

# Determination of the Weak Mixing Angle

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On behalf of the ATLAS, CMS, and LHCb collaborations

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QCD@LHC2022



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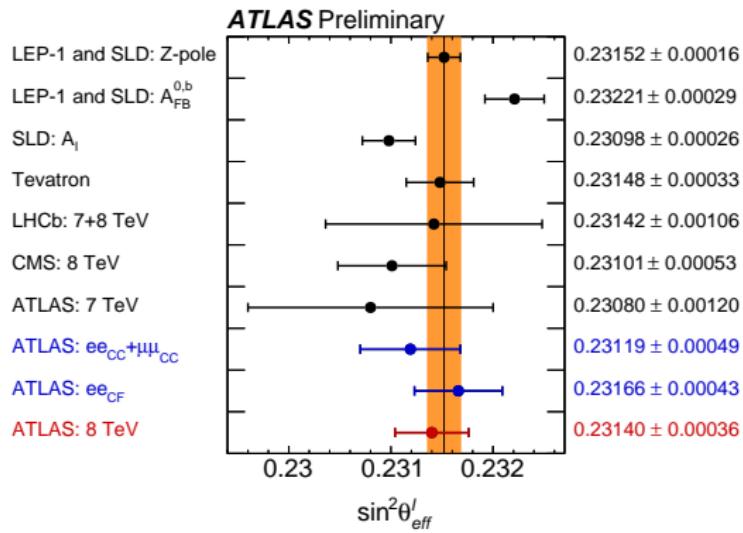


# What is the weak mixing angle

- Key parameter in the electroweak sector of the SM
  - $\sin^2(\theta_w) = 1 - \frac{m_W^2}{m_Z^2}$ ,
- We can also define an effective leptonic mixing angle which at leading order
  - $k_\ell \sin^2(\theta_w) = \sin^2(\theta_{\text{eff}}^{\text{lep}}) = \frac{1}{4|Q_I|} \left(1 - \frac{g_\nu}{g_a}\right)$
- Electroweak radiative corrections in  $k_\ell$  are accurately calculated in standard model
- Precise  $\sin^2(\theta_{\text{eff}}^{\text{lep}})$  measurement can probe new physics contributions to  $m_W$  (an indirect  $m_W$  measurement) and  $k_\ell$



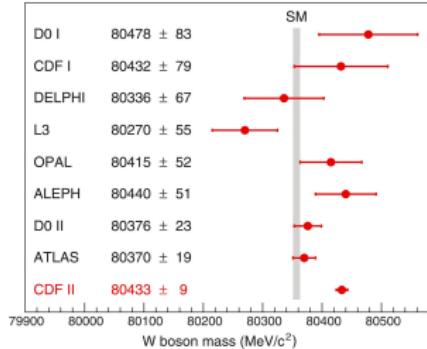
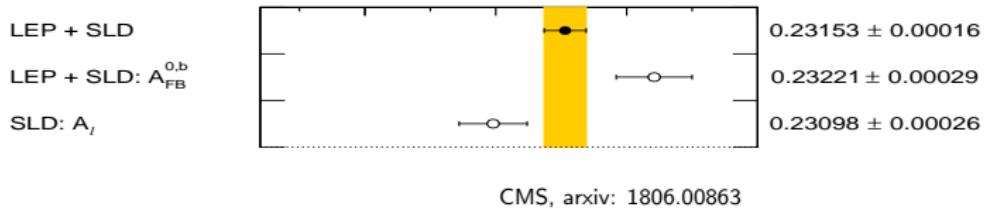
# Current Status



- Current precision driven by LEP/SLD
- Hadron collider measurements are becoming competitive

# Importance of Precision measurements of $\sin^2(\theta_{\text{eff}}^{\text{lep}})$

- The 2 most precise measurements LEP and SLD measurements disagree by  $\sim 3\sigma$ . Could be hint of non standard model processes



- The recent W mass measurement from CDF II has tensions with other measurements and disagrees with the SM at an order of  $7\sigma$

CDF II, DOI: 10.1126/science.abk1781

# Measuring $\sin^2(\theta_{\text{eff}}^{\text{lep}})$ at the LHC

- The full differential cross section in leading order

$$\frac{d\sigma}{dp_T^{\ell\ell} dy^{\ell\ell} dm^{\ell\ell} d\cos\theta d\phi} = \frac{3}{16\pi} \frac{d\sigma^{U+L}}{dp_T^{\ell\ell} dy^{\ell\ell} dm^{\ell\ell}}$$

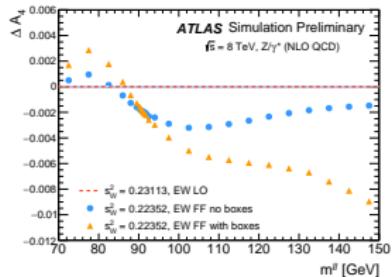
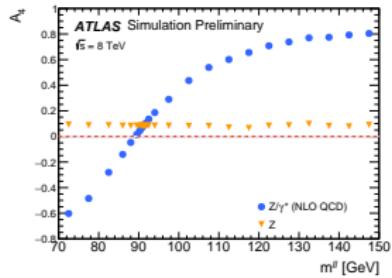
$$\left\{ (1 + \cos^2\theta) + \frac{1}{2} A_0(1 - 3\cos^2\theta) + A_1 \sin 2\theta \cos\phi \right.$$

$$+ \frac{1}{2} A_2 \sin^2\theta \cos 2\phi + A_3 \sin\theta \cos\phi + A_4 \cos\theta$$

$$\left. + A_5 \sin^2\theta \sin 2\phi + A_6 \sin 2\theta \sin\phi + A_7 \sin\theta \sin\phi \right\}.$$

- At first order, only the annihilation  $q\bar{q} \rightarrow Z$  is present

$$\frac{d\sigma}{d(\cos\theta^*)} \propto 1 + \cos^2\theta^* + A_4 \cos\theta^*,$$



ATLAS-CONF-2018-037  
CMS, arxiv: 1806.00863

# Measuring $\sin^2(\theta_{\text{eff}}^{\text{lep}})$ at the LHC

- The mixing of vector and axial vector couplings creates a forwards backwards asymmetry in the decay of Z bosons to dilepton pairs

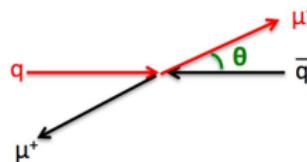
$$q\bar{q} \rightarrow Z/\gamma^* \rightarrow \ell\bar{\ell}$$

- Measure this asymmetry Collins-Soper rest frame (CS frame)

$$A_{FB} = \frac{3}{8} A_4 = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B}$$

- The Z-axis of the CS frame is along the direction of the  $q\bar{q}$  collision
- Z boson rapidity defines the quark direction

$$\frac{d\sigma}{d \cos \theta^*} = A(1+\cos^2 \theta^*) + B \cos \theta^*$$

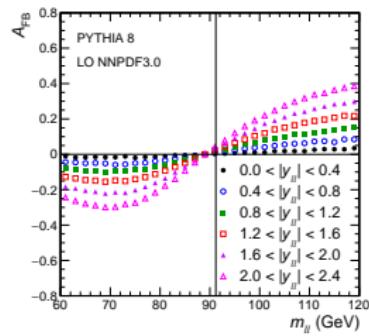
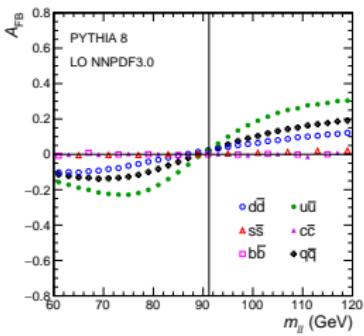
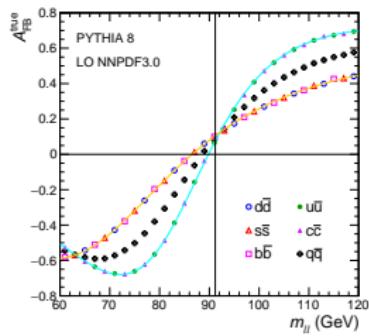


$$\cos \theta^* = \frac{2(P_1^+ P_2^1 - P_1^- P_2^+)}{\sqrt{m_{||}^2(m_{||}^2 + p_{T,||}^2)}} \frac{|p_{Z,||}|}{|p_{Z,||}|}$$

CMS, arxiv: 1806.00863

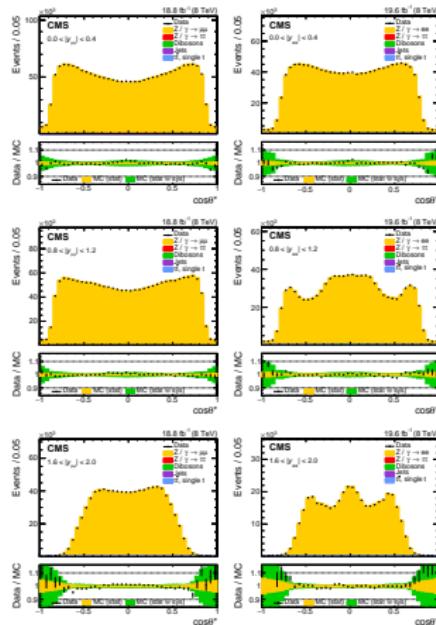
# Measuring $\sin^2(\theta_{\text{eff}}^{\text{lep}})$ at the LHC

- $A_{FB}$  increases with the rapidity of the Z boson,  $Y_Z$
- Only valence quarks contribute to  $A_{FB}$
- At higher  $Y_Z$  the high X parton is likely to be a valence quark and the low X parton the antiquark



# Weighted $A_{FB}$

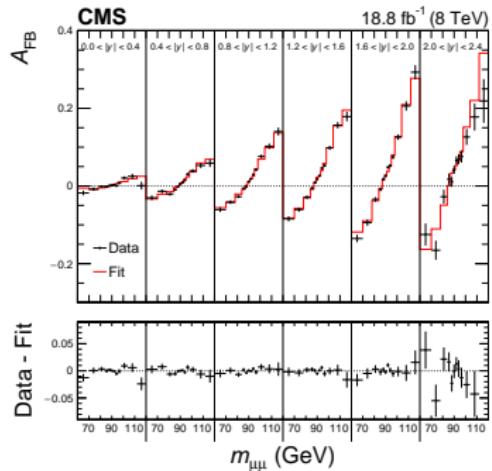
- Weight  $A_{FB}$  by  $\cos \theta^*$
- Weighted  $A_{FB}$  cancels uncertainties that come from efficiencies and acceptance



A. Bodek, Eur.Phys.J.C67:321-334,2010  
 CMS, arxiv: 1806.00863

# Extracting $\sin^2(\theta_{\text{eff}}^{\text{lep}})$

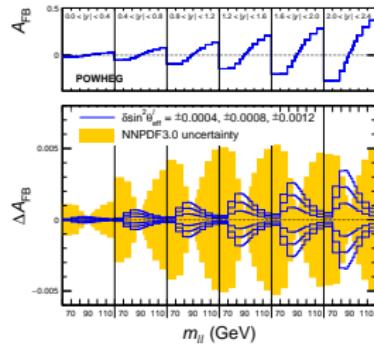
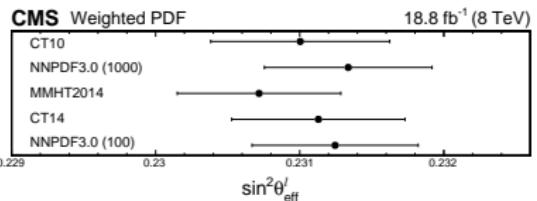
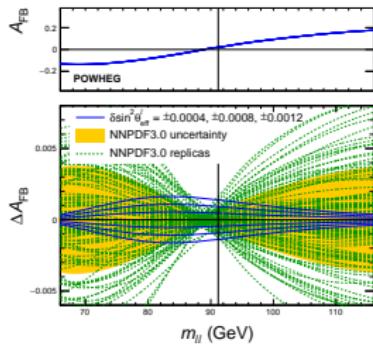
- $A_{FB}$  has a high dependence on mass, this comes from interference of  $Z$  with virtual photon
- By creating templates by varying the value of  $\sin^2(\theta_w)$  we can test which value that the data agrees with



CMS, arxiv: 1806.00863



- Measurement of  $\sin^2(\theta_{\text{eff}}^{\text{lep}})$  has strong dependence on PDFs
- Less effect in high rapidity regions
- ATLAS and CMS constrain PDFs in situ



CMS, arxiv: 1806.00863  
A. Bodek, Eur. Phys. J. C76:115

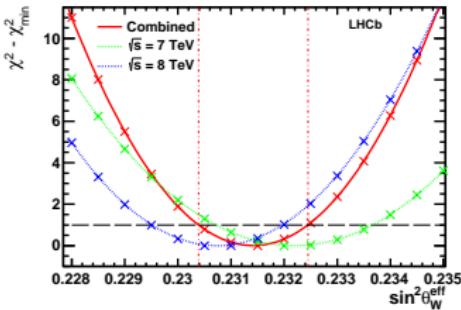
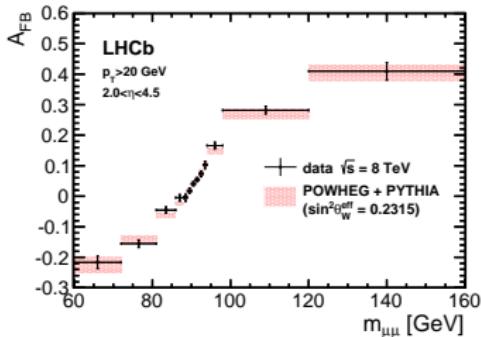
# LHCb Result (arxiv: 1509.07645)



- Combination of 7 TeV ( $1 fb^{-1}$ ) and 8 TeV ( $2 fb^{-1}$ ) data
- Measurement uses the dimuon channel
- High rapidity measurement  $2.0 < Y < 4.5$  with raw  $A_{FB}$

$$\sin^2(\theta_{\text{eff}}^{\text{lep}}) = 0.23142 \pm .0011$$

- The error breaks down as  $\pm 0.00073$  (statistical),  $\pm 0.00052$  (systematic) and  $\pm 0.00056$  (theoretical)



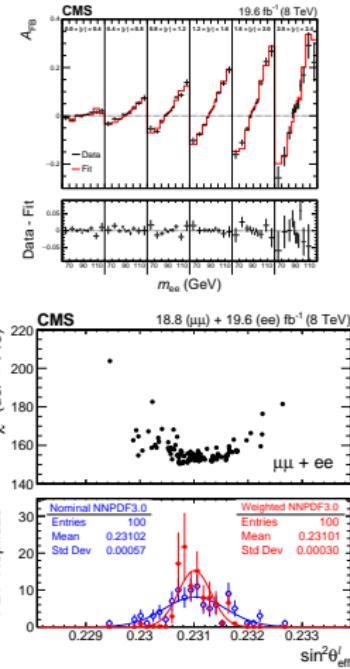
# CMS Result (arxiv: 1806.00863)



- Measurement made on 8 TeV data
- $18.8 \text{ fb}^{-1}$  in the dimuon channel and  $19.6 \text{ fb}^{-1}$  in the dielectron channel
- Uses weighted  $A_{fb}$  and constrains PDFs using the high mass region

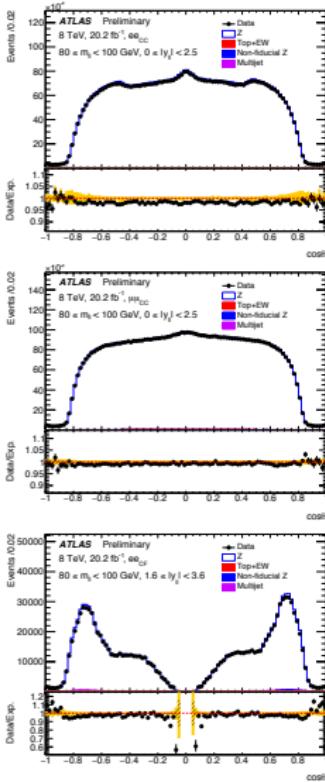
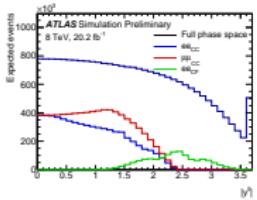
$$\sin^2(\theta_{\text{eff}}^{\text{lep}}) = 0.23101 \pm 0.00053$$

- The error breaks down as  $\pm 0.00036$  (stat)  $\pm 0.00018$  (syst)  $\pm 0.00016$  (theo)  $\pm 0.00031$  (parton distributions in proton)



# ATLAS Result (ATLAS-CONF-2018-037)

- Measurement made on 8TeV data with  $20.2\text{fb}^{-1}$
- 6 million electron pairs, 7.5 million muon pairs
- Using events with a forward electron extends the rapidity coverage to 3.6
- 1.5 million electron pairs with a forward electron (reconstructed from calorimeter, no tracker)

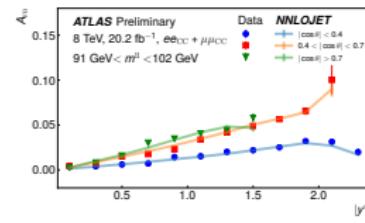
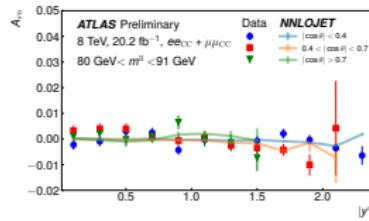
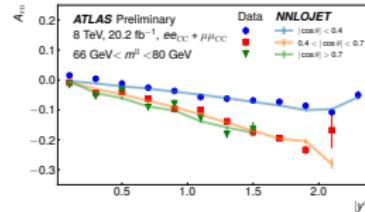


# ATLAS Result (ATLAS-CONF-2018-037)

- Extracts weak mixing angle from  $A_4(m, y)$  instead of  $A_{FB}$

$$\sin^2(\theta_{\text{eff}}^{\text{lep}}) = 0.23101 \pm 0.00036$$

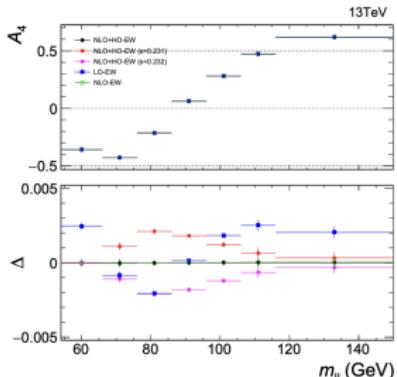
- The error breaks down as  $\pm 0.00021$  (stat)  $\pm 0.00024$  (PDF)  $\pm 0.00016$  (syst.)



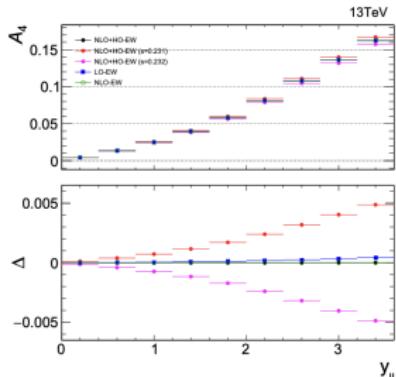
# LHC EW working group activities

- Tuned comparison/benchmarking of NLO and higher order weak and QED corrections, including FSR, ISR and IFI
- Main focus on  $\frac{d\sigma}{dM(\ell\ell)}$  and  $A_{FB}$
- Studying various electroweak input schemes, in particular new  $\sin(\theta_W)$  EW input scheme, which is needed for this measurement
- Preparatory studies in view of Run2 and future combinations

$A_4(m_{\ell\ell})$  for  $y_{\ell\ell} < 3.6$



$A_4(y_{\ell\ell})$  for  $86 < m_{\ell\ell} < 96$



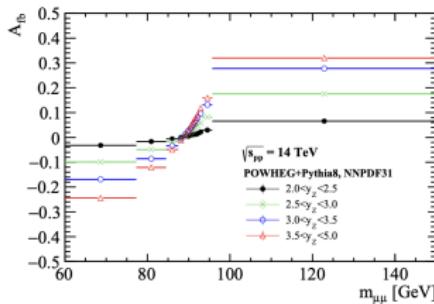
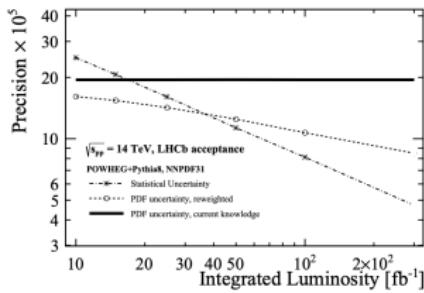


# Future measurements

- CMS Hi-lumi extended acceptance projections  
(CMS-PAS-FTR-17-001)
- ATLAS projections (ATL-PHYS-PUB-2018-037)
- LHCb projections (LHCb-PUB-2018-013)

# LHCb in HL-LHC

- The statistical sensitivity can be expected to improve by up to a factor of  $\sqrt{2}$
- Increased statistics will also allow for the analysis to be done as a function of rapidity
- Expect uncertainties to be competitive with LEP+SLD at  $L > 100 \text{ fb}^{-1}$

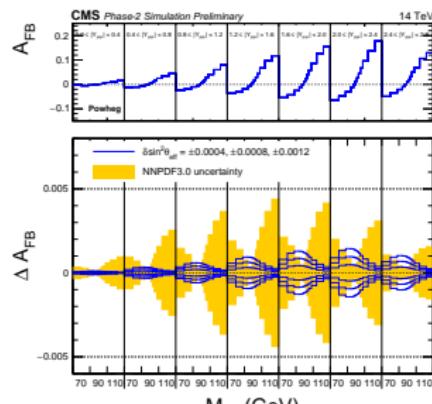
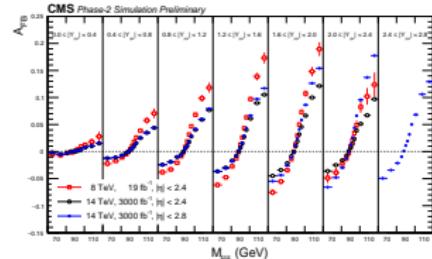
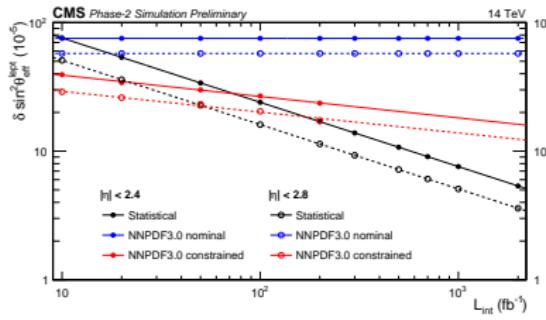


LHCb-PUB-2018-013

# CMS in HL-LHC



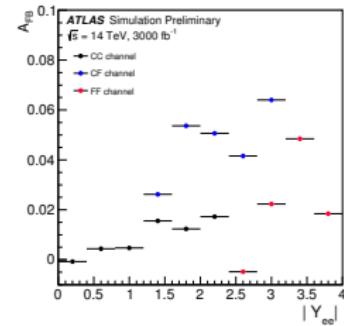
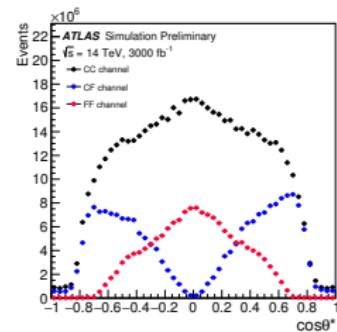
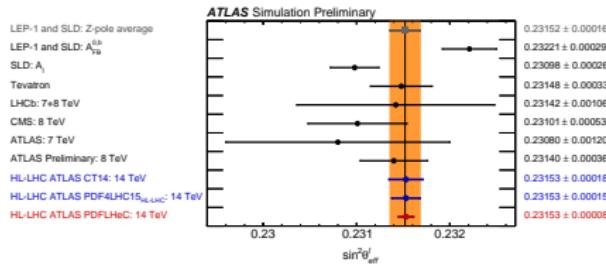
- Extension of tracker will increase acceptance to Z rapidities up to 2.8
- Studies in the muon channel predict to have uncertainties on PDFs competitive with LEP+SLD at  $L > 300 \text{fb}^{-1}$



CMS-PAS-FTR-17-001

# ATLAS in HL-LHC

- Extension of inner tracker from  $|\eta| \leq 2.4$  to  $|\eta| \leq 4.0$
- Projections for  $L > 300 fb^{-1}$  for different PDF scenarios



ATL-PHYS-PUB-2018-037



# Conclusions

- Important probe to test the SM in the electroweak sector and to search indirectly for new physics
- Run2 uncertainties expected to be competitive with LEP/SLD
- The LHC (ATLAS, CMS, LHCb) has promising plans for future measurements, and for combinations of these measurements

University of Rochester DOE Grant Number

Research supported by the U.S. Department of Energy under grant number DE-SC0008475.