

# *Exploiting a future galactic supernova to probe neutrino magnetic moments*

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(UNICAMP)**

Talk based on [arXiv:2203.01950](https://arxiv.org/abs/2203.01950)  
with Sudip Jana and Manibrata Sen

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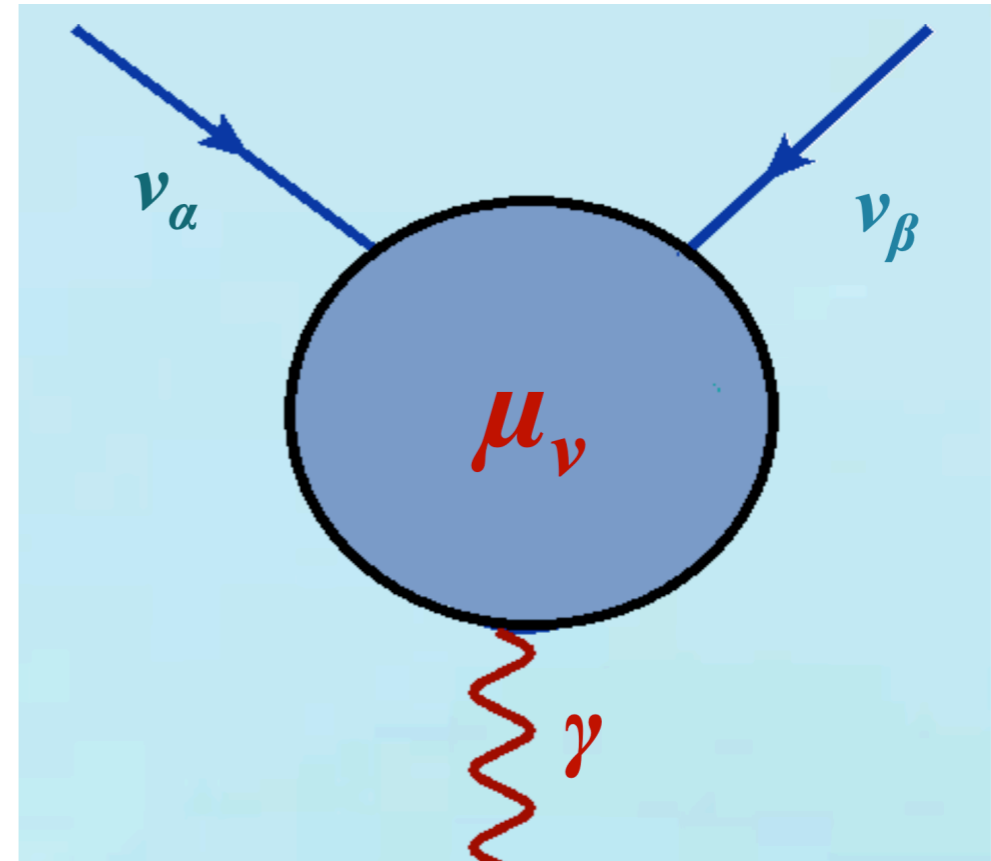


**PASCOS 2022**  
**MPIK, Heidelberg**  
**July, 2022**



# *Neutrino electromagnetic properties*

- In the standard model (SM) neutrinos do not have direct coupling to photons;
- Quantum loop corrections can induce EM properties of neutrinos;
- Study of neutrino EM interactions may shed light on the underlying theory.



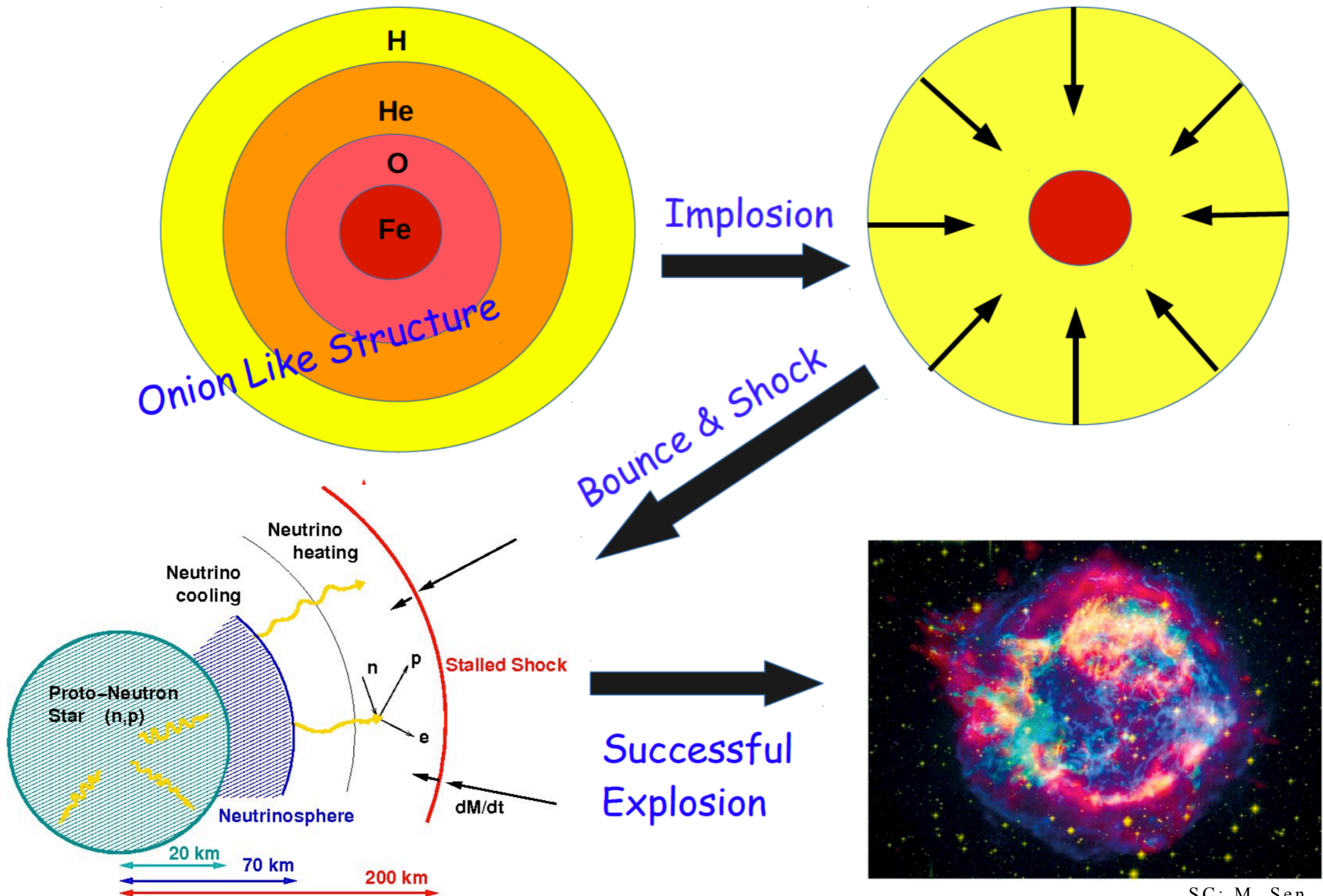
SC: S. Jana

Babu, Jana, Lindner, [arXiv:2007.04291](https://arxiv.org/abs/2007.04291)

Giunti, Studenikin, [arXiv:1403.6344](https://arxiv.org/abs/1403.6344)

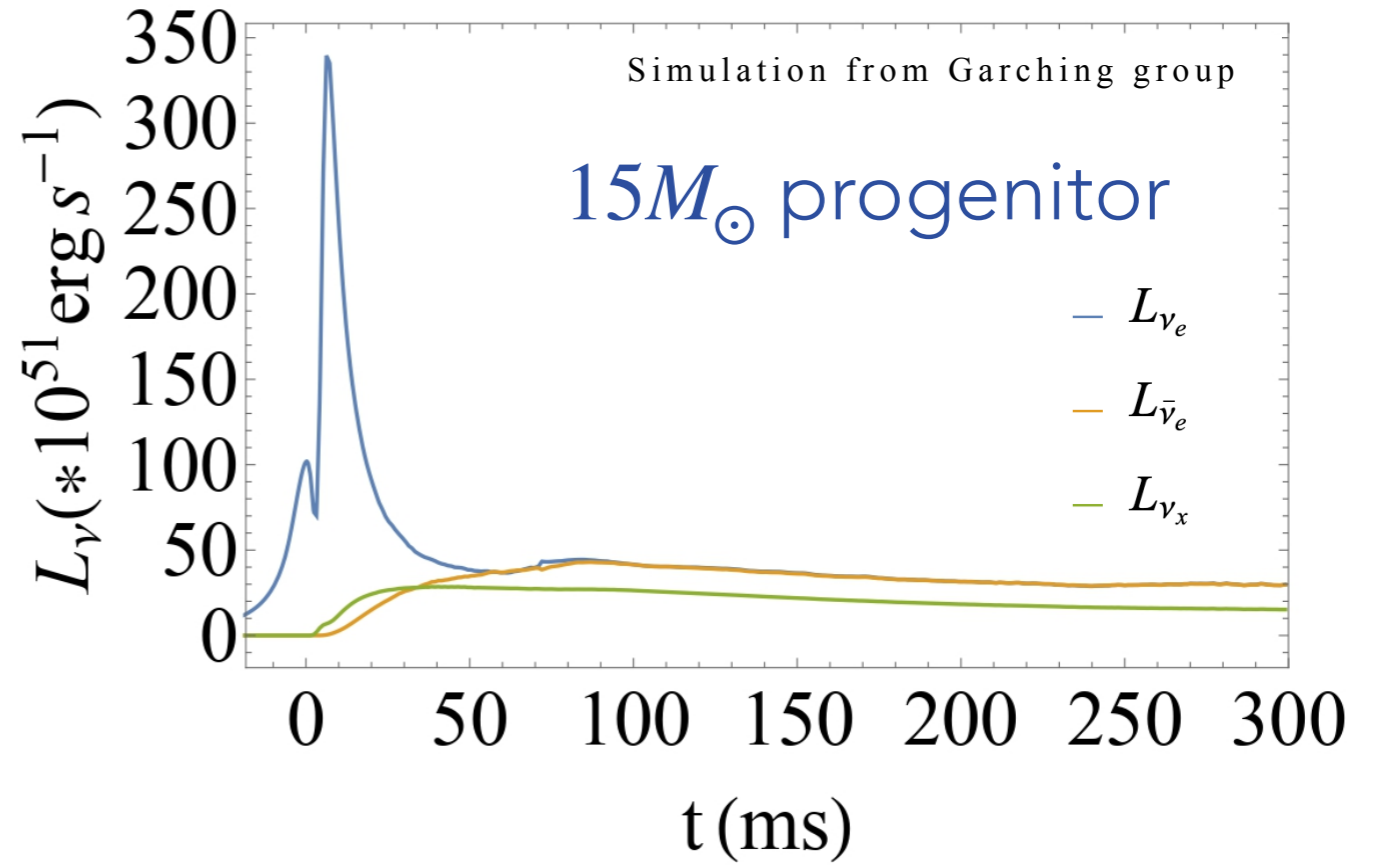
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# Core-collapse Supernova



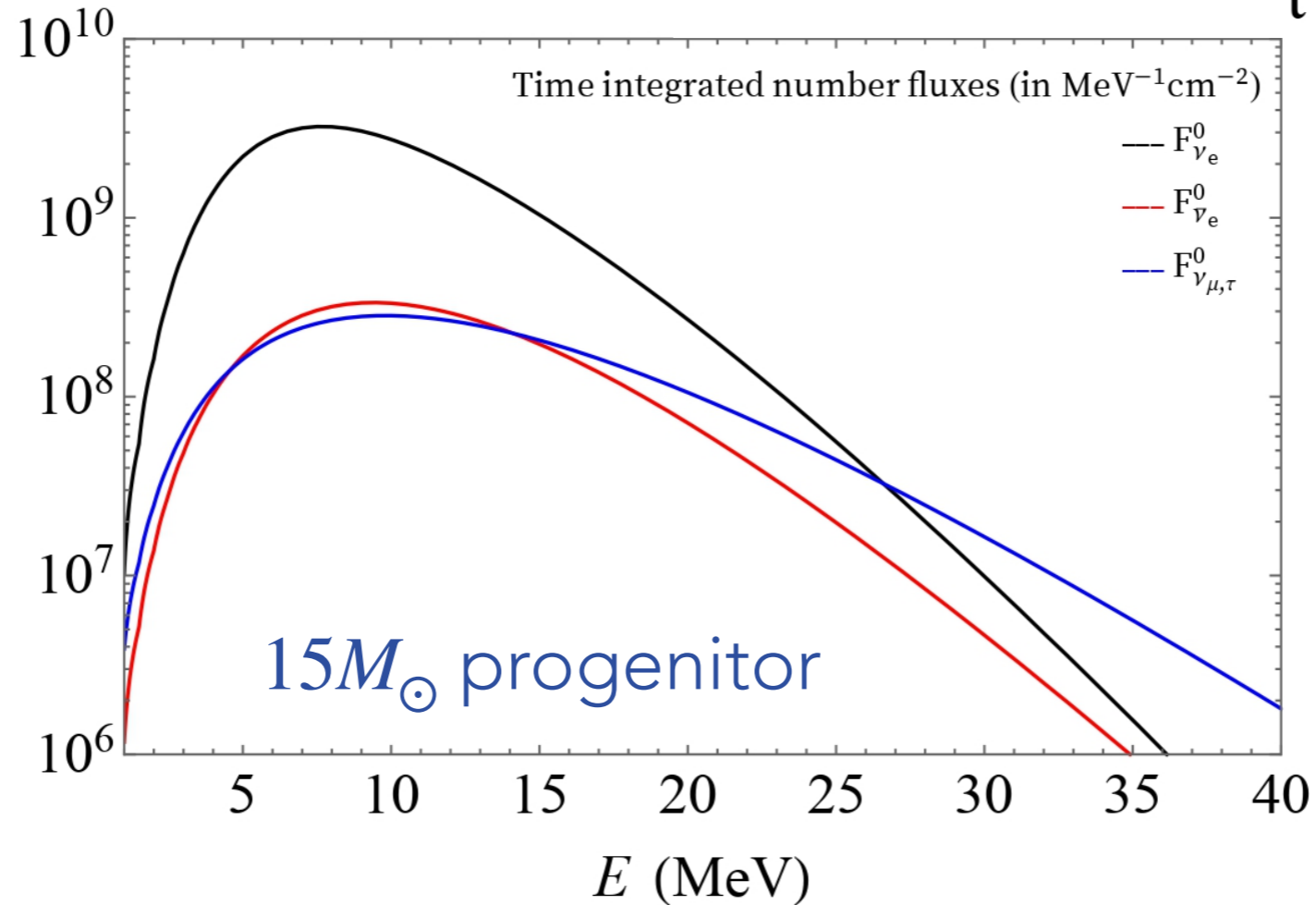
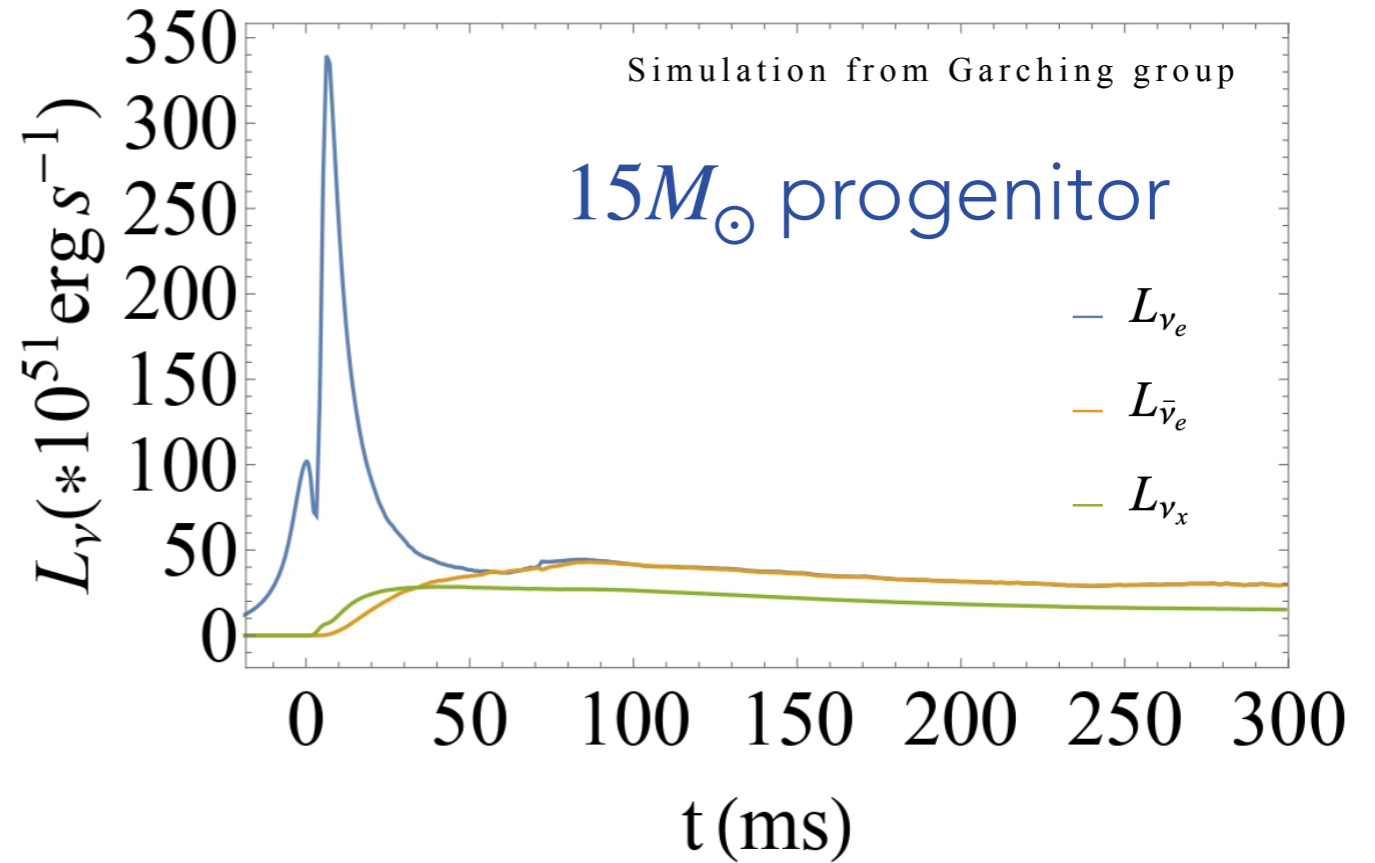
# Neutronization Burst

- It lasts for 30 ms after core bounce.
- Electron capture on protons leads to large burst of  $\nu_e$ .



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# *Flavor conversion in presence of neutrino magnetic moments*

- Transition magnetic moments:

$$\mathcal{L}_M \supset \mu_{\alpha\beta} \nu_{\alpha L}^T C \sigma_{\eta\delta} \nu_{\beta L} F^{\eta\delta}$$

- Neutrino evolution equation:

$$i \frac{d}{dr} \begin{pmatrix} \nu \\ \bar{\nu} \end{pmatrix} = \begin{pmatrix} H_\nu & B_\perp M \\ -B_\perp M & H_{\bar{\nu}} \end{pmatrix} \begin{pmatrix} \nu \\ \bar{\nu} \end{pmatrix}$$

- Neutrino Hamiltonian in matter:

$$H_\nu = \frac{1}{2E} U \begin{pmatrix} 0 & 0 & 0 \\ 0 & \Delta m_{21}^2 & 0 \\ 0 & 0 & \Delta m_{31}^2 \end{pmatrix} U^\dagger + \begin{pmatrix} V_{\nu_e} & 0 & 0 \\ 0 & V_{\nu_\mu} & 0 \\ 0 & 0 & V_{\nu_\tau} \end{pmatrix}$$

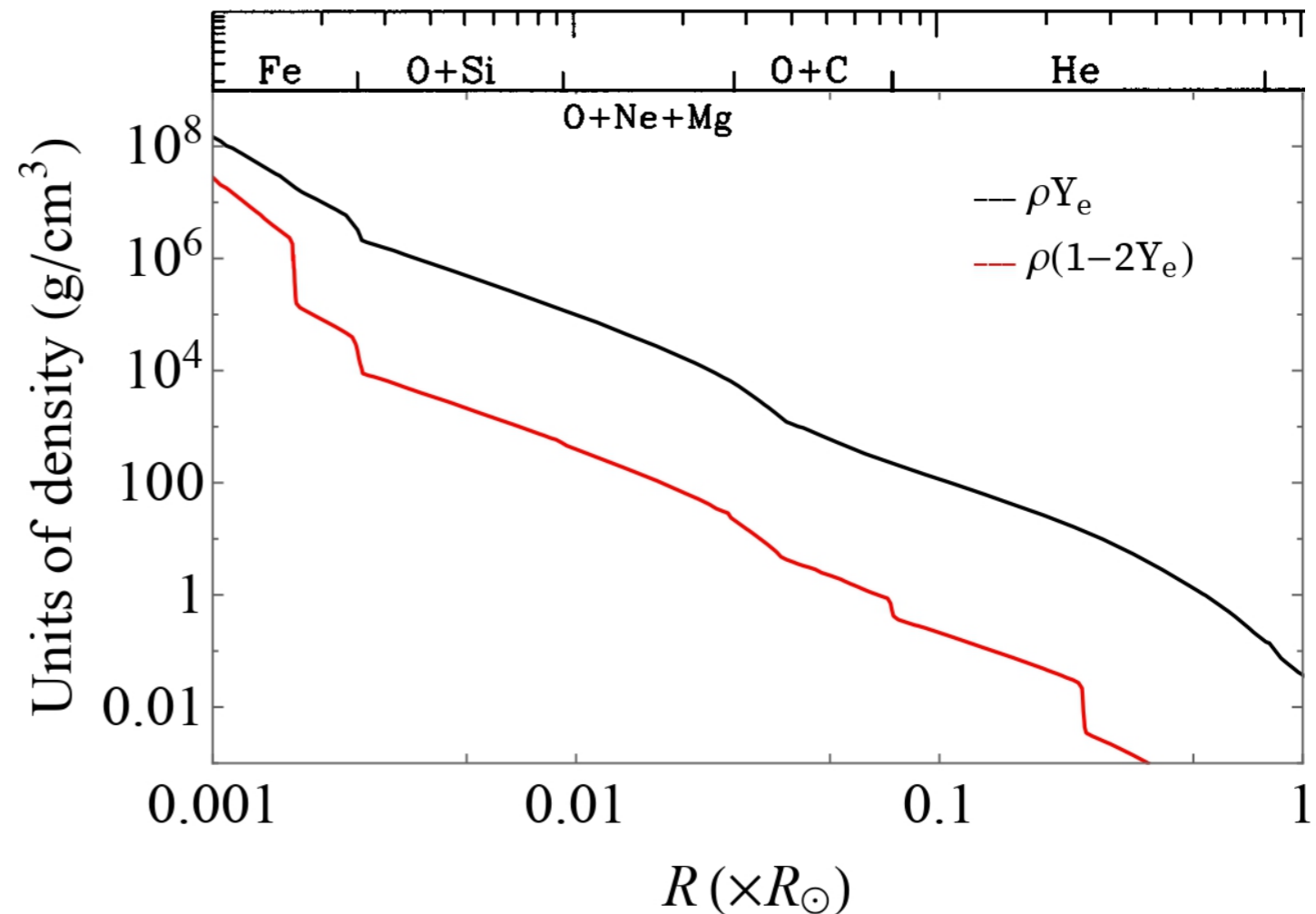
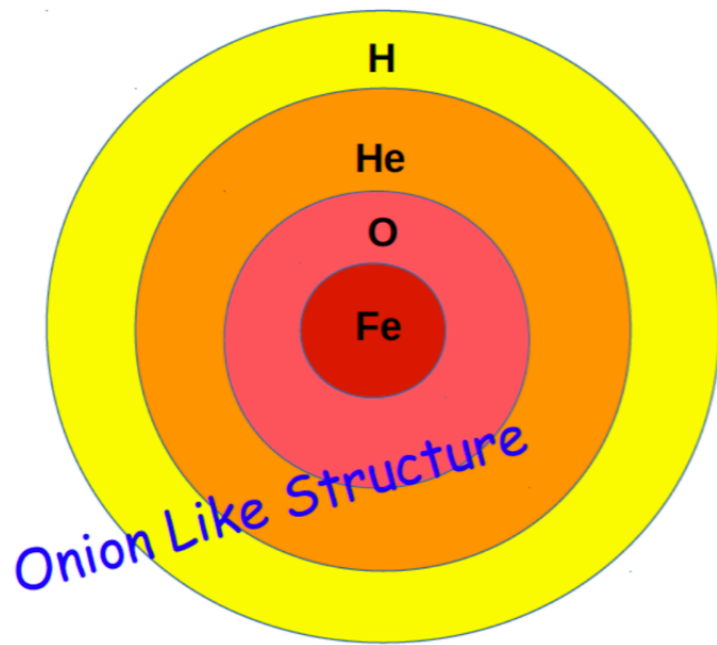
# Flavor conversion in presence of neutrino magnetic moments

- Transition magnetic moments:

$$M = \begin{pmatrix} 0 & \mu_{e\mu} & \mu_{e\tau} \\ -\mu_{e\mu} & 0 & \mu_{\mu\tau} \\ -\mu_{e\tau} & -\mu_{\mu\tau} & 0 \end{pmatrix}$$

- Magnetic field:

$$B_{\perp} = B_0 \left( \frac{r_0}{r} \right)^3$$



Woosley, Weaver, *Astrophys. J. Suppl.* 101 (1995) 181–235.

Ando, Sato, [arXiv:hep-ph/0211053](https://arxiv.org/abs/hep-ph/0211053)

Totani, Sato, [arXiv:astro-ph/9609035](https://arxiv.org/abs/astro-ph/9609035)

# Conditions for MSW and RSFP resonances

## MSW (Mikheyev-Smirnov-Wolfenstein)

Mikheyev, Smirnov (1986)

- MSW condition  
j=2 for L and j=3 for H:

$$\sqrt{2}G_F \frac{\rho}{m_N} Y_e \approx \frac{|\Delta m_{j1}^2|}{2E} \cos 2\theta_{1j}$$

- MSW-L/H adiabaticity  
parameter:

$$\gamma_{\text{MSW-H(L)}} = \frac{\sin^2 2\theta_{1j}}{\cos 2\theta_{1j}} \frac{\Delta m_{j1}^2}{2E} \left| \frac{1}{\rho Y_e} \frac{d(\rho Y_e)}{dr} \right|^{-1}$$

$$\nu_e \leftrightarrow \nu_\mu$$

$$\nu_e \leftrightarrow \nu_\tau$$

$$\bar{\nu}_e \leftrightarrow \bar{\nu}_\mu$$

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## RSFP (Resonant Spin-Flavour Precession)

- RSFP condition  
j=2 for L and j=3 for H:

$$\sqrt{2}G_F \frac{\rho}{m_N} (1 - 2Y_e) \approx \frac{|\Delta m_{j1}^2|}{2E} \cos 2\theta_{1j}$$

- RSFP-L/H adiabaticity  
parameter:

$$\gamma_{\text{RSFP-H(L)}} \simeq \frac{8E}{\Delta m_{j1}^2} (\mu_{e\beta'} B_\perp)^2 \left| \frac{1}{\rho(1 - 2Y_e)} \frac{d(\rho(1 - 2Y_e))}{dr} \right|^{-1}$$

- And we still have the RSFP-E (see Akhmedov & Fukuyama [arXiv:hep-ph/0310119](https://arxiv.org/abs/hep-ph/0310119))

$$\nu_e \leftrightarrow \bar{\nu}_\tau$$

$$\nu_e \leftrightarrow \bar{\nu}_\mu$$

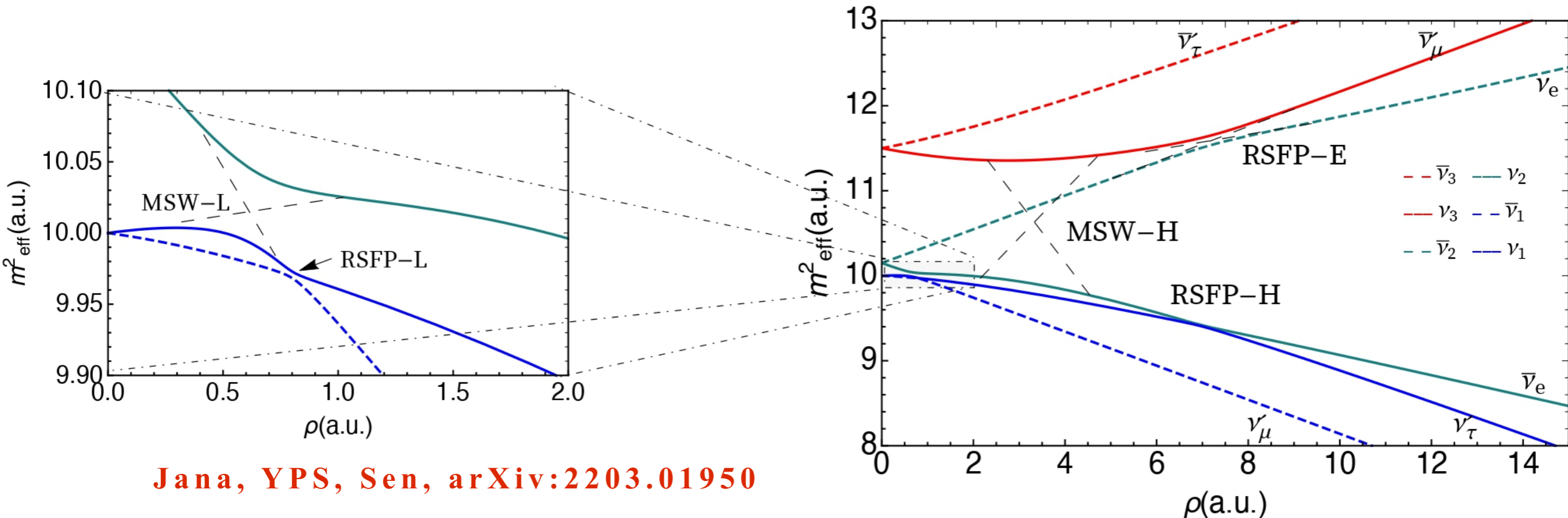
$$\bar{\nu}_e \leftrightarrow \nu_\mu$$

$$\bar{\nu}_e \leftrightarrow \nu_\tau$$

# Level crossing diagram (normal ordering)

- Five resonances: RSFP-H, RSFP-L (non-ad), RSFP-E (non-ad), MSW-H (ad) and MSW-L (ad).
- RSFP-H is partially adiabatic:  $0.5 \times 10^{-3} \mu_B G \lesssim \mu_\nu B_0 \lesssim 10^{-2} \mu_B G$
- Results depend on the hopping probability at RSFP-H:  $p_H = e^{-\frac{\pi}{2} \gamma_{RSFP-H}}$

$$\begin{aligned}
 F_{\nu_e} &= F_{\nu_e}^{MSW} - |U_{e2}|^2 (1 - p_H) (F_{\nu_x}^0 - F_{\bar{\nu}_e}^0) \\
 F_{\bar{\nu}_e} &= F_{\bar{\nu}_e}^{MSW} + |U_{e1}|^2 (1 - p_H) (F_{\nu_x}^0 - F_{\bar{\nu}_e}^0)
 \end{aligned}$$

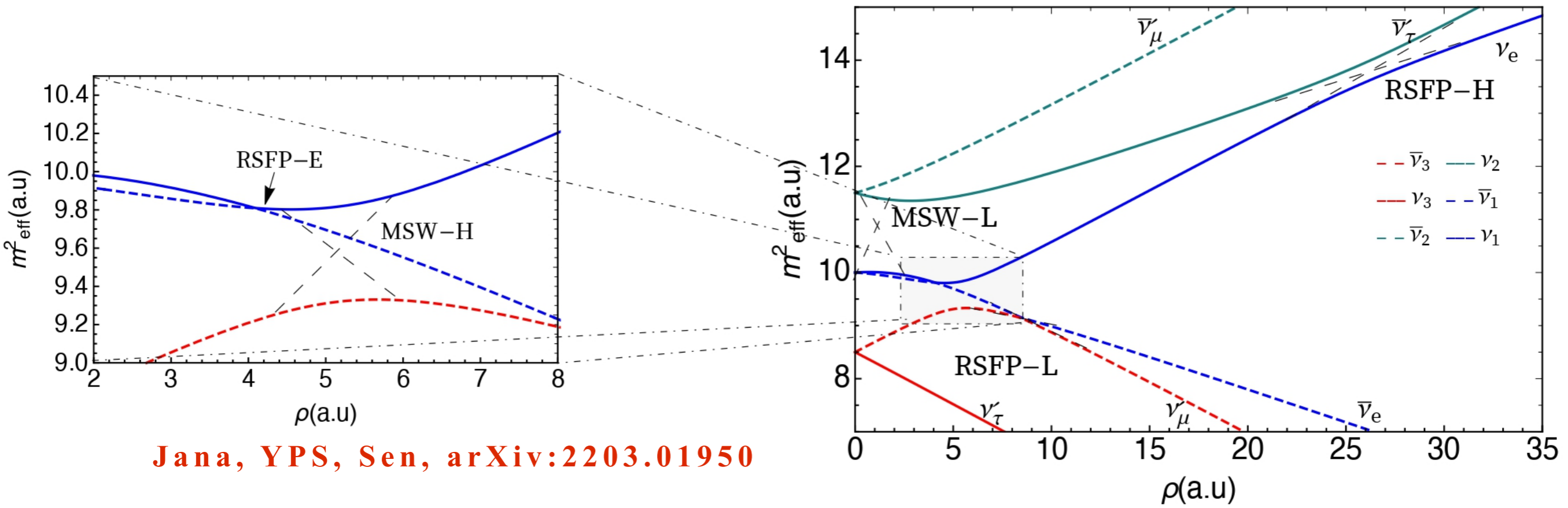


# Level crossing diagram (inverted ordering)

- Five resonances: RSFP-H, RSFP-L (non-ad), RSFP-E (non-ad), MSW-H (ad) and MSW-L (ad).
- RSFP-H is partially adiabatic:  $0.5 \times 10^{-3} \mu_B G \lesssim \mu_\nu B_0 \lesssim 10^{-2} \mu_B G$
- Results depend on the hopping probability at RSFP-H:  $p_H = e^{-\frac{\pi}{2} \gamma_{RSFP-H}}$

$$F_{\nu_e} = F_{\nu_e}^{MSW} - |U_{e2}|^2 (1 - p_H) (F_{\nu_e}^0 - F_{\nu_x}^0)$$

$$F_{\bar{\nu}_e} = F_{\bar{\nu}_e}^{MSW} + |U_{e1}|^2 (1 - p_H) (F_{\nu_e}^0 - F_{\nu_x}^0)$$



# Upcoming neutrino detectors

## DUNE

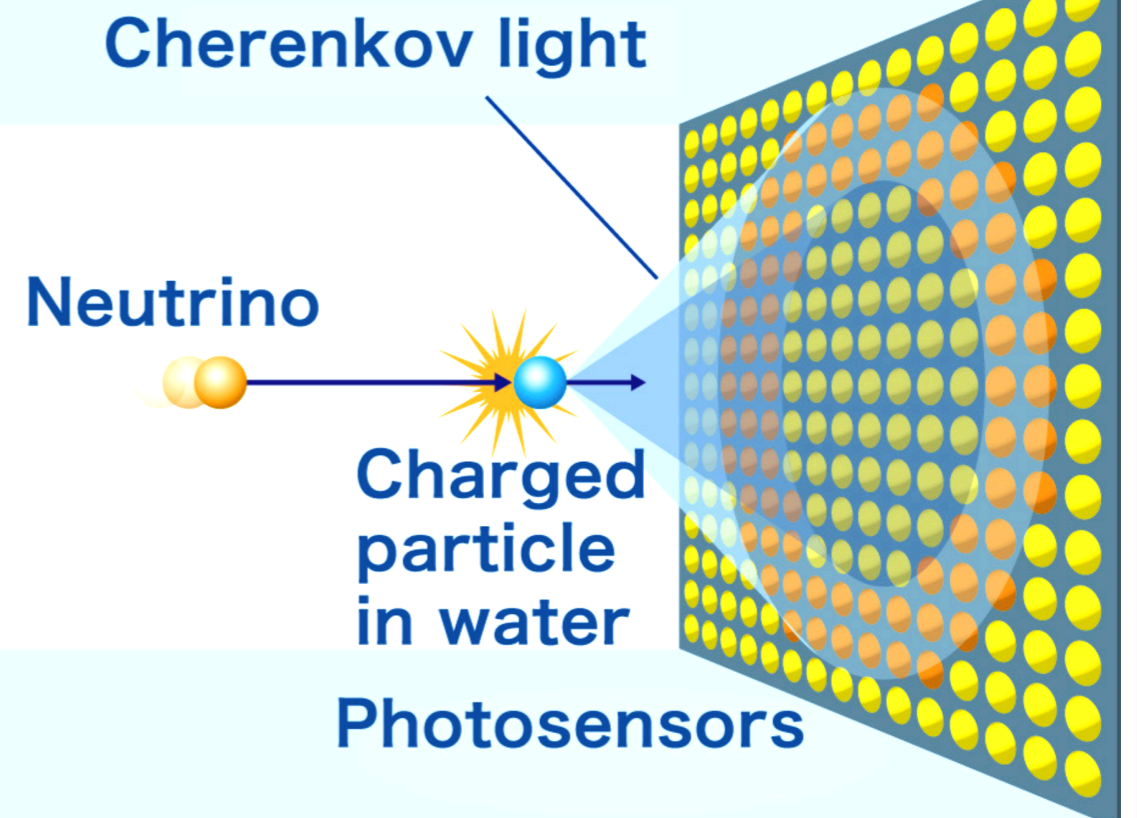
- 40-kton of liquid argon time projection chamber;
- $\nu_e + {}^{40}\text{Ar} \rightarrow {}^{40}\text{K}^* + e^-$ ;
- $\sigma_E/E_r \sim 5\%$  at 10 MeV.

DUNE FD1-HD simulation  
2.5 GeV,  $\nu_e + \text{Ar} \rightarrow e p \pi^0$

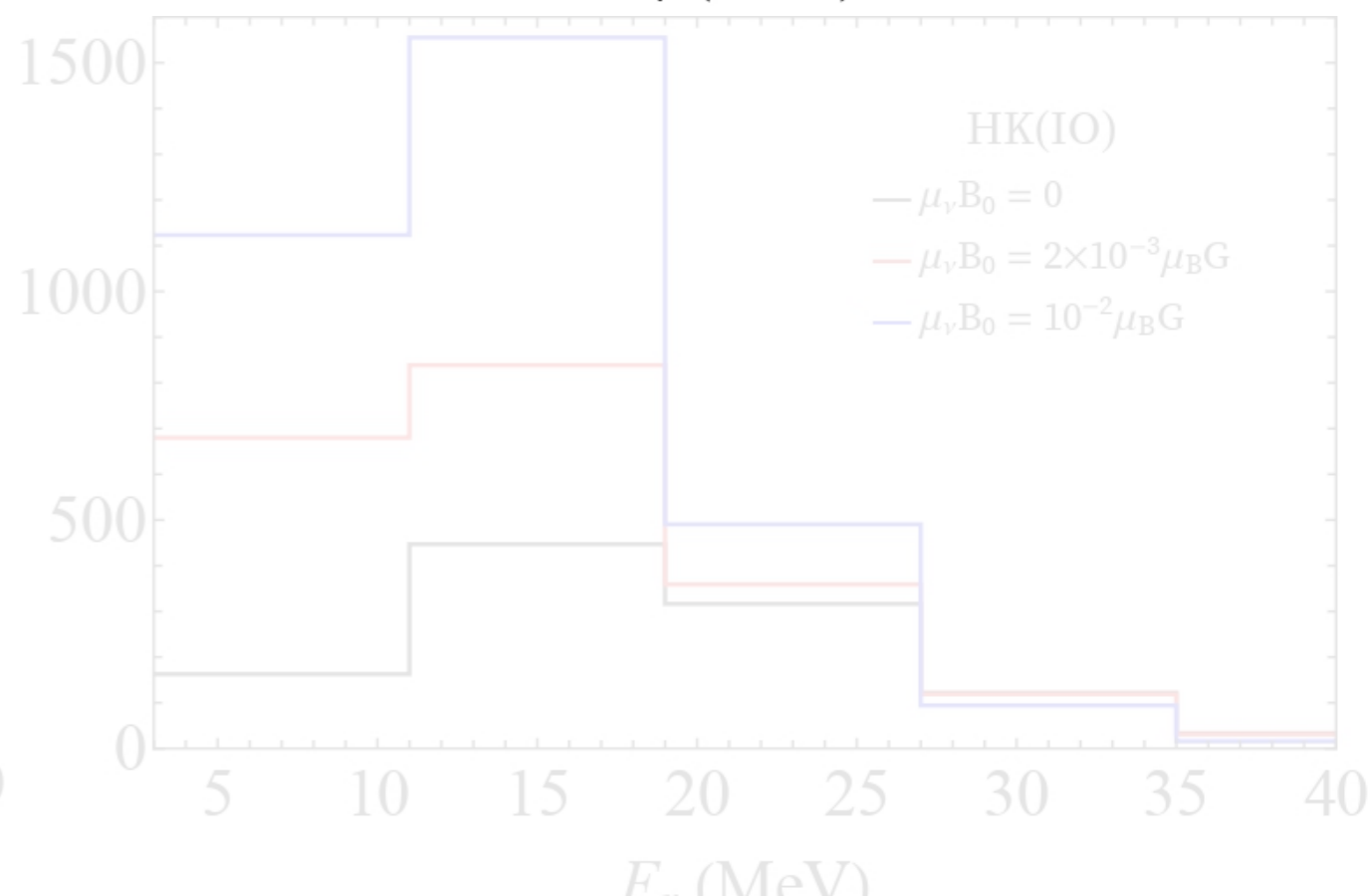
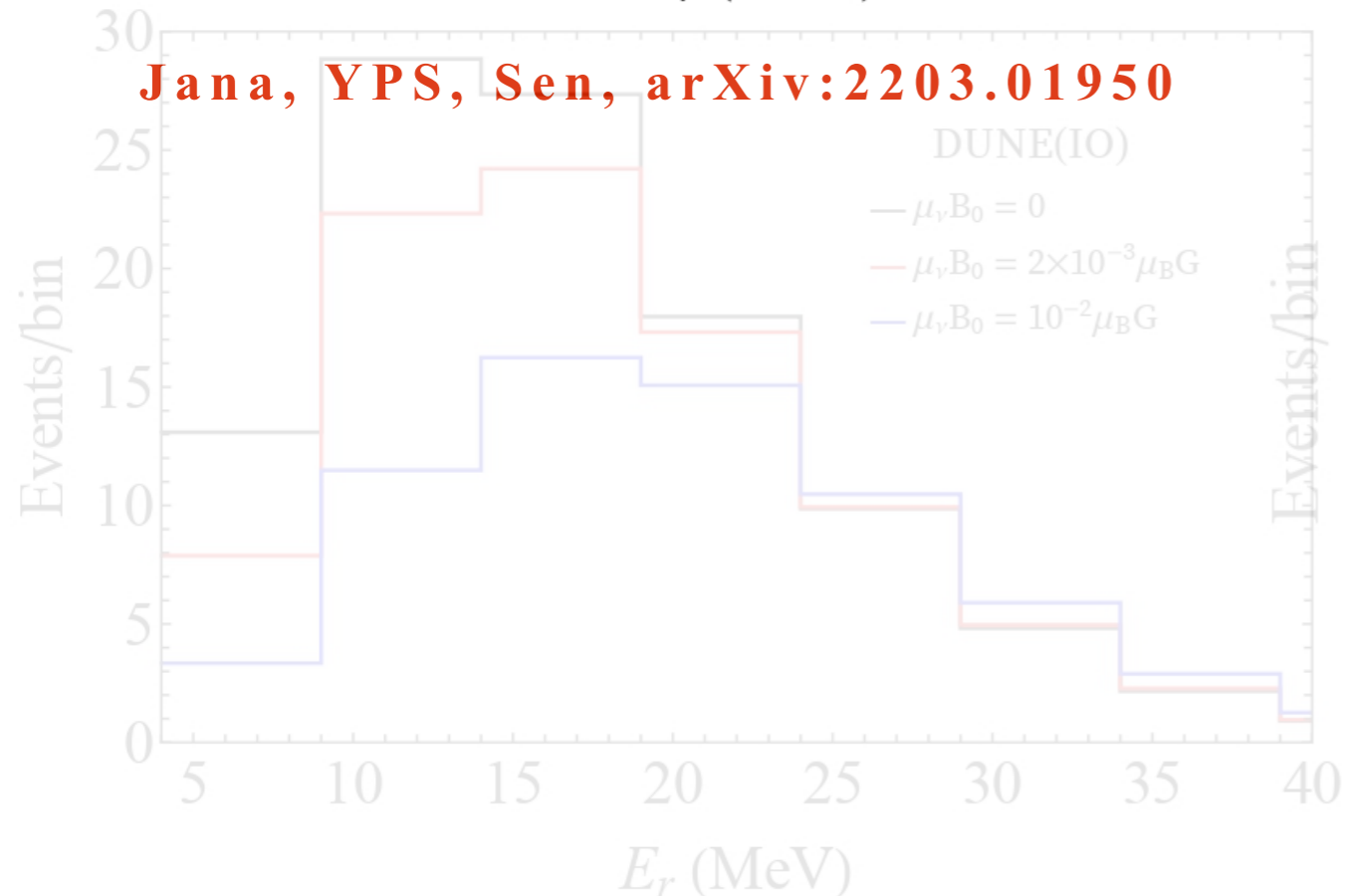
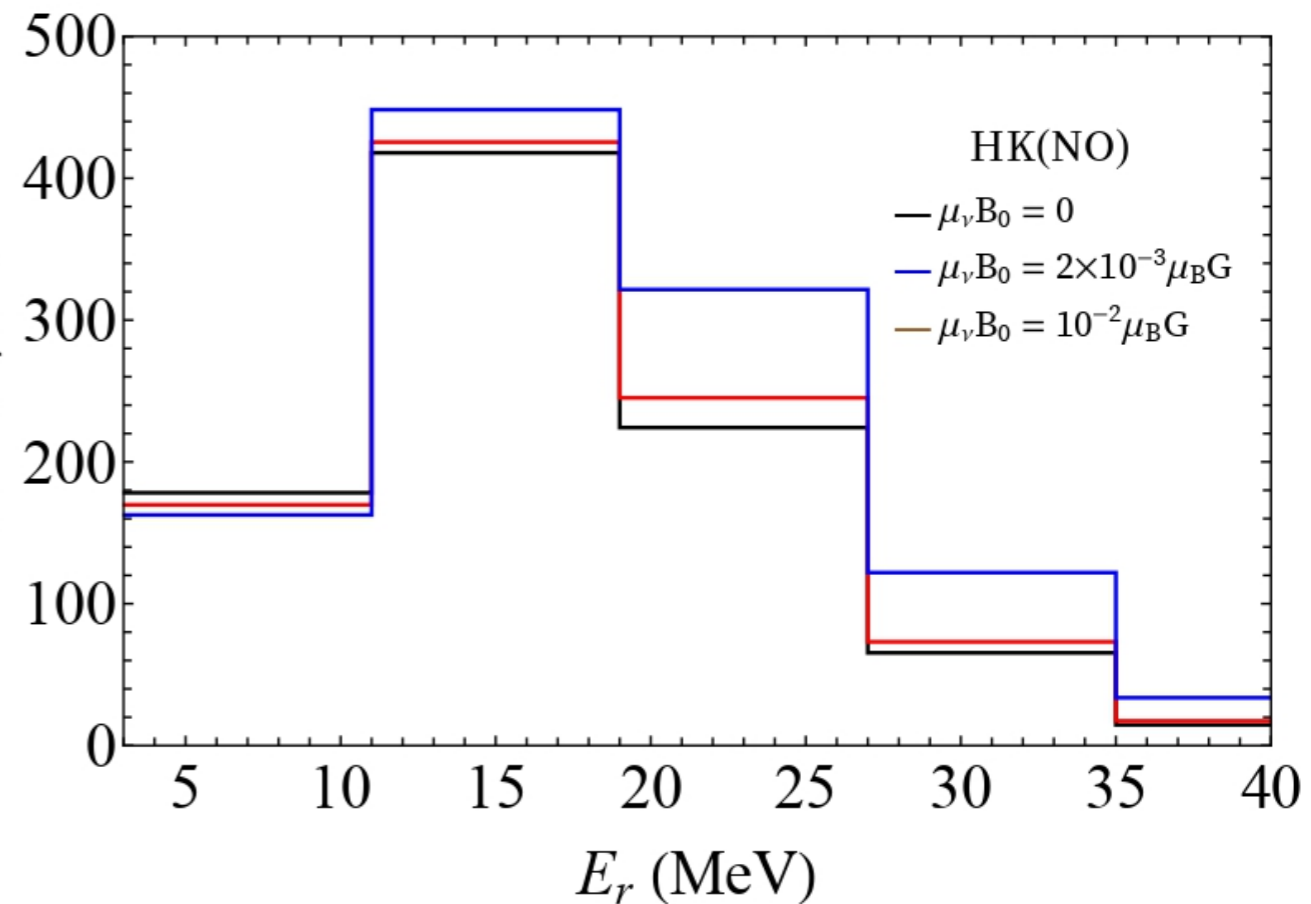
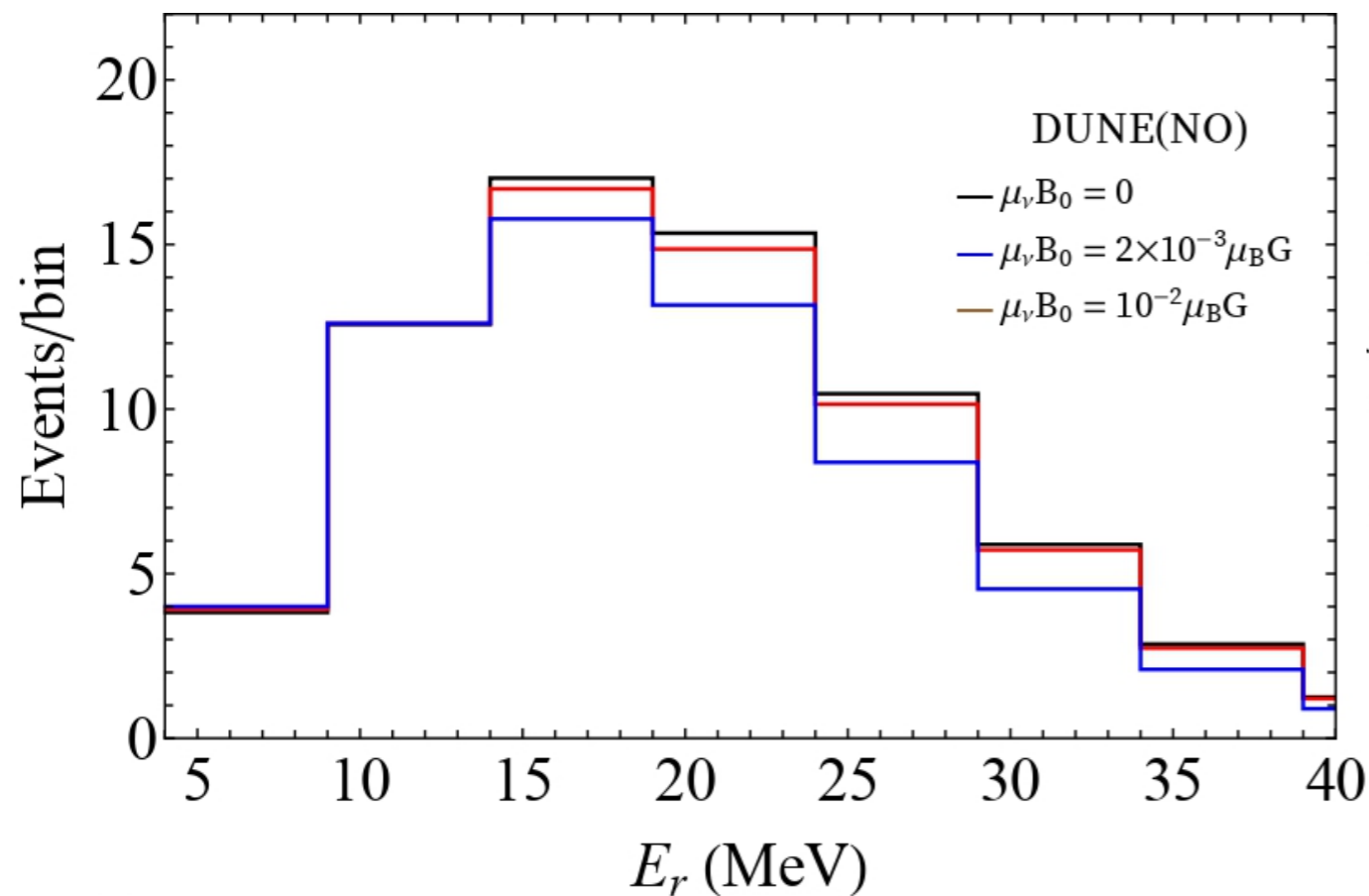


## HK

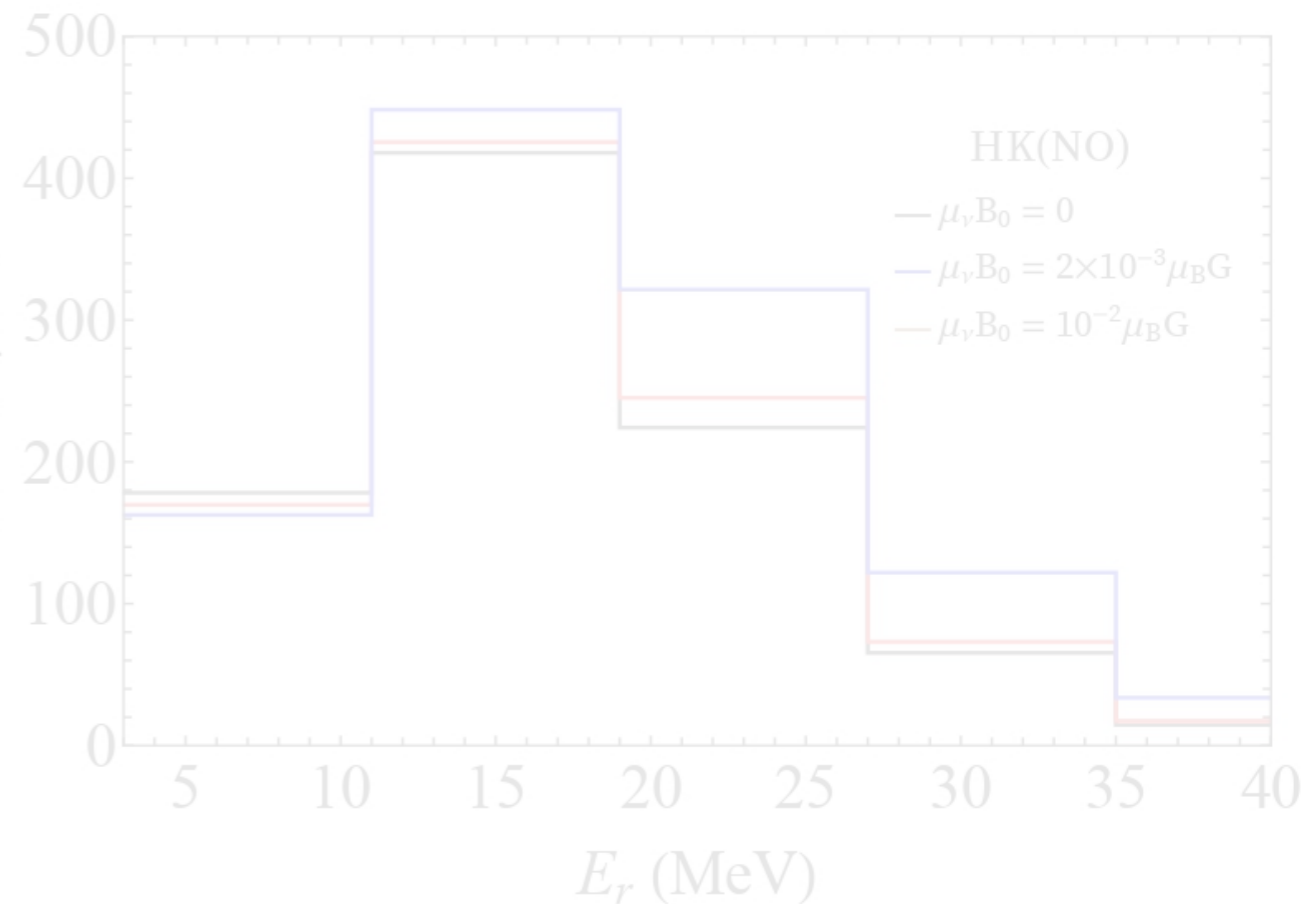
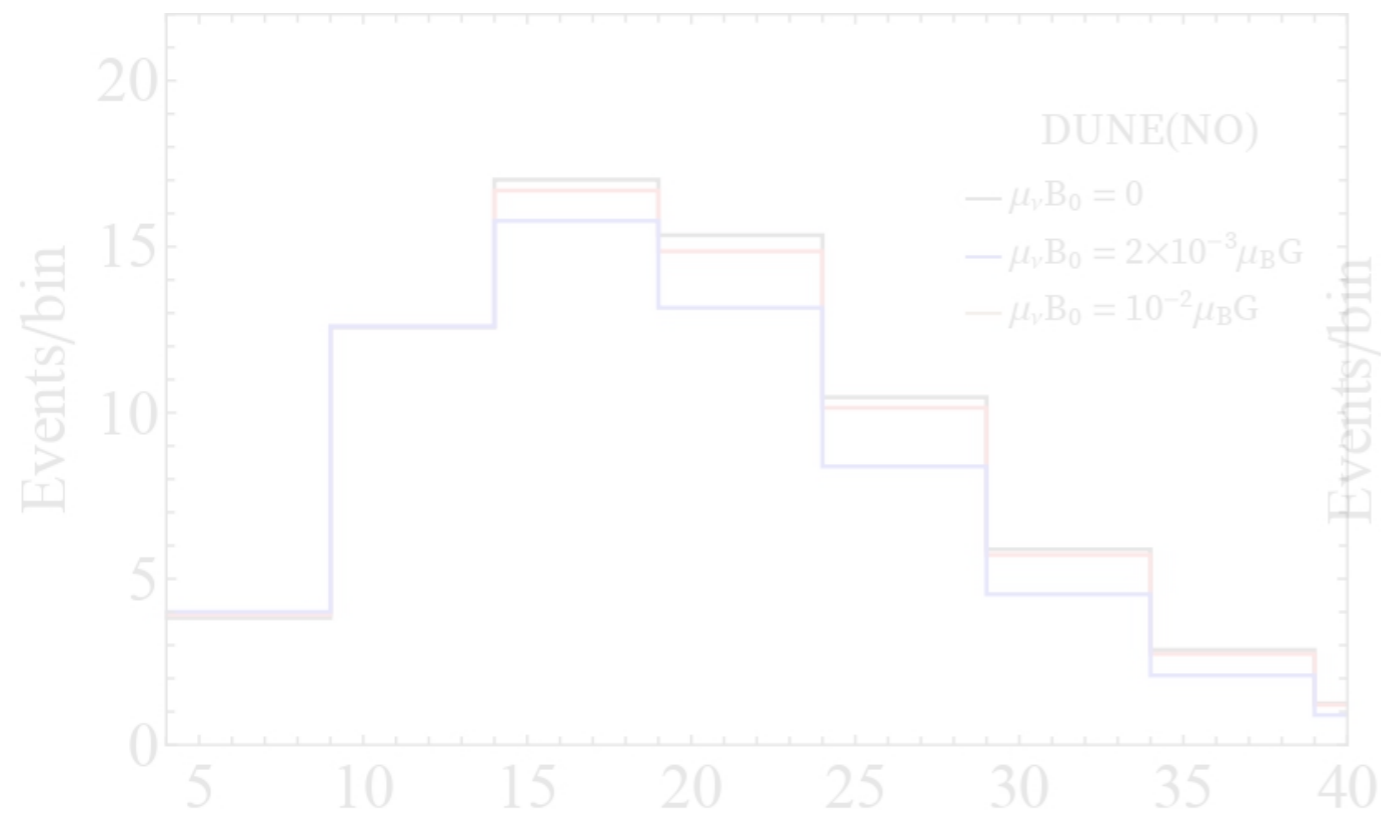
- Water cherenkov detector, fiducial volume 187 kt in each of two tanks;
- $\bar{\nu}_e + p \rightarrow e^+ + n$ ;
- $\sigma_E/E_r \sim 20\%$  at 10 MeV.



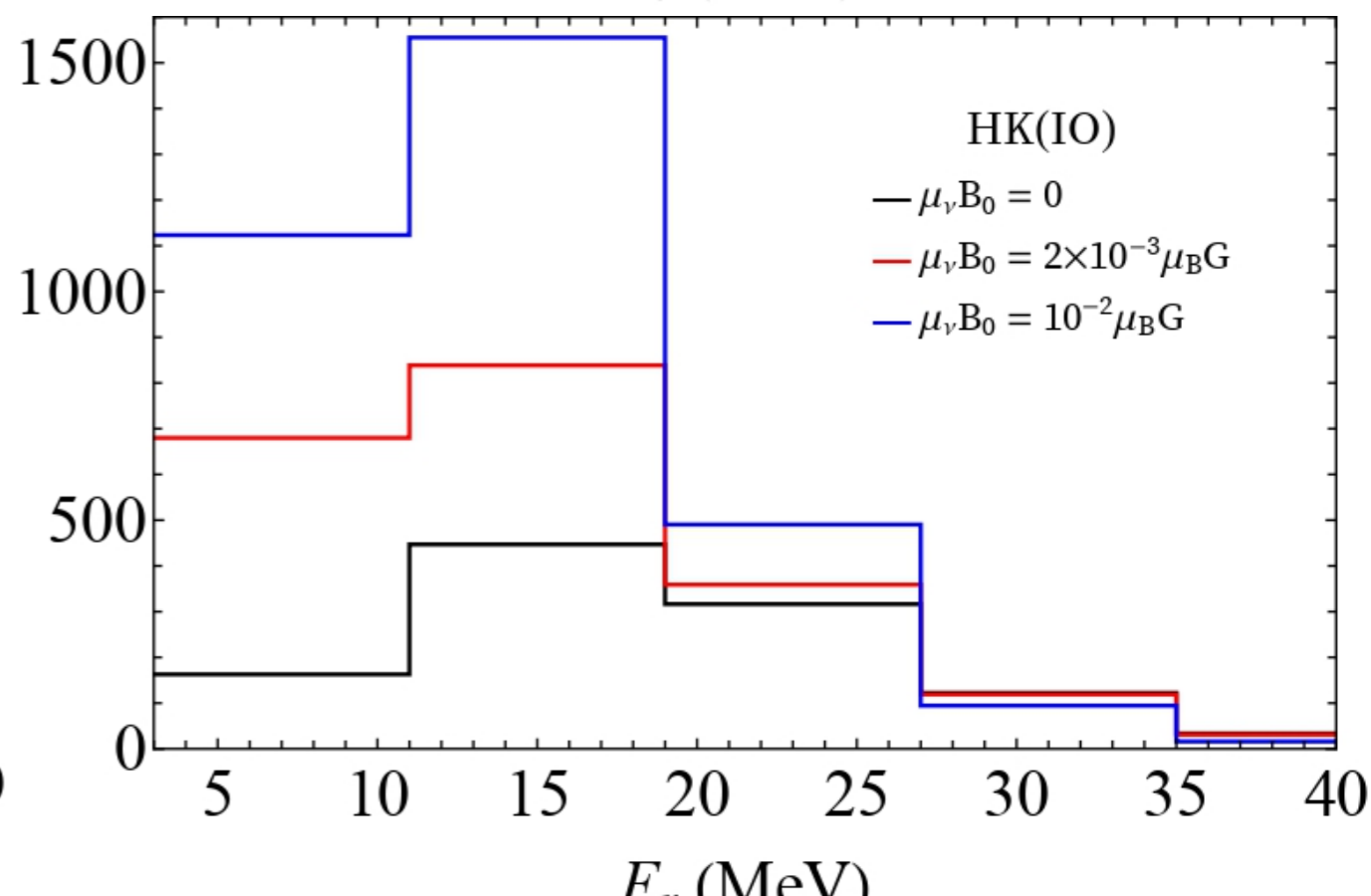
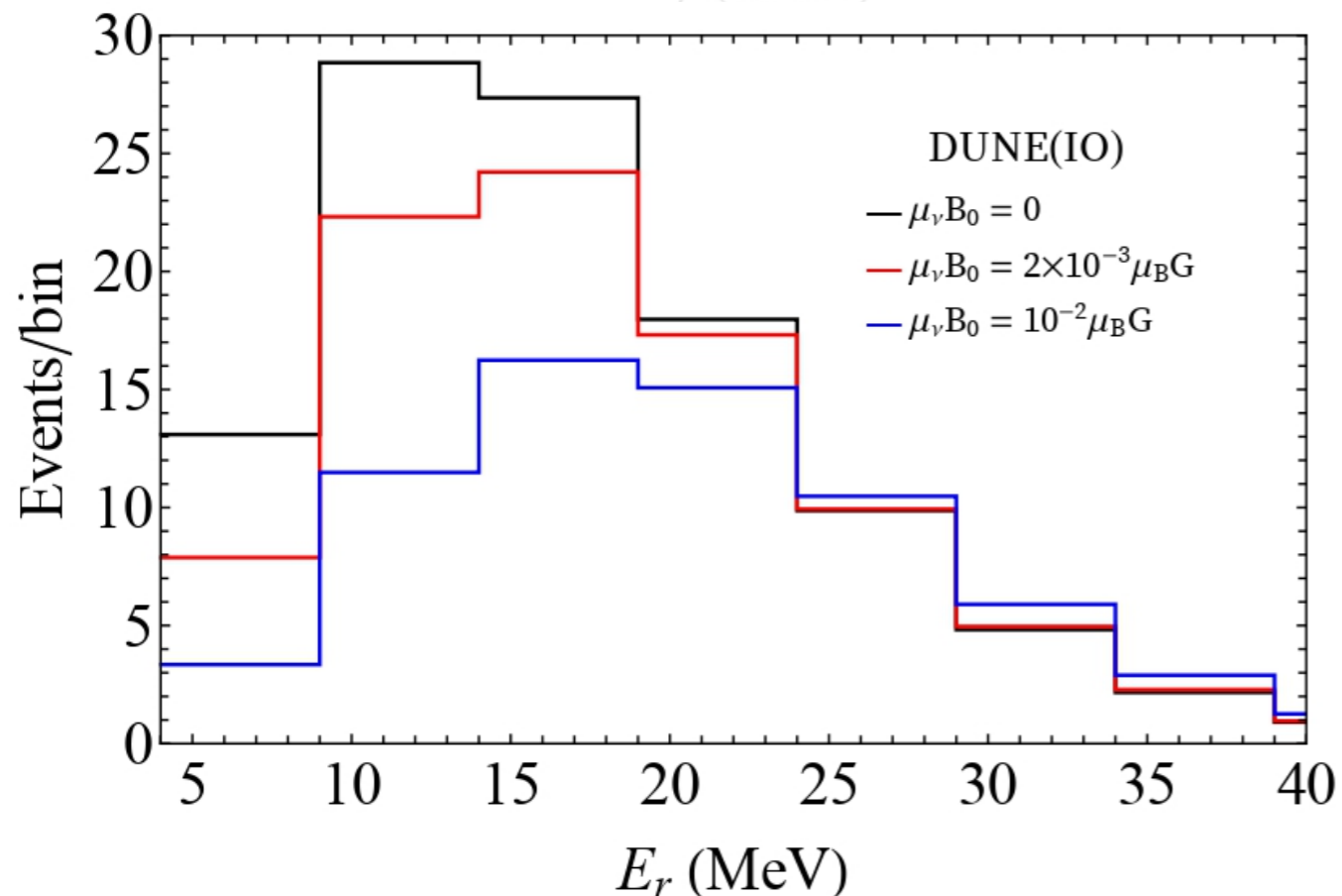
# *Event spectra (normal ordering)*



# *Event spectra (inverted ordering)*



**Jana, YPS, Sen, [arXiv:2203.01950](https://arxiv.org/abs/2203.01950)**



# *Neutrino magnetic moments sensitivities*

- For illustration: we set both  $\mu_{e\mu}$  and  $\mu_{e\tau}$  are equal, set to  $\mu_\nu$  (free parameter) for one benchmark point.
- We perform a  $\chi^2$  analysis assuming  $\mu_\nu = 0$  as the true hypothesis to find the sensitivities below (assuming  $B_0 = 10^{10}$  G and  $d = 10$  kpc):

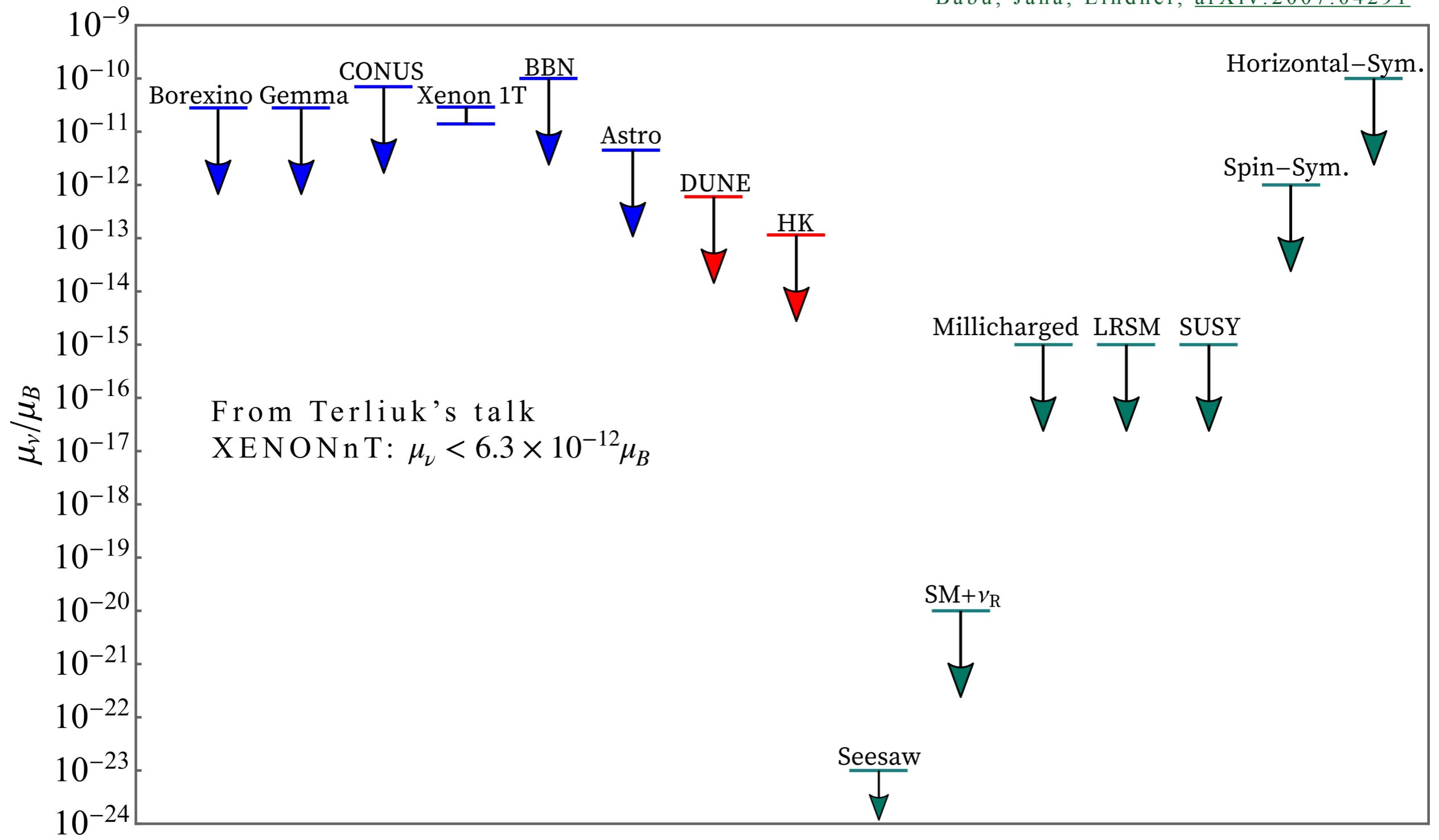
Sensitivities (in  $\mu_B$ )

<b>Experiments</b>	<b>NO</b>	<b>IO</b>
<b>HK</b>	$4.5 \times 10^{-13}$	$6 \times 10^{-14}$
<b>DUNE</b>	—	$3 \times 10^{-13}$

**Jana, YPS, Sen, arXiv:2203.01950**

# Summary of sensitivities

Babu, Jana, Lindner, [arXiv:2007.04291](https://arxiv.org/abs/2007.04291)



Jana, YPS, Sen, [arXiv:2203.01950](https://arxiv.org/abs/2203.01950)



## *Implication for neutrino properties*

- Dirac  $\mu_\nu$  over  $10^{-14}\mu_B$  would generate unacceptably large neutrino masses. Therefore, for the values of  $\mu_\nu$  considered here, more likely for neutrinos to be Majorana.
- Removing the photon line from the diagram that generates  $\mu_\nu$  a neutrino mass term is generated.

## *Take away message*

- Spin-flavor + MSW conversion leads to a suppression of  $\nu_e$  while enhancing  $\bar{\nu}_e$  spectra during neutronization burst phase.
- For a galactic SN, DUNE and HK can probe  $\mu_\nu$  from  $O[10^{-11}]\mu_B$  up to  $O[10^{-14}]\mu_B$ .
- The detection of these values of  $\mu_\nu$  can shed light on the neutrino nature and its mass mechanism.

*Thank you!*