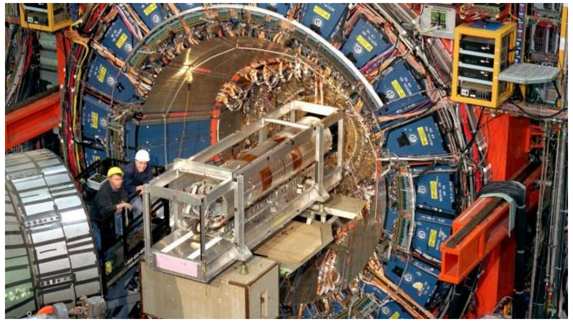
Effect of misalignements on Energy calibration and polarization
Alain Blondel for the EPOL group

-1- The importance of Energy calibration and Polarization
-2- Impact of alignement imperfections on spin motion
depolarization and interference with energy determination
➔ vertical orbit and vertical dispersion
-3- Specific polarization corrections
-- a possible exemple: 2π vertical orbit bumps and harmonic spin matching
-4- Ground motion and need for continuous corrections
-5- Collision effects
-6- List of recommendations as of today

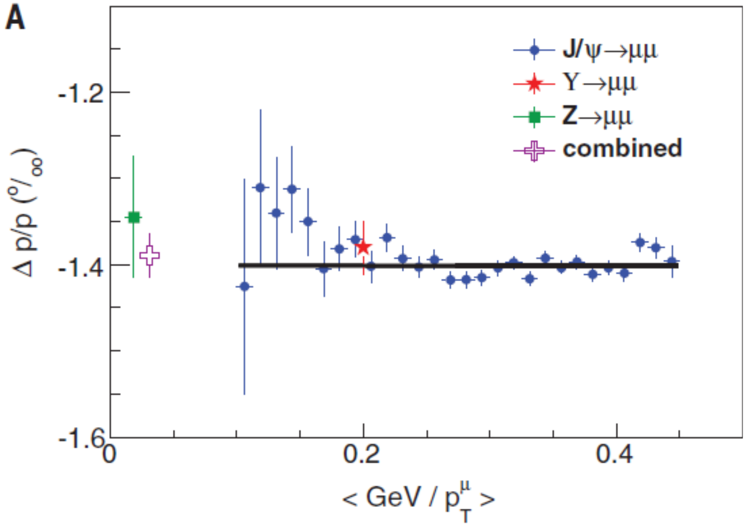
FCC-ee Energy Calibration and Polarization



Recent CDF: m_W (MeV)= 80'433.5 $\pm$ 6.4 $_{stat}$ $\pm$ 6.9$_{syst}$ (10^{-4} precision)
-- « could hint at new physics » and surely created a buzz!
-- precision measurements as broad exploration of new physics in quantum corrections, or mixing (SUSY, Heavy neutrinos, etc..)
(-- questions because inconsistent with previous measurements)

CDF measurement is remarkable in two ways:
1. (after 10 years of work)
systematic errors similar to statistical precision

2. relies for the precise calibration on J/ψ, Υ, Z masses
all measured in e+e- colliders...
using resonant depolarization!



Resonant depolarization is the cornerstone of the precision programme of FCC-ee

~40 times more precise than CDF

➔ Improvement by factor 10-1000 on a long list of precision measurements.
e.g. W mass down to ±250 keV, Z mass and width ±4 keV, $\sin^2\theta_W$ ^{eff} $\pm$ 2.10^{-6} etc..
➔ explore new physics at 10-100 TeV scale, or 10^{-5} mixing with known particles.

factor 500 more precise than LEP

First set of results obtained in the FCC Design Study:

Polarization and Centre-of-mass Energy Calibration at FCC-ee, arXiv:1909.12245

Table 15: Calculated uncertainties on the quantities most affected by the center-of-mass energy uncertainties, under the final systematic assumptions.

Quantity	statistics	ΔE_{CMabs} 100 keV	$\Delta E_{CMSyst-ptp}$ **40 keV**	calib. stats. $200\ keV/\sqrt{(N^i)}$	σE_{CM} (84) $\pm$ **0.05** MeV	stat/present
m_Z (keV)	**4**	100	**28**	1	–	500
Γ_Z (keV)	**4**	2.5	**22**	1	**10**	400
$sin^2\theta_W^{eff} \times 10^6$ from $A_{FB}^{\mu\mu}$	**2**	–	**2.4**	0.1	–	75
$\frac{\Delta\alpha_{QED}(M_Z)}{\alpha_{QED}(M_Z)} \times 10^5$	**3**	0.1	**0.9**	–	**0.05**	15 (qualitiative!)
m_W(MeV)	**0.250**	-- 0.300 --				25

Next challenges for the feasibility study.

-- Ascertain the above with integrated simulations

-- Match systematic errors with statistics.

most relevant errors : **the point-to-point systematics**

– these are effects that would lead to a deviation from relation between

-- the spin tune as measured by resonant depolarization

-- and the center-of-mass energy.

-- examples: 1. interference between depoarizing resonances and the induced depolarizing resonance because the spin tune varies with energy.

2. effects due to collision offsets folded by opposite sign dispersion

targets and procedures

1. Center-of-mass energy precision of < $\pm$ 100 keV (<10 keV ptp) around the Z peak
2. Center-of-mass energy precision of < $\pm$ 200 keV at W pair threshold
3. For the Z peak-cross-section and width, require energy spread uncertainty $\Delta\sigma_E/\sigma_E$ =0.2%

NB: at 2.3 10^{36}/cm^2/s/IP : **full LEP statistics** 10^6 $\mu\mu$ 2.10^7 qq in **6 minutes** in each expt

determine energy spread and boost of ECM → beam and beamstrahlung energy loss

-- use resonant depolarization as main measuring method

-- use pilot bunches to calibrate during physics data taking: 100 calibrations per day each 10^{-6} rel.

-- long lifetime at Z requires the use of wigglers at beginning of fills

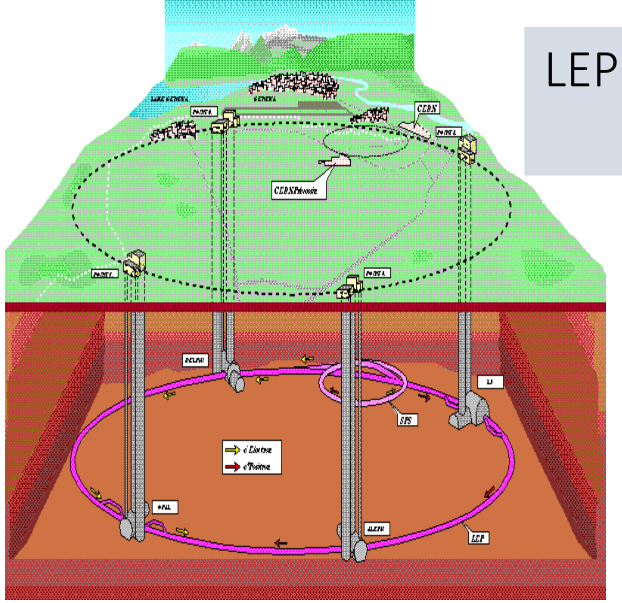
→ take data at points where self-polarization is expected

$$\nu_s = \frac{g-2}{2}\frac{E_b}{m_e} = \frac{E_b}{0.4406486(1)} \approx N + (0.5 \pm 0.1)$$

$$E_{CM} = \left(N + (0.5 \pm 0.1)\right) \text{ x } 0.8812972 \text{ GeV}$$

Given the Z and W widths of 2 GeV, this is easy to accommodate with little loss of statistics.

It might be more difficult for the Higgs 125.09+-0.2 corresponds to ν_s = 141.94+-022



LEP (1989-2000) first observation of $P_\perp$ in 1990
first resonant depolarization in 1991

$$\tau_p = \left(\frac{5\sqrt{3}}{8} \frac{\hbar r_e E_{beam}^5}{m_e^6 \rho^3} \right)^{-1}$$

= ~5 hours at LEP
but **at FCC-ee**
~256 hrs at Z pole
~14 hrs at WW thresh.
10% of that time for P=9%

$$P_\infty = 0.924 \times \frac{1}{1+\frac{\tau_p}{\tau_d}} \qquad \frac{1}{\tau_p} \propto \sum_j |B_j|^3 L_j$$

$$\tau_p^{eff} = \tau_p \times \frac{1}{1+\frac{\tau_p}{\tau_d}} . \qquad \frac{1}{\tau_d} \propto \sum_j |B_j|^3 L_j \frac{11}{18}|\Gamma_j|^2$$

Derbenev-Kondratenko
« spin-orbit coupling
= dependence of equilibrium
« spin » on particle energy

$$\nu = a_e \gamma = \frac{g_e - 2}{2} \frac{E_{Beam}}{m_e c^2} = \frac{E_{Beam}}{0.4406486(1)}$$

Spin tune at the Z peak : 103.5
The scan points 99.5 / 103.5 / 106.5 are perfect optimum for Z width and α_{QED} meast
Spin tune for W threshold 183.5

$$\frac{1}{\tau_p} \propto \sum_j |\mathbf{B}_j|^3 L_j \propto I_3,$$

can be improved by increasing the sum of |B|^3 (Wigglers)

$$\frac{1}{\tau_d} \propto \sum_j \frac{11}{18} |\mathbf{B}_j|^3 L_j |\Gamma_j|^2.$$

can be improved by 'spin matching'

the sources of depolarization can be separated into harmonics (the integer resonances) and/or into the components of motion:

horizontal betatron: $|\Gamma_x|^2 \propto \delta\eta^2\, \delta \mathbf{n}^2$

vertical betatron: $|\Gamma_y|^2 \propto \delta\eta^2,$

synchrotron: $|\Gamma_z|^2 \propto A\delta\eta^2 + B\delta\mathbf{n}^2,$

$\delta\eta$ vertical dispersion

δn average angle between 'closed orbit spin' and magnetic field

recipes:

-- reduce the emittance (esp. ε_y) and vertical dispersion $\delta\eta$

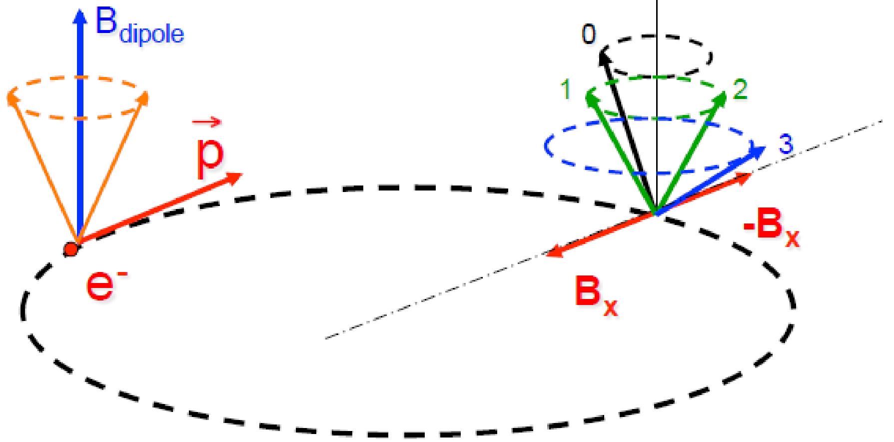
→ this is the same as for luminosity optimization!

-- reduce the vertical spin motion δn →harmonic spin matching

-- do not increase the energy spread

SPIN PRECESSION

RESONANT DEPOLARIZATION



(ν is the *spin tune*)

$\delta\theta_{spin}$ = (g-2)/2 . $E_{beam}/m_e\ \delta\theta_{trajectory}$

$\delta\theta_{spin} = \nu \cdot \delta\theta_{trajectory}$

ν = E_{beam} / 0.4406486

ν = 103.5 at the Z peak

AMPLIFICATION

➔ high precision

➔ sensitivity to misalignements

-- depolarization

-- spurious spin resonances

Once the beams are polarized, an RF kicker at the spin precession frequency (fractional part thereof) will provoke a spin rotation and depolarization

Simulation of FCC-ee by I. Kopp:

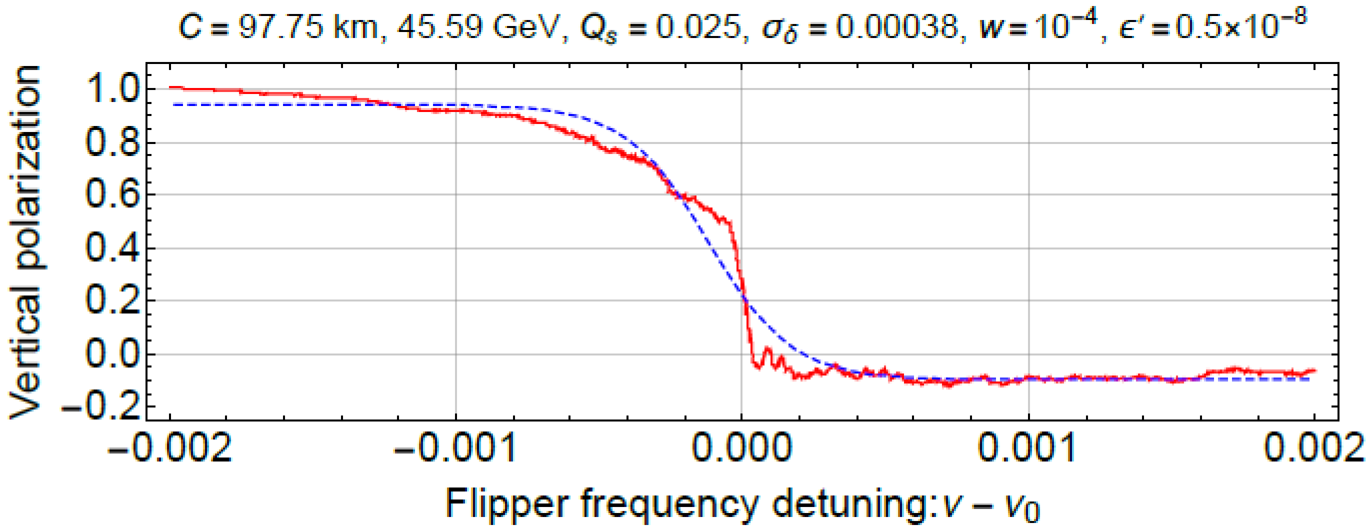
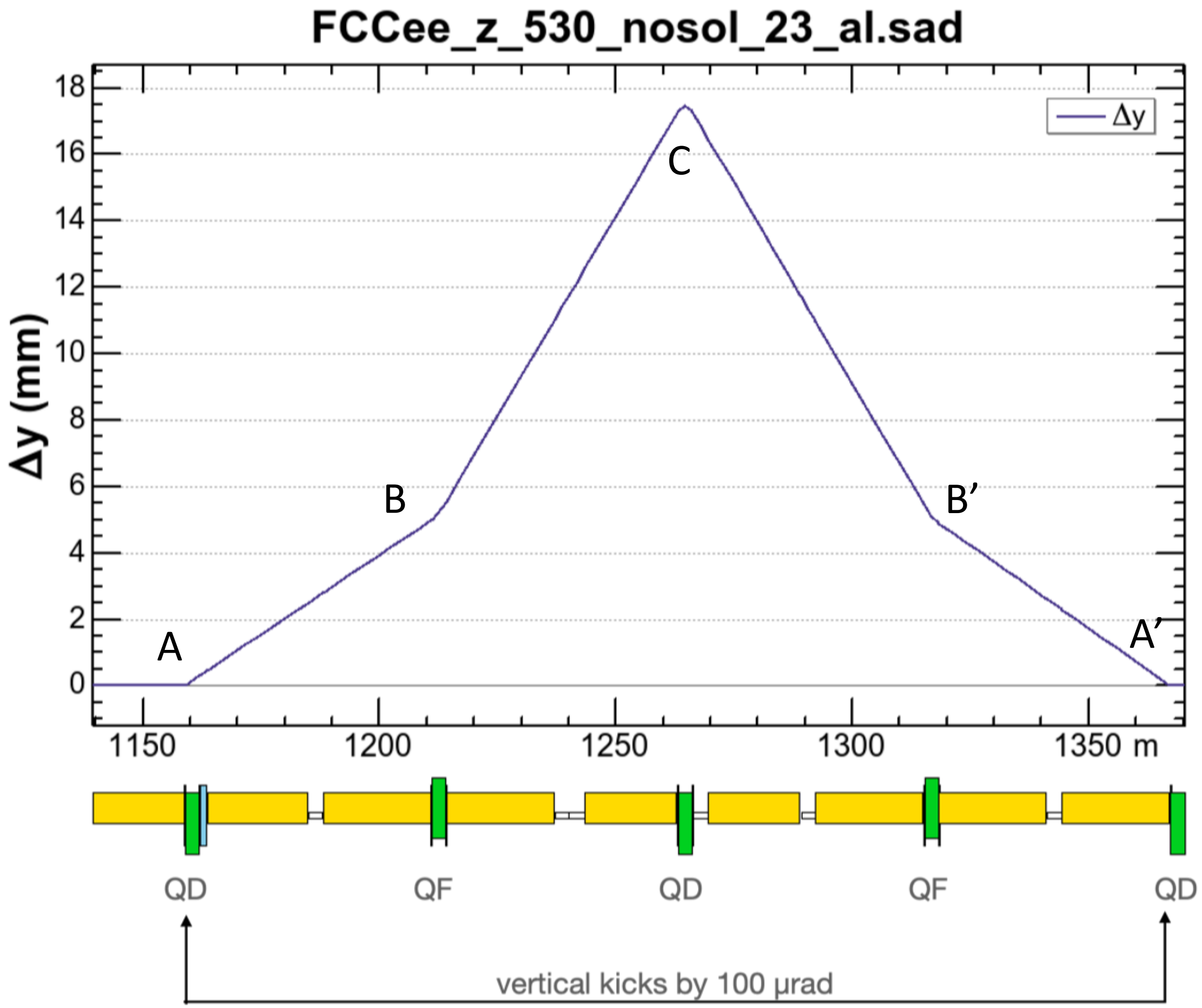
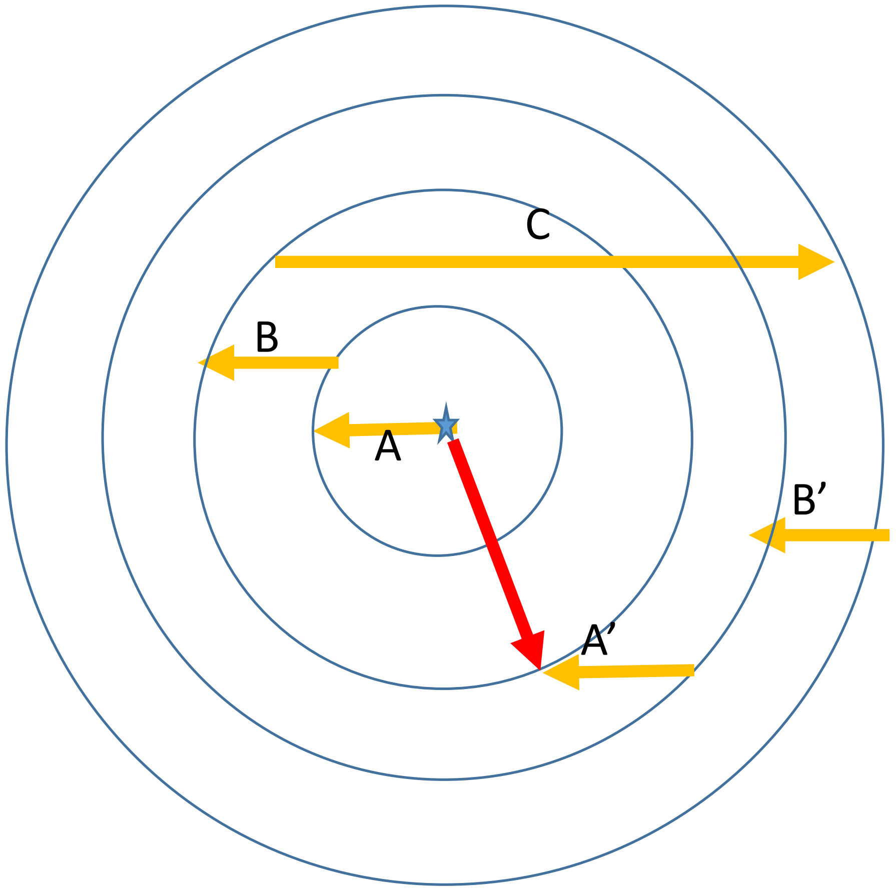


Figure 39. Simulation of a frequency sweep with the depolarizer on the Z pole showing a very sharp depolarization at the exact spin tune value.

Effect of a pi bump on spin at the Z

Large effect, relatively easy correction.





the pi bump generates a spin component rotation of the spin in the x-z direction. The largest rotation is created by the QD quadrupole (focus in vertical plane)

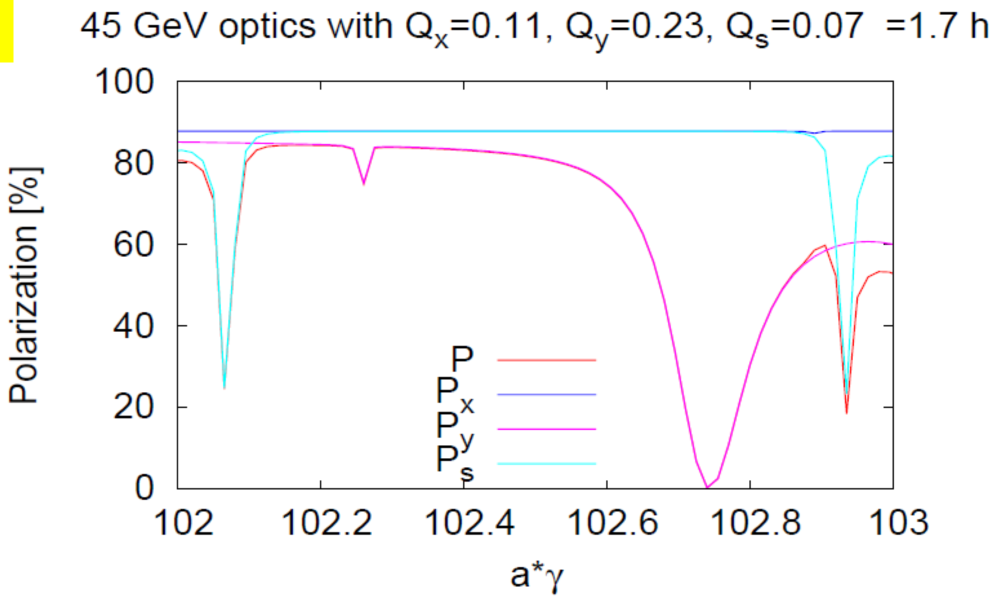
100 microrad orbit kick gets compensated by the pi bump but generates a lasting **25 mrad spin kick**

Simulations of self-polarization

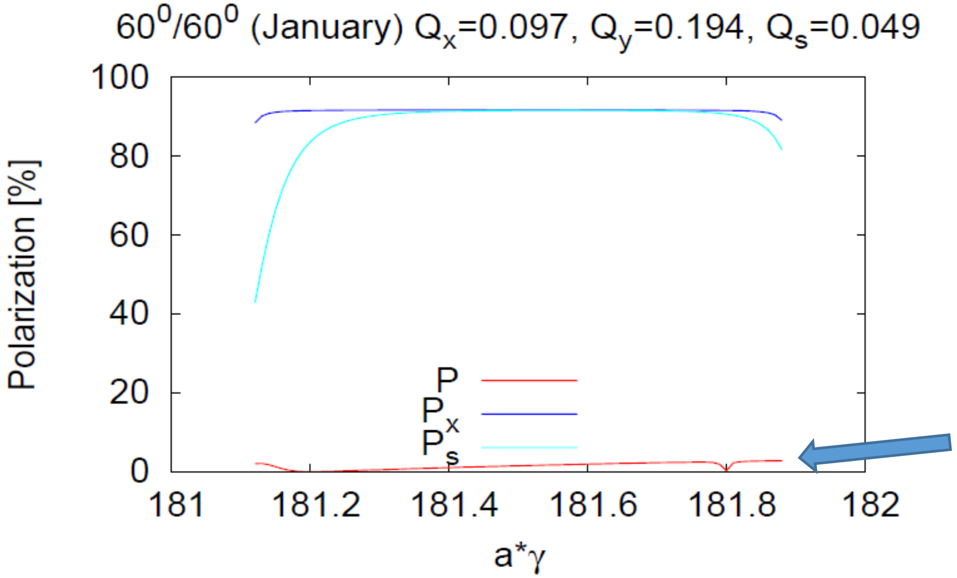
Orbit correction leading to similar values for <u>vertical dispersion</u> and <u>vertical emittance</u> than for the luminosity optimization

E. Gianfelice
arXiv:1909.12245

@ Z



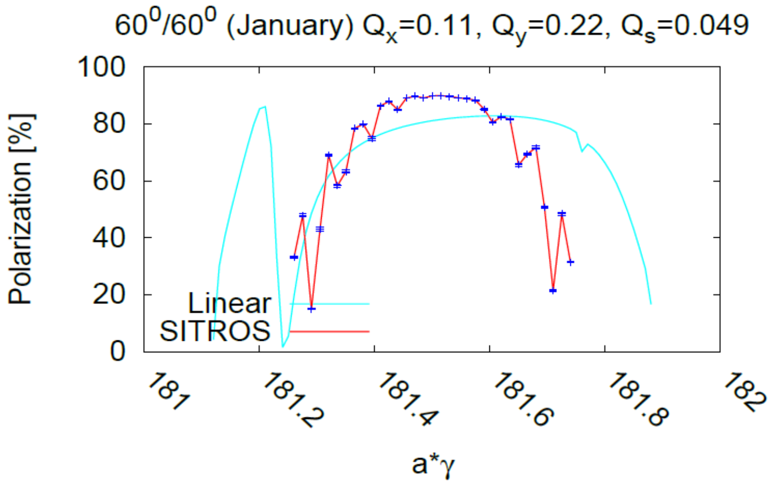
@WW



significant impact of spin resonance from vertical orbit @Z

It might kill polarization completely @W

-- Sufficient level of polarization at Z for machine that is optimized for luminosity.
-- Additional correction of dispersion and harmonic spin matching is necessary at W
-- Effect of resonant depolarization vs beam energy unknown
-- These studies will be repeated with simulation on same machine of lumi/polarization



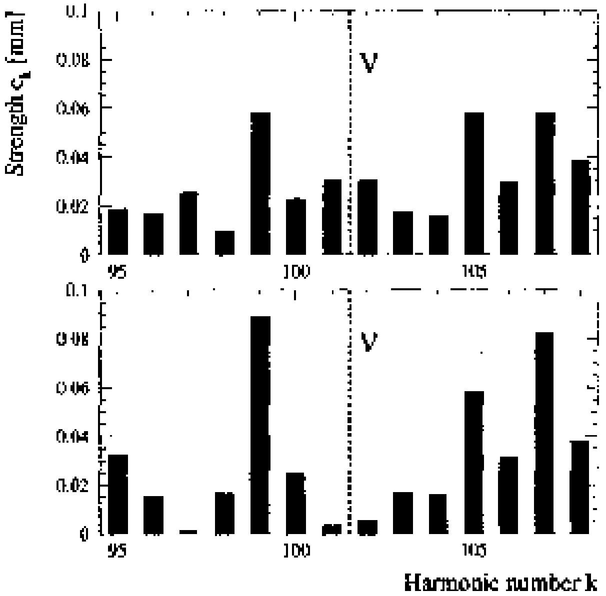
From resonant depolarization to Center-of-mass energy
- from spin tune to beam energy--

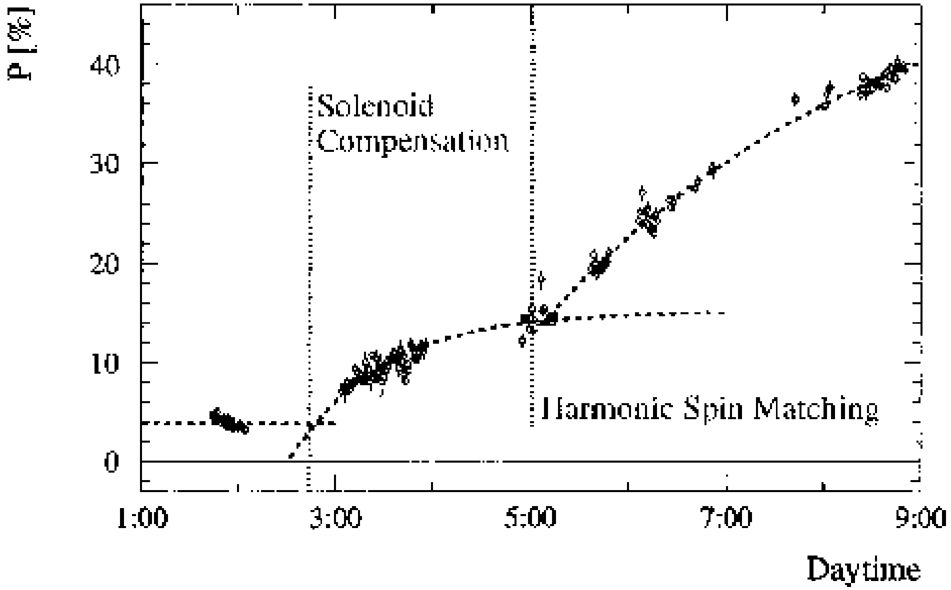
The spin tune may not be en exact measurement of the average of the beam energy along the magnetic trajectory of particles. Additional spin rotations may bias the issue. *Anton Bogomyagkov* and *Eliana Gianfelice* have made many estimates.

synchrotron oscillations	$\Delta E/E$	$-2\ 10^{-14}$
Energy dependent momentum compaction	$\Delta E/E$	10^{-7}
Solenoid compensation		$2\ 10^{-11}$
Horizontal betatron oscillations	$\Delta E/E$	$2.5\ 10^{-7}$
Horizontal correctors*)	$\Delta E/E$	$2.5\ 10^{-7}$
Vertical betatron oscillations **)	$\Delta E/E$	$2.5\ 10^{-7}$
Uncertainty in chromaticity correction $O(10^{-6})$	$\Delta E/E$	$5\ \ 10^{-8}$
invariant mass shift due to beam potential		$4\ 10^{-10}$

*) $2.5\ 10^{-6}$ if horizontal orbit change by >0.8mm between calibration is unnoticed
or if quadrupole stability worse than 5 microns over that time. consider that 0.2 mm orbit will be noticed
**) $2.5\ 10^{-6}$ for vertical excursion of 1mm. Consider orbit can be corrected better than 0.3 mm.

examples of harmonic spin matching (I)





Deterministic Harmonic spin matching :
measure orbit, decompose in harmonics, cancel components near to spin tune.
☺ NO FIDDLING AROUND.
This worked very well at LEP-Z
 and should work even better at FCC-ee-Z,W if orbit is measured better.

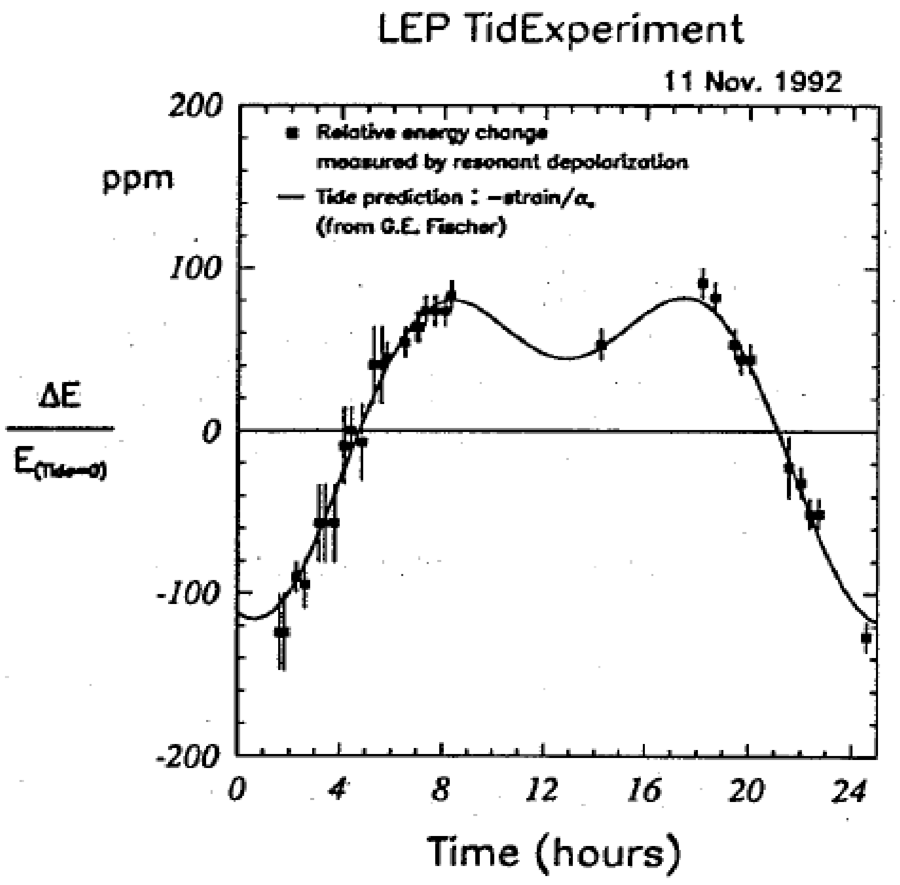


Figure 23: Beam energy variations measured over 24 hours compared to the expectation from the tidal LEP deformation.

ground motion (here earth tides) affects the beam energy by changing the ring circumference against a given RF frequency.

-- Tides can be calculated
-- The effect can be seen in the BPMs
-- the effect corresponds to a swing of up to +- 120 MeV in 6 hours at the Z pole! At max rate almost 1MeV/minute needs correction at that level for ee->H experiment

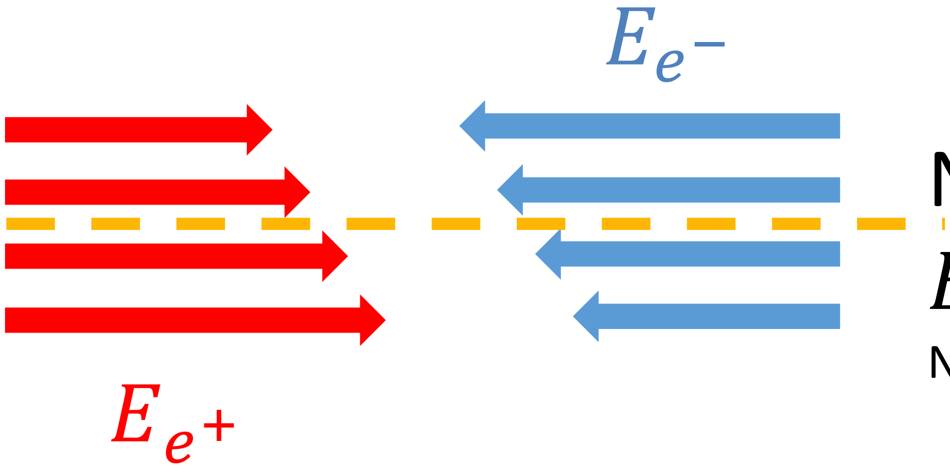
Other sources of motion: Geneva lake level, rain or snow on mountains, etc have been observed, at longer time scales.

This must be corrected at appropriate intervals by varying the RF frequency or by other methods

Such variations must be carefully recorded and the records organized on a long lasting data base: these parameters enter the centre-of-mass determination and will in fine be part of the physics results

From resonant depolarization to center-of-mass energy
from beam energy to E_{CM}

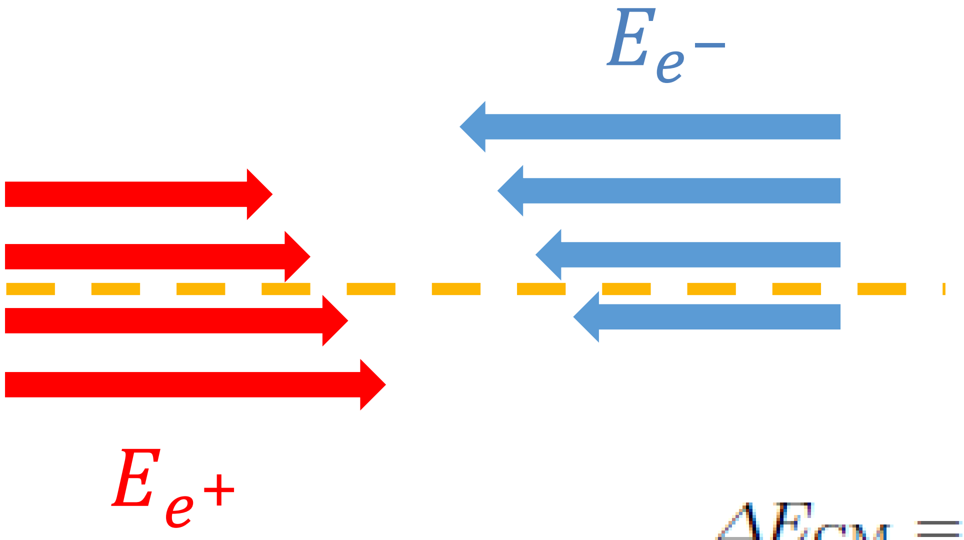
opposite sign dispersion



No effect.

$$ECM = (E_{e^+} + E_{e^-})$$

NB energy spread is reduced.



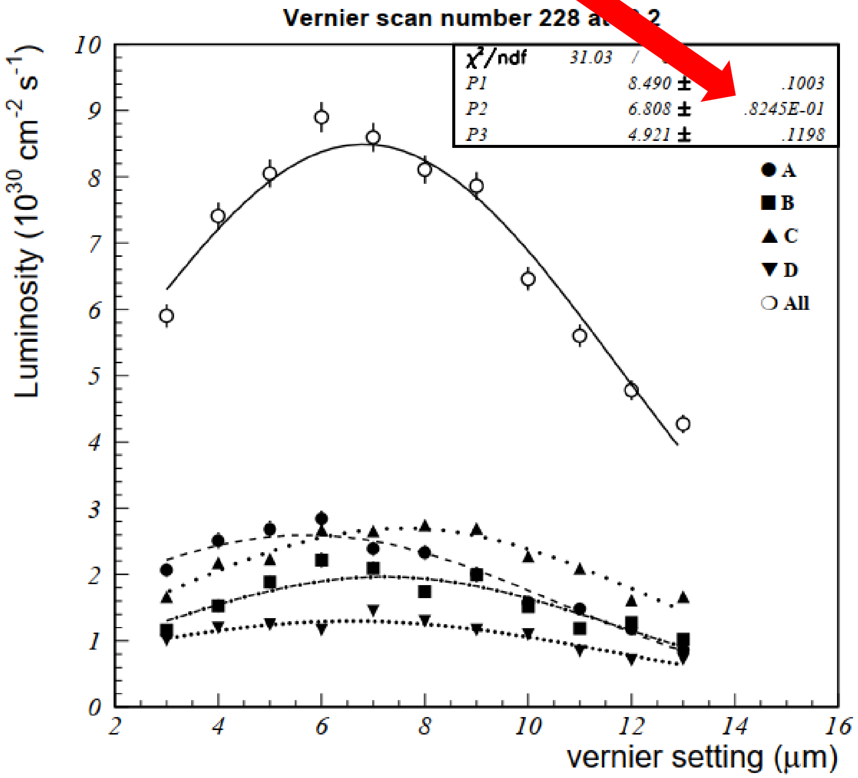
ECM lower than $(E_{e^+} + E_{e^-})$

$$\Delta E_{\mathrm{CM}} = -\frac{1}{2} \cdot \frac{\delta y}{\sigma_y^2} \cdot \frac{\sigma_{E_b^2}}{E_b} \cdot \Delta D_y^*$$

Experience from LEP – Vernier scans

Van Der Meer today

Relative position of beams measured to 80 nanometers from one scan



Recommandations

0. the running mode at Z and WW (and even more for ee-> H) will involve important activity for ECM calibration

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1. The measurements and corrections of vertical orbit and vertical dispersion are crucial
2. they should be available for pilot bunches (<10^{10} e+/e- /bunch, short bunches) as well as for lumi bunches
3. spin correction bumps should be foreseen (e.g. two pi-bumps in the arcs in 8 locations (2 around each IP))
4. Ground motion should be corrected regularly (minutes) by RF changes or otherwise
5. correction and monitoring of collision offsets and opposite sign dispersion should be devised

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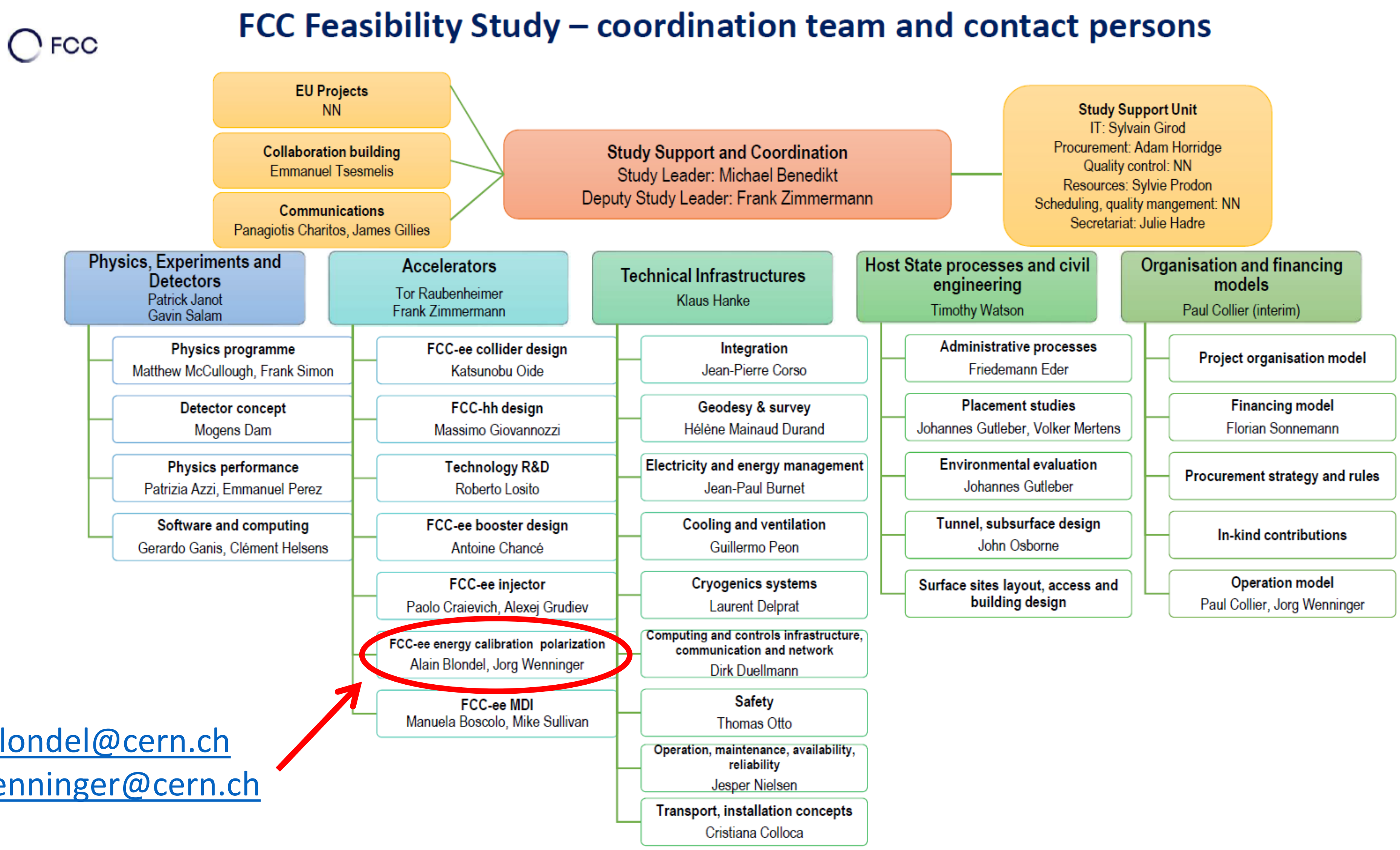
6. finally since this the ECM calibration will enter the physics results of experiments **directly,**

➔ **careful and continuous monitoring and logging of all relevant parameters should be foreseen**

FCC-ee feasibility study



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statistical precision at the Z

centre-of-mass energy errors:

$$\frac{\Delta m_Z}{m_Z} = \left\{\frac{\Delta\sqrt{s}}{\sqrt{s}}\right\}_{\rm abs} \oplus \left\{\frac{\Delta(\sqrt{s_+}+\sqrt{s_-})}{\sqrt{s_+}+\sqrt{s_-}}\right\}_{\rm ptp-syst} \oplus_i \left\{\frac{\Delta\sqrt{s^i_\pm}}{\sqrt{s^i_\pm N^i_\pm}}\right\}_{\rm sampling},$$

$$\frac{\Delta\Gamma_Z}{\Gamma_Z} = \left\{\frac{\Delta\sqrt{s}}{\sqrt{s}}\right\}_{\rm abs} \oplus \left\{\frac{\Delta(\sqrt{s_+}-\sqrt{s_-})}{\sqrt{s_+}-\sqrt{s_-}}\right\}_{\rm ptp-syst} \oplus_i \left\{\frac{\Delta\sqrt{s^i_\pm}}{\sqrt{s^i_\pm N^i_\pm}}\right\}_{\rm sampling},$$

$$\Delta A_{\rm FB}^{\mu\mu}({\rm pole}) = \frac{\partial A_{\rm FB}^{\mu\mu}}{\partial\sqrt{s}}\{\Delta(\sqrt{s_0}-0.5(\sqrt{s_+}+\sqrt{s_-}))\}_{\rm ptp-syst} \oplus_i \frac{\partial A_{\rm FB}^{\mu\mu}}{\partial\sqrt{s}}\left\{\frac{\Delta\sqrt{s^i_{0,\pm}}}{\sqrt{N^i_{0,\pm}}}\right\}_{\rm sampling},$$

$$\frac{\Delta\alpha_{\rm QED}(m_Z^2)}{\alpha_{\rm QED}(m_Z^2)} = \left\{\frac{\Delta\sqrt{s}}{\sqrt{s}}\right\}_{\rm abs} \oplus \left\{\frac{\Delta(\sqrt{s_+}-\sqrt{s_-})}{\sqrt{s_+}-\sqrt{s_-}}\right\}_{\rm ptp-syst} \oplus_i \left\{\frac{\Delta\sqrt{s^i_\pm}}{\sqrt{s^i_\pm N^i_\pm}}\right\}_{\rm sampling}, \quad (3.1)$$

with $\frac{\partial A_{\rm FB}^{\mu\mu}}{\partial\sqrt{s}} \simeq 0.09/{\rm GeV}$.

Three categories:

- **Abs**olute dominate for Z and W mass
- **ptp** Point-to-point dominate for Γ_Z & $A_{FB}^{\mu\mu}$ (peak and off-peak)
- Due to **sampling** – turns out to be negligible for 1meast /(15 min= 1000s) → 10^4 measts