Abstract. We report the results of a calculation of the neutrino- and antineutrino-induced gamma-ray production cross section for oxygen target. Our analysis is focused on the kinematical region of neutrino energy larger than \( \sim 200 \text{ MeV} \), in which single-nucleon knockout is known to be the dominant reaction mechanism. The numerical results have been obtained using a realistic model of the target spectral function, extensively tested against electron-nucleus scattering data. We find that at neutrino energy 600 MeV the fraction of neutral-current interactions leading to emission of gamma-rays of energy larger than 6 MeV is \( \sim 41\% \), and that the contribution of the \( p_{3/2} \) state is overwhelming.

The observation of gamma rays originating from nuclear deexcitation can be exploited to identify neutral-current (NC) neutrino-nucleus interactions in a broad energy range. Following the pioneering studies of nuclear excitations by neutral weak currents of Refs. [1, 2], theoretical calculations of the cross section of gamma-ray production from NC neutrino-oxygen interactions have been carried out in the neutrino energy range \( E_\nu \sim 10–500 \text{ MeV} \) [3, 4, 5].

Neutrons, while providing \( \sim 50\% \) of NC events, do not emit Cherenkov light. As a consequence, the availability of an alternative signal allowing one to identify NC interactions is very important. Events with gamma rays of energy above the observational threshold of 5 MeV can be detected in a water Cherenkov detector, like Super-Kamiokande, and contribute up to \( \sim 5\% \) of the total event number [6, 7], independent of neutrino oscillations. Note that in water \( \sim 90\% \) (16 out of 18) of the NC interactions take place in oxygen.

At low energy, elastic scattering and inelastic excitation of discrete nuclear states provide the main contribution to the neutrino-nucleus cross section. However, at \( E_\nu \gtrsim 200 \text{ MeV} \) the cross section associated with these processes tends to saturate, and quasielastic (QE) nucleon knockout becomes the dominant reaction mechanism. If the residual nucleus is left in an excited state, these processes can also lead to gamma-ray emission.

In the QE regime, neutrino-nucleus scattering reduces to the incoherent sum of elementary scattering processes involving individual nucleons, the energy and momentum of which are distributed according to the target spectral function [8]. A schematic representation of NC QE neutrino-nucleus scattering is given in Fig. 1, where the dashed line represents the threshold for nucleon emission in the continuum.

In this paper, we discuss the emission of gamma rays arising from the decay of the residual nuclei of the reactions \( \nu + {}^{16}_8\text{O} \rightarrow \nu + p + {}^{15}_7\text{N}^* \), or \( \nu + {}^{16}_8\text{O} \rightarrow \nu + n + {}^{15}_8\text{O}^* \), the cross sections of
which have been computed using a realistic model of the oxygen spectral function. Note that the presented formalism applies also to antineutrino-induced \( \gamma \)-ray production.

In our approach, covered in detail in Ref. [9], the cross section of \( \gamma \)-ray production following a NC QE interaction, \( \sigma_\gamma \), is written in the form

\[
\sigma_\gamma \equiv \sigma(\nu + ^{16}_8\text{O} \to \nu + X_\alpha + N) \, \text{Br}(X_\alpha \to \gamma + Y), \tag{1}
\]

where \( N \) is the knocked out nucleon, \( X_\alpha \) denotes the residual nucleus in the state \( \alpha \), and \( Y \) is the system resulting from the electromagnetic decay of \( X_\alpha \), e.g. \( ^{15}_7\text{N}, ^{14}_7\text{N} + n, \) or \( ^{14}_6\text{C} + p \) [10, 11]. The energy spectrum of the states of the residual nuclei is schematically illustrated in Fig. 2. The branching ratios \( \text{Br}(X_\alpha \to \gamma + Y) \) have been taken from Ref. [16].

The NC QE cross section, \( \sigma(\nu + ^{16}_8\text{O} \to \nu + X_\alpha + N) \), has been calculated within the approach discussed in Ref. [15] for the case of charged-current interactions. It may be expressed as

\[
\frac{d\sigma_{\nu A}}{d\Omega dE'_{\nu}} = \sum_{N = p, n} \int d^3p \, dEP_N(p, E) \frac{M}{E_N} \frac{d\sigma_{\nu N}}{d\Omega dE'_{\nu}}, \tag{2}
\]

where \( E_N = \sqrt{M^2 + p^2} \), \( M \) being the nucleon mass, \( d\sigma_{\nu N}/d\Omega dE'_{\nu} \) denotes the elementary neutrino-nucleon cross section and the spectral function \( P_N(p, E) \) yields the probability of removing a nucleon of momentum \( p \) from the target leaving the residual nucleus with energy \( E + E_0 - M \), \( E_0 \) being the target ground-state energy.

According to the shell model, nuclear dynamics can be described by a mean field. In the simplest implementation of this model, protons in the \( ^{16}_8\text{O} \) nucleus occupy three single-particle states, \( 1p_1/2, 1p_3/2, \) and \( 1s_1/2 \), with removal energy 12.1, 18.4, and \( \sim 42 \) MeV, respectively [12, 13, 14]. The neutron levels exhibit the same pattern, see Fig. 1, but are more deeply bound by 3.54 MeV [11].

As a consequence of a mean field dynamics, knock out of a target nucleon leaves the residual system in a bound state, and the spectral function can be conveniently written in the form

\[
P_N(p, E) = \sum_{\alpha \in \{F\}} n_\alpha |\phi_\alpha(p)|^2 f_\alpha(E - E_\alpha), \tag{3}
\]

where \( \phi_\alpha(p) \) is the momentum-space wave function associated with the \( \alpha \)-th shell-model state and the sum is extended to all occupied states belonging to the Fermi sea \( \{F\} \). The occupation
probability \( n_\alpha \leq 1 \) and the (unit-normalized) function \( f_\alpha (E - E_\alpha) \), describing the energy width of the \( \alpha \)-th state, account for the effects of nucleon-nucleon (NN) correlations, not included in the mean field picture. In the absence of correlations, \( n_\alpha \to 1 \) and \( f_\alpha (E - E_\alpha) \to \delta(E - E_\alpha) \).

A realistic model of the proton spectral function of oxygen has been obtained within the local density approximation (LDA), combining the experimental data of Ref. [12] with the results of theoretical calculations of the correlation contribution in uniform nuclear matter at different densities [15, 17]. The results reported in Ref. [15] show that the LDA spectral function provides an accurate description of the inclusive electron-oxygen cross sections at beam energies around 1 GeV. In addition, it predicts a nucleon momentum distribution in agreement with that obtained from the data of Ref. [18].

As pointed out in Ref. [19], nucleon-knockout experiments measure spectroscopic strengths, not occupation probabilities. Spectroscopic strengths are given by the area below the sharp peaks observed in the missing-energy spectra, corresponding to knockout of a nucleon occupying one of the shell-model states, corrected to take into account final-state interactions. On the other hand, occupation probabilities include contributions corresponding to larger removal energy, arising from mixing of the one-hole state with more complex final states [19].

The \( p_{1/2}, p_{3/2} \) and \( s_{1/2} \) spectroscopic strengths have been computed by integrating the oxygen spectral function of Refs. [15, 17] over the energy ranges \( 11.0 \leq E \leq 14.0 \) MeV, \( 17.25 \leq E \leq 22.75 \) MeV, and \( 22.75 \leq E \leq 62.25 \) MeV, respectively. Dividing these numbers by the degeneracy of the shell-model states, one obtains the quantities \( S_\alpha \) listed in Table 1. The same spectroscopic strengths have been used for protons and neutrons.

The branching ratios \( \text{Br}(X_\alpha \to \gamma + Y) \), necessary to calculate the cross section \( \sigma_\gamma \) according

\[
\begin{array}{|c|c|c|}
\hline
\alpha & p_{1/2} & p_{3/2} & s_{1/2} \\
\hline
S_\alpha & 0.632 & 0.703 & 0.422 \\
\text{Br}(X_\alpha \to \gamma + Y) & 0\% & 100\% & 16 \pm 1\% \\
\hline
\end{array}
\]

Table 1. Spectroscopic strengths of the \( ^{16}\text{O} \) hole states and their branching ratios for deexcitation by the \( E_\gamma > 6 \) MeV photon emission.

Figure 3. Cross section for \( \gamma \)-ray production following NC QE interaction of neutrino (solid line) and antineutrino (long-dashed line) compared to the NC QE cross section of neutrino (dotted line) and antineutrino (short-dashed line). Only the photons of energy larger that 6 MeV are considered.
to Eq. (1), are collected in Table 1 [16]. In the case of the \(p_{1/2}\)-proton (neutron) knockout, the residual nucleus is \(^{15}\text{N}\) \((^{15}\text{O})\) produced in its ground state. Hence, no \(\gamma\)-rays are produced. As the \(p_{3/2}\)-proton (neutron) hole lies below the nucleon-emission threshold, 10.21 MeV (7.30 MeV), it always deexcites through photon emission with half-life 0.146±0.008 fs (less than 1.74 fs) [11]. When a proton (neutron) is knocked out from the deepest \(s_{1/2}\) shell, the excitation energy is high enough for many deexcitation channels to open, of which only two, \(^{12}\text{C} + p\) and \(^{12}\text{N} + n\) \((^{14}\text{C} + p\) and \(^{14}\text{C} + \alpha\)), yield photons of energy higher than 6 MeV [16] (see Fig. 2).

In Fig. 3 our results for the neutrino- and antineutrino-induced \(\gamma\)-ray production cross section are compared to the neutrino and antineutrino NC QE cross sections. The error bands show the uncertainties arising from the determination of the spectroscopic strengths (5.4%), the treatment of Pauli blocking (1%), and the branching ratio of the \(s_{1/2}\) state (1%). The \(\sigma_{\gamma}\)’s dependence on neutrino energy is very similar, although not identical, to that of the NC QE cross section. The discrepancy arises from difference between the average removal energy associated with the whole spectral function and the energy of the \(p_{3/2}\) shell, yielding the overwhelming contribution to \(\sigma_{\gamma}\). The neutrino-induced \(\gamma\)-production cross section reaches its maximum at \(E_{\nu} \sim 1.9\) GeV and is slowly decreasing at larger energies. On the other hand, the corresponding antineutrino cross section is an increasing function of \(E_{\bar{\nu}}\).

In conclusion, we have computed the neutrino- and antineutrino-induced \(\gamma\)-ray production cross section for oxygen target, focussing on the kinematical region in which single-nucleon knockout dominates. Considering photons of energy larger than 6 MeV, we find that the \(p_{3/2}\) state provides the overwhelming contribution, and that the ratio \(\sigma_{\gamma}/\sigma_{\text{NC}}\), exhibiting a significant energy-dependence at \(E_{\nu} \lesssim 1\) GeV, is \(\sim 41\%\) at \(E_{\nu} = 600\) MeV. Our results, obtained using a realistic model of the target spectral function, provide an accurate estimate of a signal that can be exploited to identify neutral-current events in water-Cherenkov detectors.

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