## The QCD Equation of State

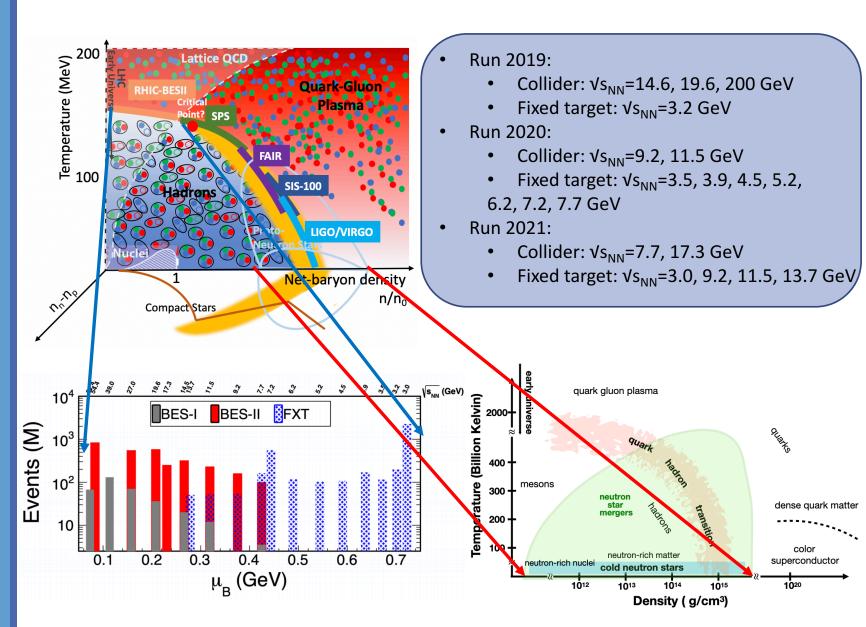
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## Motivating science goals

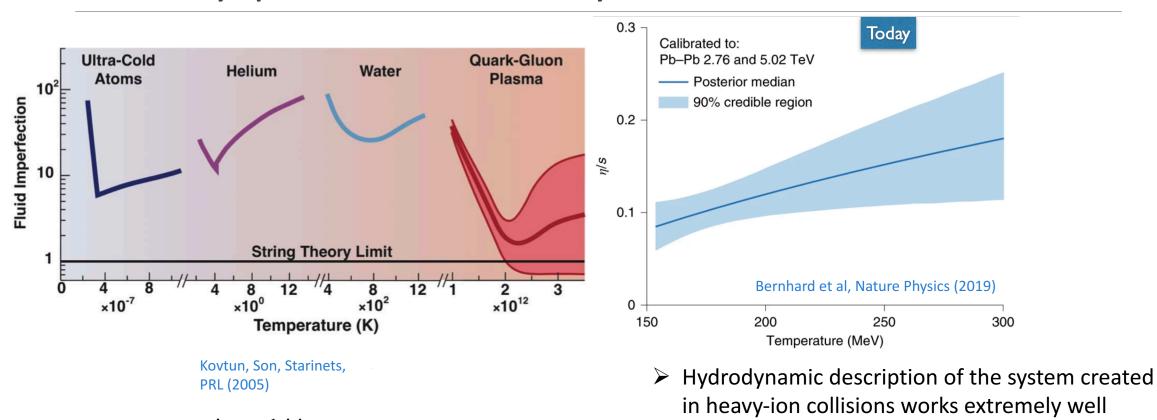
- Is there a critical point in the QCD phase diagram?
- What are the degrees of freedom in the vicinity of the phase transition?
- Where is the transition line at high density?
- What are the phases of QCD at high density?
- Are we creating a thermal medium in experiments?



## Comparison of the facilities

					Compilation by D. Cebra	
	Facilty	<b>RHIC BESII</b>	SPS	NICA	SIS-100	J-PARC HI
CP=Critical Point	Exp.:	<b>STAR</b> +FXT	NA61	MPD + BM@N	SIS-300 <b>CBM</b>	JHITS
OD= Onset of Deconfinement	Start:	<b>2019-2021</b>	2009	+ Bivi@iv 2023	2022	2025
	Energy:	7.7–19.6	4.9-17.3	2.7 - 11	2.7-8.2	2.0-6.2
DHM=Dense Hadronic Matter	√s <sub>NN</sub> (GeV) <b>Rate:</b> At 8 GeV	2.5-7.7 <b>100 HZ</b> 2000 Hz	100 HZ	2.0-3.5 < <b>10 kHz</b>	<10 MHZ	100 MHZ
	Physics:	CP&OD	CP&OD	OD&DHM	OD&DHM	OD&DHM
		Collider Fixed target	Fixed target Lighter ion collisions	Collider Fixed target	Fixed target	Fixed target





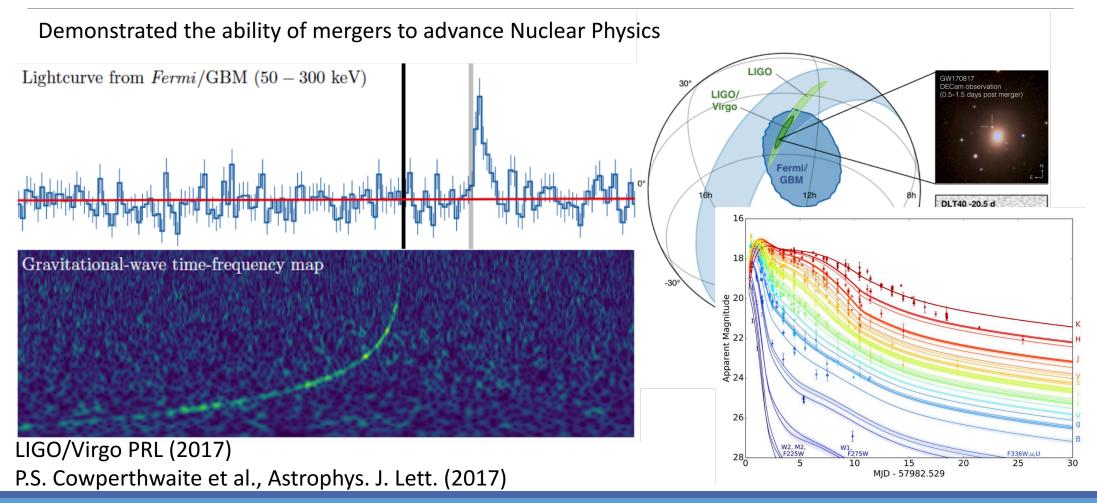
### Nearly perfect fluidity

 $\eta/s = 1/4\pi$ 

It needs an equation of state as input



## GW170817





## Simulating strongly interacting matter

Analytic solutions of QCD are not possible in the non-perturbative regime

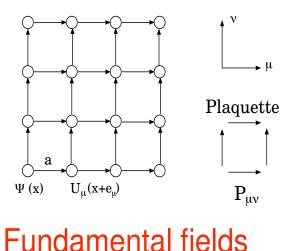
♦ Numerical approach to solve QCD: discretization of 4D space-time

 $\diamond$ Uncertainties:

≻Statistical: finite sample

Systematic: finite box size, unphysical quark masses

Results from different groups, adopting different discretizations, must converge to consistent results







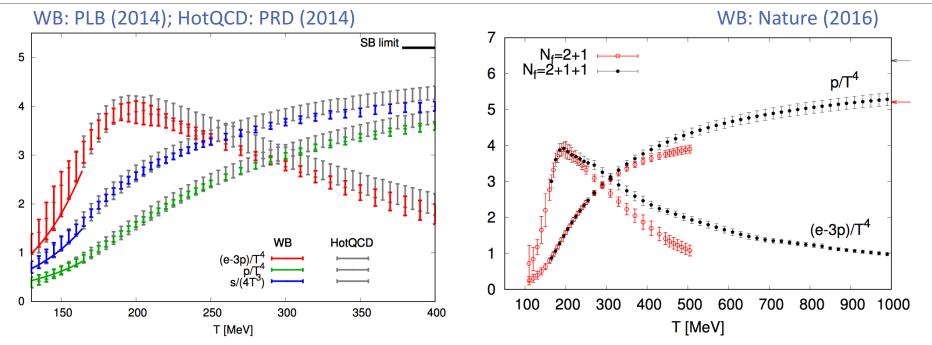
# QCD Equation of State at finite density

TAYLOR EXPANSION

NEW EXPANSION SCHEME



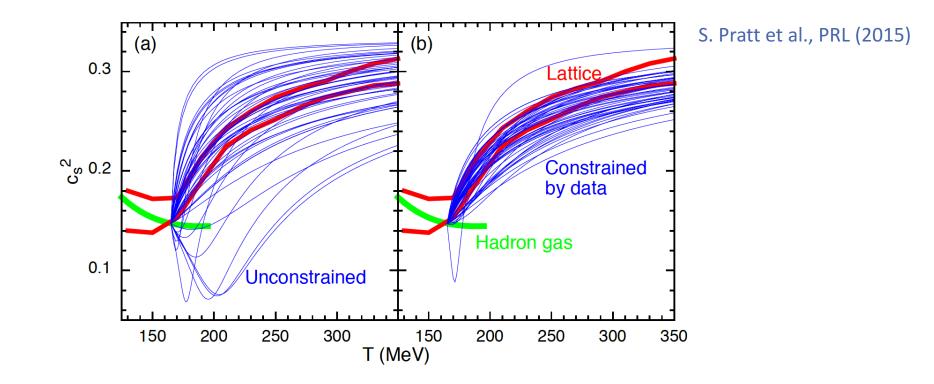
## QCD EoS at $\mu_B=0$



- EoS for N<sub>f</sub>=2+1 known in the continuum limit since 2013
- Good agreement with the HRG model at low temperature
- Charm quark relevant degree of freedom already at T~250 MeV



## Constraints on the EoS from the experiments



- Comparison of data from RHIC and LHC to theoretical models through Bayesian analysis
- The posterior distribution of EoS is consistent with the lattice QCD one



## Fermionic sign problem

The QCD path integral is computed by Monte Carlo algorithms which sample field configurations with a weight proportional to the exponential of the action

$$Z(\mu_B, T) = \operatorname{Tr}\left(e^{-\frac{H_{\mathrm{QCD}}-\mu_B N_B}{T}}\right) = \int \mathcal{D}U e^{-S_G[U]} \det M[U, \mu_B]$$

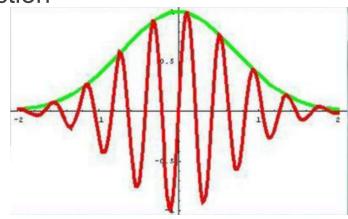
>detM[ $\mu_B$ ] complex  $\rightarrow$  Monte Carlo simulations are not feasible

- $\geq$  We can rely on a few approximate methods, viable for small  $\mu$ B/T:
  - >Taylor expansion of physical quantities around  $\mu$ B=0

Bielefeld-Swansea collaboration 2002; R. Gavai, S. Gupta 2003

Simulations at imaginary chemical potentials

Alford, Kapustin, Wilczek, 1999; de Forcrand, Philipsen, 2002; D'Elia, Lombardo 2003





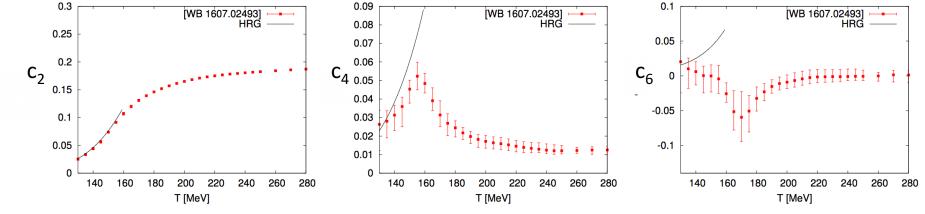
• Taylor expansion of the pressure:

$$\frac{p(T,\mu_B)}{T^4} = \frac{p(T,0)}{T^4} + \sum_{n=1}^{\infty} \frac{1}{(2n)!} \frac{\left| \frac{d^{2n}(p/T^4)}{d(\frac{\mu_B}{T})^{2n}} \right|_{\mu_B=0}}{\left| \frac{d^{2n}(p/T^4)}{d(\frac{\mu_B}{T})^{2n}} \right|_{\mu_B=0}} \left( \frac{\mu_B}{T} \right)^{2n} = \sum_{n=0}^{\infty} c_{2n}(T) \left( \frac{\mu_B}{T} \right)^{2n}$$

#### Simulations at imaginary $\mu_B$ :

Continuum, O(10<sup>4</sup>) configurations, errors include systematics

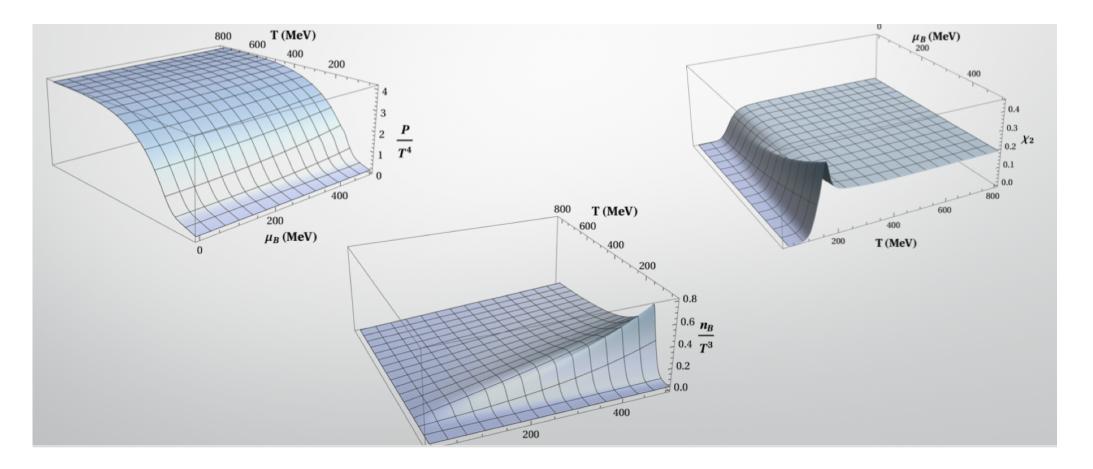
WB: NPA (2017)



See also: HotQCD, PRD (2017), PRD (2022)



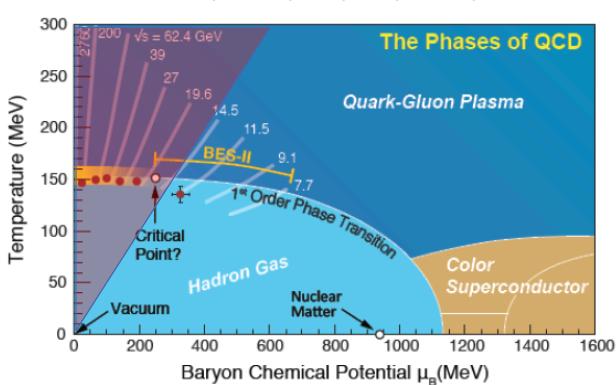
## Taylor expansion of EoS





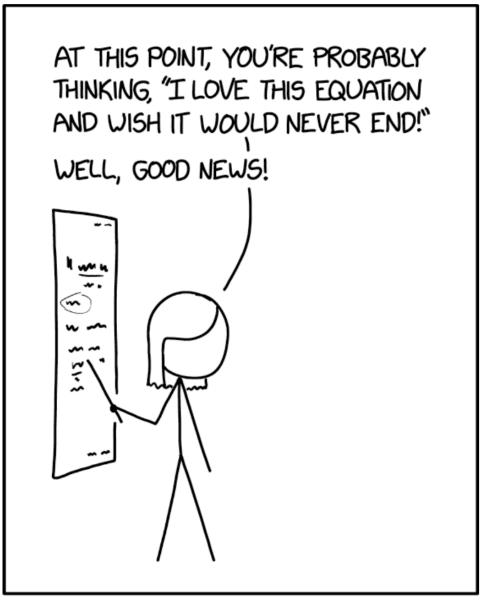
## Range of validity of equation of state

□ We now have the equation of state for  $\mu_B/T \le 2$  or in terms of the RHIC energy scan:



 $\sqrt{s} = 200, \ 62.4, \ 39, \ 27, \ 19.6, \ 14.5 \text{GeV}$ 

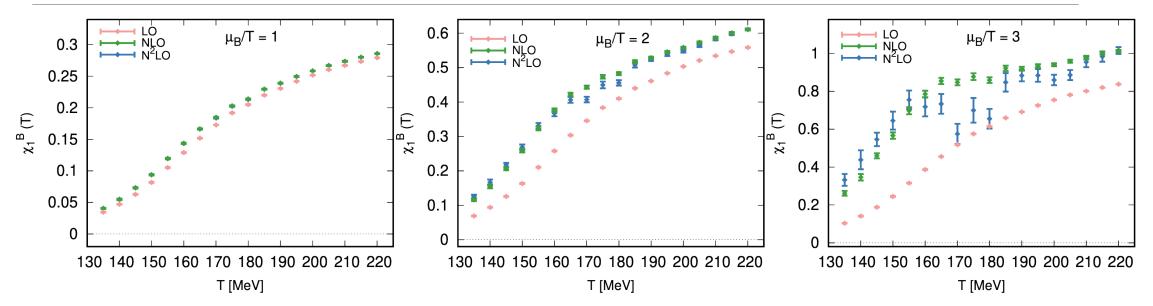




#### TAYLOR SERIES EXPANSION IS THE WORST.







 $\Box$  Poor convergence of Taylor series: need to sum many terms to reach high  $\mu_B$ 

 $\Box$  Oscillatory/non-monotonic behavior in some observables at high  $\mu_B$ 

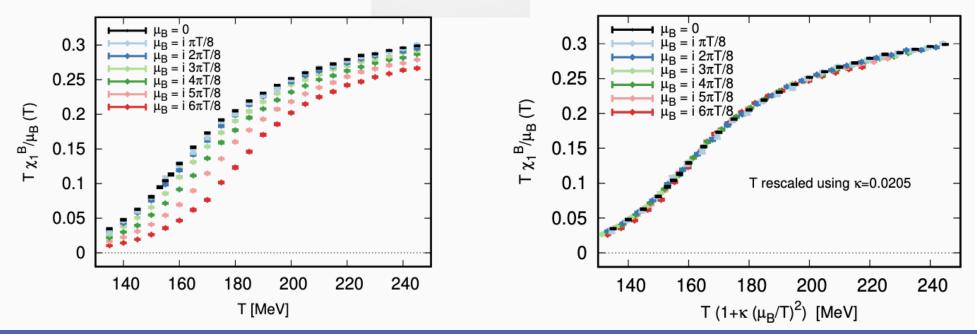
> Unphysical, due to truncation of Taylor series



## An alternative approach

From simulations at imaginary  $\mu_B$  we observe that  $\chi_1^B(T, \hat{\mu}_B)$  at (imaginary)  $\hat{\mu}_B$  appears to be differing from  $\chi_2^B(T, 0)$  mostly by a rescaling of T:

$$\frac{\chi_1^B(T,\,\hat{\mu}_B)}{\hat{\mu}_B} = \chi_2^B(T',0) \ , \quad T' = T\left(1 + \kappa\,\hat{\mu}_B^2\right)$$





## Formulation

- We have observed the  $\hat{\mu}_B$ -dependence seems to amount to a simple T- rescaling
- A simplistic scenario with a single T- independent parameter  $\kappa$  does not provide a systematic treatment which can serve as an alternative expansion scheme
- We allow for more than  $\mathcal{O}(\hat{\mu}^2)$  expansion of T' and let the coefficients be T-dependent:

$$\frac{\chi_1^B(T,\,\hat{\mu}_B)}{\hat{\mu}_B} = \chi_2^B(T',0) \ , \quad T' = T\left(1 + \kappa_2(T)\,\hat{\mu}_B^2 + \kappa_4(T)\,\hat{\mu}_B^4 + \mathcal{O}(\,\hat{\mu}_B^6)\right)$$

• **Important:** we are simply re-organizing the Taylor expansion via an expansion in the shift

$$\Delta T = T - T' = \left(\kappa_2(T)\,\hat{\mu}_B^2 + \kappa_4(T)\,\hat{\mu}_B^4 + \mathcal{O}(\,\hat{\mu}_B^6)\right)$$

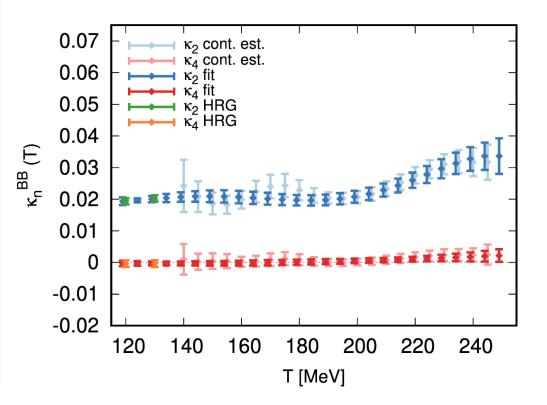
• Comparing the (Taylor) expansion in  $\hat{\mu}_B$  and our expansion in  $\Delta T$  order by order, we can relate  $\chi_n^B(T)$  and  $\kappa_n(T)$ 



## Results for the coefficients

Our initial guess was not far-off:

- Fairly constant  $\kappa_2(T)$  over a large T-range
- Clear separation in magnitude between  $\kappa_2(T)$ and  $\kappa_4(T)$  hints at better convergence
- Agreement with the HRG model results at low temperatures
- Polynomial fits of  $\kappa_2(T)$  and  $\kappa_4(T)$  before use in thermodynamics (good fit qualities)



NOTE: polynomial fits take into account both statistical and systematic correlations.



## Thermodynamics at finite $\mu_B$

Thermodynamic quantities at finite (real)  $\mu_B$  can be reconstruced from the same ansazt:

$$\frac{n_B(T, \,\hat{\mu}_B)}{T^3} = \hat{\mu}_B \chi_2^B(T', 0)$$

with  $T' = T(1 + \kappa_2^{BB}(T)\hat{\mu}_B^2 + \kappa_4^{BB}(T)\hat{\mu}_B^4).$ 

From the baryon density  $n_B$  one finds the pressure:

$$\frac{p(T,\,\hat{\mu}_B)}{T^4} = \frac{p(T,0)}{T^4} + \int_0^{\hat{\mu}_B} \mathrm{d}\hat{\mu}_B' \frac{n_B(T,\,\hat{\mu}_B')}{T^3}$$

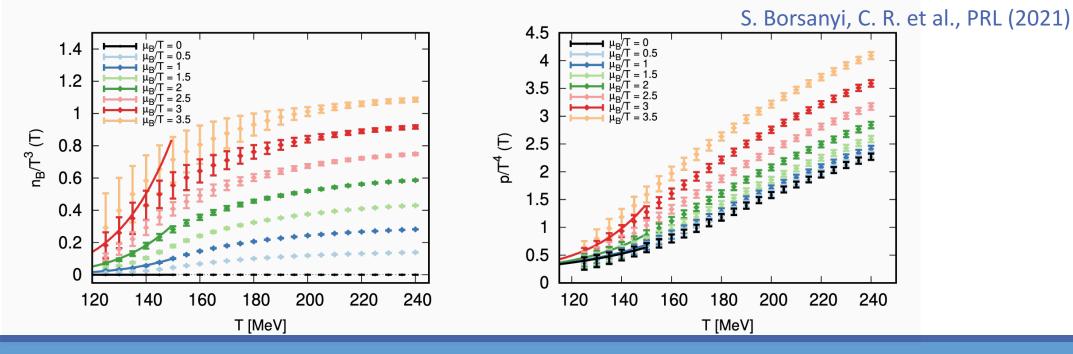
then the entropy, energy density:

$$\frac{s(T,\,\hat{\mu}_B)}{T^4} = 4\frac{p(T,\,\hat{\mu}_B)}{T^4} + T \left.\frac{\partial p(T,\,\hat{\mu}_B)}{\partial T}\right|_{\hat{\mu}_B} - \hat{\mu}_B \frac{n_B(T,\,\hat{\mu}_B)}{T^3}$$
$$\frac{\epsilon(T,\,\hat{\mu}_B)}{T^4} = \frac{s(T,\,\hat{\mu}_B)}{T^3} - \frac{p(T,\,\hat{\mu}_B)}{T^4} + \hat{\mu}_B \frac{n_B(T,\,\hat{\mu}_B)}{T^3}$$



## Thermodynamics at finite $\mu_B$ : results

- We reconstruct thermodynamic quantities up to  $\hat{\mu}_B \simeq 3.5$  with uncertainties well under control
- Agreement with HRG model calculations at small temperatures
- No pathological (non-monotonic) behavior is present

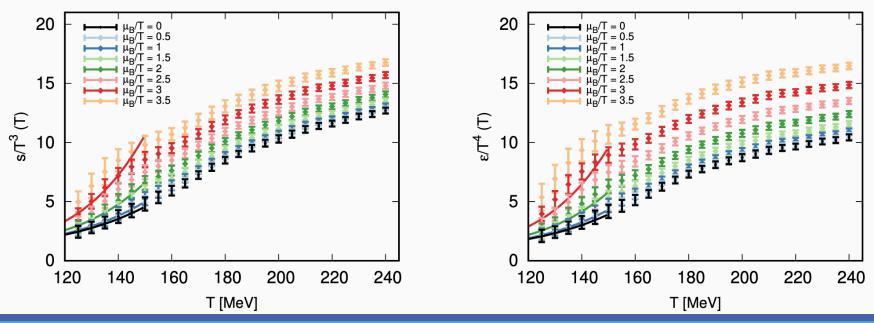




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S. Borsanyi, C. R. et al., PRL (2021)

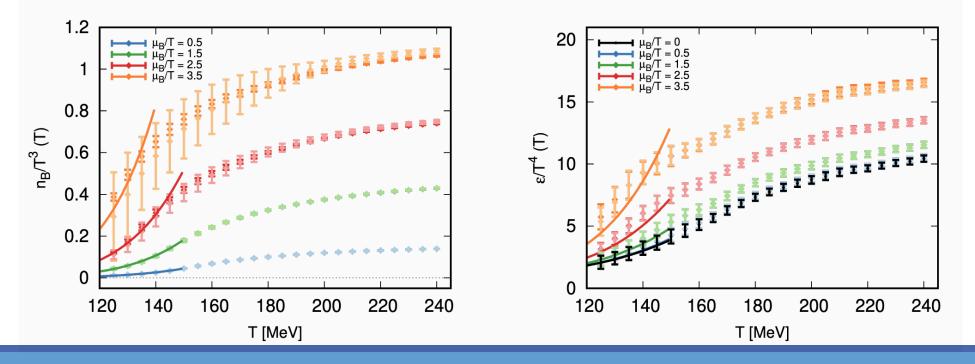




## Convergence check

- We also check the results without the inclusion of  $\kappa_4(T)$  (darker shades)
- Including  $\kappa_4(T)$  only results in added error, but does not "move" the results

 $\longrightarrow$  Good convergence

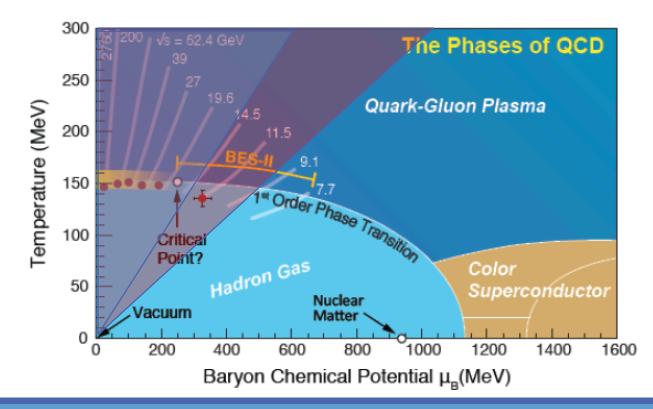




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## New range of validity of equation of state

#### □ We now have the equation of state for $\mu_B/T \le 3.5$





## Other interesting results

#### Recent development in reweighting schemes

M. Giordano et al., JHEP 05, 088; Borsanyi et al., PRD (2022)

#### >Alternative ways to resum the Taylor series

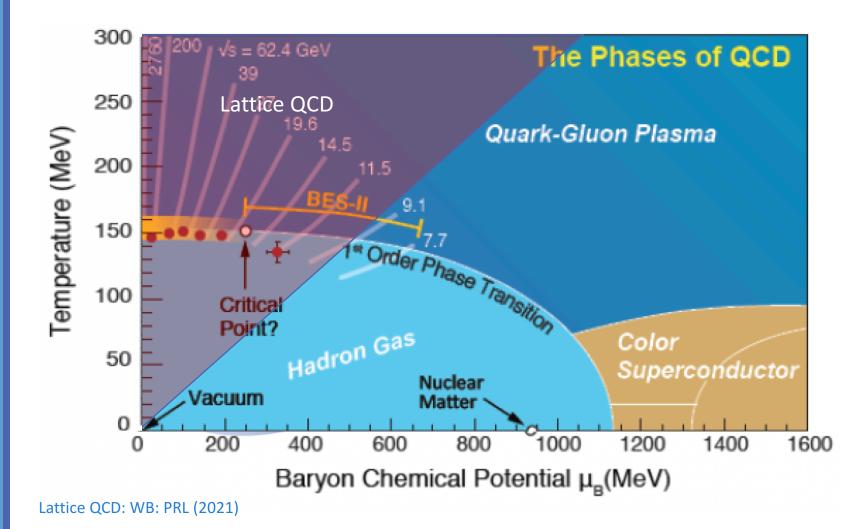
S. Mondal et al., PRL (2022); S. Mukherjee et al., PRD (2022); S. Mitra et al., 2205.08517

#### $\geq$ Recent improvement on Taylor expansion at finite $\mu_{B}$

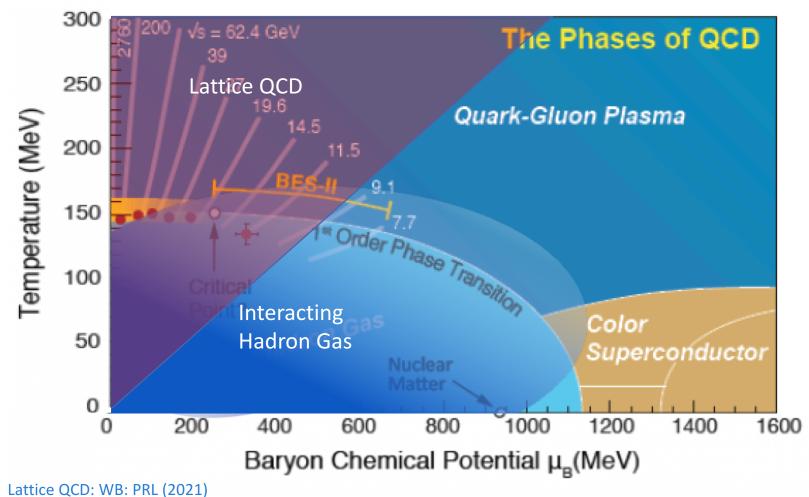
D. Bollweg et al., PRD (2022)



- We need to merge the lattice QCD equation of state with other effective theories
- Careful study of their respective range of validity
- Constrain the parameters to reproduce known limits
- Test different possibilities and validate/exclude them

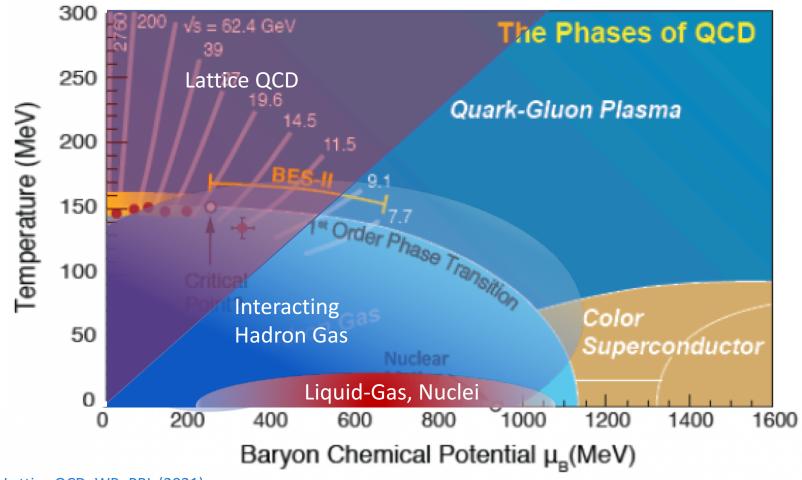


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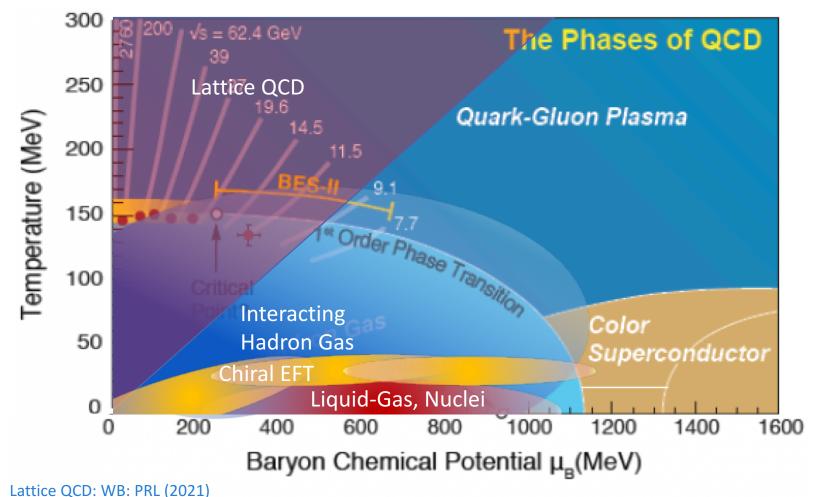
Interacting HRG: V. Vovchenko et al., PRL (2017)

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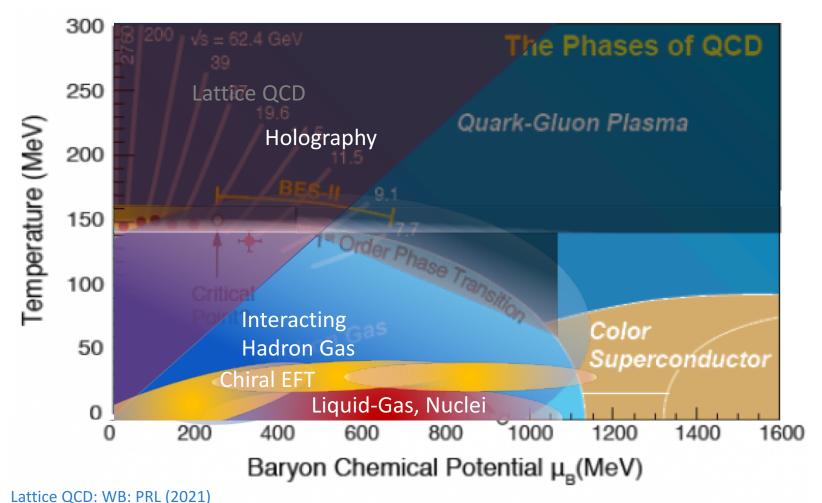
Lattice QCD: WB: PRL (2021) Interacting HRG: V. Vovchenko et al., PRL (2017) Liquid-gas, Nuclei: see e.g. Du et al. PRC (2019)

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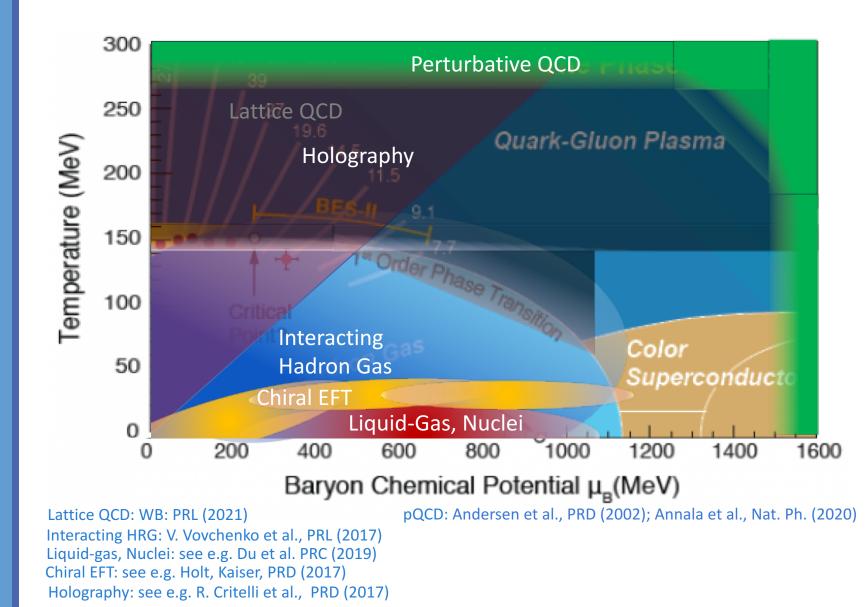
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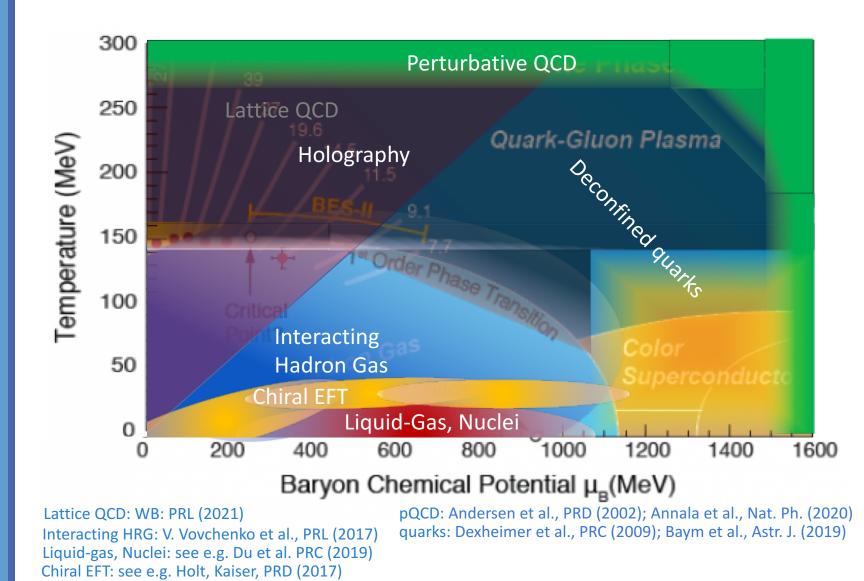


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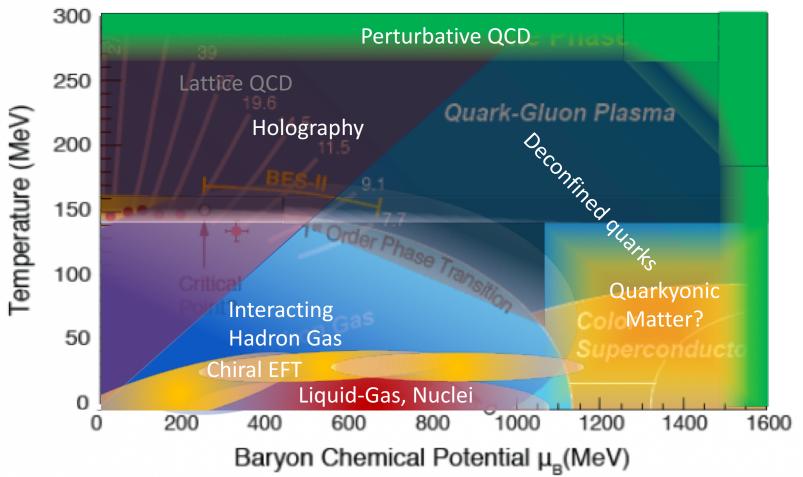
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Holography: see e.g. R. Critelli et al., PRD (2017)

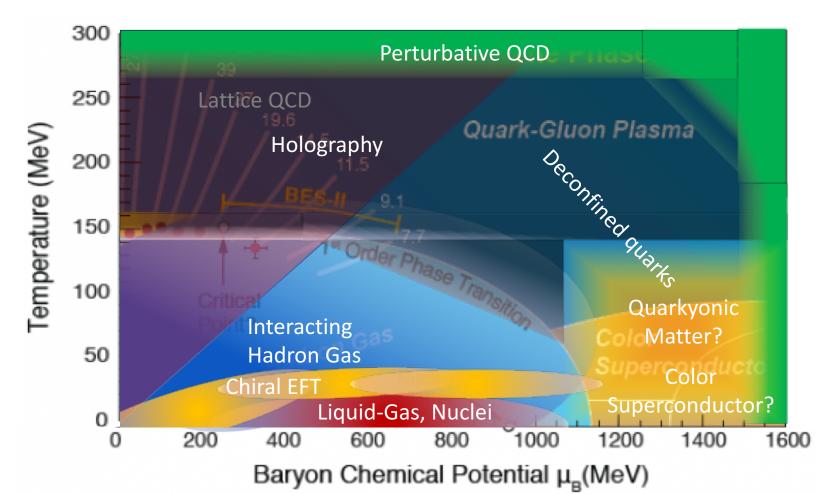
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#### Lattice QCD: WB: PRL (2021)

Interacting HRG: V. Vovchenko et al., PRL (2017) Liquid-gas, Nuclei: see e.g. Du et al. PRC (2019) Chiral EFT: see e.g. Holt, Kaiser, PRD (2017) Holography: see e.g. R. Critelli et al., PRD (2017) pQCD: Andersen et al., PRD (2002); Annala et al., Nat. Ph. (2020) quarks: Dexheimer et al., PRC (2009); Baym et al., Astr. J. (2019) quarkyonic: McLerran, Pisarski NPA (2007)

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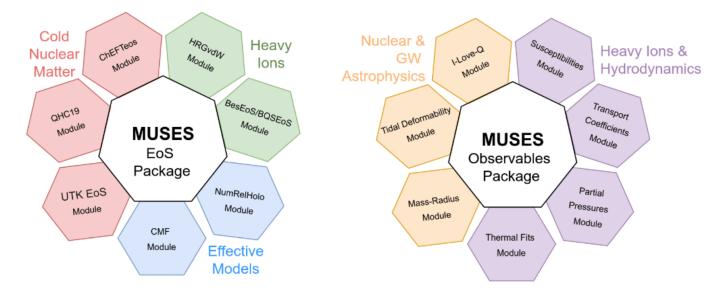
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## $M_{odular} U_{nified} S_{olver of the} E_{quation of} S_{tate} \ collaboration$

Funded by NSF through CSSI program

- Developers and Users are working together to create a sustainable software to generate equations of state in the whole phase space
- Modular: Different models (``modules") to describe the EoS in different regimes of phase space
- Unified: Modules smoothly integrated to (i) ensure maximal coverage of phase space, and (ii) respects constraints







### A possible approach at large densities

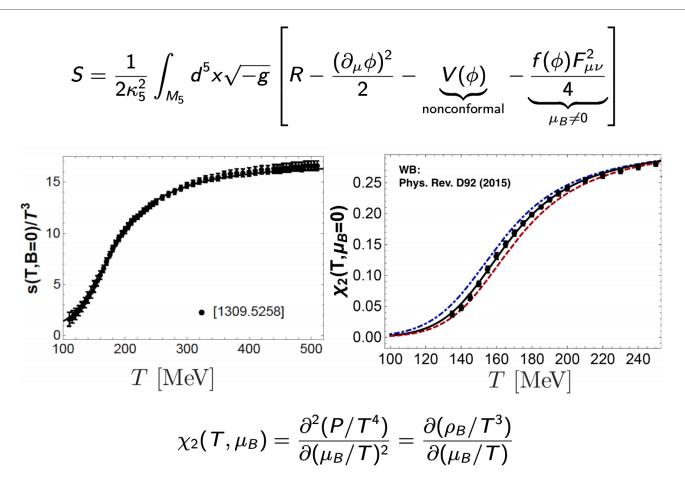
Use AdS/CFT correspondence

Fix the parameters to reproduce everything we know from the lattice

Calculate thermodynamics at finite density



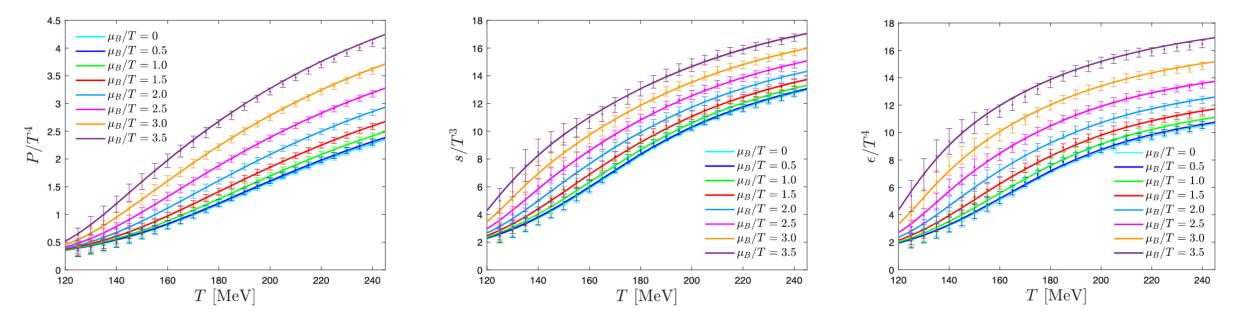
### Gravitational action



O. DeWolfe et al., PRD (2011) R. Rougemont et al., JHEP (2016) R. Critelli et al., PRD (2017)



### Comparison with lattice QCD thermodynamics



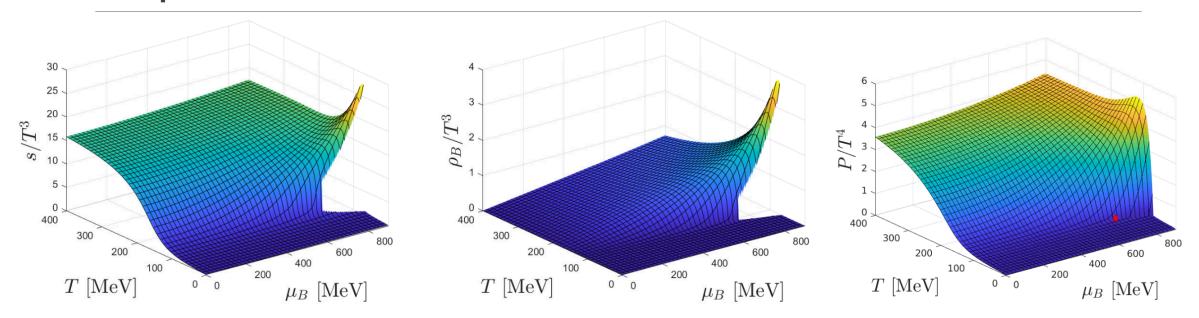
Good agreement for all thermodynamic quantities up to large  $\mu_{\text{B}}$ 

Makes us confident in our extrapolation to larger  $\mu_{\text{B}}$ 

J. Grefa et al., PRD (2021) Lattice data: S. Borsanyi et al., PRL (2021)



### **Equation of State**



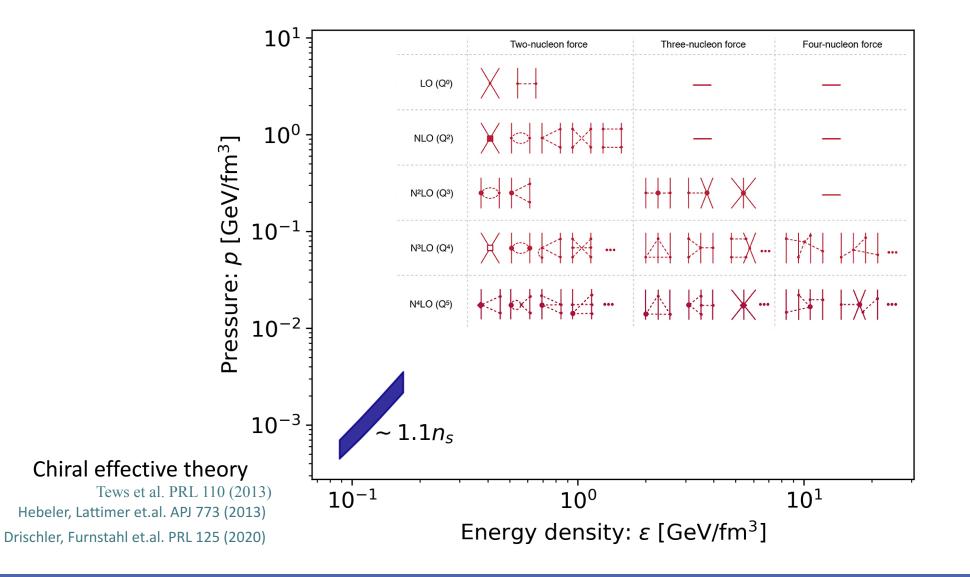
Model has a critical point at  $\mu_B \sim 723$  MeV and T~89 MeV

Equation of state can cover up to  $\mu_{B}$ ~1 GeV

Thermodynamic quantities seem too small at low T



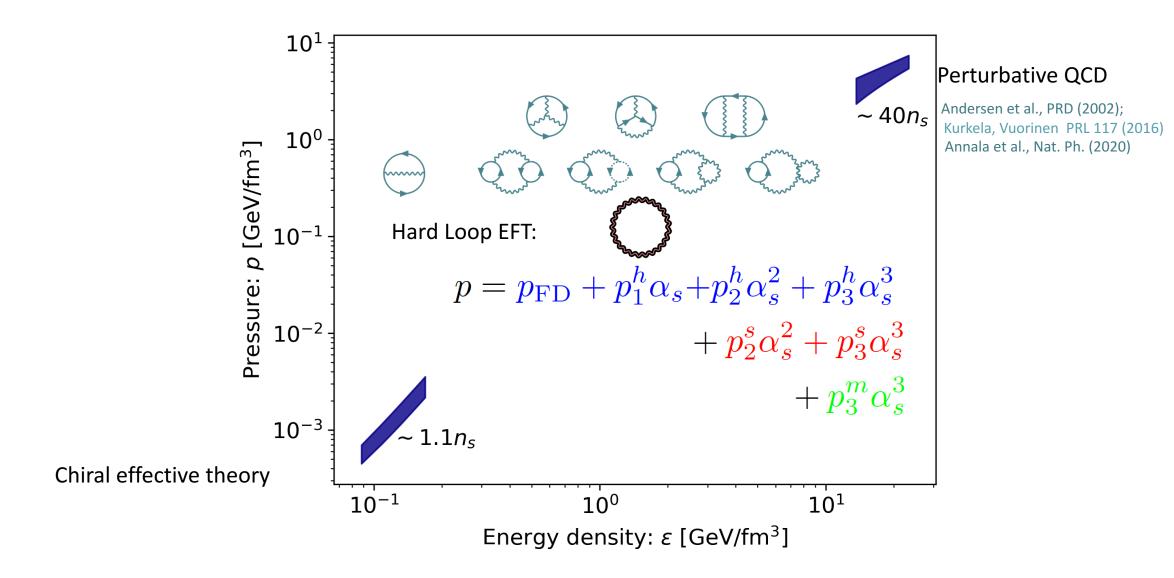
## Neutron stars and mergers



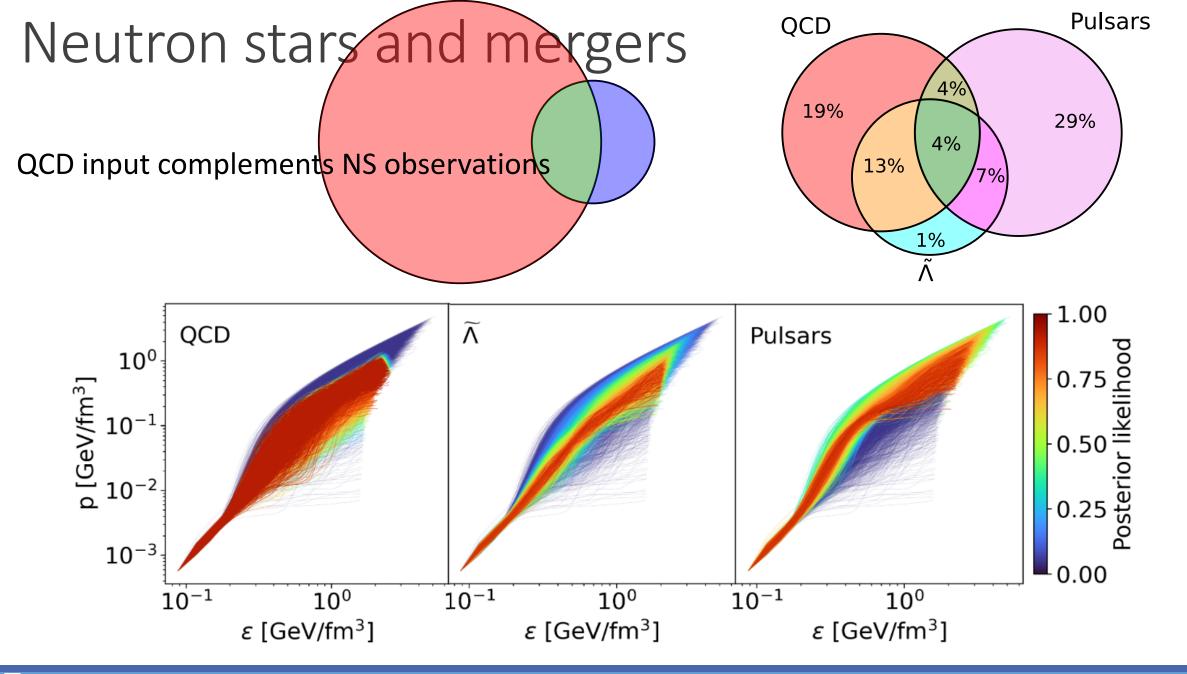


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## Neutron stars and mergers



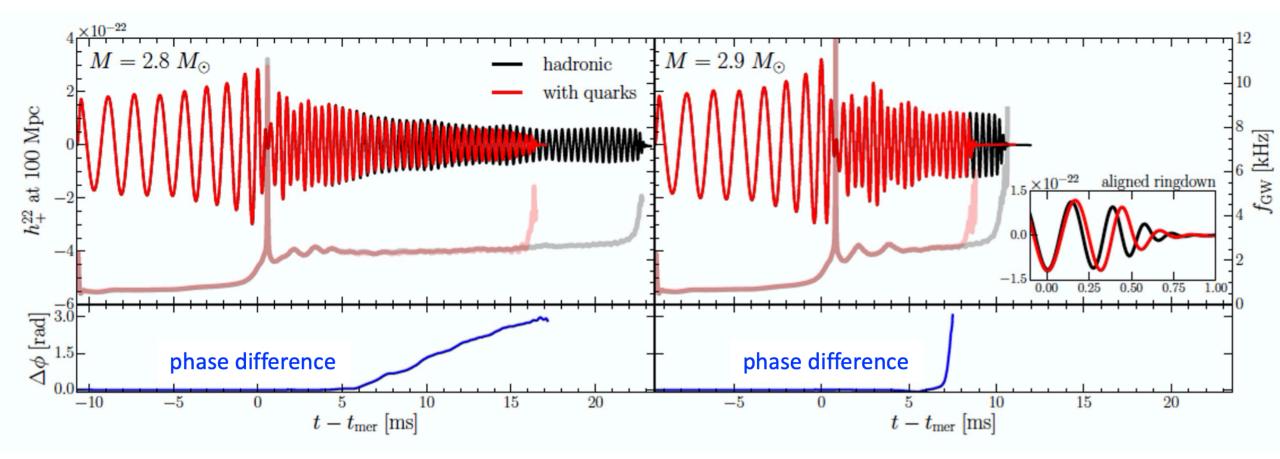






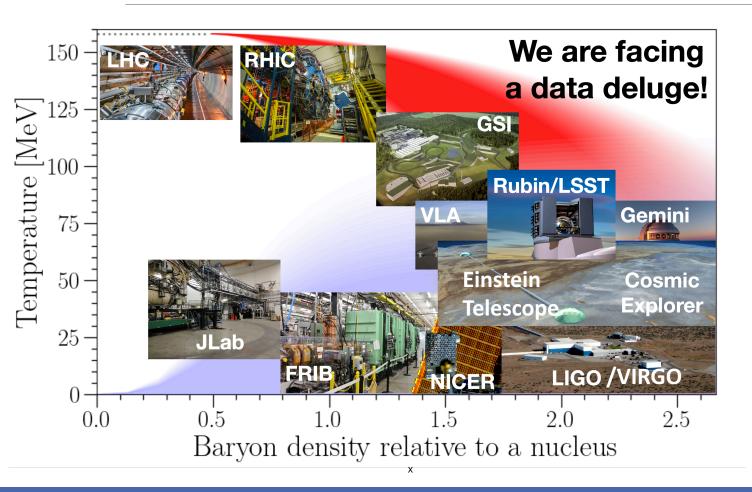
## Neutron stars and mergers

- Post-merger signal sensitive to order of the phase transition
- Next generation observatories will be able to detect it!





## Future directions



- > ALICE will continue operating till at least 2036
- CBM at FAIR (GSI) will hopefully start soon
- New generation of gravitational wave observatories will be able to see the postmerger signal (sensitive to the EoS)
- FRIB & NUSTAR (FAIR) will study nuclear structure
- Theory needs to continue to support these experimental programs



## Conclusions

Need for quantitative results at finite-density to support the experimental programs and reach out to the Neutron Star merger regime

> Current lattice results for thermodynamics available up to  $\mu_B/T \le 3.5$ 

> Extensions to higher densities by means of effective theories



## How can lattice QCD support the experiments?

Equation of state

• Needed for hydrodynamic description of the QGP

QCD phase diagram

- Transition line at finite density
- Constraints on the location of the critical point

Fluctuations of conserved charges

- Can be simulated on the lattice and measured in experiments
- Can give information on the evolution of heavy-ion collisions
- Can give information on the critical point





## Formulation

S. Borsanyi, C. R. et al., PRL (2021)

- We have observed the  $\hat{\mu}_B$ -dependence seems to amount to a simple T- rescaling
- A simplistic scenario with a single T- independent parameter  $\kappa$  does not provide a systematic treatment which can serve as an alternative expansion scheme
- We allow for more than  $\mathcal{O}(\hat{\mu}^2)$  expansion of T' and let the coefficients be T-dependent:

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• **Important:** we are simply re-organizing the Taylor expansion via an expansion in the shift

$$\Delta T = T - T' = \left(\kappa_2(T)\,\hat{\mu}_B^2 + \kappa_4(T)\,\hat{\mu}_B^4 + \mathcal{O}(\,\hat{\mu}_B^6)\right)$$

• Comparing the (Taylor) expansion in  $\hat{\mu}_B$  and our expansion in  $\Delta T$  order by order, we can relate  $\chi_n^B(T)$  and  $\kappa_n(T)$ 

## QCD phase diagram

TRANSITION TEMPERATURE

TRANSITION LINE

TRANSITION WIDTH



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## QCD matter under extreme conditions

To address these questions, we need fundamental theory and experiment

#### **Theory: Quantum Chromodynamics**

QCD is the fundamental theory of strong interactions
It describes interactions among guarks and gluons

$$L_{QCD} = \sum_{i=1}^{n_f} \overline{\psi}_i \gamma_\mu \left( i\partial^\mu - gA_a^\mu \frac{\lambda_a}{2} \right) \psi_i - m_i \overline{\psi}_i \psi_i - \frac{1}{4} \sum_a F_a^{\mu\nu} F_a^{\mu\nu}$$

$$F_a^{\mu\nu} = \partial^{\mu} A_a^{\nu} - \partial^{\nu} A_a^{\mu} + i f_{abc} A_b^{\mu} A_c^{\mu}$$

#### Experiment: heavy-ion collisions



▶ Quark-Gluon Plasma (QGP) discovery at RHIC and LHC:

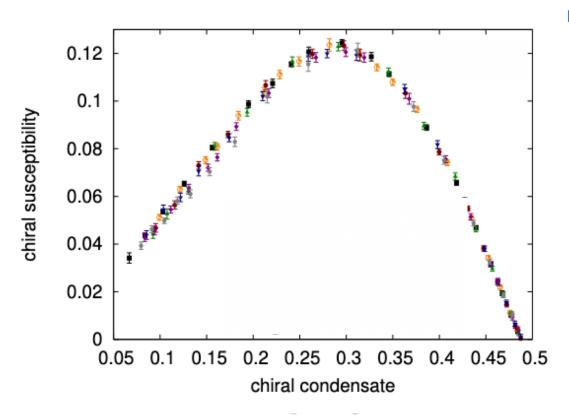
- ▶ SURPRISE!!! QGP is a PERFECT FLUID
- Changes our idea of QGP
- (no weak coupling)
- Microscopic origin still unknown





## Phase Diagram from Lattice QCD

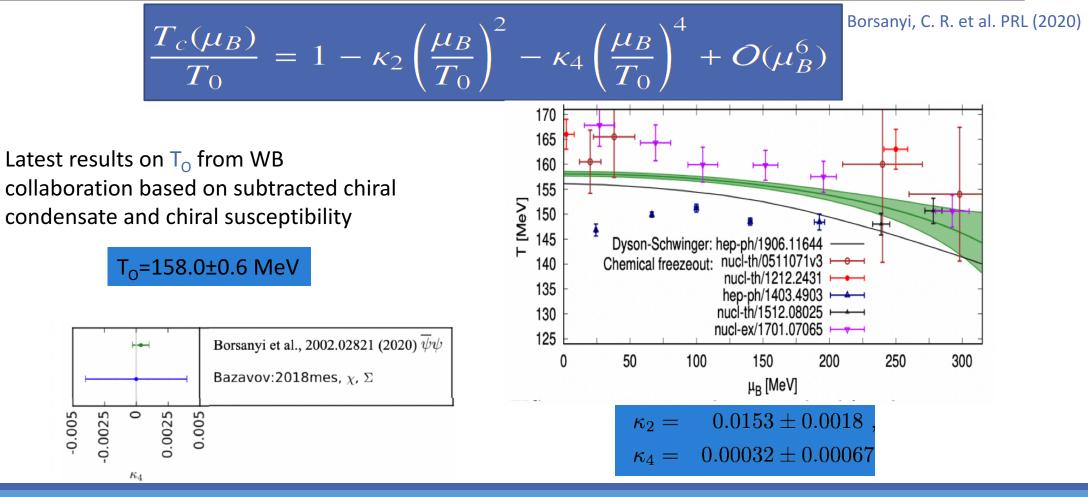
The transition at  $\mu_B$ =0 is a smooth crossover



Aoki et al., Nature (2006) Borsanyi et al., JHEP (2010) Bazavov et al., PRD (2012)



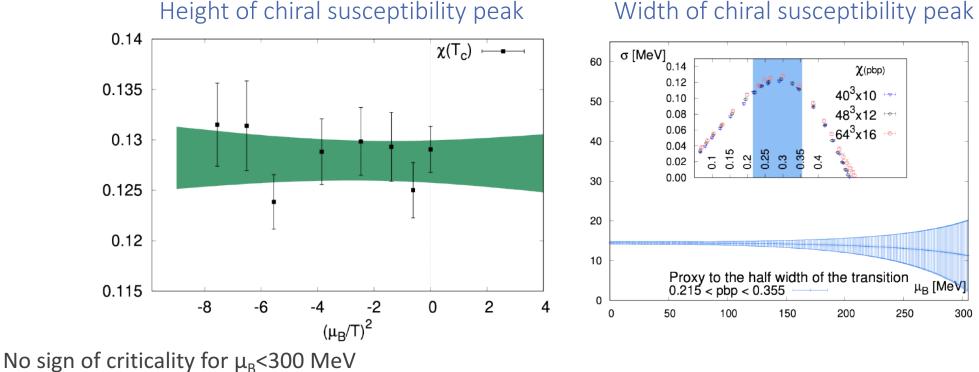
## QCD transition temperature and curvature





## Limit on the location of the critical point

For a genuine phase transition, the height of the peak of the chiral susceptibility diverges and the width shrinks to zero



#### Width of chiral susceptibility peak

# Fluctuations of conserved charges

COMPARISON TO EXPERIMENT

CHEMICAL FREEZE-OUT PARAMETERS



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## Fluctuations of conserved charges

Definition:

$$\chi^{BSQ}_{lmn} = \frac{\partial^{\,l+m+n} p/T^4}{\partial (\mu_B/T)^l \partial (\mu_S/T)^m \partial (\mu_Q/T)^n}$$

Relationship between chemical potentials:

$$\mu_{u} = \frac{1}{3}\mu_{B} + \frac{2}{3}\mu_{Q};$$
  

$$\mu_{d} = \frac{1}{3}\mu_{B} - \frac{1}{3}\mu_{Q};$$
  

$$\mu_{s} = \frac{1}{3}\mu_{B} - \frac{1}{3}\mu_{Q} - \mu_{S}$$

They can be calculated on the lattice and compared to experiment



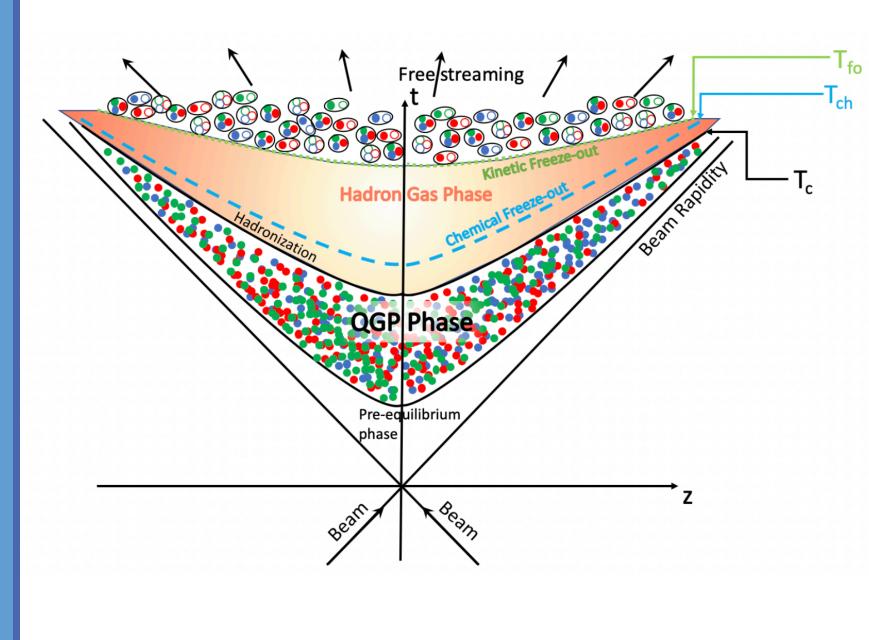
### Evolution of a heavy-ion collision

#### •Chemical freeze-out:

inelastic reactions cease: the chemical composition of the system is fixed (particle yields and fluctuations)

• Kinetic freeze-out: elastic reactions cease: spectra and correlations are frozen (free streaming of hadrons)

• Hadrons reach the detector





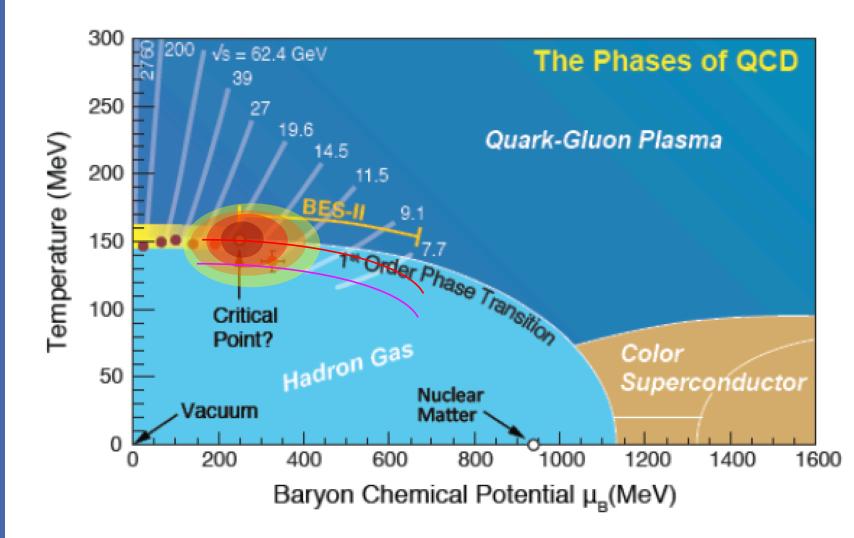
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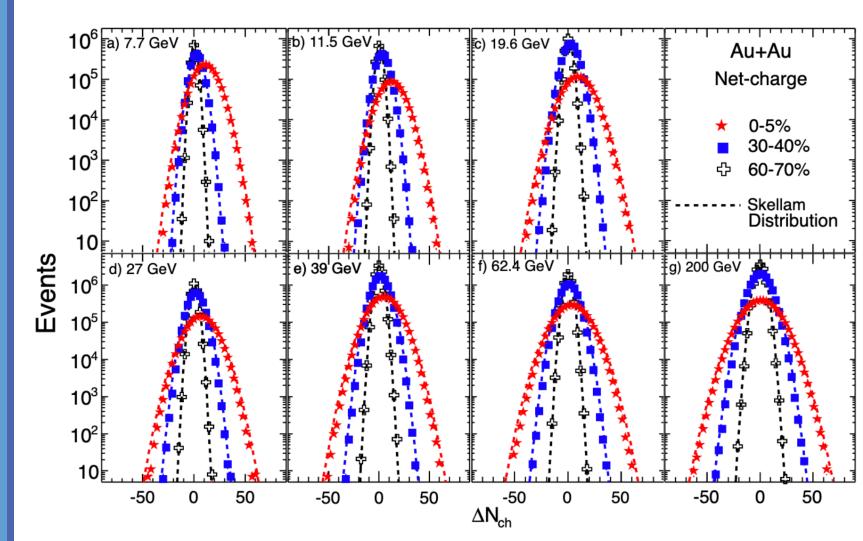




## Connection to experiment

- Consider the number of electrically charged particles N<sub>Q</sub>
- Its average value over the whole ensemble of events is <N<sub>Q</sub>>

 In experiments it is possible to measure its event-by-event distribution



STAR Collab., PRL (2014)



## Connection to experiment

Fluctuations of conserved charges are the cumulants of their event-by-event distribution

mean :  $M = \chi_1$  variance :  $\sigma^2 = \chi_2$ 

skewness :  $S = \chi_3 / \chi_2^{3/2}$  kurtosis :  $\kappa = \chi_4 / \chi_2^2$ 

 $S\sigma = \chi_3/\chi_2$   $\kappa\sigma^2 = \chi_4/\chi_2$ 

 $M/\sigma^2 = \chi_1/\chi_2 \qquad \qquad S\sigma^3/M = \chi_3/\chi_1$ 

F. Karsch: Centr. Eur. J. Phys. (2012)

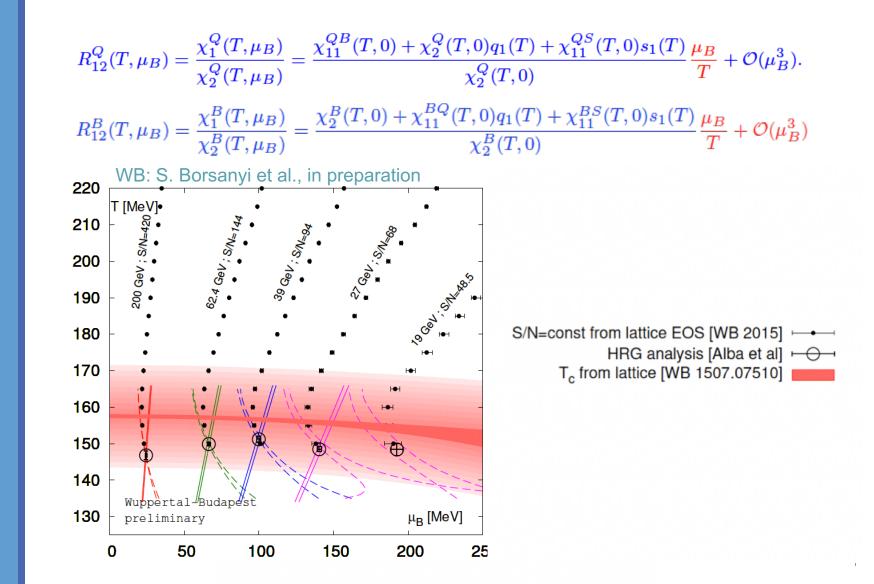
The chemical potentials are not independent: fixed to match the experimental conditions:

$$< n_{\rm S} >= 0$$
  $< n_{\rm Q} >= 0.4 < n_{\rm B} >$ 



## Freeze-out line from first principles

Use T- and  $\mu_B$ -dependence of  $R_{12}{}^Q$  and  $R_{12}{}^B$  for a combined fit:





## Conclusions

Need for quantitative results at finite-density to support the experimental programs

- Equation of state
- Phase transition line
- Fluctuations of conserved charges

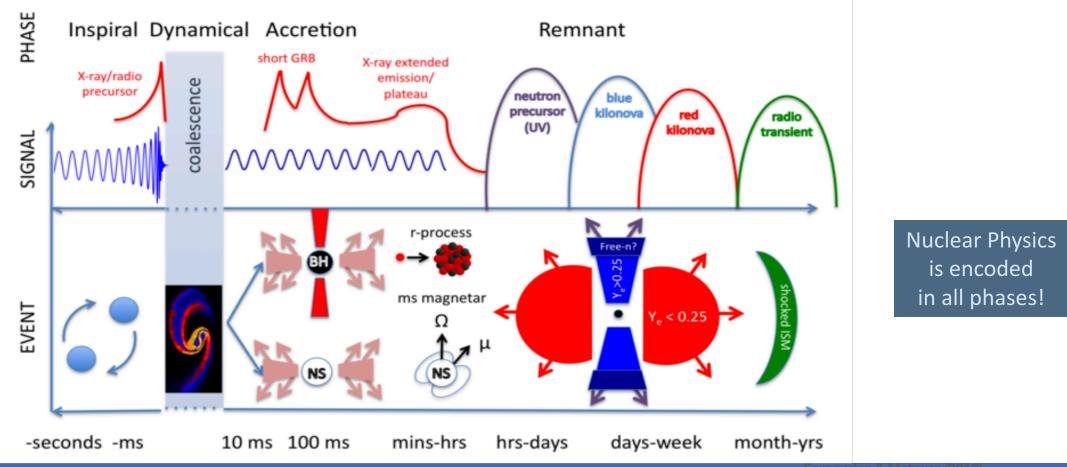
>Current lattice results for thermodynamics up to  $\mu_B/T \le 3.5$ 

> Extensions to higher densities by means of lattice-based models

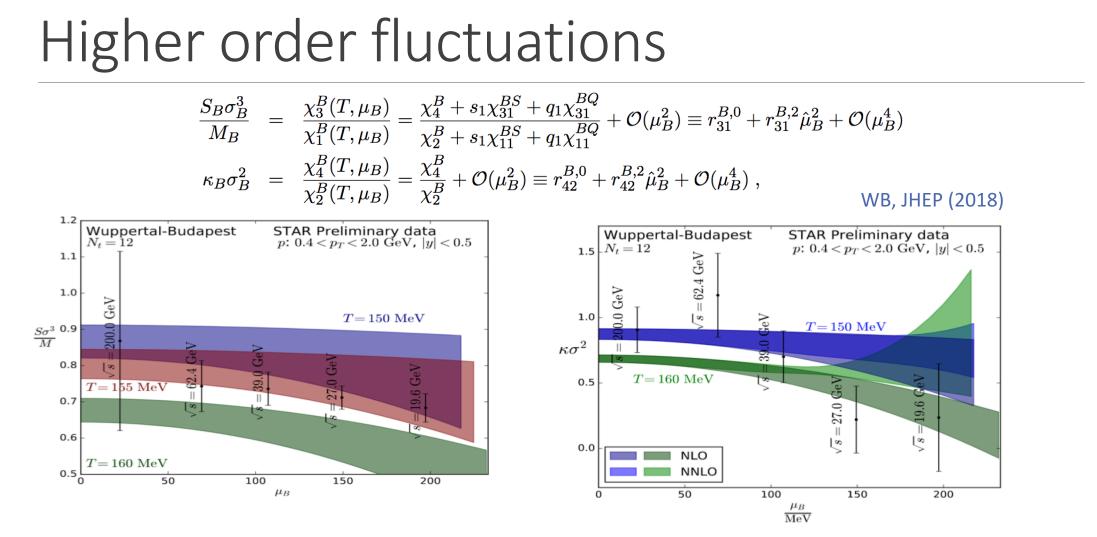
> No indication of Critical Point from lattice QCD in the explored  $\mu_B$  range



## Anatomy of a multi-messenger merger







See also HotQCD, PRD (2017)



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## "Baryometer and Thermometer"

Let us look at the Taylor expansion of  $\mathbb{R}^{B_{31}}$ 

$$R_{31}^B(T,\mu_B) = \frac{\chi_3^B(T,\mu_B)}{\chi_1^B(T,\mu_B)} = \frac{\chi_4^B(T,0) + \chi_{31}^{BQ}(T,0)q_1(T) + \chi_{31}^{BS}(T,0)s_1(T)}{\chi_2^B(T,0) + \chi_{11}^{BQ}(T,0)q_1(T) + \chi_{11}^{BS}(T,0)s_1(T)} + \mathcal{O}(\mu_B^2)$$

- To order  $\mu^2_B$  it is independent of  $\mu_B$ : it can be used as a thermometer
- Let us look at the Taylor expansion of  $\mathbb{R}^{B}_{12}$

$$R_{12}^B(T,\mu_B) = \frac{\chi_1^B(T,\mu_B)}{\chi_2^B(T,\mu_B)} = \frac{\chi_2^B(T,0) + \chi_{11}^{BQ}(T,0)q_1(T) + \chi_{11}^{BS}(T,0)s_1(T)}{\chi_2^B(T,0)} \frac{\mu_B}{T} + \mathcal{O}(\mu_B^3)$$

• Once we extract T from  $\mathbb{R}^{B}_{31}$ , we can use  $\mathbb{R}^{B}_{12}$  to extract  $\mu_{B}$ 



## The highest man-made temperature



5.5x10<sup>12</sup> °C: 340.000 times the temperature at the center of the sun!!!



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## The produced energy density is 5 GeV/fm<sup>3</sup>

In one year in America  $\sim 10^{20}$  J of energy are used

 $10^{20} \text{ J x } 1 \text{ eV} / (1.6 \text{ x} 10^{-19} \text{ J}) = 6.6 \text{ x } 10^{38} \text{ eV}$ 

At 5 GeV/fm<sup>3</sup> this would correspond to a volume:

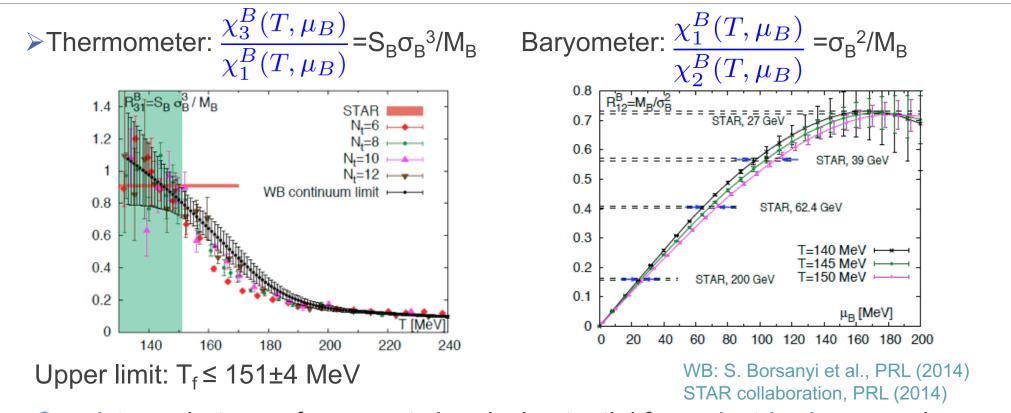
$$6.6 \times 10^{38} eV \div \frac{5 \times 10^9 eV}{fm^3} = 1.3 \times 10^{29} fm^3$$

Or, equivalently, to a box of size:

$$\sqrt[3]{1.3 \times 10^{29} fm^3} = 5 \times 10^9 fm \times \frac{1m}{10^{15} fm} \times \frac{10^6 \mu m}{1m} = 5\mu m$$



## Freeze-out parameters from B fluctuations



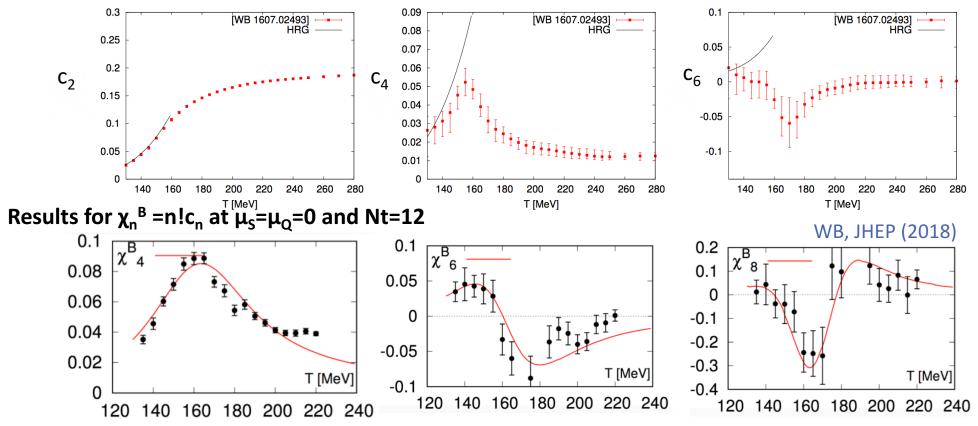
Consistency between freeze-out chemical potential from electric charge and baryon number is found.



## Pressure coefficients

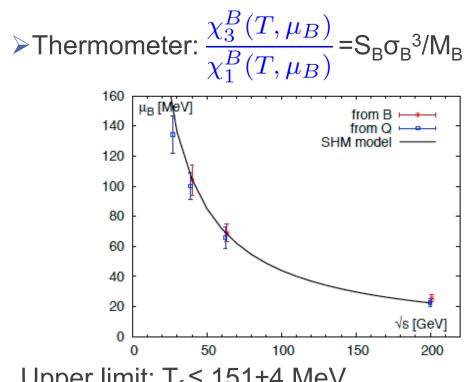
#### Simulations at imaginary $\mu_{\rm B}$ :

Continuum, O(10<sup>4</sup>) configurations, errors include systematics (WB: NPA (2017)) Strangeness neutrality





## Freeze-out parameters from B fluctuations



Baryometer: 
$$\frac{\chi_1^B(T,\mu_B)}{\chi_2^B(T,\mu_B)} = \sigma_B^2/M_B$$

$\sqrt{s}[GeV]$	$\mu_B^f$ [MeV] (from $B$ )	$\mu_B^f$ [MeV] (from $Q$ )
200	$25.8 {\pm} 2.7$	$22.8 \pm 2.6$
62.4	$69.7 \pm 6.4$	$66.6 {\pm} 7.9$
39	$105 \pm 11$	$101 \pm 10$
27	-	$136{\pm}13.8$

WB: S. Borsanyi et al., PRL (2014) STAR collaboration, PRL (2014)

Upper limit: T<sub>f</sub> ≤ 151±4 MeV

Consistency between freeze-out chemical potential from electric charge and baryon number is found.



## A few Lessons learned

➢ Heavy ion collisions:

- > Phase transition at small  $\mu_B$  is a smooth crossover
- >If a critical point exists, it is in the 3D-Ising model universality class
- > Equation of state and phase diagram are known from 1<sup>st</sup> principles at  $\mu_B/T<3.5$
- >Quark-Gluon Plasma is a strongly coupled fluid with very small viscosity/entropy

#### ➢Neutron star mergers:

- GWs travel essentially at the speed of light
- binary neutron star mergers are progenitors of short gamma ray bursts
- > they are prolific sites for the formation of heavy elements
- >constrained neutron-star radii to be between 9.5 and 13 km



## Anatomy of a heavy-ion collision

