Extracting the time of core bounce from core-collapse supernovae

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Extracting t_0 using an unbinned maximum likelihood technique

- Assume that the data derives from a Poisson PDF defined by: $P[n(t_i); \bar{n}(t_i - t_0)] = \frac{\bar{n}(t_i - t_0)^{n(t_i - t_0)} \cdot e^{-\bar{n}(t_i - t_0)}}{n(t_i)!}$
- The negative ln likelihood (NLL) is therefore:

$$\ell(t_0) = 2 \cdot \sum_{i=1}^{N} \eta \cdot \bar{n}(t_i - t_0) + n(t_i) \cdot \ln(\eta \cdot \bar{n}(t_i - t_0))$$

- Here, n(t) is the vector of data with N events (where t_i is the time stamp of the i-th event), η is the normalization condition and $\bar{n}(t)$ is the mean cumulative neutron count.
 - The determination of the mean cumulative count is depicted on the top right (exact technique is left in the backup slides).
- t_0 can be obtained from a minimization of $\ell(t_0)$ using MINOS/Minuit2.
 - An example of this can be found on the bottom left plot (where the errors on the extracted t_0 come from the points at $\ell(t_0) \pm 1$.
- The precision and resolution of the extracted t_0 can be quantified by repeating the NLL fit for 10^4 SN bursts (see bottom right).
 - Fitting data to itself does not account for systematic uncertainties (no knowledge of 'model of best fit'). To do so, mix and match various models to quantify offset.







Extracting t_0 using a digital CFD

- We noticed in our analysis that extracting t₀ as a function of distance, introduced some 'walk' from the expected t₀.
 - As will be shown later.
 - Walk was gradual, less than ½ a millisecond from 1-5 kpc.
- Elected to implement a digital constant fraction discriminator (CFD) to attempt a correction for this walk.
 - Feed input signal (cumulative events from entire burst) into CFD.
 - Invert and delay the signal, then scale it down by some value (constant fraction).
 - Sum the two signals together (see right).
 - Locate t₀ from the point where the signal crossed zero.
 - Performance of extracting t_0 is comparable to that the likelihood fit.











Extracting t_0 with a liner fit

- Linear technique arose as a method of getting around the systematic uncertainties included in the likelihood technique.
 - Use a single function as the cumulative PDF for all models.
- A relatively simple approximation is to treat the cumulative event count in the neutronization region as linear.

 $f(x) = [0] + [1] * (x - [2]) * (x > [2]) * (x < [4] + [2]) + \dots$

- Introduce a five-parameter fit (first three parameters constrain fit in neutronization region).
 - [0] intercept of linear line.
 - [1] average event rate of the tested models.
 - [2] offset (wrt time) from the true t_{0.}
- Final two parameters constrain end point of fit and event rate immediately following neutronization.
- Results for the extraction of parameter [2] for 10⁴ bursts from the Garching model at 1 kpc in HALO-1kT can be found on the bottom right plot.



p_{_} [s]



Extracting t_0 with the Anderson Darling test

- Anderson Darling (AD) test is intended to determine the probability a sample belongs to some parent CDF. ٠
 - It is an extension of the Kolmogorov Smirnov (KS) test.
 - The KS test was investigated as a candidate technique, performance collapses past 1 kpc in HALO-1kT.
- We implement it here as:

$$A^{2}(t_{0}) = -N - S(t_{0})$$

$$S(t_{0}) = \sum_{i=1}^{N} \frac{2i-1}{N} \left[\ln \bar{n}(t_{i}-t_{0}) + \ln(1-\bar{n}(t_{N+1-i}-t_{0})) \right]$$

- Where *N* is the number of events (each with timestamp t_i), and \bar{n} is the mean light curve evaluated at some offset.
- Analogous to the NLL technique, must account for systematic uncertainties when mixing model and PDF.
- Distribution of extracted t_0 for the Sukhbold et al. SFHo z9.6 model at 1 kpc can be found in the bottom right.
 - Of the five techniques implemented, the AD test has the most numerical issues.



Mean cumulative neutron count (varying fluxes, 1 kpc)

0_0.0008

-0.0006

-0.0004 -0.0002

0

0.0002

0.0004

0.0006

0.0008

0.001 Extracted f₀ [s]



Extracting t_0 via cross-correlation

- Originally intended to avoid binning our observed SN signal.
 - For HALO-1kT, relatively low statistics at 10 kpc, bins on the order 1 ms are sparsely populated.
- We implement cross-correlation as:

$$(H_n * H_{\bar{n}})(t - t_0) = -\sum_{\infty} H_n(t) \cdot H_{\bar{n}}(t - t_0)$$

- Where H_n is the 1D histogram of the observed signal, and $H_{\bar{n}}$ is the event rate (top) evaluated at some offset.
 - Observed time series is placed in a histogram with 1 ms bins.
 - $(H_n * H_{\bar{n}})$ should reach a minimum around the Monte Carlo truth $t_0 = 0$.
 - An example can be found in the middle figure.
- The extracted t_0 distribution for the Sukhbold et al. SFHo z9.6 model at 1 kpc in HALO-1kT can be found in the bottom right.







Projection of techniques













Final remarks on SNO+

- As it stands, SNO+ fails to extract t_0 with the same precision as HALO-1kT.
 - It is not a question of statistics, as SNO+ expects more events in the time window used in this analysis.
- My initial thoughts are that the neutronization burst in HALO-1kT (primarily v_e sensitive) is much easier to fit.
- A time window is necessary to reduce systematic uncertainties introduced when mixing models.
- However, with the current time window, there isn't a pronounced feature that the likelihood can easily locate.
- I have begun running some preliminary simulations of the entire burst to see if this improves our results.
 - For context, in both HALO-1kT and HALO, performance degrades as more of the burst is used. Maybe things will be different for SNO+.



Depicted above is the mean light curves as observed in HALO-1kT and SNO+ for the SFHo model at 1 kpc. The abrupt cut-off at 50 ms in SNO+ is a result of the upper time in sntools being set to 50 ms. Additionally, for context, in HALO-1kT the time of the events used comes from the capture time on ³He in the proportional counters. For SNO+, it comes from the event times as registered on the GPS clock in UTC. This is then shifted back to the Monte Carlo truth values.



Integration into SNEWPDAG

- Throughout the hackathon I have worked on implementing some of these techniques into SNEWPDAG.
 - Constant fraction discriminator
 - Negative log likelihood
 - Linear fit
 - Anderson Darling test
 - Cross-correlation
- Will move away from the full Monte Carlo treatment done in HALO-1KT, HALO and SNO+.
 - Will still have to account for detector response, background, etc.
- Run other v_e sensitive detectors through this pipeline to determine if my initial thoughts regarding the significance of the neutronization burst are true.
 - Will also be running some simulations with ν oscillations.
- Each detector will be unique and formal recommendations on the technique required to extract t_0 can be made once each detector is tested.
 - For HALO-1kT, the ideal candidate appears to be the CFD technique.





Thank you for listening! Questions?





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Negative Log Likelihood in SNO+

- We apply the same technique used in HALO-1kT (slide 2) to the output from the SNO+ Monte Carlo.
 - The background is added in, Poisson fluctuated and sampled from a physics run. ٠
 - However, the thresholds of this analysis are raised to a cleaned nhit > 800, effectively removing its contribution.
- On top of the level 2 and level 3 triggers applied to the data, we introduce an additional cūt.
 - Require 5 events with greater than 500 nhit each in a rolling 20 ms window.
 - This is intended to remove the sparse ٠ neutrino signal in the leading edge.
 - For both the likelihood and CFD technique these events caused severe issues in our ٠ extraction techniques.
 - Also cuts out many of elastic scattering on ٠ protons as a result.
- Applying these cuts will yield the event distribution on the top right.
 - The resulting likelihood function formed with the mean light curve can be found on ٠ the bottom right.



0.03 0.04 0.05 0.06 Monte Carlo truth event time [s]

0 1

0-0.52 -0.51 -0.5 -0.49 -0.48 -0.47 -0.46 -0.45

-0.01

0

0.02



Comparison to HALO-1kT

- Depicted on the top right is the extracted t₀ from the SFHo z9.6 model in both HALO-1kT (left) and SNO+ (right) at 1 kpc.
 - Precision of extracted t₀ is reduced by a factor of 3 in SNO+.
 - Difference in statistics is not attributed to failures to fit but rather the amount of simulations done.
- On the bottom right is the extracted t₀ with the systematics of fitting all models to one another included.
 - With the systematics included the difference in precision is reduced to a factor of ~2.5.
 - With the current techniques, SNO+ does not obtain sub 1 ms precision at 1 kpc.
 - The comparison between the two experiments is not much improved at further distances.

