

# Study of depth-dependent charge collection profiles in irradiated pad diodes

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- Luminosity in the CMS Phase-2 is up to  $7.5 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$ .
- This causes a neutron equivalent fluence of  $3.5 \times 10^{16} \text{ cm}^{-2}$  (after  $4000 \text{ fb}^{-1}$ ) in the first layer of the inner tracker.
- The radiation damage changes the electric field and trapping times of the sensors used in the inner tracker.

## The motivation of this talk

- Study the charge collection in highly irradiated silicon diodes which provides precise data for testing simulation of irradiated silicon sensors

## The tool of study

- Edge-on measurement using electron beam with an energy of 5.2 GeV

## The performed measurements

- Charge profiles of non-irradiated and irradiated diodes at different bias voltages

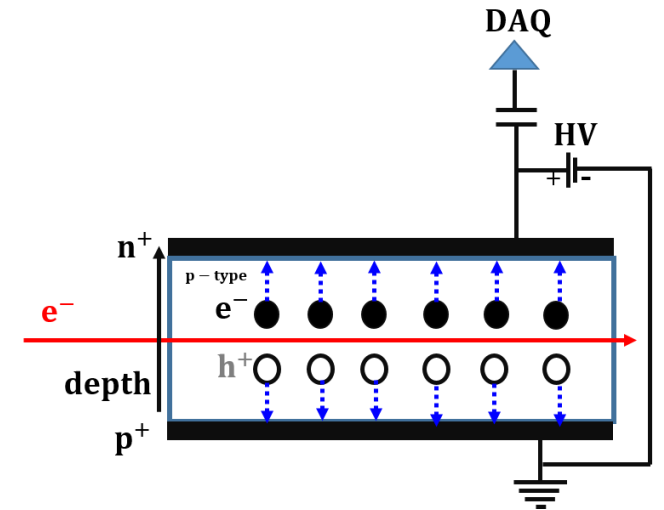


The method was introduced in previous RD50 workshop ([37<sup>th</sup> RD50](#))

The measurement results were shown for four irradiated pad diodes ([38<sup>th</sup> RD50](#))

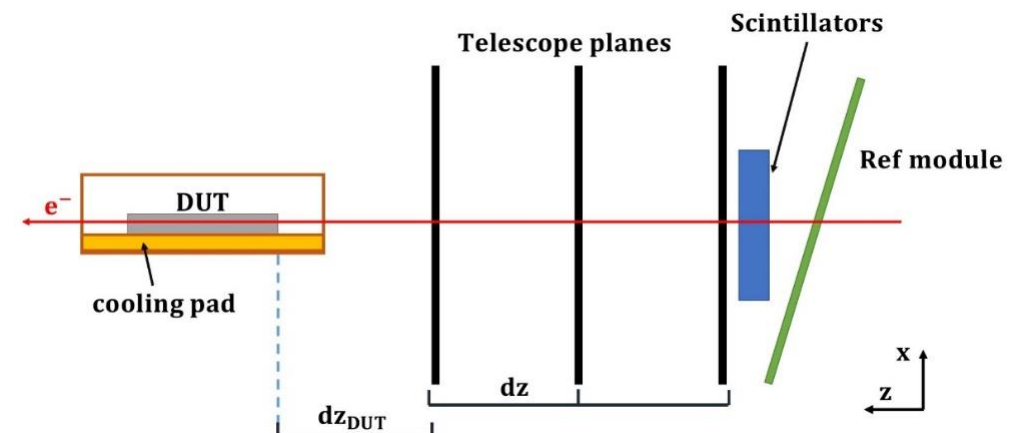
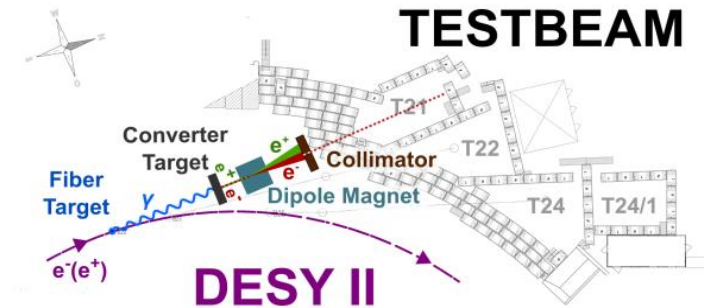
In this talk:

- The measurements results are compared with results of radiation damage models
- The data are unfolded to extract CCE profile as a function of depth.



## DESY II beam test facility:

- Electron/positron beam with energy of 1-6 GeV
- Beam energy of 5.2 GeV was chosen for the measurements
- Intrinsic resolution of each plane of telescope  $\approx 3.2 \mu\text{m}$
- Timing reference module for reducing in-time pile up
- Scintillator for providing the readout trigger
- Rotation stage for the DUT with a precision of  $0.10^\circ$  (1.7 mrad)

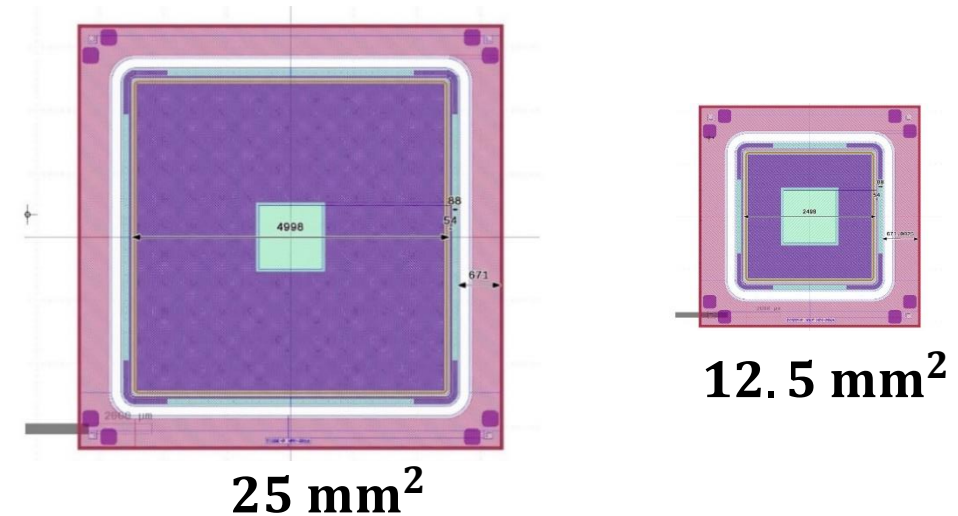


# Specifications of the diodes



Top view (dimensions are in micrometer)

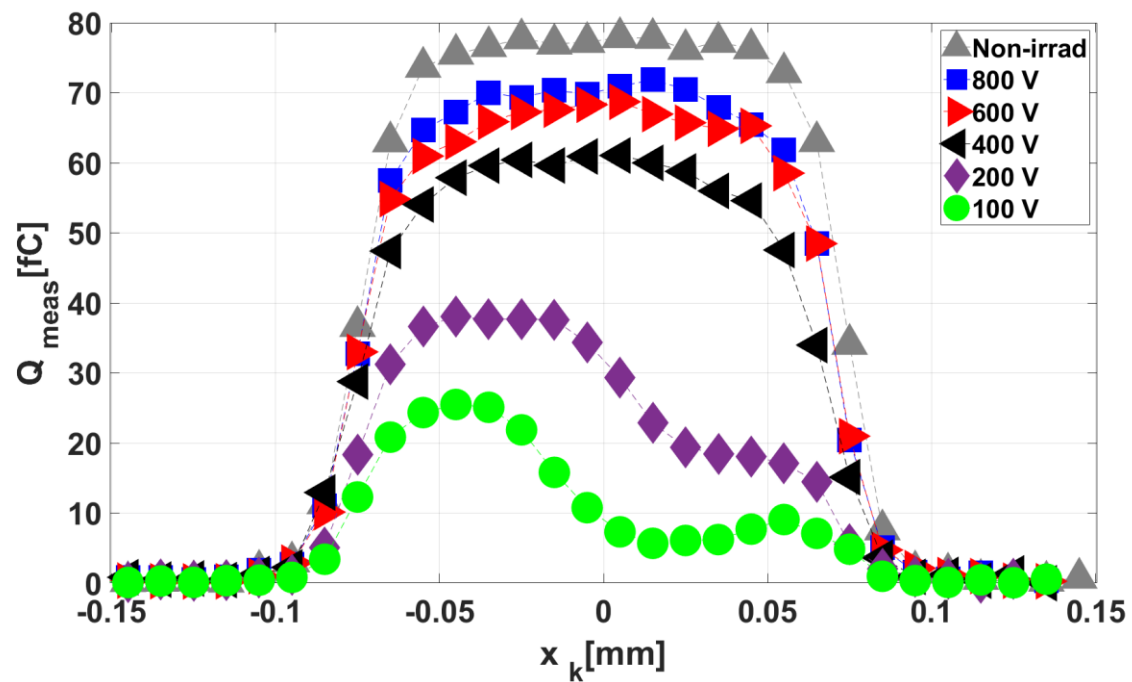
- Nominal thickness 150  $\mu\text{m}$
- Area  $\approx 25$  and  $12.5 \text{ mm}^2$
- p-type ( $n^+pp^+$  configuration)
- Doping concentration  $\approx 4.5 \times 10^{12} \text{ cm}^{-3}$
- Depletion voltage 75 V
- Manufactured by Hamamatsu Photonic K.K (HPK)
- Guard-ring is floating



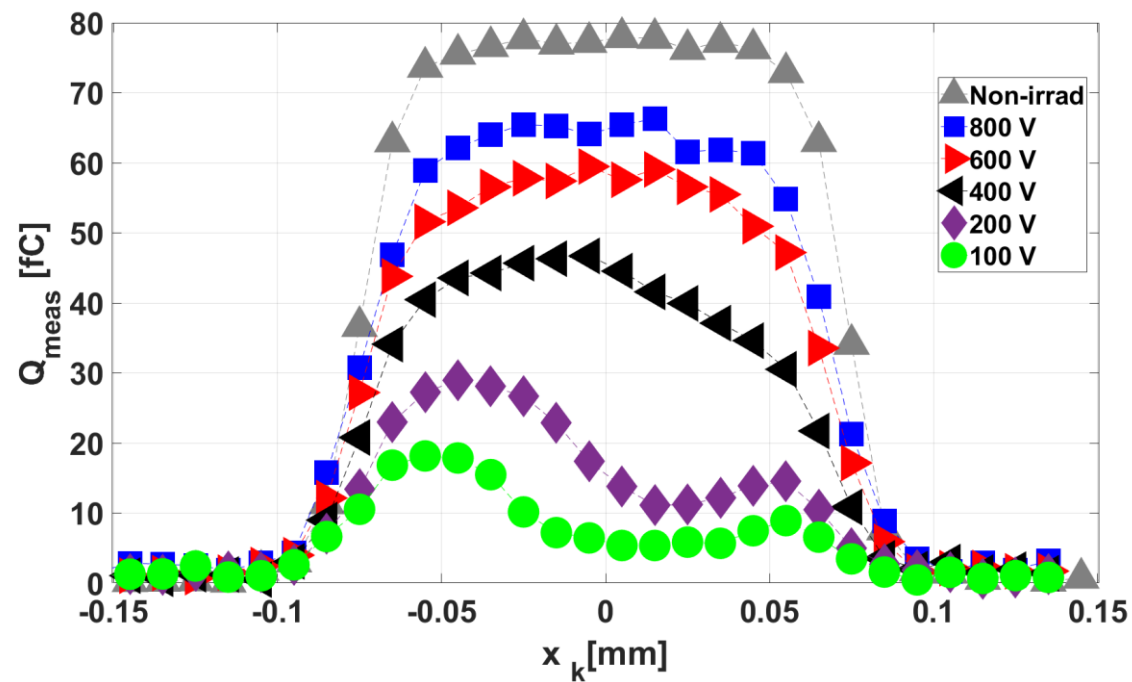
For irradiation study

- Irradiation with 23 MeV protons at Karlsruhe Institute of Technology (KIT)
- Irradiation to 1 MeV equivalent fluence  $\Phi_{\text{eq}} = 2, 4, 8$  and  $12 \times 10^{15} \text{ cm}^{-2}$  (hardness factor of  $\kappa = 2.2$ )

$$\Phi_{\text{eq}} = 2 \times 10^{15} \text{ cm}^{-2}$$

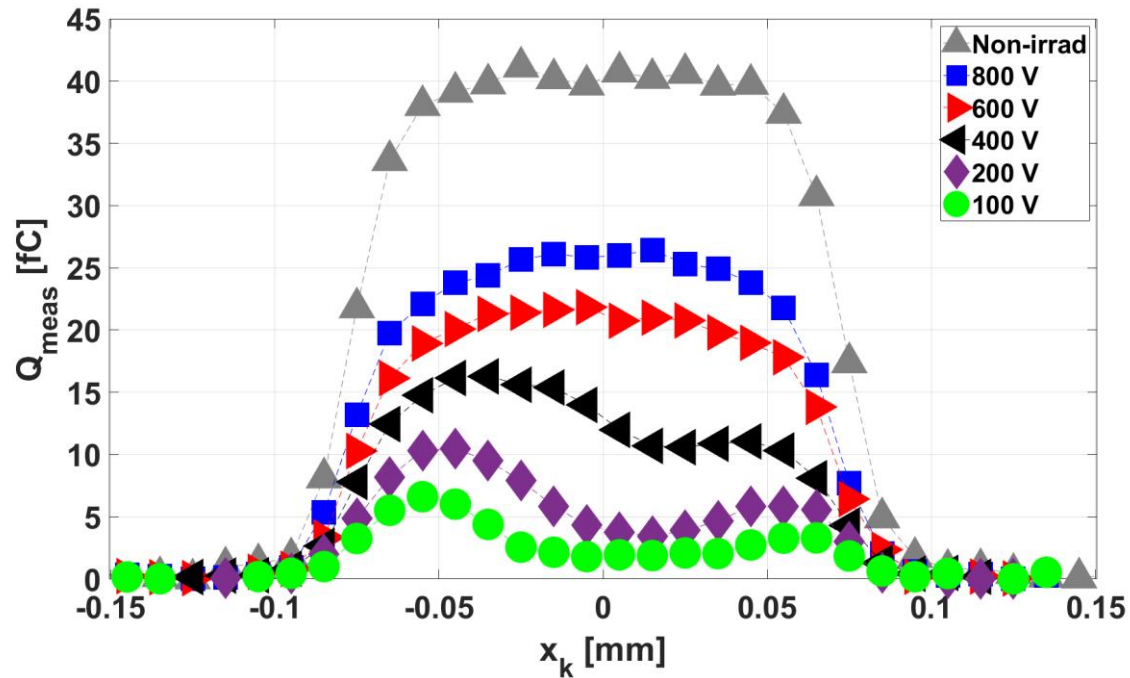


$$\Phi_{\text{eq}} = 4 \times 10^{15} \text{ cm}^{-2}$$

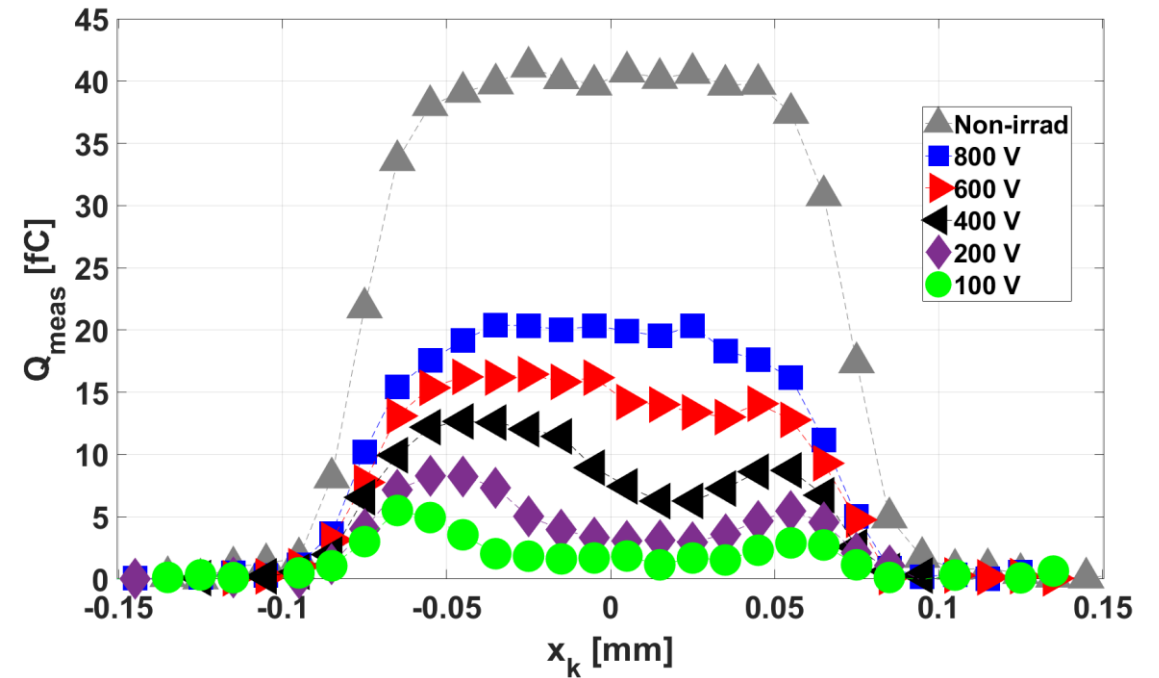




$$\Phi_{eq} = 8 \times 10^{15} \text{ cm}^{-2}$$



$$\Phi_{eq} = 12 \times 10^{15} \text{ cm}^{-2}$$





The model is optimized to describe the following experimental data:

- Capacitance versus Voltage (CV)
- Current versus Voltage (IV)
- Charge Collection Efficiency (CCE) versus Voltage

The data are taken for pad diodes:

- Active thickness: 200  $\mu\text{m}$
- Irradiation with 24 GeV protons at CERN PS facility
- Irradiation to equivalent fluence  $\Phi_{\text{eq}} = 0.3, 1, 3, 6, 8, 13 \times 10^{15} \text{ cm}^{-2}$

$$F = \sum_{i,j} w_i^j \int_{V_{\min}}^{V_{\max}} \left( 1 - \frac{Q_{i,\text{sim}}^j}{Q_{i,\text{data}}^j} \right)^2$$

i: measurement types  
 j: fluences

Defect	Type	Energy	$g_{\text{int}}$ [ $\text{cm}^{-1}$ ]	$\sigma_e$ [ $\text{cm}^2$ ]	$\sigma_h$ [ $\text{cm}^2$ ]
E30K	Donor	$E_C - 0.1 \text{ eV}$	0.0497	2.300E-14	2.920E-16
V <sub>3</sub>	Acceptor	$E_C - 0.458 \text{ eV}$	0.6447	2.551E-14	1.511E-13
I <sub>p</sub>	Acceptor	$E_C - 0.545 \text{ eV}$	0.4335	4.478E-15	6.709E-15
H220	Donor	$E_V + 0.48 \text{ eV}$	0.5978	4.166E-15	1.965E-16
C <sub>i</sub> O <sub>i</sub>	Donor	$E_V + 0.36 \text{ eV}$	0.3780	3.230E-17	2.036E-14

$g_{\text{int}}, \sigma_e, \sigma_h$ : free parameters  
 $g_{\text{int}}$ : introduction rate

The paper can be found [Here](#)





The model is optimized to describe the following experimental data:

- Charge Collection Efficiency (CCE) with  $^{90}\text{Sr}$  source

The data are taken for PiN diodes and strip sensors:

- Irradiation with 26 MeV protons
- Irradiation to equivalent fluence up to  $2.2 \times 10^{16} \text{ cm}^{-2}$

Trap Type	Energy (eV)	$\eta$ (cm <sup>-1</sup> )	$\sigma_e$ (cm <sup>2</sup> )	$\sigma_h$ (cm <sup>2</sup> )
Donor	$E_C-0.23$	0.006	$2.3 \times 10^{-14}$	$2.3 \times 10^{-15}$
Acceptor	$E_C-0.42$	1.613	$1.0 \times 10^{-15}$	$1.0 \times 10^{-14}$
Acceptor	$E_C-0.46$	0.900	$7.0 \times 10^{-15}$	$7.0 \times 10^{-14}$

$\eta$ : introduction rate

The paper can be found [Here](#)



The model is optimized to describe the following experimental data:

- IV and CV measurements

The data are taken for Low Gain Avalanche Diodes (LGADs):

- Irradiation to equivalent fluence up to  $1.0 \times 10^{16} \text{ cm}^{-2}$

Defect number	Type	Energy level	$\sigma_e$ (cm <sup>2</sup> )	$\sigma_h$ (cm <sup>2</sup> )	$\eta$ (cm <sup>-1</sup> )
1	Donor	$E_C - 0.23 \text{ eV}$	2.3e-14	2.3e-15	0.015
2	Acceptor	$E_C - 0.42 \text{ eV}$	1.0e-15	1.0e-14	10
3	Acceptor	$E_C - 0.46 \text{ eV}$	4.0e-14	4.0e-13	1.2

$\eta$ : introduction rate

The paper can be found [Here](#)

The charge collection profiles are convolution of of:

- the CCE profile
- the smearing caused by the limited spatial resolution of the track position
- the energy deposition profile of the electron beam as a function of depth in the diode

$$Q_{\text{sim}}(x) = A \cdot \left( \text{CCE}_{\text{tot}}(x) \cdot \frac{E_{\text{dep}}(x)}{E_{\text{dep}}(0)} \right) * \text{Gauss}(x, 0, \sigma_{\text{res}})$$

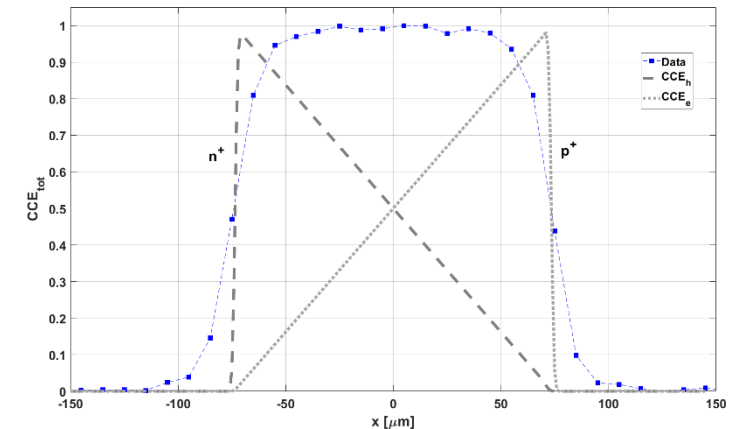
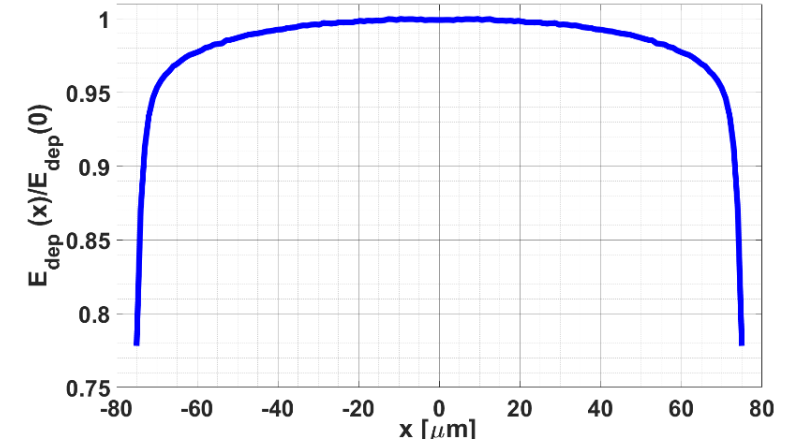
$$\text{CCE}_{\text{tot}}(x) = \text{CCE}_e(x) + \text{CCE}_h(x)$$

$$\text{CCE}_e(x) = \int_{-\frac{d}{2}}^x E_w(y) \cdot \exp\left(\int_x^y \frac{dy'}{\lambda_e(y')}\right) dy$$

$$\text{CCE}_h(x) = \int_x^{+\frac{d}{2}} E_w(y) \cdot \exp\left(\int_x^y \frac{-dy'}{\lambda_h(y')}\right) dy$$

$$E_w(x) = \frac{1}{d}$$

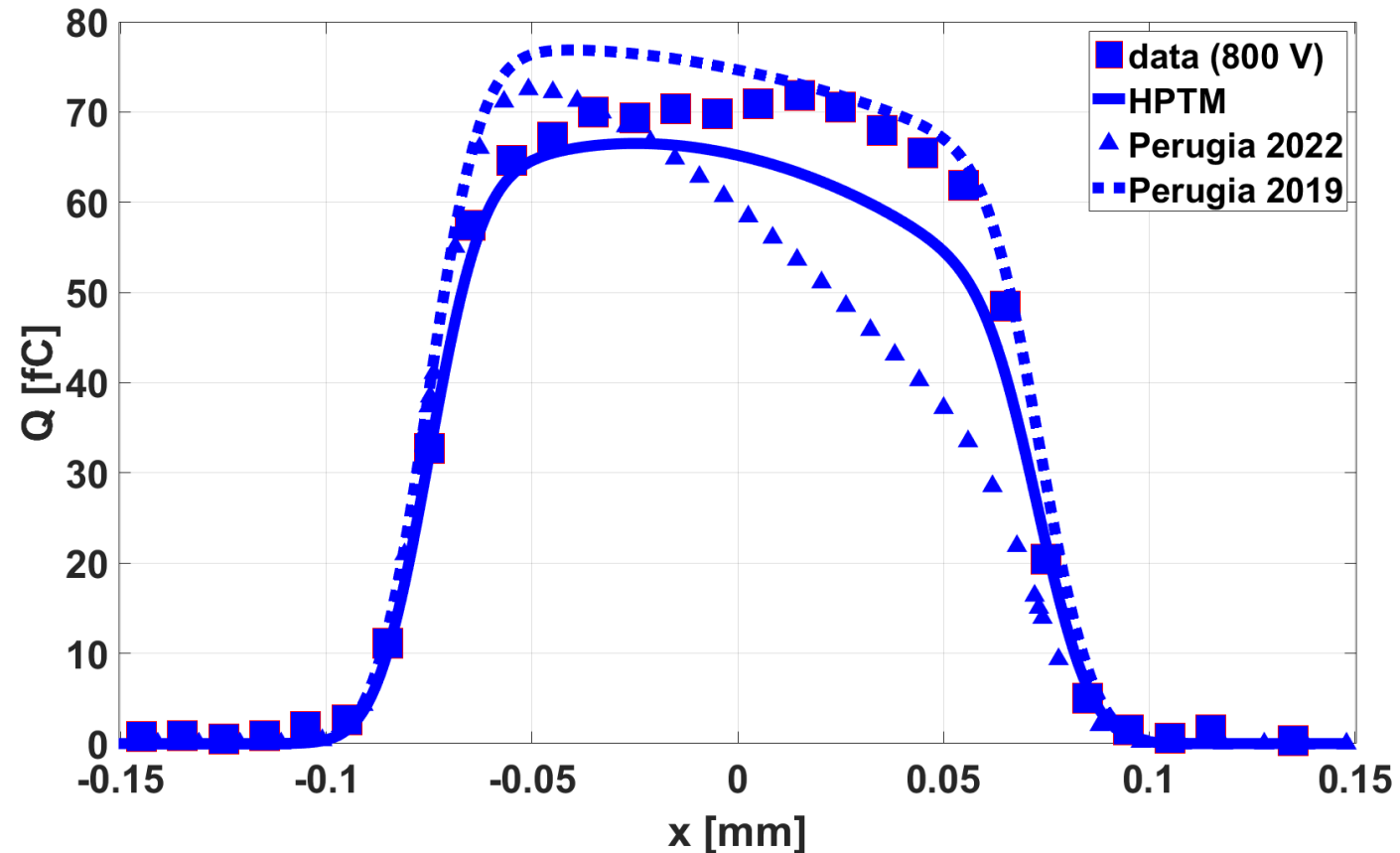
- $\lambda_{e,h}(x)$ : charge collection length of electrons and holes from the models
- $d$ : thickness of the diode (150  $\mu\text{m}$ )
- $A$ : scaling factor (76.8 for pad size of 25  $\text{mm}^2$  and 76.8 for pad size of 12.5  $\text{mm}^2$ )
- $\sigma_{\text{res}}$ : beam resolution (10  $\mu\text{m}$ )



# Comparison with simulation results



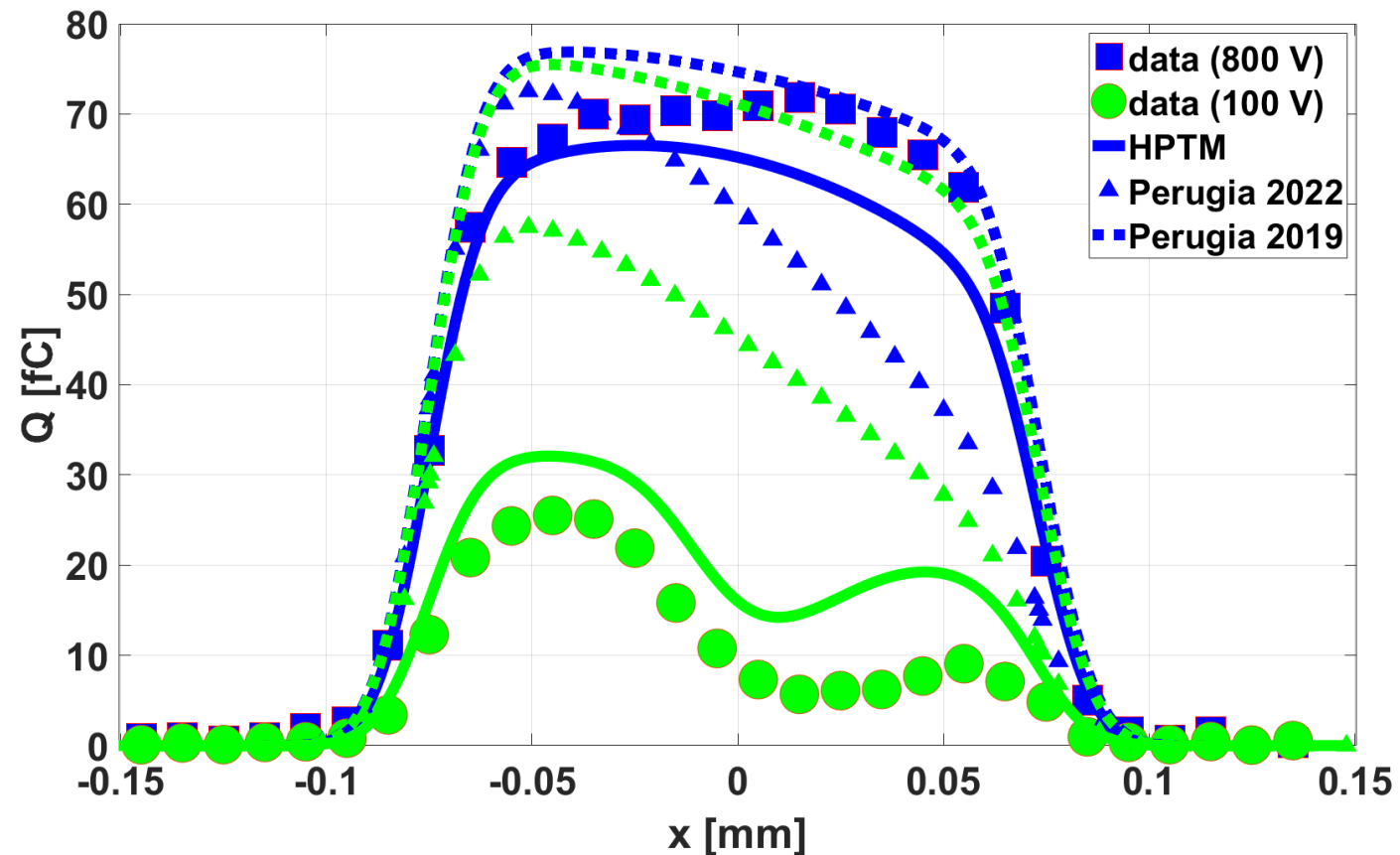
$$\Phi_{eq} = 2 \times 10^{15} \text{ cm}^{-2}$$



# Comparison with simulation results



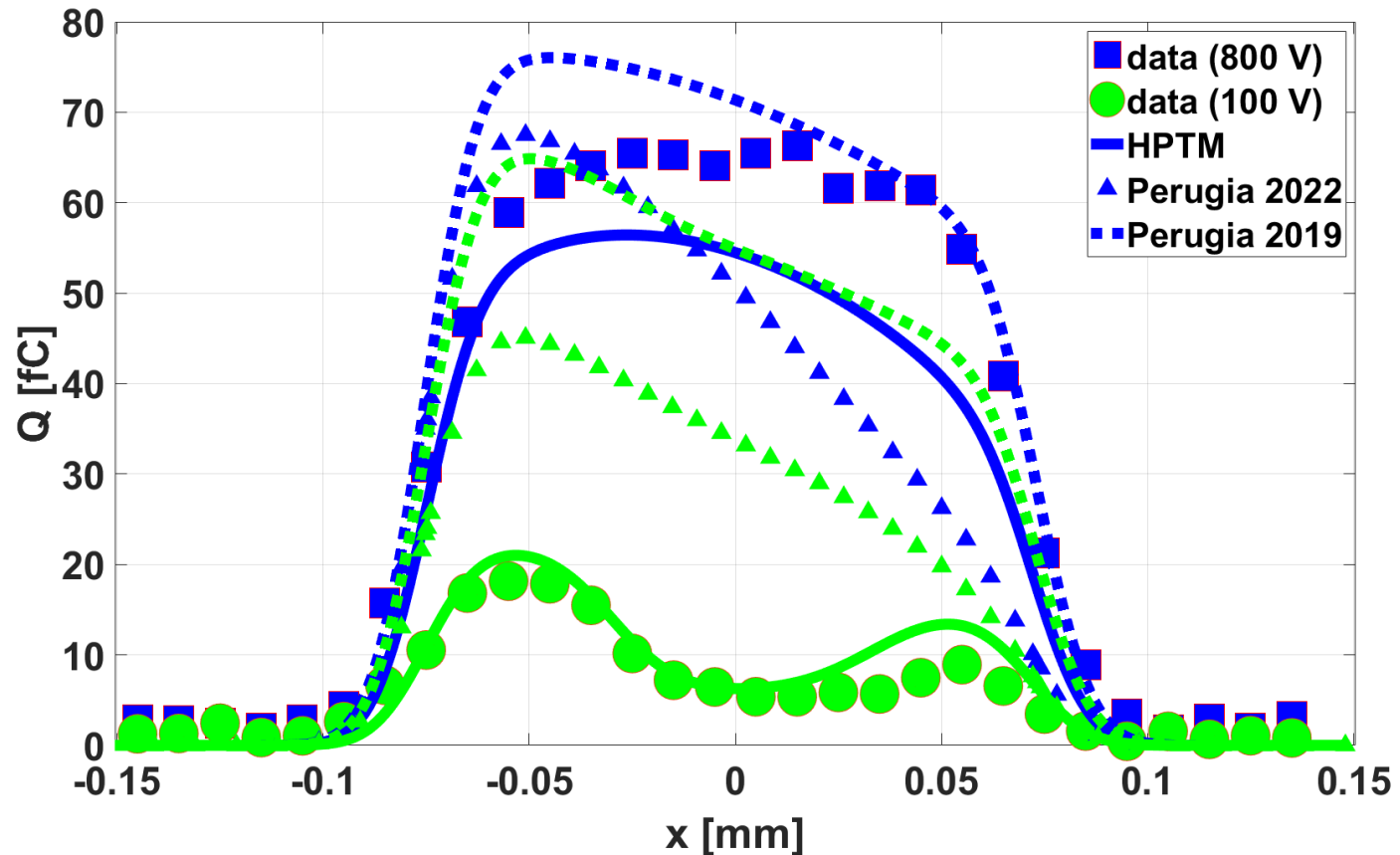
$$\Phi_{eq} = 2 \times 10^{15} \text{ cm}^{-2}$$



# Comparison with simulation results



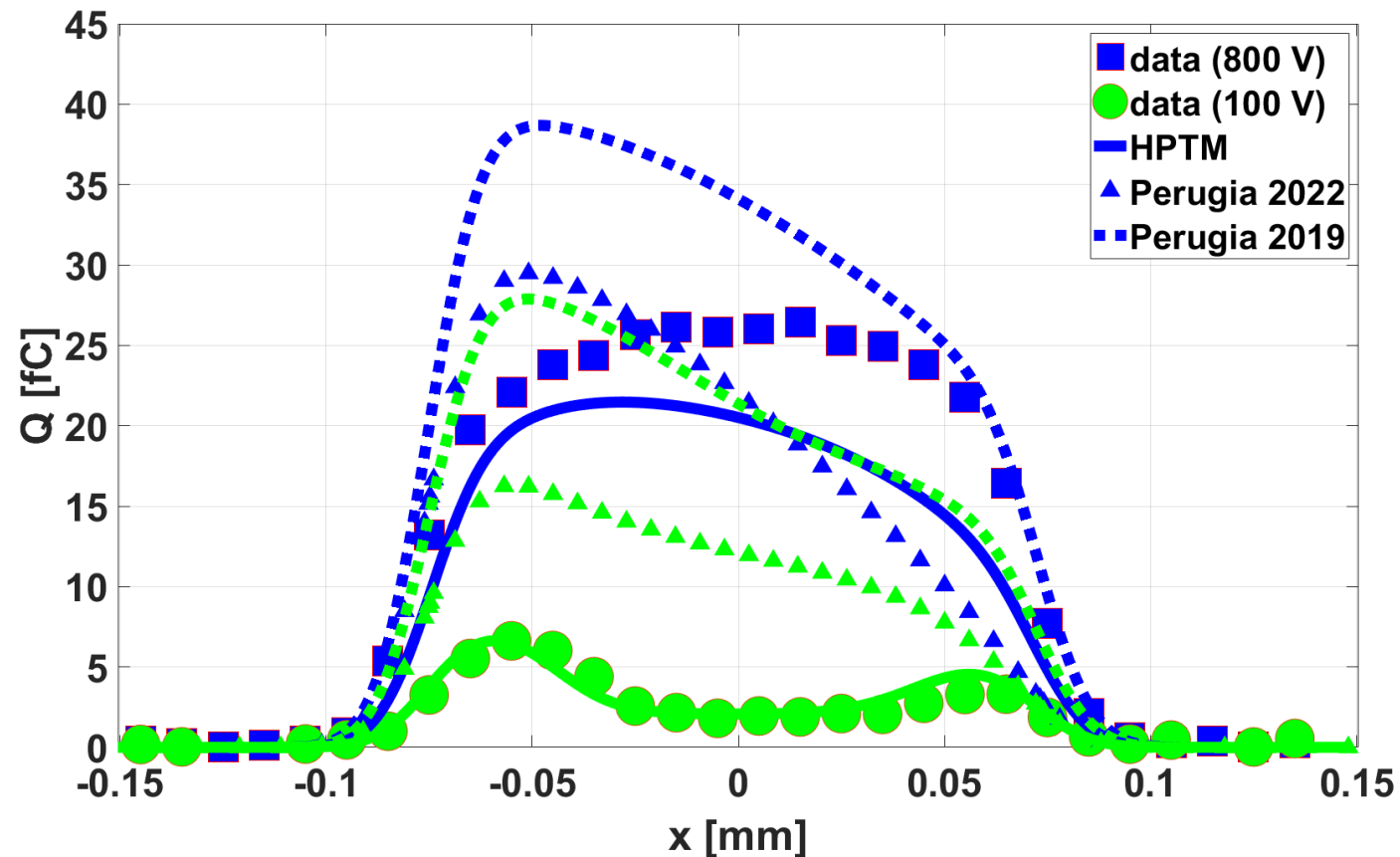
$$\Phi_{eq} = 4 \times 10^{15} \text{ cm}^{-2}$$



# Comparison with simulation results



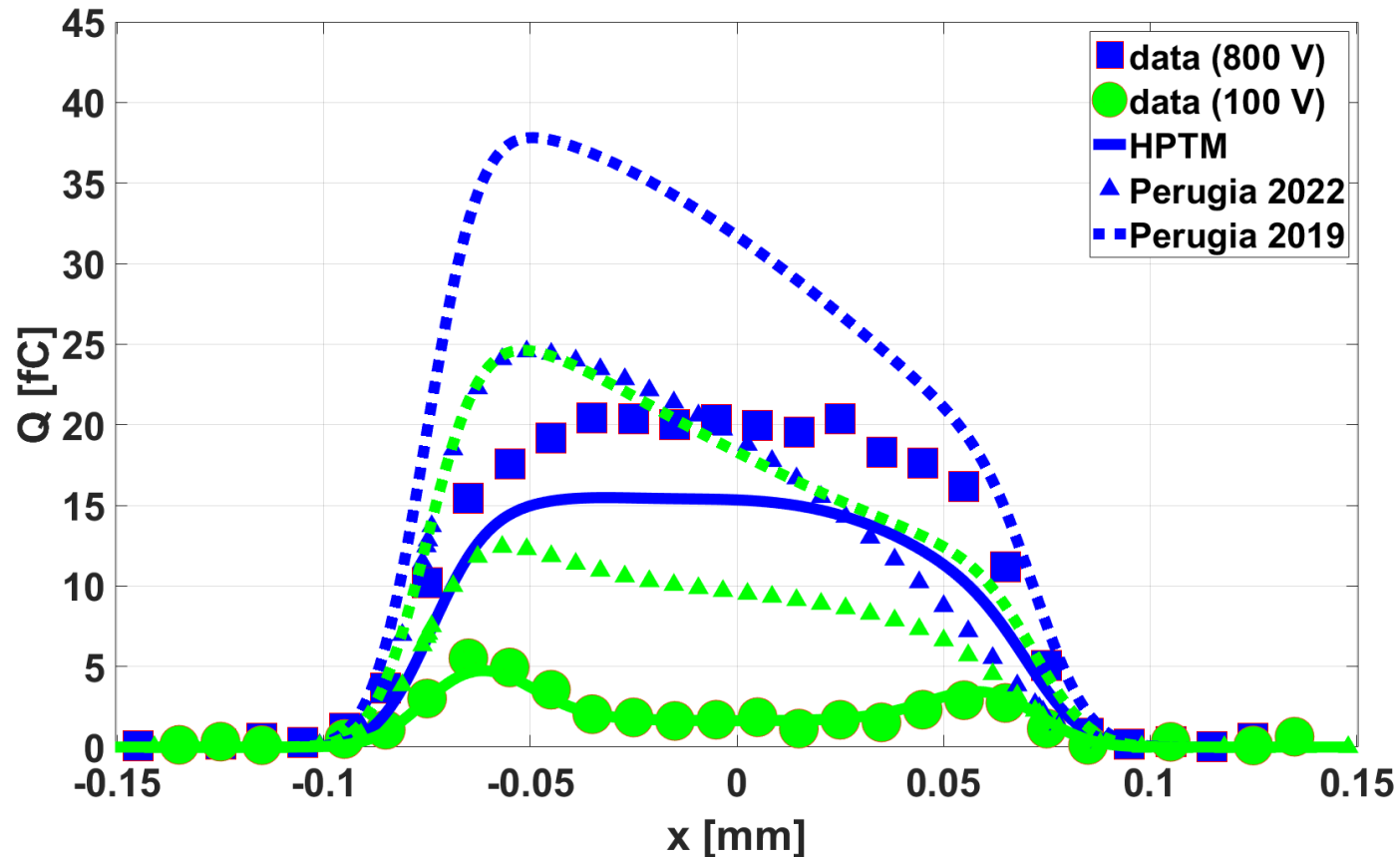
$$\Phi_{eq} = 8 \times 10^{15} \text{ cm}^{-2}$$



# Comparison with simulation results



$$\Phi_{eq} = 12 \times 10^{15} \text{ cm}^{-2}$$







Unfolding the measurements with respect to experimental effects:

$$Q_{sm}(x) = A \cdot \left( CCE_{spl}(x) \cdot \frac{E_{dep}(x)}{E_{dep}(0)} \right) * \text{Gauss}(x, 0, \sigma_{res})$$

$$CCE_{spl}(x) = \text{spline}(CCE_{x_i}), x_i = -65, -45, -25, -5, +15, +35, +55 \mu\text{m}$$

Minimizing the following function by taking  $CCE_{x_i}$  as free parameters:

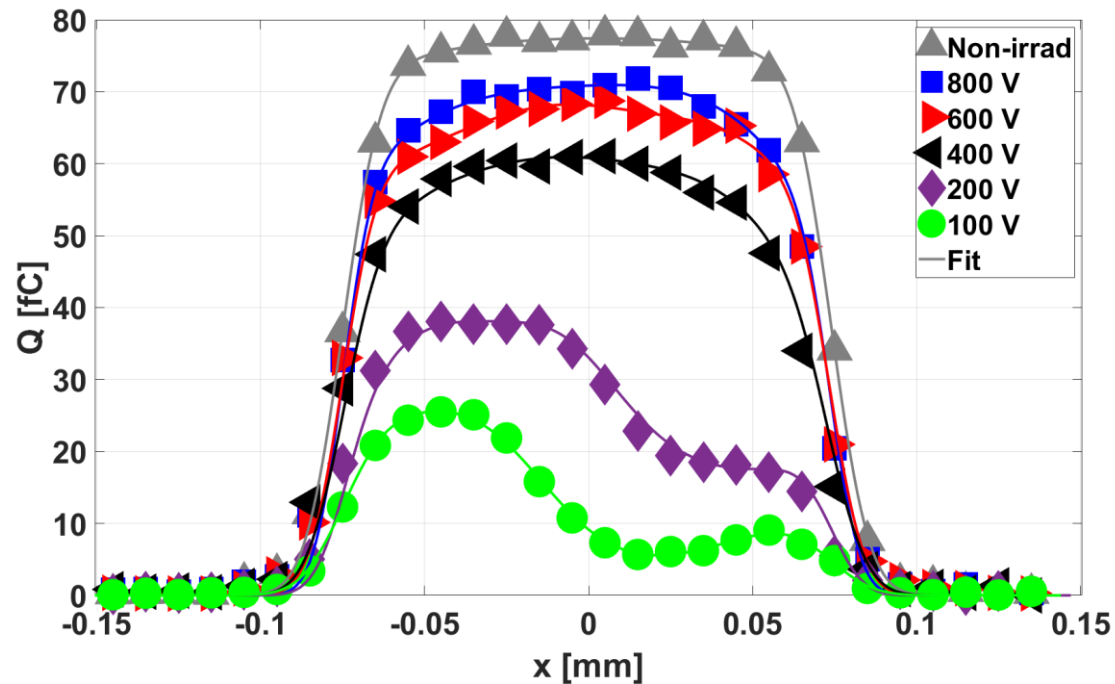
$$D^2 = \sum_k (Q_{meas}(x_k) - Q_{sm}(x_k + \Delta x_{tr}))^2 + w_{pen} \sum_{i=2}^6 \left( \frac{0.5(CCE_{x_{i+1}} + CCE_{x_{i-1}}) - CCE_{x_i}}{\Delta x} \right)^2$$

- A: scaling factor (76.8 for pad size of 25 mm<sup>2</sup> and 76.8 for pad size of 12.5 mm<sup>2</sup>)
- $\Delta x$ : distance between two adjacent points: 20  $\mu\text{m}$
- $\Delta x_{tr}$ : shift due the transformation from test-beam coordinate to the sensor coordinate system

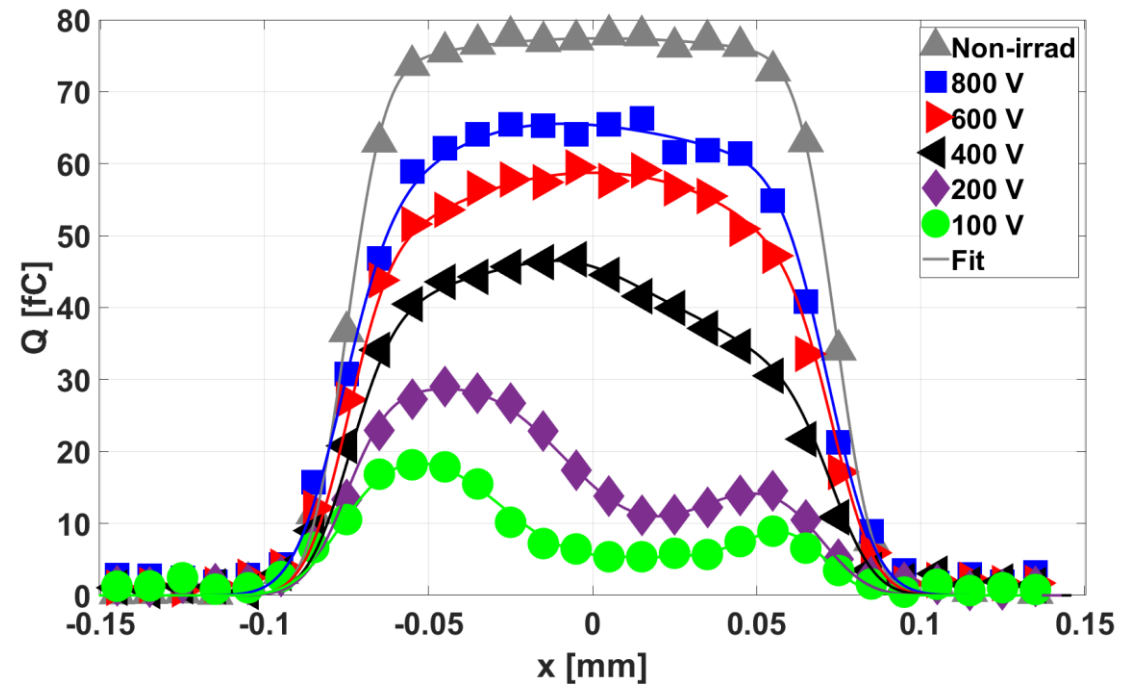
# Comparison with fit results



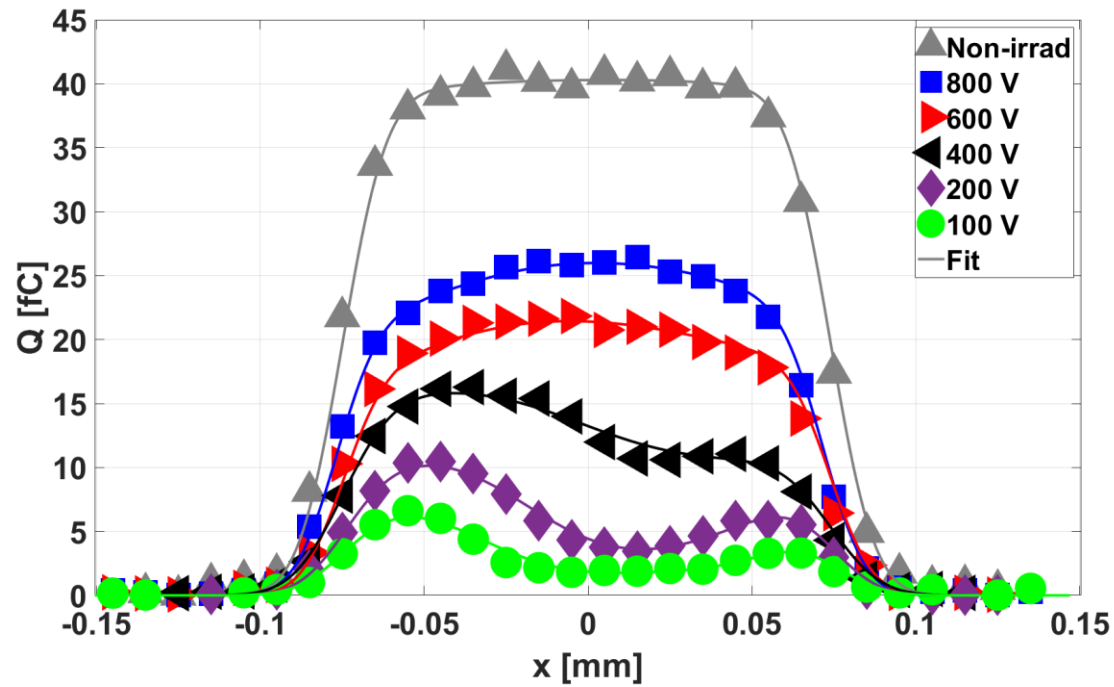
$$\Phi_{eq} = 2 \times 10^{15} \text{ cm}^{-2}$$



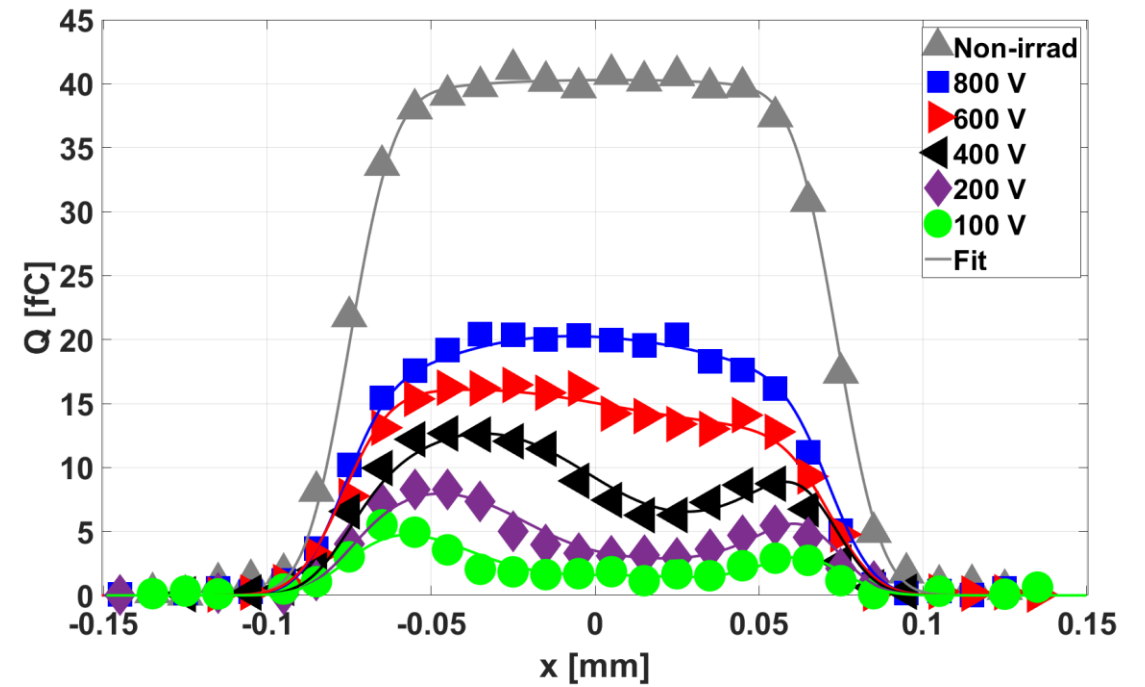
$$\Phi_{eq} = 4 \times 10^{15} \text{ cm}^{-2}$$



$$\Phi_{eq} = 8 \times 10^{15} \text{ cm}^{-2}$$



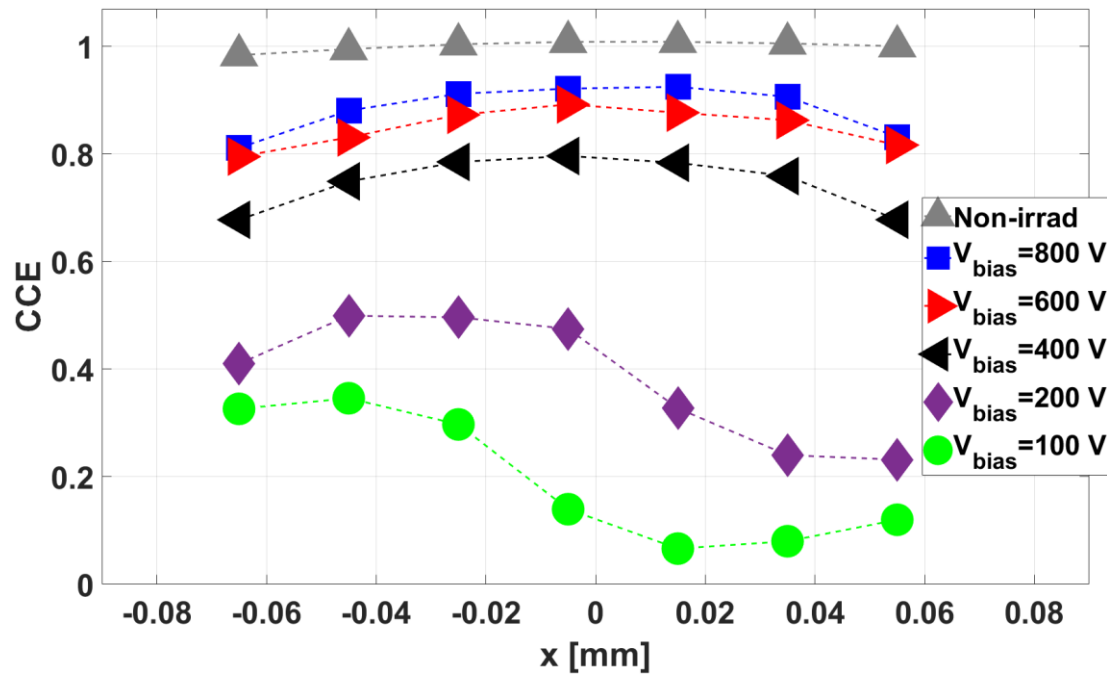
$$\Phi_{eq} = 12 \times 10^{15} \text{ cm}^{-2}$$



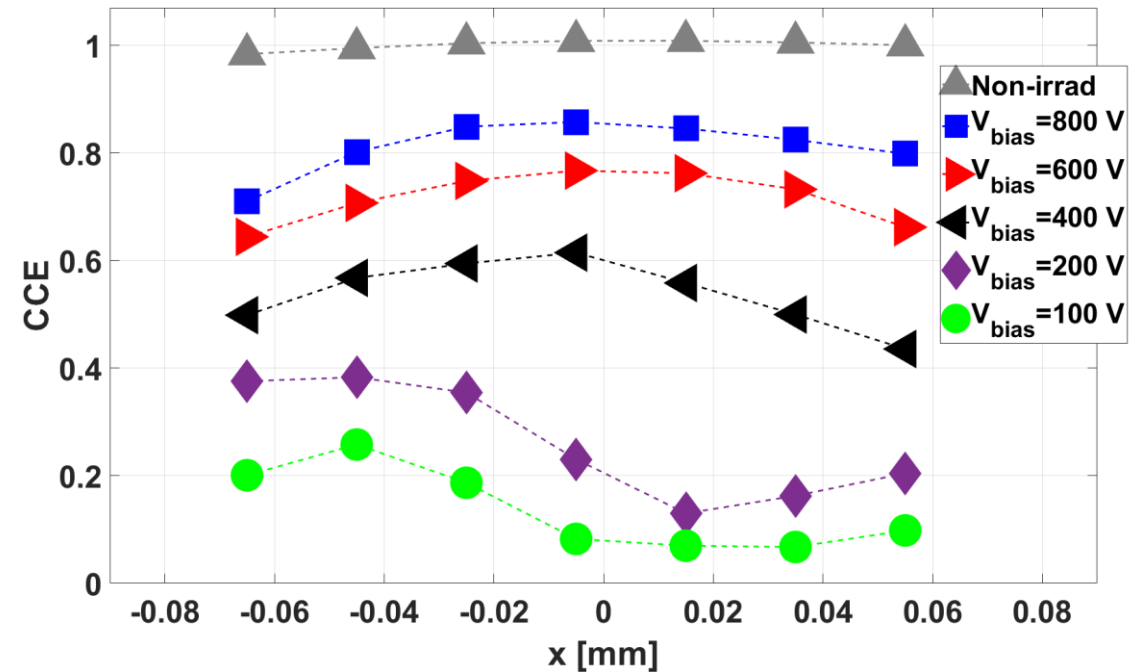
# CCE as a function of depth



$$\Phi_{eq} = 2 \times 10^{15} \text{ cm}^{-2}$$



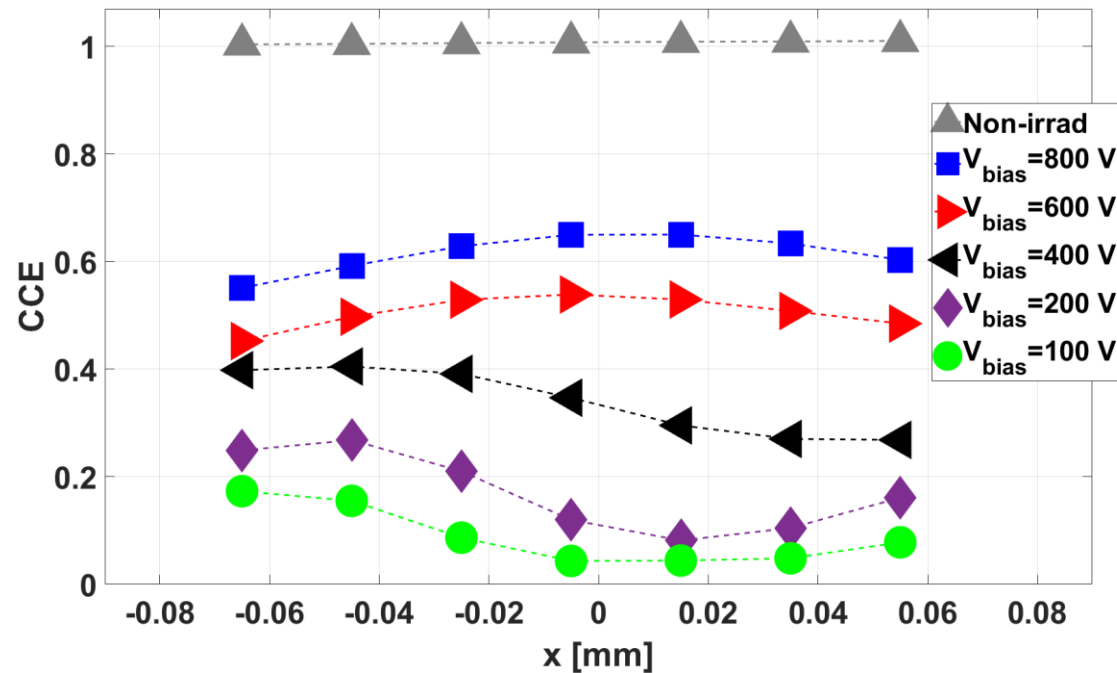
$$\Phi_{eq} = 4 \times 10^{15} \text{ cm}^{-2}$$



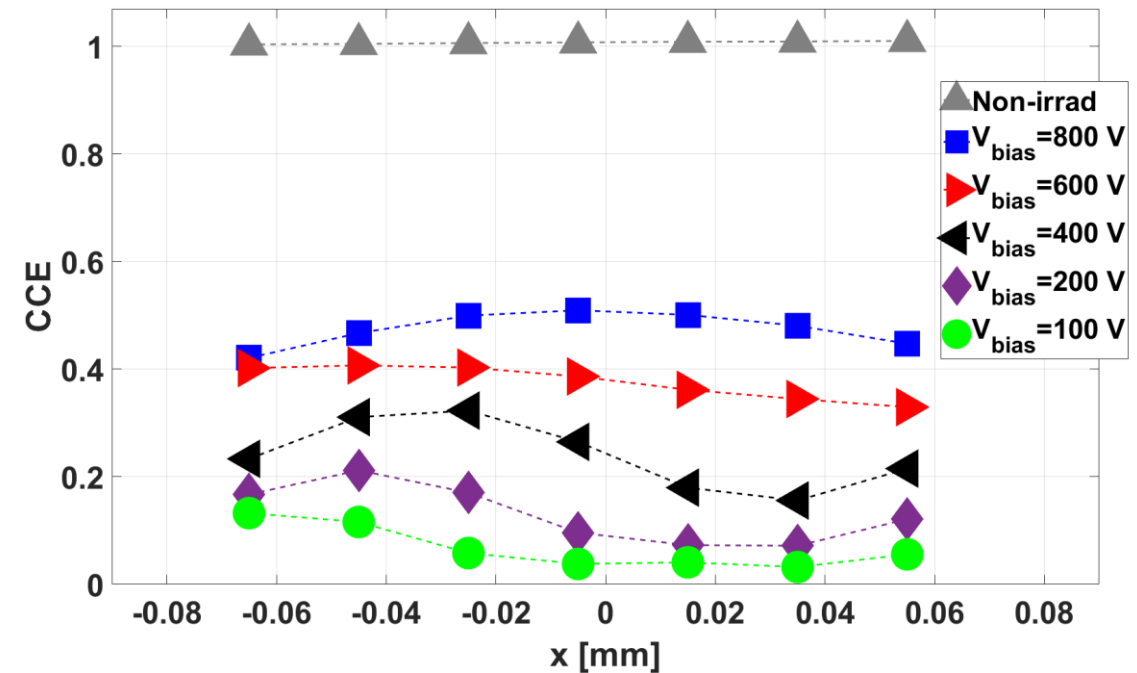
# CCE as a function of depth



$$\Phi_{eq} = 8 \times 10^{15} \text{ cm}^{-2}$$



$$\Phi_{eq} = 12 \times 10^{15} \text{ cm}^{-2}$$



# Summary and Conclusions



- Charge collection profiles of irradiated and non-irradiated diodes were measured.
- The data have been corrected for experimental effects: finite beam resolution and transverse energy leakage.
- These results provide a precise determination of the position dependence of the charge collection in radiation-damaged diodes.
- The precise CCE data can be used to tune and test radiation damage models.
- The procedure of comparing data to radiation damage models has been demonstrated for 3 models: HPTM and two Perugia models.

# Back up

## Charge distribution, non-irradiated diode

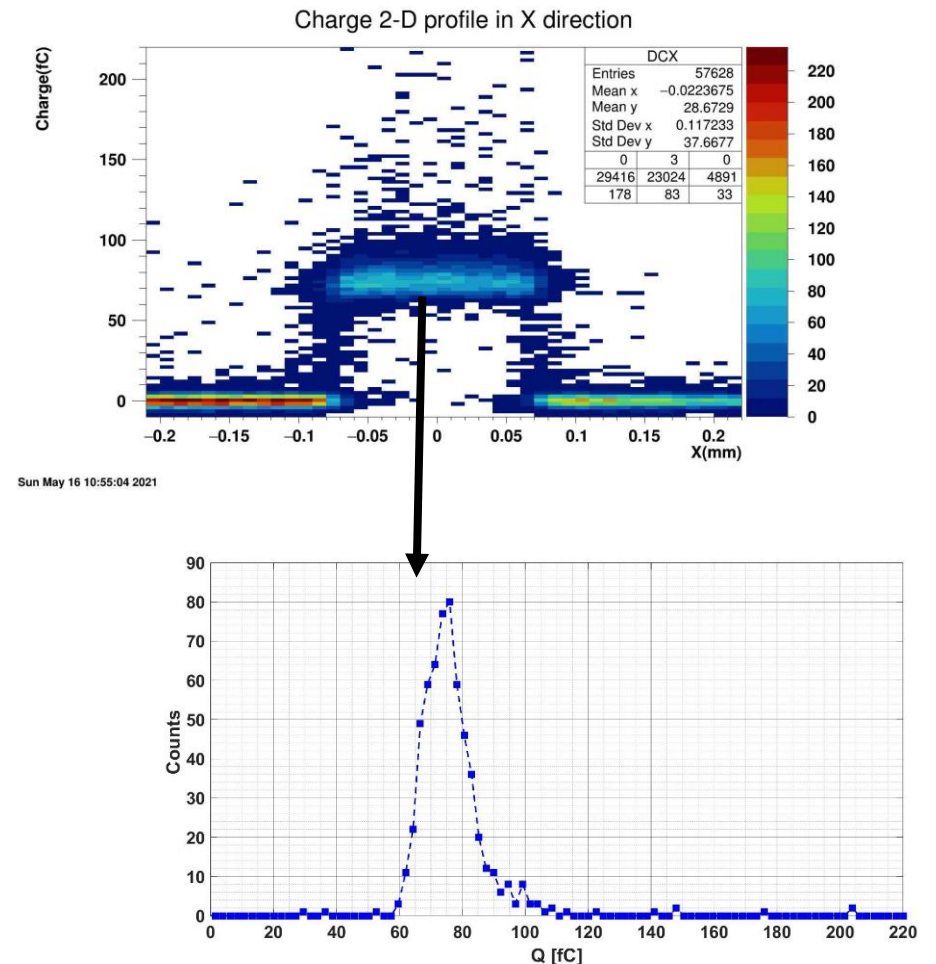


### Measurement conditions:

- Room temperature
- $V_{\text{bias}} = 120 \text{ V}$
- $\theta : 0^\circ$
- $E_{\text{beam}} = 5.2 \text{ GeV}$
- Beam divergence:  $\pm 1 \text{ mrad}$

### Observations:

- In the central region of the diode (i.e.  $0.07 \text{ mm} < X < 0.07 \text{ mm}$ ) the collected charge is well above the noise level
- Data taking without zero suppression enables us measuring very low charges (relevant for irradiated diodes)

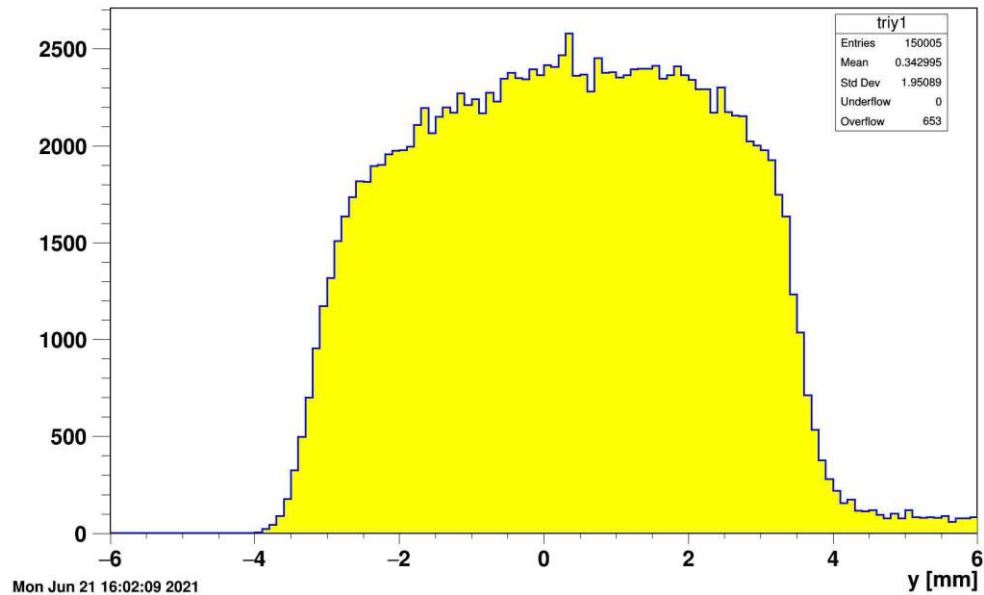


# Back up Geometrical cuts



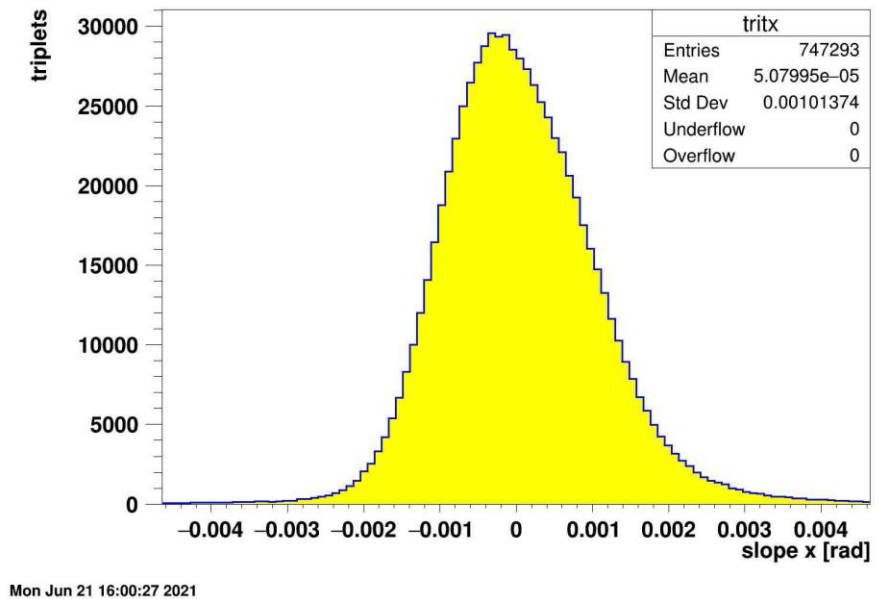
$$|y_{\text{dut}}| < 2.0 \text{ mm}$$

triplets y



$$|\theta_x| < 1 \text{ mrad}$$

triplet slope x

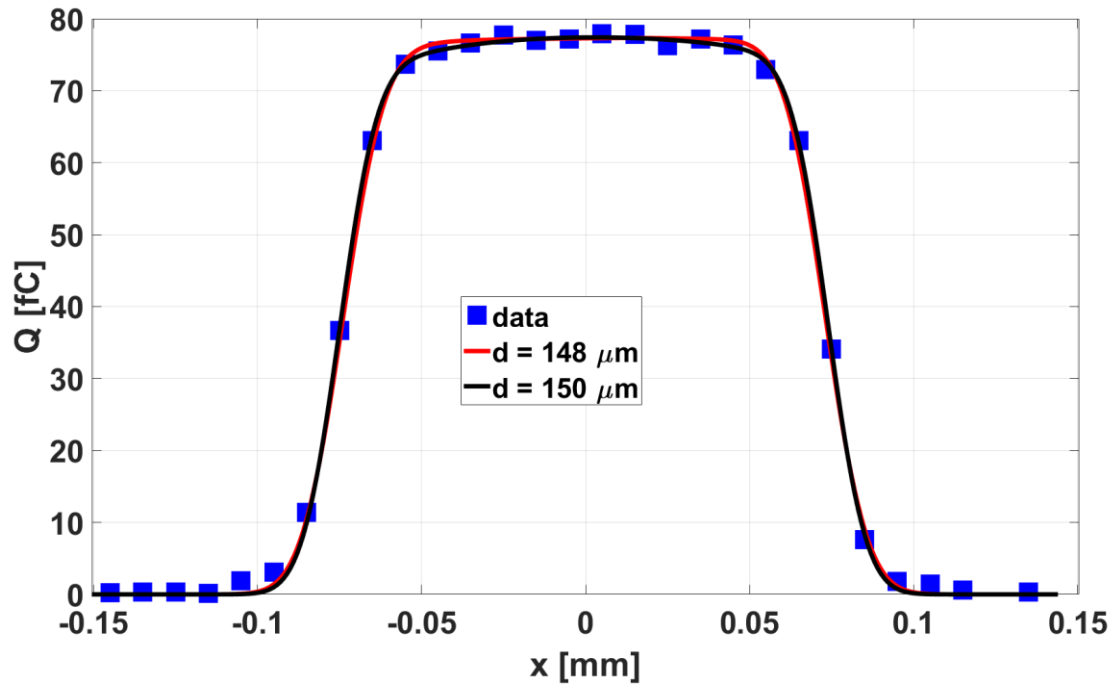




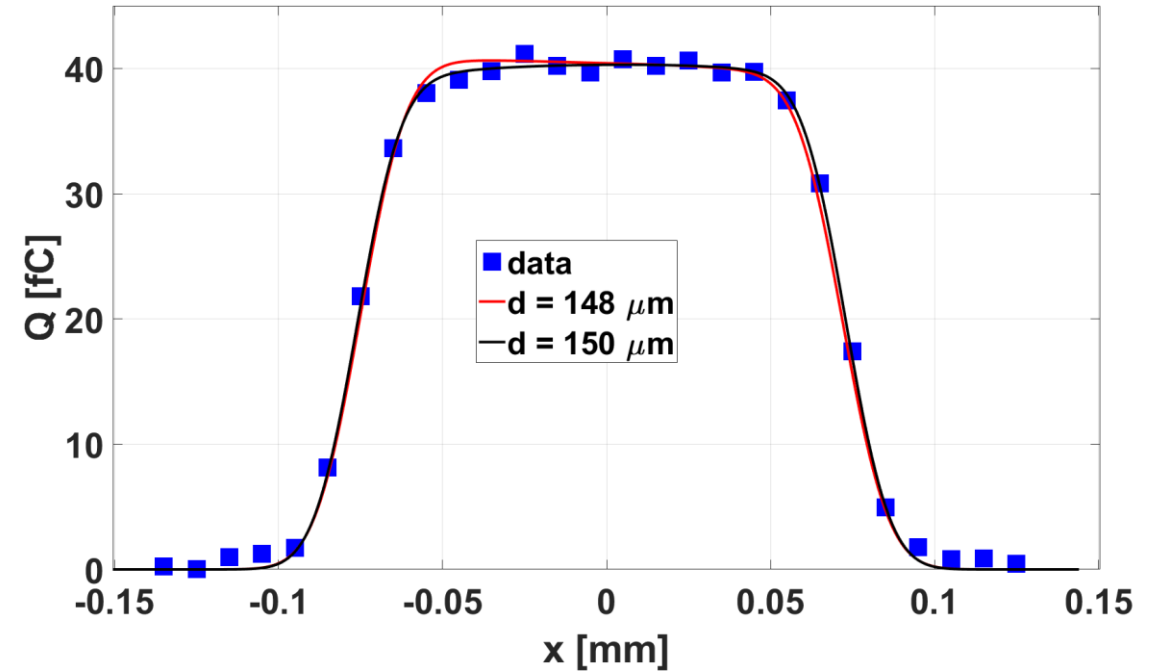
# Back up Extracted CCE for different thicknesses



$5 \times 5 \text{ mm}^2$



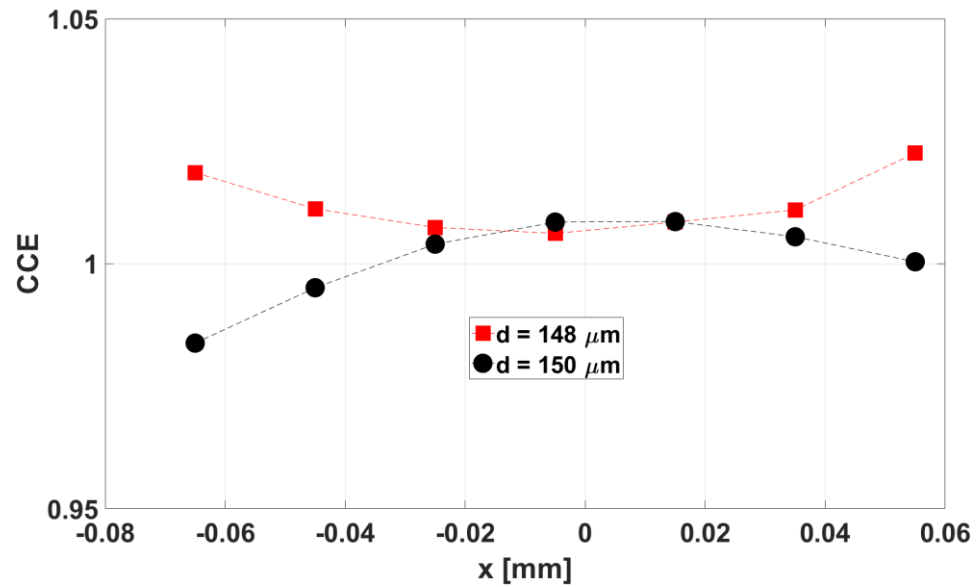
$2.5 \times 2.5 \text{ mm}^2$



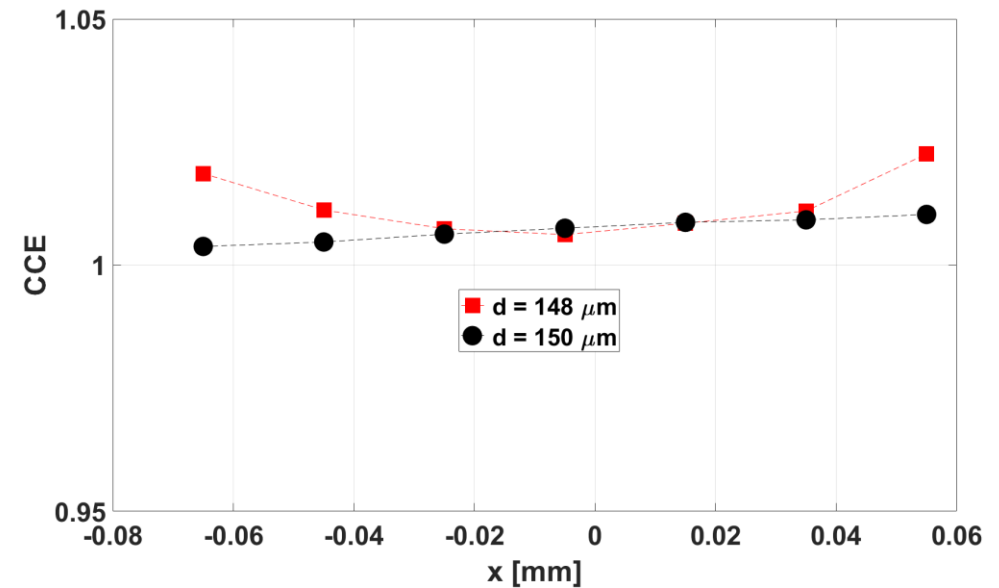
# Back up Extracted CCE for different thicknesses



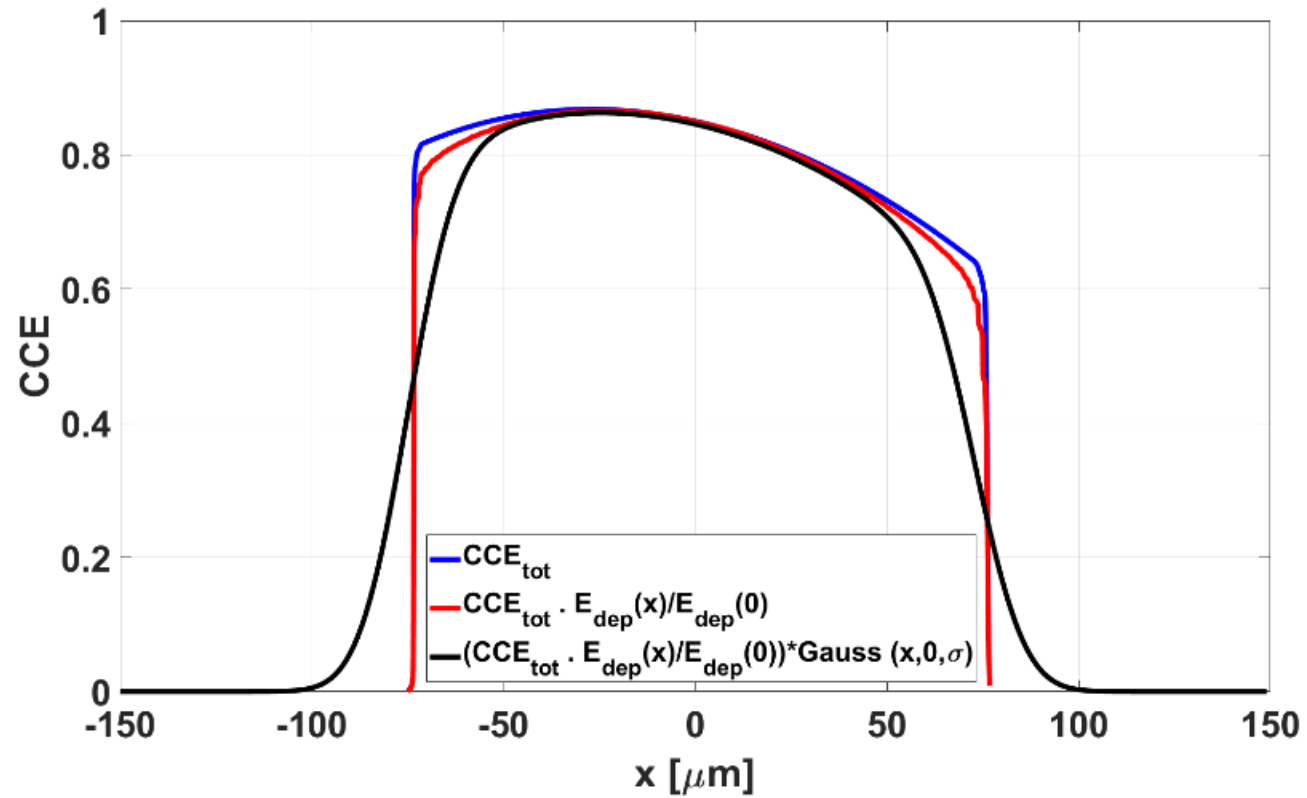
$5 \times 5 \text{ mm}^2$



$2.5 \times 2.5 \text{ mm}^2$



# Back up GEANT4 simulation result



# Back up

## CCE as a function of bias voltage



Measurement conditions:

- Temperature: -20 C
- $V_{\text{bias}} = 100 - 800 \text{ V}$

DUTs:

- Proton irradiated at  $\Phi_{\text{eq}} = 2, 4, 8, 12 \times 10^{15} \text{ cm}^{-2}$

CCE is calculated as:

$$\text{CCE}(V_{\text{bias}}) = \frac{\sum_{x=-150 \mu\text{m}}^{+150 \mu\text{m}} Q_{x,\text{irradiated}}(V_{\text{bias}})}{\sum_{x=-150 \mu\text{m}}^{+150 \mu\text{m}} Q_{x,\text{non-irradiated}}}$$

