

Why ALICE FoCal may be interesting: Some loose thoughts of a theorist

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Contents, list of possible problems

- ▶ Introduction
- ▶ Topics of potential interest
 - ▶ $pp \rightarrow pp\gamma$, different mechanisms with **Piotr Lebiedowicz**
 - ▶ $pp \rightarrow \gamma X$, saturation effects. k_t -factorization approach. with **Rafal Maciula**
 - ▶ $PbPb \rightarrow \gamma$, but more mechanisms than binary NN interactions.
 - ▶ $pPb \rightarrow \gamma$, better for saturation studies.
 - ▶ $\gamma\gamma \rightarrow \gamma\gamma$ scattering in $PbPb \rightarrow PbPb\gamma\gamma$. with **Mariola Klusek-Gawenda**
 - ▶ Production of charged leptons (e^\pm, μ^\pm) from semileptonic decays of charmed mesons in forward directions - testing forward charm production.
 - ▶ Production of J/ψ in forward directions.
 - ▶ Production of π^0 and η in FoCal.
- ▶ Results
- ▶ Conclusions and outlook

Introduction

- ▶ FOCAL can measure photons (main focus here)
- ▶ FOCAL can measure leptons (future studies)

$pp \rightarrow pp\gamma$, diffractive bremsstrahlung

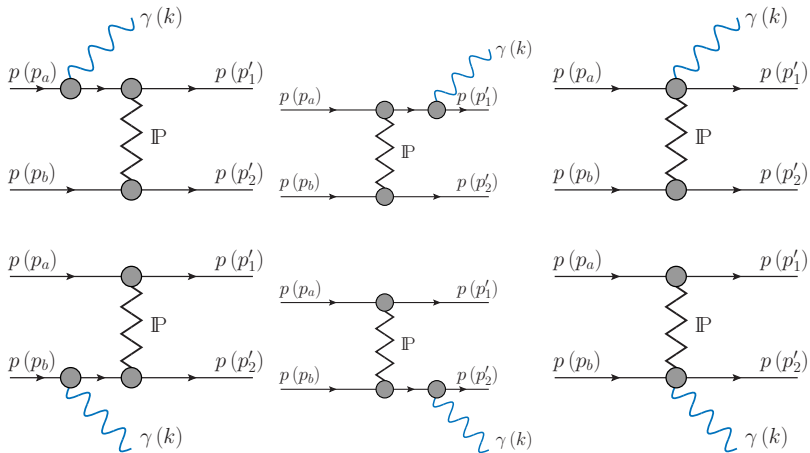


Figure: Lebedowicz, Nachtmann, Szczurek, arXiv:2206.03411

$pp \rightarrow pp\gamma$, photoproduction

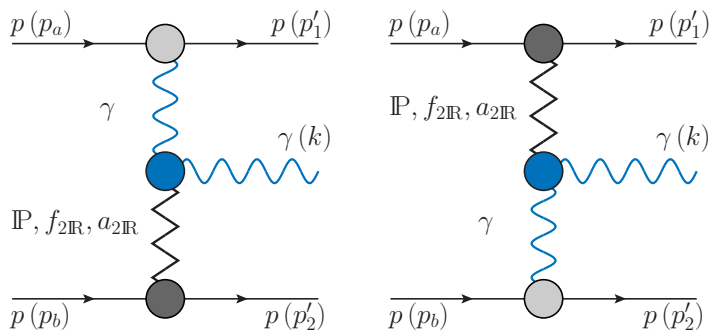
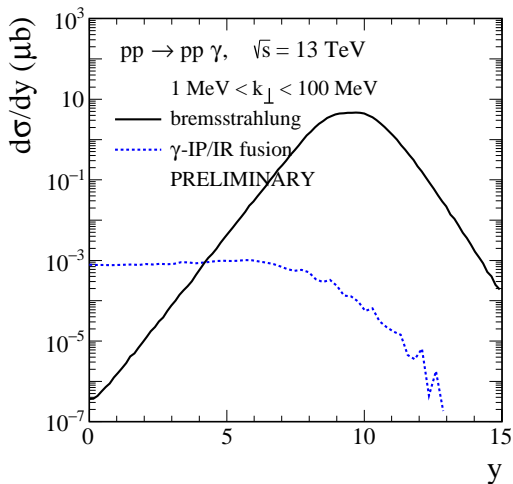


Figure: Diagrams for photoproduction.

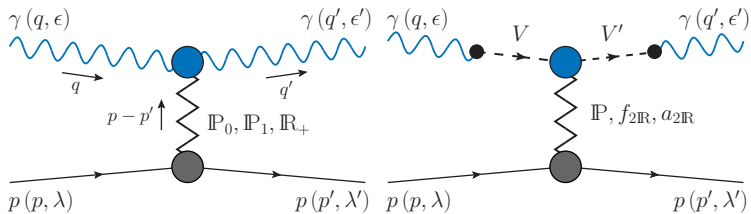
Lebiedowicz, Nachtmann, Szczurek, a paper in preparation

Window for photoproduction



There seem to be a window at midrapidity where the photoproduction may win with the bremsstrahlung

$$\gamma^* p \rightarrow \gamma p$$



Two tensor pomeron model, vertex coupling

In the tensor pomeron model two couplings for the $\gamma^*\gamma\mathbb{P}$ vertex:

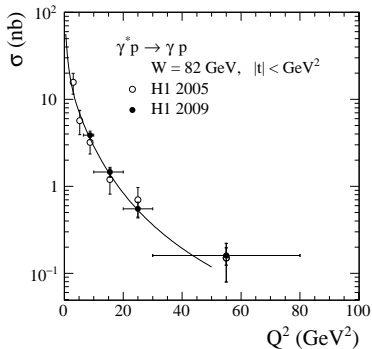
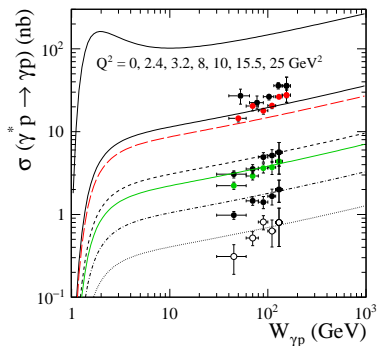
$$\Gamma_{\mu\nu\kappa\rho}(q', q) = 2a(q^2, q'^2, t)\Gamma_{\mu\nu\kappa\rho}^0(\dots) - b(q^2, q'^2, t)\Gamma_{\mu\nu\kappa\rho}^2(\dots) \quad (1)$$

Britzger, Ewerz, Glazov, Nachtmann, Schmitt fitted the coupling parameters. $a = a(Q^2)$, $b = b(Q^2)$ to DIS data
There two virtual photons with identical virtuality.

We (Lebiedowicz, Nachtmann, Szczurek) try to use the same model to DVCS.

Here one photon virtual, one photon real.

2TPM, $\gamma^* p \rightarrow \gamma p$

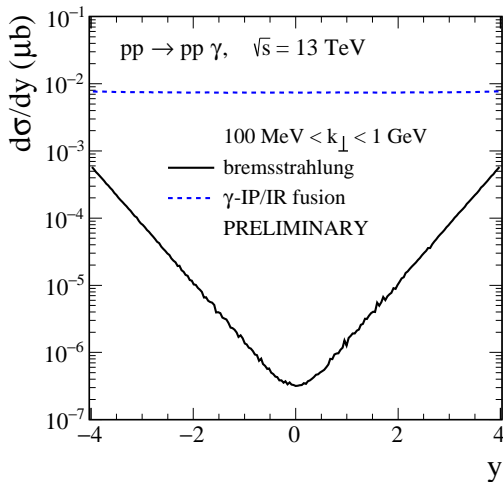


For pomeron exchange: $F(t) = \exp(-B/2t)$, $B = 4 \text{ GeV}^{-2}$

$$a/b = \sqrt{a/b(0)a/b(Q^2)}$$

quite reasonable description in a broad range of Q^2

2TPM, $pp \rightarrow pp\gamma$, general situation



There is a window where the photoproduction dominates over bremsstrahlung.

Dipole approach

In the color dipole approach the corresponding amplitude for the process can be written as:

$$\mathcal{M}_{\gamma^* p \rightarrow \gamma^* p}^{TT}(W; Q_1^2, Q_2^2) = \int d^2\rho dz \Psi_T(\rho, z, Q_1^2) \Psi_T^*(\rho, z, Q_2^2) \sigma(\rho, z, W, Q_1^2, Q_2^2). \quad (2)$$

$$\mathcal{M}_{\gamma^* p \rightarrow \gamma^* p}^{LL}(W; Q_1^2, Q_2^2) = \int d^2\rho dz \Psi_L(\rho, z, Q_1^2) \Psi_L^*(\rho, z, Q_2^2) \sigma(\rho, z, W, Q_1^2, Q_2^2). \quad (3)$$

Above Ψ_T / Ψ_L are so-called transverse/longitudinal virtual photon wave functions (see e.g. [Nikolaev-Zakharov](#)) and σ is color dipole - proton cross section.

Dipole approach

σ is color dipole - proton cross section is parametrized using GBW type of parametrization.

Consistent with their fit to DIS the crucial parameter is:

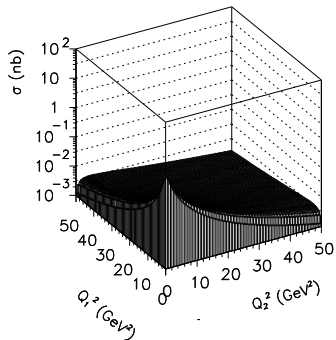
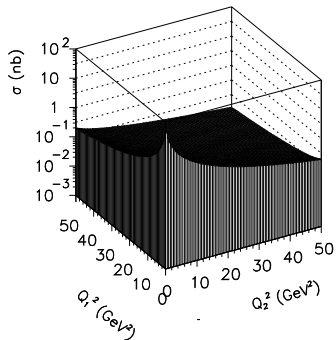
$$x_{eff} = \frac{Q^2 + M_{q\bar{q}}^2}{Q^2 + W^2}, \quad (4)$$

where $Q^2 = (Q_1^2 + Q_2^2)/2$ and

$$\sigma_{\gamma^* p \rightarrow \gamma^* p}(W; Q_1^2, Q_2^2) = |\mathcal{M}_{\gamma^* p \rightarrow \gamma^* p}|^2 / (16\pi B), \quad (5)$$

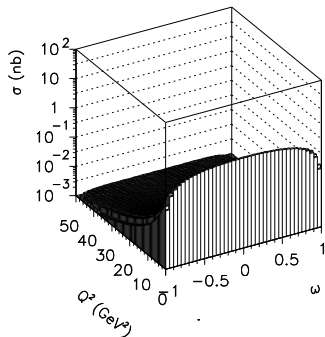
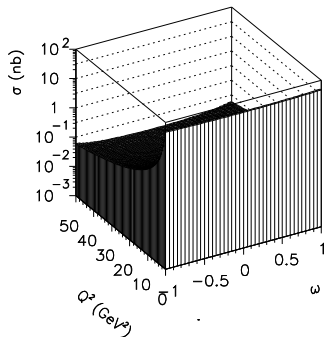
In general slope parameter B may depend on W and even Q^2 .
In the dipole approach I use $B = B(Q^2)$ proposed by Machado.

Dipole approach, $\gamma^* p \rightarrow \gamma^* p$



$LL < TT$

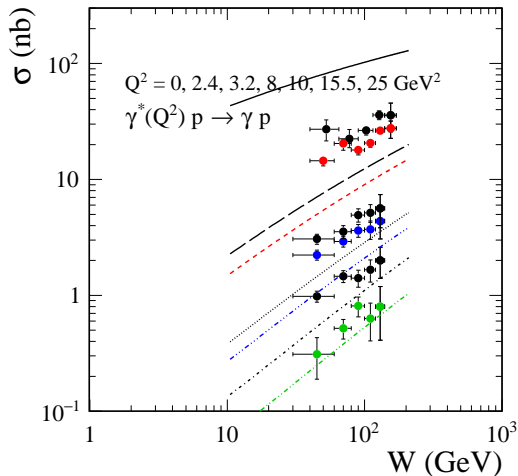
Dipole approach, $\gamma^* p \rightarrow \gamma^* p$



weak dependence on asymmetry parameter $\omega = \frac{Q_1^2 - Q_2^2}{Q_1^2 + Q_2^2}$

$$\overline{Q^2} = (Q_1^2 + Q_2^2)/2$$

Dipole approach, $\gamma^* p \rightarrow \gamma p$ vs data



Below the experimental data but:

- (a) no real part of the amplitude,
- (b) no skewedness enhancement factor,

$$pp \rightarrow pp\gamma$$

Here we first calculate:

(a) $M_{pp \rightarrow pp\gamma}^a$ for $\gamma\mathbb{P}$

(b) $M_{pp \rightarrow pp\gamma}^b$ for $\mathbb{P}\gamma$.

Then the total amplitude is obtained by adding the two components:

$$M_{pp \rightarrow pp\gamma} = M_{pp \rightarrow pp\gamma}^a + M_{pp \rightarrow pp\gamma}^b \quad (6)$$

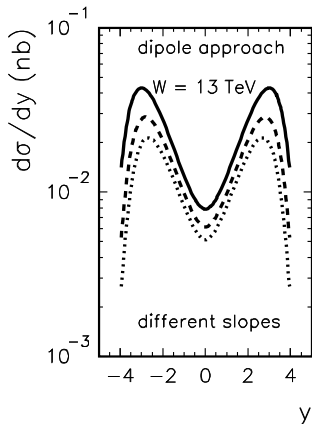
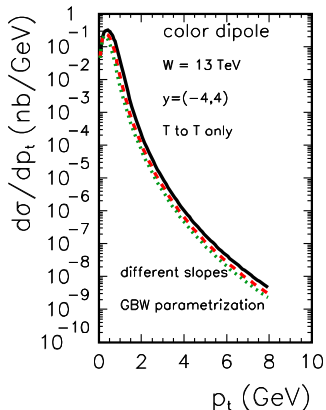
In the dipole picture the amplitude is calculated using $\gamma^*p \rightarrow \gamma p$ amplitude ([Schäfer-Szczurek 2007](#)).

Differential distributions for $pp \rightarrow pp\gamma$ are calculated as:

$$\frac{d\sigma}{dt_1 dt_2 dy d\phi} = \frac{1}{512\pi^2 s^2} \overline{|M|^2} \quad (7)$$

Careful treatment of conventions is required.

Dipole approach, B-slopes



The dipole model considered is missing **quarkish components** (is not complete)

Dipole approach, subsystem energies

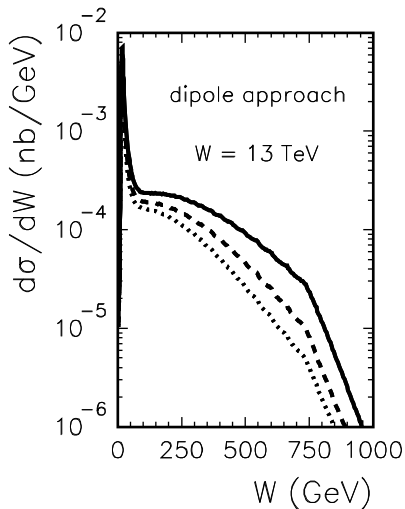
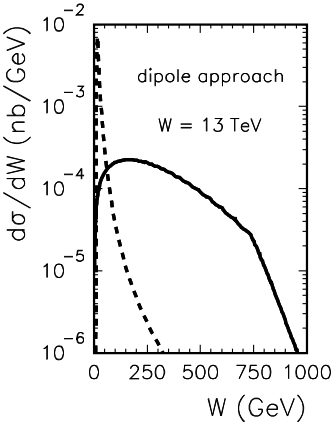
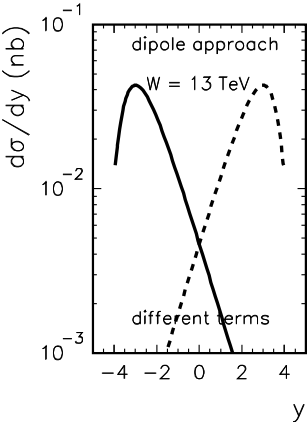


Figure: $B = 4, 6, 8 \text{ GeV}^{-2}$

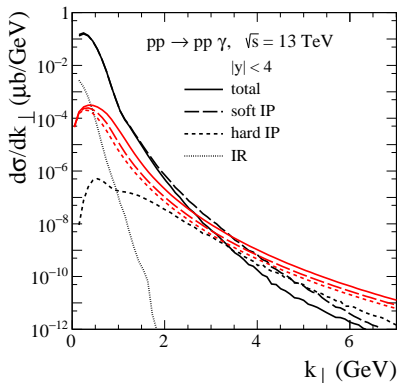
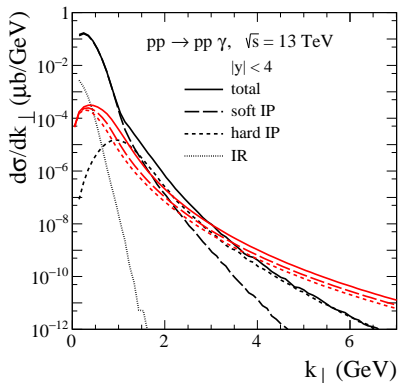
Dipole approach, terms



The two contributions are almost separated.

This is due to steep energy dependence in the dipole model.

2TPM versus color dipole

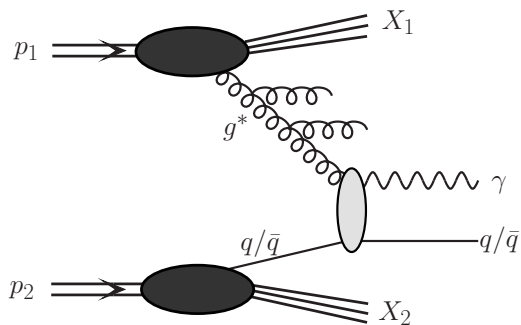


1) coupling constants from a fit to DIS data (BEGNS)

2) interpolation of coupling constants:

$$a/b = \sqrt{a/b(0)a/b(Q^2)}$$

$pp \rightarrow \gamma X$, process considered

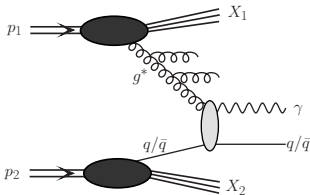


dominant mechanism for FOCAL
with Rafal Maciula

Hybrid high-energy factorization

The hybrid approach for far-forward production \Rightarrow

- ▶ combined collinear- and k_T -factorization
- ▶ used in many phenomenological studies
- ▶ the differential cross section for $g^*q \rightarrow \gamma q$ mechanism:

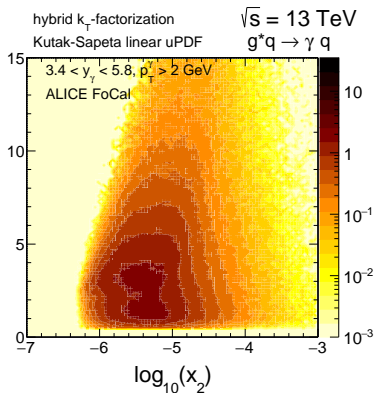
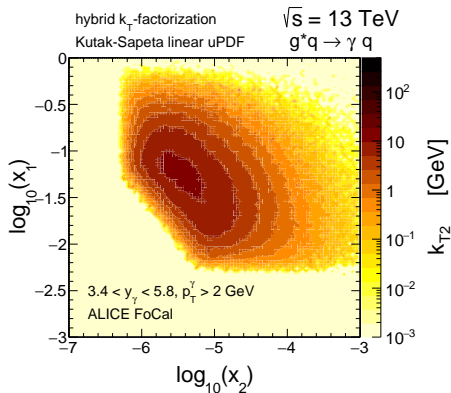


$$d\sigma_{pp \rightarrow \text{photon}}(g^*q \rightarrow \gamma q) = \sum_f \int dx_1 \int \frac{dx_2}{x_2} \int d^2 k_t$$

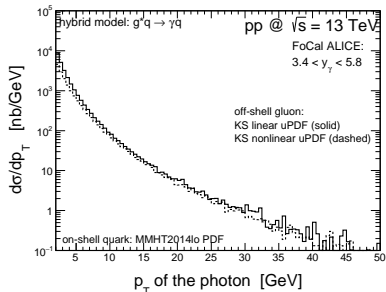
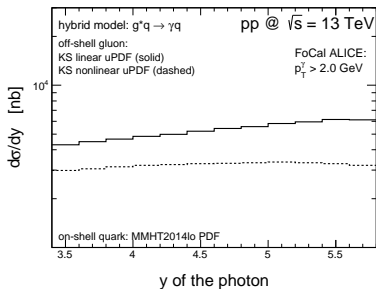
$$\times q_f(x_1, \mu^2) \cdot \mathcal{F}_g(x_2, k_t^2, \mu^2) \cdot d\hat{\sigma}_{g^*q \rightarrow \gamma q}$$

- ▶ $q_f(x_1, \mu^2) \Rightarrow$ collinear large- x quark/antiquark PDFs
we use MMHT2014lo, MMHT2014nlo, CT14nlo, JR14NLO08FF, NNPDF23
- ▶ $\mathcal{F}_g(x_2, k_t^2, \mu^2) \Rightarrow$ off-shell small- x gluon unintegrated PDFs (uPDFs)
we use KMR/MRW, KS linear/nonlinear, PB-NLO-set1, JH2013set1 CCFM models
- ▶ $d\hat{\sigma}_{g^*q \rightarrow \gamma q}$ is the hard partonic cross section obtained from a gauge invariant off-shell tree-level amplitudes (available in KaTie Monte Carlo generator)
- ▶ regularization needed at $p_T \rightarrow 0 \Rightarrow$ we use PYTHIA prescription:
$$F_{sup}(p_T) = \frac{p_T^2}{p_{T0}^2 + p_T^2}, \alpha_S(\mu_R^2 + p_{T0}^2), \text{ where } p_{T0} = 1.0 \text{ GeV (free parameter)}$$
- ▶ a derivation of the hybrid factorization from the dilute limit of the Color Glass Condensate approach can be found in the literature

$pp \rightarrow \gamma X$, kinematics



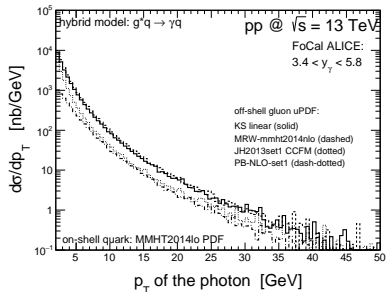
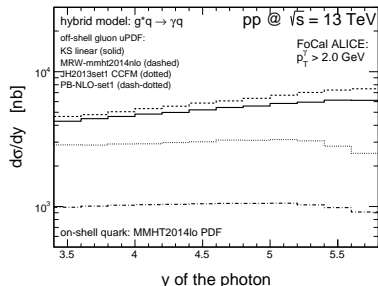
$pp \rightarrow \gamma X$, results



saturation vs no saturation

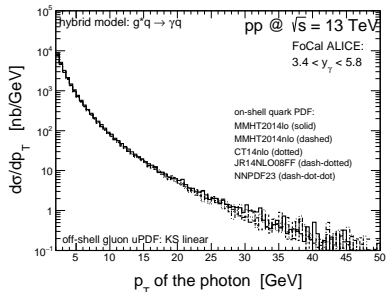
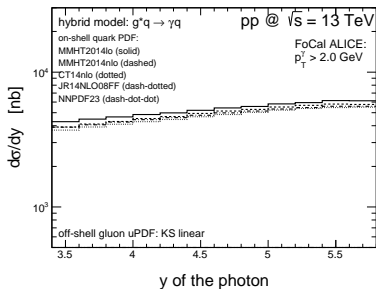
sizeable effect, especially at small transverse momenta

$pp \rightarrow \gamma X$, results



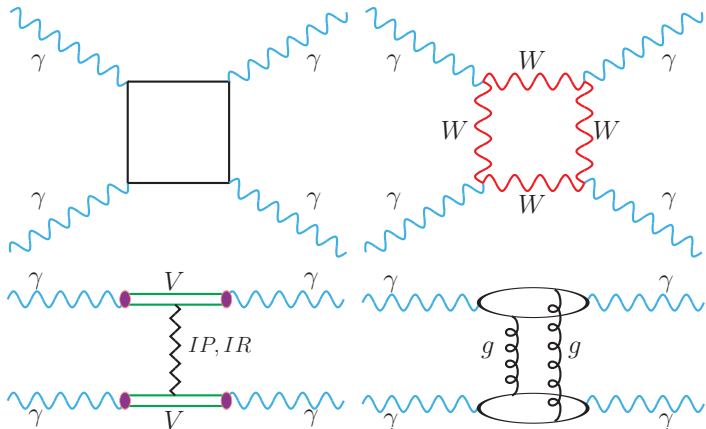
different UPDFs
sizeable effect

$pp \rightarrow \gamma X$, results

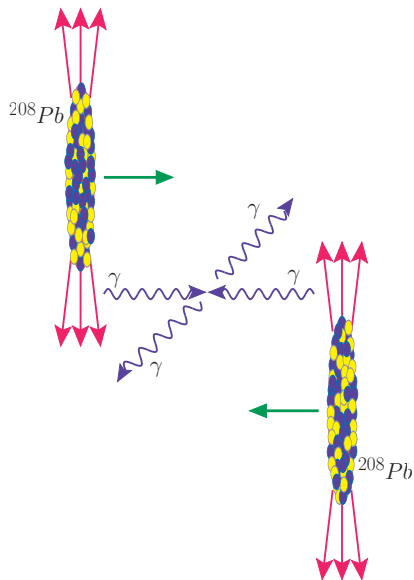


different PDFs
no large effect

Mechanisms of photon-photon scattering

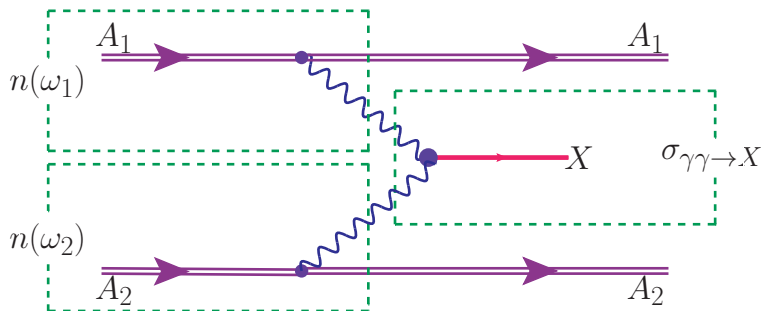


How to look at such a process ?



EM fields can be converted to photon fluxes

How to calculate cross section ?



Equivalent photon approximation (EPA)

EPA in the impact parameter space

Ultrapерipheral collisions: $b > R_{min} = R_1 + R_2 \approx 14$ fm

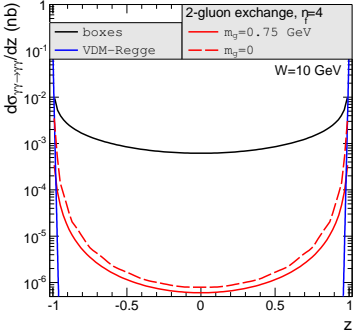
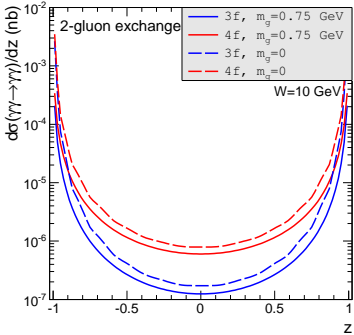
Consider reaction: $A_1 A_2 \rightarrow A_1 A_2 X_1 X_2$

$$\begin{aligned} \sigma_{A_1 A_2 \rightarrow A_1 A_2 X_1 X_2} &= \\ &= \int N(\omega_1, \mathbf{b}_1) N(\omega_2, \mathbf{b}_2) S_{abs}^2(\mathbf{b}) \\ &\times \sigma_{\gamma\gamma \rightarrow X_1 X_2}(W_{\gamma\gamma}) \\ &\times 2\pi b db d\bar{b}_x d\bar{b}_y \frac{W_{\gamma\gamma}}{2} dW_{\gamma\gamma} dY_{X_1 X_2} \end{aligned}$$

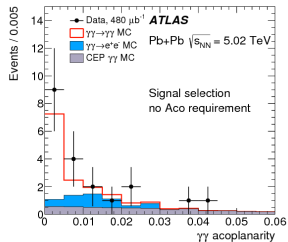
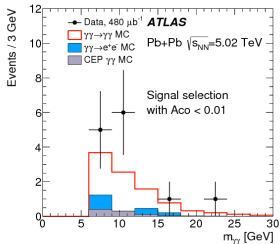
Ultrapерipheral condition contained in S_{abs}

Can be generalized to calculate distributions

Elementary cross section

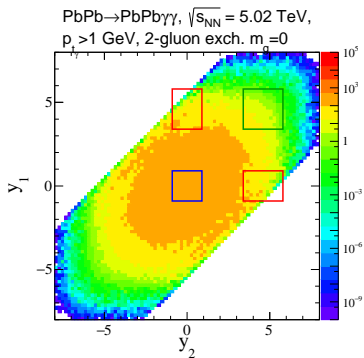
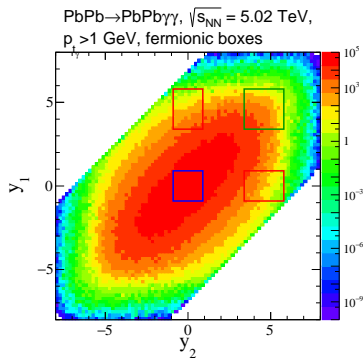


First observation of light-by-light scattering



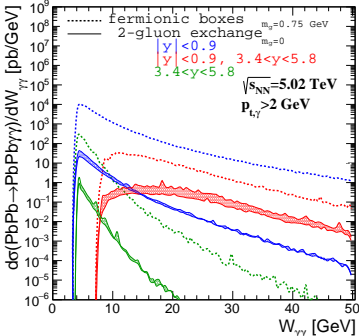
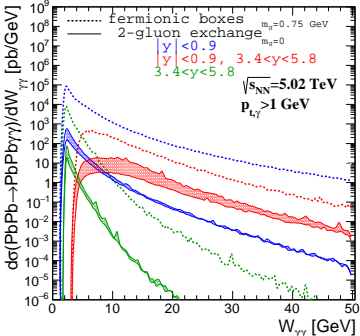
Our predictions vs ATLAS data.
Also CMS has similar data.

FoCal acceptance



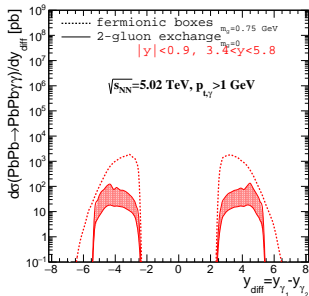
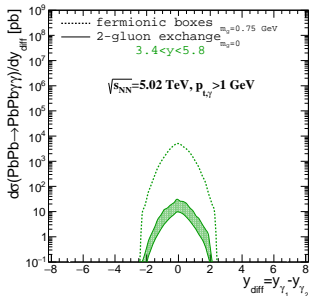
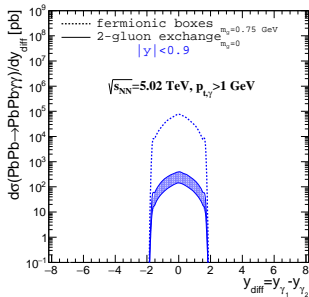
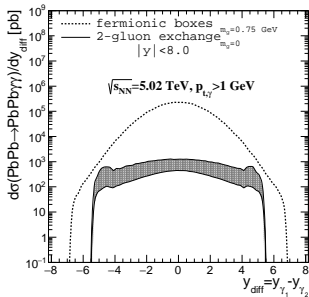
Shown are different possible combinations of measurements,
Photon can be measured in main detector and/or in FoCal.

Diphoton invariant mass distributions



$p_t > 1$ GeV (left) and $p_t > 2$ GeV (right)

y_{diff} distributions



Conclusions

- ▶ $pp \rightarrow pp\gamma$ at midrapidity never done, interesting. **Photoproduction mechanism** seems crucial.
- ▶ Two different approaches were used:
 - (a) **two tensor pomeron model**
 - (b) **color dipole model**The results are different.
We are trying to understand the situation.
Interesting to check experimentally.
- ▶ $pp \rightarrow \gamma X$ calculated in the k_t -factorization approach **with different unintegrated gluon distributions.**
- ▶ No dramatic saturation effect is predicted.
The differences between different UGDFs much bigger.
- ▶ $PbPb \rightarrow PbPb\gamma\gamma$ was calculated for the FOCAL kinematics.
Both boxes as well as two-gluon exchanges were included.
- ▶ There are some regions where **two-gluon exchanges** or **improved two-gluon exchanges** (resummation) may give visible contribution.
One photon in central detector, one in FOCAL - the most interesting case.

Outlook, questions

- ▶ Separation of decay photons ? How precise ?
- ▶ Calculate photon production in nucleus-nucleus collisions.
Plasma gives interesting contributions.
- ▶ Isospin effects in NN binary collisions.
- ▶ $\pi\pi \rightarrow \gamma M$ in A+A collisions in addition to binary collisions.
- ▶ How the leptons/dileptons measured in FOCAL depend on rapidity of charm.
- ▶ Calculation of J/ψ production in FOCAL
(k_t -factorization, color evaporation)
- ▶ Calculate forward dijet (minijet) production and combine it with hadronization to get π^0 distributions.