

Implications of R^2 -Higgs inflation with two doublets for collider experiments

Tanmoy Modak



UNIVERSITÄT
HEIDELBERG
ZUKUNFT
SEIT 1386

Unterstützt von / Supported by



Alexander von Humboldt
Stiftung / Foundation

Institute for Theoretical Physics
Heidelberg University

With: S. M. Lee, TM, K.-y. Oda, T. Takahashi; 2108.02383 (EPJC'22)

PASCOS, July 25 - 29, 2022 MPIK, Heidelberg, Germany

Outline

- » Overview
- » R^2 -Higgs Inflation in 2HDM
- » Implications at collider experiments
- » Summary and outlook



Overview

- **Higgs inflation**: One of the best-fit model to CMB data.
- Requires large non-minimal coupling: issue is perturbative unitarity.
- **R^2 -Higgs** inflation: can restore perturbative unitarity. (see talk by Minxi He)
- Additional Higgs doublets may exist in nature.
- Focus of interest is Two Higgs doublet model (2HDM).



R²-Higgs Inflation in 2HDM

Two Higgs doublet

Higgs sector:

$$\begin{aligned} V(\Phi, \Phi') = & \mu_{11}^2 |\Phi|^2 + \mu_{22}^2 |\Phi'|^2 - (\mu_{12}^2 \Phi^\dagger \Phi' + h.c.) \\ & + \frac{\eta_1}{2} |\Phi|^4 + \frac{\eta_2}{2} |\Phi'|^4 + \eta_3 |\Phi|^2 |\Phi'|^2 + \eta_4 |\Phi^\dagger \Phi'|^2 \\ & + \left[\frac{\eta_5}{2} (\Phi^\dagger \Phi')^2 + (\eta_6 |\Phi|^2 + \eta_7 |\Phi'|^2) \Phi^\dagger \Phi' + h.c. \right] \end{aligned}$$

(e.g. Davidson and Haber PRD'05,
Hou and Kikuchi, EPL' 18)

► Additional-Higgs bosons:

H, A, H^\pm

$m_A, m_{H^\pm}, m_H \sim 200\text{--}800 \text{ GeV}$

$m_h = 125 \text{ GeV}$



$c_\gamma \sim 0.2 - 0.1$

(W.-S. Hou, M. Kohda, TM PRD'19)

Yukawa sector:

$$\lambda^u \equiv \begin{pmatrix} \lambda_u & & \\ & \lambda_c & \\ & & \lambda_t \end{pmatrix}, \quad \lambda^d \equiv \begin{pmatrix} \lambda_d & & \\ & \lambda_s & \\ & & \lambda_b \end{pmatrix}, \quad \lambda^l \equiv \begin{pmatrix} \lambda_e & & \\ & \lambda_\mu & \\ & & \lambda_\tau \end{pmatrix} \quad \text{with, } \lambda^f = \frac{\sqrt{2}m_f}{v}$$

$$\rho^u \equiv \begin{pmatrix} \rho_{uu} & \rho_{uc} & \rho_{ut} \\ \rho_{cu} & \rho_{cc} & \rho_{ct} \\ \rho_{tu} & \rho_{tc} & \color{red}{\rho_{tt}} \end{pmatrix}, \quad \rho^d \equiv \begin{pmatrix} \rho_{dd} & \rho_{ds} & \rho_{db} \\ \rho_{sd} & \rho_{ss} & \rho_{sb} \\ \rho_{bd} & \rho_{bs} & \color{red}{\rho_{bb}} \end{pmatrix}, \quad \rho^\ell \equiv \begin{pmatrix} \rho_{ee} & \rho_{e\mu} & \rho_{e\tau} \\ \rho_{\mu e} & \rho_{\mu\mu} & \rho_{\mu\tau} \\ \rho_{\tau e} & \rho_{\tau\mu} & \rho_{\tau\tau} \end{pmatrix}$$

Higgs bosons couplings with fermions:

$$h\bar{f}_i f_j : -\lambda_{ij} s_\gamma + \rho_{ij} c_\gamma$$

$$c_\gamma \lesssim 0.2$$

$$H\bar{f}_i f_j : \lambda_{ij} c_\gamma + \rho_{ij} s_\gamma$$



h couples to λ^f

$$A\bar{f}_i f_j : -i \operatorname{sgn}(Q_f) \rho_{ij}$$

H, A, H^\pm couple to ρ^f

$$\bar{u}_i d_j H^+ : (V\rho^D)_{ij} P_R - (\rho^{U\dagger} V)_{ij} P_L$$

2HDM R^2 inflation

Inflationary dynamics:

$$\Phi = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \rho_1 \end{pmatrix} \quad \text{and} \quad \Phi' = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \rho_2 + i\rho_3 \end{pmatrix}.$$

$$\phi^I(x^\mu) = \bar{\phi}^I(t) + \delta\phi^I(x^\mu); \text{ with } \phi^I = \{\varphi, \rho_1, \rho_2, \rho_3\}$$

$$S_E = \int d^4x \sqrt{-g} \left[\frac{M_P^2}{2} R - \frac{1}{2} (\partial_\mu \varphi)^2 - \frac{1}{2} e^{-\sqrt{\frac{2}{3}} \frac{\varphi}{M_P}} ((\partial_\mu \rho_1)^2 + (\partial_\mu \rho_2)^2 + (\partial_\mu \rho_3)^2) - V_E \right]$$

$$V_E(\varphi, \rho_1, \rho_2, \rho_3) = \frac{1}{8} e^{-2\sqrt{\frac{2}{3}} \frac{\varphi}{M_P}} \left[V(\rho_1, \rho_2, \rho_3) + 2 \frac{M_P^4}{\xi_R} \left(e^{\sqrt{\frac{2}{3}} \frac{\varphi}{M_P}} - 1 - \frac{\xi_{11}}{M_P^2} \rho_1^2 \right)^2 \right]$$

Background and perturbations:

$$\mathcal{D}_t \dot{\bar{\phi}}^I + 3H\dot{\bar{\phi}}^I + G^{IK}V_{E,K} = 0$$

$$\mathcal{D}_t^2 Q^I + 3H\mathcal{D}_t Q^I + \left(\frac{k^2}{a^2} \delta_J^I + \mathcal{M}_J^I - \frac{1}{2a^3} D_t \left(\frac{a^3}{H} \dot{\bar{\phi}}^I \dot{\bar{\phi}}_J \right) \right) Q^J = 0$$

$$\mathcal{M}_J^I = G^{IM} \mathcal{D}_J \mathcal{D}_M V_E - R_{MNJ}^I \dot{\bar{\phi}}^M \dot{\bar{\phi}}^N; \quad \delta \mathcal{M}_J^I = -\frac{1}{2a^3} \mathcal{D}_t \left(\frac{a^3}{H} \dot{\bar{\phi}}^I \dot{\bar{\phi}}_J \right)$$

Adiabatic and isocurvature modes:

Spanned by unit vectors: $\hat{\sigma}_I, \hat{\omega}_I, \hat{\pi}_I, \hat{\tau}_I$

$$\begin{aligned} Q_\sigma &= \hat{\sigma}_I Q^I, & \mathcal{R} &= \frac{H}{\dot{\sigma}} Q_\sigma, \\ Q_s &= \hat{\omega}_I Q^I, & \mathcal{S} &= \frac{H}{\dot{\sigma}} Q_s, \\ Q_u &= \hat{\pi}_I Q^I, & \mathcal{U} &= \frac{H}{\dot{\sigma}} Q_u, \\ Q_v &= \hat{\tau}_I Q^I & \mathcal{V} &= \frac{H}{\dot{\sigma}} Q_v \end{aligned}$$

$$\begin{aligned} \mathcal{P}_{\mathcal{R}}(t; k) &= \frac{k^3}{2\pi^2} P_{\mathcal{R}}(k) \\ \mathcal{P}_{\mathcal{S}}(t; k) &= \frac{k^3}{2\pi^2} |\mathcal{S}| \\ \mathcal{P}_{\mathcal{U}}(t; k) &= \frac{k^3}{2\pi^2} |\mathcal{U}|^2 \\ \mathcal{P}_{\mathcal{V}}(t; k) &= \frac{k^3}{2\pi^2} |\mathcal{V}|^2 \end{aligned}$$

Numerical results

Low-scale:

$$\mu_{22} < 1 \text{ TeV}; |\eta_i| < 1.$$

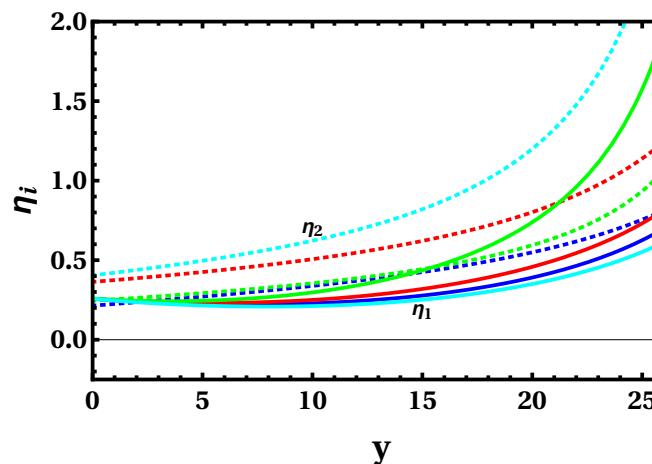
Perturbativity, Unitarity, Stability and EW precision observable.

BPs	η_1	η_2	η_3	η_4	η_5	η_6	η_7	m_{H^+}	m_A (GeV)	m_H (GeV)	$\frac{\mu_{22}^2}{v^2}$ (GeV)	c_γ
<i>a</i>	0.258353	0.214212	-0.104774	0.321234	-0.00339535	-0.0474321	0.132779	424	436	435	3.017	0.0165
<i>b</i>	0.257981	0.363637	-0.026754	0.194828	-0.225193	-0.0337426	0.0418302	429	443	428	3.043	0.0122
<i>c</i>	0.259349	0.245545	0.469357	-0.579992	-0.014849	-0.050576	0.061887	347	322	321	1.756	0.0352
<i>d</i>	0.258161	0.40482	0.134086	0.028604	0.059236	-0.066433	0.086559	681	681	683	7.581	0.0089

High-scale:

Perturbative Unitarity, Positivity

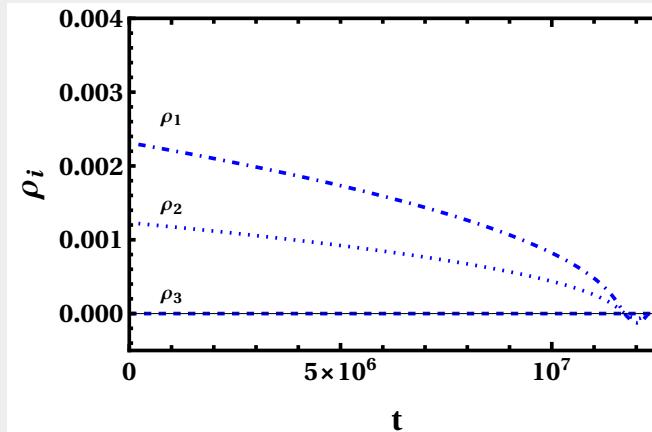
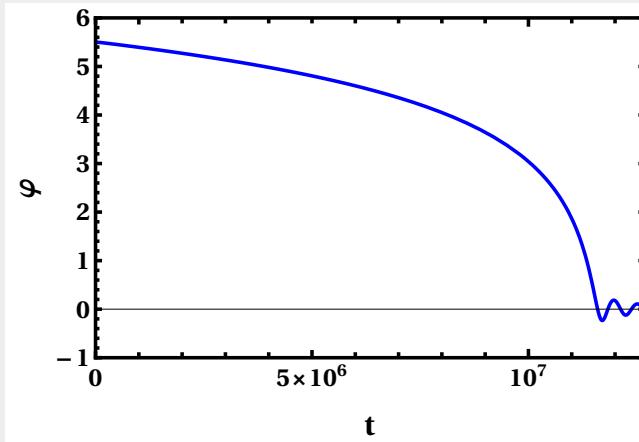
BPs	$\tilde{\eta}_1$	$\tilde{\eta}_2$	$\tilde{\eta}_3$	$\tilde{\eta}_4$	$\tilde{\eta}_5$	$\tilde{\eta}_6$	$\tilde{\eta}_7$	ξ_{11}	ξ_R
<i>a</i>	0.72459	0.834059	-0.287252	0.489654	-0.010900	-0.510739	0.333532	1	2.4×10^9
<i>b</i>	0.845674	1.281688	0.017365	0.611085	-0.776203	-0.361704	0.050345	1800	2.25×10^9
<i>c</i>	2.08746	1.11479	2.56305	-1.93179	-0.0412796	-0.521398	-0.0743505	10^{-3}	2.42×10^9
<i>d</i>	0.634249	2.98825	0.083228	0.087188	0.152301	-0.494063	0.679174	200	2.4×10^9



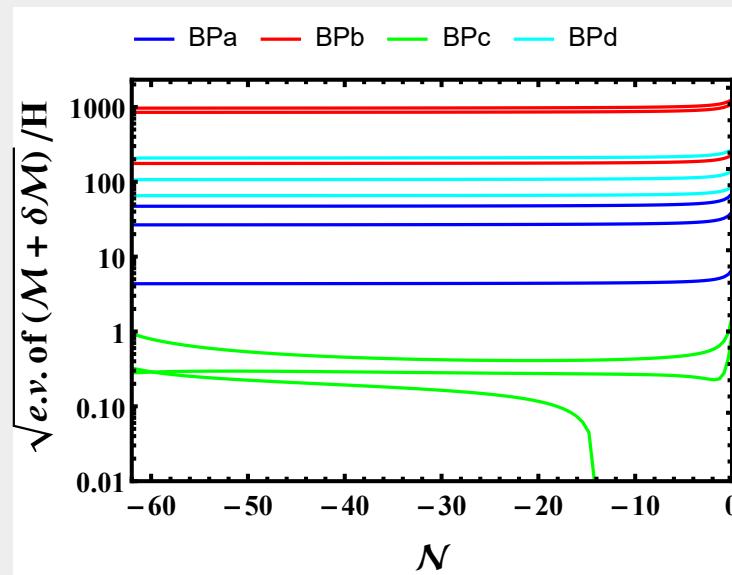
$$y = \ln(\mu/m_W)$$

Background evolution:

φ plays the role of inflaton



Mass eigen values of isocurvature modes:

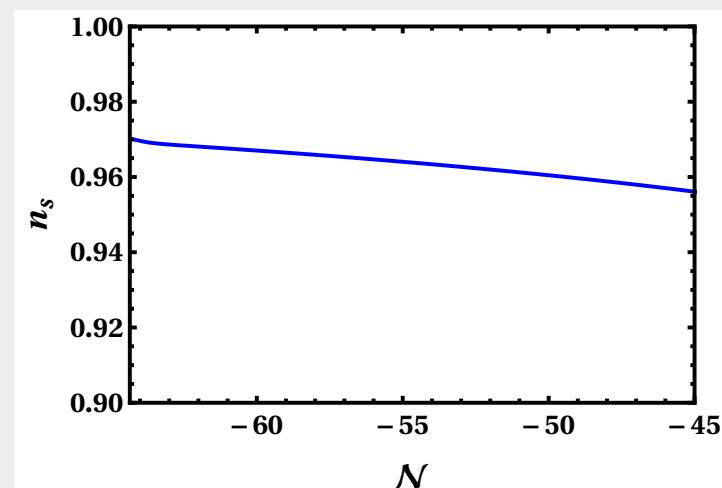
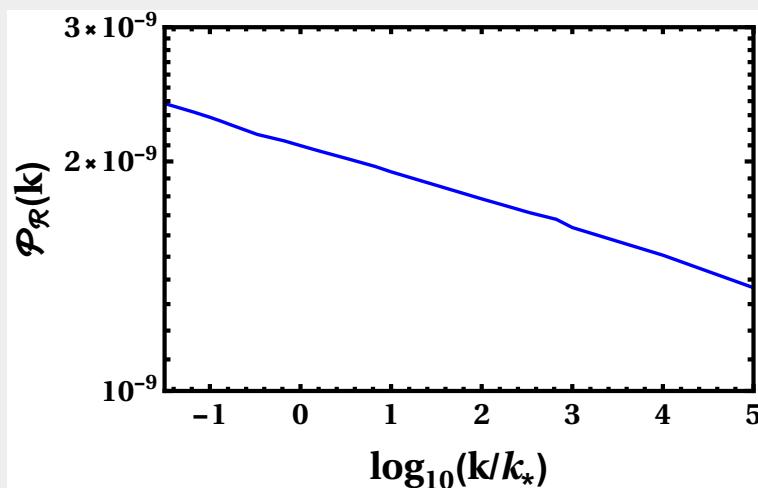


(Planck 2018)

$$n_s^* = 0.9649 \pm 0.0042$$

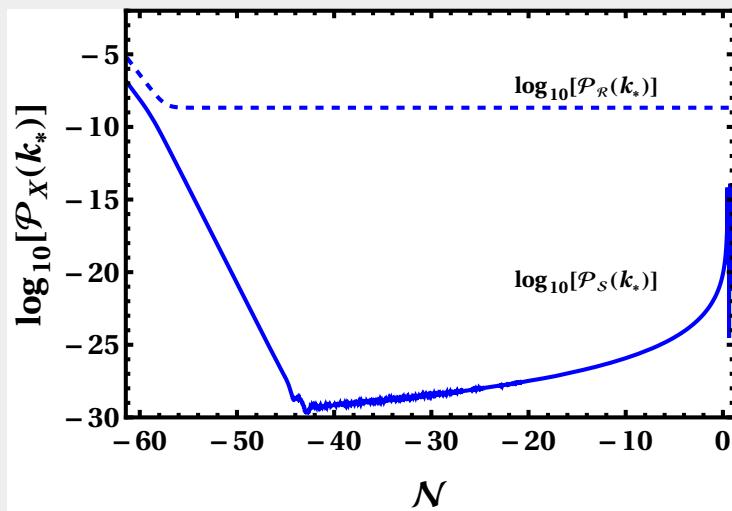
$$A_s^* = (2.099 \pm 0.014) \times 10^{-9}$$

$$r_{\varphi^*} < 0.056$$

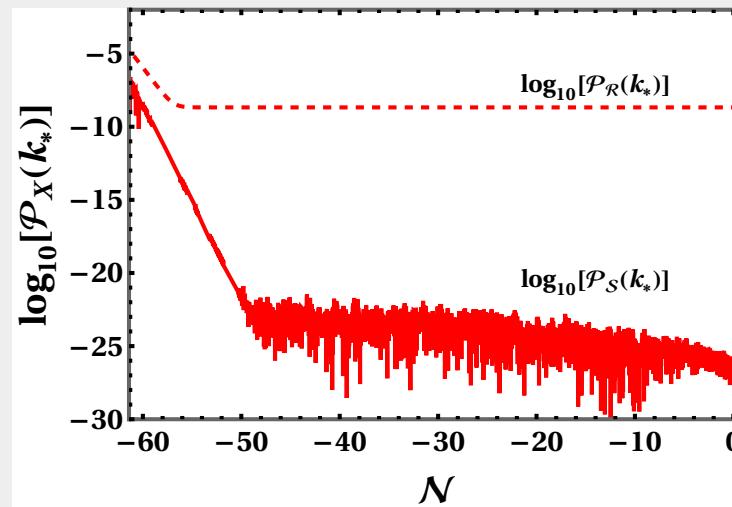


$$r_{\varphi*} \approx 3.3 \times 10^{-3}, \quad n_s^* = 0.965$$

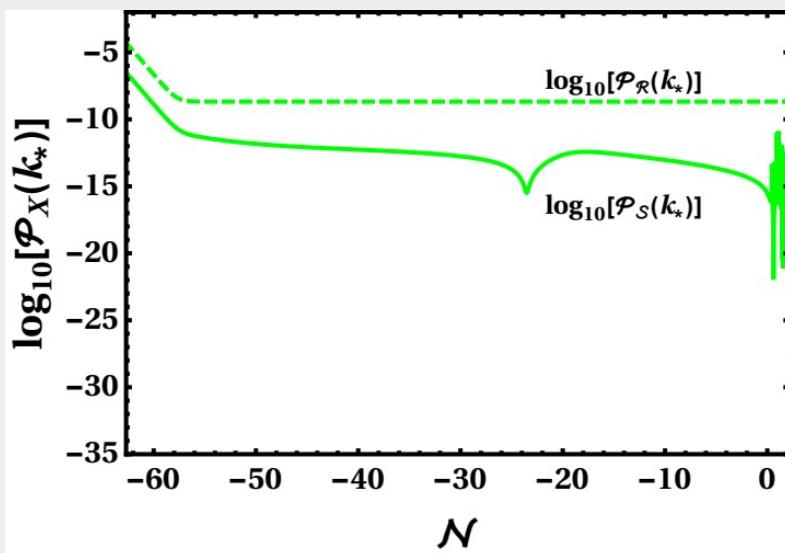
BPa



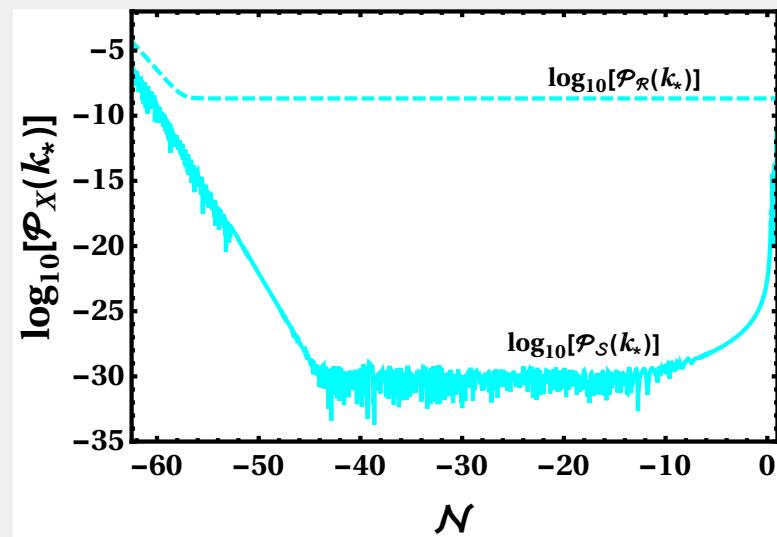
BPb



BPC



BPD



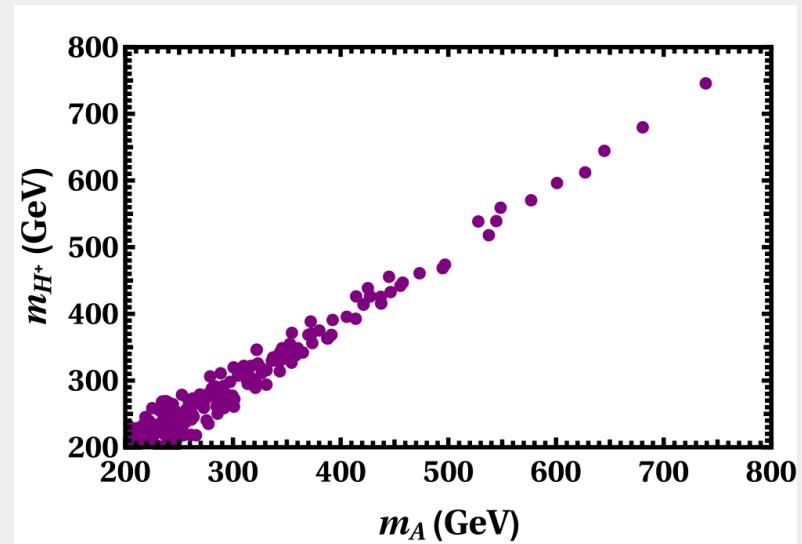
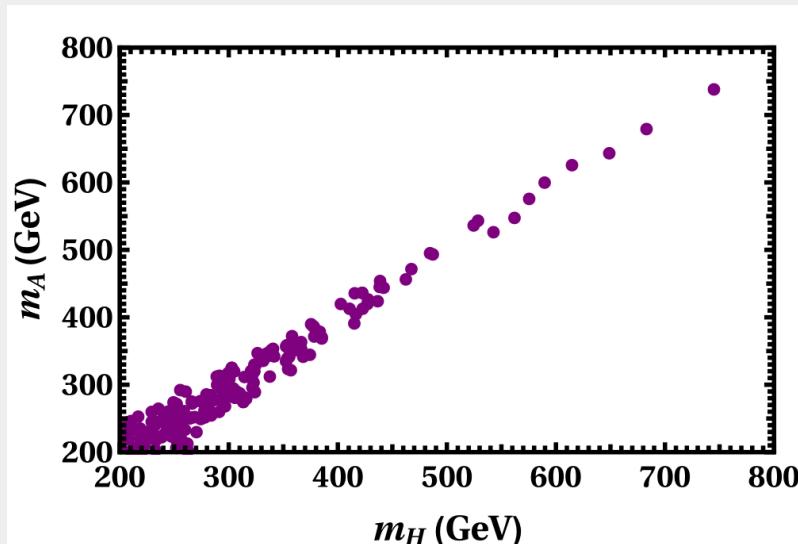
Implications at collider experiments

$$m_{H^\pm}^2 = \frac{1}{2}\eta_3 v^2 + \mu_{22}^2,$$

$$m_A^2 = \frac{1}{2}(\eta_3 + \eta_4 - \eta_5)v^2 + \mu_{22}^2,$$

$$m_{h,H}^2 = \frac{1}{2} \left[m_A^2 + (\eta_1 + \eta_5)v^2 \mp \sqrt{(m_A^2 + (\eta_5 - \eta_1)v^2)^2 + 4\eta_6^2 v^4} \right].$$

- Quasi-degenerate mass spectra favored by 2HDM inflation.



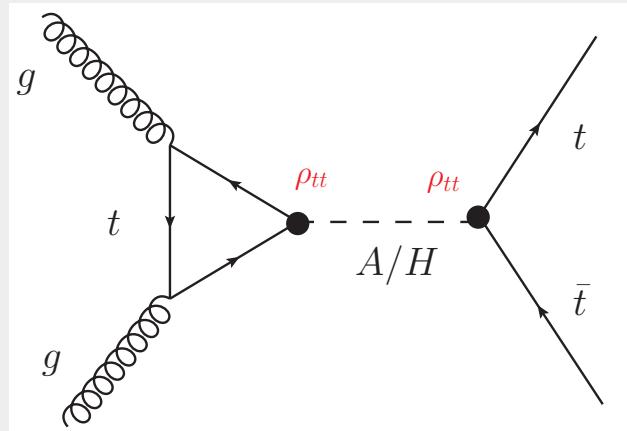
Discovery and mass reconstruction

ρ_{tt} driven discovery:

$$gg \rightarrow A/H \rightarrow t\bar{t}$$

$$gg \rightarrow Z^* \rightarrow A/H$$

$$gg \rightarrow A \rightarrow Zh$$

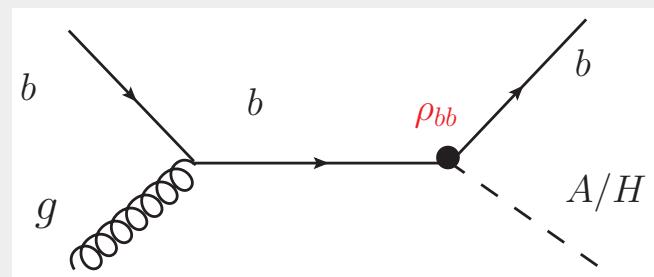


ρ_{bb} driven discovery:

$$bg \rightarrow bA \rightarrow bZH$$

$$bg \rightarrow bA \rightarrow bZh$$

$$e^+e^- \rightarrow AH \rightarrow 4b/6b$$

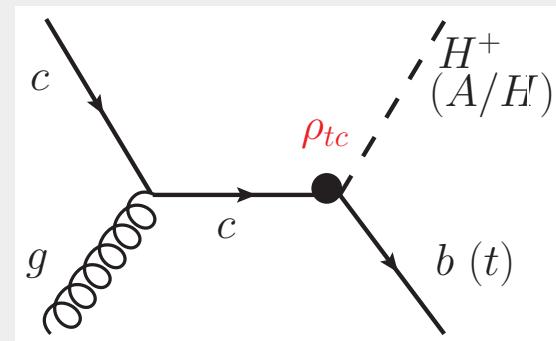


Indirect signature of quasi-degeneracy

$pp \rightarrow tA/tH \rightarrow tt\bar{c}$ (Same-sign top)

$pp \rightarrow tA/tH \rightarrow tt\bar{t}$ (Triple-top)

$pp \rightarrow bH^+ \rightarrow b\bar{t}\bar{b}$ (single-top)



For non-degenerate masses:

In terms of discovery: Same-sign top >> triple-top, single-top.

For quasi-degenerate masses:

Same-sign top ~ triple-top, single-top

EWBG + Inflation? Perhaps not

- $10^{-2} \lesssim |\rho_{tt}| \lesssim 1$ or $|\rho_{tc}| \gtrsim 0.5$ (K. Fuyuto, W.-S Hou, E. Senaha; PLB '18)
- $|\text{Im}(\rho_{bb})| \gtrsim 0.1$ (TM, E. Senaha; PRD '19, PLB'21)



Supports strongly 1st order EWPT

BP	η_1	η_2	η_3	η_4	η_5	η_6	η_7	m_{H^\pm} (GeV)	m_A (GeV)	m_H (GeV)	$\frac{\mu_{22}^2}{v^2}$
<i>a</i>	0.282	2.034	4.053	-1.039	1.343	-0.243	1.231	391	285	405	0.5
<i>b</i>	0.289	1.959	4.064	-0.418	1.56	-0.316	-1.216	414	334	456	0.8
<i>c</i>	0.303	0.413	5.129	-0.477	1.534	-0.455	0.457	508	444	541	1.7



Summary and outlook



- 2HDM-R² inflation: Four field dynamics.
- Quasi-degenerate mass spectra.
- Discovery and mass reconstruction: LHC and future collider experiments.
- Inflation+ EWBG ???

Thank You