Higgs-boson induced reheating and ultraviolet freeze-in dark matter

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based on: A. Ahmed, B. Grządkowski, AS 2111.06065 and 2207.11218

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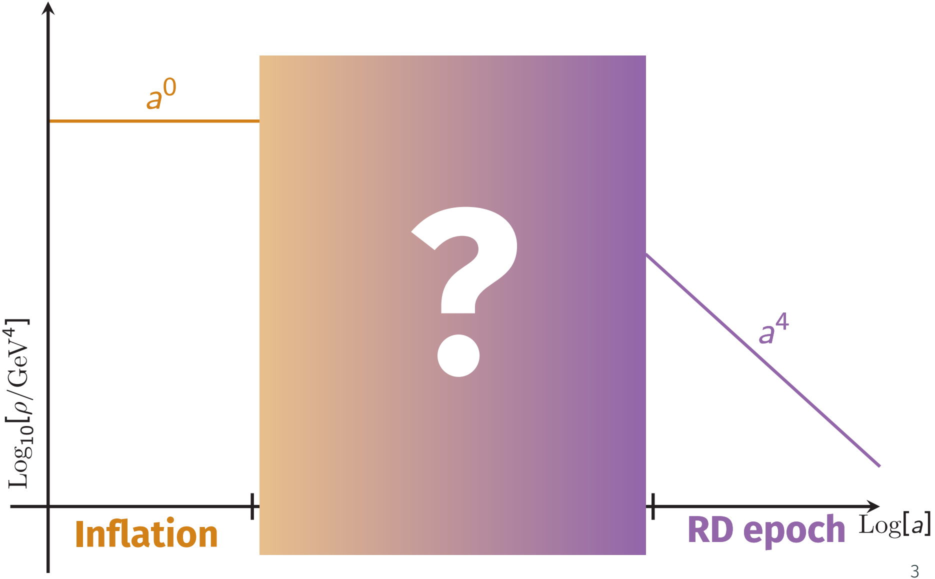
- The relevance of the reheating dynamics is typically ignored with a minimal assumption, such as instantaneous reheating.
- Even in the case of non-instantaneous reheating models, it is usually assumed that the inflaton decay rate, Γ_ϕ, is constant.
- However, this widely used assumption of constant can be violated in generic models of perturbative reheating, e.g., when the inflaton has a non-trivial potential.
- The understanding of the reheating era is essential for the dark matter sector, especially in the context of the freeze-in DM production.

Non-instantaneous reheating



Time-averaged Boltzmann equations

Expansion | **Interactions**

$$\dot{\rho}_\phi + 3(1+\overline{w})H\rho_\phi = -\langle\Gamma_\phi\rangle\rho_\phi$$

$$\dot{\rho}_\mathcal{R} + 4H\rho_\mathcal{R} = \langle\Gamma_\phi^\mathcal{R}\rangle\rho_\phi$$

$$\overline{w} \equiv \langle p_\phi\rangle / \langle\rho_\phi\rangle$$

$$H^2 = \frac{\rho_\phi + \rho_\mathcal{R}}{3M_{pl}^2}$$

Time-dependent decay rate

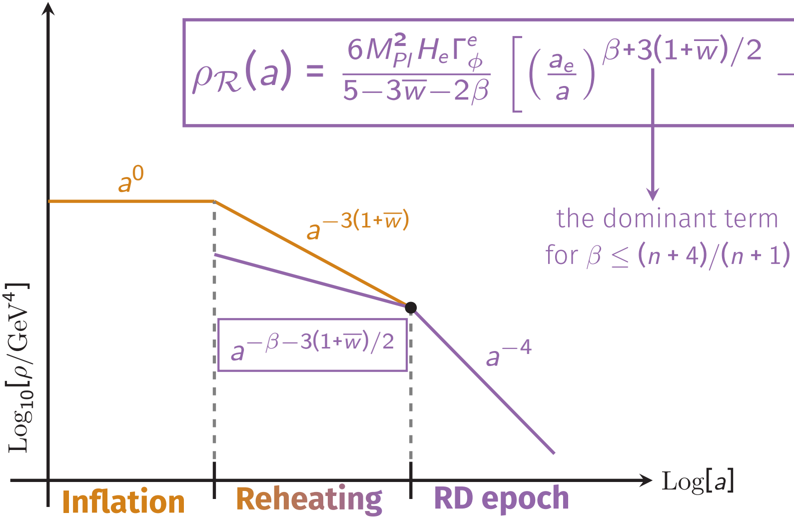
$$\langle\Gamma_\phi^\mathcal{R}\rangle \simeq \langle\Gamma_\phi\rangle = \Gamma_\phi^e\left(\frac{a_e}{a}\right)^\beta$$

constant parameter (β)

Non-instantaneous reheating

$$\rho_\phi(a) \overset{H \gg \Gamma_\phi}{\simeq} 3M_{\rm Pl}^2 H_e^2 \left(\frac{a_e}{a}\right)^{3(1+\overline{w})}$$

$$\rho_{\mathcal{R}}(a) = \frac{6M_{Pl}^2 H_e \Gamma_\phi^e}{5-3\overline{w}-2\beta} \left[\left(\frac{a_e}{a}\right)^{\beta+3(1+\overline{w})/2} - \left(\frac{a_e}{a}\right)^4\right]$$



Example model

As an illustration, we consider
the α-attractor T-model:

$\alpha = 1/6$,
$\Lambda = 3 \cdot 10^{-3}\, \mathrm{M_{Pl}}$

$$V(\phi) = \Lambda^4 \tanh^{2n}\left(\frac{|\phi|}{\sqrt{6\alpha}M_{\rm Pl}}\right)$$

R. Kallosh et al. , arXiv:1306.5220
R. Kallosh et al. , arXiv:1311.0472

$$\simeq \begin{cases} \Lambda^4 & |\phi| \gg M_{\rm Pl} \\ \Lambda^4 \left|\dfrac{\phi}{M_{\rm Pl}}\right|^{2n} & |\phi| \ll M_{\rm Pl} \end{cases},$$

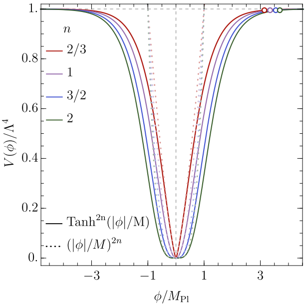
where $n > 0$, $\sqrt{6\alpha} \lesssim 10$, and $\Lambda \lesssim 1.6 \times 10^{16}\ \mathrm{GeV}$.

N. Aghanim et al.,arXiv:1807.06209

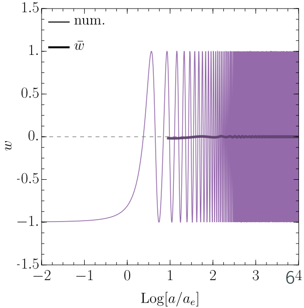
For power-low potentials

$$\overline{w} = \frac{n-1}{n+1}$$

- $n = 2/3$ → $-1/5$
- $n = 1$ → 0 matter-like
- $n = 3/2$ → $1/5$
- $n = 2$ → $1/3$ radiation-like

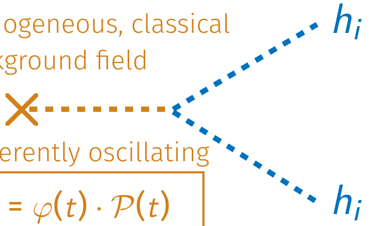


$n=1,\ \alpha=1/6,\ \Lambda=3\cdot10^{-3}\,M_{\rm Pl}$



Higgs portal

$$g_{h\phi} M_{\rm Pl} \phi |\mathbf{h}|^2$$



Y. Shtanov, et al., arXiv:9407247

$$\phi = \varphi(t) \cdot \mathcal{P}(t)$$

- $\mathcal{P}(t)$: rapidly-oscillating
- $\varphi(t)$: slowly-varying envelope

⇨ **Reheating** i.e., energy transfer between the inflaton and the SM sector

$$\frac{1}{V}\frac{dE_g}{dt} = \rho_\phi \Gamma_\phi = g_{h\phi}^2 M_{\rm Pl}^2 \frac{\varphi^2(t)}{8\pi} \sum_{i=0}^{3} \sum_{k=1}^{\infty} k\omega |\mathcal{P}_k|^2 \sqrt{1 - \left(\frac{2m_{h_i}}{k\omega}\right)^2}$$

⇨ **Higgs mass** induced by the oscillating inflaton background

$$m_{h_0}^2 = g_{h\phi} M_{\rm Pl} \varphi \begin{cases} |\mathcal{P}|\,, & \mathcal{P}(t) > 0 \\ 2|\mathcal{P}|\,, & \mathcal{P}(t) < 0 \end{cases} \qquad v_h = \begin{cases} 0\,, & \mathcal{P}(t) > 0 \\ \sqrt{|m_{h_0}^2|/(2\lambda_h)}\,, & \mathcal{P}(t) < 0 \end{cases}$$

Kinematic suppression

The inflaton decay rate can be written as

effective mass

$$\langle \Gamma_\phi \rangle = \frac{g_{h\phi}^2}{32\pi} \frac{M_{\rm Pl}^2}{m_\phi(a)} \gamma_h(a), \qquad m_\phi(a) = V_{,\phi\phi}|_{\phi=\varphi}$$

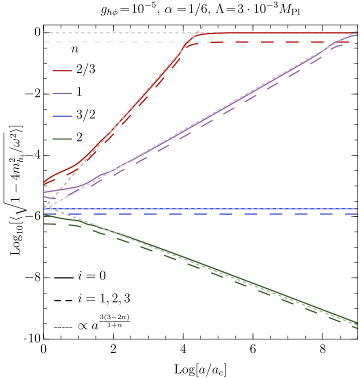
$$\gamma_h(a) \simeq \sum_{i=0}^{3} \sum_{k=1}^{\infty} k |\mathcal{P}_k|^2 \left\langle \sqrt{1 - \left(\frac{2 m_{h_i}(a)}{k\omega(a)}\right)^2} \right\rangle \qquad \omega \propto m_\phi$$

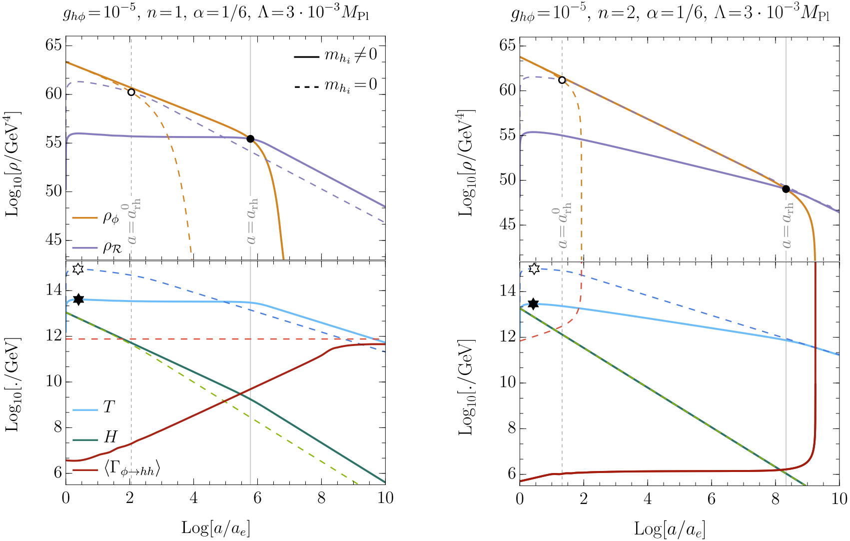
It turns out that

$$\gamma_h \propto \begin{cases} a^0, & m_{h_i} = 0 \\ a^{\frac{3(3-2n)}{1+n}}, & m_{h_i} \neq 0 \end{cases}$$

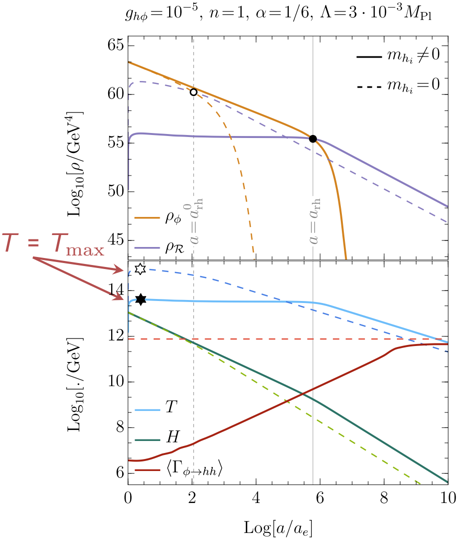
which, in turn, implies

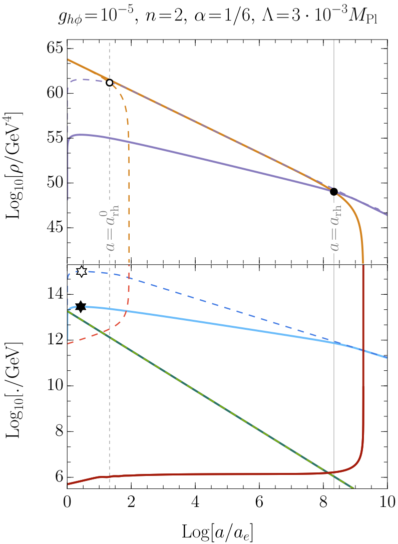
$$\langle \Gamma_\phi \rangle \propto \begin{cases} a^{\frac{3(n-1)}{n+1}}, & m_{h_i} = 0 \\ a^{\frac{6-3n}{1+n}}, & m_{h_i} \neq 0 \end{cases} \qquad -\beta$$





$g_{h\phi}=10^{-5}$, $n=1$, $\alpha=1/6$, $\Lambda=3\cdot10^{-3}M_{\rm Pl}$
$g_{h\phi}=10^{-5}$, $n=2$, $\alpha=1/6$, $\Lambda=3\cdot10^{-3}M_{\rm Pl}$
$m_{h_i}\neq0$
$m_{h_i}=0$
ρ_ϕ
$\rho_{\mathcal{R}}$
$a=a_{\rm rh}^0$
$a=a_{\rm rh}$
T
H
$\langle\Gamma_{\phi\to hh}\rangle$
$\mathrm{Log}_{10}[\rho/\mathrm{GeV}^4]$
$\mathrm{Log}_{10}[\cdot/\mathrm{GeV}]$
$\mathrm{Log}[a/a_e]$





$m_{h_i}=0$ | $\beta=0,\ \rho_{\mathcal{R}}\propto a^{-3/2}$ | $\beta=-1,\ \rho_{\mathcal{R}}\propto a^{-1}$

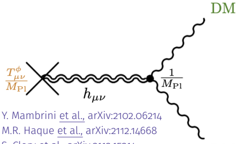
$m_{h_i}\neq0$ | $\beta=-\frac{3}{2},\ \rho_{\mathcal{R}}\propto a^{0}$ | $\beta=0,\ \rho_{\mathcal{R}}\propto a^{-2}$

Spin-1 Dark Matter

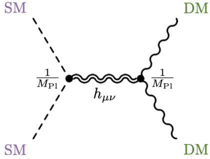
$$\mathcal{L}_{\rm DM} = -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} + \frac{1}{2} m_X^2 X_\mu X^\mu + \mathcal{L}_{\rm int}$$

$$\mathcal{L}_{\rm int} = \frac{h^{\mu\nu}}{M_{\rm Pl}} \left(T^{\mu\nu}_{\phi} + T^{\mu\nu}_{X} + T^{\mu\nu}_{\rm SM} \right)$$

Gravitational production



Y. Mambrini et al., arXiv:2102.06214
M.R. Haque et al., arXiv:2112.14668
S. Clery et al., arXiv:2112.15214



M. Garny et al., arXiv:1511.03278
Y. Tang et al., arXiv:1708.05138
M. Garny et al., arXiv:1709.09688

Boltzmann equation

$$\frac{dN_X}{da} = \frac{a^2}{H} \left(S_\phi + S_{\rm SM} \right)$$

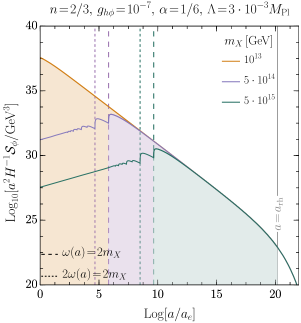
$$N_X \equiv n_X a^3$$

Gravitational production

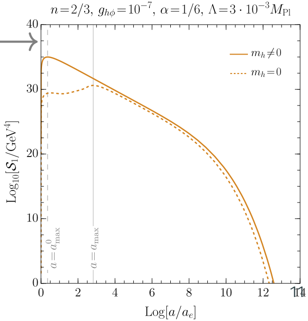
The source terms are

time dependent

$$\mathcal{S}_\phi = \frac{1}{8\pi}\frac{\rho_\phi^2}{M_{\rm Pl}^4}\sum_{k=1}^{\infty}|\mathcal{P}_k^{2n}|^2\left[\left(1-\frac{2m_X^2}{(k\omega)^2}\right)^2+\frac{8m_X^4}{(k\omega)^4}\right]\times\sqrt{1-\frac{4m_X^2}{(k\omega)^2}}$$



$$\mathcal{S}_{\rm SM} = \left[n_0\langle\sigma|v|\rangle_0 + n_{1/2}\langle\sigma|v|\rangle_{1/2} + n_1\langle\sigma|v|\rangle_1\right]\bar{n}_X^2$$



$$\langle\sigma|v|\rangle_1\bar{n}_X^2 \propto \begin{cases} \frac{T^4}{\pi^5}\left(\frac{T}{M_{\rm Pl}}\right)^4, & m_X \ll T, \\ \frac{1}{16\pi^4}\frac{m_X^5\,T^3}{M_{\rm Pl}^4}e^{-2m_X/T}, & m_X \gg T. \end{cases}$$

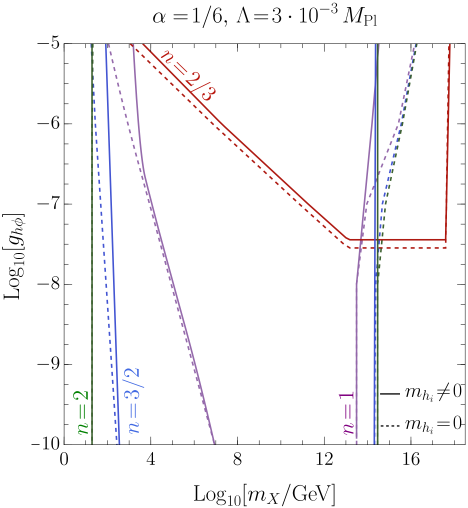
Thermally-averaged cross-section for the annihilation of massless SM vectors

The DM relic abundance can be calculated as

$$\Omega_X^{\rm grav} h^2 \simeq \frac{m_X}{\rho_c} \frac{N^{\rm grav}(a_{\rm rh})}{a_{\rm rh}^3} \frac{s_0}{s(a_{\rm rh})} h^2 .$$

Successful DM model has to predict the correct amount of DM i.e.,

$$\Omega_X^{\rm grav} h^2 = \Omega_X^{\rm (obs)} h^2 = 0.1198 \pm 0.0012$$



Heavy DM particles are produced by the freeze-in from the SM sector

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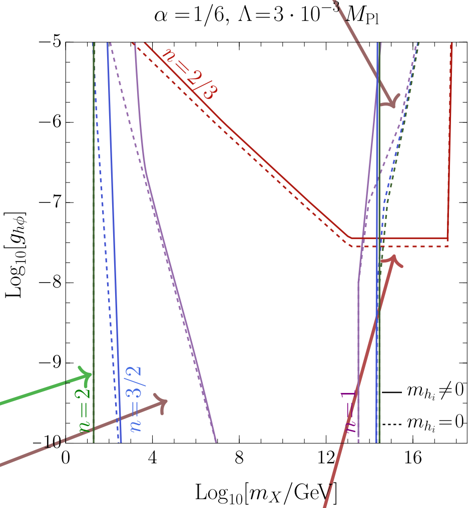

For the $n = 2$ case, $\Omega_X^{\rm grav} h^2$ does not depend on $g_{h\phi}$

Light DM particles are dominantly produced from the inflaton

For the $n = 2/3$ case, $\Omega_X^{\rm grav} h^2$ does not depend on m_X for heavy DM

Summary

We have demonstrated that the non-standard $(n \neq 1)$ cosmologies and the kinematical suppression of radiation production significantly affect the thermal bath evolution and the DM production.

- In particular, we have shown that the duration of reheating and the evolution of the radiation energy density, $\rho_{\mathcal{R}}$, are sensitive to the inflaton potential shape.

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- Moreover, we have discussed the role of kinematical suppression in the reheating dynamics. We have demonstrated that the non-zero mass of the Higgs boson leads to the elongation of the reheating period, changes the $\rho_{\mathcal{R}}(a)$ and $T(a)$ evolution, and conduces to the decrease of $T_{\max}$.

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- Finally, we have pointed out that the DM freeze-in production is very sensitive to the reheating dynamics.

Thank you for your attention!

Back-up slides

EoM for the inflaton

The equation of motion (EoM) for the ϕ field is:

$$\ddot{\phi} + 3H\dot{\phi} + V_{,\phi}(\phi) = 0, \qquad H^2 = \rho_\phi/(3M_{\rm Pl}).$$

We can distinguish two types of solutions to the ϕ's EoM:

1. Slow-roll $\ddot{\phi} \simeq 0$, $\epsilon_V, \eta_V \ll 1$

$$\phi(t) \simeq const.$$

$\epsilon_V = M_{\rm pl}/2(V_{,\phi}/V)^2$

$\eta_V = M_{\rm pl}^2(V_{,\phi\phi}/V)^2$

2. Oscillations

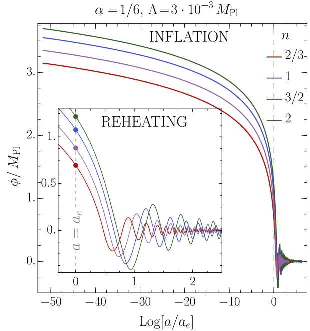
$$\phi(t) = \varphi(t) \cdot \mathcal{P}(t)$$

Slowly-varying Envelope function

$\rho_\phi = V(\varphi)$

Rapidly-oscillating quasi-periodic function

Y. Shtanov et al.,arXiv:9407247



value of the scale factor at the end of inflation ($\epsilon_V = 1$)

Analytical solutions to the inflaton EoM after the end of inflation

negative ($n > 0$)

The EoM for the envelope function φ is given by:

$$\dot{\varphi} = -\frac{3}{n+1} H\varphi, \quad \Rightarrow \quad \varphi(a) = \varphi(a_e)\left(\frac{a}{a_e}\right)^{-\frac{3}{n+1}},$$

while $\mathcal{P}$ satisfies the following approximate equation:

M. A. G. Garcia et al.,arXiv:2004.08404
M. A. G. Garcia et al.,arXiv:2012.10756

$$\dot{\mathcal{P}} \simeq \pm\sqrt{\frac{m_\phi^2(1-|\mathcal{P}|^{2n})}{n(2n-1)}}, \qquad m_\phi^2 = 2n(2n-1)\Lambda^2\left(\frac{\Lambda}{\sqrt{6\alpha}M_{\rm Pl}}\right)^2\left(\frac{\rho_\phi}{\Lambda^4}\right)^{\frac{n-1}{n}}.$$

The solution to the above equation can be written as

Inverse of the regularized incomplete beta function

$$\mathcal{P}(t) = \left[I_z^{-1}\left(\frac{1}{2n}, \frac{1}{2}\right)\right]^{\frac{1}{2n}}, \quad z = 1 - \frac{4}{T}(t-t_0),$$

where T denotes the period of the oscillations:

$$T = \frac{\sqrt{16\pi n(2n-1)}}{m_\phi}\frac{\Gamma\left(1+\frac{1}{2n}\right)}{\Gamma\left(\frac{1}{2}+\frac{1}{2n}\right)}.$$

depend on time for $n \neq 1$

Particles production in a classical inflaton background

The inflaton field can be regarded as a homogeneous, classical field that coherently oscillates in time.
For the interactions linear in $\phi = \varphi \cdot \mathcal{P}$, the energy gain per unit volume per unit time due to the pair production of f particles with mass m can be calculated as

$$\frac{1}{V}\frac{dE_g}{dt} = \frac{\varphi^2(t)}{8\pi}\sum_{k=1}^{\infty} k\omega|\mathcal{P}_k|^2\left|\mathcal{M}_{0\to f}(k)\right|^2 \mathrm{Re}\left[\sqrt{1-\frac{4m^2}{k^2\omega^2}}\right],$$

where

$$\mathcal{P}(t) = \sum_{k=-\infty}^{\infty} \mathcal{P}_k e^{-ik\omega t}, \qquad \mathcal{P}_k = \frac{1}{\mathcal{T}(t_0)}\int_{t_0}^{t_0+\mathcal{T}(t_0)} dt\, \mathcal{P}(t) e^{ik\omega t}.$$

The matrix element $\mathcal{M}_{0\to f}$ accounts for the quantum process of two particles production out of the vacuum.

Particles production in a classical inflaton background

For the interactions proportional to the $\phi = \varphi \cdot \mathcal{P}$ term, the lowest-order non-vanishing S-matrix element takes the form

$$\mathcal{S}_{if}^{(1)} = \sum_k \mathcal{P}_k \langle f| \int d^4 x \varphi(t) e^{-ik\omega t} \mathcal{L}_{\rm int}(x) |i\rangle$$

where

$$|i\rangle \equiv |0\rangle , \qquad |f\rangle \equiv \hat{a}_f^\dagger \hat{a}_f^\dagger |0\rangle .$$

If the envelope $\varphi(t)$ varies on the time-scale much longer than the time-scale relevant for processes of particle creation, the S-matrix element can be written as

$$S_{if}^{(1)} = i\varphi(t) \sum_k \mathcal{P}_k \mathcal{M}_{0\to f}(k) \times (2\pi)^4 \delta(k\omega - 2E_f)\delta^3(p_{f_1} + p_{f_2}).$$