# **Computational Tools and Methods**

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RTU Course in "Accelerator Technologies" - April 2022

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# Purpose of this course

In these two lessons, we will outline the fundamental concepts in scientific computing and guide the novice through the multitude of tools available. We will describe the main tools and explain which tool should be used for a specific purpose, dispelling common misconceptions, and suggest good practices.

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We will exclusively refer to free and open-source software running on Linux or other Unix-like operating systems. Also, we will unveil powerful shell commands that can speed up simulations, facilitate data processing, and in short, increase your scientific throughput.

### Some references

- "Numerical Recipes: The Art of Scientific Computing", W. Press, S. Teukolsky, W. Vetterling, and B. Flannery, 1992 (2nd edition) 2007 (3rd edition)
- 2. Abramowitz and Stegun, "Handbook of Mathematical Functions with Formulas", 1964
- Olver, F., Lozier, D., Boisvert, R. and Clark, C., "The NIST Handbook of Mathematical Functions", 2010
- Donald Knuth, "The Art of Computer programming", 1968 (the book is still incomplete)
- Gradshteyn and Ryzhik, "Table of Integrals, Series, and Products", Academic Press Inc;
   édition (27 octobre 2014)
- 6. Zyla, P. A., et al., "Review of Particle Physics", Oxford University Press.





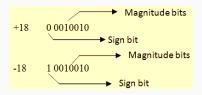






### **Integers**

Int, or integer, is a whole number, positive or negative, without decimals. In binary format



- Typically, an integer occupies four bytes, or 32 bits.
- The possible range for 32-bit integers is

$$-2^{31} < X < 2^{31} - 1$$

(from -2,147,483,648 to 2,147,483,647).

### Integer types

• In compiled languages such as C and C++, specific types exist for better control:

Data Type		Size	Size in bytes	Signed range
[un signed]	char	8 bits	1	-128 to 127
[un signed]	short int	16 bits	2	-32768 to 32767
[un signed]	int	32 bits	4	-2147483648 to 2147483647
[un signed]	long int	32 bits	4	-2147483648 to 2147483647
[un signed]	long long int	64 bits	8	$-2^{63}$ to $2^{63}-1$

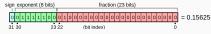
Arithmetic between numbers in integer representation is exact, if the answer is not
outside the range of integers that can be represented.

### Real numbers

Real numbers use a floating-point representation IEEE-754

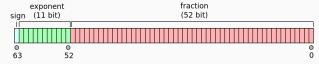
value = 
$$(-1)^{\text{sign}} \times 1$$
.fraction  $\times 2^{\text{exponent}}$ 

• Single-precision floating point representation (32 bits)



The C/C++ type is float.

• Double-precision floating point representation (64 bits)



The C/C++ type is double.

### Real numbers

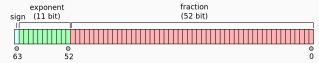
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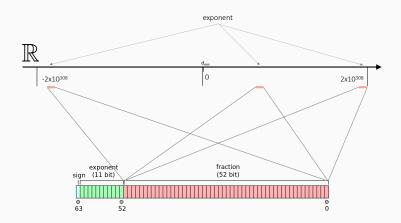
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The C/C++ type is double.

Note: Some CPUs internally store floating point numbers in even higher precision: 80-bit in extended precision, and 128-bit in quadruple precision. In C++ quad. precision may be specified using long double. 7/47 A. Latina - Numerical Tools - RTU Course in "Accelerator Technologies" - April 2022

# Range of double-precision numbers



7-digit precision in base 10. min  $\bullet$  52 bits of mantissa correspond to about 15-digit precision in base 10. In single precision, there are just

- Double-precision numbers as integers are exact within the range  $\pm 2^{53}$  ( $\approx \pm 10^{16}$ ).
- The smallest possible number that can be represented is  $d_{\rm min}=2^{-1074}\approx 4.94\times 10^{-324}$

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# Machine epsilon, $\varepsilon_m$

• The machine epsilon, or accuracy,  $\varepsilon_m$ , is the gap between 1 and the next representable double. The smallest double number such that:

$$1.0 + \varepsilon_m \neq 1.0$$

• For double precision

$$\varepsilon_m = 2^{-52} \approx 2 \cdot 10^{-16},$$

For single precision

$$\varepsilon_m = 2^{-23} \approx 3 \cdot 10^{-8}$$
.

• It is important to understand that  $\varepsilon_m$  is not the smallest floating-point number that can be represented on a machine.

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**Note:** The smallest number,  $d_{\min}$ , depends on how many bits there are in the exponent.  $\varepsilon_m$  depends on how many bits there are in the mantissa.

# **Special numbers**

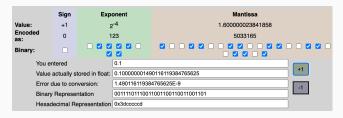
IEEE-754 floating-point types may support special values:

- infinity (positive and negative)
- the **negative zero**, -0.0. It compares equal to the positive zero, but is meaningful in some arithmetic operations, e.g. 1.0/0.0 == INFINITY, but 1.0/-0.0 == -INFINITY)
- Not-a-number (NaN), which does not compare equal with anything (including itself)

### Round-off error

The *round-off error*, also called *rounding error*, is the difference between the exact result and the result obtained using finite-precision, rounded arithmetic.

As an example of round-off error, see the representation of the number 0.1



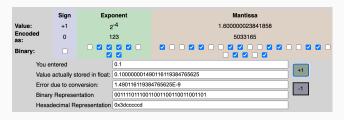
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If, in the course of obtaining a calculated value, one performs N such arithmetic operations, one might end up having a total round-off error on the order of  $\sqrt{N}\epsilon_m$  (when lucky)

(Note: The square root comes from a random-walk, as the round-off errors come in randomly up or down.)

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The golden rule: try to reduce the number of operations required to perform a calculation. 11/47 A. Latina - Numerical Tools - RTU Course in "Accelerator Technologies" - April 2022

# Round-off error: example

```
Example

set format = ".30f"; ! after the 17th digit, it's noise

a = 0.7; !0.7 -> 0.699999999999999955591079014994
! one or two iterations? may not be portable...

while (a < 0.8) {!0.8 -> 0.80000000000000044408920985006
a = a + 0.1; !0.1 -> 0.1000000000000005551115123126
print a;
}
```

→ Most decimal numbers don't have exact binary representations.

# Overflow and underflow, cancellation error

The **Overflow** occurs when an operation attempts to create a numeric value that is outside of the range that can be represented with a given number of digits – either higher than the maximum or lower than the minimum representable value.

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Example: Take for example

$$1e100 + 1 - 1e100 = ?$$

The result is zero... which is simply wrong. This is called "catastrophic" cancellation.

# **Catastrophic cancellations**

Catastrophic cancellation can occur in the evaluation of expressions like:

1. Algebraic binomials, e.g.

$$x^{2} - y^{2}$$

can incur in underflow errors if  $y^2 \ll x^2$  (when  $y^2/x^2 < \varepsilon_m$ ). This expression is more accurately evaluated as

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$$(x+y)(x-y)$$

- 2. Summations of many numbers of very large different magnitude. There are two solutions:
  - 1. Sort the numbers by abs(magnitude) and sum from the smallest to the largest
  - 2. Kahan summation algorithm

# Catastrophic cancellations /II

3. Quadratic formula:

$$r_{1} = \frac{-b + \sqrt{b^{2} - 4ac}}{2a}$$

$$r_{2} = \frac{-b - \sqrt{b^{2} - 4ac}}{2a}$$

cancellation can occur.

# Catastrophic cancellations /II

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The solution is to rewrite  $r_1$  and  $r_2$  to avoid cancellation:

• 
$$r_1$$
: if  $b^2 \gg ac$  and  $b > 0$ , use  $r_1 = \frac{2c}{-b - \sqrt{b^2 - 4ac}}$ 

• 
$$r_2$$
: if  $b^2 \gg ac$  and  $b < 0$ , use  $r_2 = \frac{2c}{-b + \sqrt{b^2 - 4ac}}$ 

Internally, all functions are implemented using Taylor expansions:

$$\log(x) = (x-1) - \frac{(x-1)^2}{2} + \frac{(x-1)^3}{3} - \frac{(x-1)^4}{4} + \dots$$

which makes the function incur in cancellation whenever  $x < \varepsilon_m$ .

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### log1p(x)

To overcome this problem, the C standard library, as well as Octave and Python, provide the function log1p, which implements

log1p(x) = log(1+x) = x - 
$$\frac{x^2}{2}$$
 +  $\frac{x^3}{3}$  -  $\frac{x^4}{4}$  + ...

this is numerically stable. So, whenever the argument of a logarithm is in the form 1 + x, use log1p.

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Functions like:  $1 - \cos(x)$ ,  $1 - \cosh(x)$ , require a similar approach.

## hypot(a,b)

provides a numerically stable implementation of

$$c = \sqrt{a^2 + b^2}$$

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hypot(a,b), which is part of the C standard library, computes:

$$c = m \cdot \sqrt{1 + (M/m)^2}$$

where  $m = \min(|a|, |b|), M = \max(|a|, |b|).$ 

# Implementation of functions

#### Sin cardinal

Also the implementation of functions requires attention. Take for example the function "sin cardinal",

$$\operatorname{sinc}(x) = \begin{cases} 1 & \text{for } x = 0\\ \frac{\sin(x)}{x} & \text{otherwise.} \end{cases}$$

Numerical instabilities might appear due to the division between two nearly-zero numbers. A robust implementation comes from a careful consideration of this function.

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If we look at the right-hand side, we can appreciate the fact that in this form, when x is small, the numerical instability simply disappears. The final result will differ from zero if and only if

$$\left|-\frac{x^2}{6}\right| < \varepsilon_m,$$

If x is made explicit, a robust implementation should return 1 when:

$$|x| < \sqrt{6 \, \varepsilon_m}$$
.

### **Truncation error**

### **Finite differentiation**

Imagine that you have a procedure which computes a function f(x), and now you want to compute its derivative f'(x). Easy, right? The definition of the derivative,

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

practically suggests the program: Pick a small value h; evaluate f(x + h) and f(x), finally apply the above equation.

Applied uncritically, the above procedure is almost guaranteed to produce inaccurate results.

There are two sources of error in equation: the **truncation error** and the **round-off error**.

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Let's focus on the truncation error now, we know that

$$f(x+h) = f(x) + hf'(x) + \frac{1}{2}h^2f''(x) + \dots$$

(Taylor expansion), therefore

$$\frac{f(x+h)-f(x)}{h}=f'+\frac{1}{2}hf''+\dots$$

Then, when we approximate f' as in the above equation, we make a **truncation error**:

$$\varepsilon_t = \frac{1}{2}hf'' + \ldots = O(h)$$

In this case, the truncation error is linearly proportional to h. Higher-order formulations of the instandaring time regive. smaller carror "Accelerator Technologies" - April 2022

# Example of finite difference formulæ

• First derivative to first order (forward difference):

$$f'(x) = \frac{f(x+h) - f(x)}{h} + O(h)$$

• First derivative to second order (centered difference):

$$f'(x) = \frac{f(x+h) - f(x-h)}{2h} + O(h^2)$$

• First derivative to fourth order (centered difference):

$$f'(x) = \frac{-f_{x+2h} + 8f_{x+h} - 8f_{x-h} + f_{x-2h}}{12h} + O(h^4)$$

• Second derivative to second order (centered difference):

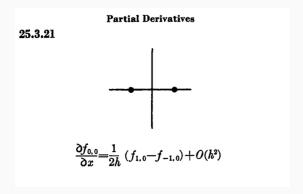
$$f''(x) = \frac{f_{x+h} - 2f_x + f_{x-h}}{h^2} + O(h^2)$$

• Second derivative to fourth order (centered difference):

$$f''(x) = \frac{-f_{x+2h} + 16f_{x+h} - 30f_x + 16f_{x-h} - f_{x-2h}}{12h^2} + O(h^4)$$

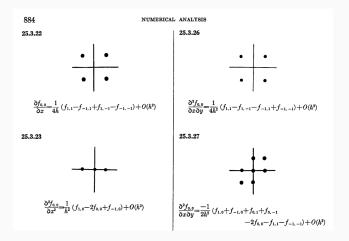
# Finite difference formulæ

# Abramowitz and Stegun, page 883 and following



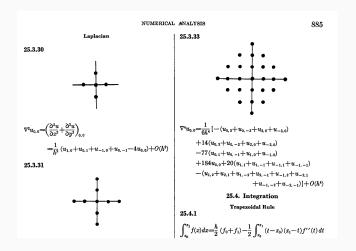
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# **Numerical integration**

Newton-Cotes formulas of the closed type, for functions sampled at equidistant points.

For  $\{i \in \mathbb{N} \mid 0 \le i \le n\}$ , let  $x_i = a + i \frac{b-a}{n} = a + i h$ , and  $f_i = f(x_i)$ : then the integral can be approximated with a sum

$$\int_{a}^{b} f(x) dx \approx \sum_{i=0}^{n} w_{i} f(x_{i})$$

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$$\int_a^b f(x) dx \approx \sum_{i=0}^n w_i f(x_i)$$

where:

n	Step size h	Common name	Formula	Error
1	b — a	Trapezoidal rule	$\frac{h}{2}\left(f_0+f_1\right)$	$-\frac{1}{12}h^3f^{(2)}(\xi)$
2	<u>b—a</u>	Simpson's rule	$\frac{h}{3}(f_0+4f_1+f_2)$	$-\frac{1}{90}h^5f^{(4)}(\xi)$
3	<u>b−a</u> 3	Simpson's 3/8 rule	$\frac{3h}{8}\left(f_0+3f_1+3f_2+f_3\right)$	$-\frac{3}{80}h^5f^{(4)}(\xi)$
4	<u>b−a</u>	Boole's rule	$\frac{2h}{45} \left(7f_0 + 32f_1 + 12f_2 + 32f_3 + 7f_4\right)$	$-\frac{8}{945}h^7f^{(6)}(\xi)$

# Numerical integration /II

For a function that is known analytically but cannot be integrated, one can use the Gauss-Legendre integration.

$$\int_{a}^{b} f(x) dx \approx \sum_{i=0}^{n} w_{i} f(x_{i})$$

where:

- ullet the function is defined in the interval [-1,1]
- $w_i = \frac{2}{(1-x_i)^2 [P'_n(x_i)]^2}$
- $P_n(x)$  are the Legendre polynomials, normalised such that  $P_n(1) = 1$
- $x_i$  is the *i*-th root of  $P_n$

# Numerical integration /III

Abramowitz and Stegun suggest a generalisation to address different cases:

$$\int_{a}^{b} \omega(x) f(x) dx \approx \sum_{i=0}^{n} w_{i} f(x_{i})$$

#### where:

- $\omega(x)$  is positive weight function
- $\bullet$   $w_i$  depend on the method used
- $x_i$  is the *i*-th root of  $P_n$

Interval	$\omega(x)$	Orthogonal polynomials	A & S
[-1, 1]	1	1 Legendre polynomials	
(-1, 1)	$(1-x)^{lpha}(1+x)^{eta},  lpha, eta > -1$	Jacobi polynomials	25.4.33 ( $\beta = 0$ )
(-1, 1)	$\frac{1}{\sqrt{1-x^2}}$	Chebyshev polynomials (first kind)	25.4.38
[-1, 1]	$\sqrt{1-x^2}$	Chebyshev polynomials (second kind)	25.4.40
[0, ∞)	$e^{-x}$	Laguerre polynomials	25.4.45
[0, ∞)	$x^{lpha}e^{-x},  lpha > -1$	Generalized Laguerre polynomials	
$(-\infty, \infty)$	$e^{-x^2}$	Hermite polynomials	25.4.46

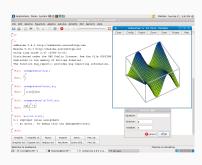
#### For more details see A & S.

# **Exact and arbitrary-precision numbers**

In cases where double-, extended- or even quadruple-precision are not enough, there exist a couple of solutions to achieve higher precision and in some cases even exact results.

• Symbolic calculation is the "holy grail" of exact calculations.

Programs such as Maxima, Mathematica<sup>©</sup>, or Maple<sup>©</sup>, know the rules of math and represents data as symbols rather rounded numbers. It is free software released under the terms of the GNU General Public License (GPL). An excellent front end for Maxima is wxMaxima



• Arbitrary-precision arithmetic can be achieved using dedicated libraries that can handle arbitrary, user-defined precision such as GMP, the GNU Multiple Precision Arithmetic Library for the C and C++ programming languages.



# **Tools: Python vs Octave**

**Python** is described as "A clear and powerful object-oriented programming language, comparable to Perl, Ruby, Scheme, or Java". Python is a general purpose programming language created by Guido Van Rossum.

Libraries such as numpy, matplotlib, pandas offer many functionalities that make it similar to MATLAB and Octave.

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Octave is detailed as "A programming language for scientific computing". It is software featuring a high-level programming language, primarily intended for numerical computations. Octave helps in solving linear and nonlinear problems numerically, and for performing other numerical experiments using a language that is mostly compatible with MATLAB.

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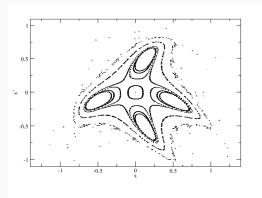
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https://www.octave.org

https://octave.sourceforge.io

### **Tools: Octave**

## Example: impact of nonlinear elements on linear optics



$$\begin{pmatrix} x_{n+1} \\ x'_{n+1} \end{pmatrix} = \begin{pmatrix} \cos(2\pi Q) & \sin(2\pi Q) \\ -\sin(2\pi Q) & \cos(2\pi Q) \end{pmatrix} \begin{pmatrix} x_n \\ x'_n + x_n^2 \end{pmatrix}$$

- Q=0.2516
- linear motion near center (circles)
- More and more square
- Non-linear tuneshift
- Islands
- · Limit of stability
- Dynamic Aperture
- Crucial if strong quads and chromaticity correction in s.r. light sources
- many non-linearities in LHC due to s.c. magnet and finite manufacturing tolerances

### **Tools: Octave simulation**

```
m SextupolarKick.m
                                                                                     >>
      Open Recent Revert Save Print
                                     Undo Redo Cut Copy Paste Search
% N = number of particles
% 0 = tune
% R = transfer matrix
% X = gaussian bunch
% lattice
0 = 0.2516;
phi = 2*pi*0;
R = [ cos(phi) sin(phi); -sin(phi) cos(phi)]; % 1-turn map
% a bunch with N = 10000 particles
N = 10000;
0 = zeros(1,N);
X = 0.2 * randn(2,N);
% simulate 1000 turns with a sexupolar kick each turn
for i=1:1000
 X = X + [0; X(1,:).^2]; % add a sextupolar kick
                          % track through the ring
 X = R * X;
end
% plot
f = figure;
plot(X(1,:), X(2,:), '.');
axis(Γ -1 1 -1 1 ]);
xlabel('x [mm]');
vlabel('x'' [mrad]');
% save the plot as a PDF file
print(f, 'SextupolarKick.pdf', '-dpdf', '-FTimes New Roman:16');
-: **- SextupolarKick.m All (19.28) (MATLAB Fill)
```

#### Maxima and wxMaxima

Maxima is a computer algebra system with a long history. It is based on a 1982 version of Macsyma.

It is written in Common Lisp and runs on all POSIX platforms such as macOS, Unix, BSD, and Linux, as well as under Microsoft Windows and Android.

It is free software released under the terms of the GNU General Public License (GPL). It is a valid alternative to commercial alternatives, and offers some advantage.

An excellent front end for Maxima is wxMaxima.



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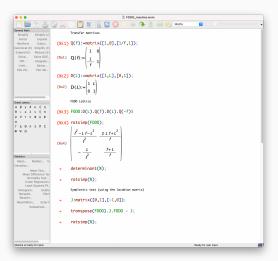
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## Octave and Python

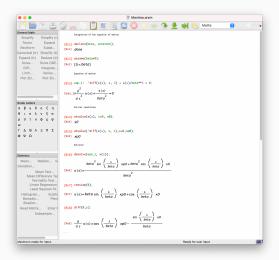
Symbolic computations can also be performed within Octave and Python. Dedicated packages add the possibility to perform basic symbolic computations, including common Computer Algebra System tools such as algebraic operations, calculus, equation solving, Fourier and Laplace transforms, variable precision arithmetic and other features, in scripts.



#### FODO cell in wxMaxima



#### A 1D harmonic oscillator with wxMaxima



# The Octave "symbolic" package

```
1 % Load the symbolic package
2 pkg load symbolic
3
4 % This is just a formula to start with, have fun and change it if you want to.
5 f = @(x) x.^2 + 3*x - 1 + 5*x.*sin(x);

6
7 % These next lines take the Anonymous function into a symbolic formula
8 syms x;
9 ff = f(x);
10
10 % Now we can calculate the derivative of the function
12 ffd = diff(ff, x);
13
14 % and convert it back to an Anonymous function
15 df = function_handle(ffd)
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```

## The Python "sympy" library

```
1 >>> from sympy import *
2 >>> x = symbols('x')
3 >>> simplify(sin(x)**2 + cos(x)**2)
4 1
```

#### units

The ability to evaluate complex expressions involving <u>units makes many computations easy</u> to do, and the checking for compatibility of <u>units guards against errors</u> frequently made in scientific calculations. Units is a conversion program, but also calculator with units.

 Example 1: average beam power, bunch charge 300 pC, 15 GeV energy, 50 Hz repetition rate:

```
1 $ units -v

2 You have: 300 pC * 15 GV * 50 Hz

3 You want: W

4 300 pC * 15 GV * 50 Hz = 225 W

5 300 pC * 15 GV * 50 Hz = (1 / 0.0044444444444444) W
```

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 Example 1: average beam power, bunch charge 300 pC, 15 GeV energy, 50 Hz repetition rate:

• Example 2: beam size at the interaction point of an electron collider,

```
\sigma=\sqrt{eta^\star\cdotarepsilon_{
m geometric}}, with eta^\star=1\,{
m mm}, arepsilon_{
m normalized}=5\,{
m nm}, E=1.5\,{
m TeV}:
```

#### bc

It's a programmable shell calculator that supports arbitrary-precision numbers

```
| $ bc

2 bc 1.06

3 Copyright 1991-1994, 1997, 1998, 2000 Free Software Foundation, Inc.

4 This is free software with ABSOLUTELY NO WARRANTY.

5 For details type 'warranty'.

6 scale=1

7 sqrt(2)

8 1.4

9 scale=40

10 sqrt(2)

11 1.412135623730950488016887242096980785696
```

The variable "scale" allows one to select the total number of decimal digits after the decimal

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#### gnuplot

It's a portable command-line-driven graphing utility originally created to allow scientists and students to visualise mathematical functions and data interactively. It has grown to support many non-interactive uses. It implements excellent fitting routines.

## Use of named pipes for interprocess communication (of FIFOs)

Let's see how to create and use a named pipe:

```
s mkfifo mypipe

s prw-r----. 1 myself staff 0 Jan 31 13:59 mypipe
```

Notice the special file type designation of "p" and the file length of zero. You can write to a named pipe by redirecting output to it and the length will still be zero.

### Use of named pipes for interprocess communication (of FIFOs)

Let's see how to create and use a named pipe:

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2 $ ls -1 mypipe
3 prw-r----. 1 myself staff 0 Jan 31 13:59 mypipe
```

Notice the special file type designation of "p" and the file length of zero. You can write to a named pipe by redirecting output to it and the length will still be zero.

```
s echo "Can you read this?" > mypipe
s prw-r----. 1 myself staff 0 Jan 31 13:59 mypipe
```

So far, so good, but hit return and nothing much happens. While it might not be obvious, your text has entered into the pipe, but you're still peeking into the input end of it. You or someone else may be sitting at the output end and be ready to read the data that's being poured into the pipe, now waiting for it to be read.

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```
1 $ cat mypipe
2 Can you read this?
```

Once read, the contents of the pipe are gone.

# A word about the choice of units...

The International System (SI) is not suitable for accelerator physics. The beam size isn't of the order of meters, the force shouldn't be expressed in Newtons.

### Example:

Let's compute the force exerted by one of the LHC superconductive dipoles, in Newton:

```
1 $ units -v
2 You have: c * e * 8.5 T
3 You want: N
4 c * e * 8.5 T = 4.082724005684724e-10 N
5 c * e * 8.5 T = (1 / 2449345090.698306) N
```

# A word about the choice of units...

The International System (SI) is not suitable for accelerator physics. The beam size isn't of the order of meters, the force shouldn't be expressed in Newtons.

### Example:

Let's compute the force exerted by one of the LHC superconductive dipoles, in Newton:

#### Example of "practical" units:

quantity	units	quantity	units	quantity	units
position	mm	energy	MeV	momentum	MeV/c
angles	mrad	time	mm/c	force	MeV/m

In fact.

#### c \* e \* 8.5 T = 2548.235893 MeV/m

## A word about data files...

#### An example of questionable choice:

```
$> tail ASTRA distr at cathode.ini
 1.0700E-04 4.5476E-04 0.0000E+00 4.2084E+02 -7.2666E+02 5.8264E+02 -1.3444E-03 -6.1600E-06
-9.7655E-04 -7.9998E-04 0.0000E+00 7.0706E+02 -8.1272E+01 7.2854E+02
                                                                      1.0902E-03 -6.1600E-06
                                                                                                  -1
-2.4085E-04 1.9553E-04
                         0.0000E+00 -4.0670E+02 -2.4789E+02 9.7767E+02 -6.3584E-04 -6.1600E-06
                                                                                                  -1
 -1.4163E-04 -3.7871E-04
                         0.0000E+00 -9.3474E+02 -4.2633E+02
                                                          3.4603E+02
                                                                      2.2061E-04 -6.1600E-06
                                                                                                  -1
            1.1817E-05
                         0.0000E+00 -9.4943E+02 -2.6439E+02 3.1839E+02 -1.8247E-03 -6.1600E-06
 -2.8669E-04
                                                                                                  -1
  9.1701E-04 -3.8281E-04 0.0000E+00 -7.7430E+02
                                               4.2284E+02 1.2272E+02 -1.5230E-03 -6.1600E-06
 2.2139E-04 1.0007E-04 0.0000E+00 2.8189E+02 1.0234E+02 4.5108E+02 -1.7515E-03 -6.1600E-06
                                                                                                  -1
  4.4429E-04 -8.8646E-05
                         0.0000E+00 -2.0888E+02 3.8810E+02 7.3747E+02 -9.6443E-05 -6.1600E-06
                                                                                                  -1
 -4.6858E-04 4.6416E-04
                         0.0000E+00 1.8117E+02
                                              7.8001E+02 4.9974E+02 -1.5143E-03 -6.1600E-06
                                                                                                  -1
  2.8663E-04 4.0295E-04
                         0.0000E+00 -4.4856E+02 -5.0962E+02 3.8406E+02
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                                                                                                  -1
$>
```

In C, use:

printf("%.15g\n", x);

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                                                                                                  -1
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                                                                                                  -1
$>
```

In C, use:

In C++, use:

```
std::cout << std::setprecision(15) << x << std::endl;</pre>
```

You want to look for bit-wise preservation of the information.

#### **Parallelism**

Parallelism can be achieved in different ways, depending on the problem:

 Embarrassingly parallel problems. Embarrassingly parallel problems are those where a large number of tasks need to be performed, with each single task being completely independent of the others. Examples: imperfections studies; tracking of single-particles.

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- 2. MPI "massively parallel" problems

MPI, the Message Passing Interface, is just a protocol, to design codes that run on clusters of computers.

There exist several open-source implementations of MPI, which fostered the development of a parallel software industry, and encouraged development of portable and scalable large-scale parallel applications. Two well-established MPI implementations are "Open MPI" and "MPICH".

```
#include <npi.h>
#include <stdio.h>
4 int main()
      // Initialize the MPI environment
      MPI Init(NULL, NULL):
     // Get the number of processes
      int world size:
     MPI_Comm_size(MPI_COMM_WORLD, &world_size);
     // Get the rank of the process
      int world rank:
     MPI_Comm_rank(MPI_COMM_WORLD, &world_rank);
     // Get the name of the processor
     char processor_name[MPI_MAX_PROCESSOR_NAME];
      int name_len;
     MPI Get processor name(processor name, &name len);
     // Print off a hello world message
     printf("Hello world from processor Xs, rank Xd out of Xd processors\n",
             processor name, world rank, world size);
     // Finalize the MPI environment.
      MPI Finalize():
```

#### **Parallelism**

3. OpenMP. Multi-core parallelism. Hacking an existing code to make it parallel.

OpenMP is a programming interface that supports multi-platform shared-memory multiprocessing programming in C, C++, and Fortran. In simpler words, it makes programs run in parallel on multi-cores computers, exploiting the multi-threaded architecture of modern CPUs.

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```
int main()
{
  int a[100000];

    #pragma comp parallel for
    for (int i = 0; i < 100000; i++) {
        a[i] = 2 + i;
    }

    return 0;
}</pre>
```

#### 4 C++ threads

```
1 // thread example
 2 #include <iostream>
                            // std..cont
                            // std::thread
 3 #include <thread>
 5 void foo()
    // do stuff...
10 void bar(int x)
    // do stuff...
13 }
15 int main()
16 {
    std::thread first (foo);
                                 // spawn new thread that calls foo()
    std::thread second (bar,0); // spawn new thread that calls bar(0)
    std::cout << "main, foo and bar now execute concurrently...\n";
   // synchronize threads:
    first.join();
                                  // pauses until first finishes
    second.join();
                                 // pauses until second finishes
    std::cout << "foo and bar completed.\n";
```

# High-performance computing in C/C++

#### C scientific library

 The GNU Scientific Library. The GNU Scientific Library (GSL) is an excellent numerical library written in C. It provides more than 1000 mathematical routines such as random number generators, special functions, least-squares fitting, etc. Uses BLAS and LAPACK for linear algebra functionality

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Standard template library (STD), provides useful container classes, eg.
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 std::map<K,T>. Efficient algorithms, like std::qsort, are provided in <algorithm>.

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- Eigen, another C++ template library for linear algebra. Includes numerical solvers and related algorithms

### Advanced programming

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### **GPU Programming**

OpenCL (Open Computing Language) is a framework for writing programs that execute
across heterogeneous platforms consisting of central processing units (CPUs), graphics
processing units (GPUs), digital signal processors (DSPs), field-programmable gate arrays
(FPGAs) and other processors or hardware accelerators. OpenCL is an open standard
maintained by the non-profit technology consortium Khronos Group. Conformant
implementations are available from Altera, AMD, Apple, ARM, Creative, IBM,
Imagination, Intel, Nvidia, Qualcomm, Samsung, Vivante, Xilinx, and ZiiLABS.

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  Imagination, Intel, Nvidia, Qualcomm, Samsung, Vivante, Xilinx, and ZiiLABS.
- CUDA (an acronym for Compute Unified Device Architecture) is a proprietary model created by Nvidia to program Nvidia GPUs for general purpose processing. The CUDA platform is a software layer that gives direct access to the GPU's virtual instruction set and parallel computational elements, for the execution of compute kernels.

### **Accelerator physics codes**

#### MAD-X

MAD-X is a CERN code used world-wide, with a long history going back to the 80's in the field of high energy beam physics (i.e. MAD8, MAD9, MADX). It is an all-in-one application with its own scripting language used to design, simulate and optimise particle accelerators: lattice description, machine survey, single particles 6D tracking, optics modelling, beam simulation & analysis, machine optimisation, errors handling, orbit correction, aperture margin and emittance equilibrium. [rings, optics, tracking]

#### MAD-NG

MAD-NG is a recent CERN code aiming to replace MAD-X. It is an all-in-one application using Lua as a scripting language, to design, simulate and optimise particle accelerators: lattice description, machine survey, single particles 6D tracking, optics modelling, and other functionalities similar to MAD-X are available. [rings, optics, tracking]

#### SixTrack

CERN's single-particle 6D symplectic tracking code optimised for long term tracking in high energy rings. Uses its own description language. [rings, tracking]

#### **PyHEADTAIL**

Python macro-particle simulation code library developed at CERN for modelling collective effects beam dynamics in circular accelerators. Interfaced with Python. [rings, tracking, collective effects]

### Accelerator physics codes /II

#### **PLACET**

The "Program for Linear Accelerator Correction and Efficiency Tests", is a code developed at CERN that simulates the dynamics of a beam in the main accelerating or decelerating part of a linac (CLIC) in the presence of wakefields. In includes also the emission of incoherent and coherent synchrotron radiation. Interfaced with Tcl, Octave, and Python. [linacs, tracking, collective effects, imperfections]

### **ELEGANT**

The "ELEctron Generation ANd Tracking", it's a code developed at the Argonne National Laboratory (ANL, USA) that can generate particle distributions, track them, and perform optics calculations. Uses its own description language. [linacs & rings, tracking, optics]

## Accelerator physics codes /III

#### **ASTRA**

"A Space Charge Tracking Algorithm" is a tracking code developed at DESY (Hamburg, Germany), can simulate injectors and track in field maps. Uses its own description language. [injectors, tracking, space charge]

#### RF-Track

RF-Track was developed at CERN, to simulate beams of particles with arbitrary energy, mass, and charge, even mixed, in field maps and conventional elements. It can simulate space-charge, short- and long-range wakefields, electron cooling, inverse Compton scattering. Interfaced with Python and Octave. [injectors & linacs, tracking, collective effects, design, imperfections]

And many others, but some aren't maintained or they are not open-source and free...

The end.

Thank you for your attention.

Any questions?

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