# Cherenkov detectors and particle identification

## Graduate student Lecture

## HighRR Lecture week





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## Outline

- Part 1: Introduction:
  - Particle identification (PID)
- Part 2: Cherenkov detectors for PID
  - Basic principles
  - Photon detectors
- Part 3: Examples of Cherenkov detector systems
- Part 4: Techniques for PID, other than those using Cherenkov radiation

- Main focus on the principles that are useful for particle identification
- Not Covered : PID using Calorimeters
- Further details
  In the references listed

# Acknowledgements

Many great scientists have written papers and given talks on the topic of Cherenkov detectors. I used material from some of these papers and talks for this lecture.





T.Ypsilantis



J.Vavra



B.N.Ratcliff



J.Séguinot



There are many others also.

O.Ullaland

The references to the papers are listed at the end of this lecture.

# Introduction

- Particle identification is an important part of many experiments in high energy physics
  - These include accelerator based experiments and astroparticle experiments
- Types of particles :
  - Long-lived particles which create signals in a detector :
    - Use experimental techniques to find out if they
      - are electrons, muons, protons, charged pions, charged kaons, photons etc.

- short-lived particles : identified from their decays into long-lived particles example: D-mesons
- quarks, gluons : these are normally inferred from the hadrons, jets of particles etc. that are created from them, using hadronization.
- This lecture: Identification of long-lived particles



## **Detector terminology**

Tracking Detector	: Dire They They in sci	ctions of charged particles create hits create in silicon detectors, wire chambers etc. can also create photons ntillating fibres which in turn are detected by photon detectors.			
Tracking Detector + Magnet (Tracking system)	: Cha Mea and	Charges and momenta of the charged particles Measure of the bending of the particles in magnetic field and use that to infer the momentum of the particle			
Electromagnetic Calorimeter (	(ECAL)	: Energy of photons, electrons etc. Measure the energy deposited in the clusters of hits they create, use the shapes of these clusters.			
Hadronic Calorimeter (HCAL)		: Energy of hadrons : protons, charged pions etc. Measure the energy deposited in the clusters of hits, use the shapes of these clusters			
Muon Detector		: Tracking detector for muons			

Particle identification (PID) detector : Detectors dedicated for PID

# Introduction



Some of the methods for particle identification:

- Electron : ECAL cluster has a charged track pointing to it and its energy from ECAL is close to its momentum from Tracking system.
- Photon : ECAL cluster has no charged track pointing to it.

photon conversion : photon creating e<sup>+</sup> e<sup>-</sup> pair electron bremsstrahlung : electron emitting photons

Muon : Signals in the tracking system , muon chambers and calorimeters

## Introduction

- Particle Identification (PID ) detector:
  - To distinguish between charged kaons, charged pions, protons etc.
  - To separate charged pions from electrons
  - To distinguish between muons and electrons (in neutrino experiments)
  - Reduction of combinatorial backgrounds



- These goals are achieved efficiently using Cherenkov detectors in many experiments.
- More examples and other types of PID detectors later in the lecture.
- Calorimeters and tracking detectors covered in other lectures.

## **Cherenkov Detectors**

- Cherenkov Radiation: General Ideas
- Brief History of the development of Cherenkov detectors
- Classification of Cherenkov detectors
- Photon detectors to detect Cherenkov Radiation
- Examples of large Cherenkov Detector systems

#### Basics of Cherenkov Radiation

In a medium, consider particle with speed v. Let speed of light =  $c_M$  in the medium  $\beta = v/c$ ,  $n = c/c_M$ , where c= speed of light in vacuum

For Cherenkov radiation, the speed of the particle should be such that  $\beta > \beta_{thr} = 1/n$ 



 $\cos(\theta_c) = ((c/n)\Delta t) / (\beta c \Delta t) = 1/(n\beta)$ 

#### $\cos \theta_{c} = 1/n\beta$

 $\theta=0$  : Cherenkov threshold for the charged particle. At threshold,  $\beta_{thr}=1/n$ 

Here  $n = n(\lambda)$ , where  $\lambda = photon wavelength$ 



**Basics of Cherenkov Radiation** 



 $\cos(\theta) = 1/(n \beta)$ 

where **n** = Refractive Index = 
$$c/c_M = n(E_{ph})$$

 $\beta = v/c = p/E = p/(p^2 + m^2)^{0.5} = 1/(1+(m/p)^2)^{0.5}$ 

 $\beta$ = velocity of the charged particle in units of speed of light (c) vacuum p, E, m = momentum, Energy, mass of the charged particle. C<sub>M</sub> = Speed of light in the Medium (Phase velocity), E<sub>ph</sub> = Photon Energy,  $\lambda$ =Photon wavelngth.

Theory of Cherenkov Radiation: Classical Electrodynamics by J.D.Jackson (Section 13.5)

The energy radiated by the charged particle as Cherenkov radiation per unit length =

$$\label{eq:eq:constraint} dE/dx \ = \ (Z/c)^2 \int_{\epsilon(\omega)} 1/\beta^2 \ \omega \ (1-1/(\beta^2 \ \epsilon(\omega)) \ ) \ d\omega \qquad \mbox{Where } \omega = \mbox{Frequency} \\ \epsilon(\omega) \ = \ n^2 \ = \ \mbox{permeability = 1} \\ assume \ \mbox{permeability = 1} \\ Z \ = \ \mbox{charge of the particle} \end{cases}$$

Typical example: Charged particle with momentum of few GeV/c or more emitting Cherenkov photons with few eV of energy  $\cos(\theta) = 1/(n \beta)$ 

- $\theta=0$ : Cherenkov threshold for the charged particle. At Threshold,  $\beta=1/n$
- $\theta$  has Maximum in a medium when  $\beta$  almost = 1
  - ⇔ p/m sufficiently high ⇔ Saturated tracks

 $\boldsymbol{\theta}$  is always less than 90 degree in standard materials

- > Particle ID:  $\theta$  (p,m); If we measure p and  $\theta$ , we can calculate m and thus identify different particles
- Typically, in accelerator based experiments, momentum (p) is measured by a magnetic spectrometer (Tracking system+magnet)
- > Cherenkov detectors: Measure  $\theta$  : Resolution can be expressed in terms of ( $\Delta \beta / \beta$ )

Photonic Crystals: No Cherenkov Threshold and  $\theta$  can be more than 90 degree. Covered briefly at the end of this lecture: Reference: http://ab-initio.mit.edu/photons

#### Basics of Cherenkov Radiation



Cherenkov Angle vs Charged Particle Momentum

The separation between the plots for different particle types enables to discriminate between them.

#### Note on the History of Cherenkov Radiation

> The formula  $\cos \theta = 1/n\beta$  was already predicted by Heaviside in 1888

> ~1900: 'Blue glow' seen in fluids containing concentrated Radium (Marie & Pierre Curie)

- Pavel Alexeevich Cherenkov (1904-1990): Lebedev Physical Institute of the Russian Academy of Sciences.
- Discovery and Validation of Cherenkov Effect : 1934-37
- ➢ Full Explanation using Maxwell's equations: I.M. Frank and I.E. Tamm in 1937
- ➢ Nobel Prize in 1958: Cherenkov, Frank and Tamm.







Typical Apparatus used by Cherenkov to study the angular distribution of Cherenkov photons. (Incident  $\gamma$  ray produces electrons by compton scattering in the liquid).

- P. Cherenkov established that:
  - Light Intensity is proportional to the electron path length in the medium.
  - Light comes only from the 'fast' electrons above a velocity threshold, in his Apparatus.
  - Light emission is prompt and the light is polarized.
  - The wavelength spectrum of the light produced is continuous. No special spectral lines.
  - The angular distribution of the radiation, its intensity, wavelength spectrum and its dependence on the refractive index agree with the theory proposed by his colleagues Frank and Tamm.

Components of a Cherenkov Detector

- Main Components: Radiator : To produce photons
  - Mirror/lens/quartz bar etc. : To help with the transport of photons
  - Photon detector : To detect the photons
- > Radiator: Any medium with a Refractive Index.

# Example of radiators

Medium	n-1	Υth	Photons/m					
He (STP)	3.5 10 <sup>-5</sup>	120	3					
CO <sub>2</sub> (STP)	4.1 10 <sup>-4</sup>	35	40					
Silica aerogel	0.025-0.075	4.6-2.7	2400-6600					
water	0.33	1.52	21300					
Glass	0.46-0.75	1.37-1.22	26100-33100					

Aerogel: network of SiO<sub>2</sub> nano-crystals



$$\gamma = 1/\sqrt{1-\beta^2}$$

> The atmosphere, ocean are the radiators in some Astro Particle Cherenkov Detectors <sup>15</sup>

## Photons from Cherenkov Radiation

>  $n = n(\lambda)$ : Different photons from the same charged track

can have different Cherenkov Angles.(cos ( $\theta$ )=1/n  $\beta$ )).

This spread in angles gives rise to 'Chromatic Error' when measuring the average  $\theta$  from a track.



To reduce the Chromatic error various methods have been tried:

- Filter out the low wavelength photons before they reach the photodetector.
- Appropriate choice of the radiator material
- Recent development: Measure the variation in Time-Of-Propagation of photons (TOP)

from their production point to the detection point.

This can be used to correct for the Chromatic Error

## Photons from Cherenkov Radiation

- Photon production depends on the phase velocity (  $v_{phase}$  ) of photons
- Photon propagation depends on the group velocity (v<sub>group</sub>) of photons



Calibrate dt (variation TOP) with  $d\theta$  (variation in Cherenkov angle) for the photons. Measure the time of arrival at the photon detectors and correct for  $d\theta$ This assumes association between tracks and photons. (*Covered later in the lecture*)

## Photons from Cherenkov Radiation

- Current photon detectors used for detecting Cherenkov light are sensitive to visible + part of UV. This part of the EM spectrum produced by the Cherenkov Radiation is the only range relevant for Cherenkov detectors. λ<sub>ph</sub> ranges from 135 nm to 800 nm depending upon the photodetector.
- Number of photons produced by a particle with charge Z, along a Length L: (From Frank-Tamm theory)

$$N_{prod} = (\alpha/hc) Z^2 L \int_{E_1}^{E_2} \sin^2(\theta) dE_{ph} \qquad \text{where} \quad \alpha/hc = 370 \text{ eV}^{-1}\text{cm}^{-1}, E_{ph} = hc/\lambda.$$

- If the photons are reflected by a Mirrror with Reflectivity R(E<sub>ph</sub>), are transmitted through a quartz window of Transmission T(E<sub>ph</sub>) and then are detected by a photon detector with efficiency Q (E<sub>ph</sub>)
- Number of photons detected :

$$N_{det} = (\alpha/hc) Z^2 L \int R Q T \sin^2(\theta) dE_{ph}$$

=  $N_0 L \sin^2(\theta_c)$  (If we assume  $\theta$  is almost constant =  $\theta_c$  = Mean Cherenkov Angle)

> Figure of Merit of the detector =  $N_0$  For example,  $N_0 = 200$  cm<sup>-1</sup> is a good value.

Classification of Cherenkov Detectors

- Cherenkov Detector Designs:
  - Threshold Counters
  - Imaging Counters: > Differential Cherenkov Detectors
    - Ring Imaging Cherenkov Detectors (RICH)
      - Detector for internally reflected light (DIRC) covered later in the lecture

- > Types of photon detectors:
- (a) Gas Based (b) Vacuum Based (c) Solid State

> Applications:

- In Accelerator Based High Energy Physics Detectors
- In AstroParticle Physics Detectors

Threshold Cherenkov Counters



Signal produced from only those particles which are above Cherenkov threshold.

- Basic idea: Yes/No decision, on the existence of the particle type.
  For this, count the number of photoelectrons detected (N<sub>det</sub>)
- In practice : Calibrate the number of observed photoelectrons or pulse heights to discriminate between particle types.
- > For typical detectors:  $N_o = 90 \text{ cm}^{-1}$ ,

 $N_{ph}$  per unit length of the radiator =  $N_o * (m_1^2 - m_2^2)/(p^2 + m_1^2)$ 

At p= 1 GeV/c,  $N_{ph}$  per unit length = 16 /cm for Pions and 0 for Kaons. At p= 5 GeV/c,  $N_{ph}$  per unit length= 0.8 /cm for Pions and 0 for Kaons.

> Resolution :  $\Delta \beta / \beta = \tan^2 \theta / (2 * \sqrt{N_{ph}})$ 

Threshold Cherenkov Detectors

Can be used over a large area, for example : For secondary particles in a fixed target or Collider experiment.

E691 at Fermilab: To study decays of charm particles in the 1980's  $\Delta\beta/\beta = 2.3 * 10^{-5}$  using gas radiator.

BELLE Experiment: To observe CP ciolation in B-meson decays at an electron-positron collider.





#### **Differential Cherenkov Detectors**



Fig. 2. The differential Cherenkov counter used in the antiproton discovery experiment: (a) side view; (b) end view.

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Nobel Prize in 1959

Differential Cherenkov Detectors



Table 2 Some differential Cherenkov counters

Туре	Year	Length [m]	Angle [mrad]	Gas	Range for $(\pi - K)$ [GeV/c]	Remarks	Ref.
IHEP [1]	1968	5	23	He, N <sub>2</sub>	< 100	no optical	
[2]		10	12		< 200	correction	[3]
DISC	1964	2	44	CO <sub>2</sub>	<100	corrected	[4]
FNAL DISC	1973	5.5	25	He	< 500	Id.	[2]
	$(<100 \text{ for } \pi - \mu - e)$						
CEDAR W	1976	3.25	31	N <sub>2</sub>	<150	ld	[5]
N		3.90	26	He	< 340		
HYPERON	1972	0.3	120	SF <sub>6</sub>	< 40	ld.	[2]
DISC				•	( <100 for ∑-p)		1-1
For comparison:							
LDISC	1976	0.05	640	FC88 hquid	< 5	corrected high aperture	[6]

## **RICH** Detectors



> Measures both the Cherenkov angle and the number of photoelectrons detected.

- Can be used over particle identification over large surfaces.
- Requires photodetectors with single photon identification capability.

**RICH** detectors

**Resolution:** 

 $\ge \Delta \beta / \beta = \tan(\theta) * \Delta \theta_{c} = K \text{ where } \Delta \theta_{c} = <\Delta \theta > / \sqrt{N_{ph}} + C$ 

where  $<\Delta\theta>$  is the mean resolution per single photon in a ring and C is the error contribution from the tracking , alignment etc.

- For example , for 1.4 m long  $CF_4$  gas radiator at STP and a detector with  $N_0 = 75$  cm<sup>-1</sup> K = 1.6 \* 10 <sup>-6</sup> .
- This is better than similar threshold counters by a factor 125.
  This is also better than similar differential counters by a factor 2.
  Reason: RICH measures both θ and N<sub>ph</sub> directly.
- RICH detectors have better resolution than equivalent differential and threshold counters.

> Let  $u = sin^2(\theta) = 1 - (1/n^2) - (m/p^*n)^2$  for a particle with mass m and momentum p

Number of standard deviations to discriminate between particles with masses,  $m_1 \text{ an } m_2 = N_{\sigma} = (u_2 - u_1) / (\sigma_u^* \sqrt{N_{ph}})$  where  $\sigma_u : \Delta \theta$  converted into the parameter u. (  $\Delta \theta$  = error in single photon  $\theta$  measurement)

> At momentum p (= $\beta$  E), N<sub>g</sub>= sqrt((m<sub>2</sub><sup>2</sup>-m<sub>1</sub><sup>2</sup>)/(2 \* K \* p)), for  $\beta \sim 1$ 

This equation gives a general idea regarding number of  $\sigma$  separation achievable, during in the design of the RICH detectors. However it has limitations in giving a good prediction, in multi particle events with high occupancy. In practice, detailed simulations are carried out for detector design.

> One of the first large size RICH detector: in DELPHI at LEP.

# Photon detection techniques

 The RICH detectors require capability to detect 'single photons'. This is more difficult than detection of photons in other detectors. (for example a simple camera, a calorimeter etc.)

• Types of Photon detectors:

(a) Gas Based (b) Vacuum Based (c) Solid State

- ➢ Principle: Convert Photons → Photoelectrons using a photocathode
  - Detect these photoelectrons using 'charged track detectors'.
  - Measure the position and (/or ) time of photoelectrons in the tracking detector.
  - General introduction to tracking detectors and silicon detectors is not covered in this lecture. However they are covered in other lectures this week.

- In this lecture, we focus on some of the aspects related to the detection of photoelectrons in Cherenkov Detectors.
- Gas based detectors:
  MWPC (Multi Wire Proportional Chambers)
  GEM (Gas Electron Multiplier)
- Vacuum based detectors: PMT (Photomultiplier tubes) HPD (Hybrid Photodiodes)
- Solid state detectors: Silicon photomultipliers

### **Photodetectors**

- Photon Conversion:
  - Photoelectric Effect : Photon energy to be above the 'work function' (Einstein : Nobel Prize in 1921).
  - Commercial alkaline Photocathodes: Bialkali, Trialkali (S20), CsI etc. Alkali metals have relatively low 'work function'.
  - There are also gases where the photon conversion takes place.
  - Different photocathodes are efficient at different wavelength ranges.
  - Quantum Efficiency (QE) : Fraction of photons converted to electrons
  - Photon detection efficiency (PDE): Effective QE, that is measured PDE = QE x P<sub>trigger</sub> x ε<sub>PackingGeometry</sub>

PackingGeometry refers to Active area fraction, for example due gaps between pixels  $P_{triager}$  refers to where the electron is produced, for example in an SiPM.





Examples of S20- photocathodes 29

#### Photodetector with Csl photocathode



cause feedback: leading to loss of original signal info.

Gas Based Photon Detectors



- $\triangleright$  photon passes through the CaF<sub>2</sub> and converts to photoelectron by ionizing a TEA molecule.
- The photoelectron drifts towards and avalanches near the anode wires, theirby inducing a charge signal on the cathode pads.



Recent Developments: Gas Based Photodetectors

#### **GEM:** Gas Electron Multiplier





GEM with semi-transparent Photocathode (K-Cs-Sb)

- Photon and ion feed back reduced.
- Gated operation to reduce noise.
  (no readout outside a 'time window of signal')
- For now only closed geometry ( in sealed tubes): Reduced fraction of useful area for photon detection (Active Area Fraction) compared to open geometry.



#### Vacuum Based Photodetectors

PMT schematic:







MAPMT

**PMTs** 



 PMTs Commercially produced: more info in <u>www.sales.hamamatsu.com</u>



Silicon detector of HPD



Features of HPD



Signal pulse height spectrum of a 61-pixel HPD Illuminated with Cherenkov photons

Typical gain = 5000 (approx)

Very low noise: typically, only a few hundred electrons

- PMT: ➤ Typical Gain of MAPMT 300 K.
  - Excellent time resolution: ~ 150 ps (Ex: used in underwater Cherenkov detectors).
  - Active area fraction: 40 % 75% : Fraction of effective detection area. This can be Improved with a lens, at the cost of a few photons at lens surface
  - Recent developments: Flat panel pmts with 89 % active area fraction. Recent photocathodes with >45% QE at 400 nm

> HPD: > Typical gain 5K, but quite uniform across different channels.

Excellent Single photon identification capability.

> Active area fraction:  $35 \rightarrow 76 \%$
#### Comparison of photodetectors

Choice of photodetector depends on the design of the Cherenkov detectors and constraints on cost etc.

Gaseous:

- Issues: Related to photon and ion feed back and high gains at high rate.
  - Detection in visible wavelength range (for better resolution)
  - There have been recent improvements in these areas

### Advantages: • Can operate in high magnetic field

Lower cost for large size detectors compared to vacuum based detectors

#### Vacuum based:

#### Issues:

- Sensitivity to magnetic field
- cross talk between readout channels in case of PMTs
- Active Area Fraction
- There have been recent improvements in these areas

#### Advantages:

- Can easily operate at high rate (eg. LHC rates and higher).
- Operates also in visible wavelengths. (reduced chromatic error)
- Ease of operation at remote locations: underwater, in space etc.
- HPD: uniform gain over large number of tubes and small noise.

Other Types and new developments: Silicon photomultiplier, MCP etc. for single photon detection

## Recent Developments: Silicon Photomultipliers (SiPM)



- The Geiger mode operation needed for single photon detection
- > Time resolution  $\sim$  < 100 ps.
- Works in magnetic field
- ➢ gain ~ 10 <sup>6</sup>
- Electric field ~ 3-5 x 10<sup>5</sup> V/cm
- Radiation hardness: sufficient for many applications, especially when single photon detection is not needed. Tests being done for single photon detection and in very high luminosity environments
- Reducing noise levels for single photon detection is still an issue and it is being worked upon.
   One option: operate at very low temperatures to get a dark count rate < 100 kHz/mm<sup>2</sup>

S10362-33 -059C MPPC				
QE at 440nm (Silicone)	> 60 %			
P <sub>trigger</sub> - trigger probability	80 - 90 %			
Geometrical fill factor	78.5 %			
PDE = Total fraction of detected photons (includes <u>after-pulses &amp; cross-talk !!!</u> ) *	~ 52 % @ 440 nm (HPK quote)			
After-pulsing total rate	$\sim 20\%$			
Operating voltage	70 ± 10 V			
Terminal capacitance	320 pF			
Pixel size	100 μm x 100 μm			
Overall size & Sensitive size	~ 3.85 mm x 4.35 mm & 3 mm <sup>2</sup>			
Total Gain	$\sim 2.4 \ x \ 10^6$			
Noise rate (Single photoelectron threshold) *	~ 8 MHz			
Transit time spread $\sigma_{TTS}$	< 100 ps			

Recent Developments: Silicon Photomultipliers



- Photon detection efficiency of SiPM is better than that of MaPMTs
- Typical time resolution of SiPMs ( <100 ps) is better than that of MaPMTs (150 ps)
- A very active R & D is in progress to improve the properties of SiPMs.

Further info: Sensors 2019,19(2),308

## New Developments: Micro Channel Plate (MCP) Photon Detectors



10um pores in an MCP

#### New Developments: Micro Channel Plates (MCP)



Typical Size:

- 2 mm thickness,
  51 mm X 51 mm active area.
- 10 micron pores separated by 15 microns
- Chevron: 8 degree tilt : To increase the gain and reduce ion-feed back
- Gain: ~ 5 \* 10 5
- Typically ~ 1000 channels per MCP.





(SIDE VIEW)



- Measure Space and time of the hits.
- Manufactured by industry ( *Photonics for example*).
- Resolutions: Space: ~100 microns, Time: ~ 50 100 psec.
- Short flight path of photoelectrons: Resistant to magnetic fields up to 0.8 Tesla.
- Can work at 40 MHz readout rate.
- Can detect single photons (No noise from 'first dynode' as in MAPMT).
- Fast 'ageing' at large luminosity (eg: LHC) is an issue. However some solutions are being developed.

# Examples of Cherenkov detector systems

- RICH in LHCb at CERN
- DIRC in BABAR at SLAC
- IceCube in Antartica

## The LHCb Experiment



2 <  $\eta$  < 5, Forward spectrometer. Overall acceptance ~ 10 $\rightarrow$ 300 mrad, Momentum range : 2-100 GeV/c

- Precision measurement of B-Decays and search for signals beyond standard model.
- Two RICH detectors cover the full momentum range . Until 2014, it had aerogel, C<sub>4</sub>F<sub>10</sub> gas and CF<sub>4</sub> gas as radiators.

## LHCb-RICH original Design

RICH1: Aerogel L=5cm p:2 $\rightarrow$ 10 GeV/c n=1.03 (nominal at 540 nm) C<sub>4</sub>F<sub>10</sub> L=85 cm p: < 70 GeV/c n=1.0014 (nominal at 400 nm) Upstream of LHCb Magnet Acceptance: 25 $\rightarrow$ 250 mrad (vertical) 300 mrad (horizontal) Gas vessel: 2 X 3 X 1 m<sup>3</sup>

RICH2: CF<sub>4</sub> L=196 cm p: < 100 GeV/c n =1.0005 (nominal at 400 nm) Downstream of LHCb Magnet Acceptance: 15→100 mrad (vertical) 120 mrad (horizontal) Gas vessel : 100 m<sup>3</sup>

- Original version used HPDs as photon detectors.
- The design was upgraded in the last decade. At present, it uses MaPMTs as photon detectors. The aerogel was removed.



## LHCb-RICH Specifications



#### **RICH1 OPTICS**



#### LHCb- RICH1 SCHEMATIC



 Spherical Mirror tilted to keep photodetectors outside acceptance (tilt ~ 0.3 rad)

#### RICH1 Photos

RICH1-HPDs







#### **RICH1** mirrors



## LHCb- RICH2 STRUCTURE



Entrance Window (PMI foam between two carbon fibre epoxy Skins)



RICH2

### Typical Hits on LHCb-RICH HPDs





- > LHCb-RICH collected data during 2010-2018 (RUN1, RUN2).
- > The signals from the HPDs are subjected to time and space alignment.

#### RICH data from simulation for RUN3 in 2022



Y vs X of the hit coordinates on the detector planes, from simulations.

## Performance of LHCb RICH

From isolated Cherenkov rings from RICH1 in Real Data



Compare with the expectations plotted earlier.

### LHCb-RICH performance from simulations: RUN2 and RUN3

# Examples of Cherenkov Angle Resolutions and yields

Resolution (in mrad)	RICH1-2015 HPD, C <sub>4</sub> F <sub>10</sub>	RICH1- upgrade MaPMT, C <sub>4</sub> F <sub>10</sub>	RICH2-2015 HPD, CF <sub>4</sub>	RICH2- upgrade MaPMT, CF <sub>4</sub>
Chromatic	0.84	0.58	0.48	0.31
Pixel	0.60, PSF=0.86	0.44	0.19 PSF=0.29	0.19
Emission point	0.76	0.37	0.27	0.27
Overall Overall+Track	1.60 1.65	0.78 0.88	0.65 0.76	0.45 0.60
Yield	32	42	24	22

 Yield: Mean Number of RICH hits per saturated track (Beta ~1).

Ref: "Overview of LHCb RICH Upgrade", S.Easo, Nucl.Inst.Meth. A 876 (2017) 160-163

- Chromatic: From the variation in refractive index.
- Emission Point: Essentially from the tilt of the mirrors.
- Pixel Size: From the granularity of the pixels in HPD/MaPMT
- PSF ( Point Spread Function): From the spread of the Photoelectron direction as it travels inside the HPD.

RUN3 starts in 2022

## LHCb-RICH resolution

Single photon resolutions



From simulation in 2011:  $\sigma_{\Delta\theta} = 1.53 \text{ mrad}$ 

From simulation in 2011:  $\sigma_{\Delta\theta} = 0.68 \text{ mrad}$ 

## LHCb-RICH detector: data taking

 The refractive index (n) is dependent on the pressure(P) and temperature (T) of the gas radiator.

(n-1)  $\alpha$  P/T

Hence it was required to monitor this continuously

 The CF<sub>4</sub> scintillates. This creates additional photons which go in 4π directions and forms background to the signal photons.
 A solution was found by mixing this gas with a small amount of CO<sub>2</sub>.
 The CO<sub>2</sub> essentially quenches most of the scintillation photons.

Here the scintillation is from a 'cascade-free' emission. The quenching happens due to a radiationless transition from a donor molecule to an acceptor molecule with a subsequent transmission in infrared wavelengths. Ref: Nucl. Inst. Meth. A 791 (2015) 27-31

#### **RICH** data from simulation for RUN3

Singe event



Pattern Recognition in accelerator based Cherenkov Detector

 Events with large number of charged tracks giving rise to several overlapping Cherenkov Rings on the photo detector plane.
 Problem: To identify which tracks correspond to which hits and then identify the type (e, p, π etc.) of the particle which created the tracks.

 Hough Transform: (used by ALICE at CERN)

- > Project the particle direction on to the detector plane
- Accumulate the distance of each hit from these projection points in case of circular rings.
- Collect the peaks in the accumulated set and associate the corresponding hits to the tracks.

· Likelihood Method:

(used by LHCb at CERN)

- For each of the track in the event, for a given mass hypothesis, create photons and project them to the detector plane using the knowledge of the geometry of the detector and its optical properties. Repeat this for all the other tracks.
  - From this calculate the probability that a signal would be seen in each pixel of the detector from all tracks.
  - Compare this with the observed set of photoelectron signal on the pixels, by creating a likelihood.
  - Repeat all the above after changing the set of mass hypothesis of the tracks. Find the set of mass hypothesis, which maximize the likelihood.

(Ref: R.Forty: Nucl. Inst. Mech. A 433 (1999) 257-261)

## LHCb-RICH PID performance



## LHCb RICH Data in Physics Analysis



## **RICH Detectors in LHCb**





RICH PID useful for physics analysis

#### LHCb-RICH data in 2011



• Examples of signals for  $\Phi -> KK$ ,  $K_s -> \pi \pi$ ,  $D -> K\pi$ ,  $\Lambda -> p \pi$  obtained using RICH.

The data from RICH are used for Physics Analysis.

## LHCb-RICH upgrades

Recent upgrades:

- Installed arrays of MaPMTs as photon detectors.
- Improved the optics geometry for RICH1.
- These improve the resolutions and yields of the photons in the two detectors
- The reconstruction software for PID, is running online



Arrays of MaPMTs in RICH1





Arrays of MaPMTs in RICH2

**RICH2** mirrors

## LHCb-RICH upgrades

• Starting to collect data with the new system:



- Future upgrades are also being planned:
  - Usage of fast timing with new readout chips and new types of photons detectors to obtain a resolution below 100 ps
  - Improvement in all other aspects of the system, including the optics
  - Usage of modern GPUs for simulation and reconstruction

#### LHCb: Hit distribution from simulations

Single event



- Fast timing can help to improve the RICH performance.
- This is planned for the future upgrade of these detectors

## **DIRC PRINCIPLE**

- If  $n > \sqrt{2}$  some photons are always totally internally reflected for  $\beta \approx 1$  tracks.
- Radiator and light guide: Long, rectangular Synthetic Fused Silica ("Quartz") bars (*Spectrosil:* average <n(λ)> ≈ 1.473, radiation hard, homogenous, low chromatic dispersion)
- Photons exit via wedge into expansion region

(filled with 6m<sup>3</sup> pure, de-ionized water).





- Pinhole imaging on PMT array (bar dimension small compared to standoff distance). (10,752 traditional PMTs ETL 9125, immersed in water, surrounded by hexagonal "light-catcher", transit time spread ~1.5nsec, ~30mm diameter)
- DIRC is a 3-D device, measuring: x, y and <u>time</u> of Cherenkov photons, defining  $\theta_c$ ,  $\phi_c$ ,  $t_{propagation}$  of photon.



# **DIRC** detector

## Photon detector:



## Cherenkov radiator:



- Bar dimensions (glued out of 4 segments): 488 cm x 3.5 cm x 1.7 cm
- ~11,000 1 inch dia. ETL PMTs, sitting in water to minimize the photon loss.

## DIRC PERFORMANCE

Number of Cherenkov photons per track (di-muons) vs. polar angle:



Between 20 and 60 signal photons per track.



Resolution of Cherenkov angle fit per track (di-muons):



 $\sigma(\Delta \theta_c) = 2.4 \text{ mrad}$ 

## Track Cherenkov angle resolution is within ~10% of design



## **DIRC PERFORMANCE**

DIRC time resolution:

Difference between measured and expected time:



- This helps to reduce the background
- However, in order to correct for chromatic corrections, further improvement needed. In recent years R&D to achieve this goal was performed.



# **DIRC** performance

Background reduction from fast timing:



The cut on  $\Delta t$  helps to reduce background and avoid forward-backward ambiguity.

## **DIRC PERFORMANCE**



New Development: Focussing DIRC



### $v_{group}(red) > v_{group}(blue)$

- Red photons arrive before blue photons
- Time of Propagation= PathLength/ v group
- Correct for Chromatic error from the measurement of time of propagation.



Size of the expansion volume reduced

- Chromatic error reduced
- Needs photon timing resolution  $\sigma \sim 200 \text{ ps}$

Ref: NIMA 595(2008)104-107

Cherenkov Detectors in Astro Particle Physics

Goal: Contribute to the understanding of our Universe.

- Understanding production mechanism ('cosmic accelerators') of HE cosmic rays ;
   Study very energetic galactic / extragalactic objects : SN remnants, microquasars, GRB, AGN,...;
  - Search for Dark matter (wimps)

. . .

Micro-

quasars

SNR



AGN



GRB



Binary systems



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### Astro Particle Physics



Search for :

- ➢ Neutrinos → muons
- > High energy Gamma and other Cosmic rays  $\rightarrow$  Air showers
- > Ultra high energy Gamma ( > 10 <sup>19</sup> eV )  $\rightarrow$  Air showers



Neutrinos: Advantages: • Neutral : Hence

- Neutral : Hence Weak interaction only
- Neutrinos point back to the astrophysical production source
  - Unlike photons which interact with CMB and matter
  - or protons: which also undergo deflection by magnetic fields

Disadvantages:

- Rate of arrival very low. Hence need very large detectors.
- Using the Ocean , ice in Antartica etc. as Cherenkov radiators



# Typically 1γ / PMT 40 m from μ axis

• Measure position and time of the hits.

Angle between the directions of  $\mu$  and  $\nu$  =

Importance of Timing Resolution c in water ~ 20 cm/ns Chromatic dispersion ~ 2 ns (40 m typ. Path) (PMT TTS σ ~1.3ns) so detector not dominant source of error



#### ANTARES Experiment in the sea





Glass pressure Sphere.

**Optical Module** 





Hamamatsu PMT : Size :10 inch

# IceCube Experiment in Antartica





#### IceCube Experiment









#### **Design Specifications**

- Fully digital detector concept.
- Number of strings 75
- Number of surface tanks 160
- Number of DOMs 4820
- Instrumented volume 1 km<sup>3</sup>
- Angular resolution of in-ice array < 1.0°
- Fast timing: resolution < 5 ns DOM-to-DOM
- Pulse resolution < 10 ns
- Optical sens. 330 nm to 500 nm
- Dynamic range
  - 1000 pe / 10 ns
  - 10,000 pe / 1 us.
- Low noise: < 500 Hz background
- High gain: O(10<sup>7</sup>) PMT
- Charge resolution: P/V > 2
- Low power: 3.75 W
- Ability to self-calibrate
- Field-programmable HV generated internal to unit.
- 10000 psi external

Ice Cube/AMANDA Event signatures :

All signals are from Cherenkov Radiation.



# IceCube event signatures

Every DOM gets about 500-800 hits per second, mainly from dark counts. Hits from Physics events are ~1 order of magnitude lower. After trigger, per year:

- 10<sup>10</sup> events caused by atmospheric muons
- 10<sup>9</sup> events caused by noise
- 10<sup>5</sup> events from atmospheric neutrinos
- A handful of very high energy events likely to be of astrophysical origin

Tracks:

Mainly  $v_{\mu}$  CC interactions or atmospheric muons



#### Cascades:

Mainly  $v_e$ ,  $v_t$  CC as well as NC interactions



Double Bang: Very high energy taus with second decay shower (~ 50 m /Pev)



#### High Energy Cosmic Ray Spectrum.



- Measure the Energy Spectrum
- Determine the Arrival Direction distribution etc.
- Composed of Baryons, photons, neutrinos etc.

>10<sup>19</sup> eV 1 km<sup>-2</sup> year<sup>-1</sup> sr<sup>-1</sup>







- 1600 surface stations
  1.5 km spacing
  over 3000 square kilometers
- Fluorescence Detectors: 4 Telescope enclosures, each with 6 telescopes.

# AUGER Project: Water Cherenkov Detector



• . First set of results are published

Time difference between test signals from nearby detectors

# Some other techniques for PID

- Techniques using energy loss (dE/dx)
- Time-of-Flight detectors
- Transition radiation detectors

#### Momentum ranges for PID detectors

Typical ranges:

- Hadron PID over large momentum range (1-100 GeV/c)
  with high resolution :
  - RICH with different radiators in different momentum range
  - Requires large radiator length at high momenta In the future photonic crystals may reduce the radiator length?
- PID in the 1-5 GeV/c range : DIRC (using Cherenkov effect), detectors using energy loss (dE/dX).

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- PID in the 1-6 GeV/ range
- Electron-pion separation (0.5 – 200 GeV/c range)
- PID in the TeV range (Astro particle detectors)

- Time of flight (TOF) detectors In the future up to 10 GeV/c.
- : Transition radiation detectors (TRD).
  - Cherenkov effect from secondary particles which are at relatively lower momentum.

### dE/dx PID technique

dE/dx : Energy lost per unit length by the particle due to various processes like ionization



• Calculated first by Bethe-Bloch in the 1930's.



#### Energy loss : Bethe-Bloch formula for dE/dx



## dE/dx detectors: Silicon based



Energy loss by ionization

Ref: NIMA 469(2001) 311-315



Fig. 1. Landau  $\langle dE/dx \rangle$  distributions for pions of momenta 220, 100 and 50 MeV going through 300 µm of silicon.

FWHM= 30-35 %

## dE/dx detectors: Silicon based

For minimum ionizing particles in silicon,

dE/dx ~ 39 keV/100  $\mu$ m

An energy deposition of 3.6 eV will produce one e-h pair

Hence, in 300  $\mu$ m we should get a mean of 32k electron-hole (e-h) pairs. The most probable value is ~0.7 of the mean of the landau distribution.



Hence we expect to get, 22K e as signal.

Typical S/N at LHC = 17/1 In practice the most probable value is estimated from measurements from different silicon layers.

# dE/dx Detectors : Silicon based

- Each Silicon sensor gives a single dE/dX measurement.
- Estimate the Most Probable Value from several (10-25) measurements (Truncated Mean: Ignore upper 40%)

CMS Silicon tracker:



### dE/dx Detectors: Drift Chambers

- Larger Landau fluctuations compared to those from silicon detectors. Hence many measurements needed to get the average.
- Bethe-Bloch formula with <u>Sternheimer</u> parametrization of the density function:





Mean ionization potential = I ~ (10 eV ) \* Z Electron density =  $n_{el} = N_A * Z * \rho/A$ 

for X > X.

 $\delta = 4.606(X - X_{.})$ 

## *dE/dx Detectors: Drift Chambers*

#### **BABAR Drift Chamber:**

Gas mixture 80% helium, 20% isobutane, 3500–4000 ppm water vapor,  $\sim$  80 ppm O<sub>2</sub>







Good  $\pi/K$  separation up to  $\sim$  700 MeV/c. Ref: IEEE-TNS VOL:47 , NO:6, Dec2000.

 $\mathrm{d}E/\mathrm{d}x$  resolution  $\sim$  7.5% 92

• For a charged particle traversing a detector:

using L=v t,  $\beta = v/c = p/E = p/(p^2 + (mc)^2)^{0.5}$ 

m=mass, p=Momentum, t=time, L= distance travelled, c=speed of light in vacuum Using SI units

t ( = TOF ) measured, is related to the mass of the particle

Typically, the mass resolution here is dominated by the time resolution , dp/p  $\sim$  1% and dL/L  $\sim$  0.001.

For two particles, with mass  $m_1$  and  $m_2$  for p >>  $m_1$ ,  $m_2$ 

$$\Delta t = (L_{path}/c) * (1/\beta_1 - 1/\beta_2) = (L_{path}/c) * [\sqrt{(1 + (m_1 c/p)^2)} - \sqrt{(1 + (m_2 c/p)^2)}] = (L_{path}/c) + (L_{path}/c) + (m_1 c/p^2) + (m_1 c/p$$

The expected particle separation =

$$N_{\sigma} = [(L_{path}c/2p^2) * (m_1^2 - m_2^2)] / \sigma_{Total}$$

where  $\sigma_{\text{Total}}$  has many contributions :

$$\sigma_{\text{Total}} \sim \sqrt{\left[ (\sigma_{\text{TTS}} / \sqrt{N_{\text{pe}}})^2 + (\sigma_{\text{Chromatic}} / \sqrt{N_{\text{pe}}})^2 + \sigma_{\text{Electronics}}^2 + \sigma_{\text{Track}}^2 + \sigma_{\text{T0}}^2 \right]}$$

At very high momentum,  $\Delta t$  will be too small and become comparable to detector resolution.

An example: L= 1.8 m,  $\sigma_{total}$ =25 ps, for 3  $\sigma$  separation for  $\pi/K$  at p = 3 GeV/c

Comparison of dE/dx and TOF methods for BaBar DIRC/Super-B



These are ideal level of separations.

The TOF methods was used mostly for PID below 2-3 GeV/c



New detectors reach somewhat higher momentum limit.
 Example: LHCb upgrade proposal has a detector named TORCH.
 It is proposed to be placed at L ~ 10 m with Δ t=40 ps, reaching up to 10 GeV/c for 3σ π–K separation.



Measurement of time: Using scintillators

Ref: CERN-EP/99-001

Energy loss (dE/dx) from the charged particle= 2MeV/cm This energy is re-emitted as optical photons in UV. (Approx 1 photon/100 eV) Too small attenuation length and low yield.

Fluorescent material added to scintillator so that the photon re-emitted at longer wavelengths (ex: 400 nm) longer attenuation length (ex: 1 meter) and high yield. These photons collected by a PMT. (0.002 pe per emitted photon)

NA 49: Heavy ion expt, Scintillator thickness=2.3 cm, time resolutions up to 59 ps.



ALICE at CERN: using MRPC (Multigap Resistive Plate Chamber) Gas detector at a radius of 3.6 m with 150 m<sup>2</sup> area





Performance in testbeam Time resolution= 50 ps

PID best in 0.5->2.5 GeV/c  $2\sigma$  K- $\pi$  separation up to 5 GeV/c





Cathode pickup

Differential signal to front-end electronics

Resistive plates made of glass. 2 X5 gaps : 250 m m The resistive plates stop the avalanche development, but transparent to the fast signal. Use HPTDC (High Performance TDC)

Anode pickup electrode

Transition Radiation: Radiation in the x-ray region when ultra relativistic particles cross the boundary between 2 media with different dielectric constants.
 Mainly for e-π separation in 0.5 GeV/c → 200 GeV/c.

Full explanations and the derivations from Maxwell's equations:

Nucl. Inst. Meth. A 326 (1993) 434-469 and references there in.



> The radiation is peaked at a small angle  $\theta = 1/\gamma$ .

The intensity of the radiation (after some approximations) becomes

$$\frac{d^2 W}{d\omega \ d\theta} = \frac{2\alpha}{\pi} f_0(\theta) \qquad \text{where} \qquad f_0(\theta) = \theta^3 \left( \frac{1}{\gamma^{-2} + \theta^2 + \xi_g^2} - \frac{1}{\gamma^{-2} + \theta^2 + \xi_f^2} \right)^2$$
$$\xi_i = \omega_i / \omega \quad \text{, } \omega_f = \text{plasma freqency of medium } I$$

Integrating the previous equation, one can get , for  $\xi_q = 0$ ,

W $_{TR}$ = 2.43 x 10 $^{-3}$ $\omega_{f} \gamma$	Here $\gamma = E/m$ of the particle. This makes PID possible by measuring W. Lighter particle give larger signal
	$\omega_{\rm f}~$ = plasma frequency = 28.8 ( $\rho$ Z/A) <sup>0.5</sup> eV
	ρ=density, Z=atomic weight, A=atomic number

For example, for  $\omega_{\rm f} = 0.02 \text{ keV}$  and  $\gamma = 5000$ , most of the photon energy is in the range 10 keV<  $\omega < 100 \text{ keV}$  (ie.  $0.1 \omega_{\rm c} < \omega < \omega_{\rm c}$  where  $\omega_{\rm c} = \text{cut-off frequency}$ ).

Number of photons produced = 
$$N(>\omega) = \frac{\alpha}{\pi} \left\{ \ln \frac{\omega_c}{\omega} \left( \ln \frac{\omega_c}{\omega} - 2 \right) + \frac{\pi^2}{12} + 1 \right\}.$$

For  $\omega_c = 100 \text{ keV}$  and  $\omega = 1 \text{ keV}$ , N= 0.03 for a single surface. Hence to get sufficient number of photons, large number of interfaces are used : a stack of many foils with gaps in between.

Formation zone: For relativistic particles,

most of the energy is emitted from within a small region of size  $R = \gamma^2 c / \omega$  next to the interface.

• The minimum thickness of the foils and air gaps are determined by the size of the 'formation zone' and the interference effects.

( for example, foils can be 10-20  $\mu$  m thick and are made of polypropelene)

• Behind a TRD foil stack there is a MWPC or drift chamber where the TRD signal is detected along with the signal from the charged track.









#### Barrel and endcap TRT



Ionization loss of charged particles ~ 2.5 keV TR photon > 5 keV. (Photon emission spectrum peaks at 10-30keV)



For 90% electron identification efficiency, pion rejection probability (mis-id ) using three different methods



## Photonic crystals as radiators

Concept:

- Assemble materials to produce the desired 'effective refractive index'
- Requires designing photonic crystals from transparent dielectrics



Photonic crystals:

- Typically made from two materials with different refractive indices, in alternating layers.
- The magnitude of layer thickness is similar to that of the photon wavelengths.
- Production of layers as thin as optical wavelengths, feasible in recent years. This creates the current interest in using the crystals, as radiators



#### **Resonance Transition Radiation :**

- Has the features of conventional Cherenkov radiation
- Both forward and backward radiation are possible

Nature physics 14, 816-821 (2018)



Example of natural photonic crystal

### Photonic crystals as radiators

Example of forward configuration with 1d crystal





- Can be configured for different momentum ranges
- This can result in radiators which are only few mm thick.

Topics for R&D:

- The periodicity of the crystal structure can cause chromatic error. Many options to mitigate this are being investigated.
  - Use materials with anisotropy which can compensate for achromaticty
  - Use filters to limit the wavelength range
  - Improving photon yield, ensure radiation hardness etc.



- The field of Particle identification detectors is an evolving field.
- They have contributed to some of the important discoveries in High Energy Physics in the last 50 years and they continue to be a crucial part of some of the recent experiments.
- The RICH detectors offer excellent particle identification capability for the hadrons since they can be designed to have very good single photon Cherenkov angle resolution and large photoelectron yield. Recent advances in photodetectors enhance the capability of these detectors.
- The particle ID using dE/dx, time-of-flight and Transition Radiation detectors continue to provide particle identification in different experiments.
- Particle identification is a crucial part of some of the Astroparticle physics experiments and long base line neutrino experiments

### References

Acknowledgement: Thanks to all the authors of the papers from which the material for this lecture has been compiled. For information on Cherenkov detectors: (1) <u>http://pdg.lbl.gov</u>

- (2) T. Ypsilantis et.al. Nucl. Inst. Meth A (1994) 30-51
- (3) J.Vavra : Lecture : Super-B Particle identification systems (2009)
- (4) M.Ahlers, F.Halzen : Opening a New Window onto the Universe with IceCube: arXiv:1805.11112 [astro-ph.HE] (2018)
- (5) B.Dey et.al. Design and performance of the Focusing DIRC detector arXiv:1410.0075 [physics.ins-det]
- (6) Adinolfi,M. et.al (LHCb-RICH collaboration)
  Performance of the LHCb RICH detector at the LHC
  Eur.Phys. J. C 73 (2013) 2431

The Lord of the Rings

Photons from ice and sea under the sky, Photons from vast water tanks in halls of stone, Photons from the atmosphere in an insect's eye, Photons from aerogels, light, clear, blown, Photons from liquids, gases, crystals flying by, Photons from fused silica expanding on a cone. In RICH detectors where PID truths lie. One Ring to rule them all, One Ring to find them, One Ring to bring them all, correlate, and bind them In RICH detectors where PID truths lie.

(From B.N.Ratcliff, Nucl. Inst. Mech. A 501(2003) 211-221)

# EXTRA SLIDES
Long Base Line Experients: T2K



Neutrino production: Protons incident on graphite target to create pions, which decay into  $\mu$  and  $\nu_{\mu}$ . The muons and and any remaining protons and pions are stopped by a second layer of graphite; but the  $\nu_{\mu}$  pass through towards SuperK. Beam energy: Centered around 600 MeV (to maximize the oscillation probability into  $\nu_{\epsilon}$ ).

Far-detector: underground to reduce cosmic rays.

#### Super-K water cherenkov detector



40 m high, 17 m radius.



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Super-K Cherenkov signals

 ν<sub>e</sub>/ν<sub>µ</sub> strike nuclei in H<sub>2</sub>O, produce e<sup>-</sup>/µ<sup>-</sup> via weak charged-current (CC) interactions.

The leptons create Cherenkov light in the water.



- □ e; p > 0.6 MeV/c
- m; p > 120 MeV/c (muon)
- π; p > 160 MeV/c
- K; p > 563 MeV/c
- p; p > 1,070 MeV/c
- + ~50MeV to identify a Cherenkov ring.

$$\theta_{c} = 42^{\circ}$$
 for relativistic particle in water  $\beta \sim 1$ 

(in water)

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#### Super-K signals



Measure the charge and time of each pulse. From this estimate :

- (a) energy of the charged particle.
  - (Charge  $\alpha$  number photons  $\alpha$  energy loss)
- (b) position (vertex) of the interaction.
- (c) direction of the charged particle.

Each dot represents a PMT hit by light

Muons create sharp rings, Electrons scatter and shower and hence create 'fuzzy' rings.

## LHCb-RICH pattern recognition

## Cherenkov angle reconstruction:

reconstructing the Cherenkov angle for each hit and for each track in the region of interest, assuming all photons are originating from the mid point of the track in the radiator.



Find the reflected point with respect to the flat mirror. Use the fact that for the spherical mirror, the detection point (D), center of curvature (C), the reflection point (M) and the emission point (E) are on the same plane. Use D,C,E to solve for the reflection point M.

The Cherenkov angle is the angle between EM and the track direction.

Cherenkov angle reconstruction:

$$(Rd_y + 2ed_x \sin\beta) \cos\beta = R(e + d_x) \sin\beta + ed_y(1 - 2\sin^2\beta)$$

Squaring both sides and rearranging the terms, one gets a quartic equation to solve for sin  $\beta$ . With the solution, one determines the point M



Reconstructed Cherenkov angles. The solid points are for the angles from the true track which created the hit

# Brief description of the global algorithm for PID

- Project each charged track to the detector plane and select all RICH hits which are around each track projection, within the maximum possible Cherenkov radius.
- Create combinations of tracks and RICH hits.

These constitute candidates for the 'photons' that created the hits. Determine the Cherenkov angles for these 'candidate photons'.

• For all the combinations of tracks and particle type hypotheses, determine the 'expected signals' on each MaPMT pixel and their uncertainty.

This is done using a 'fast simulation' procedure. The average level of background expected for each MaPMT pixel is also added to this.

- The 'expected signal' is compared with the signal from 'candidate photons' in Cherenkov angle space. This is used to accumulate the 'likelihood' for each combination of tracks and particle type hypotheses. *This enables to find the combination with the best 'likelihood'*.
- The results on PID for each track are quoted in terms of the logarithm of likelihood ratios.

Ratio = likelihood for a particle type hypothesis / likelihood for pion hypothesis.

The algorithm runs in the Cherenkov angle space

Local algorithm Each track is taken in turn.

$$\ln \mathbb{L} = \sum_{i} \ln \left( 1 + \frac{1}{\sqrt{2\pi}\sigma_{\Theta}\kappa} \exp \left[ -\frac{(\Theta_{i} - \Theta_{x})^{2}}{2\sigma_{\Theta}^{2}} \right] \right)$$

 $\Theta_i$ : calculated emission angle for hit *i*  $\Theta_x$ : expected angle for hypothesis *x*  $\sigma_{\Theta}$ : angular resolution  $\kappa$ : hit selection parameter

Global algorithm: This is actually used by LHCb these days The likelihood is constructed for the whole event:

$$\ln \mathbb{L} = -\sum_{\text{track } j} \mu_j + \sum_{\text{pixel } i} n_i \ln \left( \sum_{\text{track } j} a_{ij} + b_i \right)$$

*a<sub>ij</sub>*: expected hits from track *j* in detector/pixel *i* 

 $\mu_{j} = \Sigma_{i} a_{ij}$   $n_{i}: \text{ hits in detector } i$   $b_{i}: \text{ expected background in detector } i$ 



Ref: "RICH pattern recognition in LHCb", R.Forty Nucl.Inst.Meth. A 433 (1999) 257-261

Observed number of photoelectrons in each pixel a small region on detector plane

LHCb-RICH pattern recognition

The probability distribution expected for signal photoelectrons:

$$f_{h_j}(\theta,\phi) = \frac{1}{(2\pi)^{3/2} \sigma(\theta)} \exp\left[-\frac{1}{2} \left(\frac{\theta - \theta_{\rm c}(h_j)}{\sigma(\theta)}\right)^2\right]$$



• The result of the algorithm is expressed in terms of  $\Delta \ln \mathbb{L}_{K\pi} = \ln \mathbb{L}(K) - \ln \mathbb{L}(\pi)$ 



Expected number of photoelectrons in a small region on detector plane