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Oblique S and T parameters at one-loop and heavy resonances

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Work in progress

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JHEP 05 (2019) 092 [arXiv: 1810.10544]
JHEP 04 (2017) 012 [arXiv: 1609.06659]
PRD 93 (2016) 055041 [arXiv: 1510.03114]
JHEP 01 (2014) 157 [arXiv: 1310.3121]
PRL 110 (2013) 181801 [arXiv: 1212.6769]
JHEP 08 (2012) 106 [arXiv: 1206.3454]

OUTLINE

- 1) Motivation
- 2) The effective resonance Lagrangian
- 3) Oblique Electroweak Observables: S and T at NLO
- 4) Phenomenology
- 5) Conclusions

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- 1) **Motivation**
- 2) The effective resonance Lagrangian
- Oblique Electroweak Observables: Sand Pat NLO

 Phenomenology

 Conclusions 3)
- 4)
- 5)



1. Motivation

- The Standard Model (SM) provides an extremely successful description of the electroweak and strong interactions.
- A key feature is the particular mechanism adopted to break the electroweak gauge symmetry to the electroweak subgroup, SU(2)_L x U(1)_Y → U(1)_{QED}, so that the W and Z bosons become massive. The LHC discovered a new particle around 125 GeV*.



 Up to now all searches for New Physics have given negative results: Higgs couplings compatible with the SM and no new states. Therefore, we can use EFTs because it seems there is a large mass gap.



Effective Field Theories

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Effective Field Theories

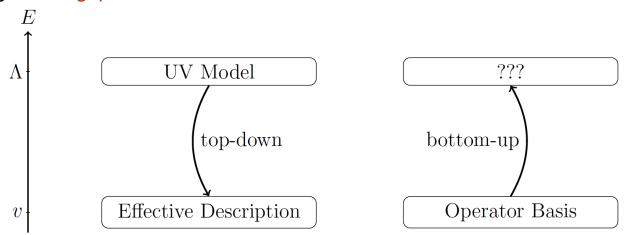
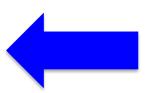


Diagram by C. Krause [PhD thesis, 2016]

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- Depending on the nature of the EWSB we have two possibilities for these EFTs (or something in between):
 - The decoupling (linear) EFT: SMEFT
 - SM-Higgs (forming a doublet with the EW Goldstones, as in the SM)
 - Weakly coupled
 - LO: SM
 - Expansion in canonical dimensions
 - The more general non-decoupling (non-linear) EFT: EWET, HEFT, EWChL
 - Non-SM Higgs (being a scalar singlet)
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What do we want to do?

S and T at NLO



Inclusion of BSM resonances in the effective Lagrangian in order to calculate S and T at NLO in terms of resonance parameters.

Short-distance constraints



Short-distance contraints are fundamental because we understand the resonance Lagrangian as an interpolation between low- and high energies and in order to reduce the number of resonance parameters.

Phenomenology



Following a typical bottom-up approach, what values for resonance masses are compatible with phenomenology?

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Similarities to Chiral Symmetry Breaking in QCD

- i) Custodial symmetry: The Lagrangian is approximately invariant under global $SU(2)_L \times SU(2)_R$ transformations. Electroweak Symmetry Breaking (EWSB) turns to be $SU(2)_L \times SU(2)_R \rightarrow SU(2)_{L+R}$.
- ii) Similar to the Chiral Symmetry Breaking (ChSB) occurring in QCD, *i.e.*, similar to the "pion" Lagrangian of Chiral Perturbation Theory (ChPT)* $^{\wedge}$, by replacing f_{π} by v=1/ $\sqrt{(2G_F)}$ =246 GeV. Rescaling naïvely we expect resonances at the TeV scale.

^{*} Weinberg '79

^{*} Gasser and Leutwyler '84 '85

^{*} Bijnens et al. <u>'99 '00</u>

^{**} Ecker et al. '89

^{**} Cirigliano et al. '06

[^]Dobado, Espriu and Herrero '91

[^]Espriu and Herrero '92

[^]Herrero and Ruiz-Morales '94

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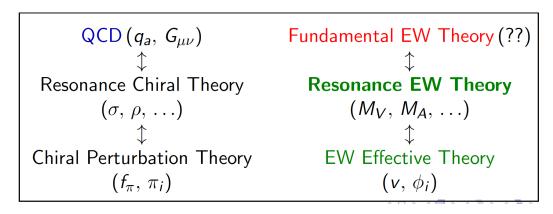


Diagram by J. Santos [VIII CPAN days, 2016]

2. The effective resonance Lagrangian

- Custodial symmetry
- Degrees of freedom: bosons x (EW goldstones, gauge bosons, h) + BSM resonances (V,A). The inclusion of fermions ψ is the next step in the project.
- Chiral power counting*

$$rac{\chi}{v} \sim \mathcal{O}\left(p^0
ight) \qquad \partial_{\mu}, \, m \sim \mathcal{O}(p) \qquad \mathcal{T} \sim \mathcal{O}(p) \qquad g, \, g' \sim \mathcal{O}(p)$$

Inclusion of odd-parity operators, not considered in Pich, IR, Santos and Sanz-Cillero '13'14.

$$\mathcal{M}(2\to 2) \ \approx \ \frac{p^2}{v^2} \ \left[\ 1 \ + \ \left(\frac{c_k^r \, p^2}{v^2} \ - \ \frac{\Gamma_k \, p^2}{16\pi^2 v^2} \, \ln \frac{p}{\mu} \ + \ldots \right) \ + \ \mathcal{O}(p^4) \ \right]$$
 LO (tree) NLO (1-loop) (tree) suppression suppression
$$\begin{array}{c} \text{NLO (1-loop)} \\ \text{-1/M}^2 + \ldots \\ \text{--/(16}\pi^2 v^2) \end{array} \right]$$
 (heavier states) (non-linearity)

* Weinberg '79

* Appelguist and Bernand '80

* Hirn and Stern '05 * Longhitano '80 '81

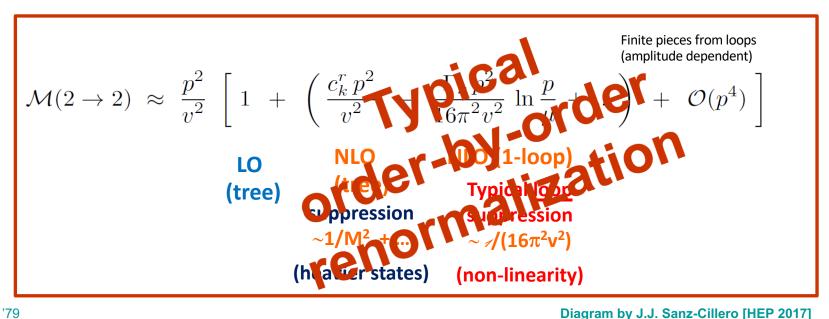
- * Alonso et al. '12 * Delgado et al. '14
- * Buchalla, Catá and Krause '13 * Pich, IR, Santos and Sanz-Cillero '16 '17 * Manohar, and Georgi '84
- * Gasser and Leutwyler '84 '85 Brivio et al. '13 * Krause, Pich, IR, Santos and Sanz-Cillero '19

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✓ The Lagrangian reads:

$$\begin{split} \Delta \mathcal{L}_{\text{RT}} &= \frac{v^2}{4} \left(1 + \frac{2 \kappa_W}{v} h \right) \langle u_{\mu} u^{\mu} \rangle_2 \\ &+ \langle V_{3 \, \mu \nu}^1 \left(\frac{F_V}{2 \sqrt{2}} f_+^{\mu \nu} + \frac{i G_V}{2 \sqrt{2}} [u^{\mu}, u^{\nu}] + \frac{\widetilde{F}_V}{2 \sqrt{2}} f_-^{\mu \nu} + \frac{\widetilde{\lambda}_1^{hV}}{\sqrt{2}} \left[(\partial^{\mu} h) u^{\nu} - (\partial^{\nu} h) u^{\mu} \right] \right) \rangle_2 \\ &+ \langle A_{3 \, \mu \nu}^1 \left(\frac{F_A}{2 \sqrt{2}} f_-^{\mu \nu} + \frac{\lambda_1^{hA}}{\sqrt{2}} \left[(\partial^{\mu} h) u^{\nu} - (\partial^{\nu} h) u^{\mu} \right] + \frac{\widetilde{F}_A}{2 \sqrt{2}} f_+^{\mu \nu} + \frac{i \widetilde{G}_A}{2 \sqrt{2}} [u^{\mu}, u^{\nu}] \right) \rangle_2 \,. \end{split}$$

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- Including resonance masses, we have 10 resonance parameters. This number can be reduced by using short-distance information, but in contrast to the QCD case, we ignore the underlying dynamical theory (BSM).
 - ✓ Vanishing form factors at high energies allow us to determine $\left(G_V, \widetilde{G}_A, \lambda_1^{hA}, \widetilde{\lambda}_1^{hV}\right)$ in terms of the remaining parameters:

$$\frac{G_V}{F_A} = -\frac{\widetilde{G}_A}{\widetilde{F}_V} = \frac{\lambda_1^{hA}v}{\kappa_W F_V} = -\frac{\widetilde{\lambda}_1^{hV}v}{\kappa_W \widetilde{F}_A} = \frac{v^2}{F_V F_A - \widetilde{F}_V \widetilde{F}_A}$$

- ✓ Weinberg sum rules (WSRs) at LO and at NLO.
 - ✓ 1st WSR. Vanishing of the 1/s term of $\Pi_{VV}(s) \Pi_{AA}(s)$: $\left(F_V^2 \widetilde{F}_V^2\right) \left(F_A^2 \widetilde{F}_A^2\right) = v^2$
 - \checkmark 2nd WSR. Vanishing of the 1/s² term of $\Pi_{VV}(s) \Pi_{AA}(s)$: $\left(F_V^2 \widetilde{F}_V^2\right) M_V^2 \left(F_A^2 \widetilde{F}_A^2\right) M_A^2 = 0$

3. Oblique Electroweak Observables: S and T at NLO

✓ Universal oblique corrections via the EW boson self-energies (transverse in the Landau gauge)

$$\mathcal{L}_{\text{v.p.}} \doteq -\frac{1}{2} W_{\mu}^{3} \Pi_{33}^{\mu\nu}(q^{2}) W_{\nu}^{3} - \frac{1}{2} B_{\mu} \Pi_{00}^{\mu\nu}(q^{2}) B_{\nu} - W_{\mu}^{3} \Pi_{30}^{\mu\nu}(q^{2}) B_{\nu} - W_{\mu}^{+} \Pi_{WW}^{\mu\nu}(q^{2}) W_{\nu}^{-}$$

✓ S parameter*: new physics in the difference between the Z self-energies at $Q^2=M_Z^2$ and $Q^2=0$.

$$e_3 = \frac{g}{g'} \widetilde{\Pi}_{30}(0), \qquad \Pi_{30}(q^2) = q^2 \widetilde{\Pi}_{30}(q^2) + \frac{g^2 \tan \theta_W}{4} v^2, \qquad S = \frac{16\pi}{g^2} (e_3 - e_3^{SM}).$$

✓ T parameter*: custodial symmetry breaking

$$e_1 = \frac{\Pi_{33}(0) - \Pi_{WW}(0)}{M_W^2} \stackrel{**}{=} \frac{Z^{(+)}}{Z^{(-)}} - 1$$
 $T = \frac{4\pi}{g'^2 \cos^2 \theta_W} \left(e_1 - e_1^{\text{SM}} \right)$

✓ We follow the useful dispersive representation introduced by Peskin and Takeuchi* for S and a dispersion relation for T (checked for the lowest cuts):

$$S = \frac{16\pi}{g^2 \tan \theta_W} \int_0^\infty \frac{\mathrm{d}t}{t} \left(\rho_S(t) - \rho_S(t)^{\mathrm{SM}} \right)$$
$$T = \frac{16\pi}{g'^2 \cos^2 \theta_W} \int_0^\infty \frac{\mathrm{d}t}{t^2} \left(\rho_T(t) - \rho_T(t)^{\mathrm{SM}} \right)$$

- ρ_S(t) and ρ_T(t) are the spectral functions of the W³B and of the difference of the neutral and charged Goldstone boson self-energies, respectively.
- ✓ They need to be well-behaved at short-distances to get the convergence of the integral.
- ✓ S and T parameters are defined for a reference value for the SM Higgs mass.

- Ve consider only the lightest two-particle absorptive cuts $(\phi\phi,\,h\phi)$ and in general we take as working assumptions $M_A > M_V$ and $\widetilde{F}_{V,A}^2 < F_{V,A}^2$.
- ✓ LO result (T_{LO}=0):
 - \checkmark With 1st and 2nd WSR: $S_{\text{LO}} = \frac{4\pi v^2}{M_V^2} \left(1 + \frac{M_V^2}{M_A^2}\right) \rightarrow \frac{4\pi v^2}{M_V^2} < S_{\text{LO}} < \frac{8\pi v^2}{M_V^2}$
 - \checkmark Assuming only the 1st WSR: $S_{\text{LO}} > \frac{4\pi v^2}{M_V^2}$
- ✓ NLO result including 1st and 2nd WSR:

$$\begin{split} S_{\rm NLO} &= 4\pi v^2 \bigg(\frac{1}{M_V^{r\,2}} + \frac{1}{M_A^{r\,2}}\bigg) + \Delta S_{\rm NLO}^{\rm P-even} + \Delta S_{\rm NLO}^{\rm P-odd} \\ \Delta S_{\rm NLO}^{\rm P-even} &= \frac{1}{12\pi} \left[\left(1 - \kappa_W^2\right) \left(\log \frac{M_V^2}{m_h^2} - \frac{11}{6}\right) + \kappa_W^2 \left(\frac{M_A^2}{M_V^2} - 1\right) \log \frac{M_A^2}{M_V^2} \right] \\ \Delta S_{\rm NLO}^{\rm P-odd} &= \frac{1}{12\pi} \left(\frac{\widetilde{F}_V^2}{F_V^2} + 2\kappa_W^2 \frac{\widetilde{F}_V \widetilde{F}_A}{F_V F_A} - \kappa_W^2 \frac{\widetilde{F}_A^2}{F_A^2}\right) \left(\frac{M_A^2}{M_V^2} - 1\right) \log \frac{M_A^2}{M_V^2} + O\left(\frac{\widetilde{F}_V^4}{F_V^4}\right) \\ T_{\rm NLO} &= \Delta T_{\rm NLO}^{\rm P-even} + \Delta T_{\rm NLO}^{\rm P-odd} \\ \Delta T_{\rm NLO}^{\rm P-even} &= \frac{3}{16\pi \cos^2 \theta_W} \left[\left(1 - \kappa_V^2\right) \left(1 - \log \frac{M_V^2}{m_A^2}\right) + \kappa_W^2 \log \frac{M_A^2}{M_V^2} \right] \\ \Delta T_{\rm NLO}^{\rm P-odd} &= \frac{3}{16\pi \cos^2 \theta_W} \left[2\lambda_V^2 \frac{A}{F_A} - 2\frac{\widetilde{F}_V}{F_V} + 2\left(\frac{\widetilde{F}_V}{F_V} M_V^2 - \kappa_W^2 M_A^2 \frac{\widetilde{F}_A}{F_A}\right) \frac{\log \frac{M_A^2}{M_V^2}}{M_A^2 - M_V^2} \right] \\ &+ 3\left(\left(\frac{\widetilde{N}_2}{F_V^2} - \kappa_W^2 \frac{\widetilde{F}_A^2}{F_A^2}\right) \left(M_A^2 + M_V^2\right) + 2\frac{\widetilde{F}_V \widetilde{F}_A}{F_V F_A} \left(M_V^2 - \kappa_W^2 M_A^2\right)\right) \frac{\log \frac{M_A^2}{M_V^2}}{M_A^2 - M_V^2} \\ &+ 6\left(\kappa_W^2 \frac{\widetilde{F}_A^2}{F_A^2} - \frac{\widetilde{F}_V^2}{F_V^2} - \left(1 - \kappa_W^2\right) \frac{\widetilde{F}_V \widetilde{F}_A}{F_V F_A}}\right) \right] + \mathcal{O}\left(\frac{\widetilde{F}_{V,A}^3}{F_{V,A}^3}\right) \end{split}$$

 $\Delta S_{
m NLO}^{
m P-even}$ and $\Delta T_{
m NLO}^{
m P-even}$ correspond to Pich, IR and Sanz-Cillero '13 '14

Expansion in $\frac{\widetilde{F}_{V,A}}{F_{V,A}}$.

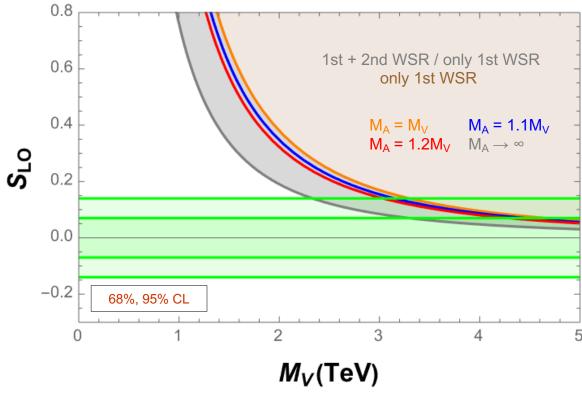
4. Phenomenology

$$S = 0.00 \pm 0.07 *$$

 $T = 0.05 \pm 0.06 *$

- ✓ Oblique electroweak observables** (S and T).
- Short-distance constraints.
- Assumptions: lightest two-particle absorptive cuts, $M_A > M_V$ and $\widetilde{F}_{V,A}^2 < F_{V,A}^2$.

i) LO results



* PDG '22

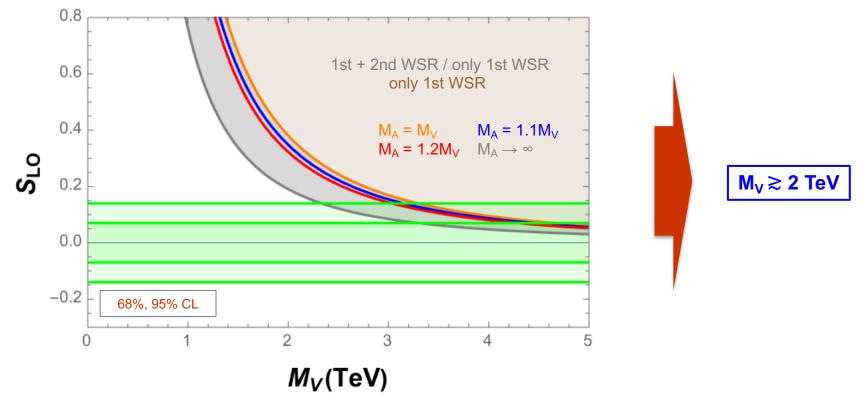
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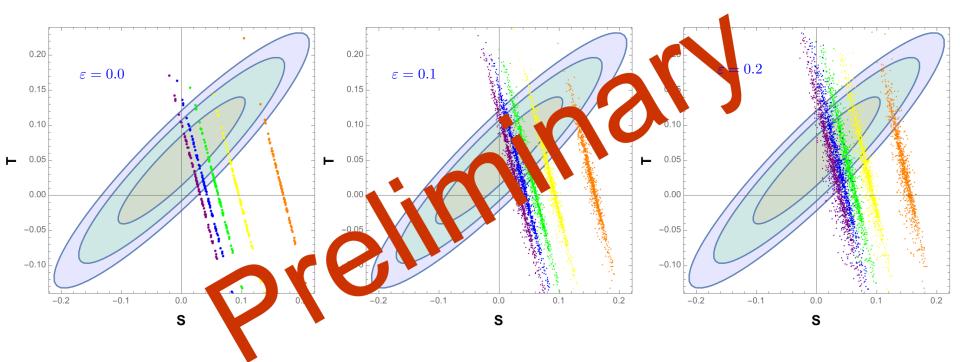
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ii) NLO results

Results in terms of only M_V, M_A, κ_{W} and $\frac{\widetilde{F}_{V,A}}{F_{V,A}}$





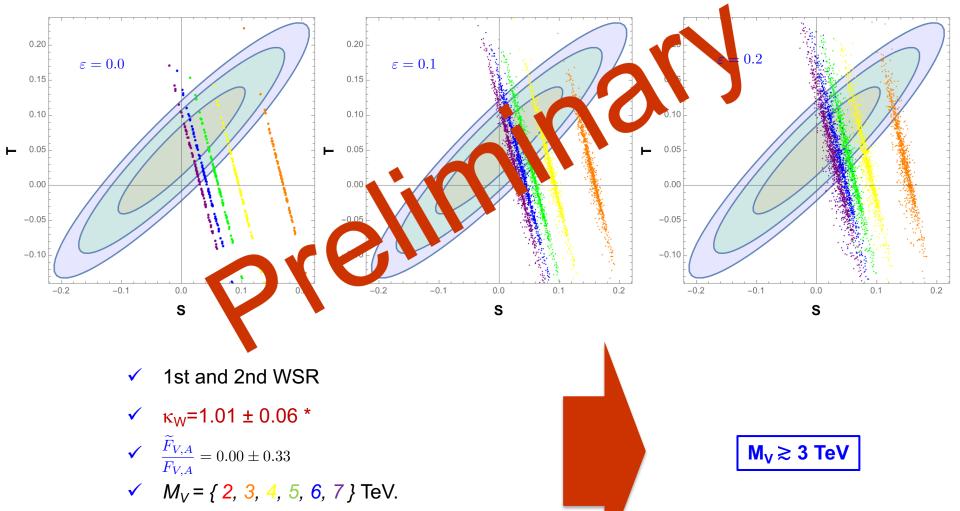
- 1st and 2nd WSR
- κ_W =1.01 ± 0.06 *
- $\checkmark \quad \frac{\widetilde{F}_{V,A}}{F_{V,A}} = 0.00 \pm 0.33$
- \checkmark $M_V = \{ 2, 3, 4, 5, 6, 7 \}$ TeV.
- \checkmark $M_A = M_V (1+\varepsilon)$

^{*} de Blas, Eberhardt and Krause '18

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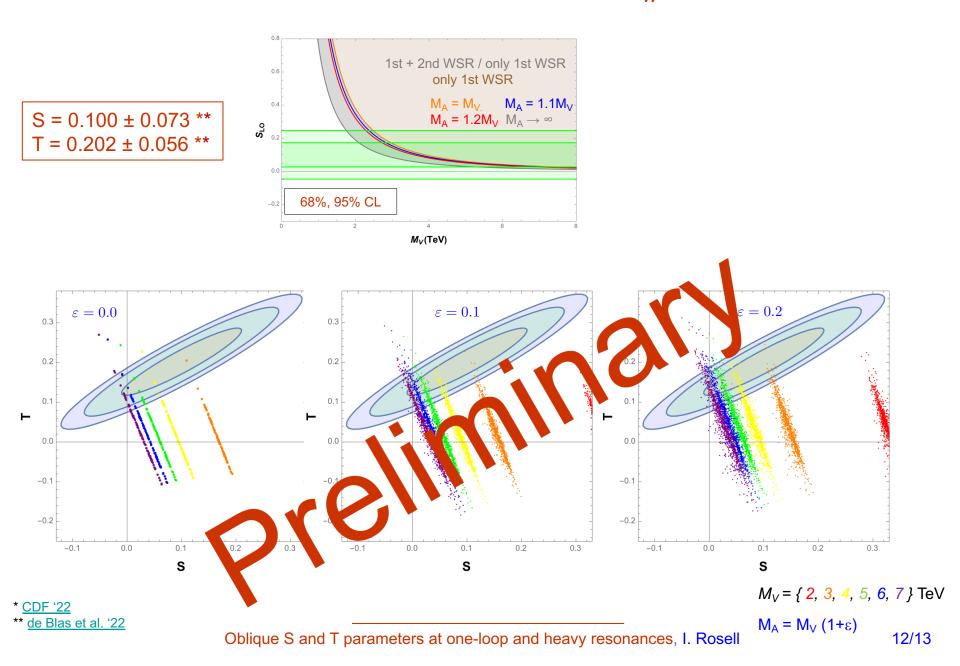




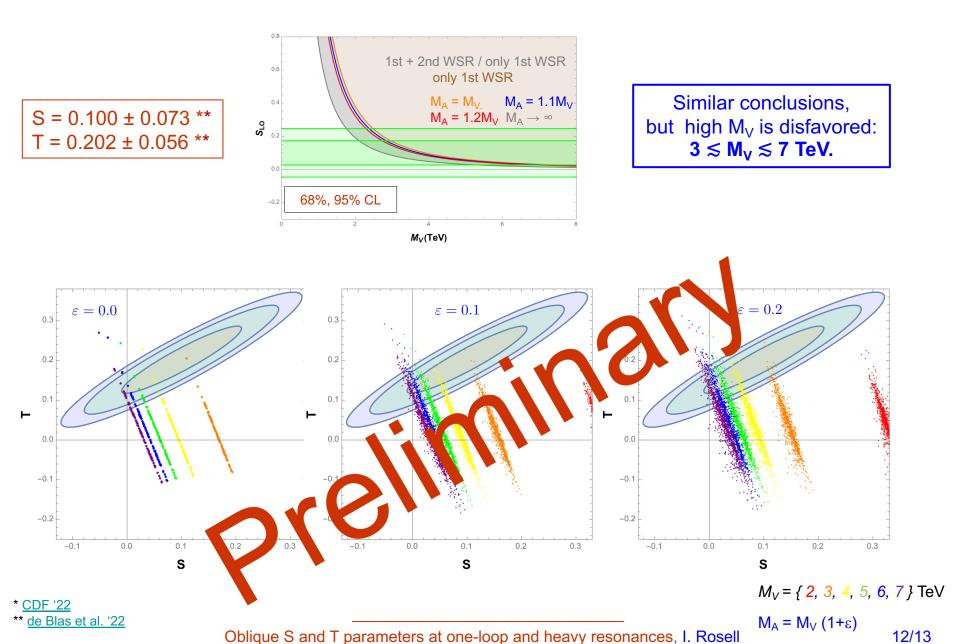
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What if we consider the new value of M_W from CDF*?



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4. Conclusions

- ✓ Up to now all searches for New Physics have given negative results: Higgs couplings compatible with the SM and no new states. Therefore we can use EFTs because we have a mass gap.
- As a consequence of the mass gap, bottom-up EFTs are appropriate to search for BSM. Depending on the nature of the EWSB we have two possibilities:
 - ✓ Decoupling (linear) EFT: SMEFT
 - ✓ SM-Higgs and weakly coupled
 - Expansion in canonical dimensions
 - ✓ Non-decoupling (non-linear) EFT: EWET (HEFT or EWChL)
 - ✓ Non-SM Higgs and strongly coupled
 - ✓ Expansion in loops or chiral dimensions



- ✓ Phenomenology: S and T at NLO
 - Short-distance constraints: WSRs and well-behaved form factors at high energies.
 - ✓ Assumptions: lightest two-particle absorptive cuts, $M_A \gtrsim M_V$ and $\tilde{F}_{V,A}^2 < F_{V,A}^2$.
 - \checkmark Results in terms of only M_V , M_A , κ_W and $\frac{\widetilde{F}_{V,A}}{F_{V,A}}$

Room for these BSM scenarios and $M_V \gtrsim 3$ TeV.