

EPPS21 nuclear PDFs

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Reference: EPJC 82, 413 [arXiv:2112.12462]

Recent nuclear PDFs

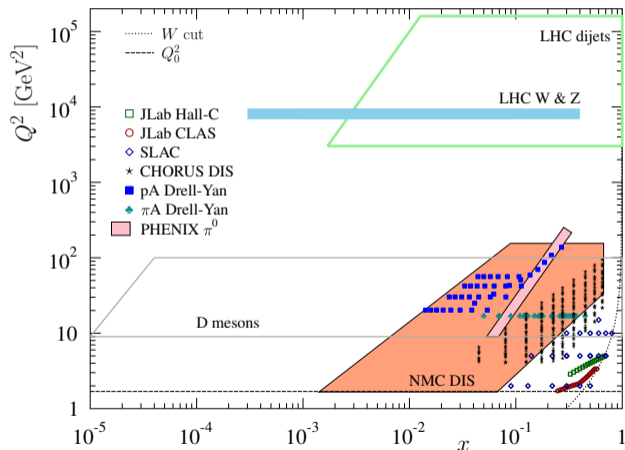
	EPPS16	TUJU21	NNPDF3.0	NCTEQ15WZSIH	EPPS21
Order in α_s	NLO	NLO + NNLO	NLO	NLO	NLO
DIS $\ell^- + A$	✓	✓	✓	✓	✓
DIS $\nu + A$	✓	✓	✓		✓
Drell-Yan p+A	✓		✓	✓	✓
Drell-Yan in $\pi + A$	✓				✓
p+Pb dijets	✓		✓		✓
p+Pb W & Z	✓	✓	✓	✓	✓
p+Pb D-mesons			✓		✓ <i>New!</i>
p+Pb direct γ			✓		
p+Pb π^0, π^\pm, K^\pm				✓	
d+Au π^0, π^\pm	✓			✓	✓
datapoints	1811	2410	2188	940	2077
free parameters	20	16	256	19	24
error analysis	Hessian	Hessian	Monte-Carlo	Hessian	Hessian
heavy-quark scheme	SACOT	FONLL	FONLL	SACOT	SACOT
fitted flavours	6	4	6	5	6
proton PDF correlations			✓		✓ <i>New!</i>
reference	EPJC 77, 163	2112.11904	2201.12363	PRD 104, 094005	EPJC 82, 413

fixed target data

collider data

The kinematic/virtuality reach of the data in EPPS21

- The available x, Q^2 region is getting wider
- New data in EPPS21 vs. EPPS16:
 - CMS 5TeV double-diff. dijets
 - LHCb 5TeV double-diff. D mesons
 - CMS 8.16TeV W^\pm
 - JLab Hall-C and CLAS DIS



- Our definition of nuclear PDFs

Free proton baseline = **CT18A**

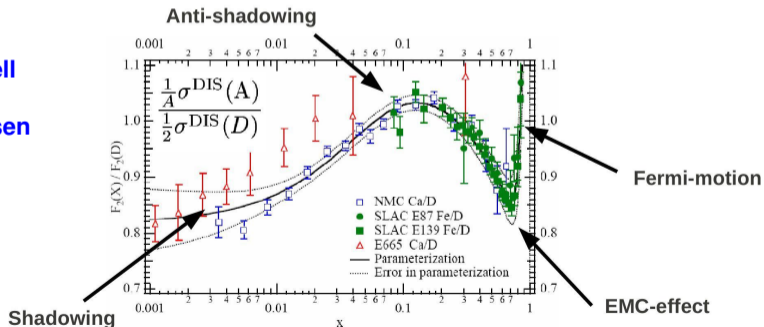
$$f_i^{P/A}(x, Q^2) \equiv R_i^{P/A}(x, Q^2) f_i^P(x, Q^2)$$

Nuclear modifications

- Fit ratios $\sigma^{\text{DIS}}(\ell^- A)/\sigma^{\text{DIS}}(\ell^- D)$

⇒ **Need a free-proton PDF as well**

⇒ **Nuclear PDFs tied to the chosen free-proton PDFs**



- Our definition of nuclear PDFs

Free proton baseline = **CT18A**

$$f_i^{P/A}(x, Q^2) \equiv R_i^{P/A}(x, Q^2) f_i^P(x, Q^2)$$

Nuclear modifications

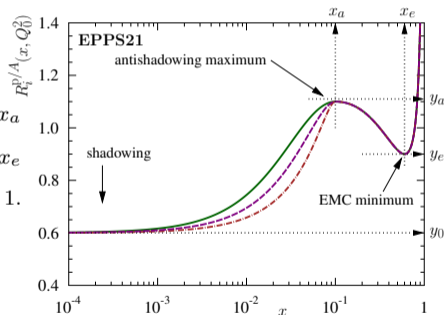
- Fit function x dependence at $Q_0^2 = m_{\text{charm}}^2$

$$R_i^{P/A}(x, Q_0^2) = \begin{cases} a_0 + a_1(x - x_a) \left[e^{-x a_2/x_a} - e^{-a_2} \right], & x \leq x_a \\ b_0 x^{b_1} (1-x)^{b_2} e^{x b_3}, & x_a \leq x \leq x_e \\ c_0 + c_1 (c_2 - x) (1-x)^{-\beta}, & x_e \leq x \leq 1. \end{cases}$$

- The A dependence parametrized at $x \rightarrow 0$, x_a , and x_e

$$y_i(A) = 1 + \left[y_i(A_{\text{ref}}) - 1 \right] \left(\frac{A}{A_{\text{ref}}} \right)^{\gamma_i}, \quad A_{\text{ref}} = 12$$

- For strange $\gamma_{y_0} \rightarrow \gamma_{y_0} y_0 \theta(1 - y_0)$ to keep away from overly negative strangeness



- Our definition of nuclear PDFs

Free proton baseline = **CT18A**

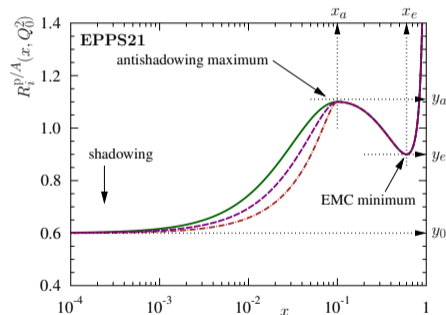
$$f_i^{P/A}(x, Q^2) \equiv R_i^{P/A}(x, Q^2) f_i^P(x, Q^2)$$

Nuclear modifications

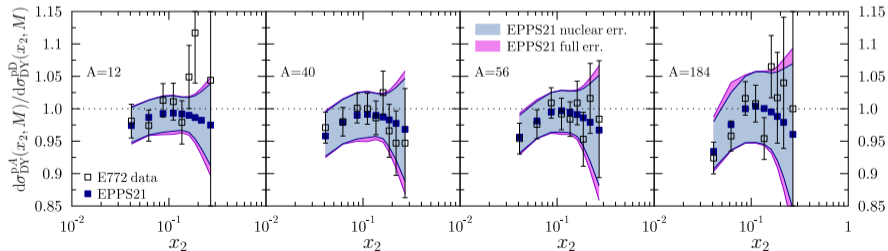
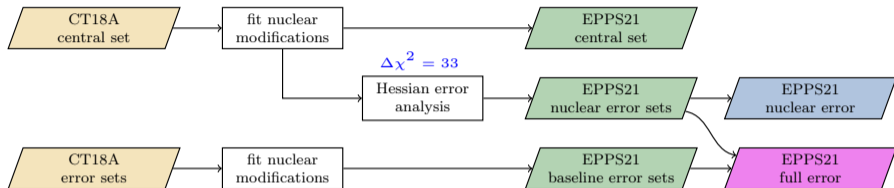
- For **small nuclei** the smooth A dependence appears to work less well. Introduce extra parameters,

$$R_i^{P/A}(x, Q_0^2) \longrightarrow 1 + f_A [R_i^{P/A}(x, Q_0^2) - 1]$$

central fit results with $f_3 = 0.291$, $f_6 = 0.495$.



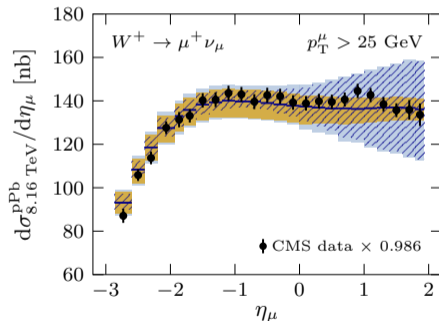
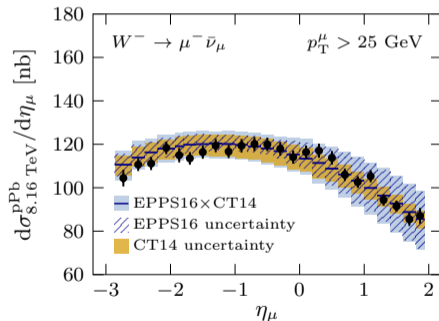
- Dependence of proton PDFs estimated by repeating the fit with CT18A error sets



- Absolute cross sections sensitive to both free-proton PDFs & nuclear modifications

$$d\sigma = \sum_{i,j} f_i^P(Q_f^2) \otimes d\sigma_{ij}(Q_f^2, Q_r^2) \otimes f_j^{Pb}(Q_f^2)$$

$$f_i^{P/Pb}(x, Q^2) = R_i^{P/Pb}(x, Q^2) f_i^P(x, Q^2)$$

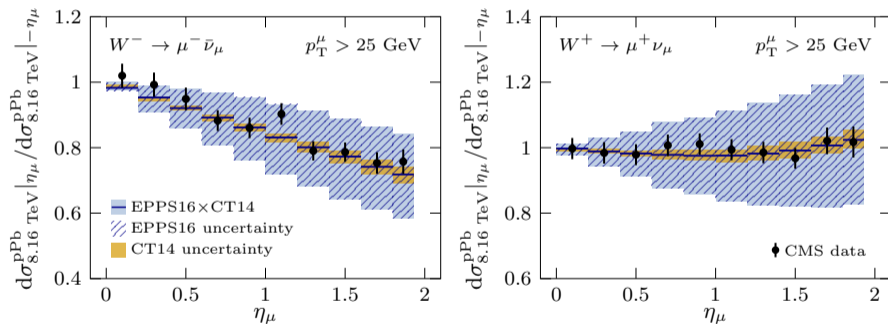


[EUR.PHYS.J.C 82 (2022) 3, 271]

- Proton-PDF uncertainty can exceed the nuclear-PDF uncertainty

- Forward-to-backward ratios

$$\frac{d\sigma^{\text{pPb}}(\eta)}{d\sigma^{\text{pPb}}(-\eta)}$$

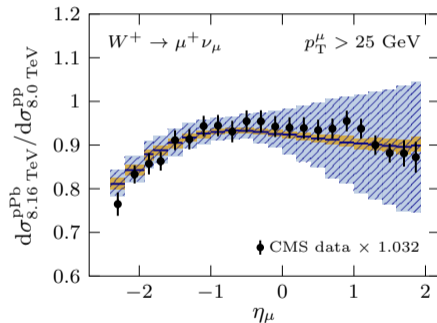
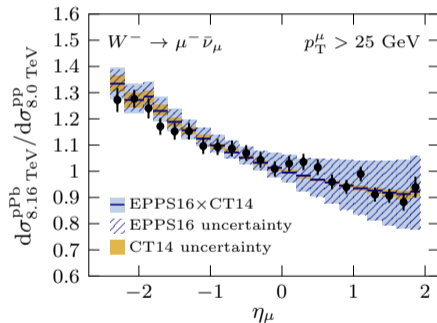


[EUR.PHYS.J.C 82 (2022) 3, 271]

- A good (but not perfect) cancellation of proton uncertainties

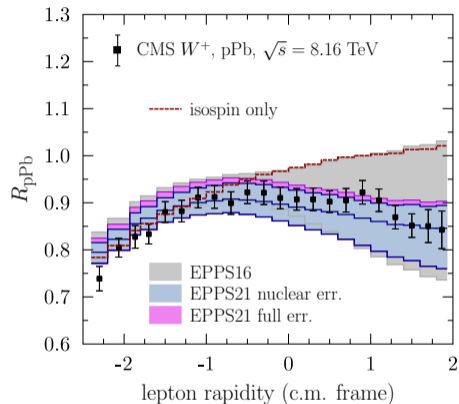
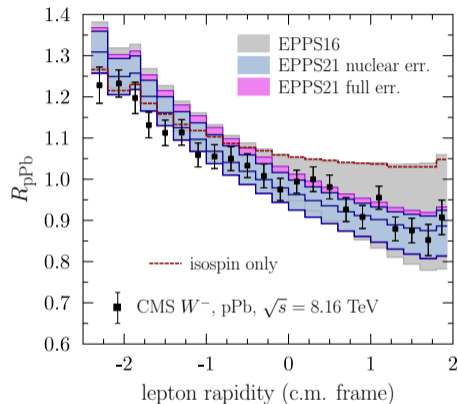
- Ratios of cross sections in p-Pb and p-p

$$\frac{d\sigma^{\text{pPb}}(\eta)}{d\sigma^{\text{pp}}(\eta)}$$



[EUR.PHYS.J.C 82 (2022) 3, 271]

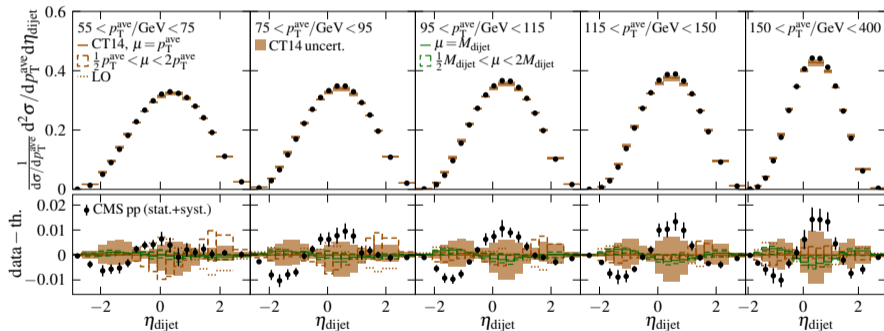
- A good (but not perfect) cancellation of proton uncertainties



- Central values appear to overshoot at backward but still $\chi^2/N_{\text{data}} \approx 0.94$

- A precision jet observable

$$\frac{d^2 \sigma^{\text{PP}}}{dp_{\text{T}}^{\text{ave}} d\eta_{\text{dijet}}} \left(\frac{d\sigma^{\text{PP}}}{dp_{\text{T}}^{\text{ave}}} \right)^{-1}$$

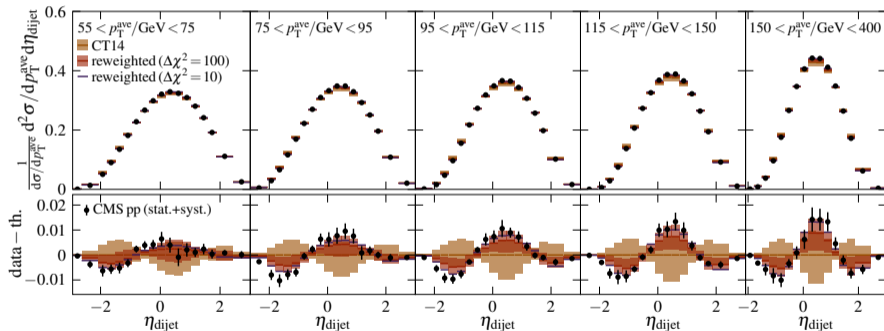


[EUR.PHYS.J.C 79 (2019) 6, 511]

- NLO QCD differs significantly from the data (note: smallish cone $R = 0.3$)

- A precision jet observable

$$\frac{d^2 \sigma^{\text{PP}}}{dp_{\text{T}}^{\text{ave}} d\eta_{\text{dijet}}} \left(\frac{d\sigma^{\text{PP}}}{dp_{\text{T}}^{\text{ave}}} \right)^{-1}$$

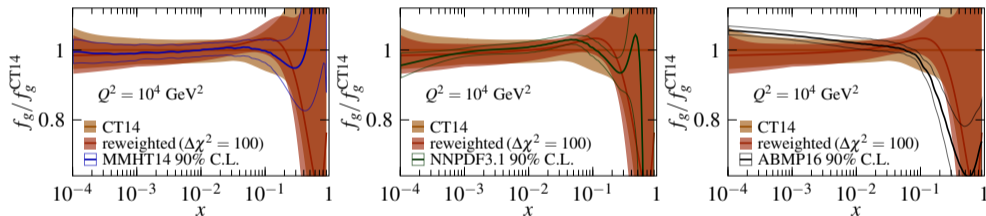


[EUR.PHYS.J.C 79 (2019) 6, 511]

- Can improve the description by Hessian PDF reweighting/profiling

- A precision jet observable

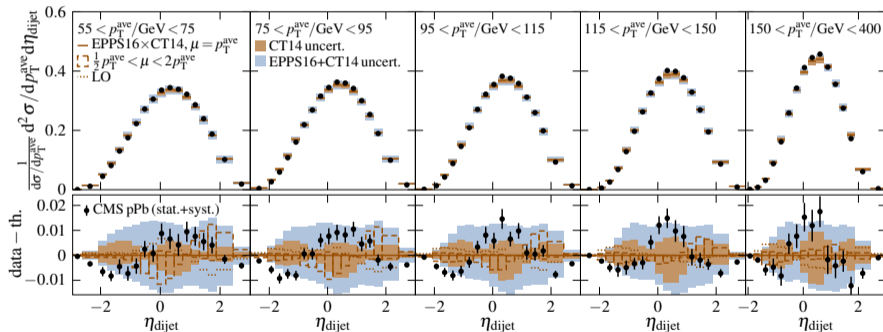
$$\frac{d^2 \sigma^{\text{PP}}}{dp_{\text{T}}^{\text{ave}} d\eta_{\text{dijet}}} \left(\frac{d\sigma^{\text{PP}}}{dp_{\text{T}}^{\text{ave}}} \right)^{-1}$$



- Would require large changes in the CT14 PDFs

- A precision jet observable

$$\frac{d^2 \sigma^{\text{pPb}}}{dp_T^{\text{ave}} d\eta_{\text{dijet}}} \left(\frac{d\sigma^{\text{pPb}}}{dp_T^{\text{ave}}} \right)^{-1}$$

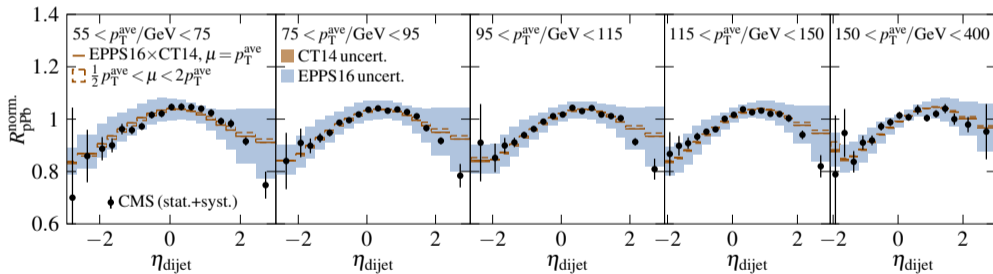


[EUR.PHYS.J.C 79 (2019) 6, 511]

- The p-Pb data show similar differences w.r.t NLO calculation as p-p

- A precision jet observable

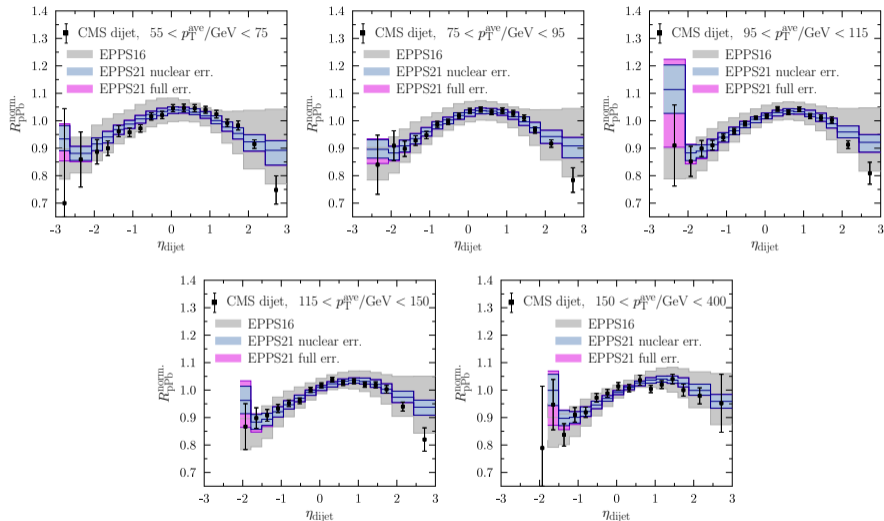
$$\frac{d^2\sigma^{\text{pPb}}}{dp_T^{\text{ave}} d\eta_{\text{dijet}}} \left(\frac{d\sigma^{\text{pPb}}}{dp_T^{\text{ave}}} \right)^{-1} \bigg/ \frac{d^2\sigma^{\text{pp}}}{dp_T^{\text{ave}} d\eta_{\text{dijet}}} \left(\frac{d\sigma^{\text{pp}}}{dp_T^{\text{ave}}} \right)^{-1}$$



[EUR.PHYS.J.C 79 (2019) 6, 511]

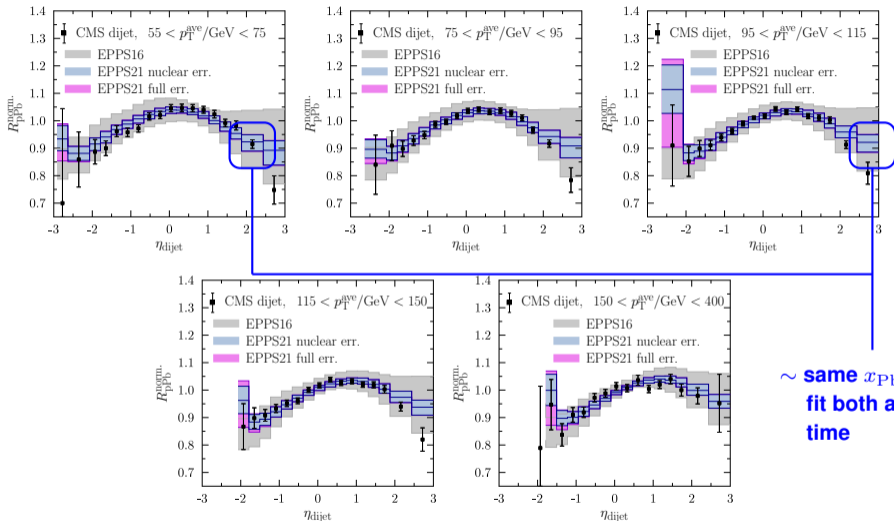
- The ratio p-Pb over p-p compatible with EPPS16

Double-differential dijet data [PHYS.REV.LETT. 121 (2018) 6, 062002]: Comparison with the EPPS21 fit



- Generally a very good agreement except the most forward data points

Double-differential dijet data [PHYS.REV.LETT. 121 (2018) 6, 062002]: Comparison with the EPPS21 fit



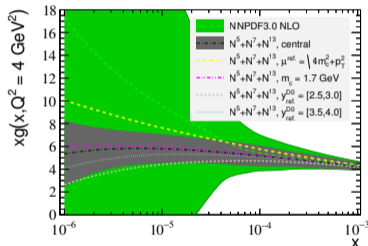
~ same x_{PB} – can't fit both at the same time

- Generally a very good agreement except the most forward data points

Open heavy-flavour measurements promising PDF constraints

- The potential of D (and B) meson production as a PDF constraint has been actively investigated [GAULD, ROJO, PRL 118, 072001 ; PROSA, EPJ C75, 396 ; KUSINA ET.AL. PRL 121,052004]

reduction of NNPDF3.0 gluon uncertainty
upon including LHCb D-meson data



- Theoretical description typically based on fixed-order QCD [Mangano et.al. NP B373, 295], FONLL [CACCIARI ET.AL. JHEP 9805, 007], or Powheg+Pythia [Frixione et.al. JHEP 0709, 126]
- We use a **general-mass variable-flavour-number scheme (GM-VFNS)** approach [KNEIHL ET.AL PRD71, 014018, HELENIUS, PAUKKUNEN, JHEP 1805 (2018) 196]

- The master formula for D-meson production in GM-VFNS:

sum over all
partonic subprocesses

$$\frac{d\sigma(h_1 + h_2 \rightarrow D + X)}{dP_T dY} = \sum_{ijk} \int_{z^{\min}}^1 \frac{dz}{z} \int_{x_1^{\min}}^1 dx_1 \int_{x_2^{\min}}^1 dx_2$$

here $z \equiv E_D/E_k$, but
generally not unique

$f_i^{h_1}(x_1, \mu_{\text{fact}}^2)$

$$\frac{d\hat{\sigma}^{ij \rightarrow k+X}(x_1, x_2, m^2, \mu_{\text{ren}}^2, \mu_{\text{fact}}^2, \mu_{\text{frag}}^2)}{dp_T dy}$$

$f_j^{h_2}(x_2, \mu_{\text{fact}}^2)$

$D_{k \rightarrow D}(z, \mu_{\text{frag}}^2)$

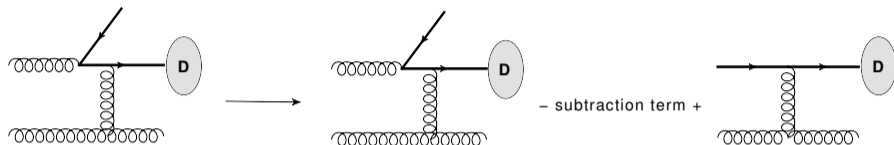
Coefficient functions behave as FFNS at low p_T ,
but as zero-mass $\overline{\text{MS}}$ matrix elements at high p_T

Scale-dependent, universal
fragmentation functions (FFs)

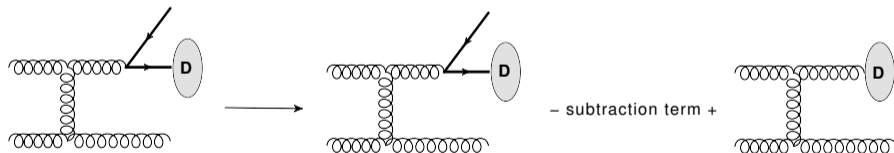
- In comparison, fixed flavour-number scheme (FFNS) produces heavy quarks explicitly in three partonic processes

$$g + g \rightarrow Q + X, \quad q + \bar{q} \rightarrow Q + X, \quad q + g \rightarrow Q + X,$$

- In GM-VFNS the contributions **initiated by heavy-quarks...**



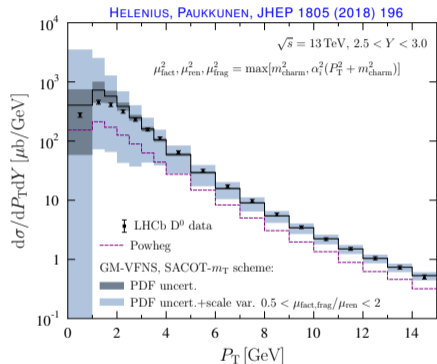
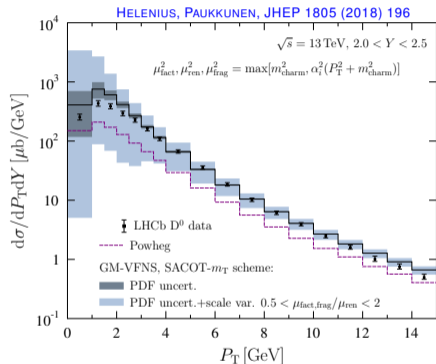
...and those in which a **light quark/gluon fragments** into a D meson...



...are scheme dependent

- We adopt the **SACOT- m_T** scheme [HELENIUS, PAUKKUNEN, JHEP 1805 (2018) 196]

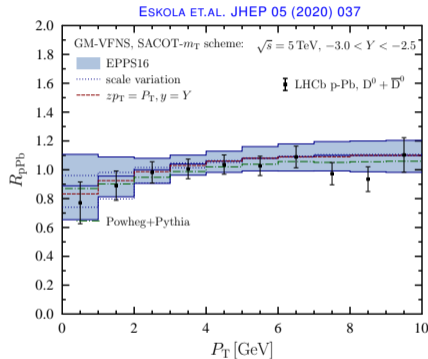
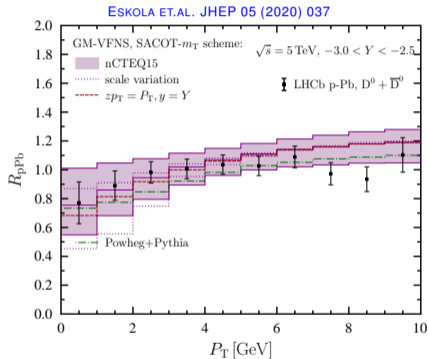
- LHCb p-p cross sections well reproduced by the SACOT- m_T approach



PDF = NNPDF3.1NLO (pch)
FF = KKKS08

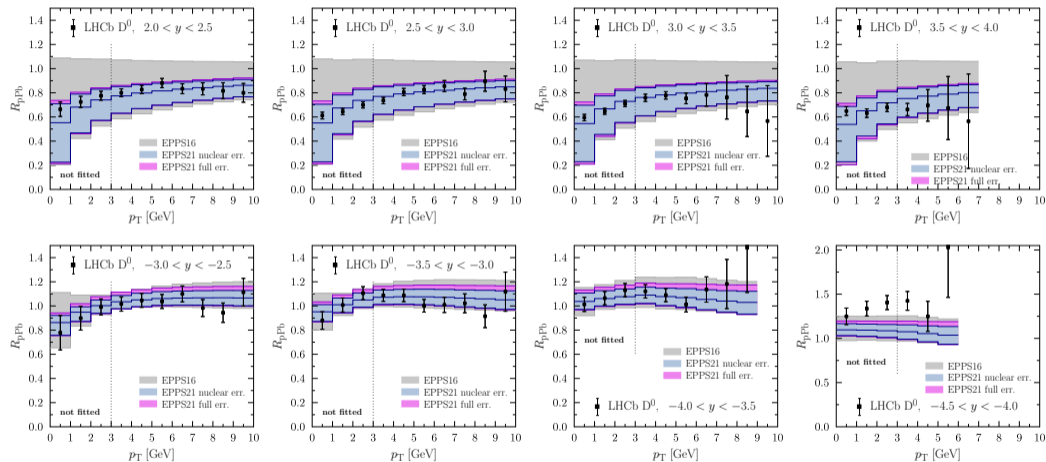
- Sizable theory uncertainties at low p_T : scale-choice and proton-PDF uncertainties shown, but there are others too (scheme dependence, fragmentation,...)

- As an example, LHCb data w.r.t. nCTEQ15 and EPPS16



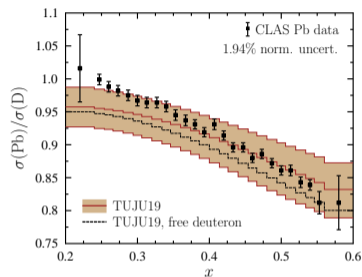
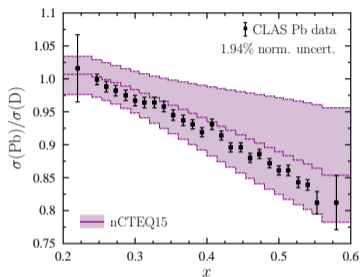
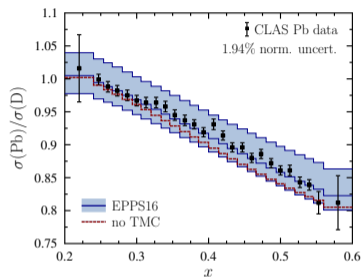
- Uncertainties due to **scale choices** and **fragmentation variable z** in $D_{k \rightarrow D}(z, \mu_{\text{frag}}^2)$ and **proton-PDF uncertainties** grow towards low p_T

The LHCb data [JHEP 10 (2017) 090] σ_{pPb}/σ_{pp} vs. EPPS21



- Good fit across a wide range of rapidity – no sign of e.g. non-linear effects at small- x

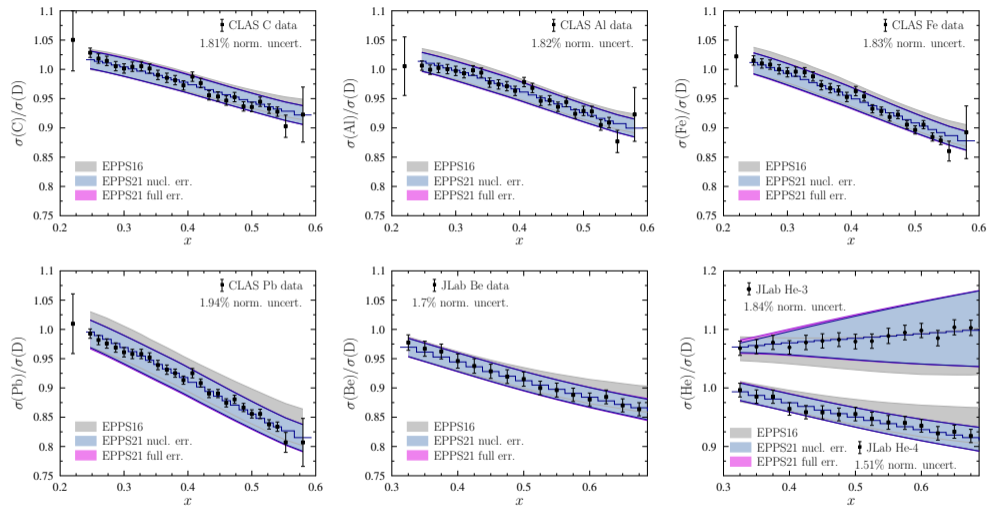
- Probe kinematic region often left out from PDF fits, $1.62 < Q^2/\text{GeV}^2 < 3.37, W \geq 1.8\text{GeV}$



- The **target-mass corrections** matter, essentially $x \rightarrow \xi = \frac{2x}{1 + \sqrt{1 + 4x^2 M_{\text{nucleon}}^2 / Q^2}}$

- No visible A -dependent higher-twist effects = reproduce also data at same x but higher Q^2

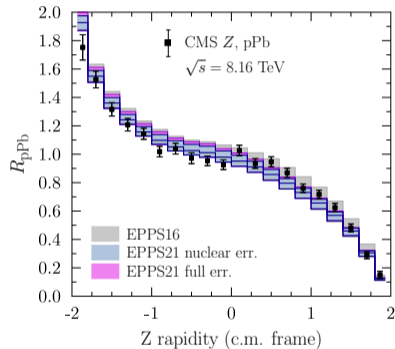
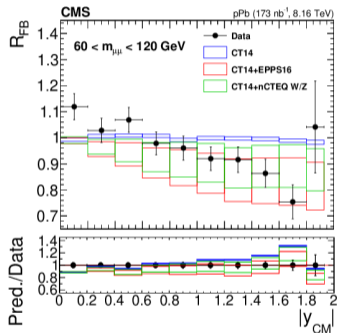
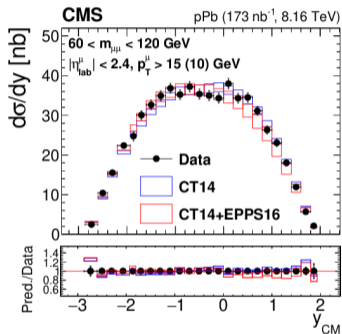
JLab CLAS & Hall-C data vs. the EPPS21 fit



- Good description of the A -systematics from He-3 to Pb-208

The case of CMS p-Pb 8.16 TeV Z-boson production

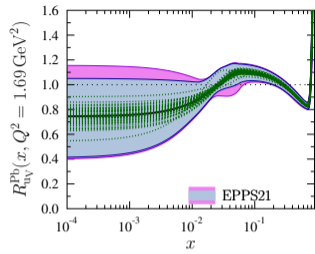
- Precise CMS Z data [JHEP 05 (2021) 182] broadly consistent with nuclear-PDF predictions



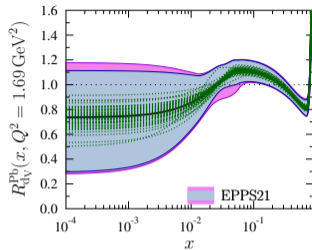
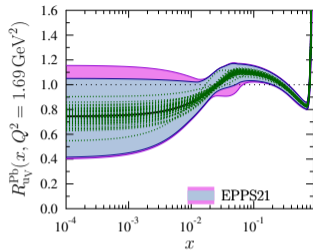
- However, $\chi^2/N_{\text{data}} \sim 2$ – fitting nor NNLO corrections helps here

⇒ **Not included in EPPS21**

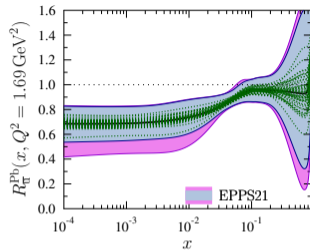
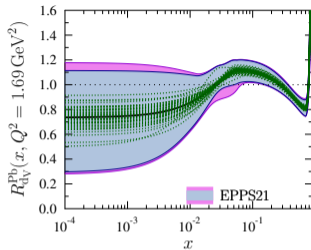
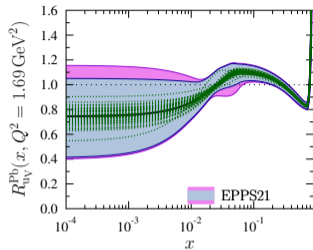
Nuclear modifications $(Z f_i^{\text{p}/A} + N f_i^{\text{n}/A}) / (Z f_i^{\text{p}} + N f_i^{\text{n}})$ for Pb at $Q^2 = m_{\text{charm}}^2$



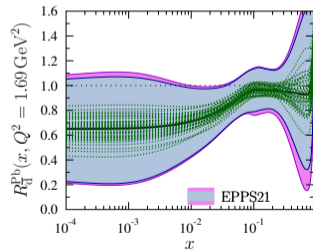
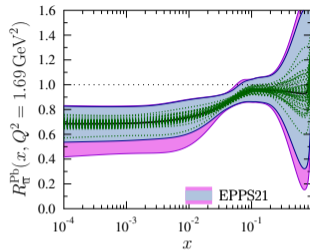
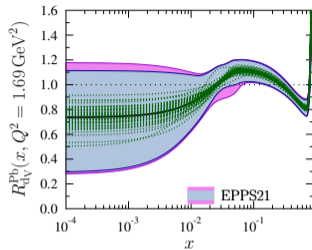
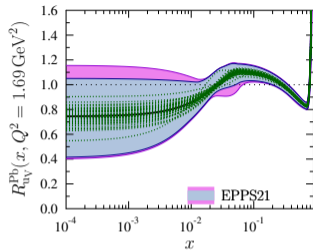
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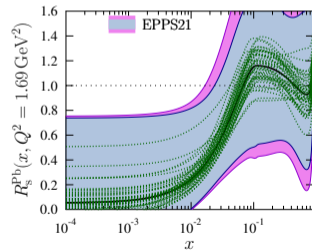
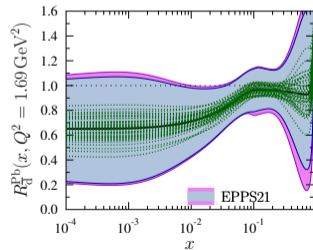
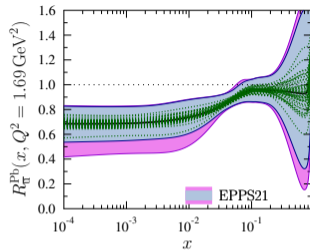
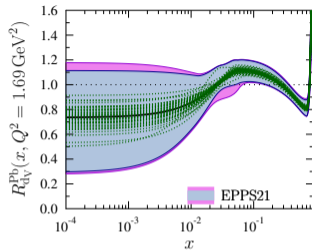
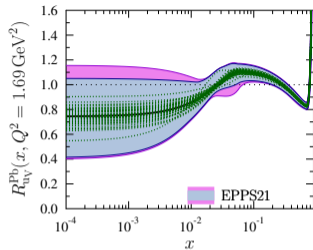
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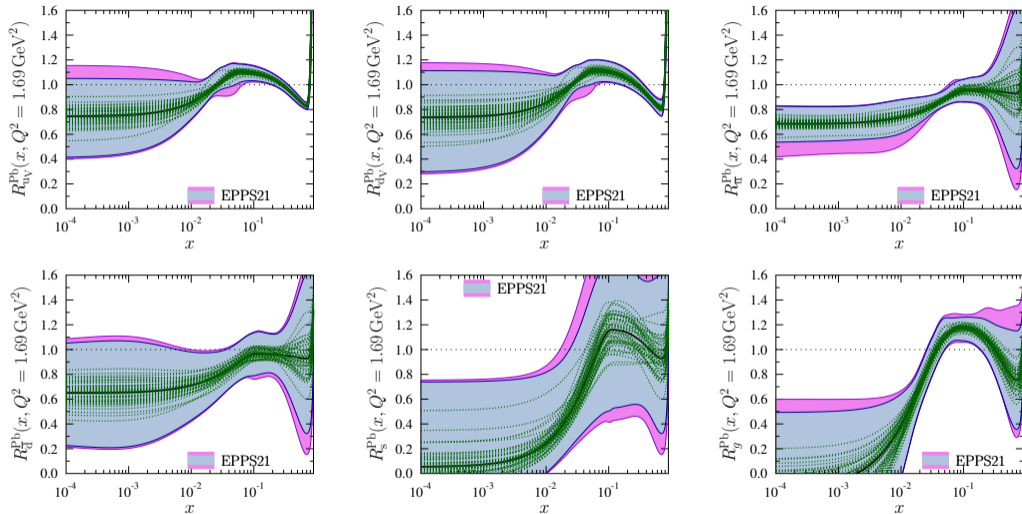
Nuclear modifications $(Z f_i^{p/A} + N f_i^{n/A}) / (Z f_i^p + N f_i^n)$ for Pb at $Q^2 = m_{\text{charm}}^2$



Nuclear modifications $(Z f_i^{p/A} + N f_i^{n/A}) / (Z f_i^p + N f_i^n)$ for Pb at $Q^2 = m_{\text{charm}}^2$

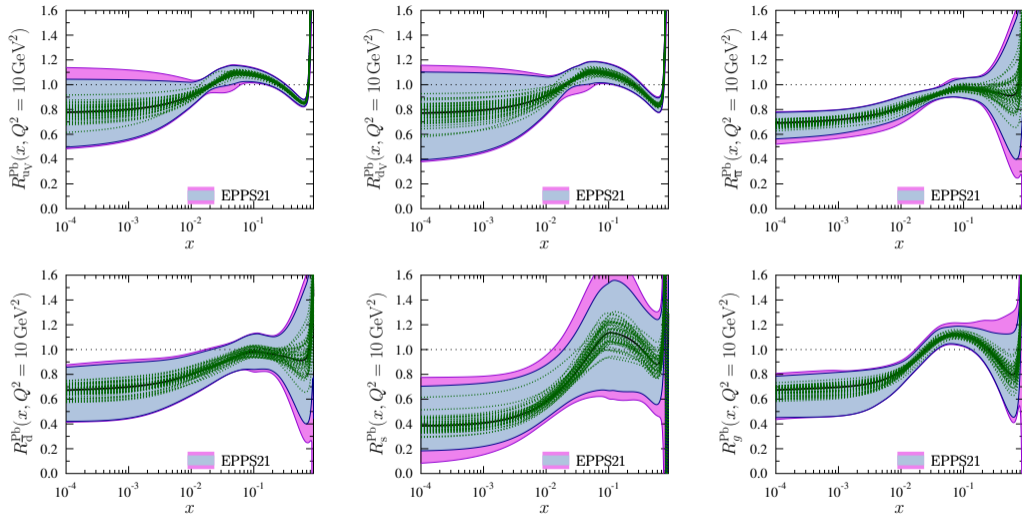


Nuclear modifications $(Z f_i^{p/A} + N f_i^{n/A}) / (Z f_i^p + N f_i^n)$ for Pb at $Q^2 = m_{\text{charm}}^2$



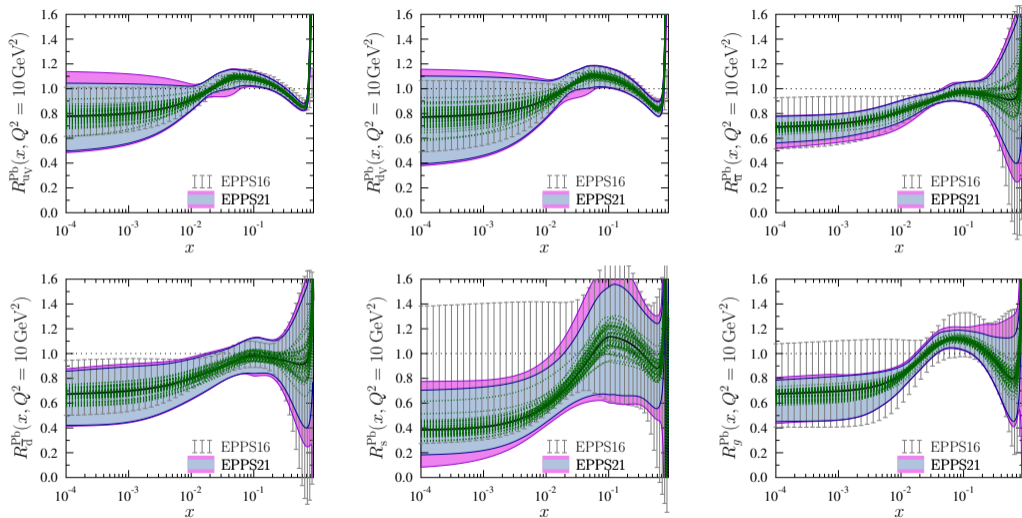
- The free-proton PDF uncertainties typically subdominant in nuclear effects – largest in strangeness

Nuclear modifications $(Z f_i^{p/A} + N f_i^{n/A}) / (Z f_i^p + N f_i^n)$ for Pb at $Q^2 = 10 \text{ GeV}^2$



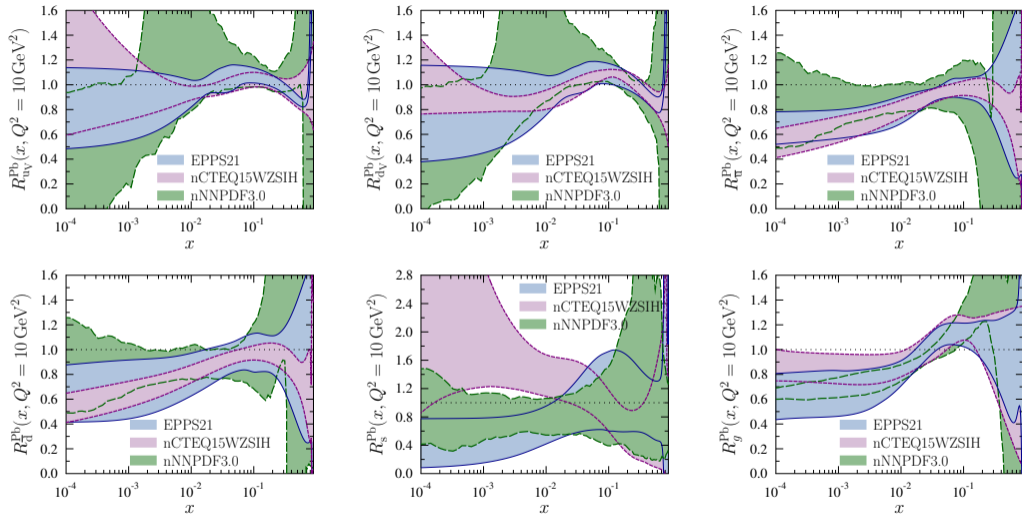
- The free-proton PDF uncertainties typically subdominant in nuclear effects – largest in strangeness

Nuclear modifications Pb at $Q^2 = 10 \text{ GeV}^2$, EPPS16 vs. EPPS21



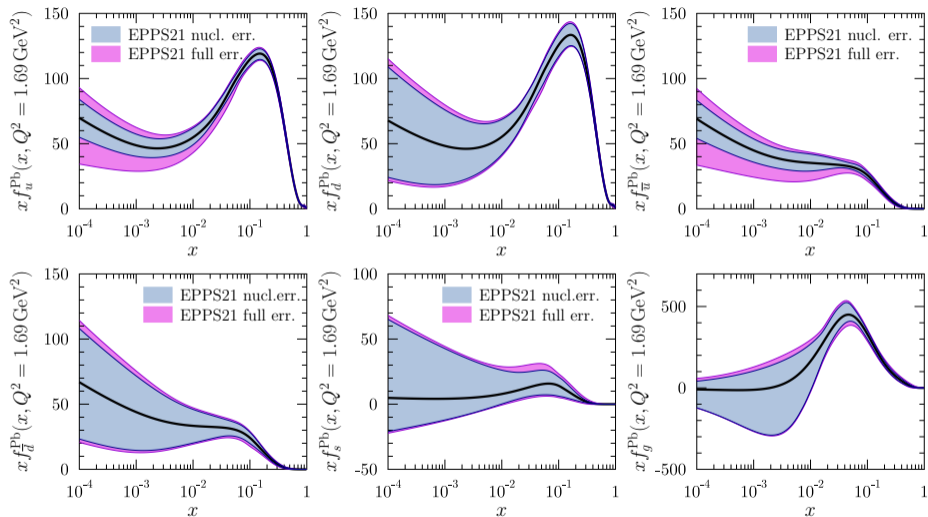
- Largest impact vs. EPPS16 seen in the gluon – strangeness also affected by fit function

Nuclear modifications $(Z f_i^{p/A} + N f_i^{n/A}) / (Z f_i^p + N f_i^n)$ for Pb at $Q^2 = 10 \text{ GeV}^2$

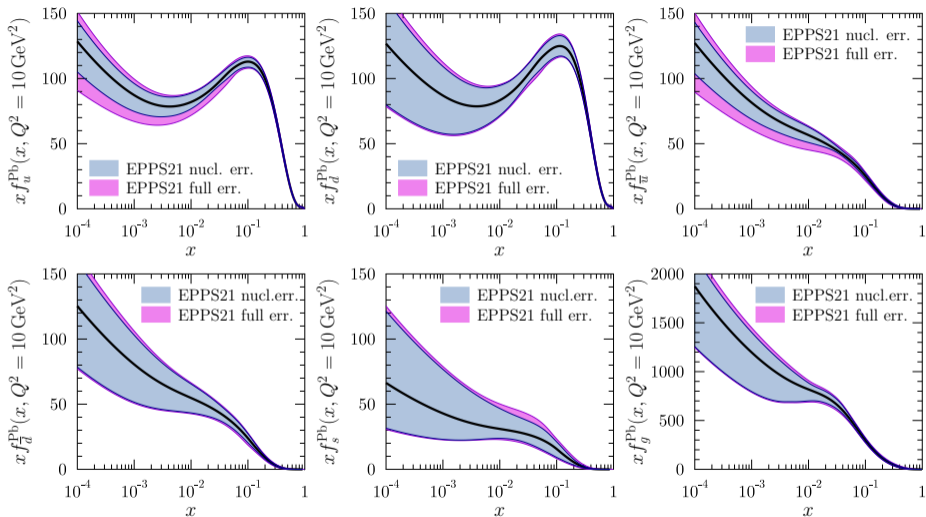


- Broadly mutually consistent – shapes and uncertainties still very different between fits

Absolute nuclear PDFs for Pb at $Q^2 = m_{\text{charm}}^2$

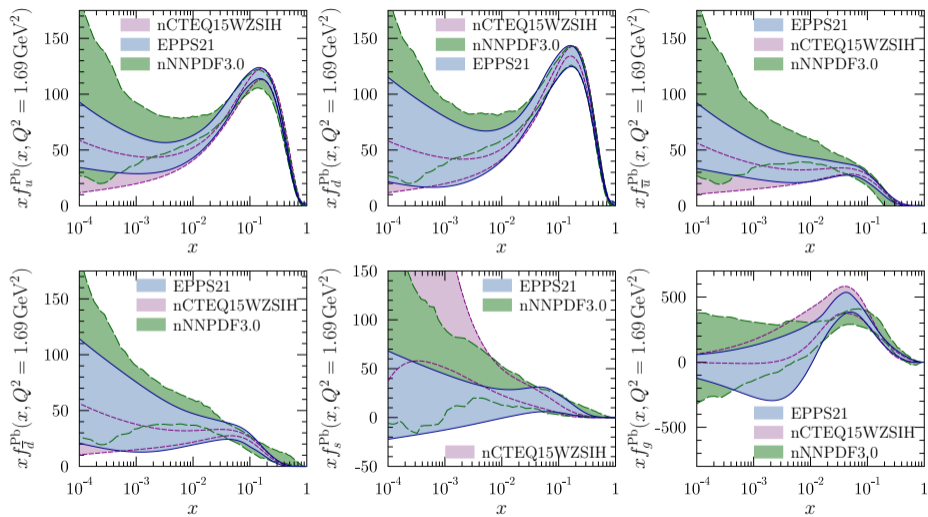


- Free-proton uncertainties visible e.g. in up quarks



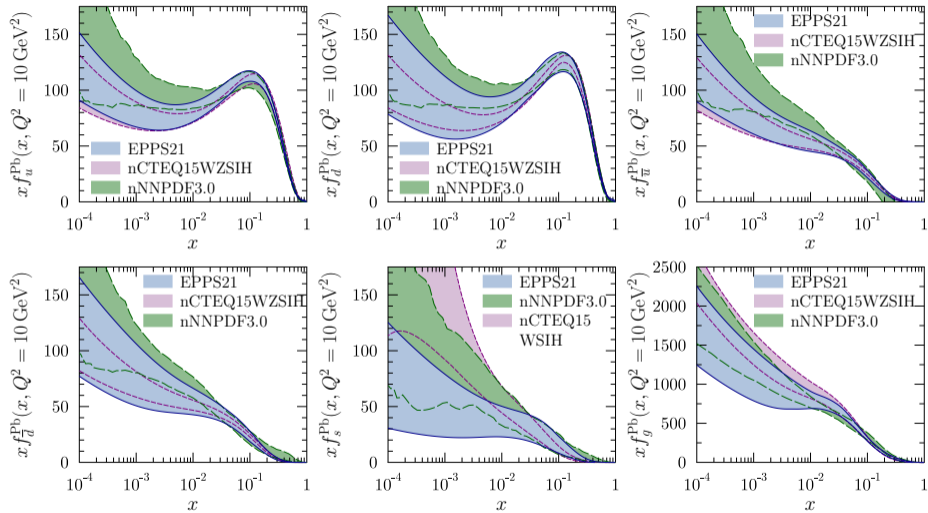
- Free-proton uncertainties visible e.g. in up quarks

Absolute nuclear PDFs at $Q^2 = m_{\text{charm}}^2$, EPPS21 vs. nNNPDF3.0 vs. nCTEQ15WZSIH



- Broadly consistent but “all don’t overlap with all”

Absolute nuclear PDFs at $Q^2 = 10 \text{ GeV}^2$, EPPS21 vs. nNNPDF3.0 vs. nCTEQ15WZSIH



- Broadly consistent but “all don’t overlap with all”

- Outlined the EPPS21 analysis of nuclear PDFs
- The most important developments vs. EPPS16:
 - CMS double diff. dijets
 - LHCb double diff. D mesons \rightsquigarrow constrains for gluons through wide range in x
 - CMS 8 TeV W^\pm
 - JLab large- x DIS data \rightsquigarrow improve the A systematics at large x
 - map correlations with proton PDF \rightsquigarrow more consistent propagation of uncertainties
- More data on the way – NNLO accuracy becoming relevant?
- The LHC p-Pb data begins to be precise enough to seriously test the factorization outside p-p