



FCCIS – The Future Circular Collider Innovation Study. This INFRADEV Research and Innovation Action project receives funding from the European Union's H2020 Framework Programme under grant agreement no. 951754.

FCC HEB lattice options

B. Dalena, A. Chance

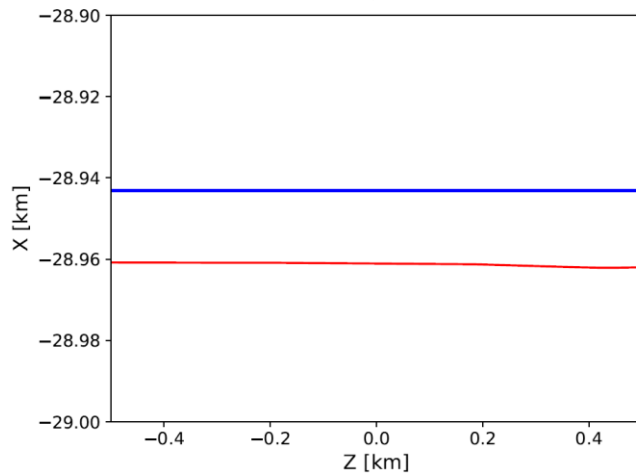
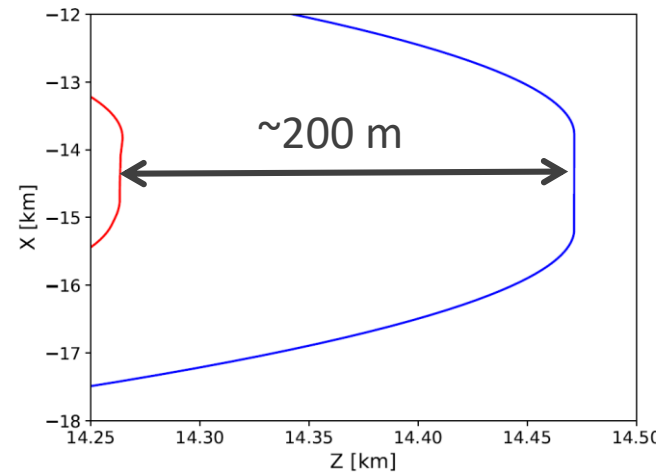
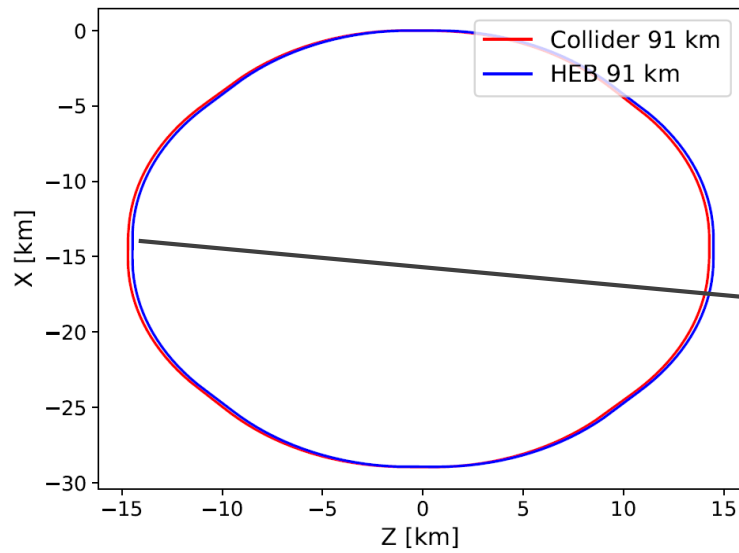
Thanks to:

B. Haerer, L. Van Riesen-Haupt, T. Charles, R. Tomas, T. Persson, F. Antoniou, O. Etisken, M. Zampetakis, M. Hofer, F. Carlier, B. Holzer, A. Franchi, A. Latina

1



- Layout of the HEB ring
- $60^\circ/60^\circ$ and $90^\circ/90^\circ$ Optics
- DA vs momentum
- Momentum detuning



Total length	m
Collider	91174.117
HEB	91172.691

Magnet	Parameter	Unit	Value
Dipole	Field at injection (20 GeV)	G	71
	Field at W energy (80 GeV)	G	284
	Length	m	11.1
Quadrupole	Gradient at injection (20 GeV)	T/m	1.74
	Gradient at W energy (80 GeV)	T/m	6.9
	Length	m	1.5
Sextupole	Gradient at injection (20 GeV)	T/m ²	75
	Gradient at W energy (80 GeV)	T/m ²	300
	Length	m	0.5

- FODO cells of ~ 52 m
- Made of 4 dipole, 2 quadrupoles and 2 sextupoles

Distance between dipoles: 0.65 m

Distance between quadrupole and sextupole: 0.15 m

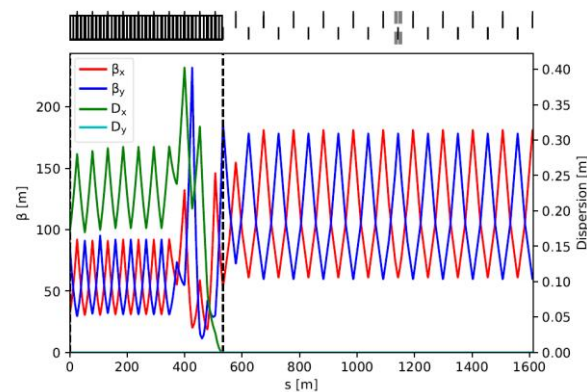
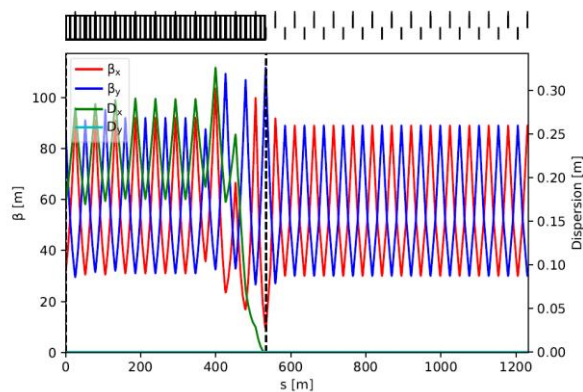
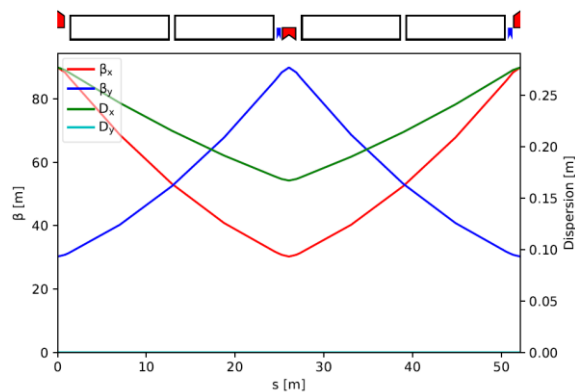
Distance between dipole and sextupole: 0.356

Distance between quadrupole and dipole: 0.704 m
(it includes BPM and dipole correctors)

dipoles = 2×2944

quadrupoles = 2944

sextupoles = 2632/6



Magnet	Parameter	Unit	Value
Dipole	Field at injection (20 GeV)	G	71
	Field at ttbar energy (182.5 GeV)	G	650
	Length	m	11.1
Quadrupole	Gradient at injection (20 GeV)	T/m	2.5
	Gradient at ttbar energy (182.5 GeV)	T/m	22.5
	Length	m	1.5
Sextupole	Gradient at injection (20 GeV)	T/m ²	174
	Gradient at ttbar energy (182.5 GeV)	T/m ²	1582
	Length	m	0.5

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- Made of 4 dipole, 2 quadrupoles and 2 sextupoles

Distance between dipoles: 0.65 m

Distance between quadrupole and sextupole: 0.15 m

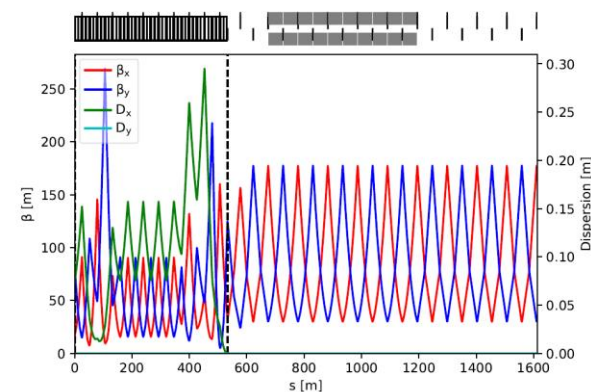
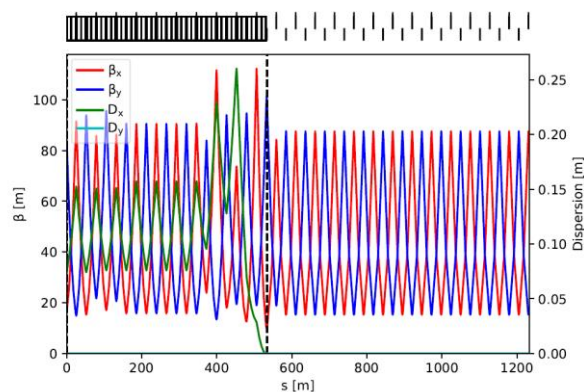
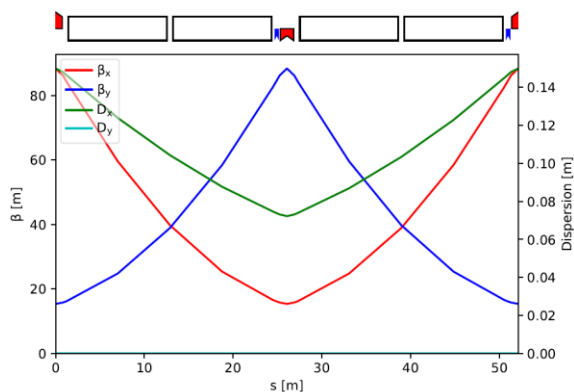
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Static dipole field errors of the CT dipole design at 56Gs considered + 10% random part

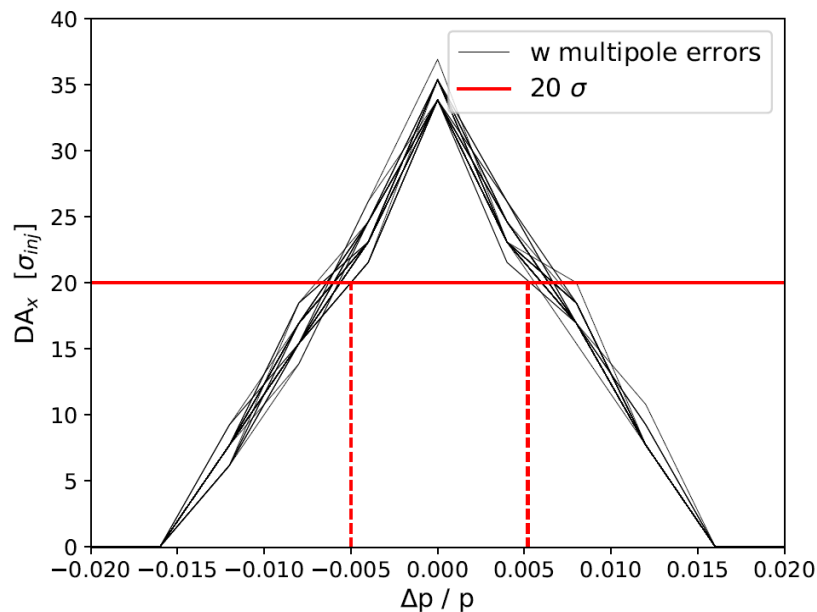
Dynamic field effect not taken into account in this simulations: dipole and multipole reproducibility expected to be $\leq 5 \times 10^{-4}$

91km 60°/60° optics

Stable initial action @ 4500 turns (~15% tx 20 GeV)

Geometric emittance injected 1.27e-9 nm

$$\beta_x = 83.2 \quad \beta_y = 32.2 \quad D_x = 0$$



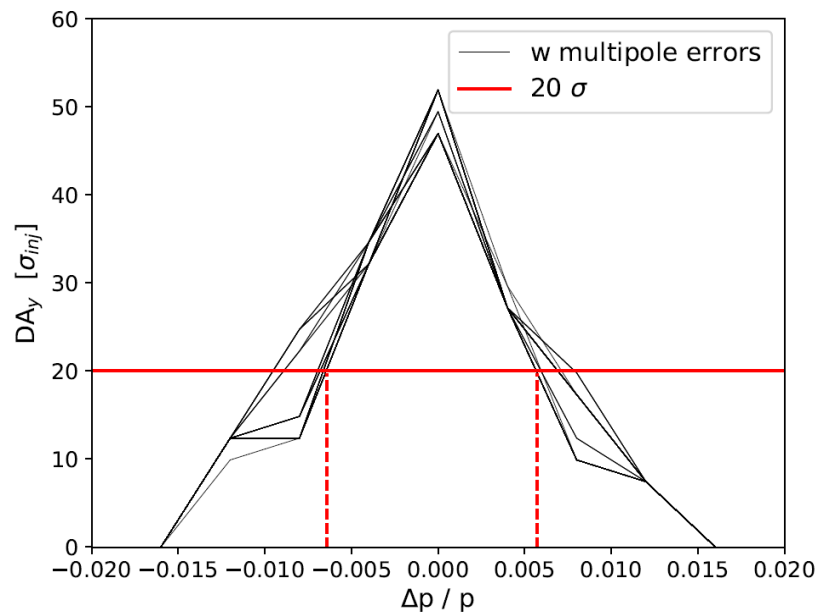
Courtesy of F. Zimmermann and Jie Gao

GFR=R26	CT dipole		Iron-core dipole	
	28Gs	56Gs	28Gs	56Gs
B1/B0	-5.20E-04	-1.04E-04	-1.56E-03	-2.60E-04
B2/B0	4.73E-04	5.41E-04	-2.03E-03	-2.03E-04
B3/B0	-7.03E-06	1.05E-04	3.52E-04	1.76E-04
B4/B0	-9.14E-04	-3.66E-04	4.57E-04	-1.83E-04
B5/B0	3.56E-05	-2.38E-05	-2.38E-05	-3.56E-05
B6/B0	6.18E-04	2.16E-04	-3.09E-04	9.27E-05

relative values @ R = 26 mm

60 seeds

MadX Thin-Lens Tracking



91km 90°/90° optics

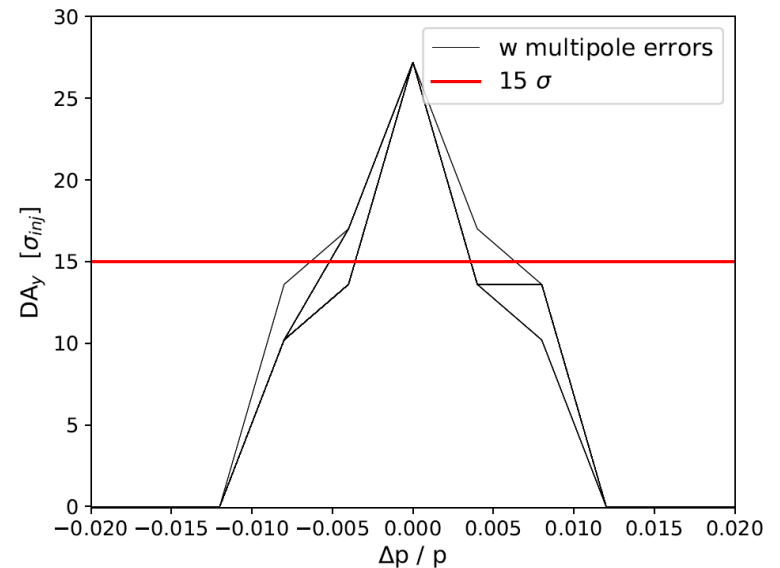
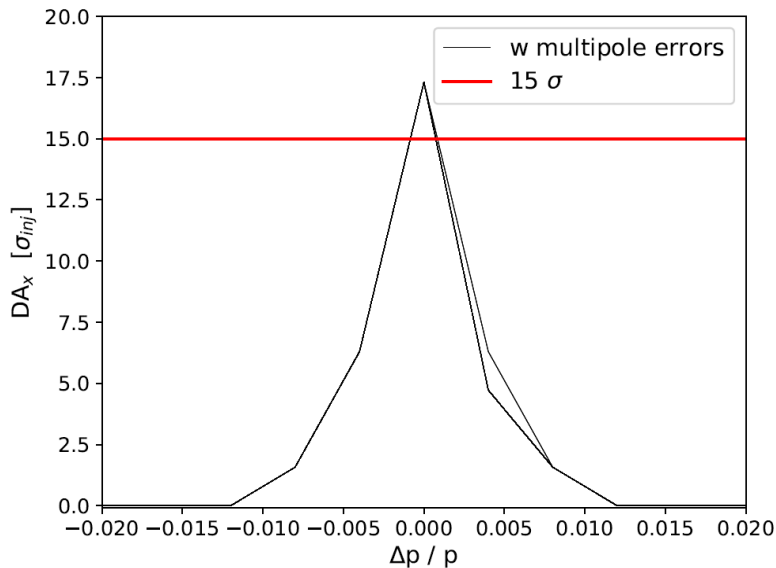
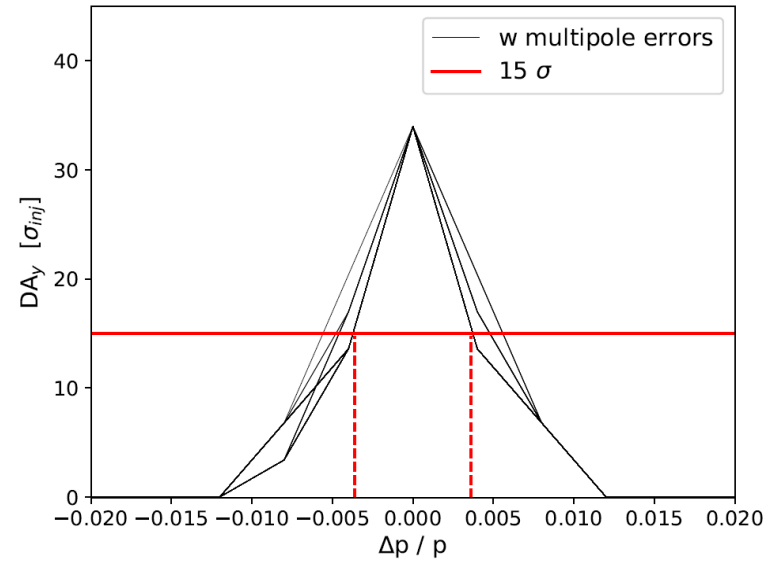
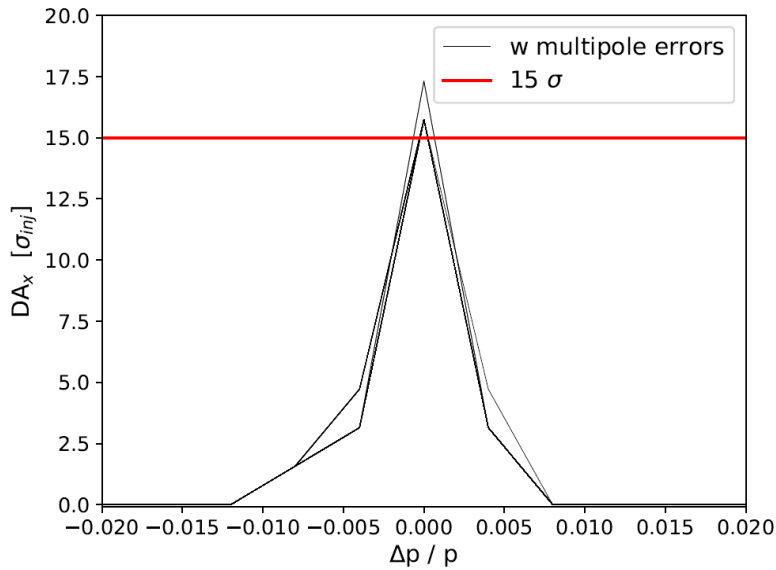
$$\beta_x = 79.5$$

$$\beta_y = 17.0$$

$$D_x = 0$$

$$Q_x = 417.225$$

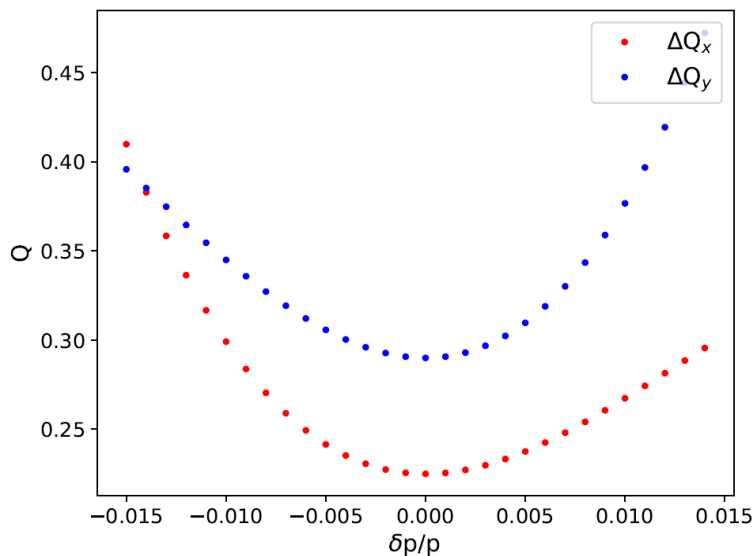
$$Q_y = 413.29$$



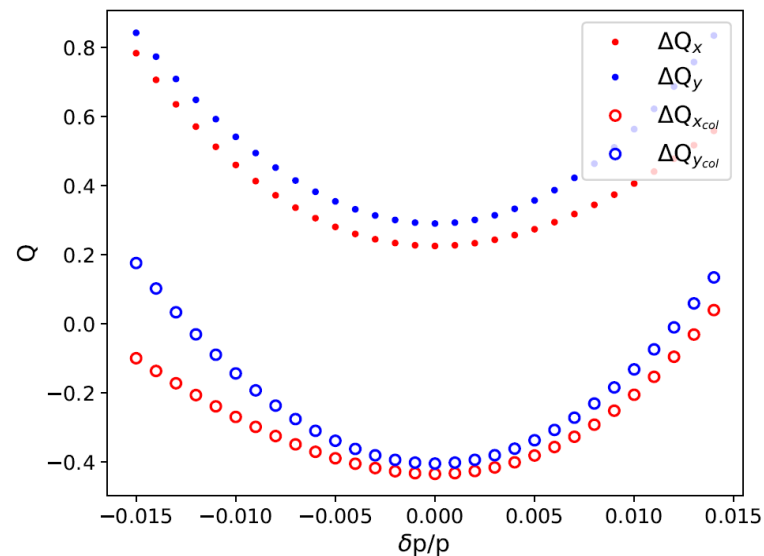
$$Q_x = 416.565$$

$$Q_y = 413.595$$

91km 60°/60° optics



91km 90°/90° optics



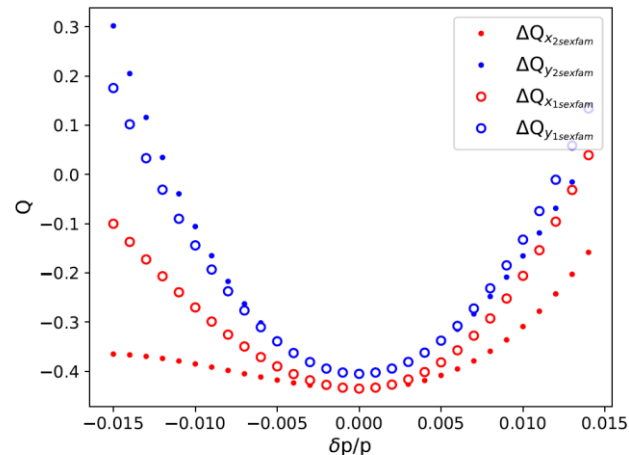
	Q	$\partial Q / \partial \delta$	$\partial^2 Q / \delta^2 \delta$	$\partial^3 Q / \delta^3 \delta$
x	.225	0	4155.317	-161460.363
y	.29	0	5244.035	66921.874
x	.225 (w/o sex)	-661.13	924.534	-569581.860
y	.29 (w/o sex)	125.94	1716.270	287914.529
x	.565	0	3940.796	192685.700
y	.595	0	5336.346	35042.450

Strategy:

$$Q_z \left(\frac{\delta p}{p_0} \right) = Q_{z0} + \underbrace{Q'_z \left(\frac{\delta p}{p_0} \right)}_0 + \frac{1}{2!} \underbrace{Q''_z \left(\frac{\delta p}{p_0} \right)^2}_{\text{abs} < 0.2} + \frac{1}{3!} \underbrace{Q'''_z \left(\frac{\delta p}{p_0} \right)^3}_{\text{abs} < 0.05} + \dots$$

$\left(\frac{\delta p}{p_0} = 0.01 \right)$

- difficult to reduce Q'' without increasing Q'''
- Montague functions become more regular but higher
- DA doesn't improve



	Q	$\partial Q / \partial \delta$	$\partial^2 Q / \delta^2$	$\partial^3 Q / \delta^3$
x	.565	0	3940.796	192685.700
y	.595	0	5336.346	35042.450
x	.565 (2 sex fam)	0	1761.903	227601.518
y	.595 (2 sex fam)	0	5388.272	-178897.067

- ▶ **Iterate on HEB layout**
 - Improve superposition with collider with 10 m (< 10 m) shift at IPs
- ▶ **Improve off-momentum DA for the 90°/90° optics**
 - Octupoles ?
 - Phase advance between arcs?
 - Other strategy for sextupoles families optimizations (MOGA,...) ?

- ▶ **HEB optics repository and alternative optics**

- ▶ **Define tolerances and correctors for linear imperfections**



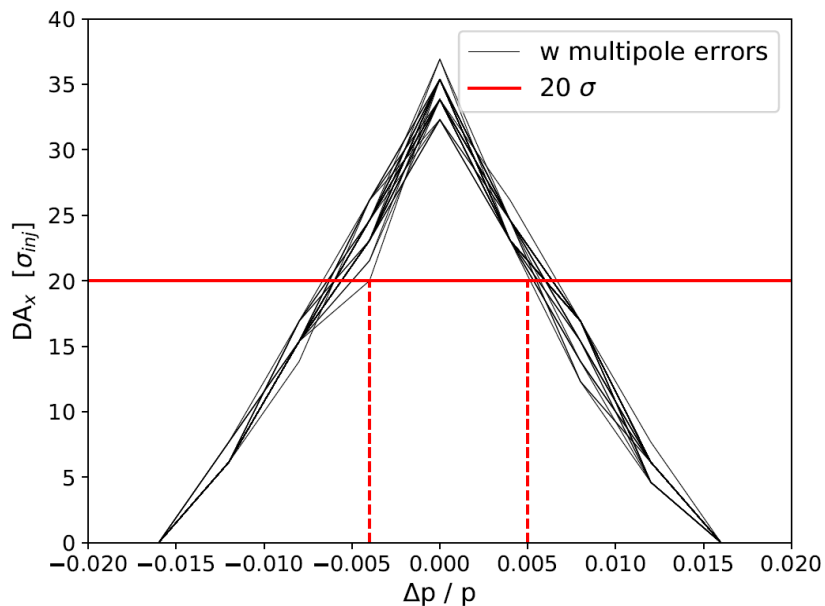
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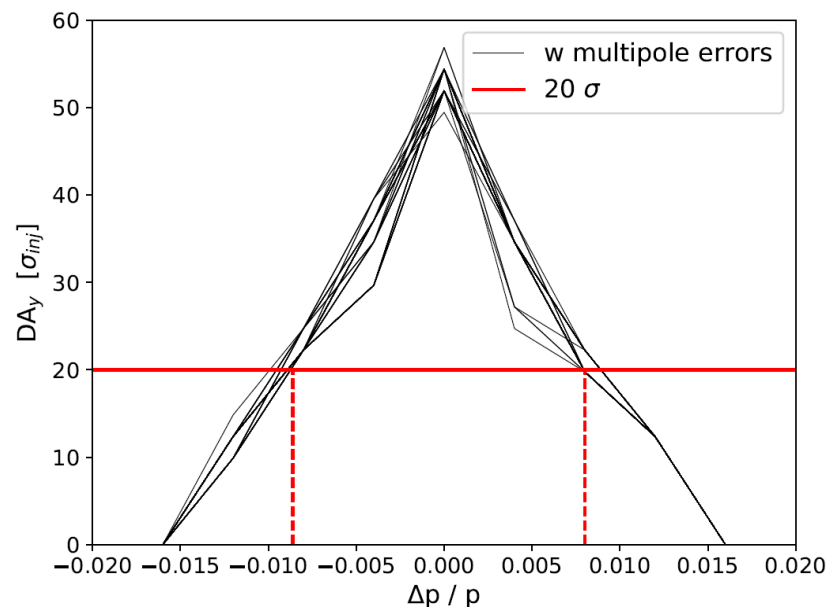
Courtesy of F. Zimmermann and Jie Gao

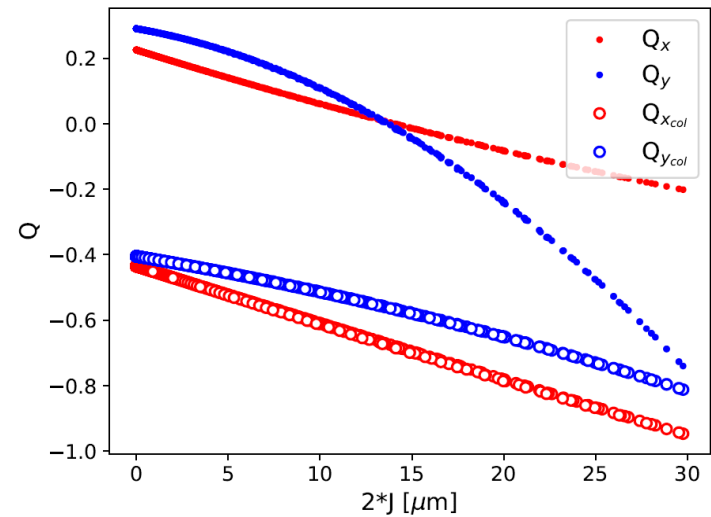
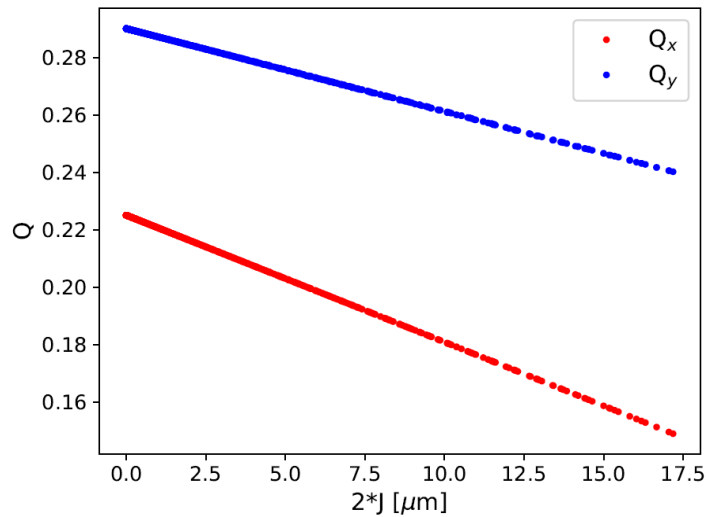
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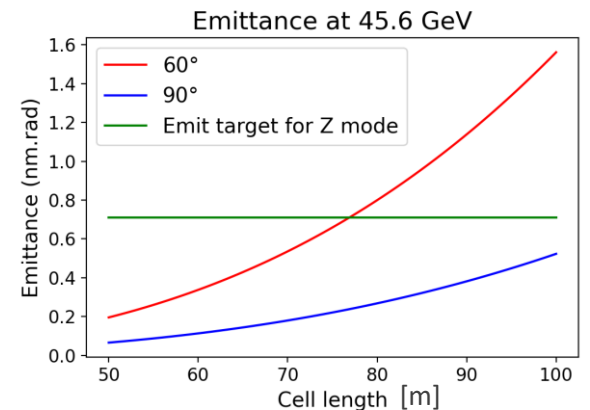
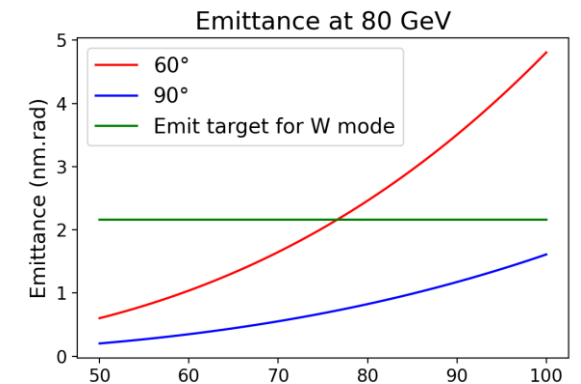
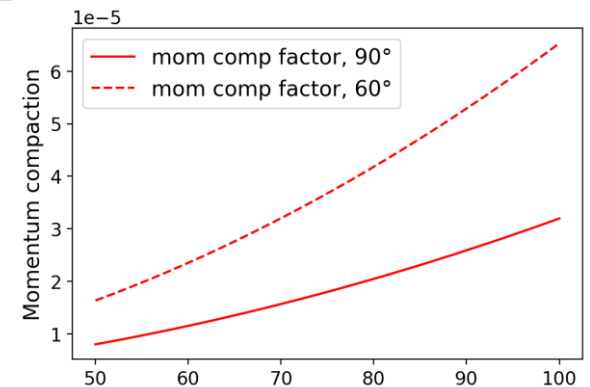




- Booster Equilibrium rms emittance \leq collider

Beam Energy [GeV]	Eq. Emittance [nm rad] 60°/60°	Eq. Emittance [nm rad] 90°/90°	Eq. Emittance Collider [nm rad]	Eq. emittance Collider new [nm rad]
45.6 (Z)	0.235	0.078	0.24	0.71
80 (W)	0.729	0.242	0.84	2.16
120 (H)	4.229	0.545	0.63	0.64
175 (tt)	3.540	1.172	1.48	1.49

- ⇒ 60°/60° retained for Z and W operation (mitigation of MI and IBS)
- ⇒ 90°/90° 100 m cell could gain a bit in momentum compaction at Z & W
- ⇒ 90°/90° required for H and ttbar final emittances



2 dipoles with two different curvatures, proposed for the electron-ion collider (EIC)

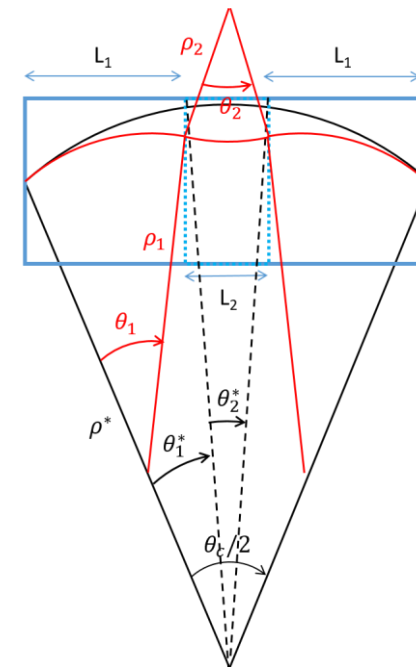
Damping time can be reduced by playing on the ratio between the two different fields.

Advantages:

- No impact on the layout
- Increase I_2 without damping wigglers
- Higher dipole field at injection energy

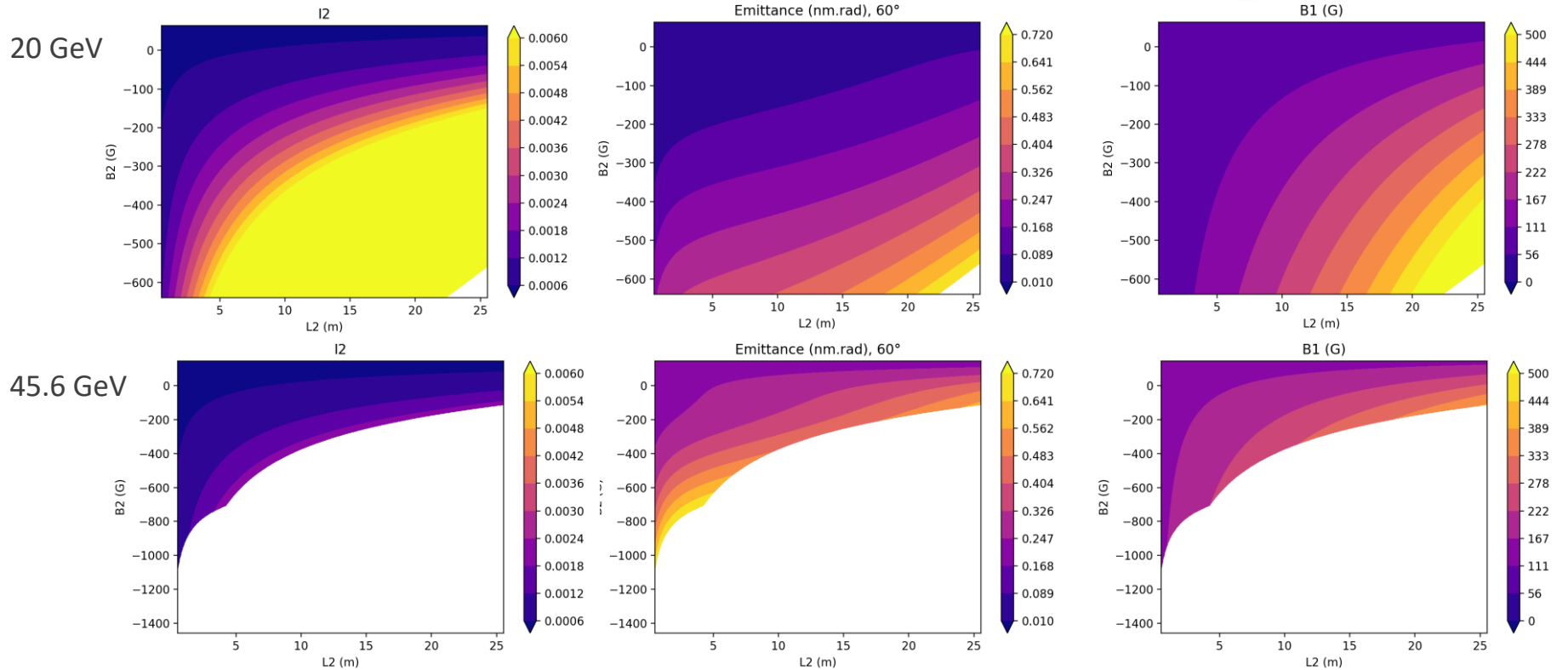
Drawbacks:

- Different reference orbits \Rightarrow **reduction of beam stay clear?**
- **More synchrotron** radiation and in **opposite direction** of foreseen absorber (at injection) \Rightarrow **vacuum quality to be investigated**



$$a = \frac{L_2}{L_0} \quad b = \frac{\rho^*}{\rho_2}$$

$$I_i = I_i(\mu_x, L_{cell}, \theta_c/2, a, b)$$

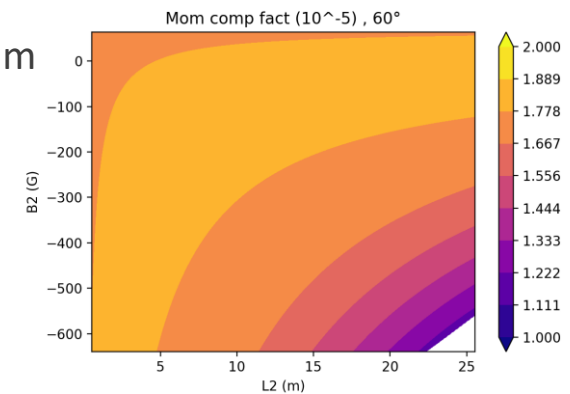


Constraints: **Energy loss** per turn ≤ 126 MeV (\sim wiggler), **eq. emit** < 0.72 nm

- $4 \times I_2$ can be obtained with a $L_2 \sim 5$ m, $B_2 \sim -200$ G, $B_1 \sim 170$ G at 20 GeV and $B_2 \sim -400$ G, $B_1 \sim 200$ G at 45.6 GeV
- **Minimum dipole field** at injection $\sim 3 \times$ present lattice
- Momentum compaction $\sim 1.8 \cdot 10^{-5}$ ($\sim 60^\circ/60^\circ$ lattice)

\Rightarrow Which is the maximum allowed budget for radiated power ?

\Rightarrow Which is the possible maximum field derivative for the two dipoles ?



H. De Grandsaignes, A. Chance

Main quadrupoles :

$b2 = 2 \times 10^{-4}$ relative random error

Main Dipoles:

$b1 = 1 \times 10^{-4}$ relative random error

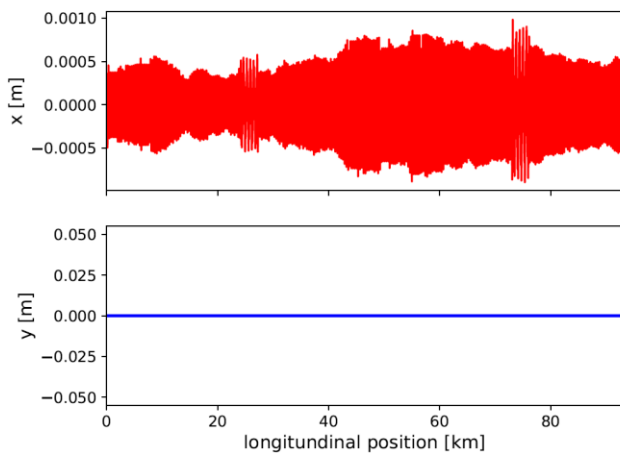
$b2 = -1 \times 10^{-4}$ relative systematic error + 10% random component



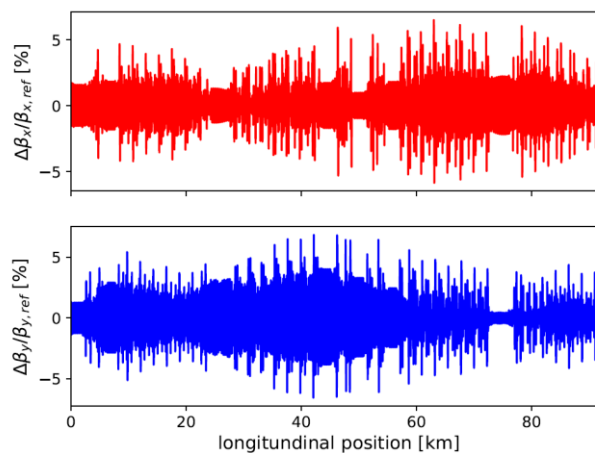
Courtesy of F. Zimmermann and Jie Gao

Without orbit, beta-beating and dispersion correction:

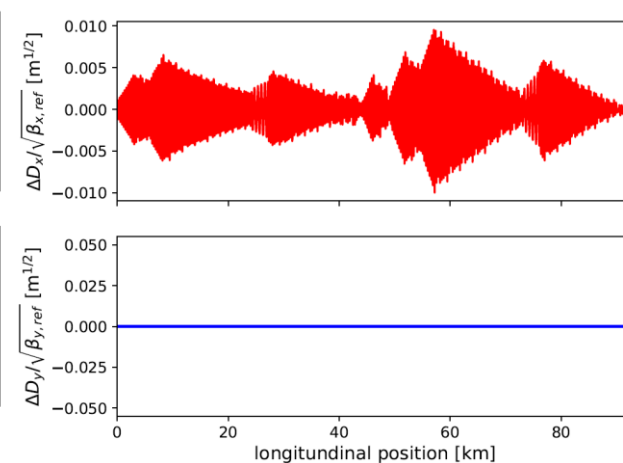
orbit



beta-beating



normalized-dispersion

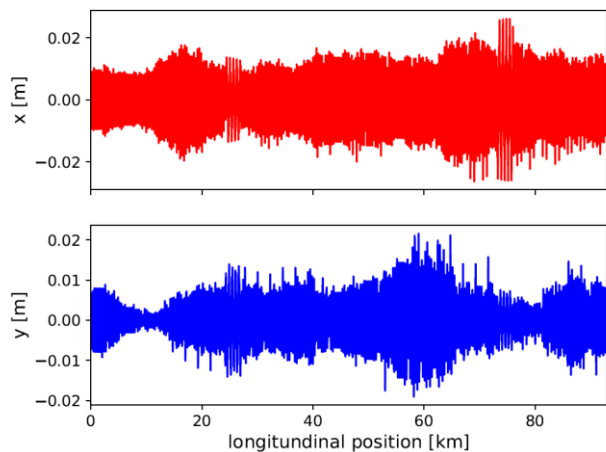


Removing all other mis-alignment except for quadrupole offsets
 Reducing the randomly distributed offset values to $\pm 3 \sigma = 100 \mu\text{m}$

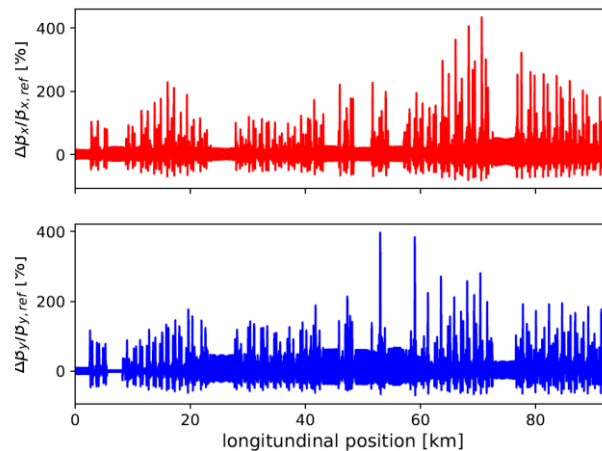
Type	Δx (μm)	Δy (μm)	ΔS (μm)	ΔTheta (μrad)	ΔPhi (μrad)	ΔPsi (μrad)	Field Errors
Arc quad	100	100					
Arc sext							
Dip							
Girders							
BPM							

Without orbit, beta-beating and dispersion correction:

orbit



beta-beating



normalized-dispersion

