



Constraining jet quenching models in heavy-ion collisions using Bayesian Inference

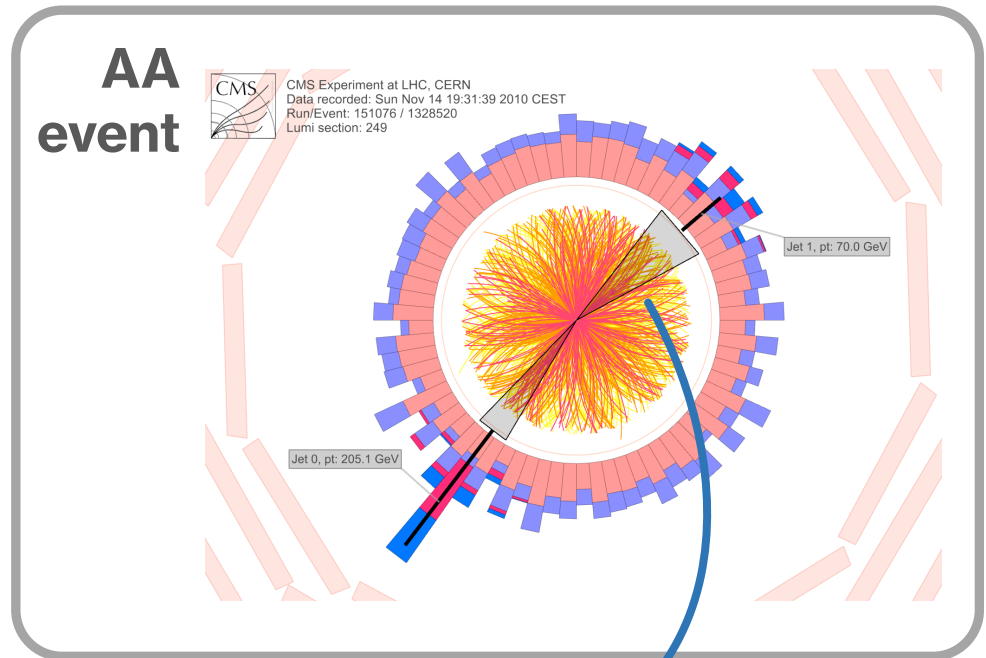
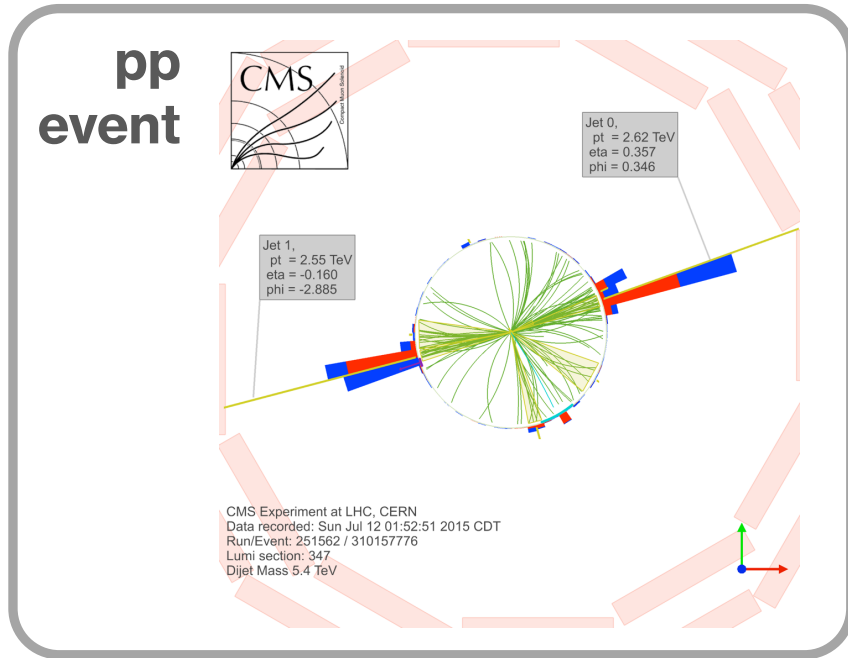
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Konrad Tywoniuk

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QCD@LHC 2022

Jet quenching in heavy-ion collisions

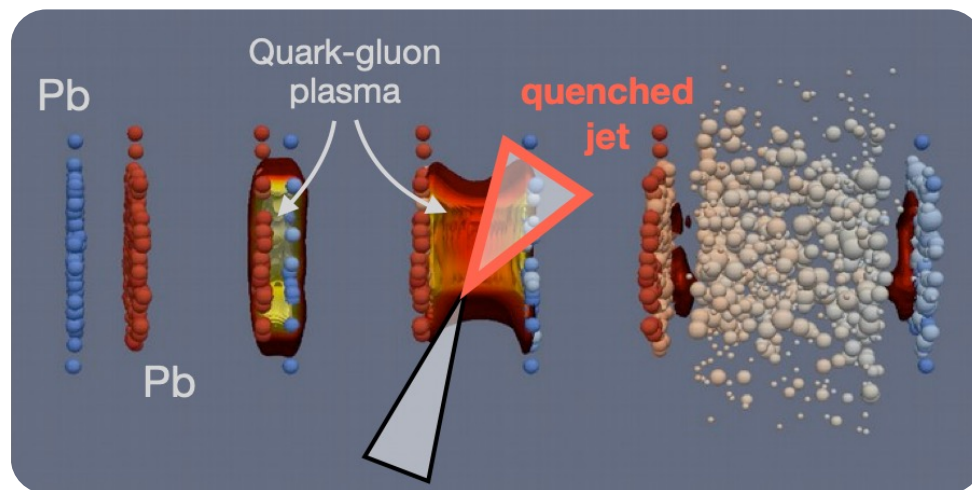
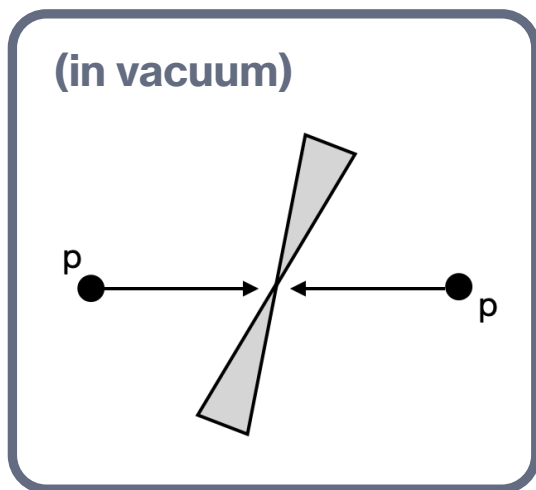


$$\left(\begin{array}{c} \text{AA} \\ \text{collision} \end{array} \right) \neq A \times \left(\begin{array}{c} \text{pp} \\ \text{collision} \end{array} \right)$$

Quenched jet:

- modification of the transverse energy balance
- modification of jet internal structure
- suppression of the jet yields

Jet energy loss distribution



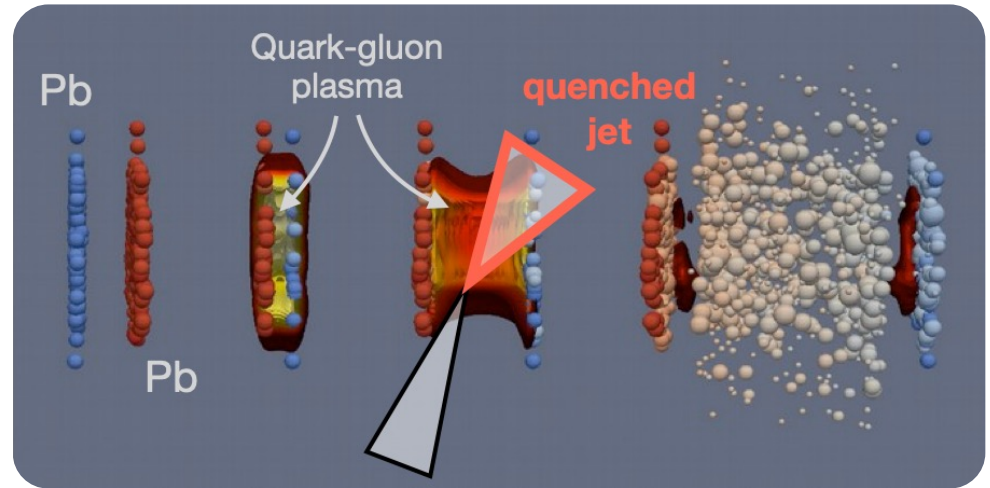
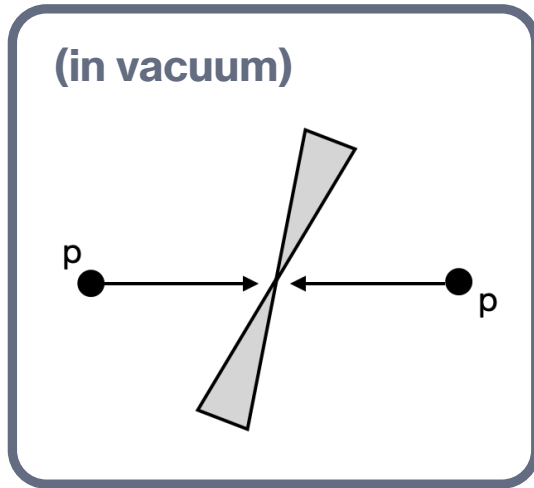
from MADAI collaboration, Hannah Petersen and Jonah Bernhard

Jets in medium:

- **Quark gluon plasma (QGP)** is created in the heavy-ion collision
- Jet created by hard process within QGP probes the medium
- Medium properties can be retrieved by studying jet quenching

$$\begin{array}{ccc}
 \text{jet quenched} & \text{jet in vacuum} & \text{lost energy to} \\
 \text{in medium} & & \text{the medium} \\
 \begin{array}{c} p_T \\ \text{[red triangle]} \end{array} & = & \begin{array}{c} p_T + \epsilon \\ \text{[black triangle]} \end{array} - \epsilon
 \end{array}$$

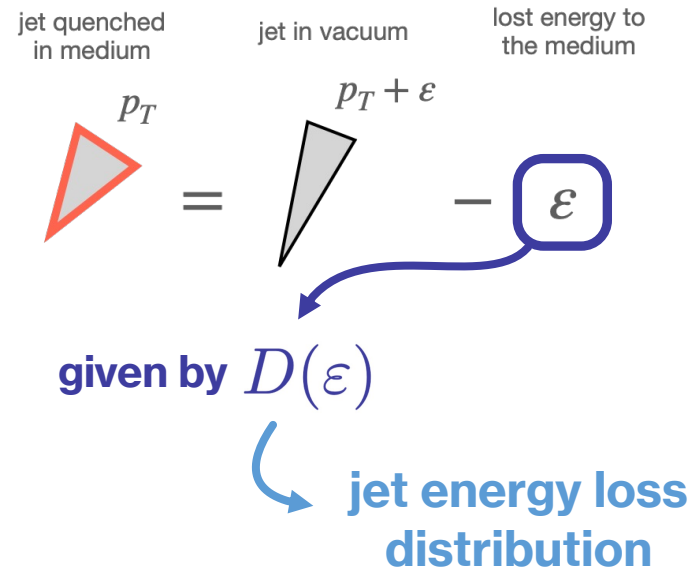
Jet energy loss distribution



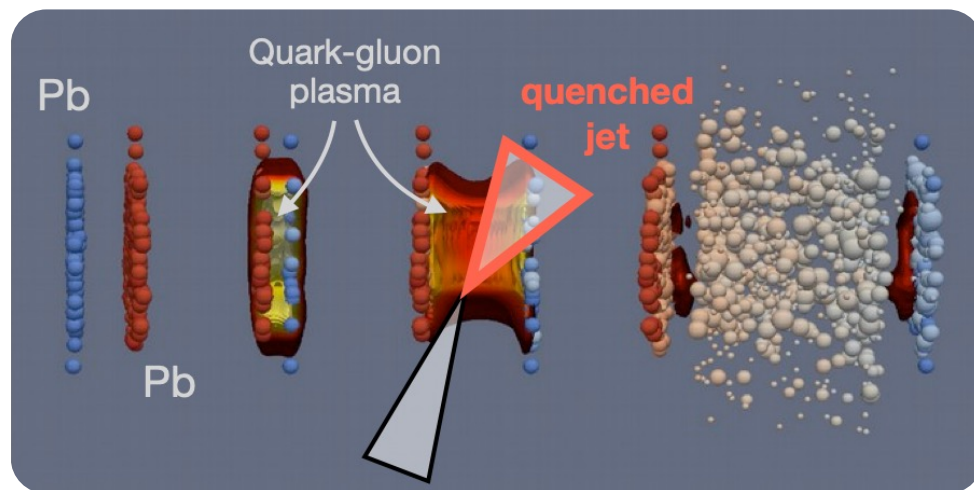
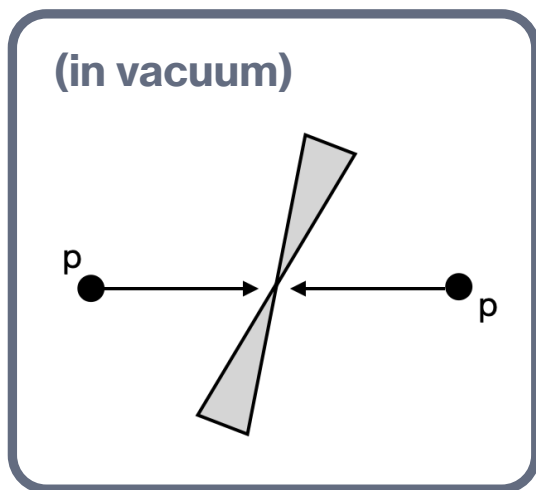
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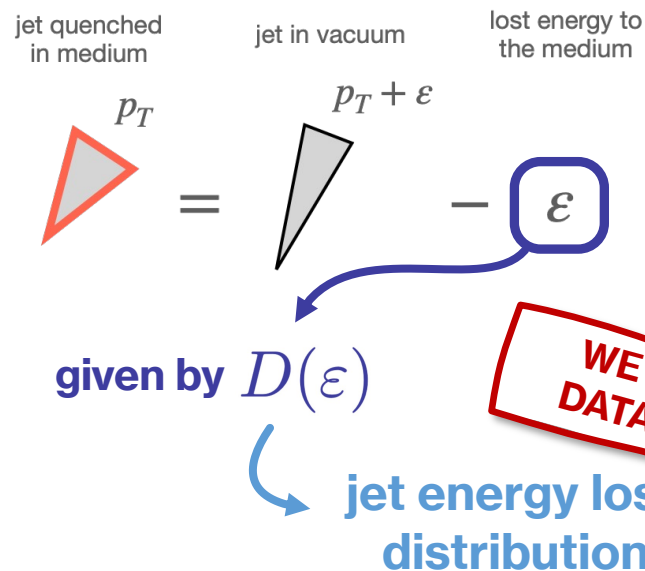
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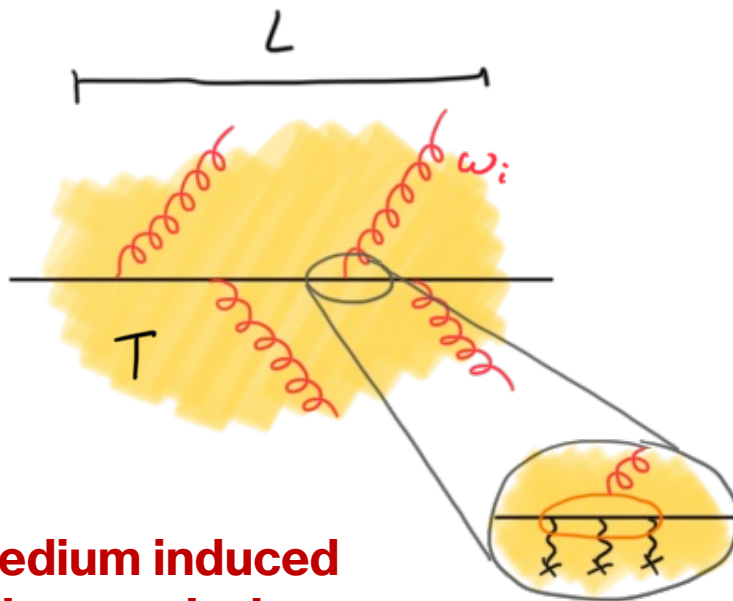
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One parton through the medium

The energy loss distribution via medium induced gluon emissions of a hard parton can be computed from the theory side [Arleo 2002, Baier 2001]



**medium induced
gluon emission**

In the one parton through the medium, it depends on:

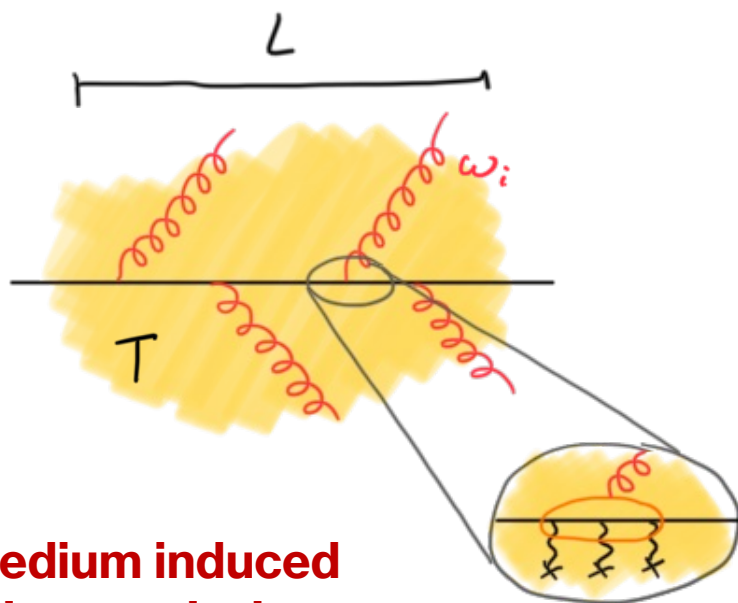
n number of radiated gluons

ω_i energy of emitted gluon i

$\frac{dI}{d\omega}$ **medium-induced
gluon spectrum**

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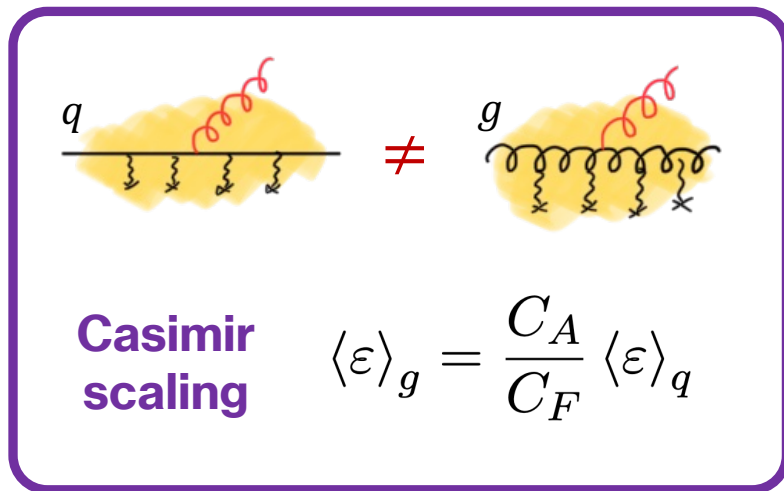
$\frac{dI}{d\omega}$ **medium-induced
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Depends on:

- medium length: L
- transport coefficient: $\hat{q}(T)$
- parton color: C_R

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$$\langle \epsilon \rangle_g = \frac{C_A}{C_F} \langle \epsilon \rangle_q$$

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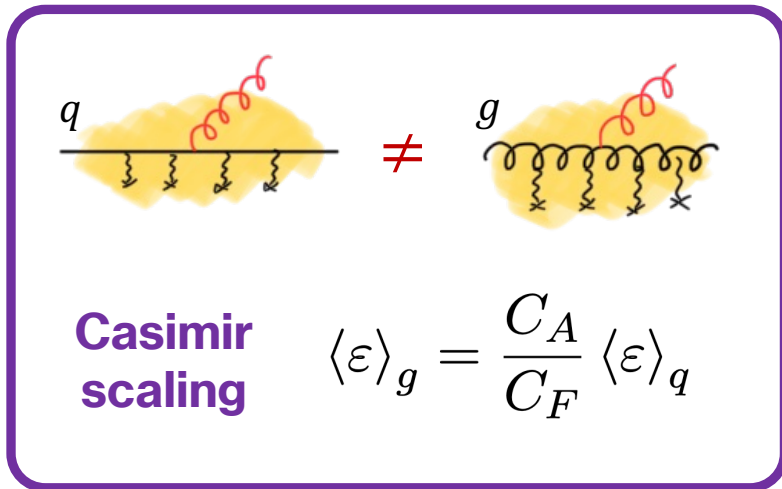
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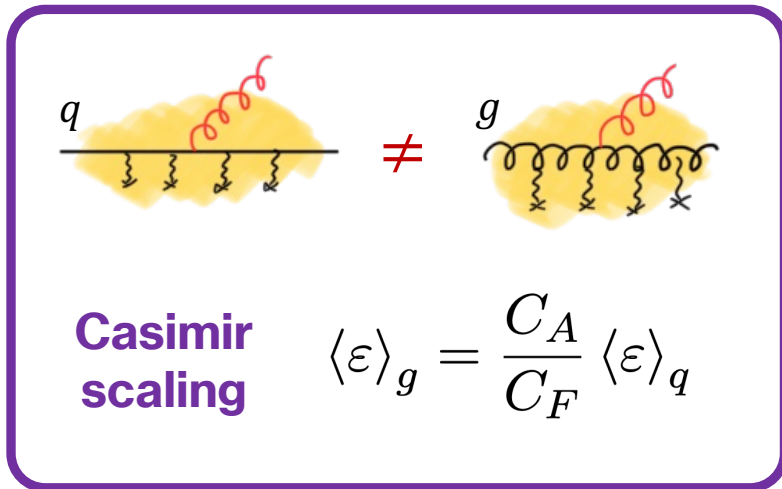
$\frac{dI}{d\omega}$ medium-induced gluon spectrum

Does not depend on:

- p_T^{jet}

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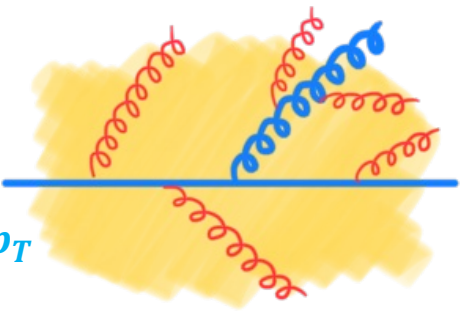
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A jet through the medium



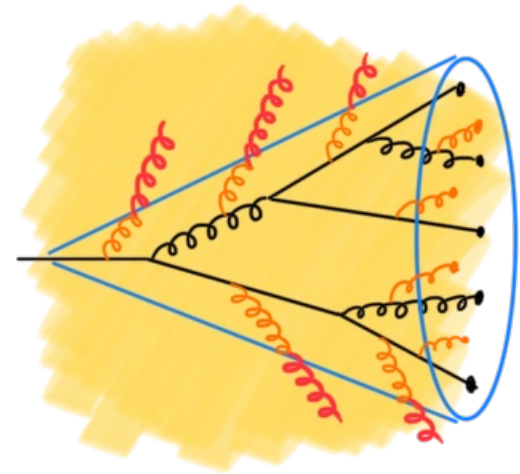
now we have p_T dependence

Factorization

What to keep in $D(\varepsilon)$ to achieve universality?

- has been done [arXiv:1808.05310]:

$$D(\varepsilon | p_T, C_R, \hat{q}(T), L, R) = D(\varepsilon)$$



Factorization

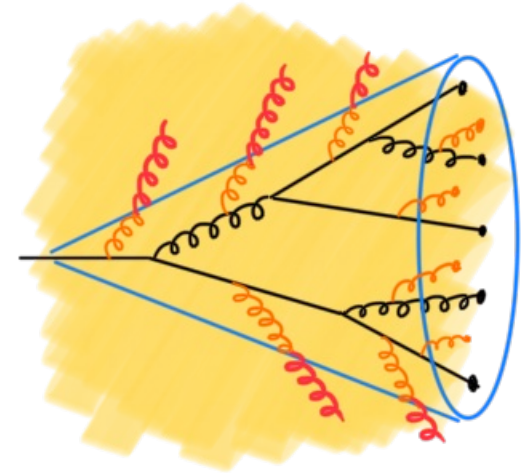
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- adding color dependence:

$$D_i(\varepsilon | p_T, \underline{C}_R, \hat{q}(T), L, R), \quad i = q, g$$



Factorization

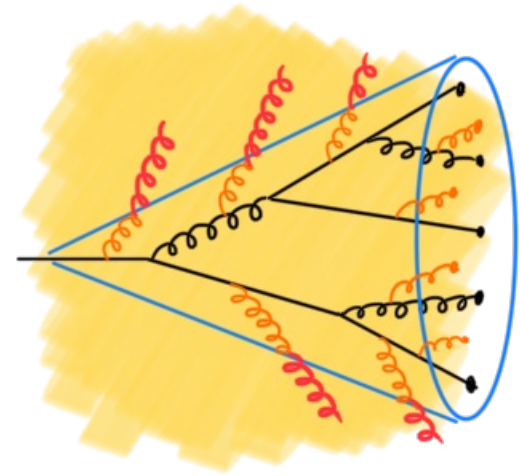
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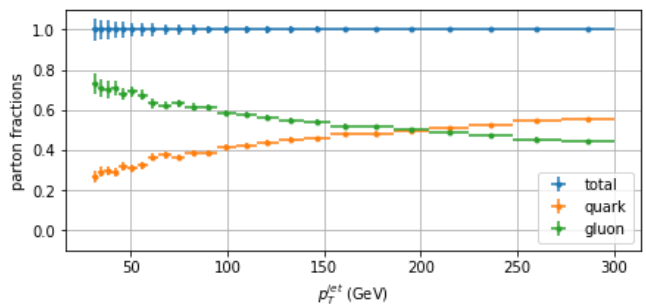
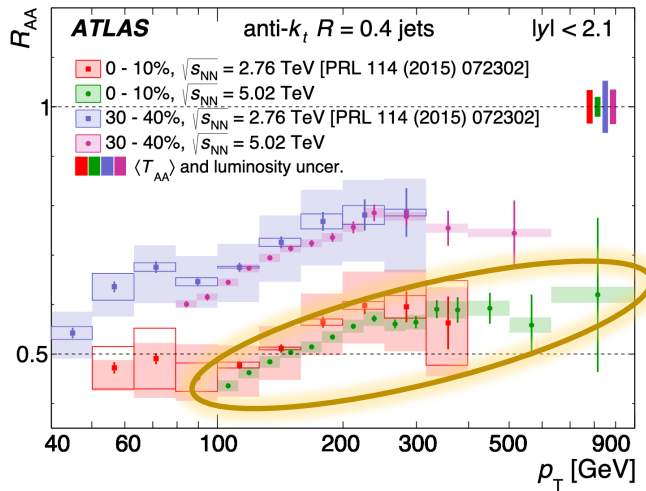
$$\left. \frac{d\sigma^{AA}}{dp_T} \right|_{p_T} = \int_0^\infty d\varepsilon \sum_{i=q,g} D_i(\varepsilon) \left. \frac{d\sigma_i^{vac}}{dp_T} \right|_{p_T+\varepsilon}$$

experimental data →
 $\frac{d\sigma^{AA}}{dp_T} \Big|_{p_T} = \int_0^\infty d\varepsilon \sum_{i=q,g} D_i(\varepsilon) \frac{d\sigma_i^{vac}}{dp_T} \Big|_{p_T+\varepsilon}$
← theory (simulation) ((PYTHIA))

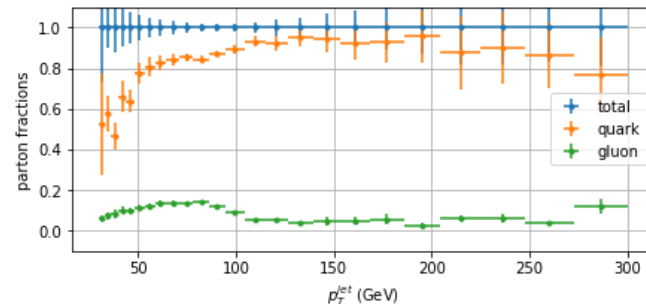
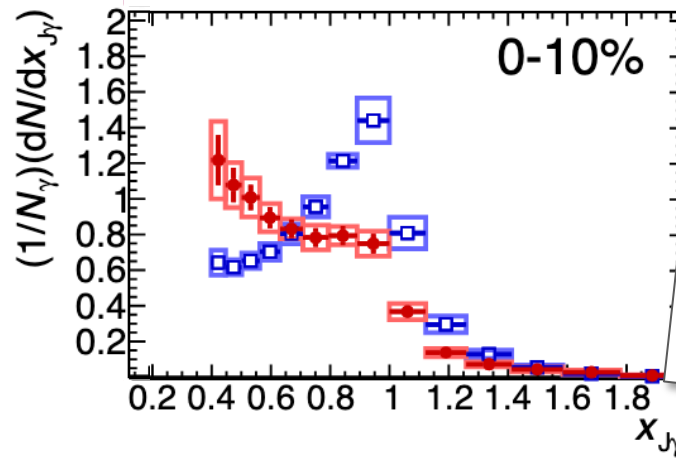
what we want

Available experimental data

inclusive jet events [arXiv:1805.05635]



photon-tagged jet events [arXiv:1809.07280]



different parton fractions

Modelling the jet energy loss



Proposed distribution:

Gamma distribution

$$D(\varepsilon) = \frac{\theta^{-\alpha} \varepsilon^{\alpha-1} e^{-\varepsilon/\theta}}{\Gamma(\alpha)}$$

parameters:

$$\theta = \langle \omega \rangle$$

$$\alpha = \langle n \rangle + 1$$

mean:

$$\langle \varepsilon \rangle = \alpha \theta$$

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Pros:

- interpretable parameters
- convolution of gamma dist. is still a gamma dist.

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Cons:

- more assumptions \Rightarrow more bias

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Different models:

No colour or p_T dependence:

$$\langle \varepsilon \rangle = \alpha \theta$$

Only colour dependence:

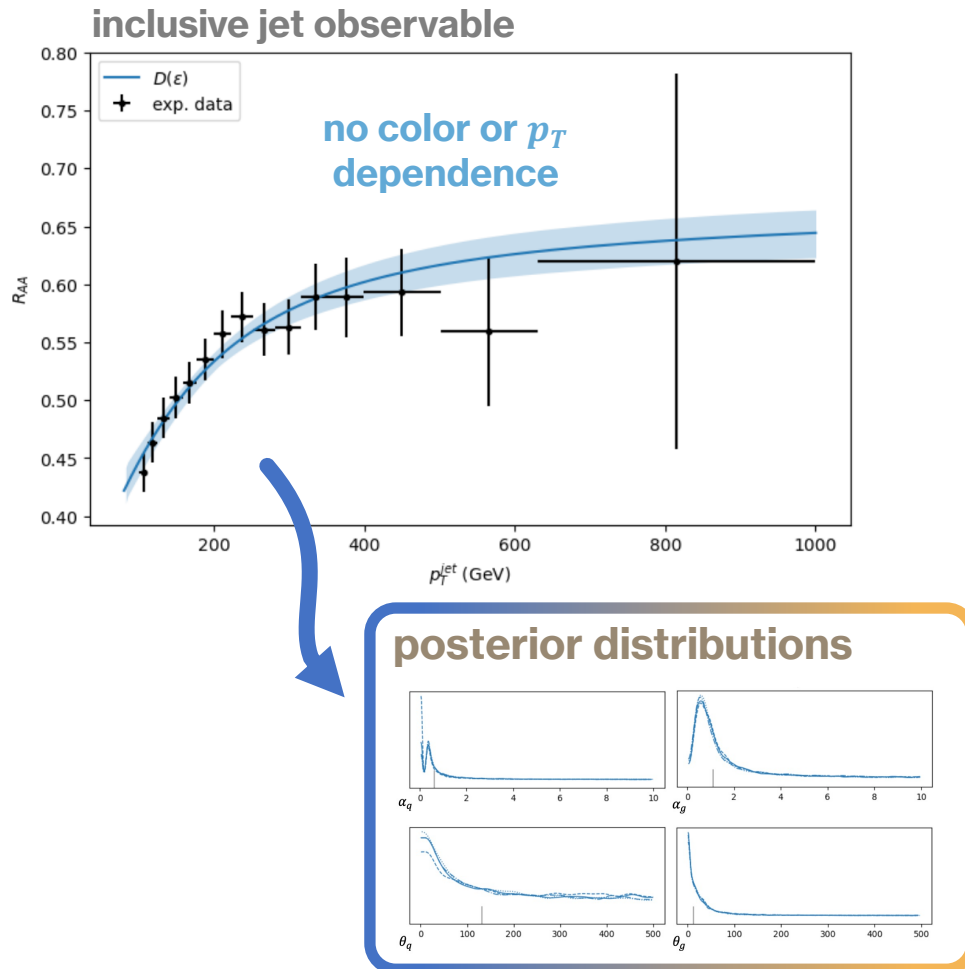
$$\langle \varepsilon \rangle_i = \alpha_i \theta_i, \quad i = q, g$$

Colour + p_T dependence:

$$\langle \varepsilon \rangle_i = \alpha_i \theta_i \ln p_T$$

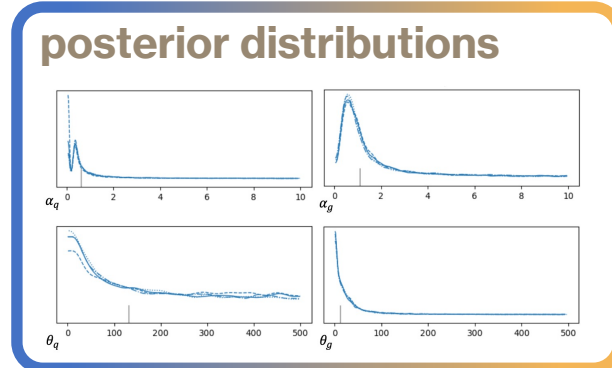
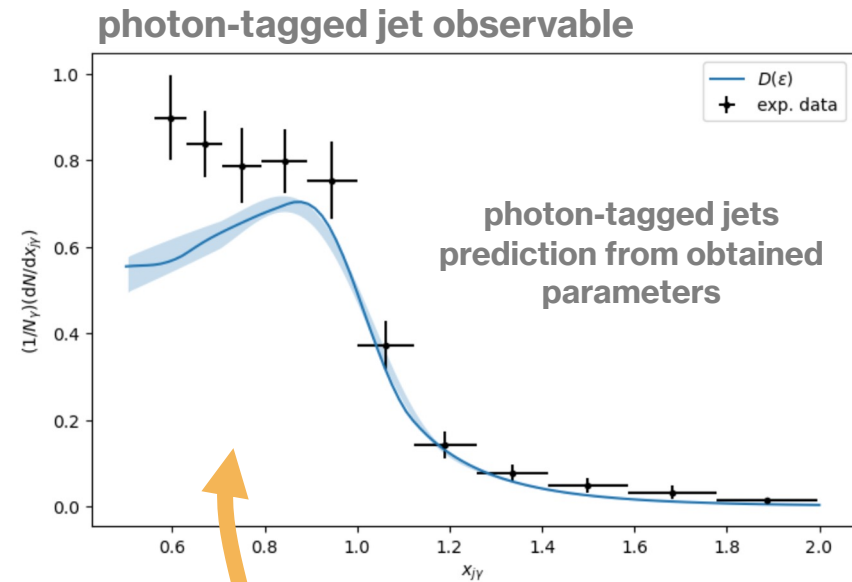
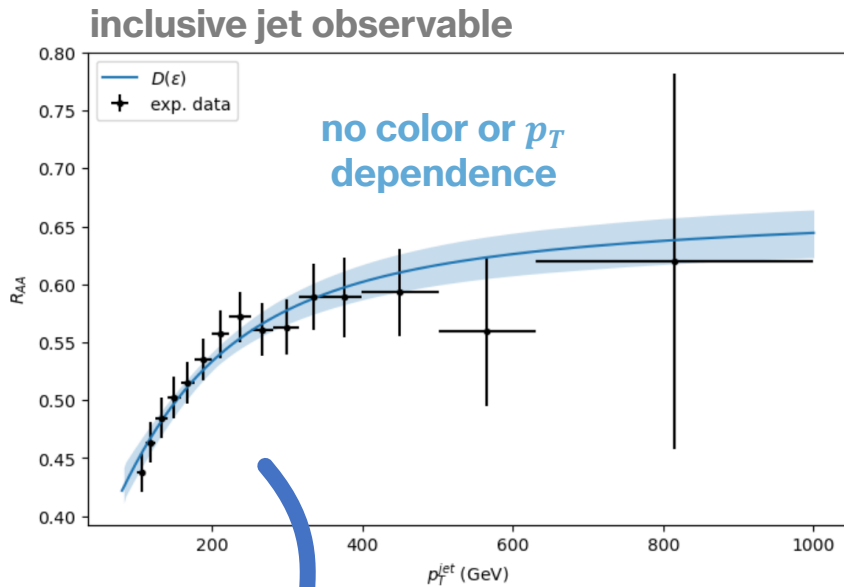
Results (very preliminary)

From the posterior distributions for the parameters, we can reconstruct the R_{AA} as well as predict other observables.



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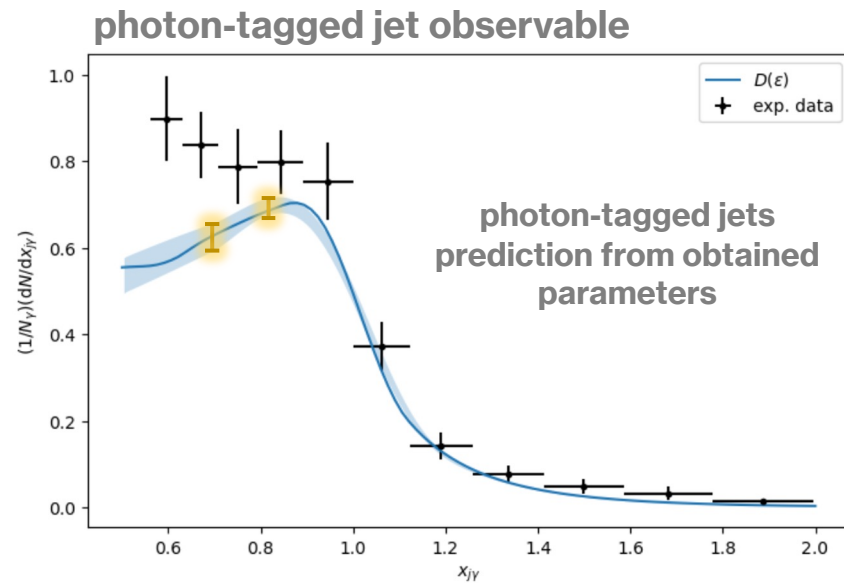
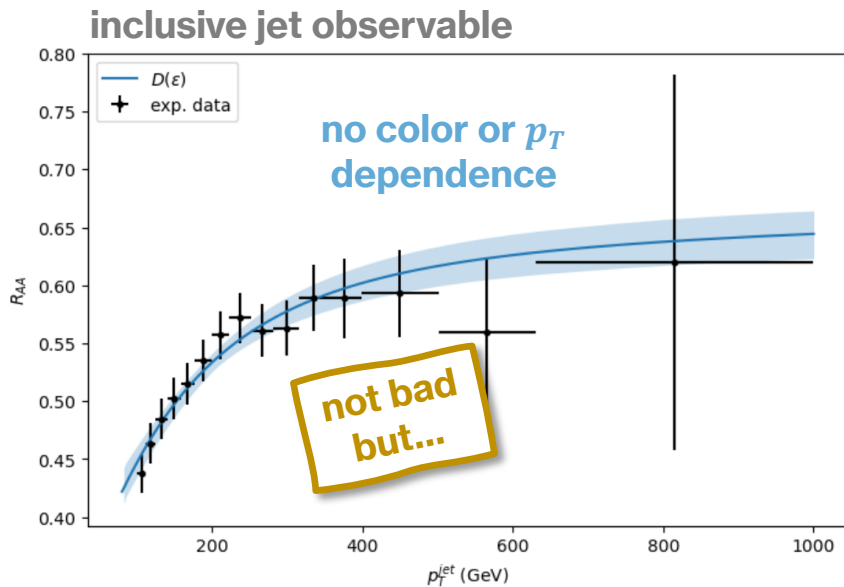
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plug them into
new observable
(which was not fitted)

Results (very preliminary)

From the posterior distributions for the parameters, we can reconstruct the R_{AA} as well as predict other observables.



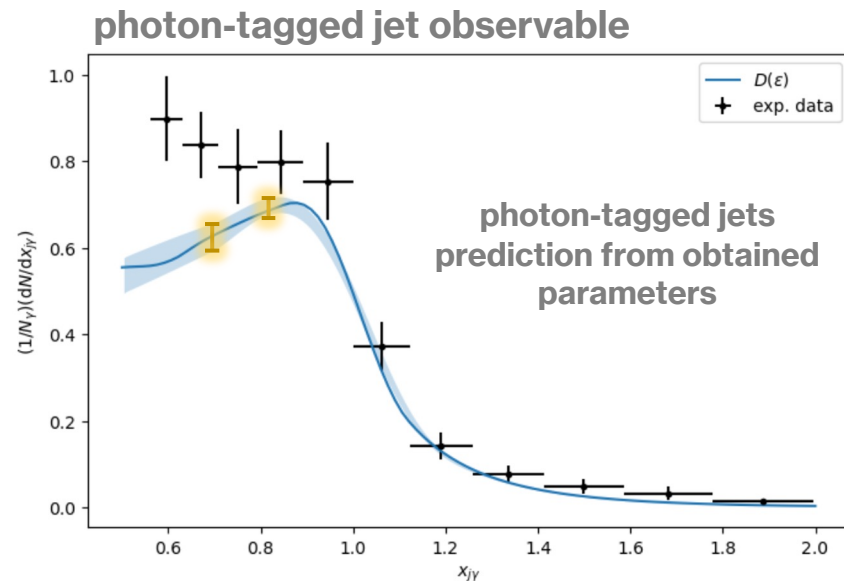
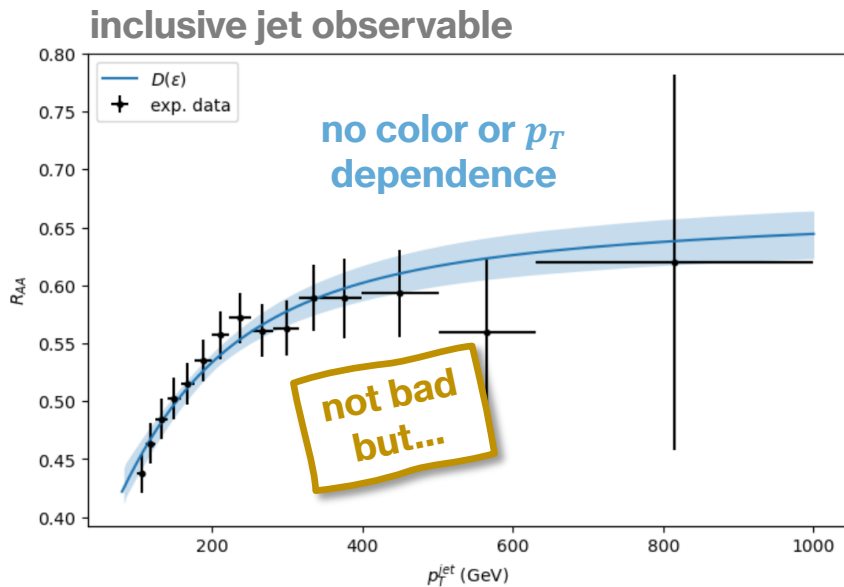
$D(\epsilon)$ with no color or p_T dependence (2 parameters)

- high bias
- low variance

⇒ **underfitting**

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- high bias
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⇒ **underfitting**

model needs to be improved

color dependence
color and p_T dependence

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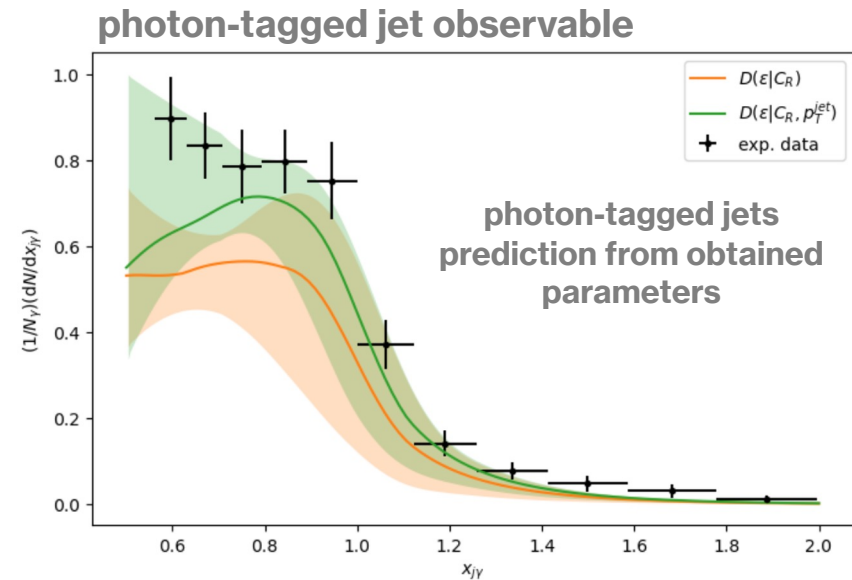
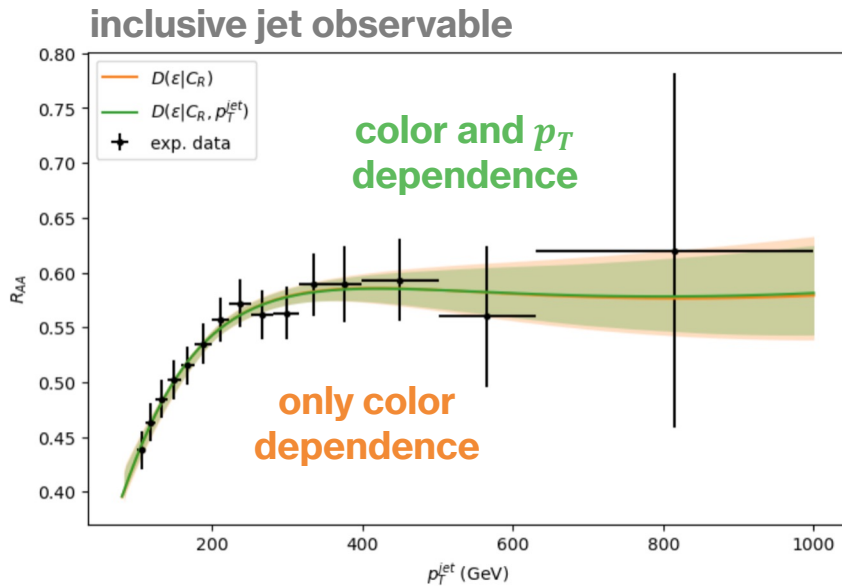
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Results (very preliminary)

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$D_i(\varepsilon)$ with color dependence (4 parameters)

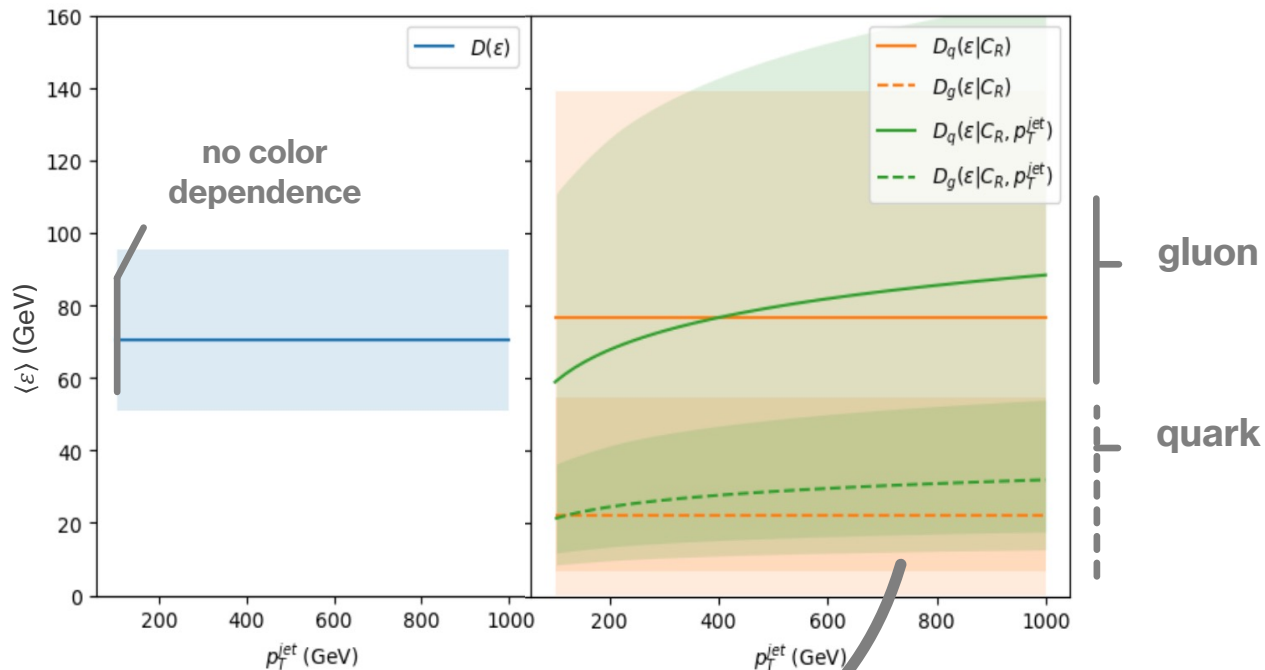
- better agreement for inclusive jet data
- lost in the photon-tagged data

$D_i(\varepsilon)$ with color and p_T dependence (4 parameters + p_T)

- same agreement for inclusive data
- agreement with photon-tagged data recovered

Results (very preliminary)

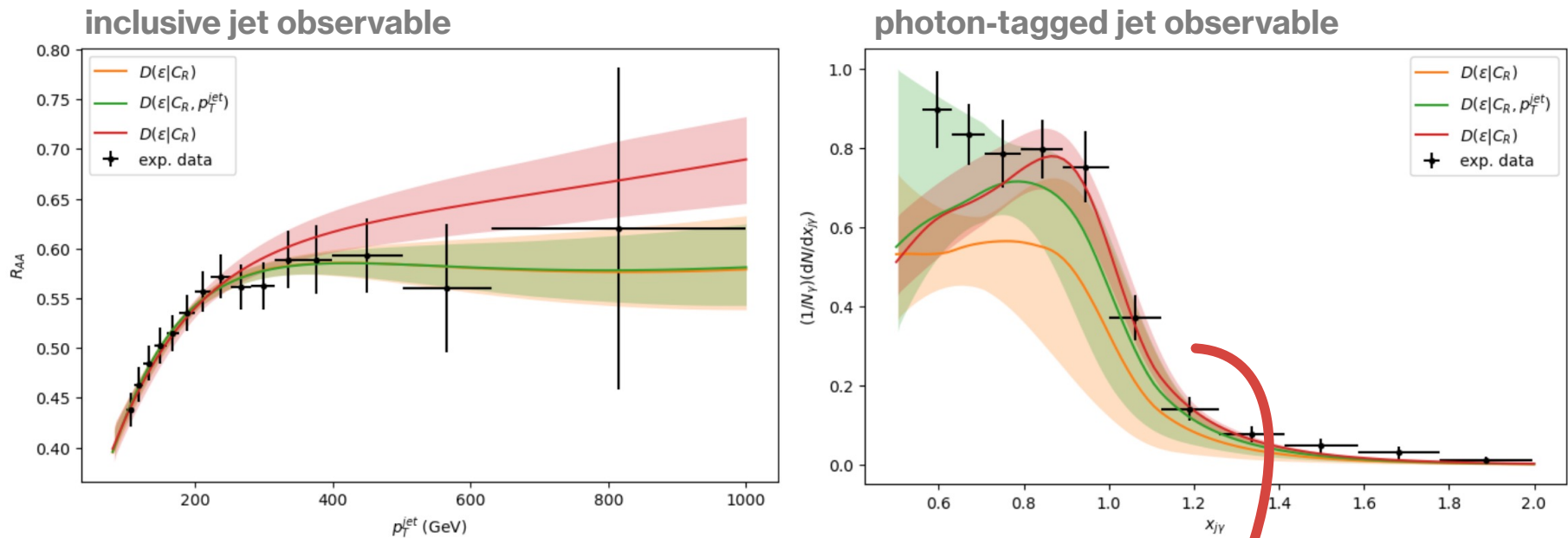
From the posterior distributions for the parameters, we can also calculate the mean energy loss $\langle \varepsilon \rangle$



The inclusive data does not distinguish clearly quarks and gluons (posteriors dist. overlap)

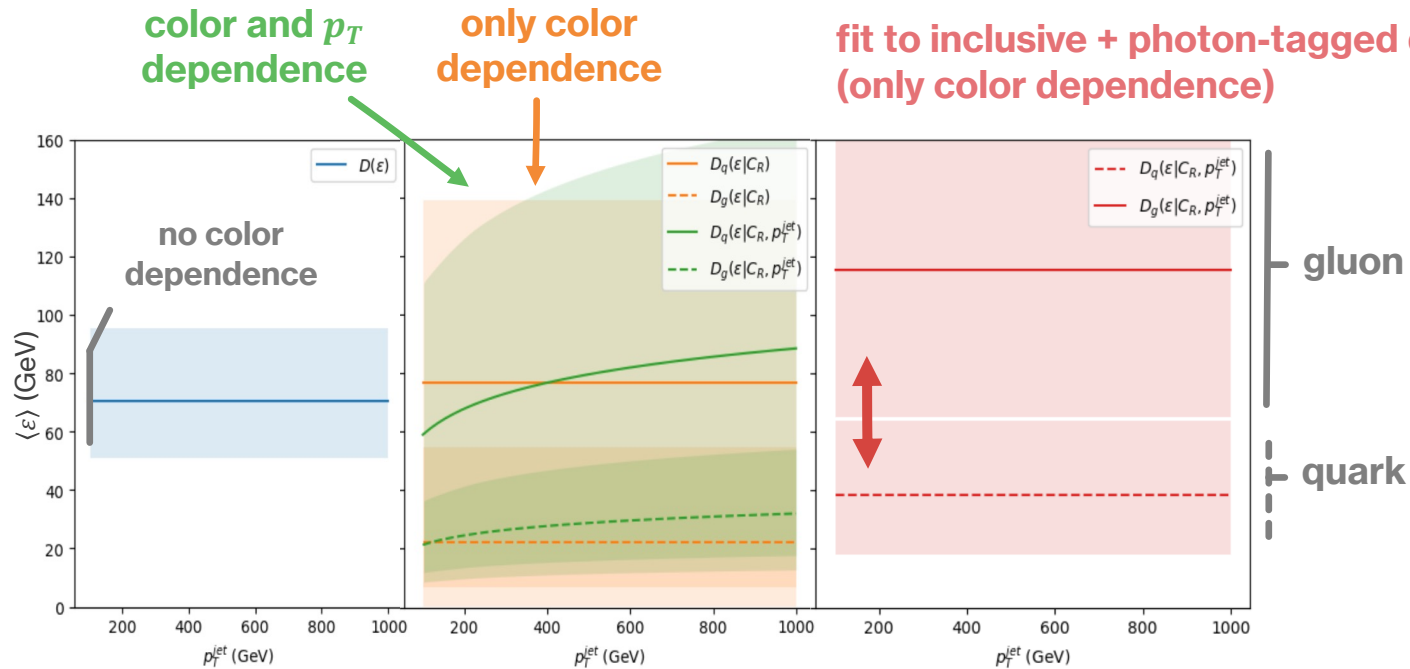
Results (very preliminary)

What if we **fit to inclusive + photon-tagged data (only color dependence)**?



Posterior distribution for photon-tagged jets improves without worsening the inclusive jets (as expected)

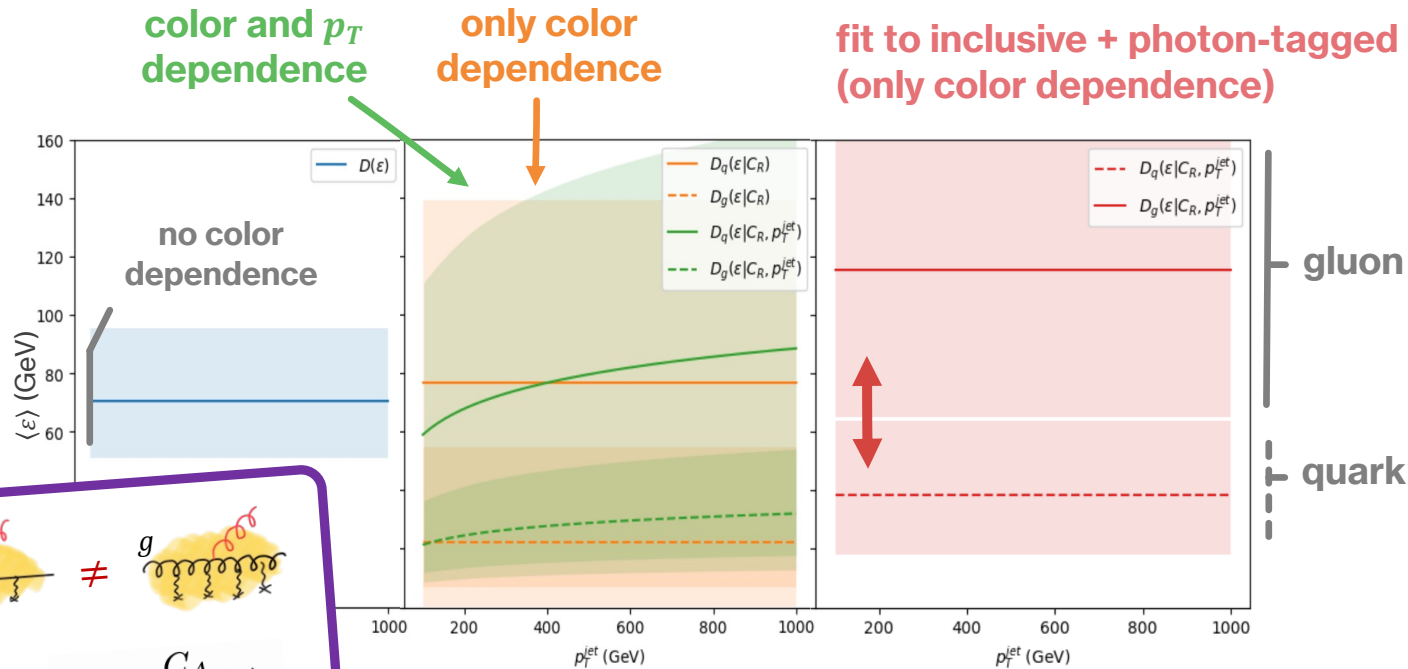
Results (very preliminary)



Adding the photon-tagged data gives more information on quark and gluon jet energy loss

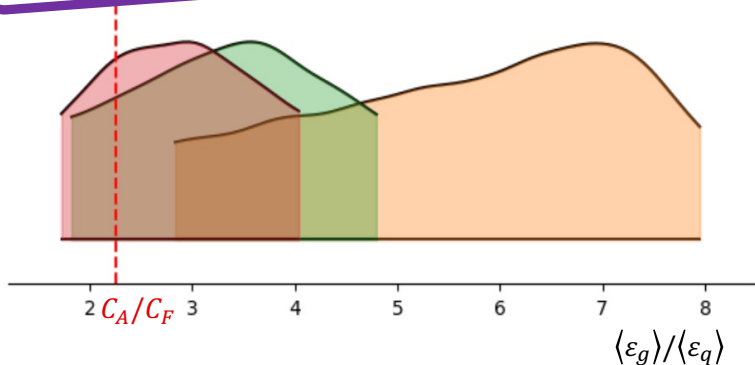
- energy loss of quarks and gluons are distinguished

Results (very preliminary)



$q \neq g$

Casimir scaling

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Adding the photon-tagged data gives more information on quark and gluon jet energy loss

- energy loss of quarks and gluons are distinguished
- Casimir scaling is seen

Summary and next steps



- From theory, we expect that quark and gluon jets lose energy differently in the medium;
- Our goal was then to see if this we can prove this in a data driven way;
- For this, we relied on Bayesian analyses;
- We concluded that by only considering inclusive jet data this distinction is not evident;
- By using photon-tagged jet data, a constrain in this quark and gluon energy loss distribution is achieved.

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Next steps:

- Add different measurements to better learn and validate the model;
- Improve the p_T dependence parameterization;
- Test the model generalization by using the extracted energy loss distributions to predict other kind of jet observables;
- Address the uncertainties from the simulation data;
- Move deeper in ML to find a less biased approach.