



Anisotropic flow at $\sqrt{s_{NN}} = 200$ GeV in Au+Au collisions in AMPT model

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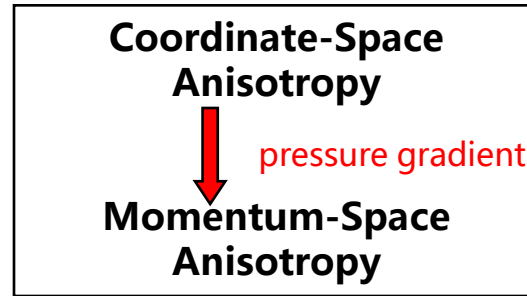
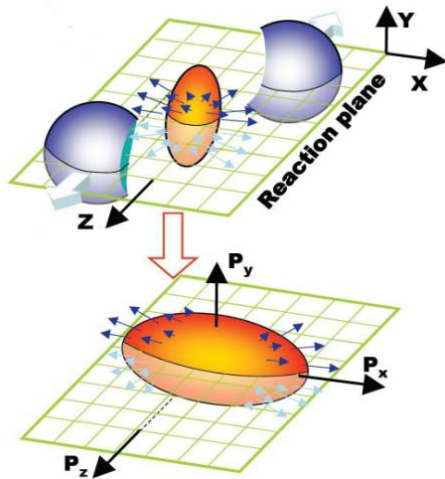
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Outline

- **Introduction**
- **Analysis methods**
- **Results and discussions**
- **Summary**

Anisotropic Flow



Azimuthal distributions of final state particles:

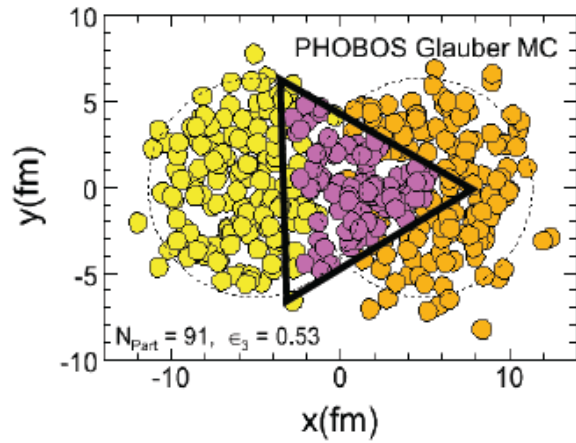
$$E \frac{d^3 N}{d^3 p} = \frac{1}{2\pi} \frac{d^2 N}{p_T dp_T dy} (1 + 2v_1 \cos(\phi - \psi_R) + 2v_2 \cos 2(\phi - \psi_R) + 2v_3 \cos 3(\phi - \psi_R) + \dots)$$

↓

elliptic flow

↓

triangular flow



B. Alver et al. PRC 81, 054905 (2010)

✓ **Triangular flow (v_3) provides a new handle on the initial collision geometry and collective expansion dynamics in heavy ion collisions.**

Analysis Methods

For $n = 2$ or 3 :

initial anisotropy:

$$\varepsilon_n = \frac{\sqrt{\langle r^2 \cos(n\phi) \rangle^2 + \langle r^2 \sin(n\phi) \rangle^2}}{\langle r^2 \rangle}$$

$$\varepsilon_n\{2\} = \sqrt{\langle \varepsilon_n^2 \rangle}$$

$$\varepsilon_n\{4\} = (2\langle \varepsilon_n^2 \rangle^2 - \langle \varepsilon_n^4 \rangle)^{1/4}$$

initial state anisotropy in AMPT model

(r, ϕ) : the polar coordinate position of each parton.

Q-cumulants: $v_n\{2\}$ and $v_n\{4\}$

Event plane method:

$$v_n\{EP\} = \frac{\langle \cos[n(\varphi - \psi_n(p_i))] \rangle}{\mathcal{R}_n}$$

$$\psi_n(p_i) = \frac{1}{n} \left[\arctan \frac{\langle \sin n\varphi \rangle}{\langle \cos n\varphi \rangle} \right]$$

φ : the azimuthal angle of each particle in momentum space.

Participant plane flow:

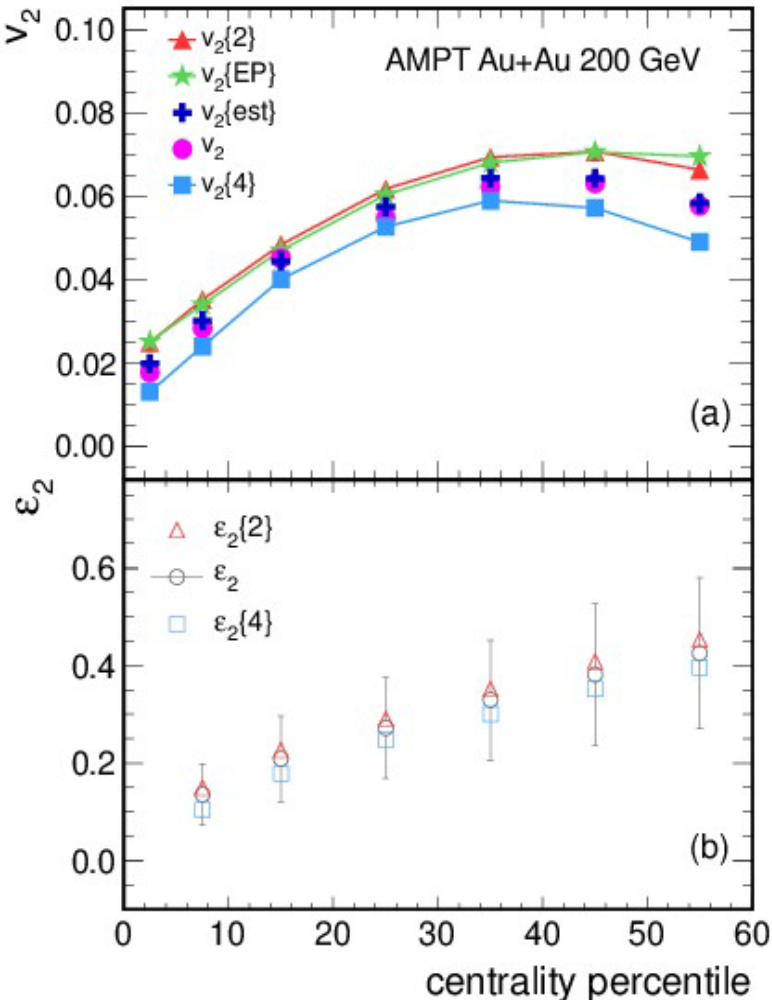
$$v_n = \langle \cos[n(\varphi - \psi_n(r))] \rangle$$

$$\psi_n(r) = \frac{1}{n} \left[\arctan \frac{\langle r^2 \sin(n\phi) \rangle}{\langle r^2 \cos(n\phi) \rangle} \right]$$

(r, ϕ) : the polar coordinate position of each parton.

anisotropic flow:

Integrated Flow (v_2)



S.Voloshin et al. PLB 659,537 (2008)

Gaussian fluctuation, for: $\sigma_{v_2} \ll v_2$

$$v_2\{2\}^2 = v_2^2 + \sigma_{v_2}^2 + \delta$$

$$v_2\{4\}^2 = v_2^2 - \sigma_{v_2}^2$$

δ corrected \rightarrow

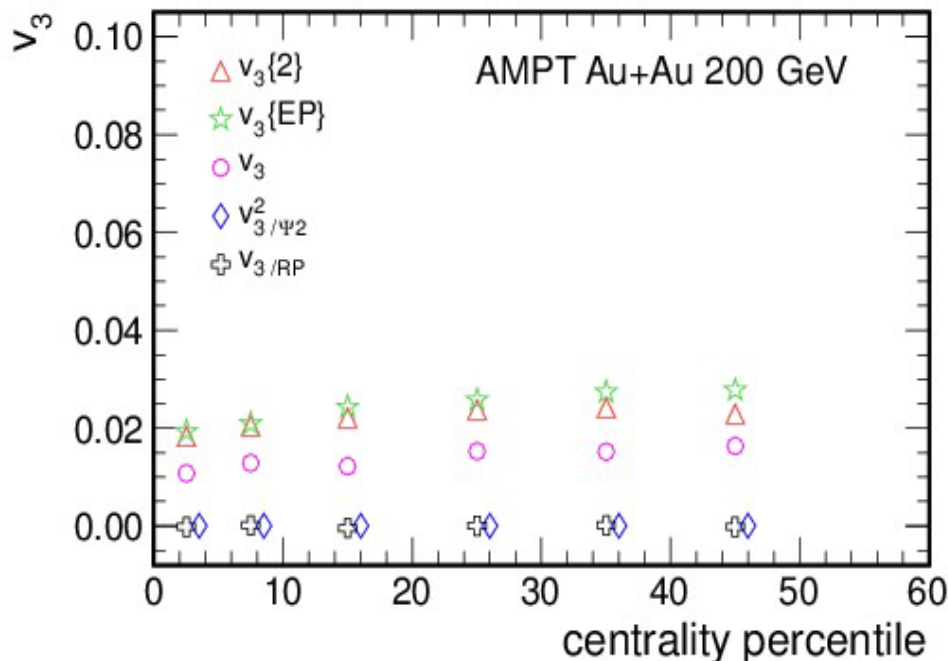
$$v_2\{est\} = \sqrt{(v_2\{2\}^2 + v_2\{4\}^2) / 2}$$

✓ It implies that we can use $v_2\{2\}$ (non-flow corrected) and $v_2\{4\}$ to estimate the participant plane v_2 in experiments.

✓ $v_2\{2\}$ corrected for non-flow effects is almost consistent with $v_2\{EP\}$. (Large η gap was used for $v_2\{EP\}$.)

✓ The efficiency of initial eccentricity transferring into the elliptic flow may be lower in the more peripheral collisions. (The error bar of ϵ_2 shows its fluctuations.)

Integrated Flow (v_3)



large η gap ($|\Delta\eta| > 1$) used for $v_3\{EP\}$.
non-flow subtracted for $v_3\{2\}$.

✓ v_3 measurements show weaker centrality dependence which is qualitatively consistent with the hydrodynamic calculations. B. Alver et al. PRC 82, 034913 (2010)

✓ Large η gap may not remove non-flow contributions entirely for $v_3\{EP\}$.

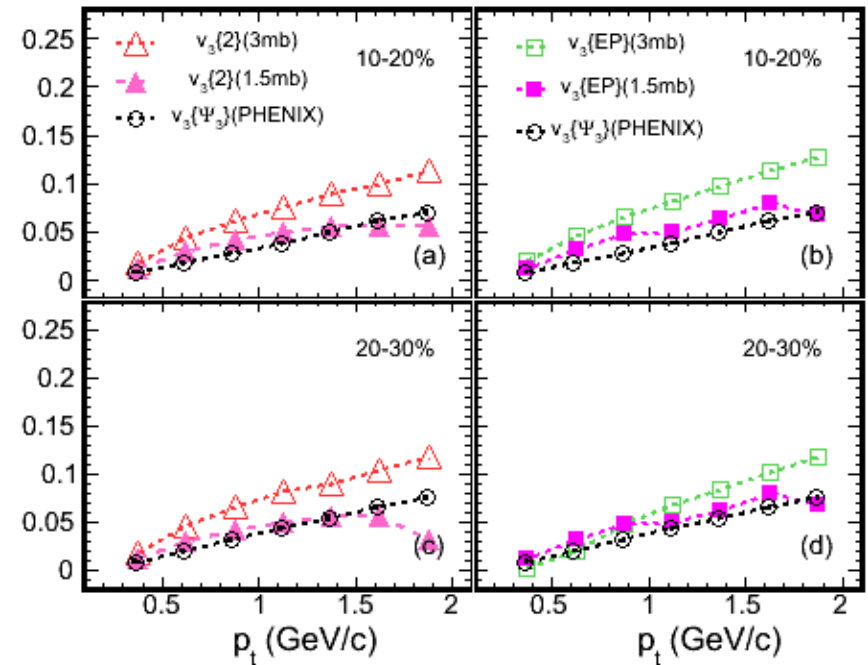
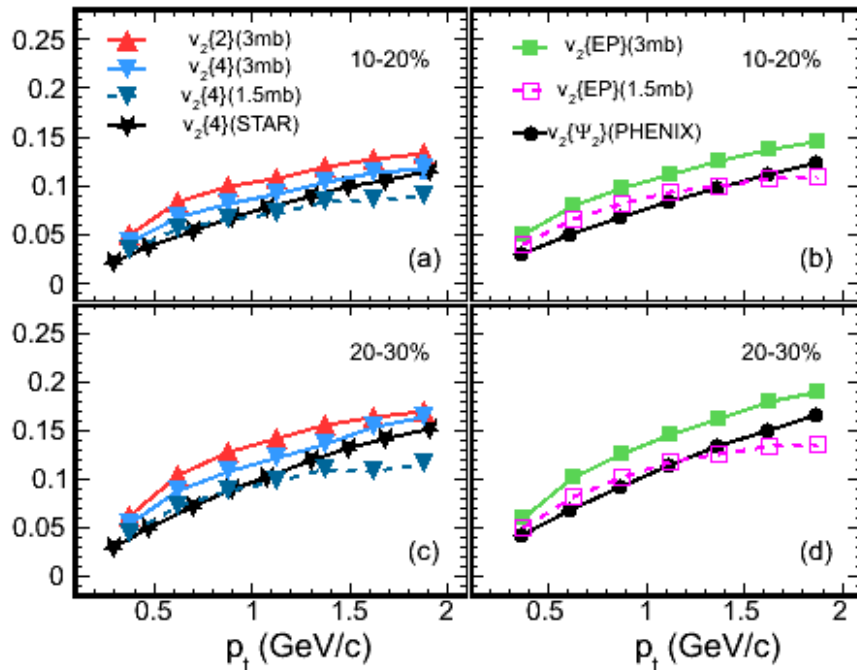
✓ Neither Ψ_{RP} nor Ψ_2 contribute to the v_3 measurement which is consistent with the experimental results. K. Aamodt et al. PRL 107, 032301 (2011)

Differential Flow (v_2, v_3)

AMPT, Au+Au 200GeV

elliptic flow

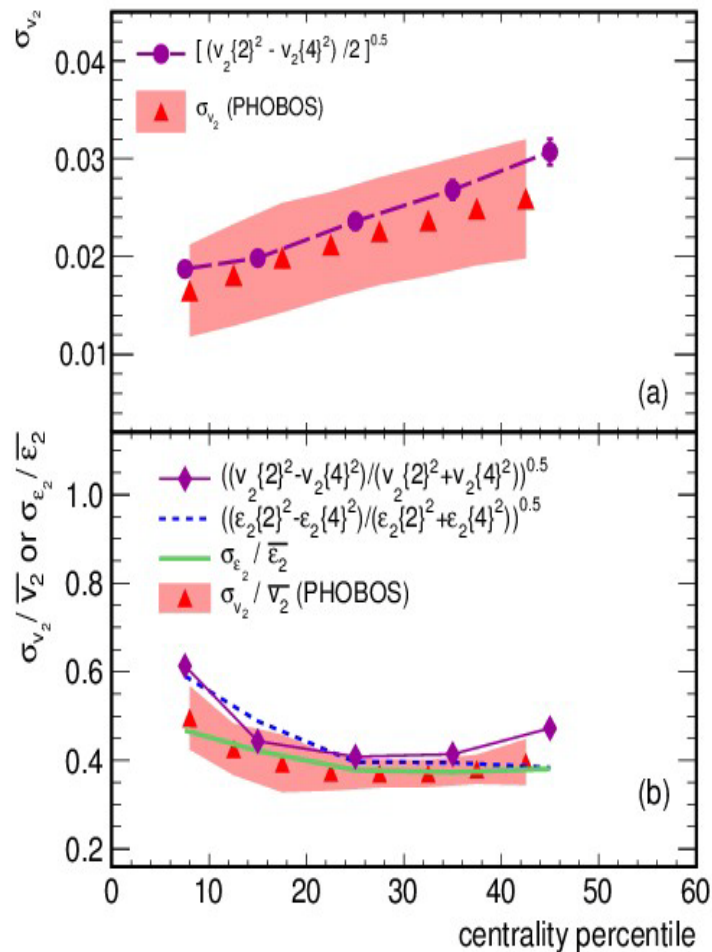
triangular flow



- ✓ Both v_2 and v_3 with 3mb overestimate the measurements in experiments.
- ✓ New set of parameters(1.5mb) can describe the experimental measurements better. It suggests that η/s equals to 0.38. [J. Xu and C. M. Ko PRC 84, 014903 \(2011\)](#)

Flow Fluctuations

AMPT, Au+Au 200GeV



initial eccentricity fluctuations \rightarrow elliptic flow fluctuations

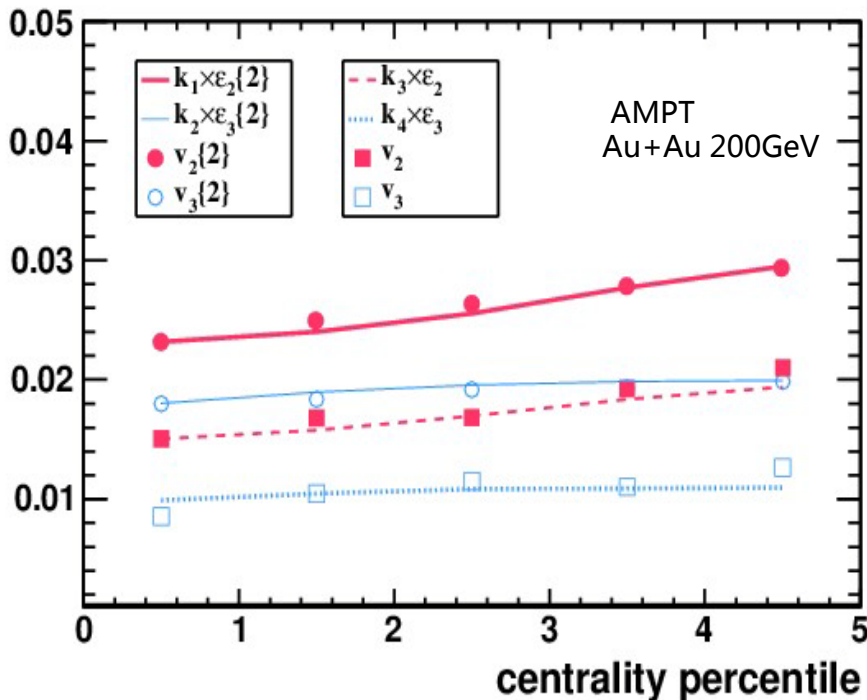
B. Alver et al. PRC 81,034915(2010) B. Alver et al. PRL 104,142301(2010)

- ✓ The estimated flow fluctuations (σ_{v_2}) follow the measurements in PHOBOS.
- ✓ The relative flow fluctuations are consistent with the relative eccentricity fluctuations except for the peripheral collisions. **It provides a basis for the initial fluctuation measurements in experiments.**
- ✓ There are deviations between the estimated and real eccentricity fluctuations in the more central collisions. (The condition ($\sigma_{v_2} \ll v_2$) may be not valid in this region.)

Anisotropy and Anisotropic Flow

In a small centrality range (0-5%), viscous effects don't change too much.
Anisotropic flow might be directly sensitive to the change in the initial spatial geometry.

K. Aamodt et al. PRL 107, 032301 (2011)



$$v_2\{2\} = k_1 \times \epsilon_2\{2\}, v_2 = k_3 \times \epsilon_2$$

$$v_3\{2\} = k_2 \times \epsilon_3\{2\}, v_3 = k_4 \times \epsilon_3$$

✓ Anisotropic flow can be described in terms of the initial eccentricity and triangularity as well as their fluctuations.

$$k_1 \neq k_3, k_2 \neq k_4 \quad \text{Why?}$$

$$v_n / \varepsilon_n$$

The efficiency of the initial anisotropy transferring into the anisotropic flow:

R. S. Bhalerao et al. PLB 627, 49 (2005)

$$k = \frac{v_n}{\varepsilon_n} = \left[\frac{v_n}{\varepsilon_n} \right]_{hydro} \frac{1}{1 + K/K_0},$$

$$\left\{ \begin{array}{l} K_0 : \text{a constant (0.7)} \\ K = (\sigma c_s \frac{1}{S} \frac{dN}{dy})^{-1} \end{array} \right. \quad (\text{Knudsen number})$$

K (related to S and dN/dy)

dN/dy (fluctuates event-by-event)

v_n / ε_n (event-by-event fluctuations)

AMPT calculation

The observed v_n / ε_n fluctuates instead of a constant value.

$$\begin{array}{l} k_1 = \langle k'^2 \rangle^{1/2}, \text{ but } k_3 = \langle k' \rangle \\ k_2 = \langle k''^2 \rangle^{1/2}, \text{ but } k_4 = \langle k'' \rangle \end{array}$$

$$\begin{array}{l} k_1 \neq k_3 \\ k_2 \neq k_4 \end{array}$$

✓The efficiency of the initial anisotropy transferring into the anisotropic flow fluctuates event-by-event.

Summary

- ✓ $v_2\{2\}$ and $v_2\{4\}$ can not only constrain but also estimate the participant plane flow.
- ✓ v_3 measurements show weaker centrality dependence which is qualitatively consistent with the hydrodynamic calculations.
- ✓ Neither Ψ_{RP} nor Ψ_2 contribute to the v_3 measurements.
- ✓ The estimated relative flow fluctuations are almost in an agreement with relative eccentricity fluctuations.
- ✓ v_2 and v_3 measurements can be described in terms of the initial eccentricity and triangularity as well as their fluctuations in the most centrality collisions.

Thanks!