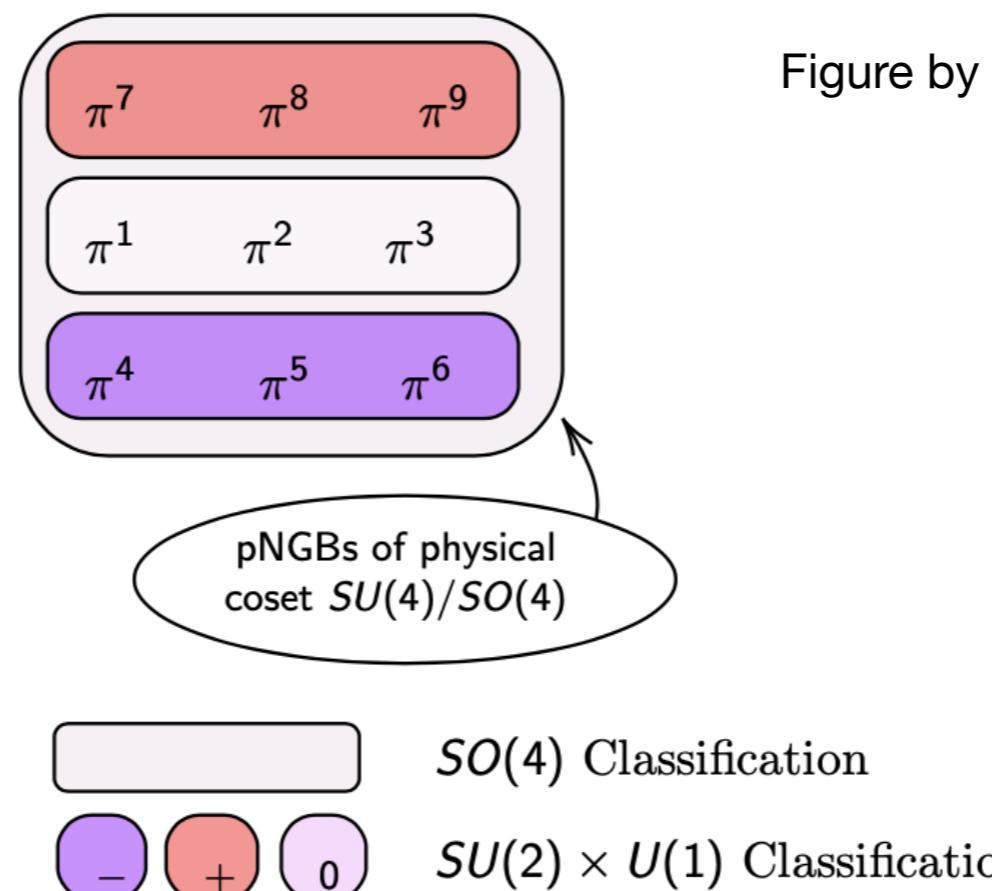


- For the first time ever, lattice calculations available for non-degenerate dark quark masses

# Number of pions can be very different - II

S.K., J. Pomper (In progress)

- SU(N) gauge groups: need three fermions in fundamental representation to get at least five pions
- Sp(N) gauge group: Two fermions in adjoint representation give nine pions  $SU(N_f)/SO(N_f)$  coset space contains  $\frac{1}{2}(N_f + 2)(N_f - 1)$  broken generators
- Coupling with  $Z'$  preserves DM stability



# Insights from UV dynamics

S.K., J. Pomper (In progress)

Witten, Nucl. Phys. B 223 (1983)

- Can not fix WZW by considering IR dynamics alone  $\pi_4(SU(4)/SO(4)) \neq 0$
- WZW can be written by considering detailed UV to IR anomaly relations (if anomaly is present in IR, it must be present in the UV  $\rightarrow$  anomaly equation  $\rightarrow$  solution is WZW term)

Chu, Ho, and Zumino, Nuclear Physics B 475 (1996)

Wess and Zumino, Physics Letters B 37 (1971)]

## Wess-Zumino effective action

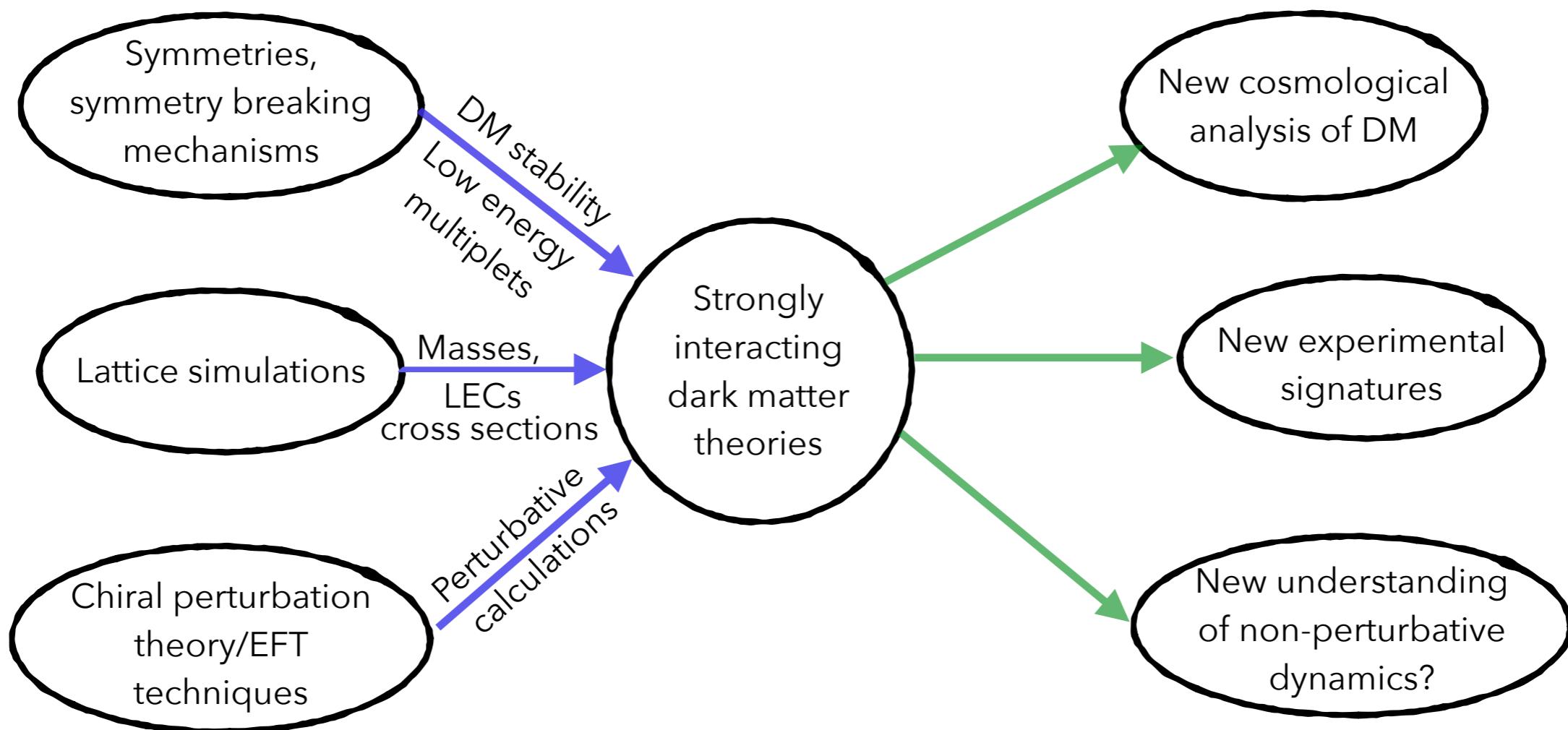
$$S_{WZ}[\xi = (\eta', \pi)] = \frac{D_C}{48\pi^2 f_\pi} \int_0^1 dt \int_{S^4} \text{Tr} \left\{ \xi ((U[t\xi])^{-1} dU[t\xi])^4 \right\}$$

$$\approx \frac{D_C}{250f_\pi\pi^2} \epsilon^{\mu\nu\sigma\rho} \int_{S^4} \text{Tr} \{ \pi \partial_\mu \pi \partial_\nu \pi \partial_\sigma \pi \partial_\rho \pi \}$$

# Fazit

in conclusion/on the balance

A systematic analysis of strongly interacting theories is possible



- Presented several examples containing dark baryon and dark pion dark matter candidates
- DM stability is ensured either via symmetries inbuilt in the theories or via careful choices of external charges
- Multiple relic density generation mechanisms can be engineered
- Portals lead to new interesting phenomenology

*Thanks for listening*

*Questions?*