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Forecasts on the speed of gravitational waves at high *z*



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Galaxies /Cosmology & Fundamental Physics SWG's / next generation Event Horizon Telescope (ngEHT)

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- 1. Introduction and Motivation
- 2. Theoretical framework
 - 2.1. Gravitational waves in modified gravity
 - 2.2. Methodology and results
- 3. Summary and conclusions





- 1. Introduction and Motivation
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Outline







1. The observation of GWI70817 binary neutron star (BNS) merger event has imposed strong bounds on the speed of gravitational waves (GWs) locally, inferring that the speed of GWs propagation is equal to the speed of light $c_T/c = 1$ ($|c_T/c - 1| \le 10^{-16}$), where c_T and c are the propagation speed of the GWs and electromagnético radiation, respectively.

2. Current GW detectors in operation will not be able to observe BNS merger to long cosmological distance, where possible cosmological corrections on the cosmic expansion history are expected to play an important role, specially for investigating possible deviations from general relativity

3. Future GW detectors designer projects will be able to detect many coalescences of BNS at high z, such as the third generation of the ground GW detector called Einstein Telescope (ET) and the space-based detector deci-hertz interferometer gravitational wave observatory (DECIGO).

4. In this work, we relax the condition $c_T/c = 1$ to investigate modified GW propagation where the speed of GWs propagation is not necessarily equal to the speed of light.







Some theoretical problems with the standard model of cosmology...!

- 1. COSMIC COINCIDENCE PROBLEM: ¿Why the density of matter and dark energy today are of the same order of magnitude?.
- 2. Fine-Tuning PROBLEM: ¿Why is the cosmological constant so small?
- 3. QUANTUM VACUUM ENERGY DENSITY: ¿Why the calculated value of the cosmological constant from quantum field theory is 120 orders of magnitude larger than the observed?



$$G_{\mu\nu} + g_{\mu\nu}\Lambda = \frac{8\pi G}{c^4} T_{\mu\nu}$$

- 1. Alternative models of dark Energy: wCDM ($w \neq -1$), Chevalier-Polarski-Linder (CPL), Interacting Dark Energy (IDE), Generalized Chapliygin Gas (GCG)..etc.
- 2. Modified Gravity: f(R), f(T), Massive Gravity, Tensor, Vector, Scalar (Horndeski).
- 3. Holographic Dark Energy: Tsallis' entropy, Kaniadakis statistics, Fluid/ Gravity Duality.



Observational Constraints on f(T) gravity from varying fundamental constants

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$$\frac{\Delta \alpha}{\alpha}(z) \approx \frac{\left[1 - b \left(\frac{1 - \Omega_{m0}}{2b - 1}\right)\right]}{\left\{1 - b \left(\frac{1 - \Omega_{m0}}{2b - 1}\right) \left[\frac{H^2(z)}{H_0^2}\right]^{(b-1)}\right\}} - 1,$$

$$G_{eff}(z) = \frac{G_N}{1 - b \left(\frac{1 - \Omega_{m0}}{2b - 1}\right) \left[\frac{H^2(z)}{H_0^2}\right]^{(b-1)}},$$

Cosmological variation of the fine structure constant and the universal constant of gravitation



Introduction and Motivation

Important equations of Universe evolution

Same equation, new nomenclature:

$$H = \dot{a}/a$$

$$H_0 = \dot{a}/a)_{\text{today}}$$

$$\rho_{cr} = 3H_0^2/8\pi G$$

$$\Omega_i = \rho_i/\rho_{cr}$$

and some numbers:

$$H_0 = 67.3 \pm 1.2 \,\mathrm{km/s/Mpc}$$

Hubble tensión





Introduction and Motivation

$$\frac{k^3}{2\pi^2}P(k,z) = \delta_H^2 \left(\frac{ck}{H_0}\right)^{3+n} T^2(k,z) D_1^2(z) / D_1^2(0).$$

$$\sigma_R = \left[\int_0^\infty \frac{dk}{k} \frac{k^3}{2\pi^2} P(k) \left| \tilde{W}_R(k) \right|^2 \right]^{1/2},$$



Power spectrum of matter

Mass fluctuación R= 8 Mpc







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GravWaves in modified gravity







GravWaves in modified gravity

Horndeski action reads

$$S = \int d^4x \sqrt{-g} \left[\sum_{i=2}^5 M_P^2 \mathcal{L}_i + \mathcal{L}_m \right], \qquad (1)$$

where g is the determinant of the metric tensor, and

$$\mathcal{L}_2 = G_2(\phi, X),\tag{2}$$

$$\mathcal{L}_3 = -G_3(\phi, X) \Box \phi, \tag{3}$$

$$\mathcal{L}_4 = -G_4(\phi, X)R + G_{4,X}[(\Box \phi)^2 - \phi_{;\mu\nu}\phi^{;\mu\nu}], \quad (4)$$

$$\mathcal{L}_5 = -G_5(\phi, X)G_{\mu\nu}\phi^{;\mu\nu} - \frac{1}{6}G_{5,X}[(\Box\phi)^3 \tag{5}$$

$$+ 2\phi_{;\mu\nu}\phi^{;\mu\sigma}\phi^{;\nu}_{;\sigma} - 3\phi_{;\mu\nu}\phi^{;\mu\nu}\Box\phi].$$
(6)

Here, G_i (*i* runs over 2, 3, 4, 5) are functions of a scalar field ϕ and the kinetic term $X \equiv -1/2\nabla^{\nu}\phi\nabla_{\nu}\phi$, and $G_{i,X} \equiv \partial G_i/\partial X$. For $G_2 = \Lambda$, $G_4 = M_P^2/2$ and $G_3 =$ $G_5 = 0$, we recover GR with a cosmological constant. For

$$M_*^2 = 2(G_4 - 2XG_{4X} + XG_{5\phi} - \phi HXG_{5X})$$
 Effective Planck mass



The most general tensor metric perturbation evolution, under the FRW metric, can be written as [39]

$$h''_A + (2+\nu)\mathcal{H}h'_A + (c_T^2k^2 + \mu^2)h_A = \Pi_A , \qquad (1)$$

where h_A is the metric tensor perturbation, being $A = \{+, \times\}$ the label of the two polarization states, and \mathcal{H} is the Hubble rate in conformal time. The quantities ν , c_T and μ represent the running of the effective Planck mass, the GW propagation speed and the effective graviton mass, respectively. The function Π_A denotes extra sources generating GWs, which we assume to be null.

$$\nu = \alpha_M$$



luminosity distance for non-trivial function ν and c_T satisfies the equation 1

$$d_L^{GW}(z) = \sqrt{\frac{c_T(z)}{c_T(0)}} \exp\left[\frac{1}{2} \int_0^z \frac{dz'}{1+z'} \nu(z')\right] \times (1+z) \int_0^z \frac{c_T(z')dz'}{H(z')},$$
(2)

where, for $\nu = 0$ and $c_T = 1$, we recover the general relativity case (Λ CDM cosmology), that is, $d_L^{GW}(z) = d_L^{EM}(z)$, where d_L^{EM} is the standard luminosity distance for an electromagnetic signal. Generalizations and inter-

Introduction and Motivation



劉LIGO

Laser Interferometer Gravitational-Wave Observatory Supported by the National Science Foundation Operated by Caltech and MIT





 $c_T/c = 1 \text{ for } z < 0.1$ Gravitational Wave Speed Runni

$$c_T^2(z) = 1 + \alpha_T(z).$$

 α_T (tensor speed excess) $\alpha_T = \alpha_{T0} a^{n_2}$ Running of the Planck mass $\alpha_M = \frac{1}{HM_*^2} \frac{dM_*^2}{dt},$

M* is the effective Planck mass

$$\alpha_M = \alpha_{M0} a^{n_1}$$



GravWaves in modified gravity



FIG. 1. Corrections on the effective GW luminosity distance (cf. Eq. (2)) as a function of the redshift for different values of the tensor speed excess α_{T0} with fixed values of α_{M0} . Left panel: $\alpha_{M0} = -0.1$, $n_1 = 3$, $n_2 = 1$. Right panel: $\alpha_{M0} = 0.1$, $n_1 = 1$, $n_2 = 1$. The limit $d_L^{EM}(z)/d_L^{EM} = 1$ represents general relativity.



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Methodology and results

GW strain signal

GW strain signal
$$h(t) = A(t) \cos[\Phi(t)]$$
.

Fourier transform

GW inspiral amplitude

$$\tilde{h}(f) = Q\mathcal{A}f^{-7/6}e^{i\Phi(f)}, \quad \mathcal{A} = \sqrt{\frac{5}{96}}\frac{\mathcal{M}_c^{5/6}}{\pi^{2/3}d_L^{GW}} \left(\sum_{i=0}^6 A_i(\pi f)^{i/3}\right)$$

$$Q^{2} = F_{+}^{2}(1 + \cos^{2}(\iota))^{2} + 2F_{\times}^{2}\cos^{2}(\iota)$$

ι is the inclination angle of the binary orbital angular momentum with respect to the line of sight

 F_{+2} , F_{\times}^2 are the two antenna pattern functions

$$\Phi(f) = 2\pi f t_c - \phi_c - \frac{\pi}{4} + \frac{3}{128\eta v^5} \left[1 + \sum_{i=2}^7 \alpha_i v^i \right]$$

inspiral phase of the binary system

Waveform emitted by the binary system





Methodology and results

GW strain signal

Simulation: 1000 data points

GW strain signal $h(t) = A(t) \cos[\Phi(t)]$,

Fourier transform

GW inspiral amplitude

$$\tilde{h}(f) = Q\mathcal{A}f^{-7/6}e^{i\Phi(f)}, \quad \mathcal{A} = \sqrt{\frac{5}{96}}\frac{\mathcal{M}_c^{5/6}}{\pi^{2/3}d_L^{GW}} \left(\sum_{i=0}^6 A_i(\pi f)^{i/3}\right)$$

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inspiral phase of the binary system







$$F_{ij} = \sum_{n} \frac{1}{\sigma_{ins}^2 + \sigma_{lens}^2(z_n) + \sigma_v^2(z_n)} \frac{\partial d_L(z_n)}{\partial \theta_i} \frac{\partial d_L(z_n)}{\partial \theta_j} ,$$
(6)
where the sum *n* runs over all standard sirens
mock events. The derivatives are performed
with respect to the cosmological parameters
 $\theta_i = \{H_0, \ \Omega_{m0}, \ \alpha_{M0}, \ \alpha_{T0}, \ n_1, \ n_2\}$ evaluated at
their fiducial input values. In our analysis, we used
 $\theta_i = \{67.4, \ 0.30, \ 0.0, \ 0.0, \ 3.0 \ (1.0), \ 1.0\}$ as fiducial

Methodology and results





FIG. 3. One-dimensional marginalized distribution, and 68% and 95% C.L. regions for the parameters of the theoretical models under study, from the ET and DECIGO experiments. On the left panel and right panel, the stability conditions $\alpha_{M0} < 0$ and $\alpha_{M0} > 0$ are considered, respectively.



IMPLICATIONS ON MODIFIED GRAVITY PHENOMENOLOGY

Parameter	$\sigma({ m ET})$	$\sigma(\text{DECIGO})$
$lpha_{T0}$	0.0099	0.0033
$lpha_{M0}$	> -0.17	> -0.055
n_1	0.60	0.22
n_2	1.50	0.59

TABLE I. Forecast constraints from the ET and DECIGO experiments, under the stability condition $\alpha_{M0} < 0$. The notations $\sigma(\text{ET})$ and $\sigma(\text{DECIGO})$ represent the 95% C.L. estimation on the fiducial input values from ET and DECIGO, respectively.

Parameter	$\sigma({\rm ET})$	$\sigma(\text{DECIGO})$
$lpha_{T0}$	0.0077	0.0032
$lpha_{M0}$	< 0.091	< 0.052
n_1	0.31	0.21
n_2	1.50	0.59

TABLE II. Forecast constraints from the ET and DECIGO experiments, under the stability condition $\alpha_{M0} > 0$. The notation is the same as in Table I.

Within the Horndeski theories of gravity

$$M_*^2 \alpha_T = 2X(2G_{4X} - 2G_{5\phi} - (\ddot{\phi} - \dot{\phi})G_{5X})$$

we consider the "derivative coupling theory" in which thescalar field couples to the Einstein tensor

 $\xi \phi G_{\mu\nu} \nabla^{\mu} \nabla^{\nu} \phi$

The parameter ξ represents the coupling constant of the theory and quantifies possible anomalies on the GWs speed propagation ($\xi = 0$ in GR), so $M_{\star}^2 \alpha_T = 2\xi \dot{\phi}^2$.

$$G_4 = M_{pl}^2/2$$
 and $G_5 = \xi \phi$

 $c_T^2 = 1 + \frac{2\dot{\phi}^2}{M_*^2}\xi$.

At intermediate z, it is reasonable to assume $\phi/M_* \simeq 1$, so that we estimate $-0.005 < \xi < 0.005 (-0.0018 < \xi < 0.0018)$ at the 95% C.L. from ET (DECIGO), in the case $\alpha_{M0} < 0$.



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Summary and conclusions



- 1. Due to extra degrees of freedom of gravitational origin, modified gravity models predict physical properties beyond the standard features of general relativity.
- 2. Motivated by this aspect, we thus performed a forecast analysis using 1000 standard siren events from BNS mergers, within the sensitivity predicted for ET and DECIGO up to z = 2 ($\simeq 15539Mpc$).
- 3. We found $|c_T/c 1| \le 10^{-2} (10^{-3})$ from ET (DECIGO), which leaves room for small possible corrections predicted by alternative theories, compared to the only information from GW170817 event at very low z.
- **4.** Nevertheless, the main findings of this work represent the first observational constraints obtained by using information from <u>SS</u> mock data from future detector design.
- 5. In this respect, our results open a new window for possible tests on $c_T(z)$ in the future.



Bibliography



Machine Learning (Gaussian Processes







$$\begin{split} -wq &= 2\Big(EE'^2 + E^2E'' - \frac{w'}{w}E^2E'\Big)(1+z)^2 \\ &- \Big[2(5+3w)E^2E' - 3\frac{w'}{w}E^3\Big](1+z) \\ &+ 9(1+w)E^3, \end{split}$$



Big announcement between Dec 2022 and Jun 2023. Stay tuned.



The NANOGrav Program for Gravitational Waves and Fundamental Physics



The North American Nanohertz Observatory for Gravitational Waves







