

# Parker Bound and Monopole Pair Production from Primordial Magnetic Fields



**Speaker:**  
**Daniele Perri**

[arXiv:2207.08246](https://arxiv.org/abs/2207.08246)



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25-29 JULY 2022 - MPIK - HEIDELBERG - GERMANY

# Contents of the Talk

- ✓ Magnetic monopoles and topological defects.
- ✓ Bounds on the monopole abundance.
- ✓ Schwinger effect and monopole pair production.
- ✓ Conclusion.

D. Perri, T. Kobayashi (2022)  
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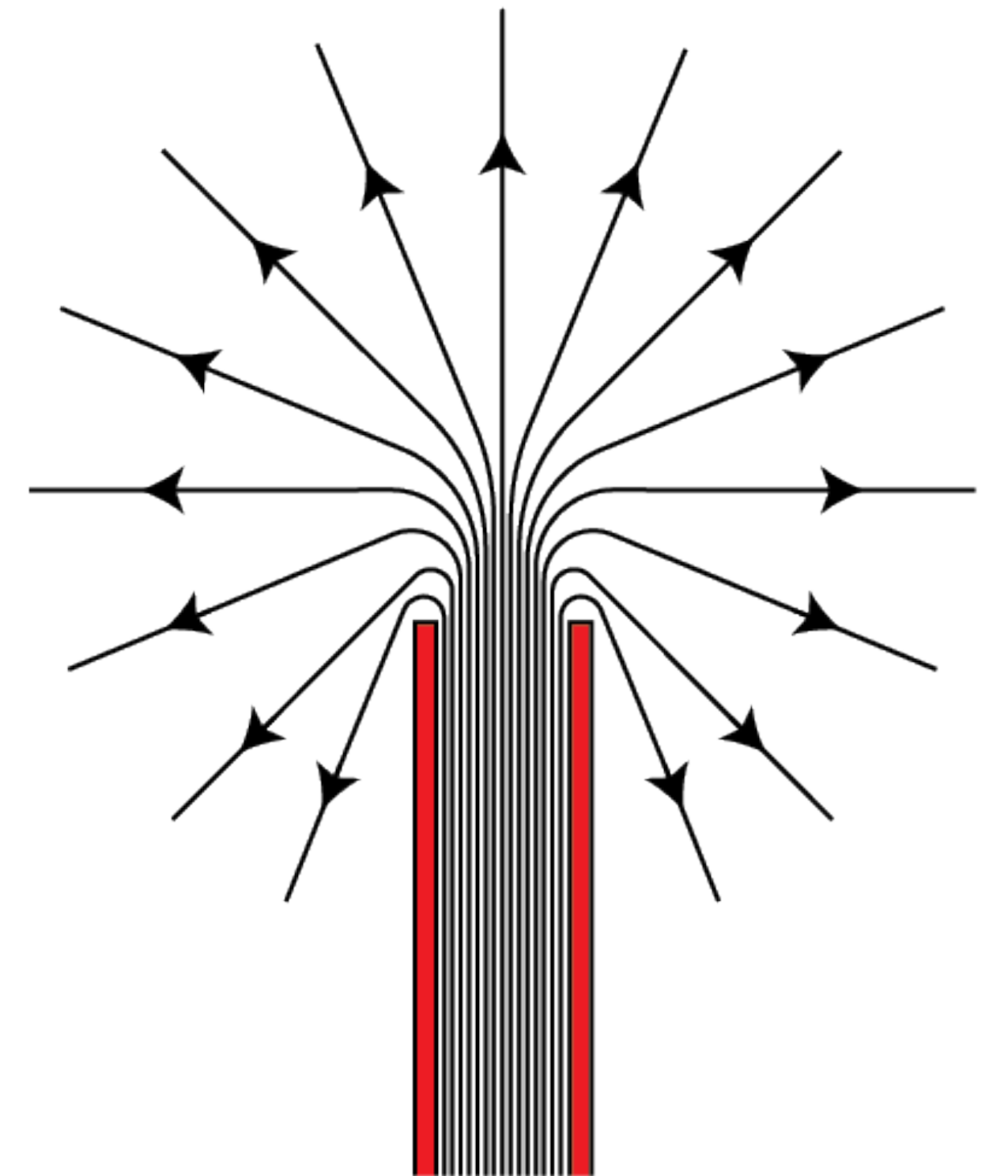


# Can a Monopole Really Exist?

## Dirac Monopoles and the Quantization of the Electric Charge

- Dirac was the first to suppose the existence of magnetic monopoles.
- In 1948 he proposed a model for a monopole made of *one semi-infinite string solenoid*.
- The existence of magnetic monopoles is consistent with quantum theory once imposed the *charge quantization condition*:
$$g = 2\pi n/e$$
- Monopoles provides a strong theoretical explanation for the quantization of the electric charge.

$$\vec{B}_{\text{mono}} = g \frac{\vec{r}}{r^3}$$



# Can a Monopole Really Exist?

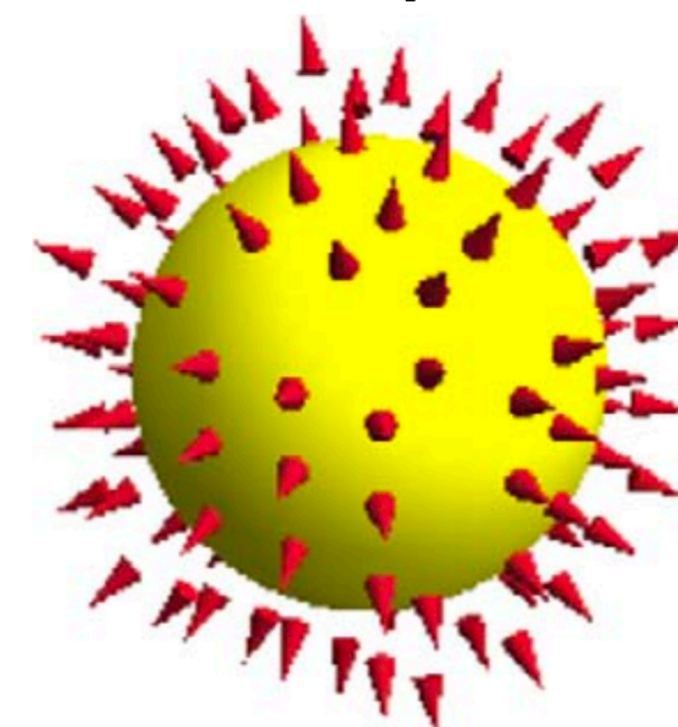
## 'T Hooft-Polyakov Monopoles and Topological Defects

- In 1974 'T Hooft and Polyakov presented a model of monopoles as zero-dimensional solitonic solutions of the vacuum manifold.
- The simplest example is the Georgi-Glashow model:  $SU(2) \rightarrow U(1)$

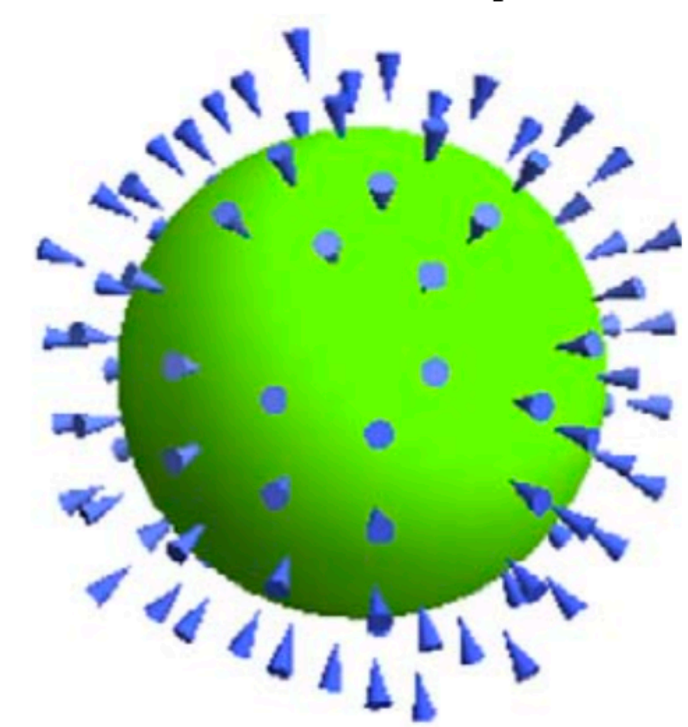
$$\mathcal{L}(t, \vec{x}) = -\frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} + \frac{1}{2} (D_\mu \phi^a) (D^\mu \phi^a) - \frac{1}{4} \lambda (\phi^a \phi^a - \eta^2)^2$$

- The monopole configuration is described by the *hedgehog solution* for the scalar field after the symmetry breaking:

$$\phi^a(\vec{x}) = \delta_{ia} \left( \frac{x^i}{r} \right) F(r)$$



$$Q_m = +1$$



$$Q_m = -1$$

# Can a Monopole Really Exist?

## 'T Hooft-Polyakov Monopoles and Topological Defects

- 'T Hooft-Polyakov monopoles can be interpreted as *topological defects* linked to non-trivial second homotopy groups of the vacuum manifold:

$$\pi_2(G/H) \neq \mathbf{I}$$

*Each time a simply connected group is broken into a smaller group that contains U(1) there is production of monopoles.*



Monopoles are *inevitable predictions* of Grand Unified Theories:

$$\text{SU}(5) \rightarrow \text{SU}(3) \times \text{SU}(2) \times \text{U}(1) \rightarrow \text{SU}(3) \times \text{U}(1)$$

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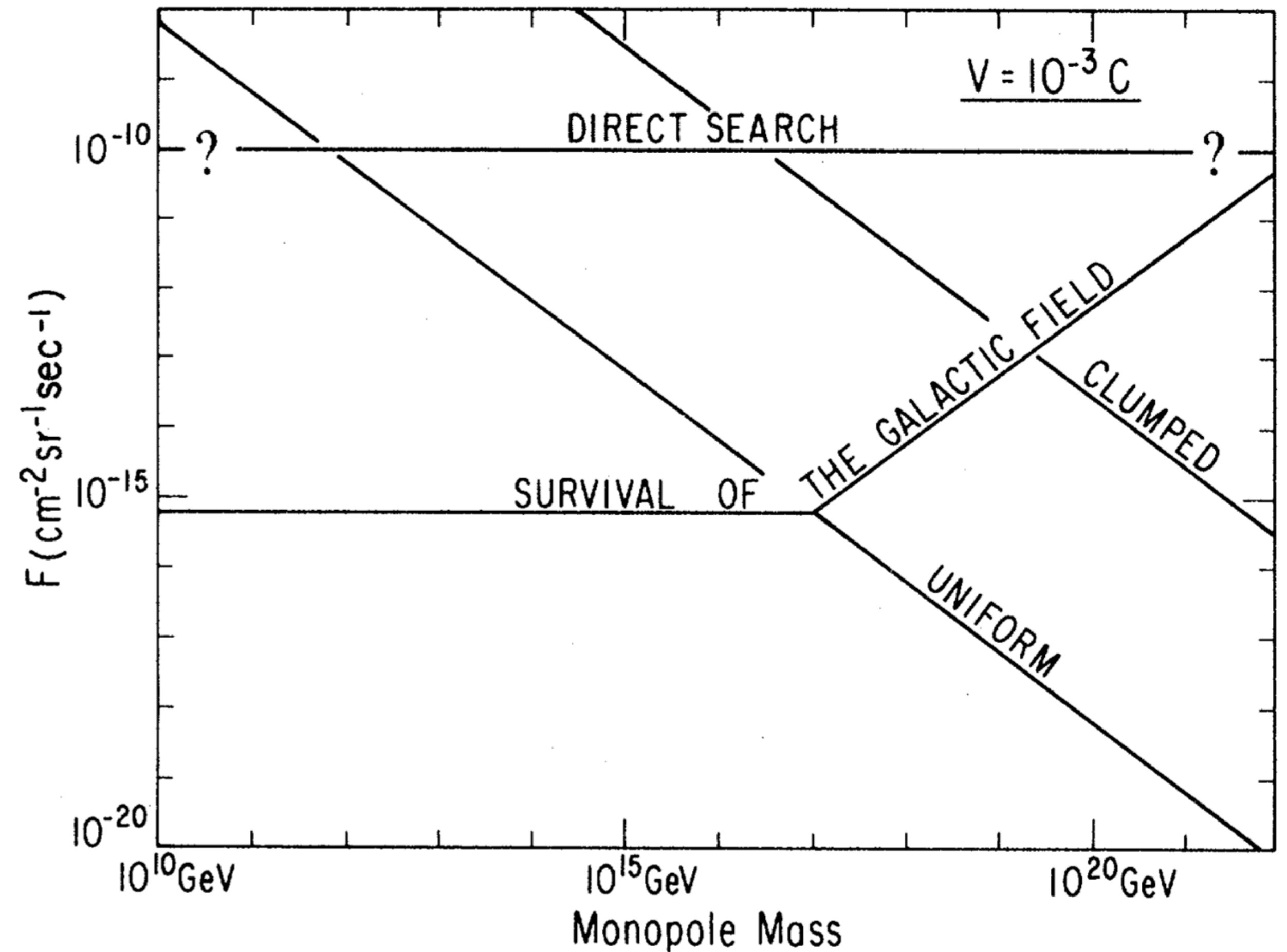
D. Perri, T. Kobayashi (2022)  
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# Parker Bound on the Monopole Flux

In 1970 Parker proposed a bound on the monopole flux today inside our galaxy:

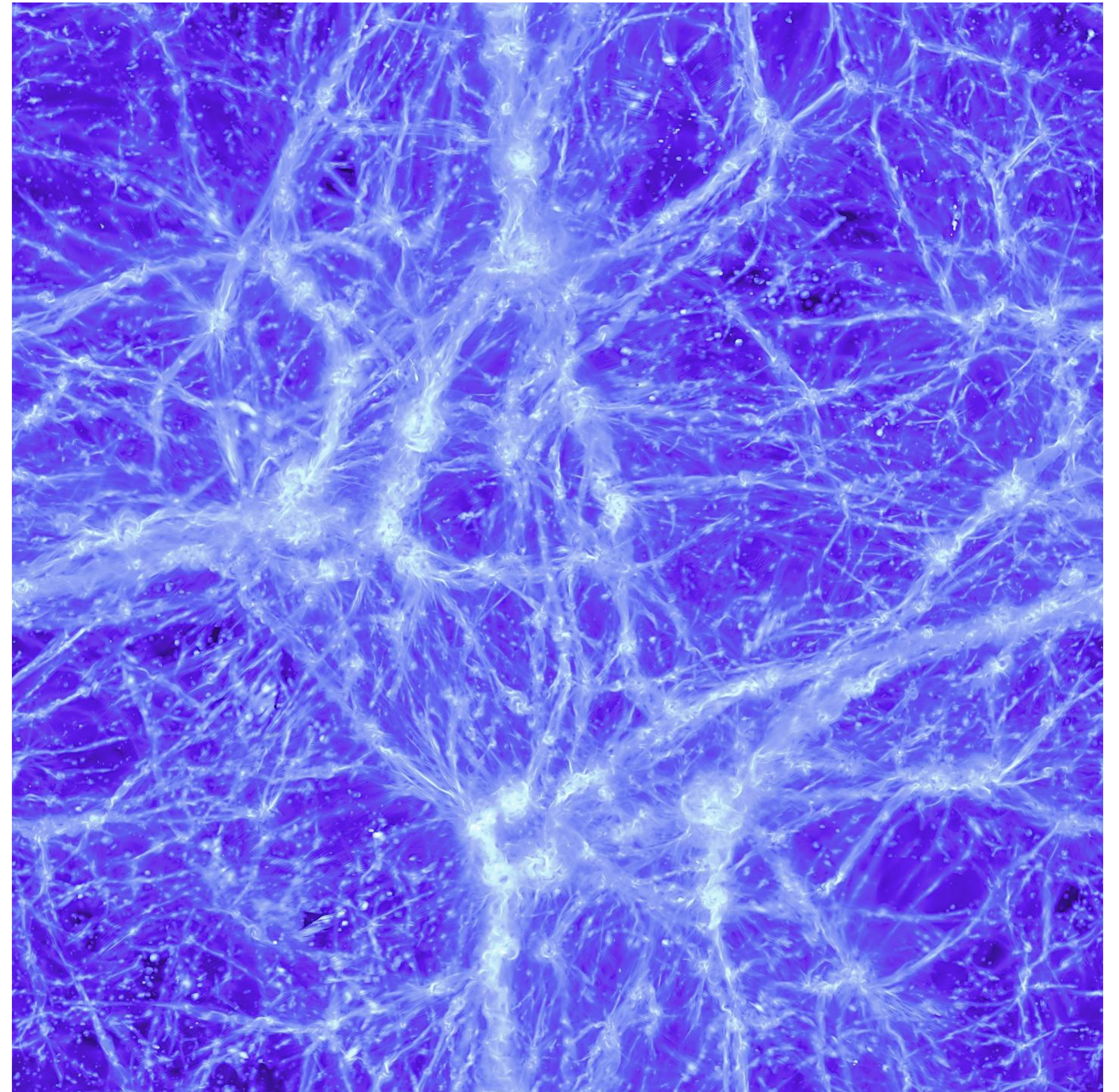
- The galaxy presents a magnetic field of  $\sim 10^{-5}$  G;
- The galactic magnetic field accelerates the monopoles losing its energy;
- The survival of the field provides a bound on the monopole flux today.



# New Parker Bounds from Primordial Magnetic Fields

- Strong evidences for intergalactic magnetic fields  $\gtrsim 10^{-15}$  G with a *primordial origin*.
- (Most of the) models of magnetogenesis provides that the production happens during inflation or soon after the end.

*An analogous of the Parker bound can be derived from the persistence of the primordial fields until today.*





# New Parker Bounds from Primordial Magnetic Fields

- The process of monopole acceleration extracts energy also from the primordial magnetic fields.
- The evolution of the *magnetic field energy density* in the presence of monopoles is described by the equation:

$$\frac{\dot{\rho}_B}{\rho_B} = -\Pi_{\text{red}} - \Pi_{\text{acc}}$$
$$\Pi_{\text{red}}(t) = 4H(t) \qquad \Pi_{\text{acc}}(t) = \frac{4g}{B(t)} v(t)n(t)$$

- The magnetic fields survive under the condition  $\Pi_{\text{acc}}/\Pi_{\text{red}} \lesssim 1$ .

*Necessary to study the equation of motion of the monopoles!!*

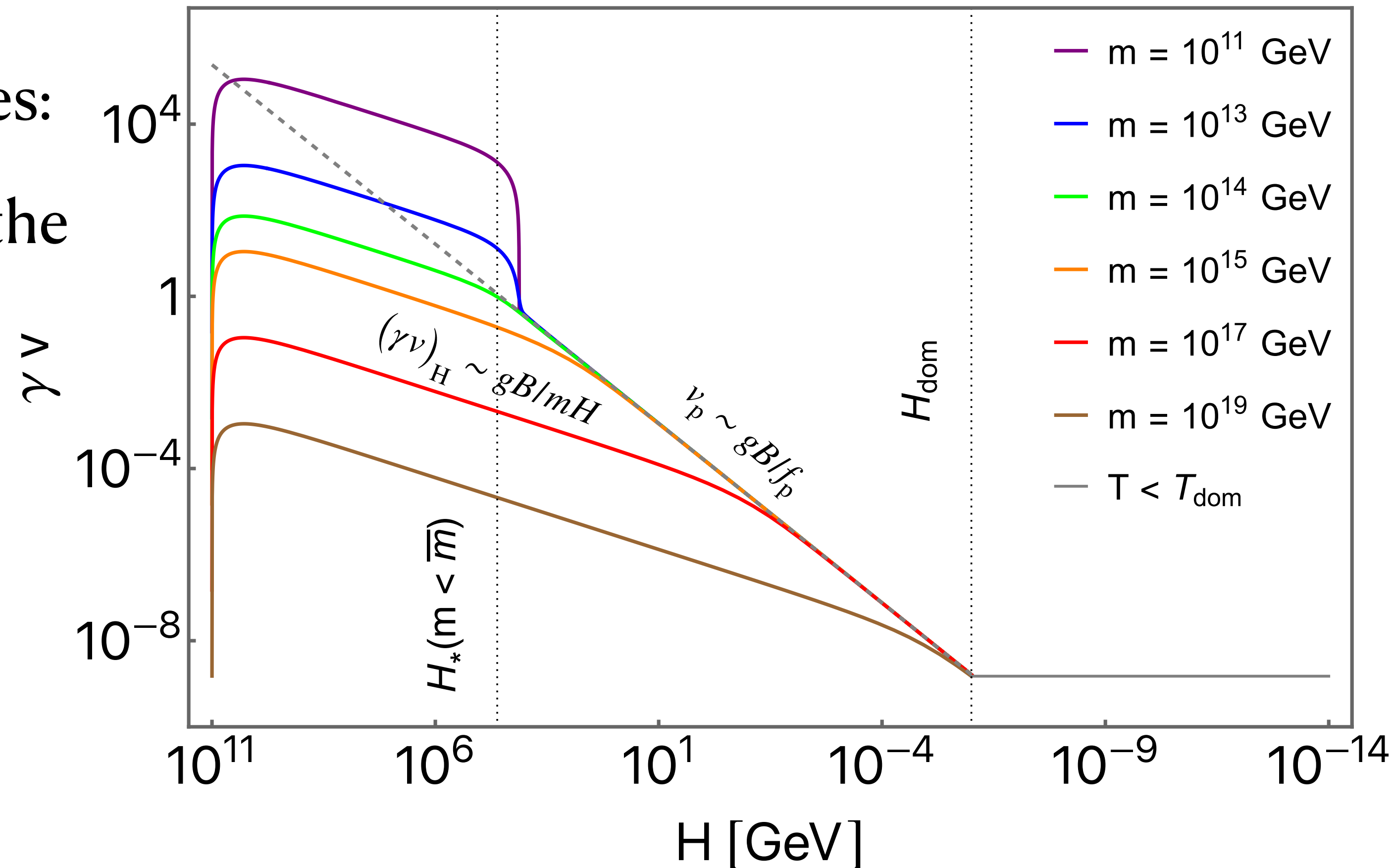
# The Equation of Motion of the Monopoles

$$m \frac{d}{dt}(\gamma v) = gB - (f_p + mH\gamma) v$$

Two external forces act on the monopoles:

- $gB$ , the *magnetic force* that accelerates the monopoles;
- $-f_p v$ , the *frictional force* due to the interaction with the particles of the primordial plasma.

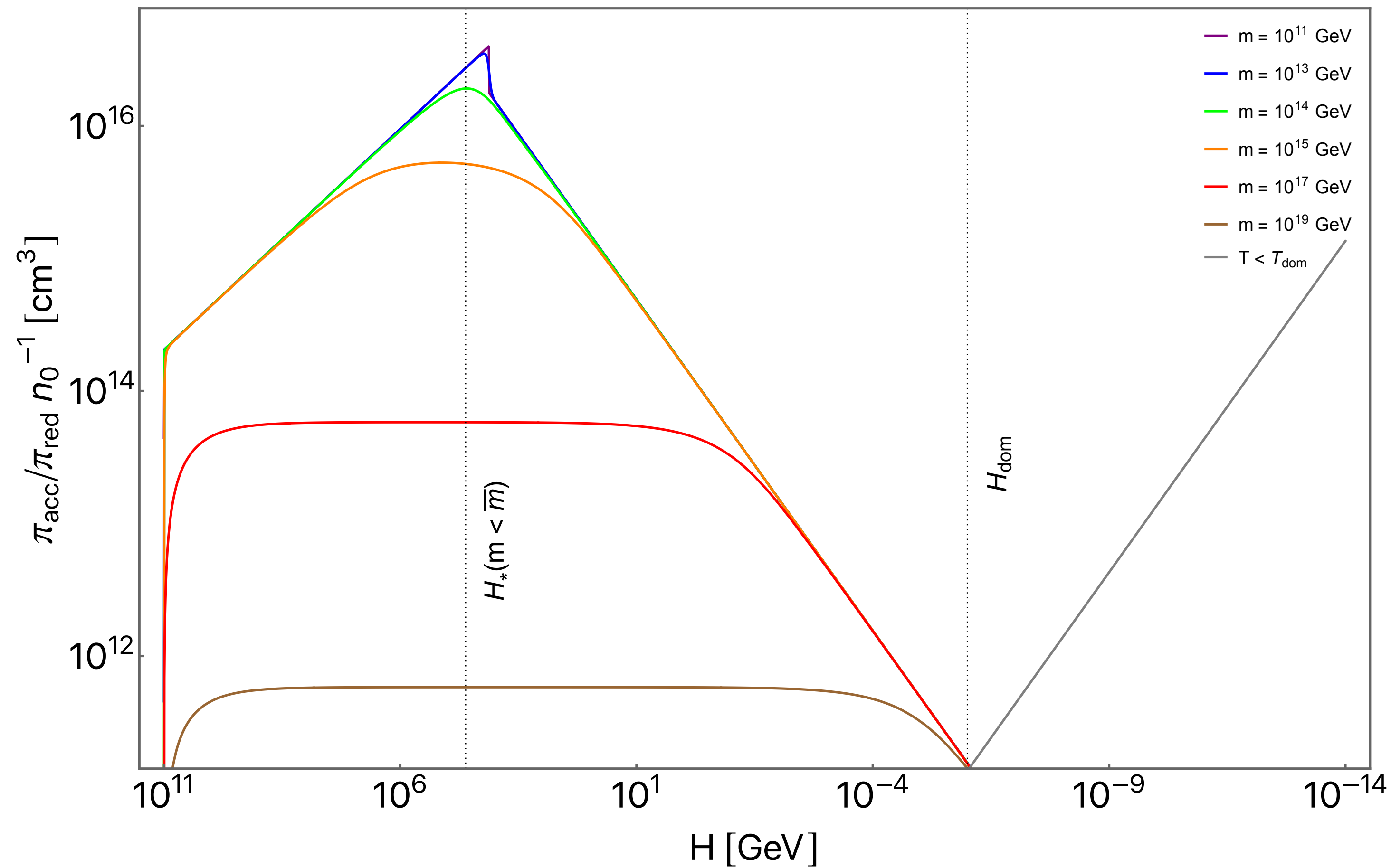
$$f_p \sim \frac{e^2 g^2 \mathcal{N}_c}{16\pi^2} T^2$$



The *expansion of the universe* acts as an effective additional frictional force.

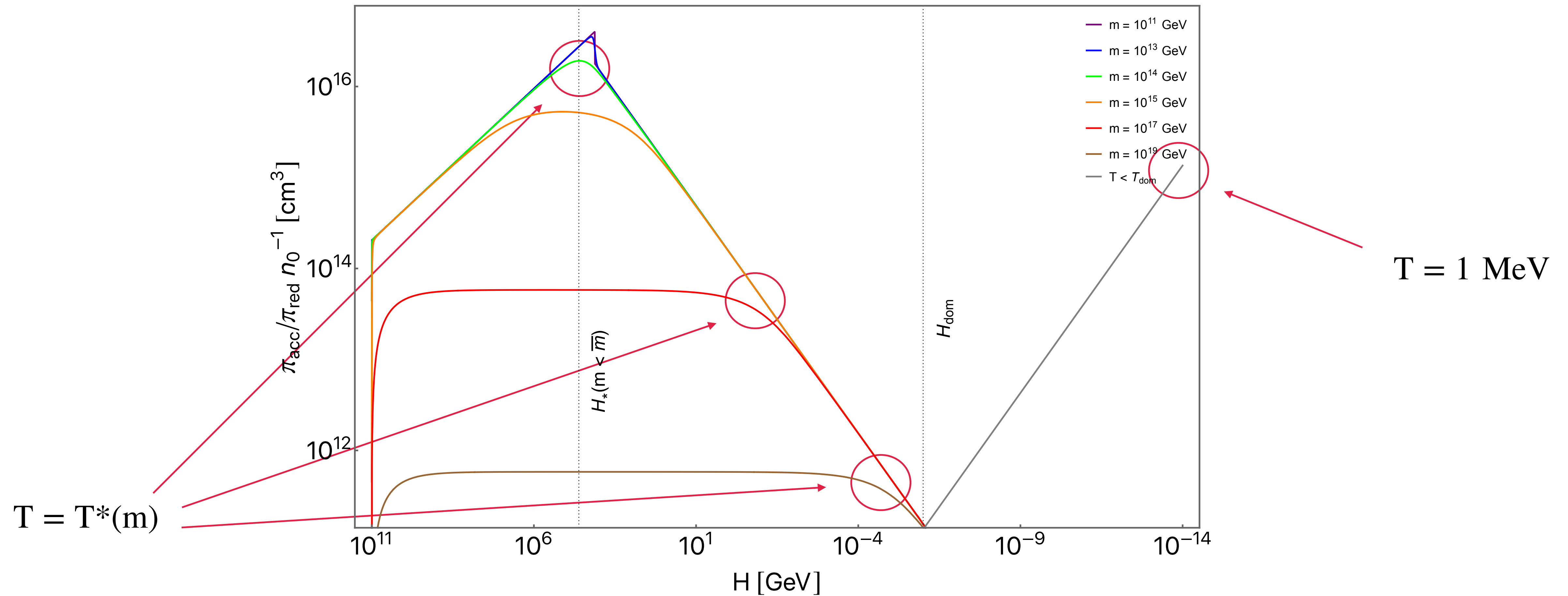
# The Evolution of $\Pi_{\text{acc}}/\Pi_{\text{red}}$

- The expression for  $\Pi_{\text{acc}}/\Pi_{\text{red}}$  presents two local maxima: one during reheating and one during the following era of radiation domination.



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# Bounds on the Monopole Flux

- From each of the two maxima through the condition  $\Pi_{\text{acc}}/\Pi_{\text{red}} \lesssim 1$  we obtain bounds on the monopole flux today:

1) Maximum at  $T = 1 \text{ MeV}$ :

$$n_0 \lesssim 10^{-21} \text{ cm}^{-3}$$

Long, Vachaspati (2015)  
[arXiv:1504.03319](https://arxiv.org/abs/1504.03319)

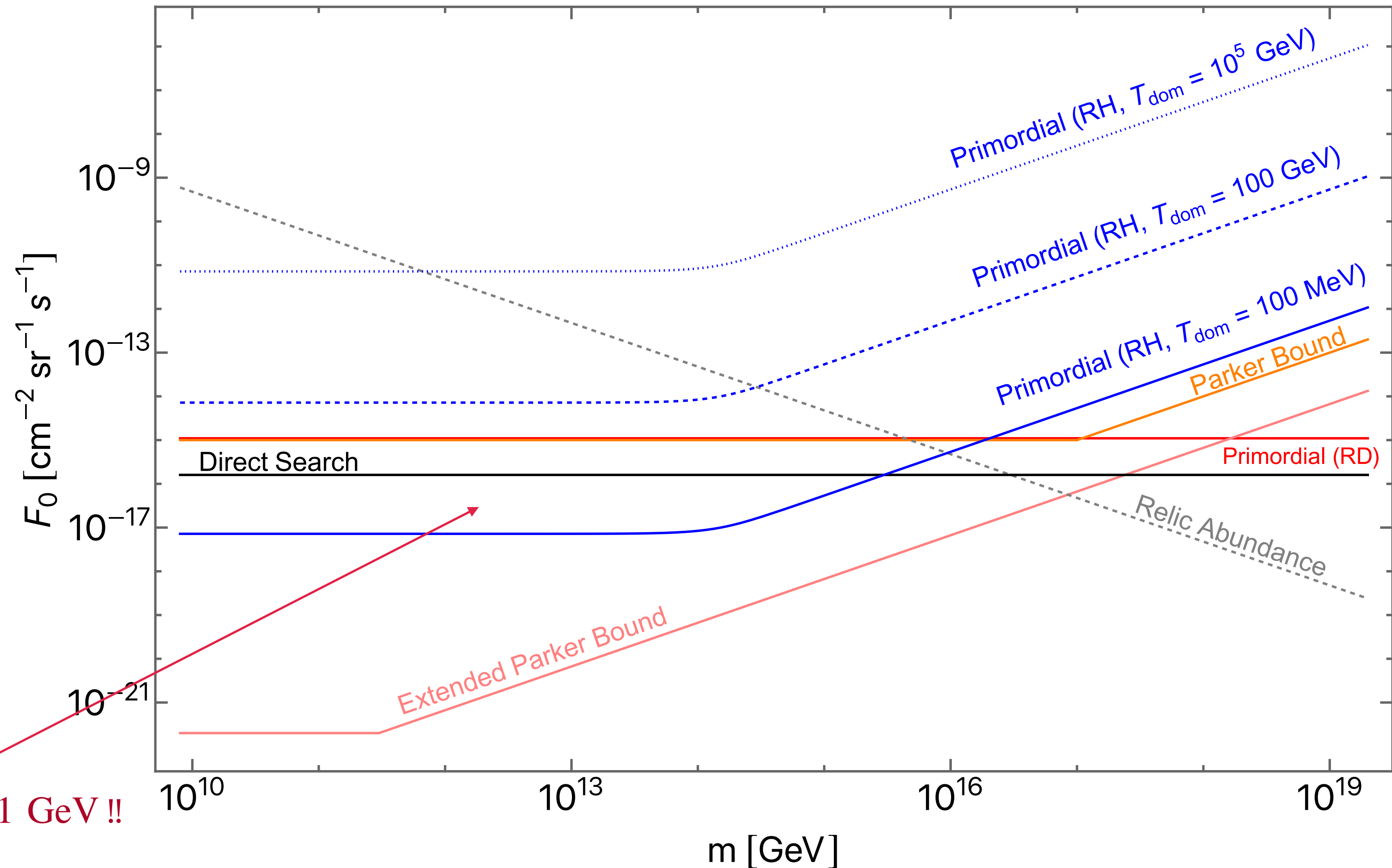
2) Maximum at  $T = T^*(m)$ :

$$n_0 \lesssim \begin{cases} 10^{-16} \text{ cm}^{-3} \left( \frac{B_0}{10^{-15} \text{ G}} \right)^{3/5} \left( \frac{T_{\text{dom}}}{10^6 \text{ GeV}} \right) \left( \frac{10}{g} \right)^{3/5} & , m \ll \bar{m}, \\ 10^{-16} \text{ cm}^{-3} \left( \frac{m}{10^{14} \text{ GeV}} \right) \left( \frac{T_{\text{dom}}}{10^6 \text{ GeV}} \right) \left( \frac{10}{g} \right)^2 & , m \gg \bar{m} \end{cases}$$

$$\bar{m} \simeq 10^{14} \text{ GeV} \left( \frac{B_0}{10^{-15} \text{ G}} \right)^{3/5} \left( \frac{g}{10} \right)^{7/5} \left( \frac{\mathcal{N}_{c,\text{dom}}}{100} \right)^{2/5}$$

# Bounds on the Monopole Flux

- We compare the new bounds with previous bounds on the monopole abundance:



Stronger for  $T_{\text{dom}} \lesssim 1 \text{ GeV} !!$

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# Schwinger Effects and Monopole Pair Production

Primordial magnetic fields are strong enough to produce significant amount of monopole-antimonopole pairs through the Schwinger Effect:

$$\Gamma = \frac{(gB)^2}{(2\pi)^3} \exp \left[ -\frac{\pi m^2}{gB} + \frac{g^2}{4} \right]$$

The computation is valid under the *weak field condition*:

$$B \lesssim \frac{4\pi m^2}{g^3}$$

*The survival of the fields after pair production and the acceleration of the produced monopoles provides the most conservative bound on the primordial magnetic fields.*



# Schwinger Effects and Monopole Pair Production

- The producing pairs extract energy from the magnetic fields that can eventually disappear.
- The bound for the survival of the field reduces to the weak field condition a part for a negligible logarithmic factor:

$$B \lesssim \frac{4\pi m^2}{g^3} \left[ 1 + \log \left( \frac{g^2 m}{8\pi^3 H} \right) \right]^{-1}$$

Takeshi Kobayashi (2021)  
[arXiv:2105.12776](https://arxiv.org/abs/2105.12776)

*Under the weak field condition the magnetic fields survive pair production.*

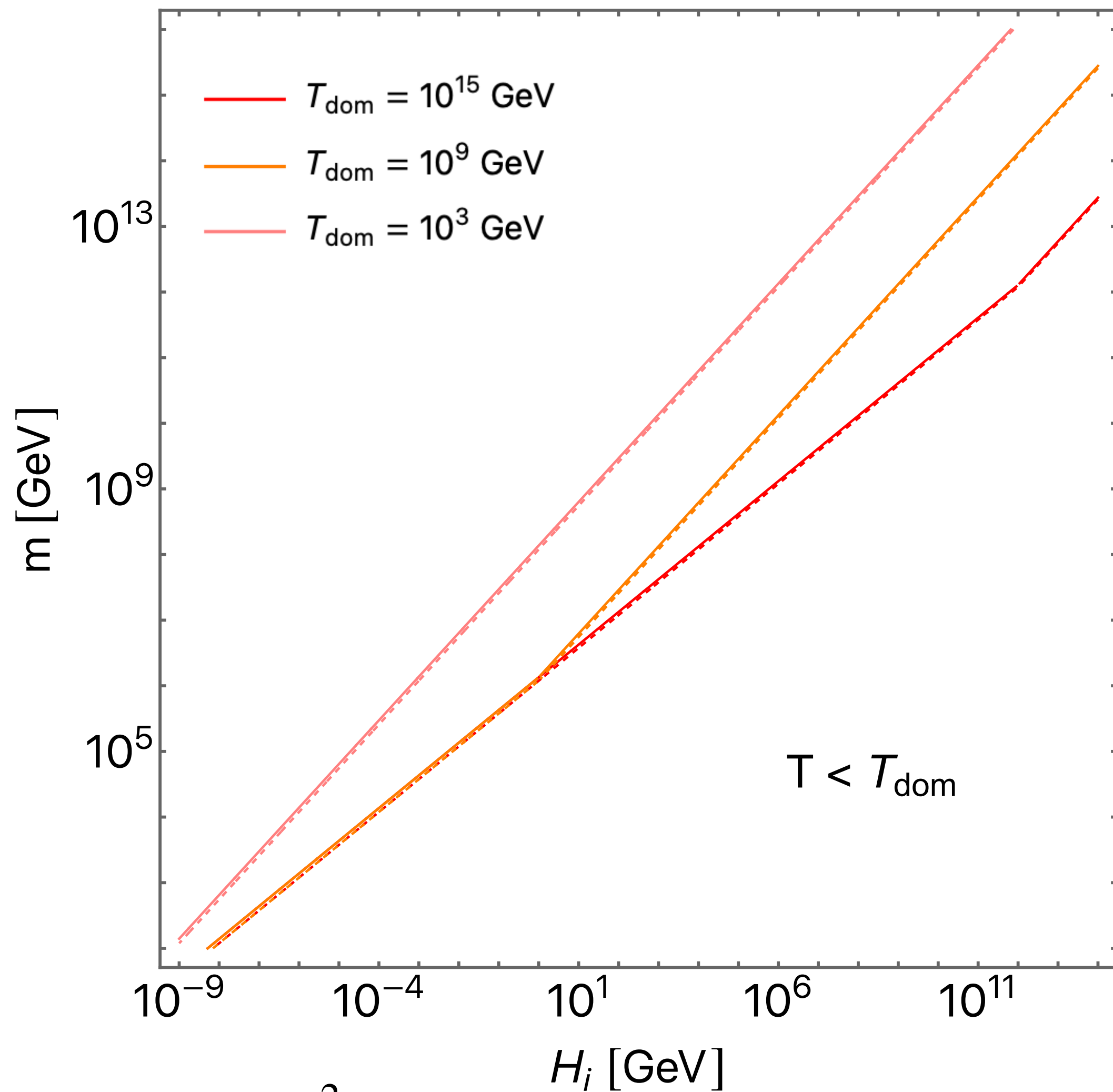
# Schwinger Effects and Monopole Pair Production

- The produced pairs are accelerated by the magnetic fields that continues to lose their energy.
- Bounds can be obtained from considering the condition  $\Pi_{\text{acc}}/\Pi_{\text{red}} \lesssim 1$  for the two maxima applied only to pair produced monopoles.
- Also in this case the bounds reduce to the weak field condition a part for a negligible logarithmic factor:

$$B \lesssim \frac{4\pi m^2}{g^3} \left[ 1 + \log \tilde{x}_{\text{D,B}}(m, H_i, T_{\text{dom}}, B_0) \right]^{-1}$$

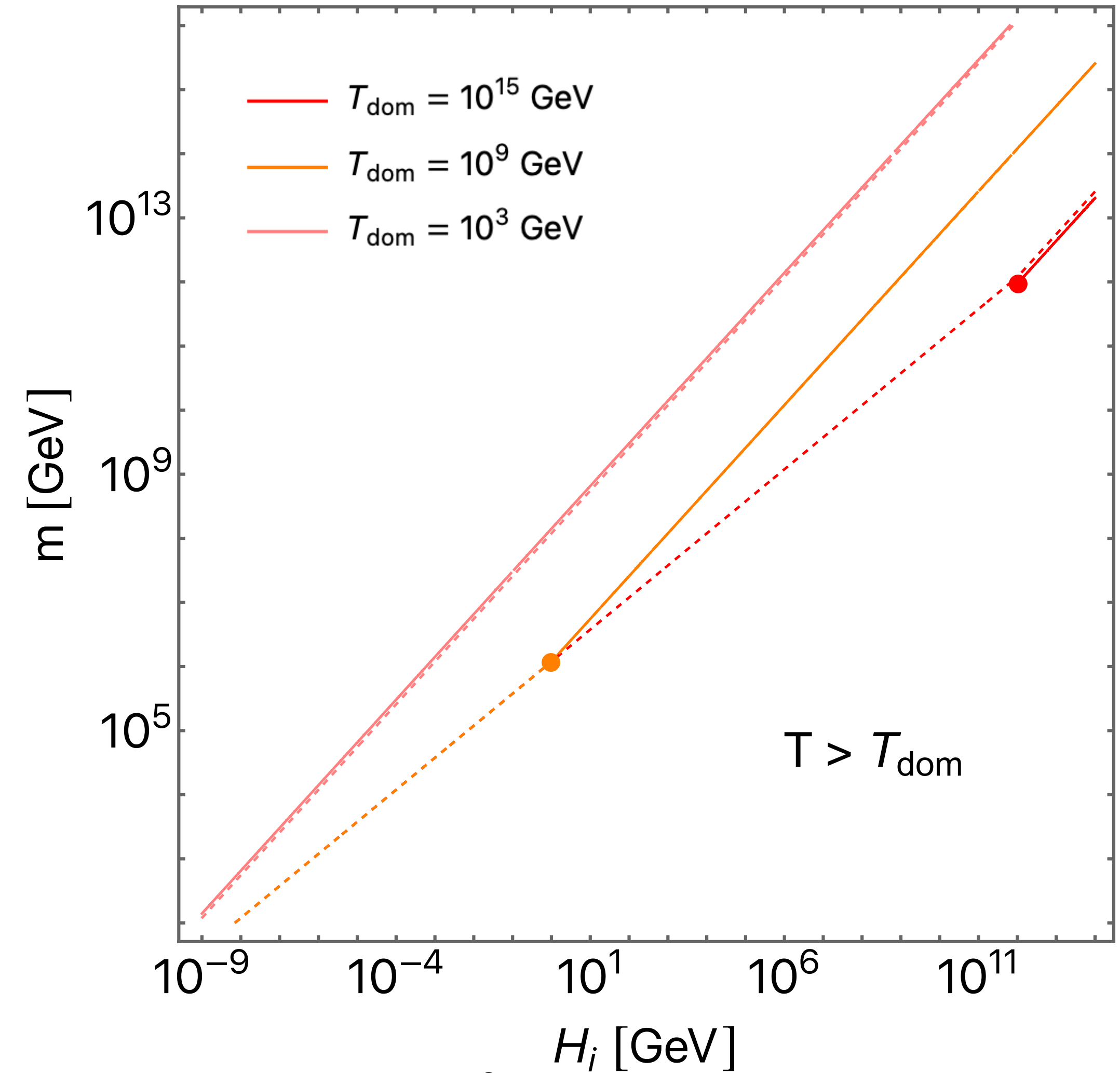
*Under the weak field condition the magnetic fields survive pair acceleration.*

# Schwinger Effects and Monopole Pair Production



$$B \lesssim \frac{4\pi m^2}{g^3} \left[ 1 + \log \tilde{x}_D(m, H_i, T_{\text{dom}}, B_0) \right]^{-1}$$

Daniele Perri, SISSA



$$B \lesssim \frac{4\pi m^2}{g^3} \left[ 1 + \log \tilde{x}_B(m, H_i, T_{\text{dom}}, B_0) \right]^{-1}$$

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# Conclusion

- ▶ We carried out a *comprehensive study of the monopole dynamics* in the early universe and their back-reaction to the *primordial magnetic fields*.
- ▶ We derived *new bounds on the abundance of magnetic monopoles* by generalizing the Parker bound to the survival of the primordial magnetic fields:
  1. For a sufficiently small temperature at the end of reheating our bound becomes *stronger than the original Parker bound and the limits from direct search*.
  2. We can neglect all the effects of the monopoles Schwinger-produced by the primordial magnetic fields once the *weak field condition* is satisfied.



# Thank You!!



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# Monopoles as topological defects

## 't Hooft - Polyakov Monopoles

- Topological defects comes from non trivial configurations of the vacuum manifold;
- They are classified in terms of the homotopy groups of the manifold;
- Examples are domain walls, cosmic strings, monopoles and textures;
- Monopoles are linked to non-trivial configuration of the second homotopy group of the vacuum manifold structure.

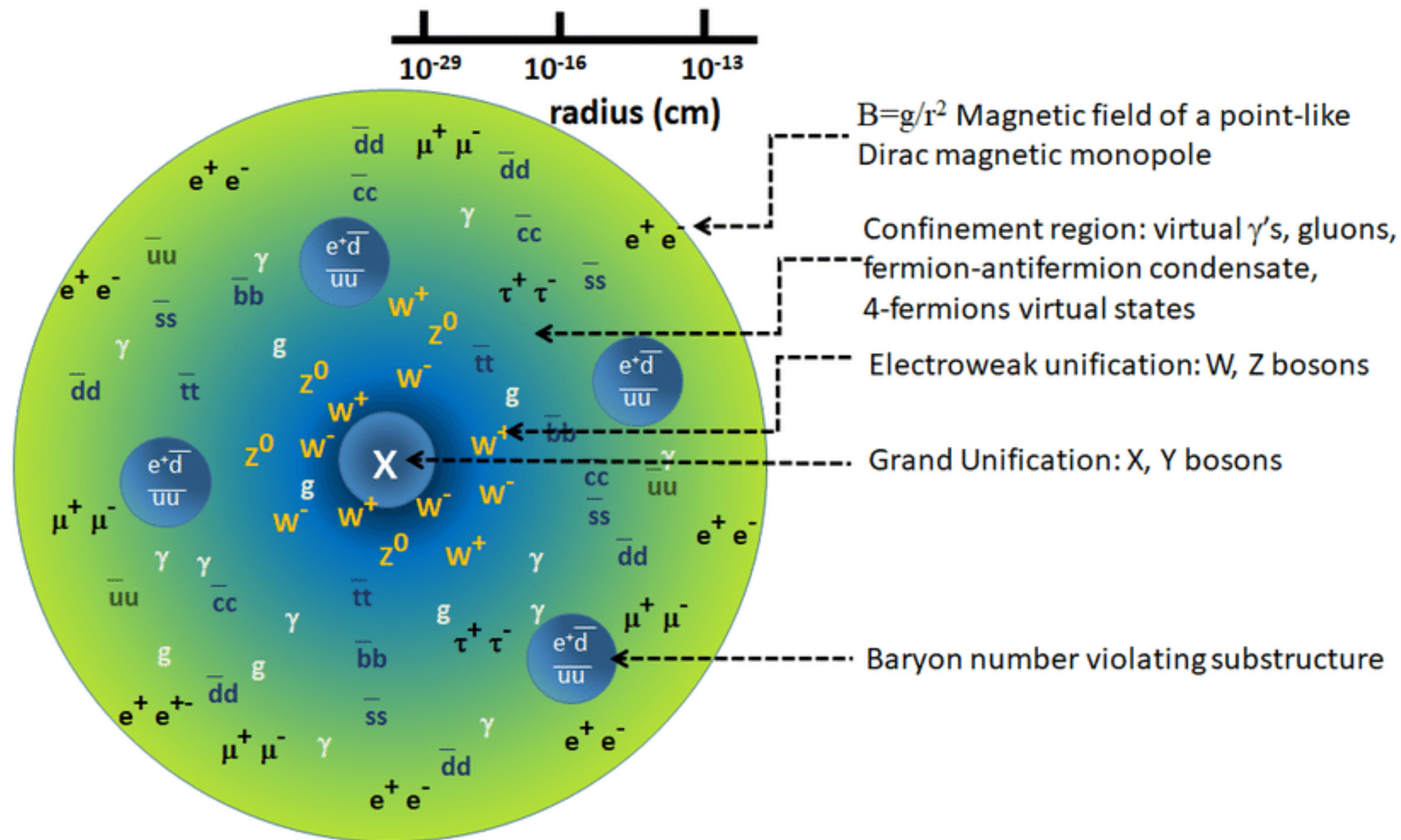
$X$	$\pi_1(X)$	$\pi_2(X)$	$\pi_3(X)$	$\pi_4(X)$	$\pi_5(X)$	$\pi_6(X)$	$\pi_7(X)$
$Sp(1)$	0	0	$\mathbb{Z}$	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}_{12}$	$\mathbb{Z}_2$
$Sp(n), n \geq 2$	0	0	$\mathbb{Z}$	$\mathbb{Z}_2$	$\mathbb{Z}_2$	0	$\mathbb{Z}$
$SU(3)$	0	0	$\mathbb{Z}$	0	$\mathbb{Z}$	$\mathbb{Z}_6$	0
$SU(n), n \geq 4$	0	0	$\mathbb{Z}$	0	$\mathbb{Z}$	0	$\mathbb{Z}$
$Spin(7)$	0	0	$\mathbb{Z}$	0	0	0	$\mathbb{Z}$
$Spin(8)$	0	0	$\mathbb{Z}$	0	0	0	$\mathbb{Z} \oplus \mathbb{Z}$
$Spin(n), n \geq 9$	0	0	$\mathbb{Z}$	0	0	0	$\mathbb{Z}$
$SO(3)$	$\mathbb{Z}_2$	0	$\mathbb{Z}$	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}_{12}$	$\mathbb{Z}_2$
$SO(5)$	$\mathbb{Z}_2$	0	$\mathbb{Z}$	$\mathbb{Z}_2$	$\mathbb{Z}_2$	0	$\mathbb{Z}$
$SO(6)$	$\mathbb{Z}_2$	0	$\mathbb{Z}$	0	$\mathbb{Z}$	0	$\mathbb{Z}$
$SO(7)$	$\mathbb{Z}_2$	0	$\mathbb{Z}$	0	0	0	$\mathbb{Z}$
$SO(8)$	$\mathbb{Z}_2$	0	$\mathbb{Z}$	0	0	0	$\mathbb{Z} \oplus \mathbb{Z}$
$SO(n), n \geq 9$	$\mathbb{Z}_2$	0	$\mathbb{Z}$	0	0	0	$\mathbb{Z}$
$G_2$	0	0	$\mathbb{Z}$	0	0	$\mathbb{Z}_3$	0
$F_4, E_6, E_7, E_8$	0	0	$\mathbb{Z}$	0	0	0	0
$S^2$	0	$\mathbb{Z}$	$\mathbb{Z}$	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}_{12}$	$\mathbb{Z}_2$
$S^3$	0	0	$\mathbb{Z}$	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z}_{12}$	$\mathbb{Z}_2$
$S^4$	0	0	0	$\mathbb{Z}$	$\mathbb{Z}_2$	$\mathbb{Z}_2$	$\mathbb{Z} \oplus \mathbb{Z}_{12}$
$S^5$	0	0	0	0	$\mathbb{Z}$	$\mathbb{Z}_2$	$\mathbb{Z}_2$

TABLE A.1: Homotopy groups of connected compact simple Lie groups [Jam95] and spheres  $S^n$  for  $2 \leq n \leq 5$  [Tod63]. Notice that there are isomorphisms  $Sp(1) \cong SU(2) \cong Spin(3)$ ,  $Sp(2) \cong Spin(5)$  and  $SU(4) \cong Spin(6)$

# Monopoles in Grand Unified Theories

Monopoles are *inevitable predictions* of Grand Unified Theories:

$$SU(5) \rightarrow SU(3) \times SU(2) \times U(1) \rightarrow SU(3) \times U(1)$$

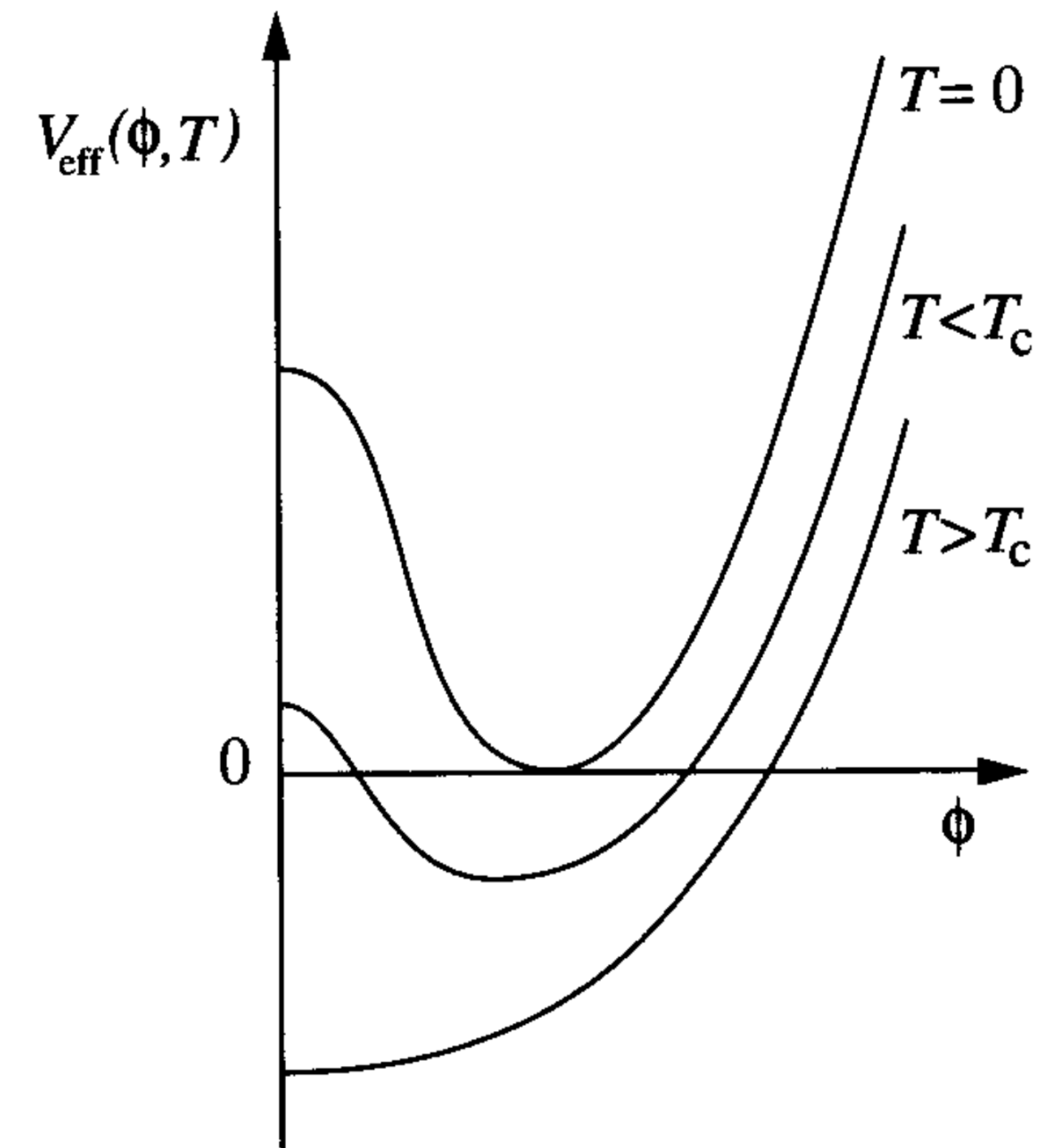
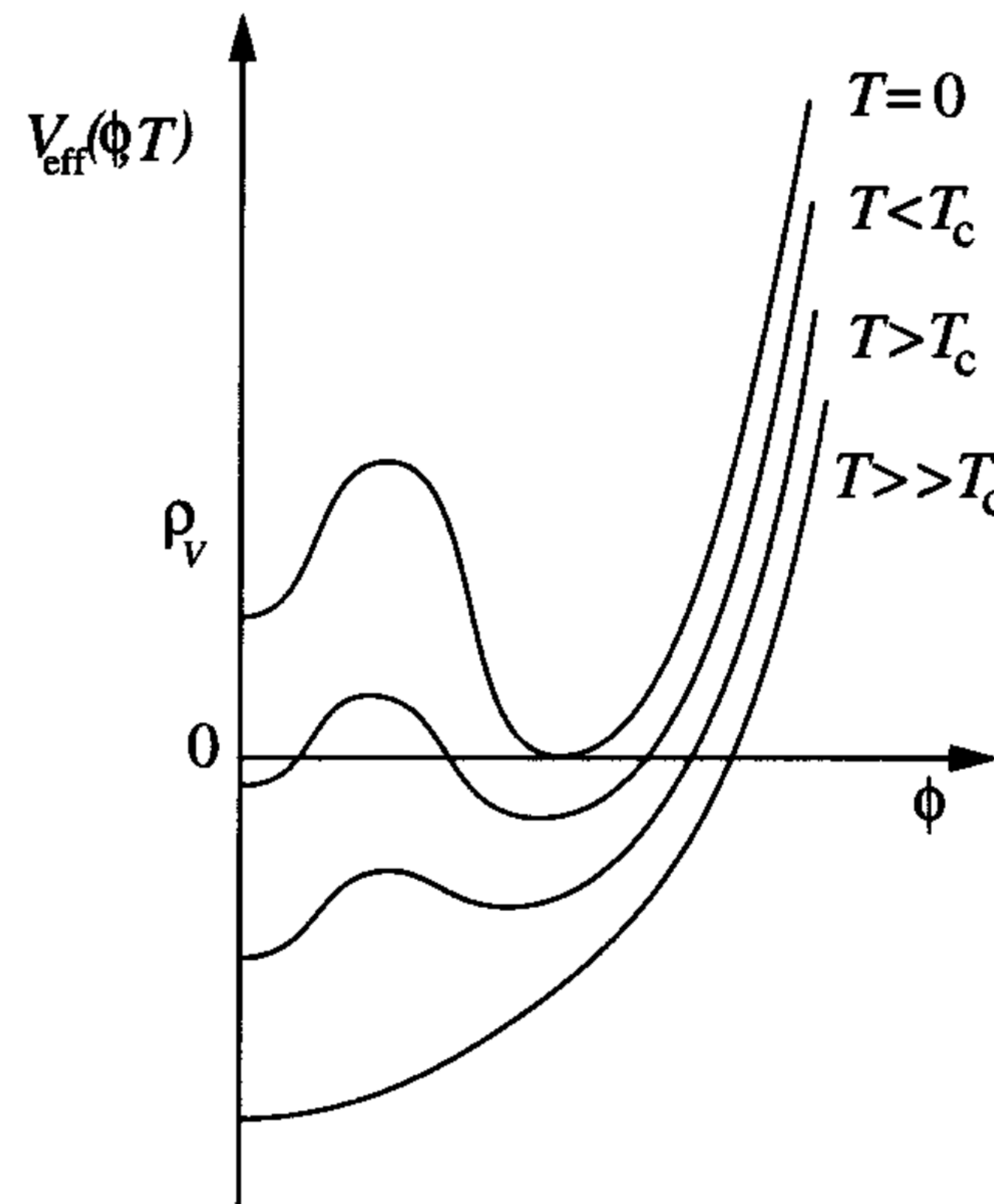


They present a complex structure inside the core where *all the states of the GUT are excited.*



# Monopole Production in Phase Transitions

- Monopoles are produced in the early universe during phase transition.
- The abundance of produced monopoles can easily over-dominate the energy density of the universe.
- Inflation provides a good solution to the problem.



# Direct Observations of Monopoles

There are different strategies used for the direct observation of magnetic monopoles:

- Induction of electric currents into a coil;
- Energy loss by ionization (Ex. MACRO experiment);
- Catalysis of nucleon decays (only for GUT monopoles).

