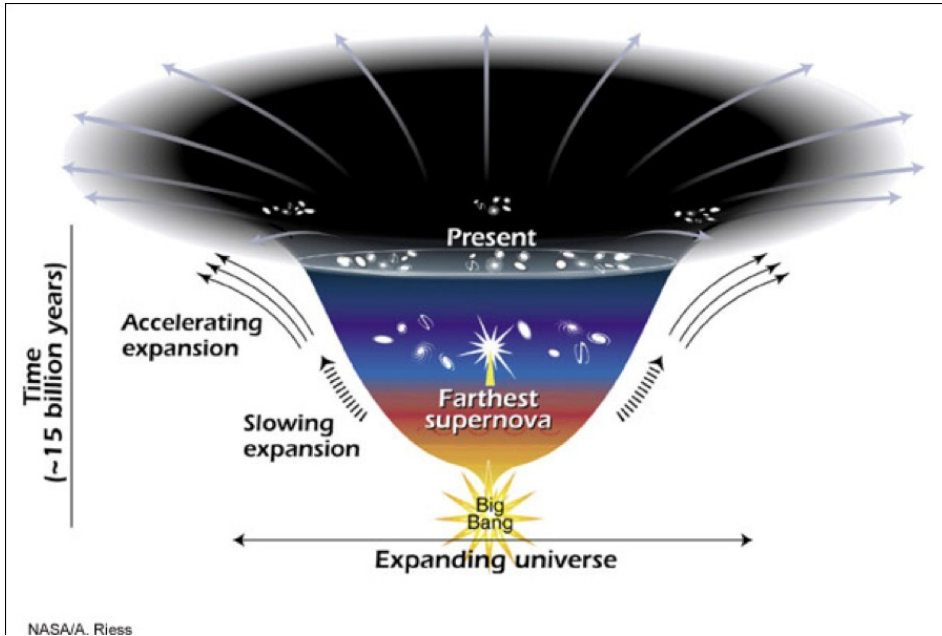
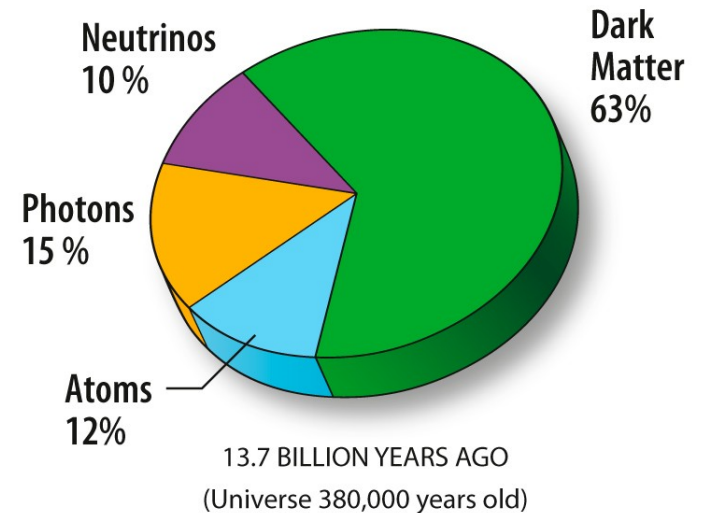
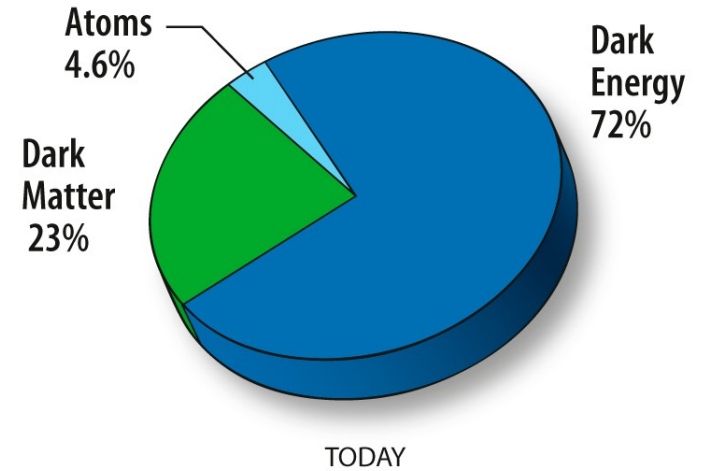


**Answering Cosmological Questions with  
Galaxy Surveys  
Will Percival (University of Portsmouth)**

# The standard “model” for cosmology based on energy



$$\frac{H^2}{H_0^2} = \Omega_R a^{-4} + \Omega_M a^{-3} + \Omega_k a^{-2} + \Omega_\Lambda$$



## An alternative model based on gravity

- Can acceleration be driven by GR modifications rather than a new component of stress-energy?
- Changes to the laws of gravitation affect the relationship between the geometry (metric) and density (matter) fields
- assume scalar degrees of freedom in the gravitational field
- two physically relevant scalar functions (or potentials)

$$ds^2 = a^2 \left[ -(1 + 2\psi)d\tau^2 + (1 - 2\phi)d\bar{x}^2 \right]$$

- conformal Newtonian gauge
- time-time (time-like) metric potential  $\Psi$
- space-space (space-like) metric potential  $\Phi$
- scale factor  $a$
- conformal time  $\tau$
- spatial coordinate  $x$

## Modified Gravity Models

- assume dominant stress-energy component can be modeled as a non-relativistic perfect fluid
  - no pressure or anisotropic stress terms
- assume conservation of stress-energy
  - continuity equation
  - Euler equation
- left with two gravitational field equations to close the system
  - no consensus in field on how to parameterize!

$$-k^2 \frac{A\phi + B\psi}{A + B} = 4\pi G\mu(k, a)\bar{\rho}_m\Delta_m$$

$$\phi = \eta(k, a)\psi$$

(e.g. Daniel et al. 2010; 1002.1962)

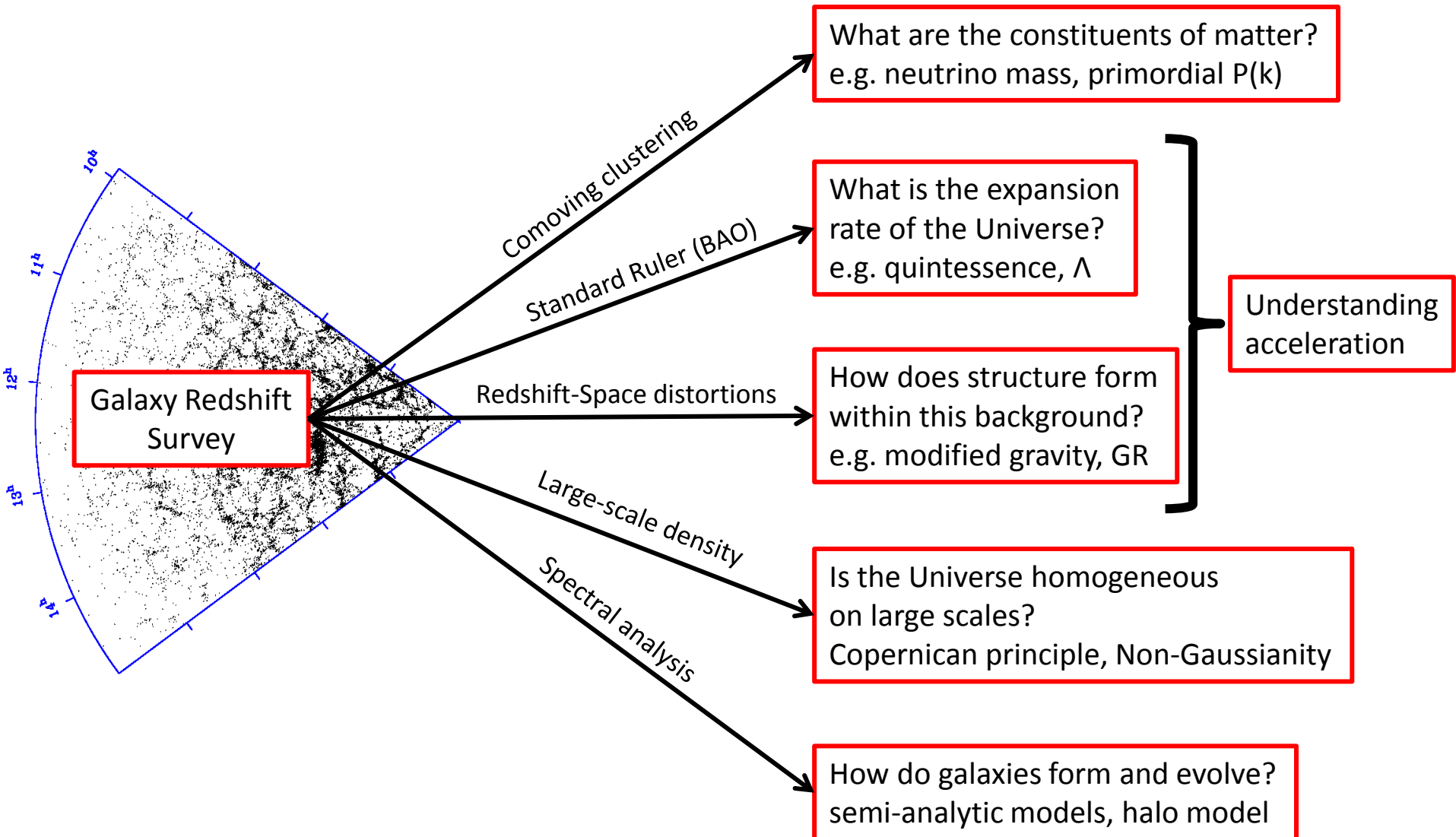
$$-k^2(\phi + \psi) = 8\pi G_N a^2 \bar{\rho}_m \Delta_m \times \mathcal{G}(k, a)$$

$$-k^2\psi = 4\pi G_N a^2 \bar{\rho}_m \Delta_m \times \mathcal{V}(k, a)$$

(e.g. Linder 2011; arXiv:1103.0282)

- need two functions: expansion and growth rates

# Galaxy Surveys can constrain model choices

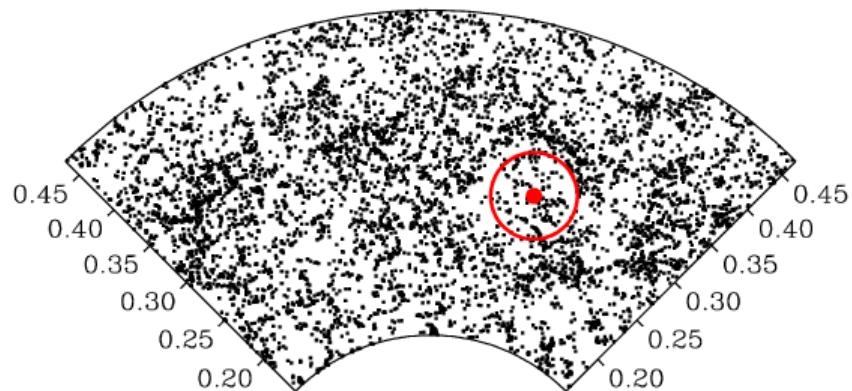
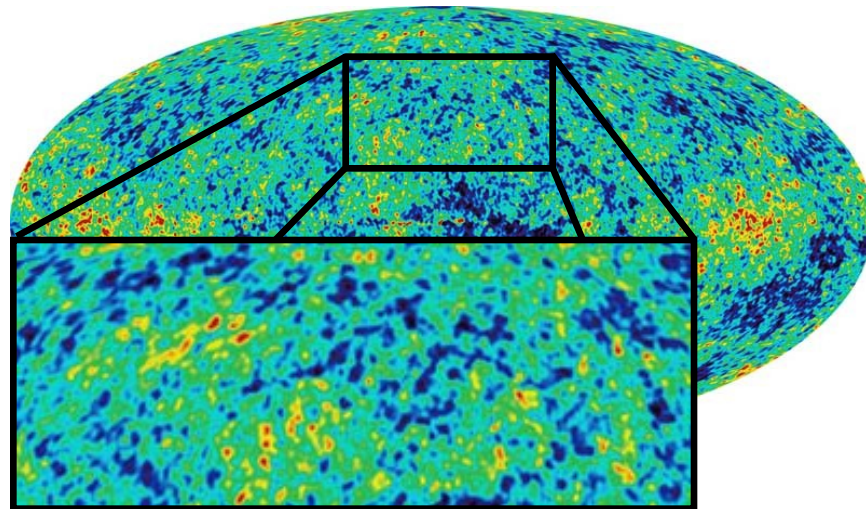
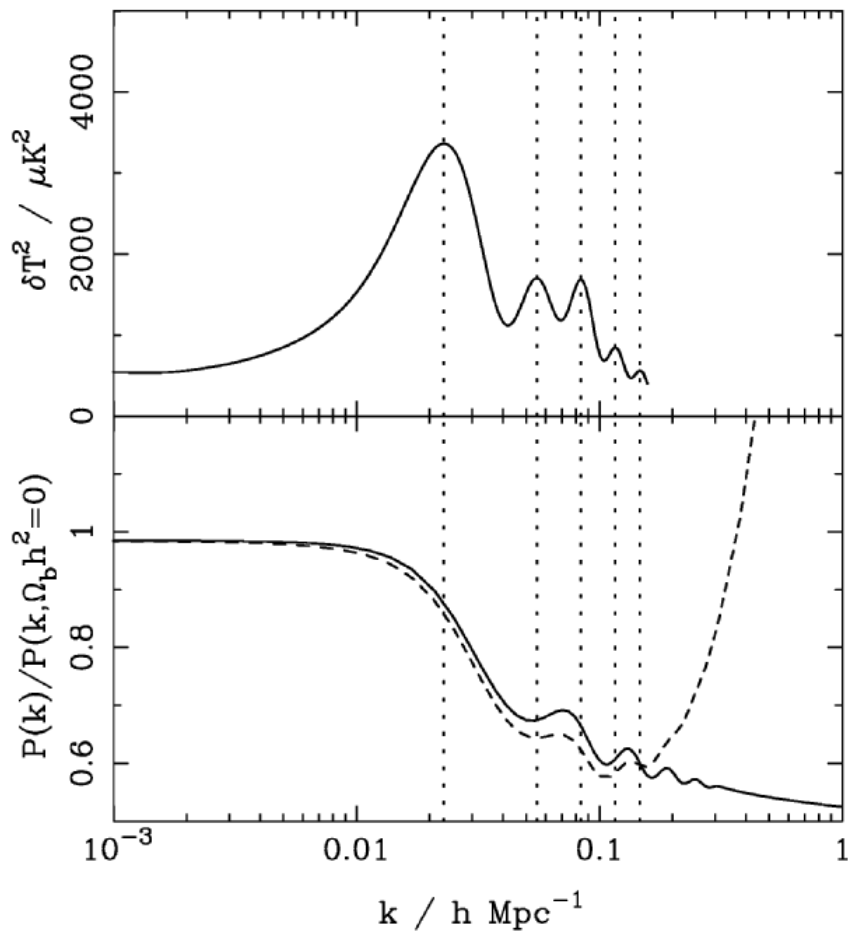


What are the constituents of matter?  
Why is the Universe homogeneous on large scales?

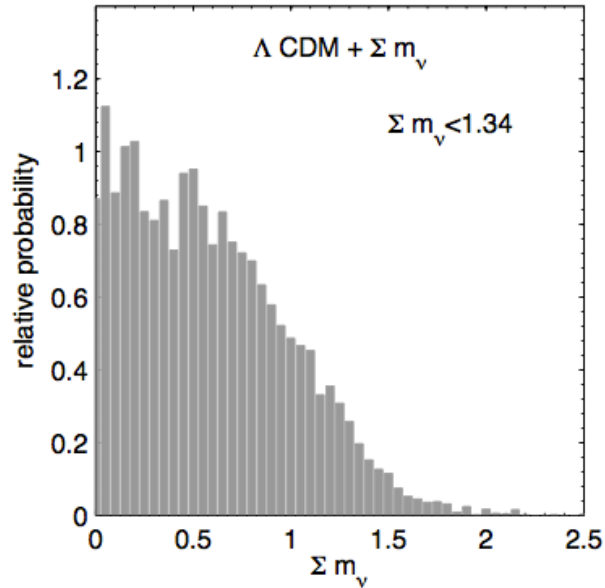


# Relationship between CMB and LSS clustering

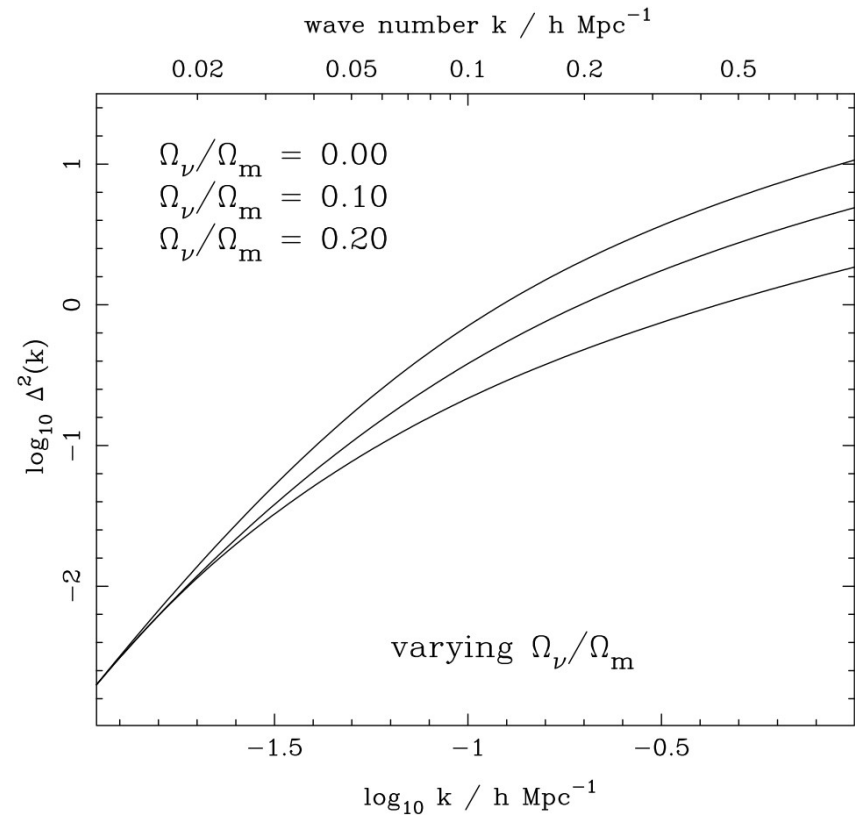
$$\Omega_m=0.3, \Omega_v=0.7, h=0.7, \Omega_b h^2=0.02$$



# neutrino mass from comoving clustering

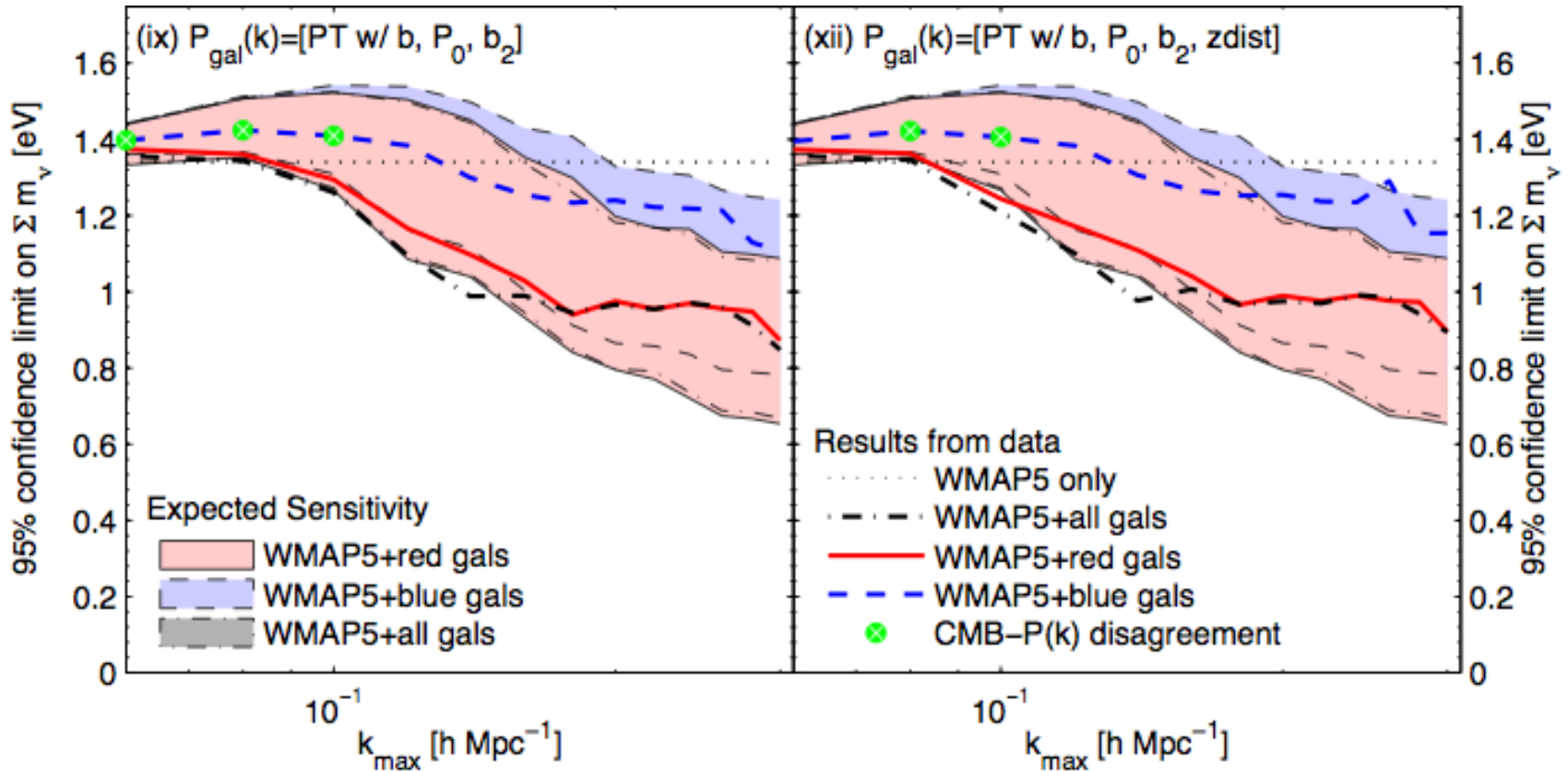


WMAP 7 year data:  
 Dunkley et al. (2009: ApJS,180, 306)



LSS can help through comoving shape  
 and breaking CMB projection degeneracies

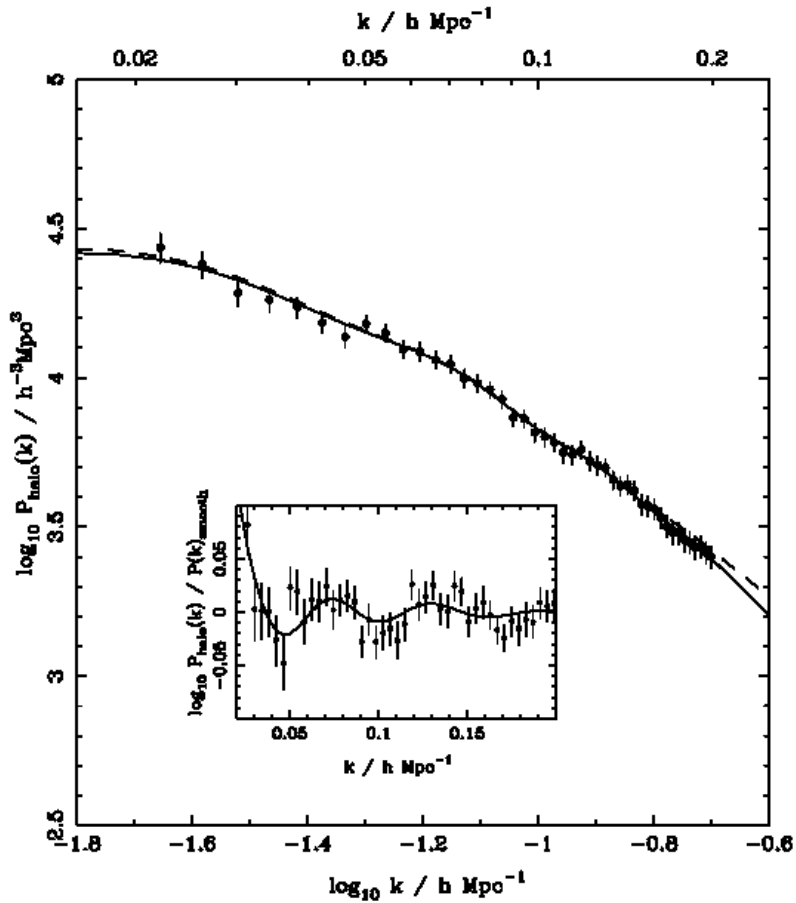




For current SDSS data: red and blue galaxies give constraints that are  $\sim 1\sigma$  apart, using shape of  $P(k)$



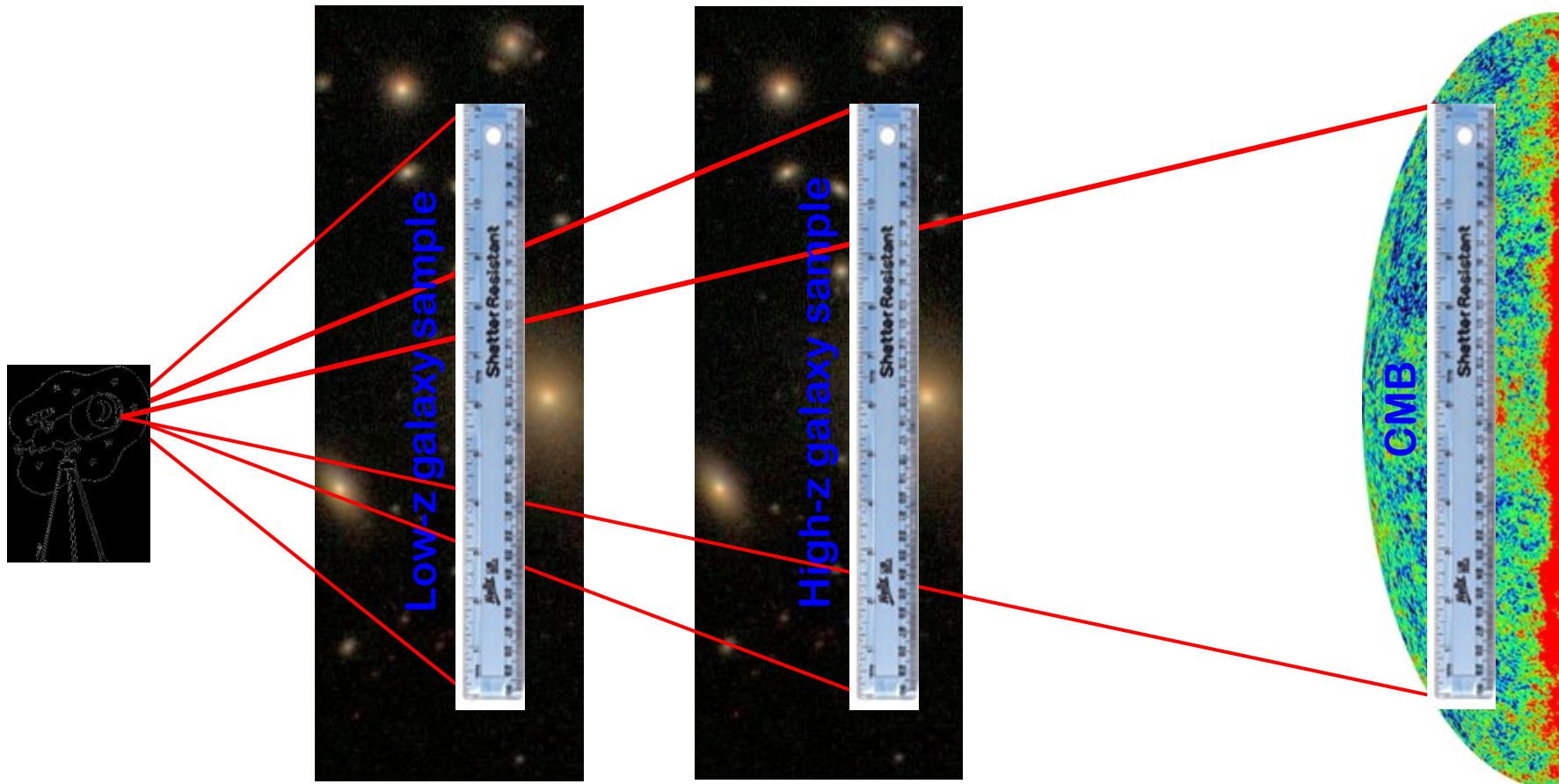
Use luminous red galaxies (LRGs) to extract the halo power spectrum and model the shape to constrain cosmological models



parameter	$\Lambda$ CDM	$\sigma\Lambda$ CDM	wCDM	owCDM
$\Omega_m$	$0.289 \pm 0.019$	$0.309 \pm 0.025$	$0.328 \pm 0.037$	$0.306 \pm 0.050$
$H_0$	$69.4 \pm 1.6$	$66.0 \pm 2.7$	$64.3 \pm 4.1$	$66.7^{+5.9}_{-5.6}$
$D_V(0.35)$	$1349 \pm 23$	$1415 \pm 49$	$1398 \pm 45$	$1424 \pm 49$
$r_s/D_V(0.35)$	$0.1125 \pm 0.0023$	$0.1084 \pm 0.0034$	$0.1094 \pm 0.0032$	$0.1078^{+0.0033}_{-0.0034}$
$\Omega_k$	-	$-0.0114^{+0.0076}_{-0.0077}$	-	$-0.009 \pm 0.012$
$w$	-	-	$-0.79 \pm 0.15$	$-1.06 \pm 0.38$
$\Omega_\Lambda$	$0.711 \pm 0.019$	$0.703 \pm 0.021$	$0.672 \pm 0.037$	$0.703^{+0.057}_{-0.058}$
Age (Gyr)	$13.73 \pm 0.13$	$14.25 \pm 0.37$	$13.87 \pm 0.17$	$14.27 \pm 0.52$
$\Omega_{tot}$	-	$1.0114^{+0.0077}_{-0.0076}$	-	$1.009 \pm 0.012$
$100\Omega_b h^2$	$2.272 \pm 0.058$	$2.274 \pm 0.059$	$2.293^{+0.062}_{-0.063}$	$2.279^{+0.066}_{-0.065}$
$\Omega_c h^2$	$0.1161^{+0.0039}_{-0.0038}$	$0.1110 \pm 0.0052$	$0.1112^{+0.0056}_{-0.0057}$	$0.1103^{+0.0055}_{-0.0054}$
$\tau$	$0.084 \pm 0.016$	$0.089 \pm 0.017$	$0.088 \pm 0.017$	$0.088 \pm 0.017$
$n_s$	$0.961 \pm 0.013$	$0.962 \pm 0.014$	$0.969 \pm 0.015$	$0.965 \pm 0.016$
$\ln(10^{10} A_{05})$	$3.080^{+0.036}_{-0.037}$	$3.068 \pm 0.040$	$3.071^{+0.040}_{-0.039}$	$3.064 \pm 0.041$
$\sigma_8$	$0.824 \pm 0.025$	$0.796 \pm 0.032$	$0.735 \pm 0.073$	$0.79 \pm 0.11$

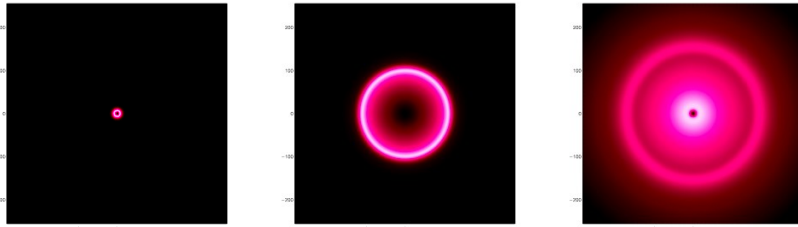
Why do we see an accelerating Universe?

# Using clustering to measure geometry



Sunyaev & Zel'dovich (1970); Peebles & Yu (1970); Doroshkevitch, Sunyaev & Zel'dovich (1978); Cooray, Hu, Huterer & Joffre (2001); Eisenstein (2003); Seo & Eisenstein (2003); Blake & Glazebrook (2003); Hu & Haiman (2003); ...

# Baryon Acoustic Oscillations (BAO)

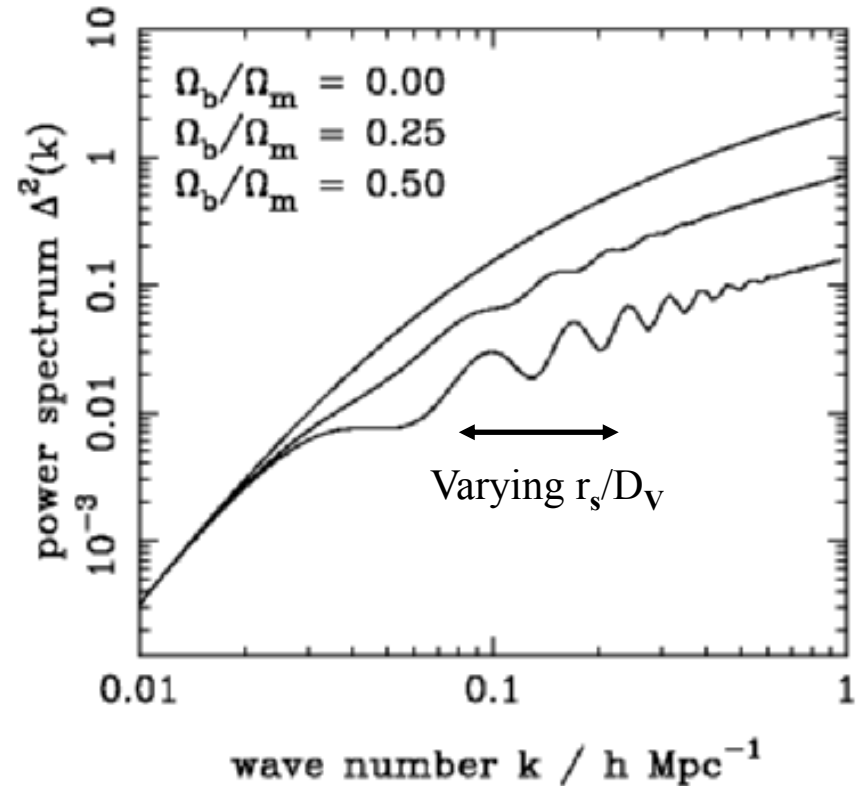


(images from Martin White)

To first approximation, comoving BAO wavelength is determined by the comoving sound horizon at recombination

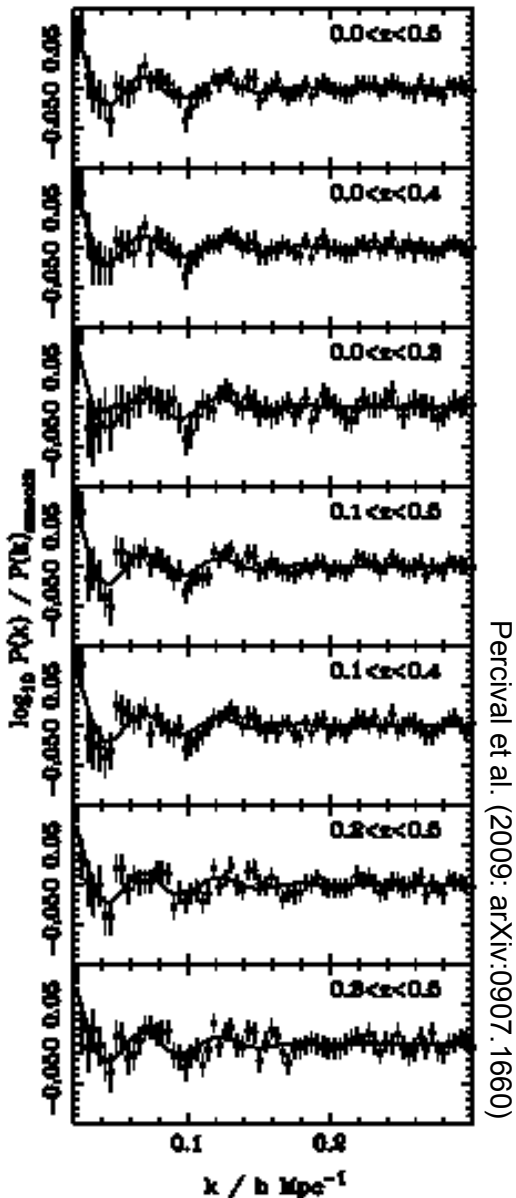
$$r_s = \frac{1}{H_0 \Omega_m^{1/2}} \int_0^{a_*} da \frac{c_s}{(a + a_{eq})^{1/2}}$$

comoving sound horizon  $\sim 110 h^{-1} \text{Mpc}$ ,  
BAO wavelength  $0.06 h \text{Mpc}^{-1}$



projection onto the observed galaxy distribution depends on

$$D_V(z) = \left[ (1+z)^2 D_A^2(z) \frac{cz}{H(z)} \right]^{1/3}$$



- Combine 2dFGRS, SDSS DR7 LRG and SDSS Main Galaxy samples
- split into redshift slices and fit  $P(k)$  with model comprising smooth fit  $\times$  BAO
- results can be written as independent constraints on a distance measure to  $z=0.275$  and a tilt around this

$$r_s(z_d)/D_V(0.275) = 0.1390 \pm 0.0037 \text{ (2.7\%)}$$

$$D_V(0.35)/D_V(0.2) = 1.736 \pm 0.065$$

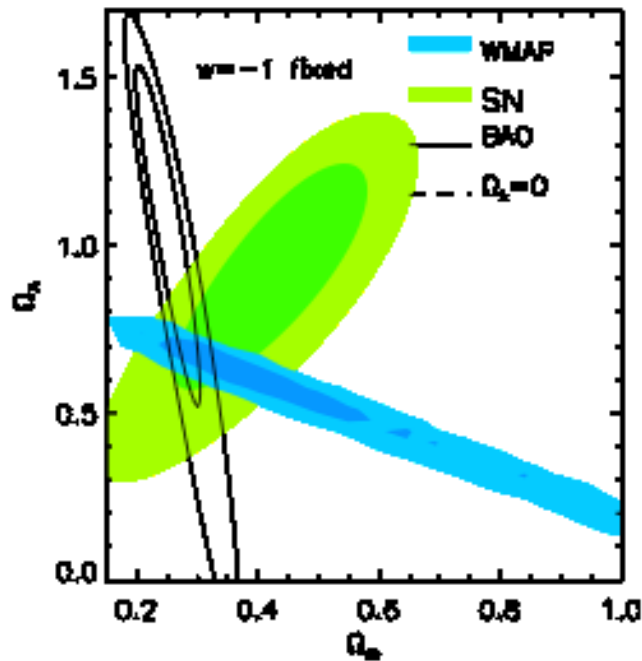
- consistent with  $\Lambda$ CDM models at  $1.1\sigma$  when combined with WMAP5



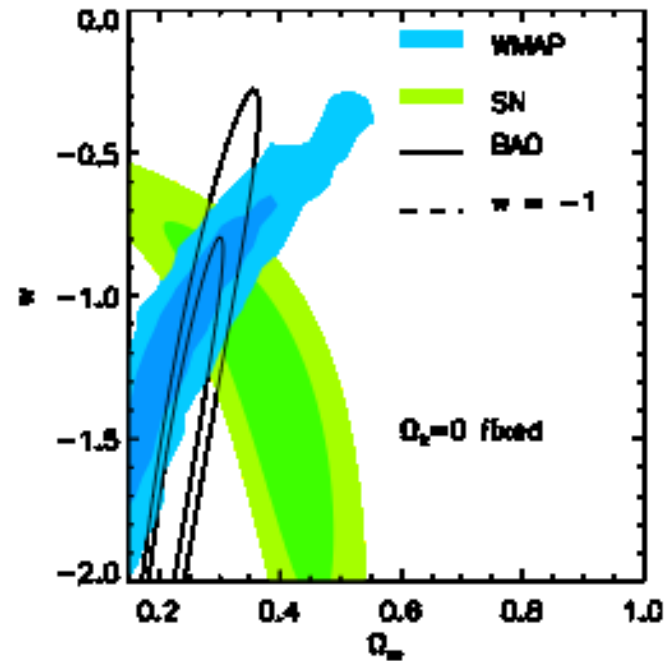
# Comparing BAO constraints vs other data






$\Lambda$ CDM models with curvature



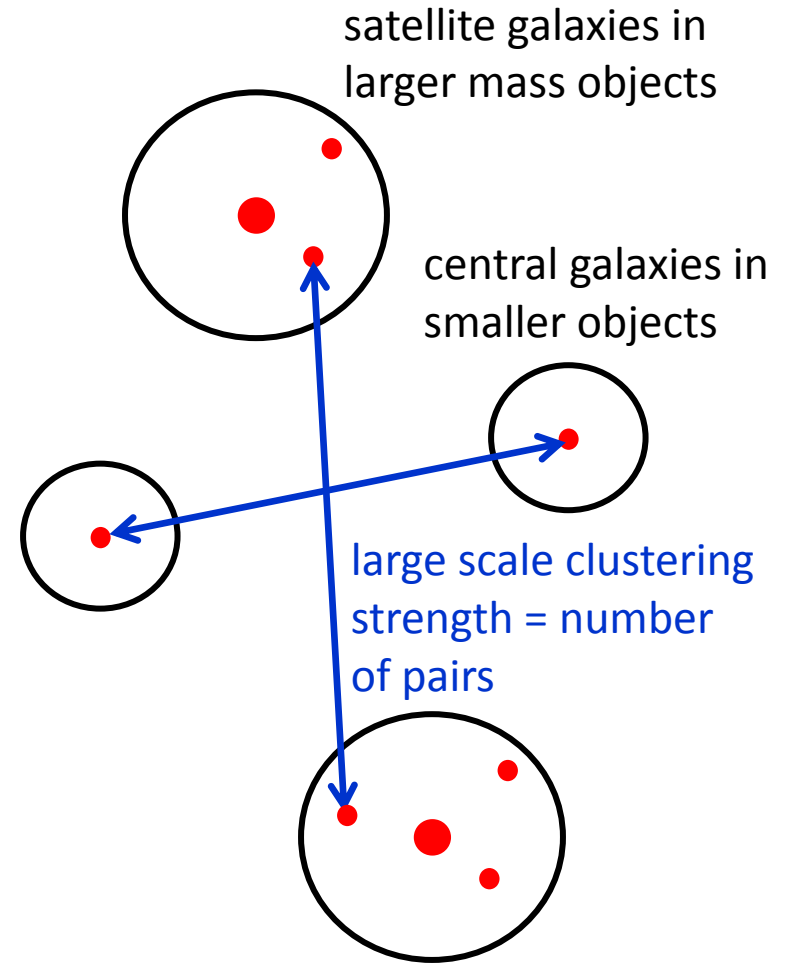
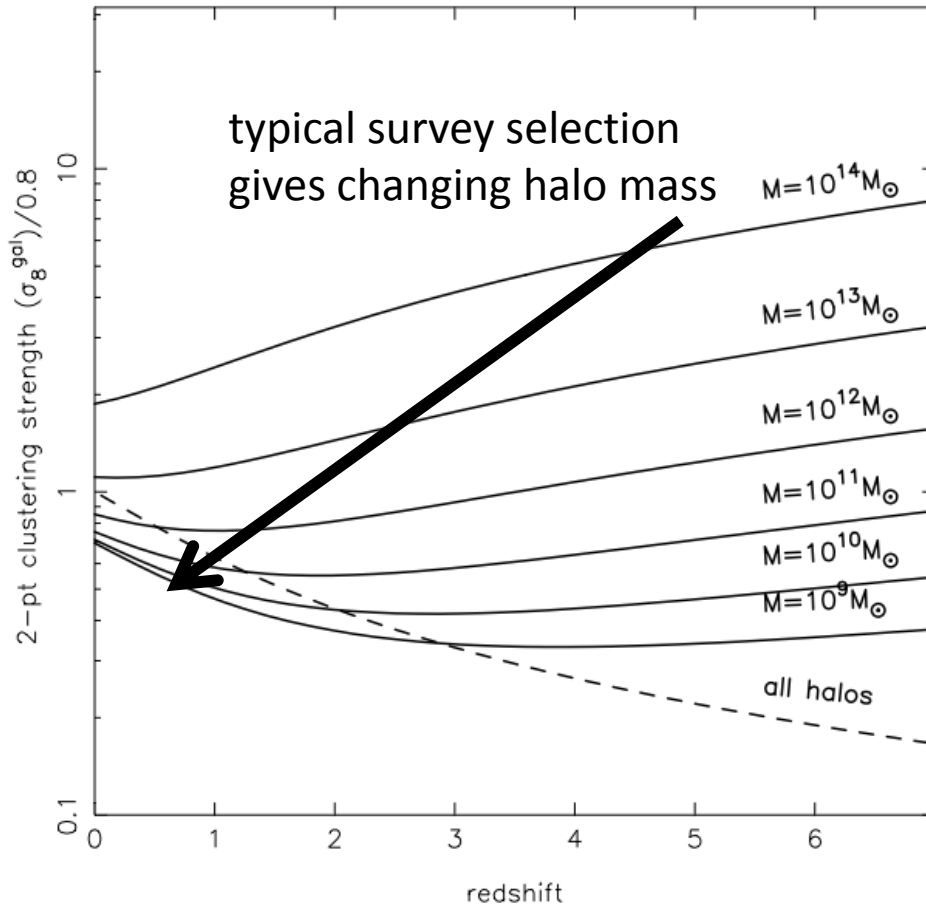
flat  $w$ CDM models



-  Union supernovae
-  WMAP 5year
-  SDSS BAO Constraint on  $r_s(z_d)/D_V(0.2)$  &  $r_s(z_d)/D_V(0.35)$

How does structure form within this background?

# We cannot see growth of structure directly from galaxies



# Redshift-Space Distortions

When we measure the position of a galaxy, we measure its position in redshift-space; this differs from the real-space because of its peculiar velocity:

$$\mathbf{s}(\mathbf{r}) = \mathbf{r} - \mathbf{v}_r(\mathbf{r})\hat{\mathbf{r}}$$

Where  $\mathbf{s}$  and  $\mathbf{r}$  are positions in redshift- and real-space and  $v_r$  is the peculiar velocity in the radial direction

# Redshift-Space Distortions

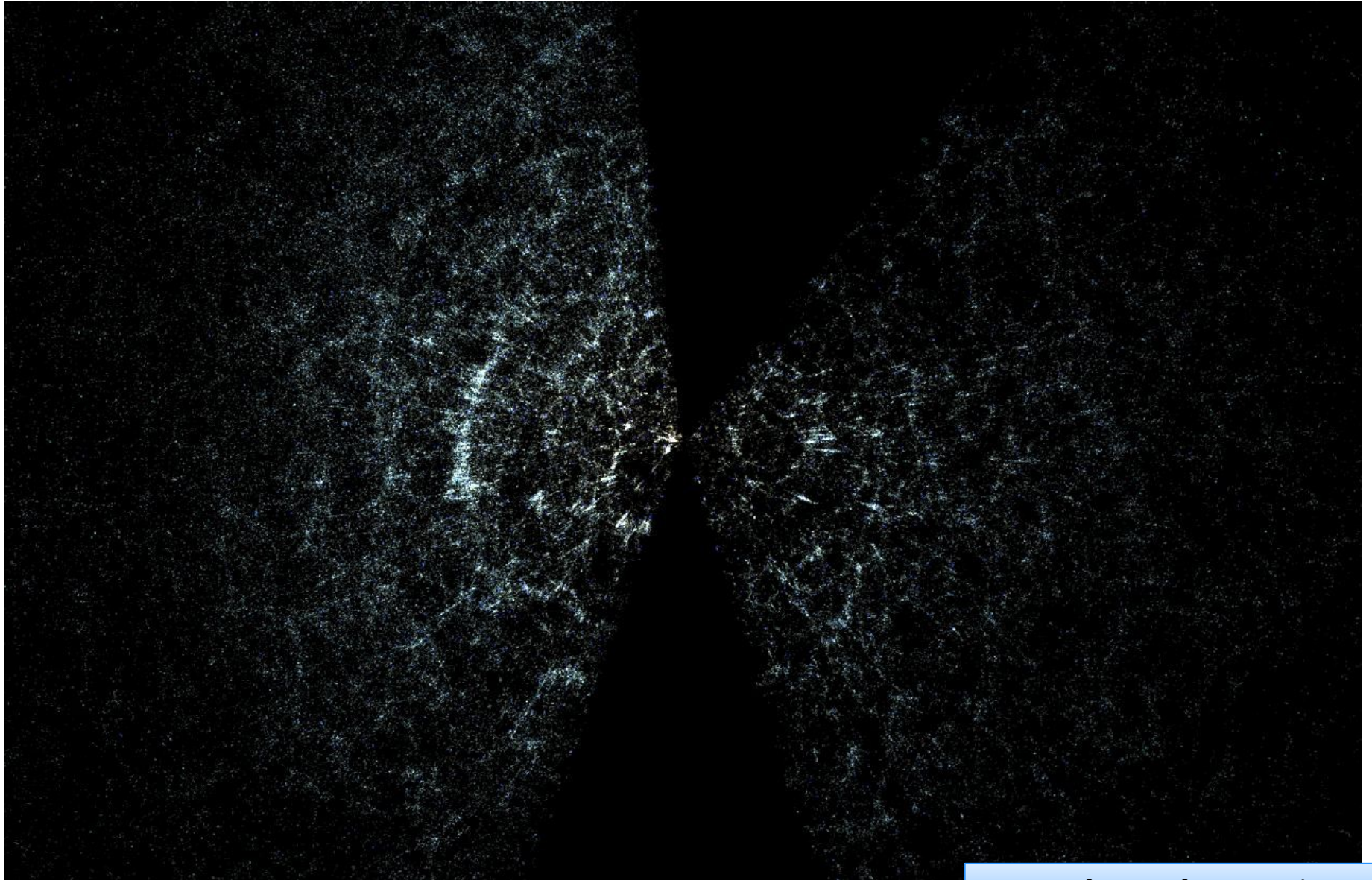
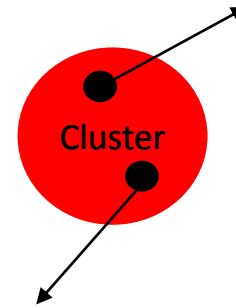
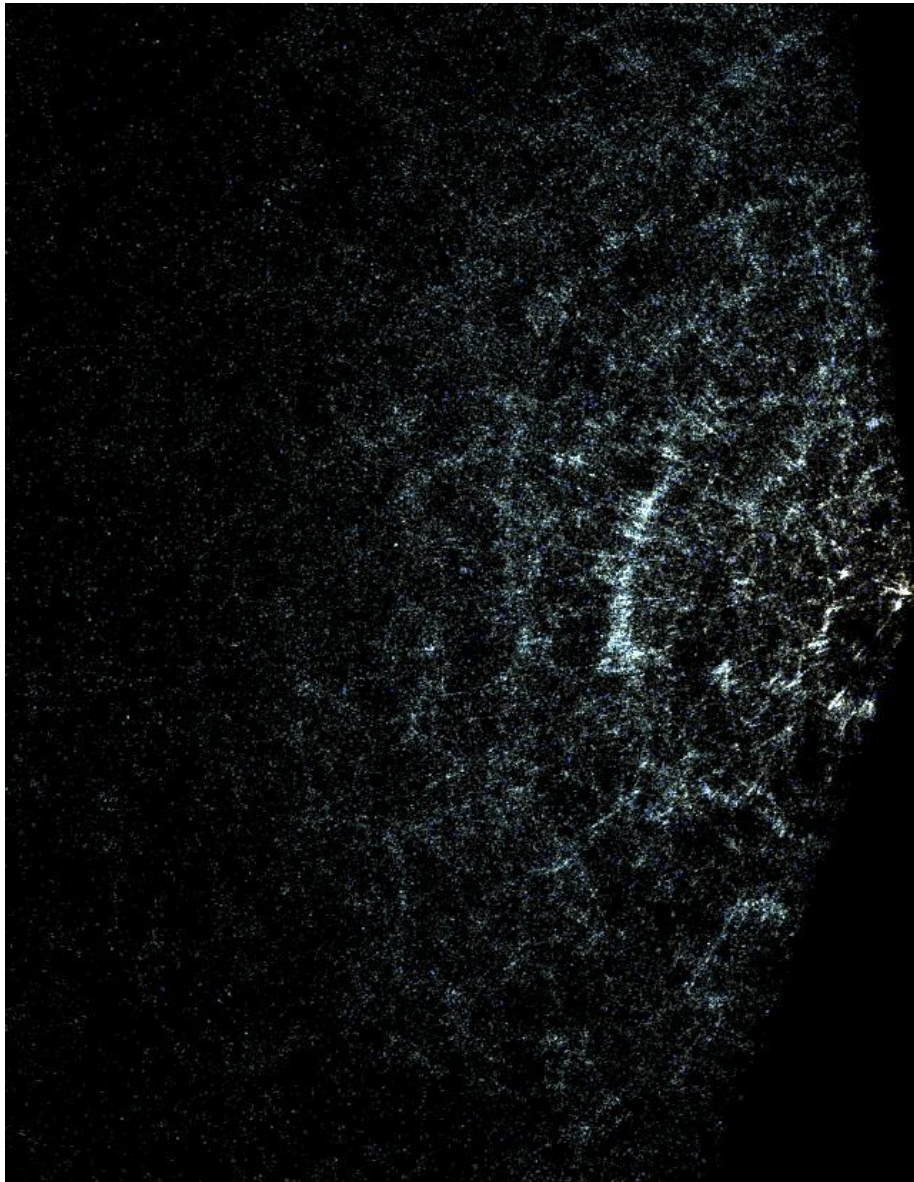


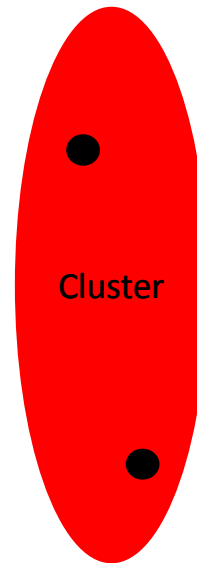
Image of SDSS, from U. Chicago



# Redshift-Space Distortions



Actual  
shape

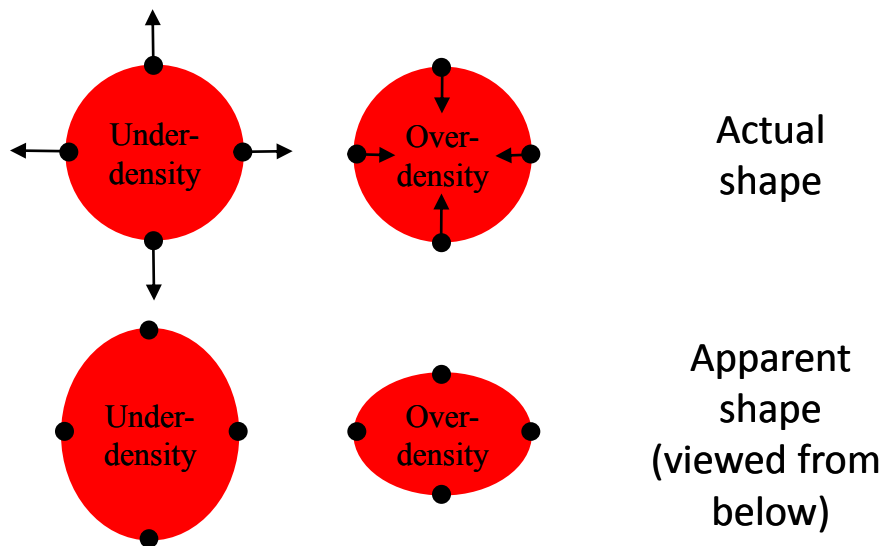


Apparent  
shape  
(viewed from  
below)

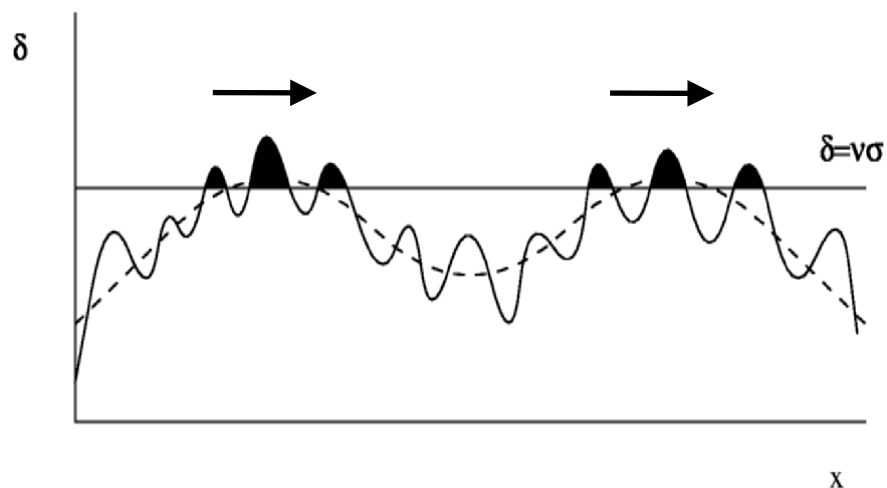


# Galaxies act as test particles

Galaxies act as test particles with the flow of matter



On large-scales, the distribution of galaxy velocities is unbiased provided that the positions of galaxies fully sample the velocity field



If fact, we can expect a small peak velocity-bias due to motion of peaks in Gaussian random fields

# Standard measurements provide good test of models

assume: irrotational velocity field due to structure growth, plane-parallel approximation, linear deterministic density & velocity bias, first order in  $\delta$ ,  $\theta$

$$\begin{aligned} \delta_{\text{gal}}(k, \mu) &= b\delta_{\text{mass}} + \mu^2 b_v \theta_{\text{mass}} \\ \delta_{\text{gal}}(k, \mu) &= b\delta_{\text{mass}} (1 + \mu^2 b_v \beta)^2 \\ \delta_{\text{gal}}(k, \mu) &= \delta_{\text{mass}} (b + \mu^2 b_v f)^2 \end{aligned}$$

Normalise RSD to  $\sigma_v$

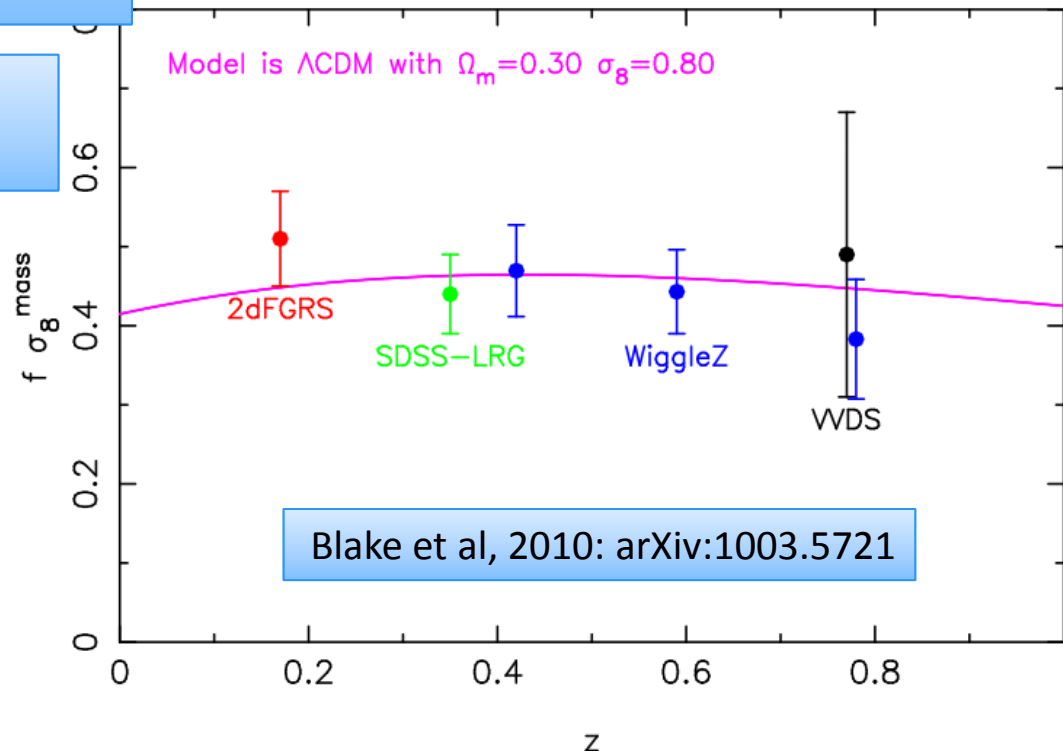
Normalise RSD to  $\beta=f/b$

Normalise RSD to  $f\sigma_8$

assume continuity, scale-independent growth

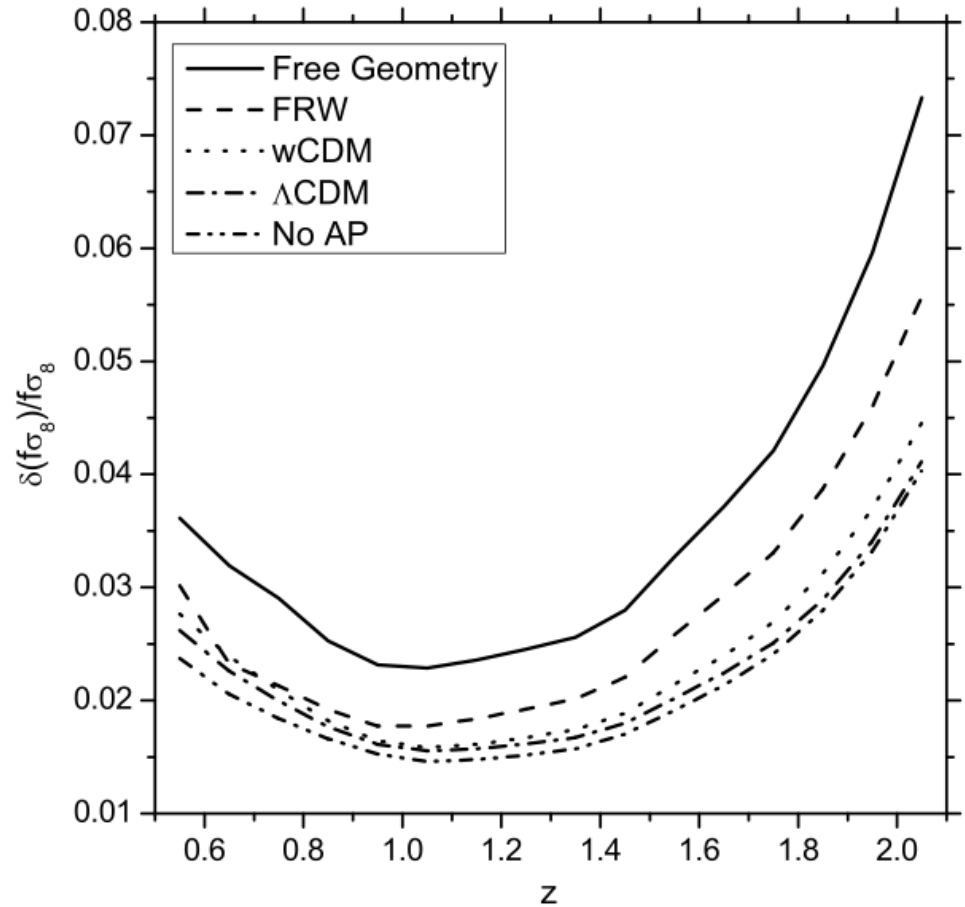
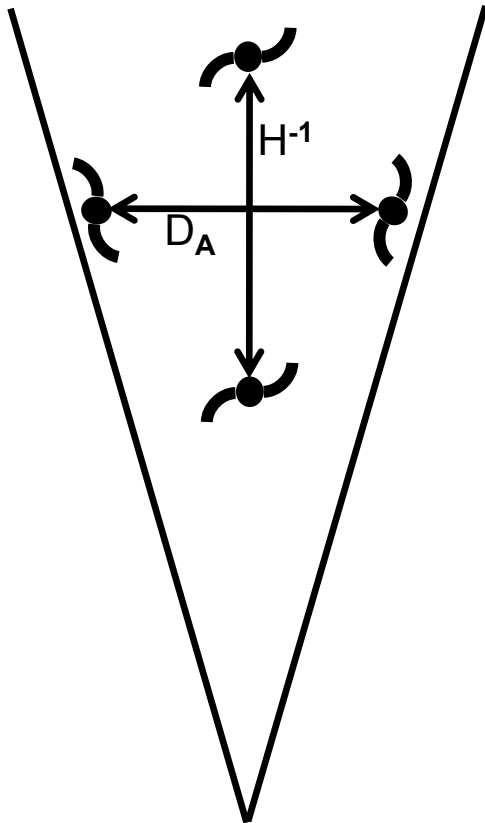
Standard assumption:  $b_v=1$  (current simulations limit this to a 10% effect).

$$\begin{aligned} f &\equiv \frac{d \log G}{d \log a} \\ f\sigma_8 &\propto \frac{dG}{d \log a} \\ G &= \frac{\delta(z, \text{mass})}{\delta(0, \text{mass})} \end{aligned}$$

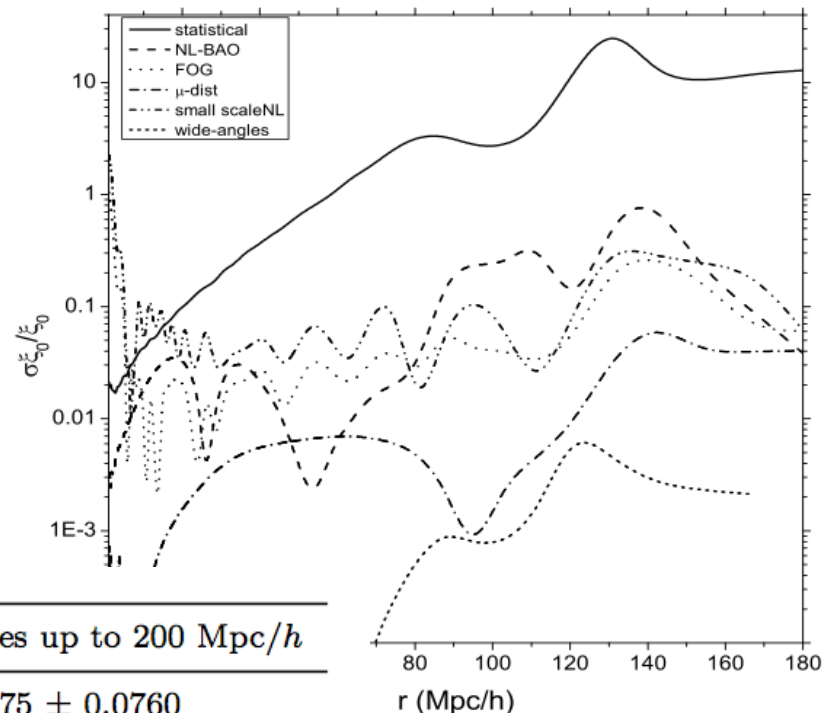


# Degeneracies – RSD vs Alcock-Palczynski

RSD distortion resembles distortion obtained by applying wrong distance-redshift relation through  $D_A H$  (Alcock-Palczynski effect)



- Consider:
  - Wide-angle effects
  - Non-linear growth of structure
  - Fingers-of-God
  - Non-Gaussian Likelihood



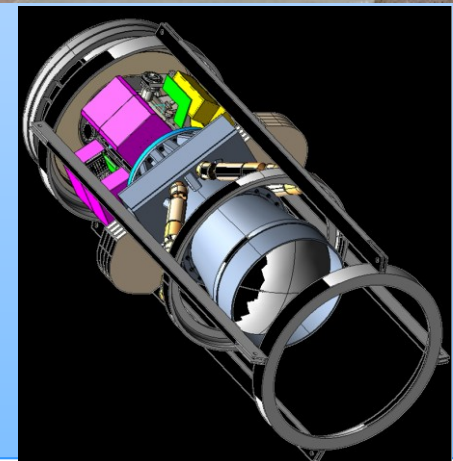
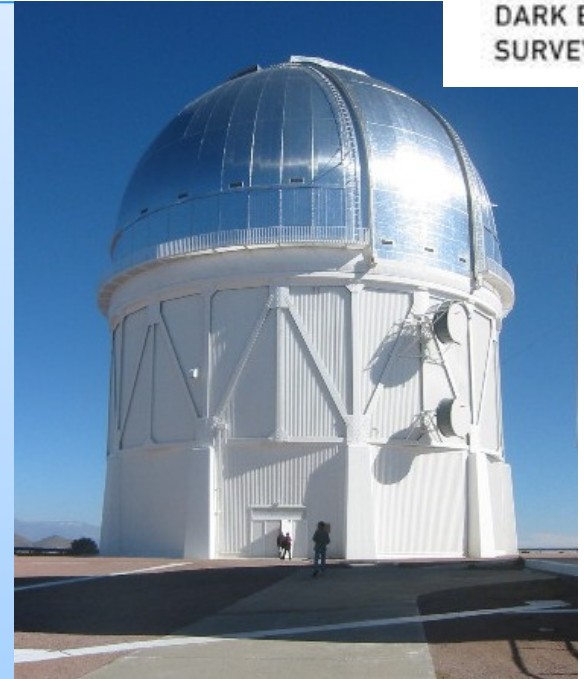
Model	Variable	Scales less than 60 Mpc/h	Scales up to 200 Mpc/h
wCDM	$b(z_1)\sigma_8(z_1)$	$1.4949 \pm 0.0772$	$1.5175 \pm 0.0760$
	$b(z_2)\sigma_8(z_2)$	$1.5316 \pm 0.0717$	$1.57435 \pm 0.0672$
$\gamma$	$b(z_1)\sigma_8(z_1)$	$1.5462 \pm 0.0911$	$1.6098 \pm 0.0840$
	$b(z_2)\sigma_8(z_2)$	$1.5522 \pm 0.0916$	$1.5882 \pm 0.0727$
	$\gamma$	$0.6545 \pm 0.1100$	$0.6007 \pm 0.1206$
Free growth	$b(z_1)\sigma_8(z_1)$	$1.4733 \pm 0.0640$	$1.4388 \pm 0.0619$
	$b(z_2)\sigma_8(z_2)$	$1.4557 \pm 0.0496$	$1.5038 \pm 0.0436$
	$f(z_1)\sigma_8(z_1)$	$0.3930 \pm 0.0457$	$0.3481 \pm 0.0594$
	$f(z_2)\sigma_8(z_2)$	$0.4328 \pm 0.0370$	$0.4522 \pm 0.0418$

## Future surveys

# Dark Energy Survey (DES)

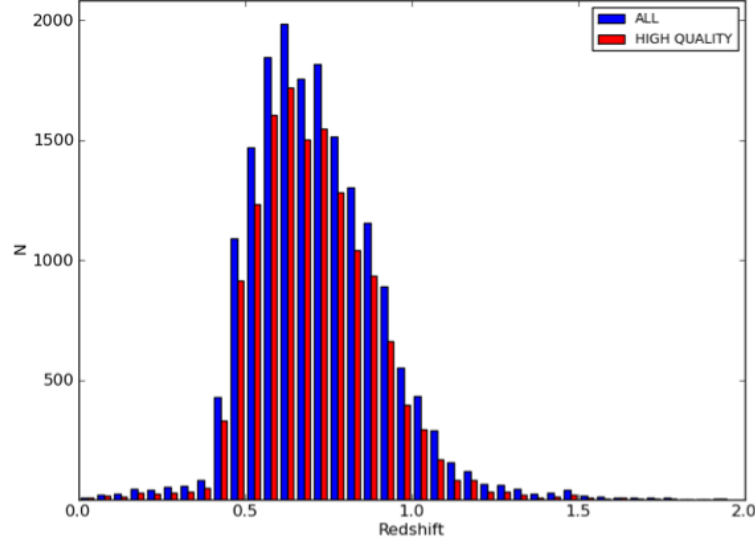
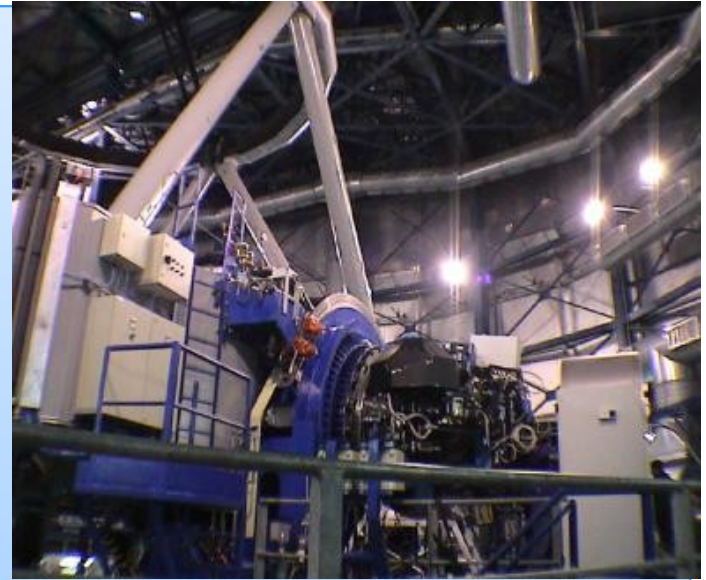


- New wide-field camera for the 4m Blanco telescope
- Currently being moved from Fermilab to site, Survey due to start autumn 2011
- $\Omega = 5,000\text{deg}^2$
- multi-colour optical imaging (g,r,i,z) with link to IR data from VISTA hemisphere survey
- 300,000,000 galaxies
- Aim is to constrain dark energy using 4 probes  
LSS/BAO, weak lensing, supernovae  
cluster number density
- Redshifts based on photometry  
weak radial measurements  
weak redshift-space distortions
- See also: Pan-STARRS, VST-VISTA, SkyMapper





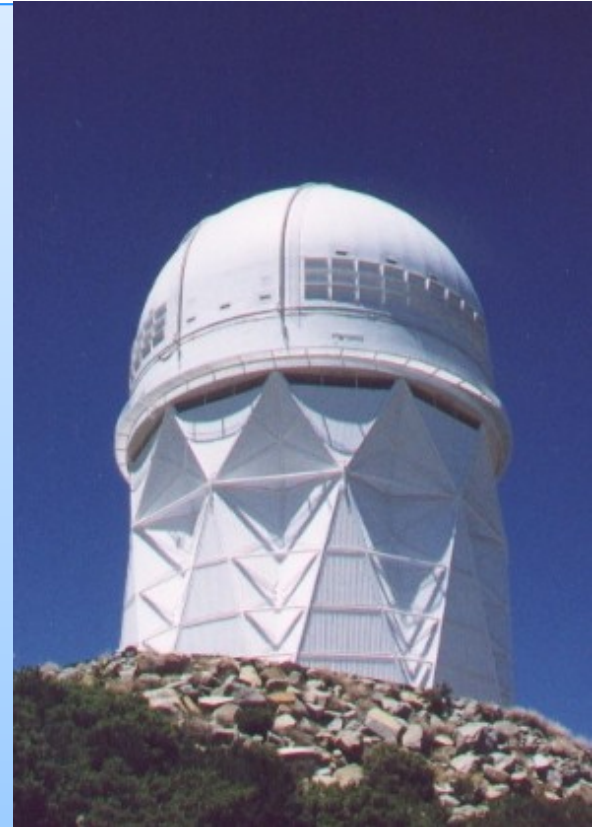
- Uses upgraded VIMOS on VLT
- $\Omega = 24\text{deg}^2$
- 100,000 galaxies
- emission line galaxies:  $0.5 < z < 1.0$
- insufficient volume for BAO measurement
- Unique redshift-space distortion science
- 18,500 redshifts from pre-upgrade data
- expect  $\sim 10,000$  redshifts this season
- see also: FMOS surveys

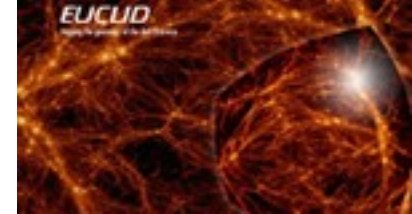


- New fibre-fed spectroscope now on the 2.5m SDSS telescope
- $\Omega = 10,000\text{deg}^2$
- 1,500,000 galaxies
- 150,000 quasars
- LRGs :  $z \sim 0.1 - 0.7$  (direct BAO)
- QSOs :  $z \sim 2.1 - 3.0$  (BAO from Ly- $\alpha$  forest)
  - 0.1<z<0.3: 1%  $d_A$ , 1.8% H
  - 0.4<z<0.7: 1%  $d_A$ , 1.8% H
  - $z \sim 2.5$ : 1.5%  $d_A$ , 1.2% H
- Cosmic variance limited to  $z \sim 0.6$  : as good as LSS mapping will get with a single ground based telescope
- Leverage existing SDSS hardware & software where possible: part of SDSS-III
- Sufficient funding is in place and project is 1 year into 5 year duration
- All imaging data now public (DR8 12/01/11)
- See also: WiggleZ

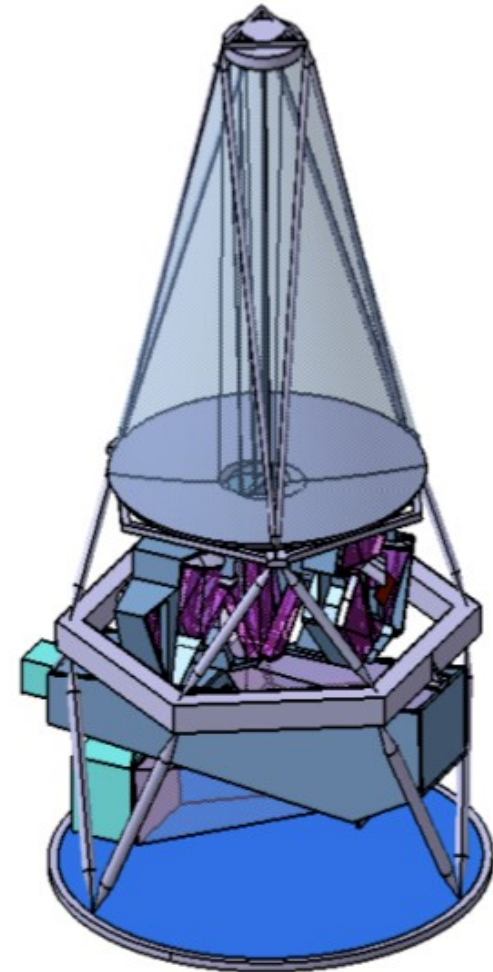


- New fibre-fed spectroscope proposed for 4m Mayall telescope
- NOAO endorsement following proposal evaluation
- $\Omega = 14,000\text{deg}^2$
- 20,000,000 galaxies (direct BAO)
- 600,000 quasars (BAO from Ly- $\alpha$  forest)
- LRGs :  $z \sim 0.1 - 1.0$
- ELGs:  $z \sim 0.5 - 1.7$
- QSOs :  $40/\text{deg}^2$ ,  $z \sim 2.1 - 3.0$ 
  - $z < 0.5$ : 0.9%  $d_A$ , 1.5% H
  - $0.5 < z < 1$ : 0.4%  $d_A$ , 0.6% H
  - $z > 1$ : 0.6%  $d_A$ , 0.8% H
- Cosmic variance limited to  $z \sim 1.4$
- See also: DESpec, WEAVE, VXMS, other instruments on 4m-class telescopes?





- ESA Cosmic Vision satellite proposal (600M€, M-class mission)
- 5 year mission, L2 orbit
- 1.2m primary mirror, 0.5 sq. deg FOV
- $\Omega = 20,000\text{deg}^2$  imaging and spectroscopy
- slitless spectroscopy:
  - 100,000,000 galaxies (direct BAO)
  - ELGs (H-alpha emitters):  $z \sim 0.5-2.1$
- imaging:
  - deep broad-band optical + 3 NIR images
  - 2,900,000,000 galaxies (for WL analysis)
  - photometric redshifts
- Space-base gives robustness to systematics
- Final down-selection due mid 2011
- nominal 2017 launch date
- See also: LSST, WFIRST, SKA



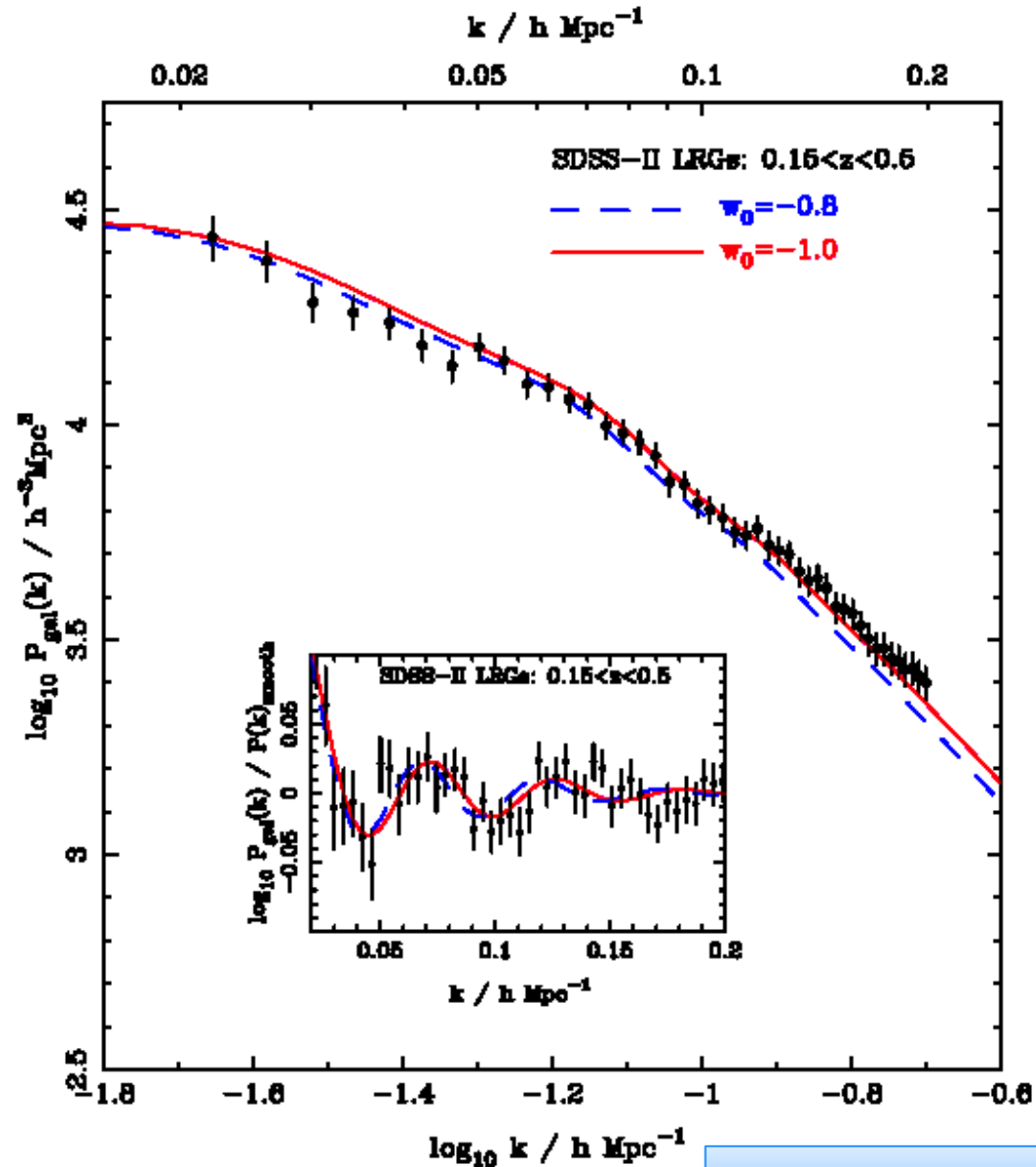
SDSS LRGs at  $z \sim 0.35$

The largest volume of the Universe currently mapped

Total effective volume

$$V_{\text{eff}} = 0.26 \text{ Gpc}^3 h^{-3}$$

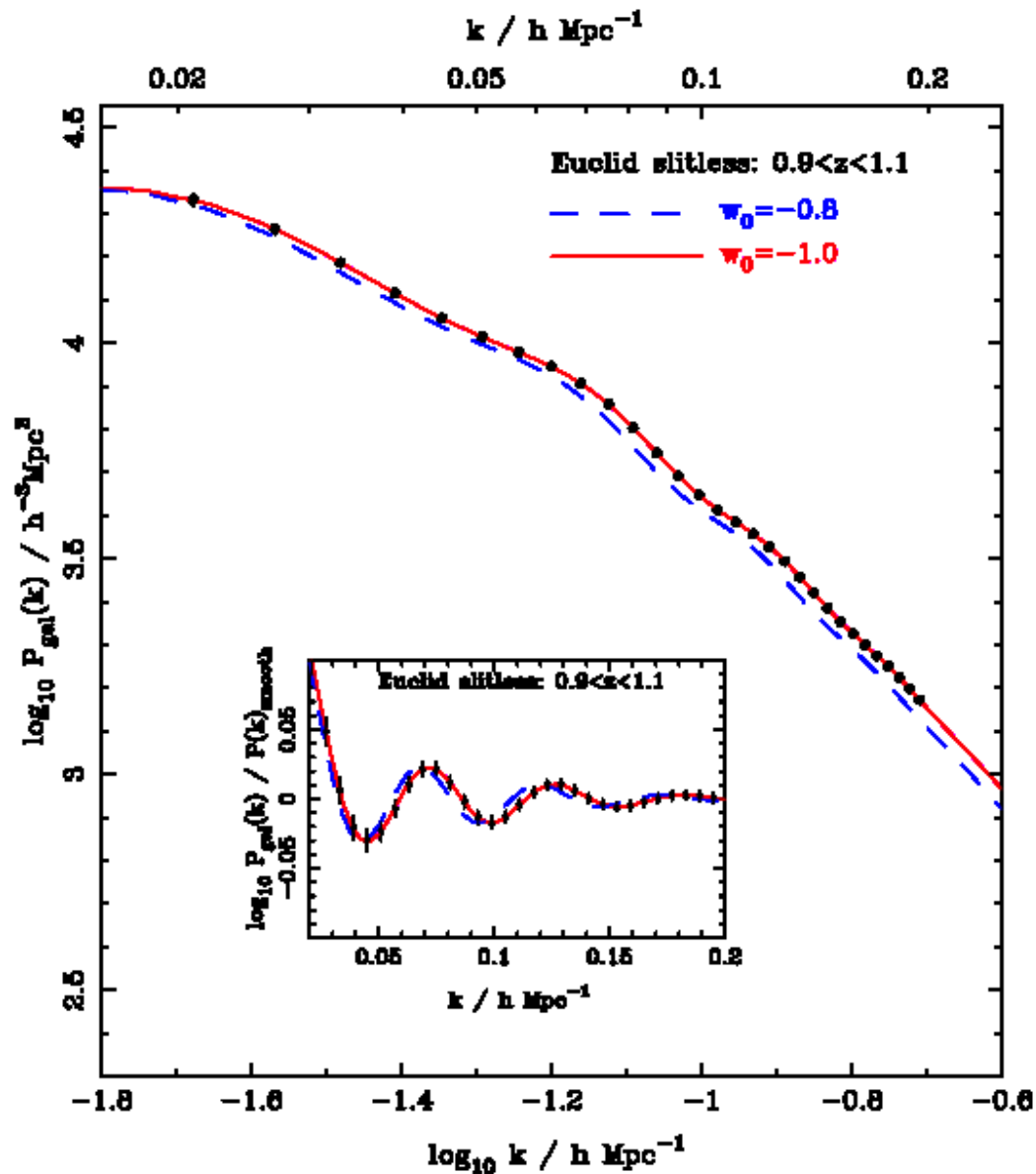
Power spectrum gives amplitude of Fourier modes, quantifying clustering strength on different scales



# Predicted galaxy clustering measurements by Euclid

20% of the Euclid data, assuming the slitless baseline at  $z \sim 1$

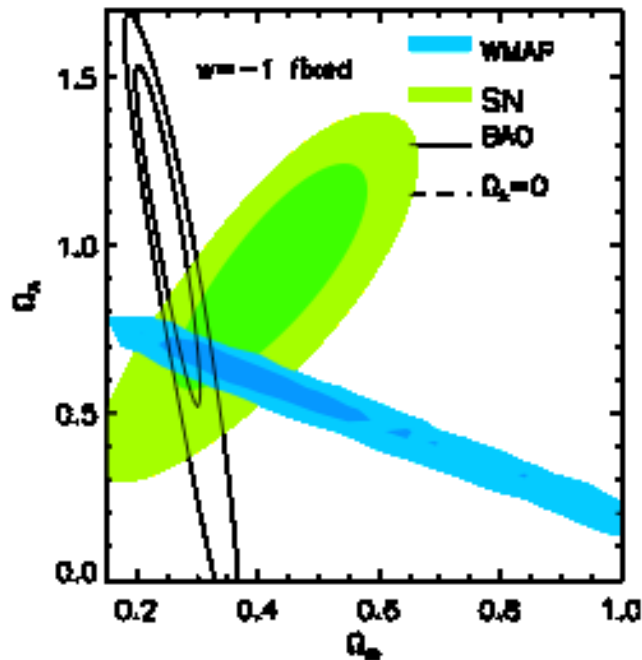
Total effective volume (of Euclid)  
 $V_{\text{eff}} = 19.7 \text{ Gpc}^3 h^{-3}$



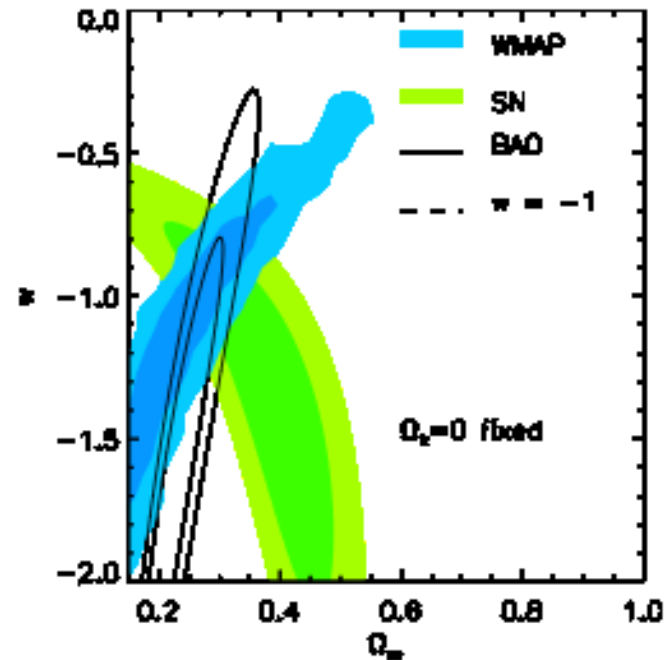





# Current BAO constraints vs other data

$\Lambda$ CDM models with curvature



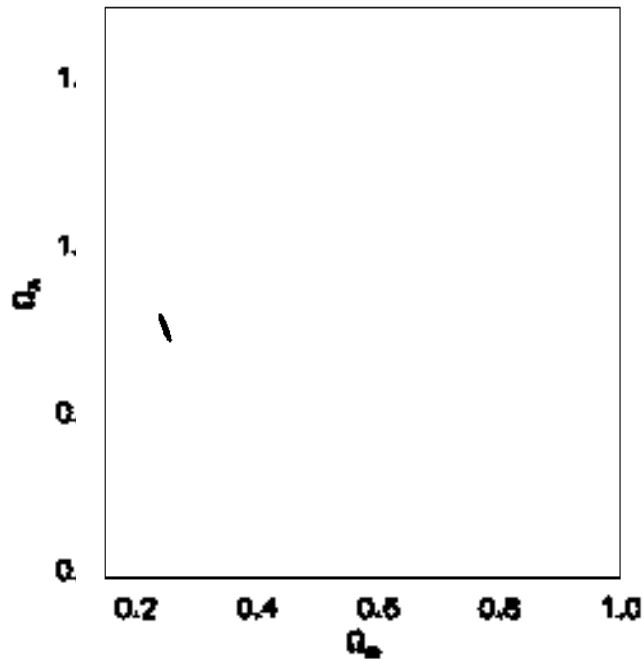
flat  $w$ CDM models



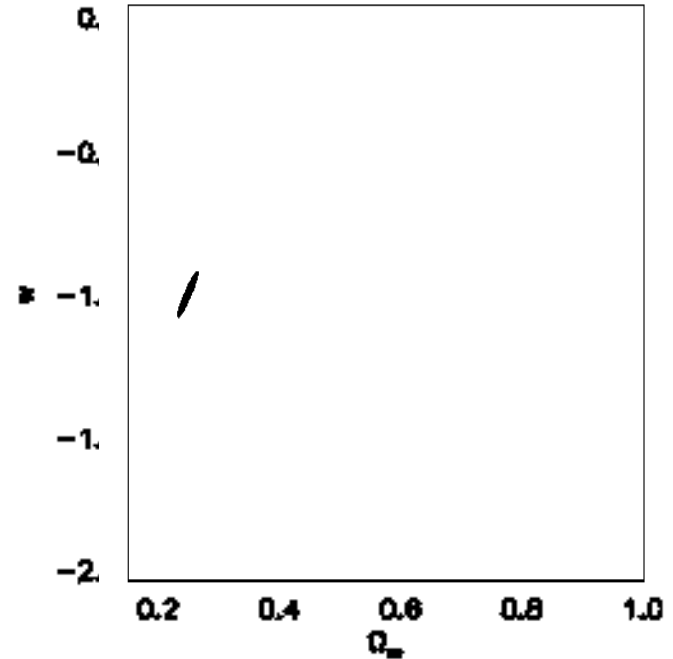
-  Union supernovae
-  WMAP 5year
-  SDSS-II BAO Constraint on  $r_s(z_d)/D_V(0.2)$  &  $r_s(z_d)/D_V(0.35)$

# How does Euclid BAO compare?

$\Lambda$ CDM models with curvature

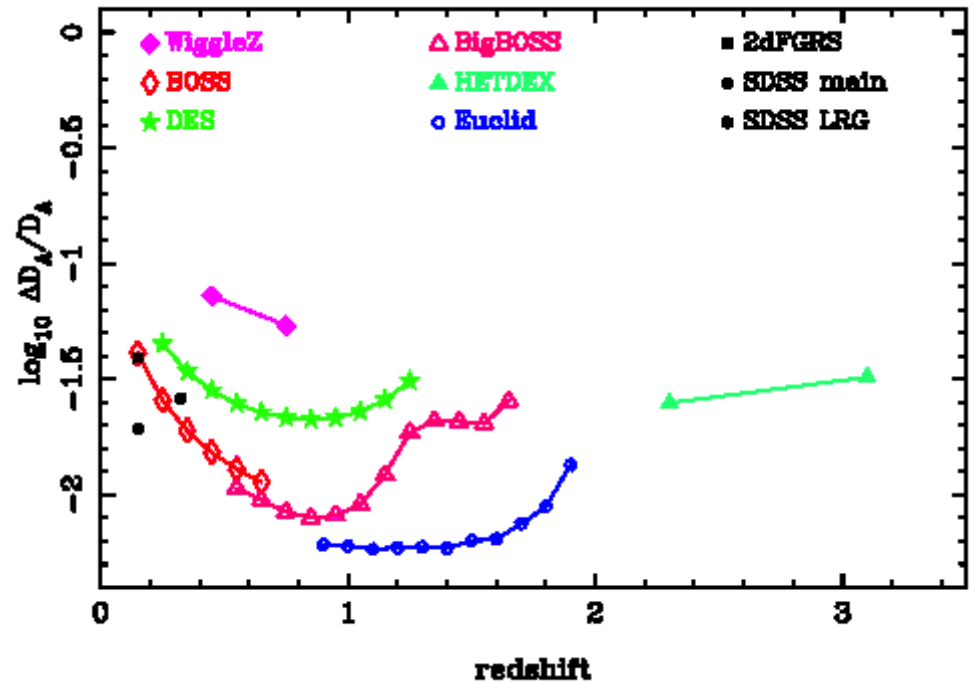
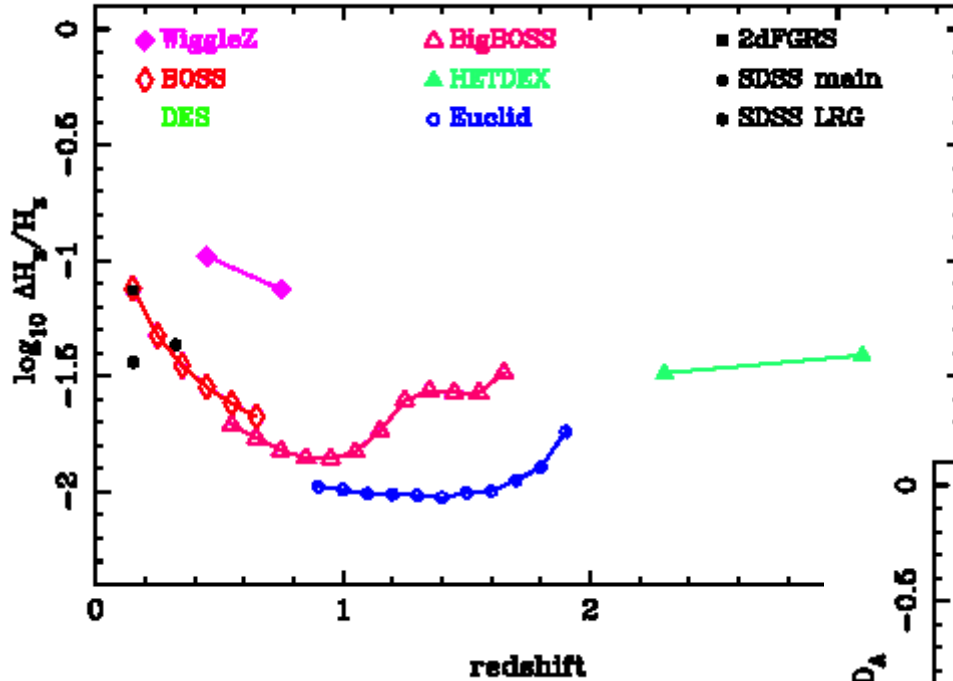


flat  $w$ CDM models



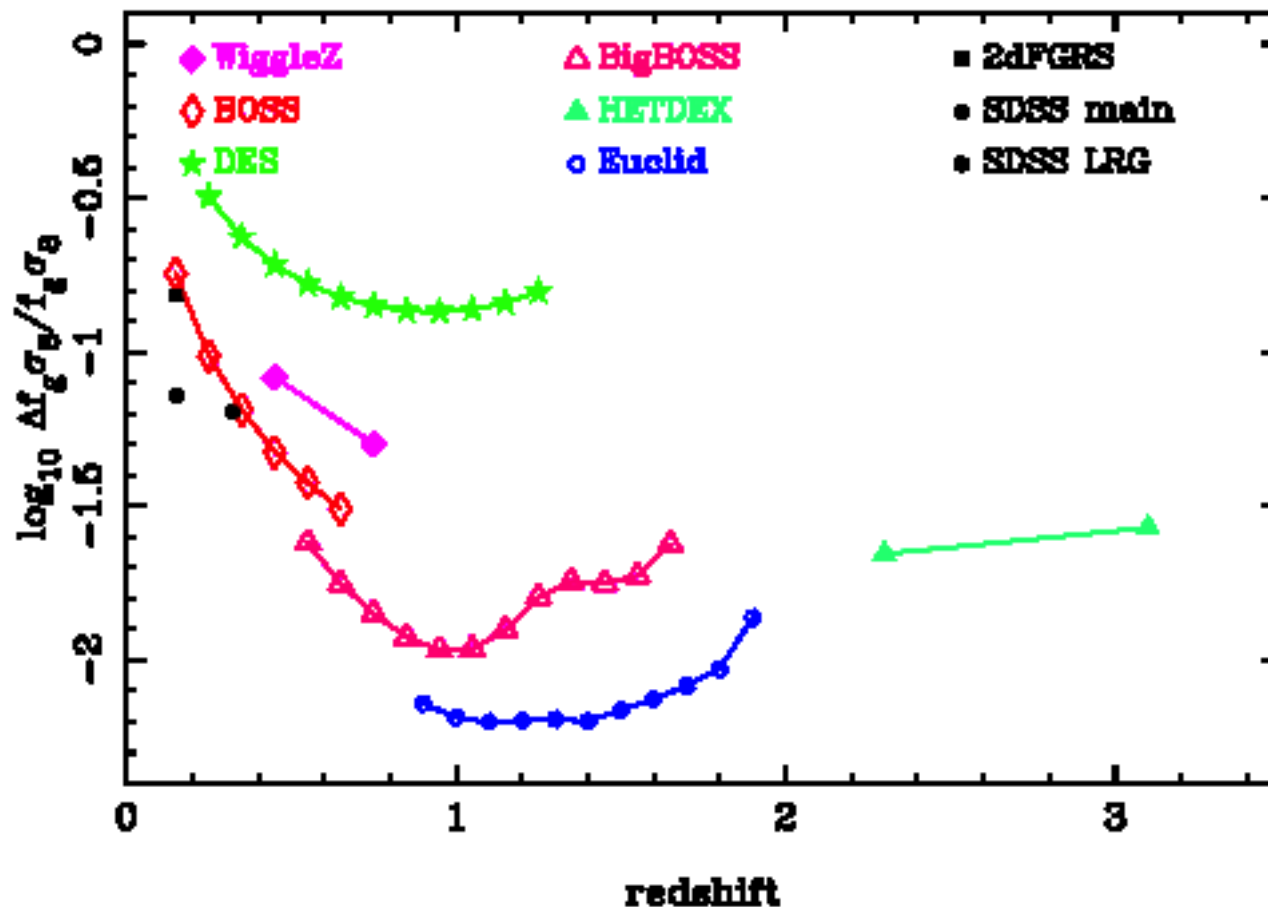
- Union supernovae
- WMAP 5year
- SDSS-II BAO Constraint on  $r_s(z_d)/D_V(0.2)$  &  $r_s(z_d)/D_V(0.35)$

# Predicted BAO constraints



Uses public code to estimate errors from BAO measurements from Seo & Eisenstein (2007: astro-ph/0701079)

# Predicted RSD Constraints



Code to estimate errors on  $f\sigma_8$  is available from:

<http://mwhite.berkeley.edu/Redshift>

- Galaxy clustering will help to answer remaining questions for astrophysical and cosmological models
- Shape of the power spectrum
  - measures galaxy properties (e.g. faint red galaxies)
  - neutrino masses (current systematic limit)
  - models of inflation
- Baryon acoustic oscillations
  - sets geometrical constraints on evolution
- Redshift-space distortions
  - avoids density bias – galaxies act as test particles
  - structure formation test so complementary to geometrical tests
  - similar to weak lensing but tests only temporal metric fluctuations
- Future surveys
  - next generation underway giving an order of magnitude better constraints
  - many different avenues being explored for future projects
  - exciting developments over the next 10–20 years