

# Silicon at Extreme Fluences

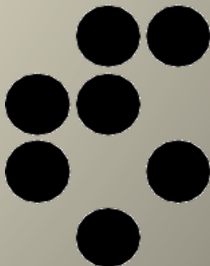
**M.Mikuž**

**University of Ljubljana & Jožef Stefan Institute**

ECFA Detector R&D Roadmap

TF3 Solid State Detectors

Zoom, April 23<sup>rd</sup>, 2021



# Extreme ?

- What is extreme ?

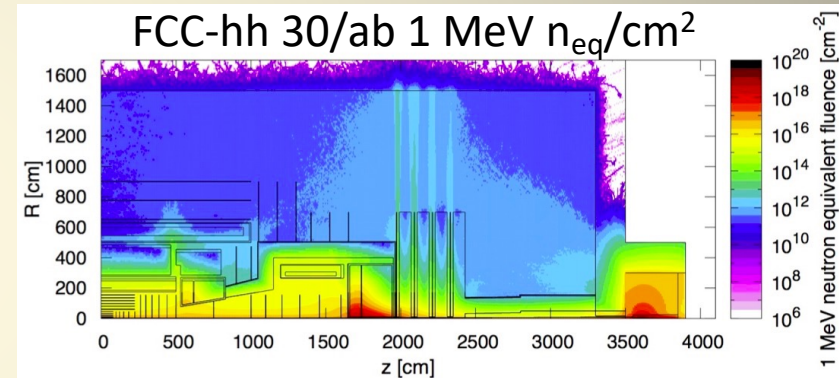
**extreme** (ɪk'stri:m)

adj

1. being of a high or of the highest degree or intensity: *extreme cold*; *extreme difficulty*.
2. exceeding what is usual or reasonable; immoderate: *extreme behaviour*.

- A rather subjective measure

- for LHC  $10^{15}$   $n_{eq}/cm^2$  was considered extreme
  - design was 730/fb @14TeV...
- HL-LHC takes it to  $nx10^{16}$  (vertex) or even  $10^{17}$  (FW calo)
  - 4000/fb @14TeV
- FCC-hh is *specifying* towards  $10^{18}$  for the tracker (*M. Aleksa: FCC-hh req's*)
  - 30/ab @100TeV
  - 300 MGy TID in addition (not addressed)
- Ratio 1:20:600 !
  - well, you need  $\sim 7^2 \approx 50$  in HL/FCC lumi...
- What is the limit of tracking sensors ?
  - TRIGA, NPP and ITER are  $10^{21} \leftrightarrow 10^{24}$



## Central tracker:

- first IB layer (2.5 cm):  $\sim 5-6 \cdot 10^{17} cm^{-2}$
- external part:  $\sim 5 \cdot 10^{15} cm^{-2}$

## Forward calorimeters:

$\sim 5 \cdot 10^{18} cm^{-2}$  for both the EM and the HAD-calo

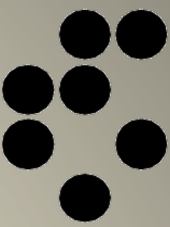


# Expectations for $10^{17} n_{eq}/\text{cm}^2$

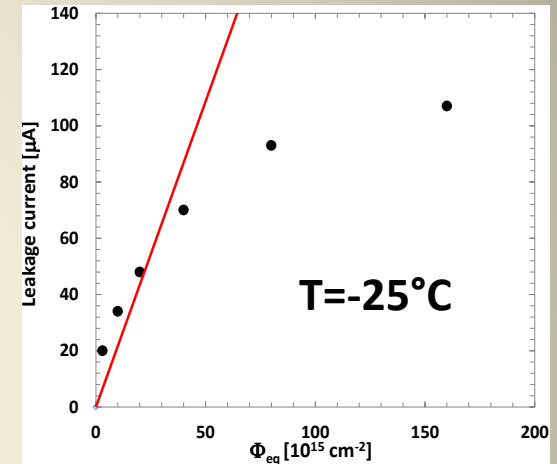


- For a ~yearly replacement of FCC-hh inner tracker !
- Linear extrapolation from low fluence data
  - Current:  $I_{leak} = 4 \text{ A/cm}^3 @ 20^\circ\text{C}$ 
    - $2 \text{ mA/cm}^2$  (2W @ 1 kV) for 300  $\mu\text{m}$  thick detector @  $-20^\circ\text{C}$
  - Depletion:  $N_{eff} \approx 1.5 \times 10^{15} \text{ cm}^{-3}$ 
    - $FDV \approx 100 \text{ kV}$
  - Trapping  $\tau_{eff} \approx 1/40 \text{ ns} = 25 \text{ ps}$ 
    - $Q \approx Q_0/d v_{sat} \tau_{eff} \approx 80 \text{ e}/\mu\text{m} \cdot 200 \mu\text{m}/\text{ns} \cdot 1/40 \text{ ns} = 400 \text{ e}$  in very high electric field ( $\gg 1 \text{ V}/\mu\text{m}$ )
- Looks much like *Mission Impossible* (part n...)

# CCE measurements up to $1.6 \times 10^{17} \text{ n}_{\text{eq}}/\text{cm}^2$



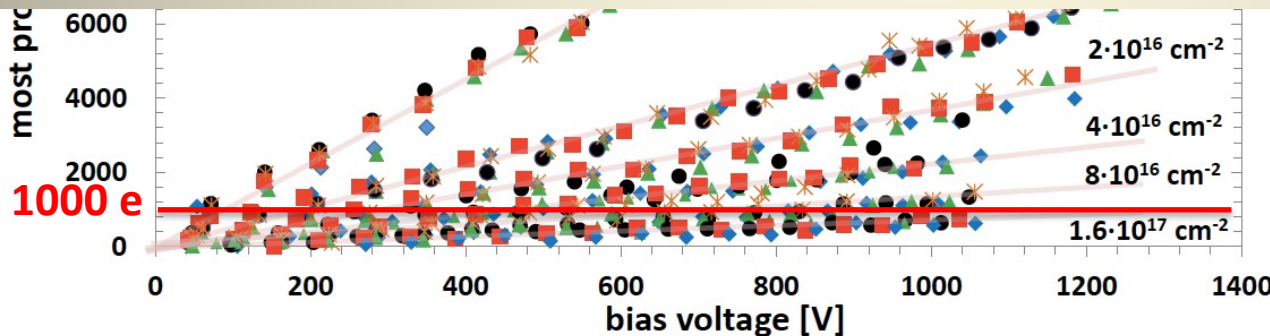
- n<sup>+</sup>p "spaghetti" strips, 300 μm
- Observed signal not at all compatible with expectations
  - Above  $3 \times 10^{15}$  linear CCE( $V_{\text{bias}}$ )
  - Power law scaling with fluence,  $b \approx -2/3$
  - Leakage current "saturating"



$$Q_{MPV}(V, \Phi) = k \cdot (\Phi / 10^{15} \text{ n}_{\text{eq}}/\text{cm}^2)^b \cdot V$$

$$k = 26.4 \text{ e}_0/\text{V}$$

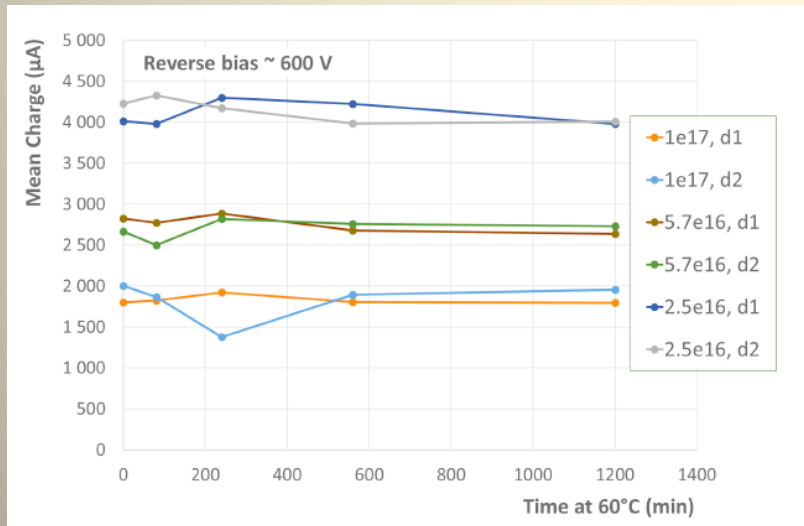
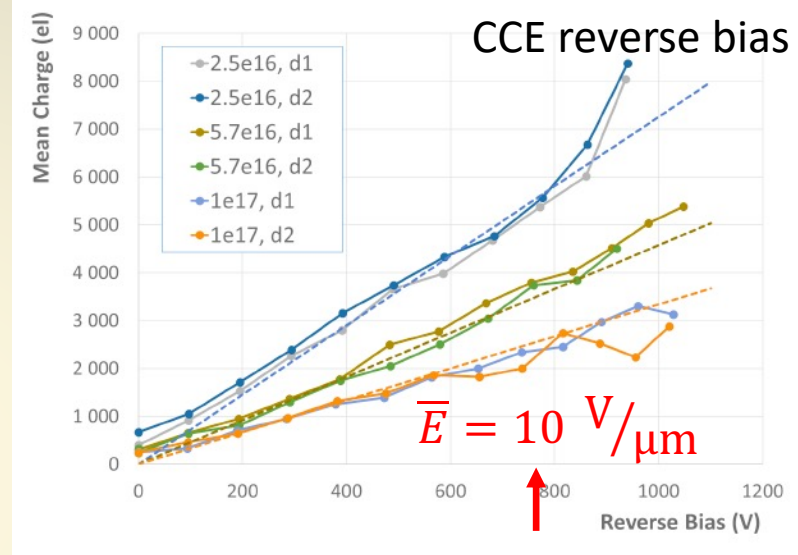
$$b = -0.683$$



From:  
**G. Kramberger et al.,  
 JINST 8 P08004 (2013).**

# More measurements on thin detectors

- 75  $\mu\text{m}$  epi detectors from CNM on low-resistivity substrate
- Irradiated to 0.25, 0.57 and  $1.0 \times 10^{17} \text{ n}_{\text{eq}}/\text{cm}^2$
- CCE in reverse and FW
- Annealing 1200 min @  $60^\circ\text{C}$



$$Q_{\text{mean}} = k \cdot \phi^b \cdot V$$

$$k_{75} = 44 \text{ e}_0/\text{V}$$

$$b_{75} = -0.56$$

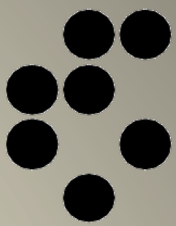
Thinner is better!

From:

I.Mandić et al.,  
**JINST 15 P11018 (2020).**

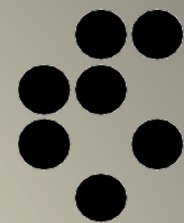


# Linear $CCE(V)$ ??



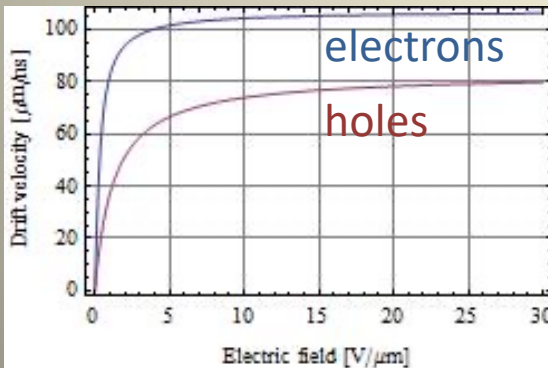
- What could be linear
  - SCR governed  $CCE(V)$  after irradiation ( $\sqrt{V}$ ), highly resistive ENB ( $\sqrt{V}$ ), without trapping
  - Trapping dominated with non-saturated drift velocity
- What is *not* linear
  - velocity saturation
  - charge multiplication
  - double junction
  - field in ENB
  - ...
- Just a nice coincidence or some physics behind ?
  - look *into* silicon to search for an answer
- Using edge-TCT to probe silicon

# Electric Field Measurement

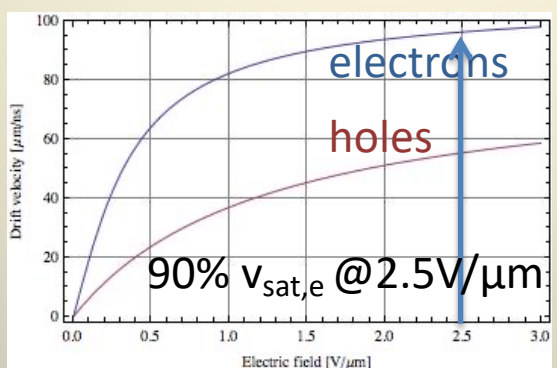


- Initial signal proportional to velocity sum at given detector depth
- Caveats for field extraction
  - Transfer function of electronics smears out signal, snapshot taken at  $\sim 600$  ps
    - Problematic with heavy trapping
    - Electrons with  $v_{sat}$  hit electrode in 500 ps
  - Mobility depends on  $E$ 
    - $v$  saturates for  $E \gg 1\text{V}/\mu\text{m}$

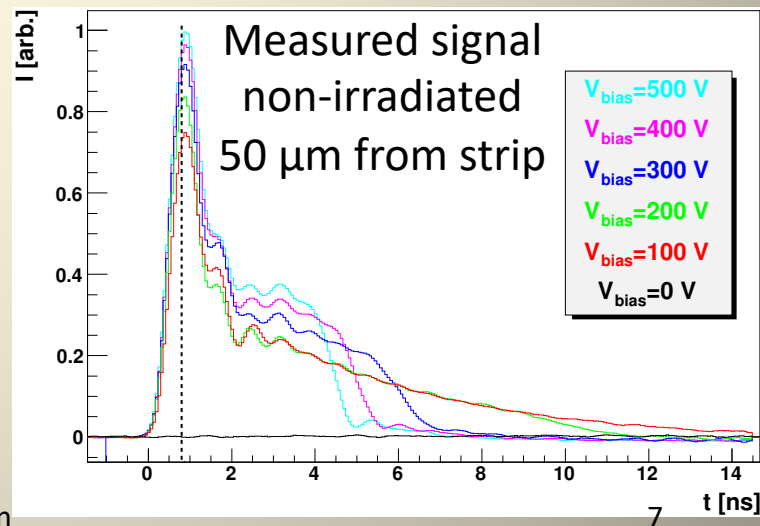
$$\begin{aligned}
 I(t=0) &= q \cdot \vec{v} \cdot \vec{E}_w = \\
 &= N_{e-h} e_0 \cdot (v_e + v_h) / d = \\
 &= N_{e-h} e_0 \cdot (\mu_e + \mu_h) \cdot E(x) / d
 \end{aligned}$$



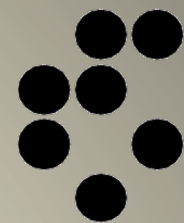
ECFA-DRM TF3, 23/4/2021



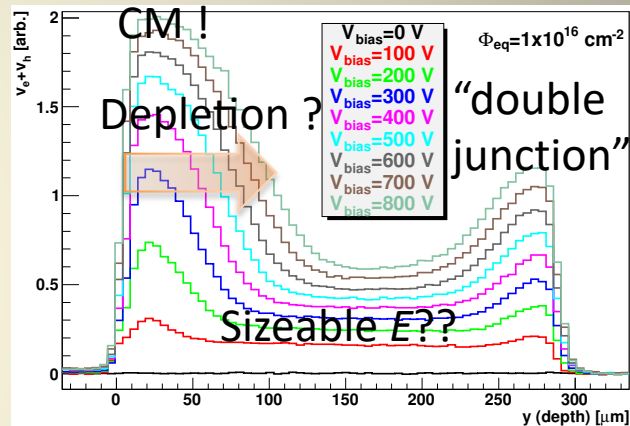
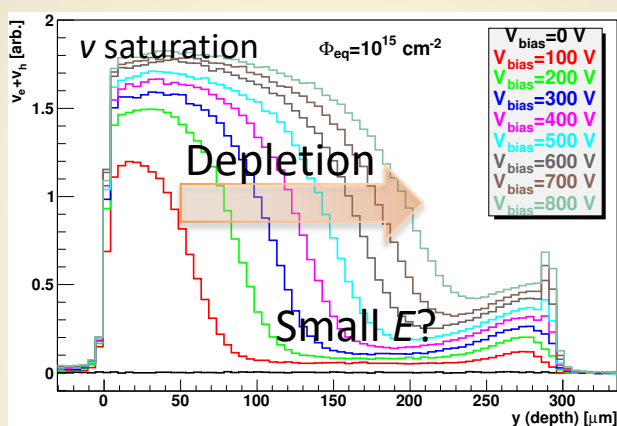
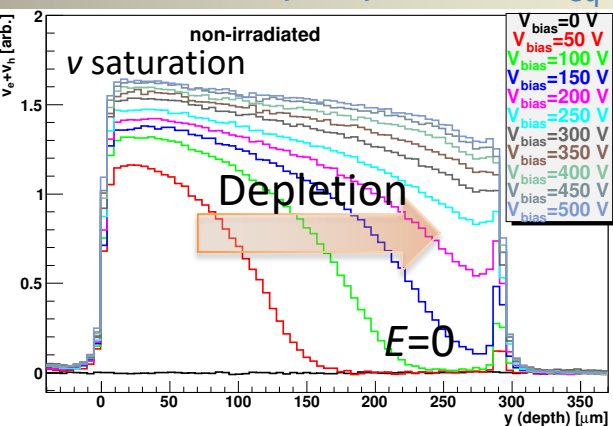
Marko Mikuž: Extreme Silicon



# Selected Results from Neutrons



- Hamamatsu ATL07 n<sup>+</sup> mini-strip, FZ p-type, neutron irradiated at JSI TRIGA reactor
  - In steps up to 10<sup>16</sup> n<sub>eq</sub>/cm<sup>2</sup>



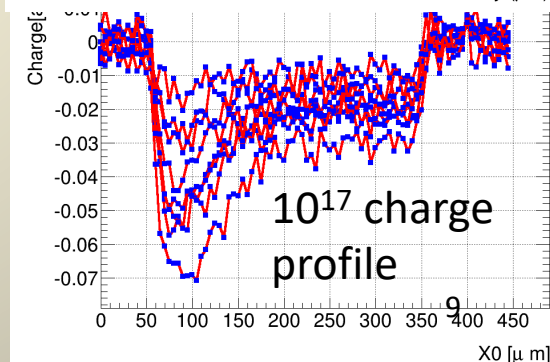
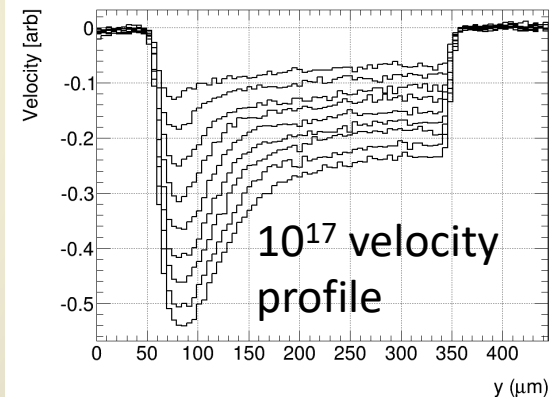
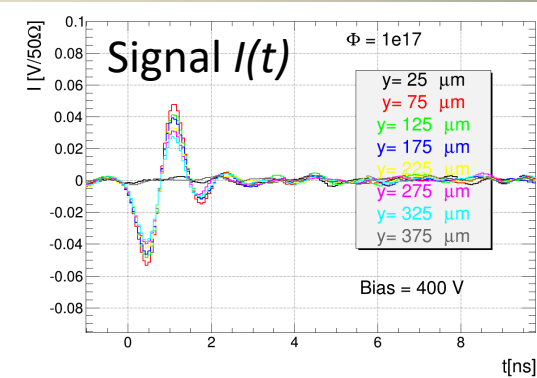
- Very instructive regarding qualitative electric field shape
  - Non-irradiated “by the book” for abrupt junction n<sup>+</sup>p diode
    - SCR and ENB nicely separated, small double junction near backplane
  - Medium fluence ( $\Phi = 10^{15}$  neutrons): some surprise
    - Smaller space charge than expected in SCR, some field in “ENB”
  - Large fluence ( $\Phi = 10^{16}$ ): full of surprises
    - Still lower space charge, sizeable field in “ENB”
    - Charge multiplication (CM) additional trouble for interpretation at large V
- Nice, but let's try to get *quantitative* !

Published in :  
G. Kramerger et al.,  
JINST 9 P10016(2014).

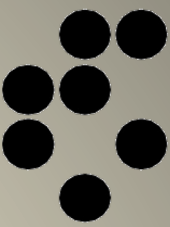


# Extending the Reach

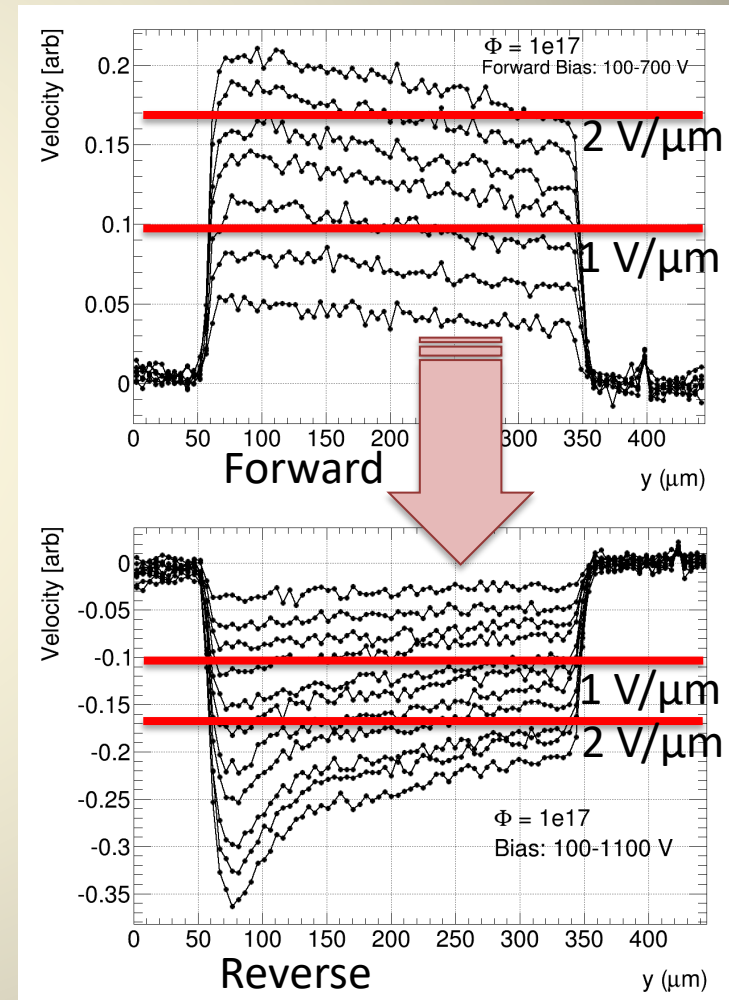
- In 2014 added  $5 \times 10^{16}$  and  $10^{17}$   $n_{eq}/\text{cm}^2$  measurements of the same detector
  - $10^{16}$  of this fluence fully annealed, the rest 80 min @  $60^\circ\text{C}$
- Intrinsic feature – signal oscillations
  - period  $\sim 5/4$  ns
  - LRC ( $C \sim 2\text{pf} \Rightarrow L \sim 20\text{ nH} \sim 1\text{cm}$  of wire)
- Velocity (slope) and charge (integral) yield consistent results
- should be, as  $Q \approx Q_0 v_{sum} \tau_{eff} / d$



# Absolute Field Measurement

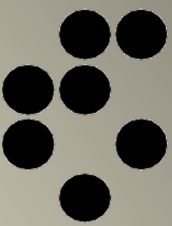


- Solution: *concurrent* forward bias  $V_{sum}$  measurements
  - Ohmic behaviour with some linear (field) dependence
    - constant (positive) space charge
  - can use  $\int E(y) dy = \bar{E}d = V$  to pin down field scale
    - corrections from  $v(E)$  non-linearity small
- Use same scale for reverse bias!
- FW measurements up to 700 V
  - know  $E$  scale up to 2.33 V/ $\mu\text{m}$
  - can reveal  $v(E)$  dependence





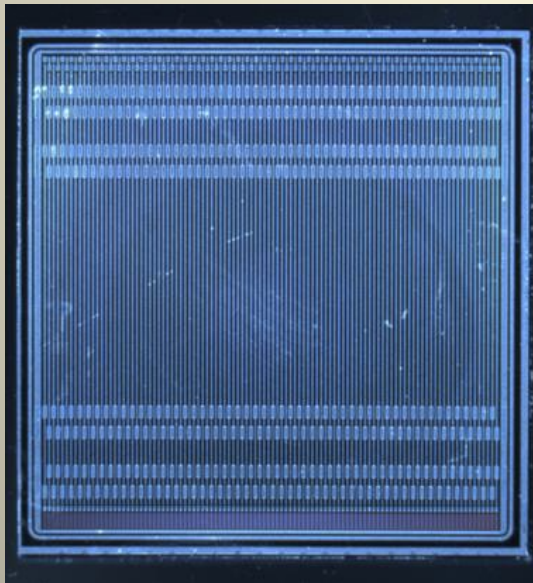
# Proton Irradiations



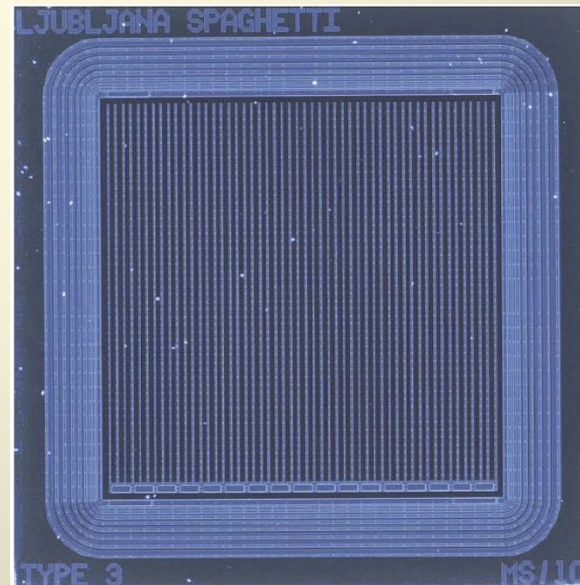
- 5 sample pairs of ATL12 mini-strips irradiated at CERN PS during summer 2015
  - got 0.5, 1.0, 2.9, 11, 28e15 protons/cm<sup>2</sup>, no scanning
  - NIEL hardness factor 0.62
  - thanks to CERN IRRAD team
    - took 41 PS days to reach the highest fluence
- Covers HL-LHC tracker range well
  - does really not look practical for 10<sup>17</sup>++
- 2 samples per fluence investigated by E-TCT for all fluences
  - concurrent forward and reverse bias measurements

# Additional irradiations

- $3e17$   $n_{eq}/cm^2$ , JSI reactor neutrons
  - A12 mini,  $7 \times 8$  mm<sup>2</sup>, 75  $\mu$ m pitch, 300  $\mu$ m thick
    - Also to  $3e16$ ,  $1e17$
  - Spaghetti:  $4 \times 4$  mm<sup>2</sup>, n-on-p, strip pitch 80  $\mu$ m, 300  $\mu$ m thick, strips connected together at side
    - $1.6e17$  received previously,  $4.6e17$  total

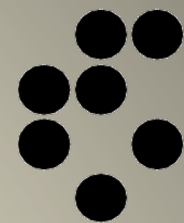


A12

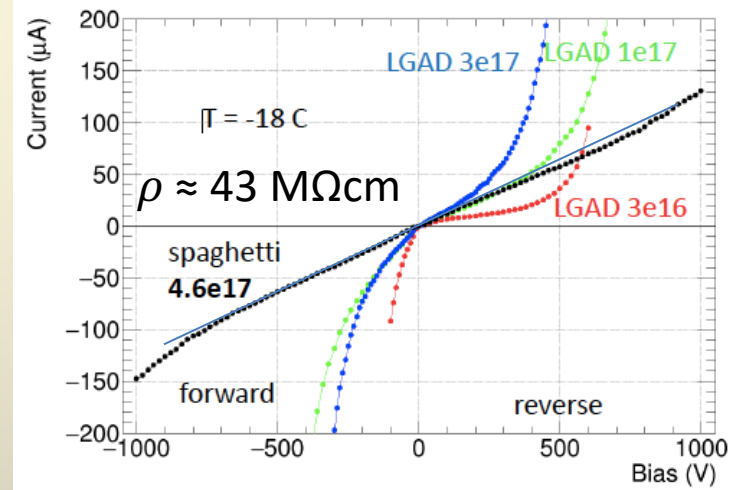
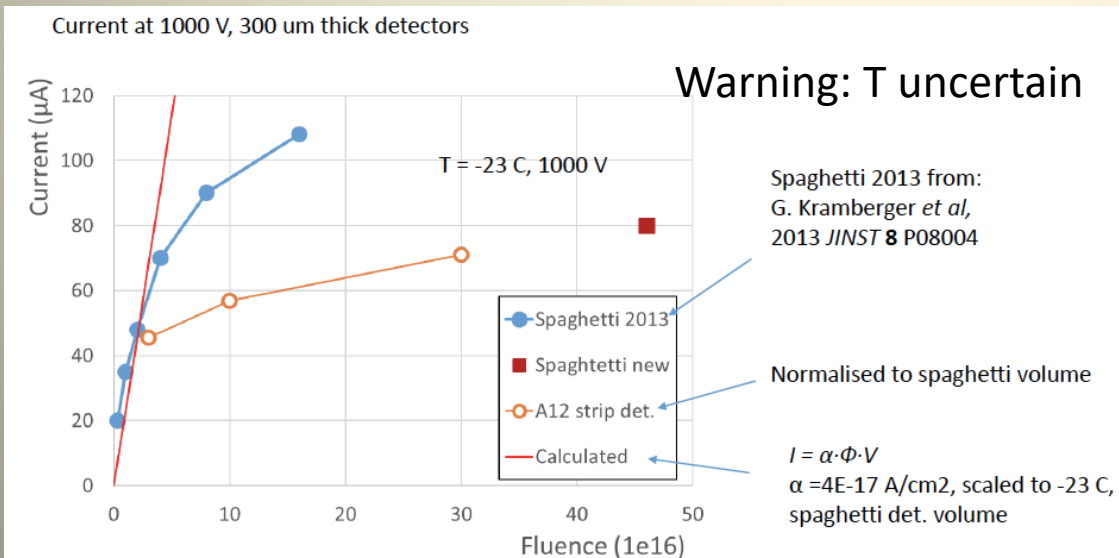
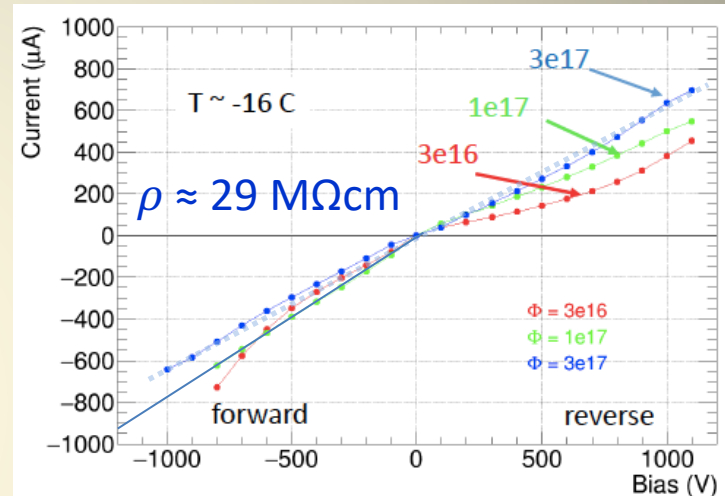


Spaghetti

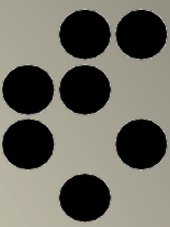
# Basic measurements



- $I$ - $V$  for 3&4.6e17 looks very linear with little difference between reverse/FW bias
  - No breakdown, as observed in LGAD's
- $I$  @1000 V does not scale linearly with fluence !
  - Not governed by generation current ?
- Tried to measure 4.6e17 spaghetti CCE with  $^{90}\text{Sr}$ 
  - No signal above background observed up to 320 V
  - Magic formula predicts 120e for 4.6e17 @320 V



# Mobility Considerations FW bias

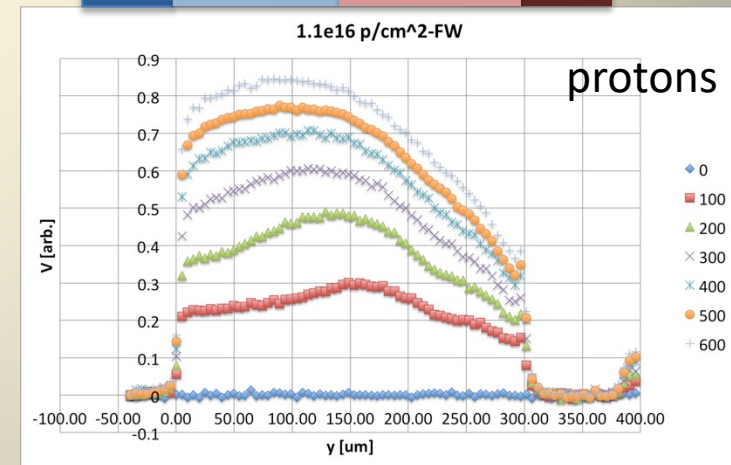
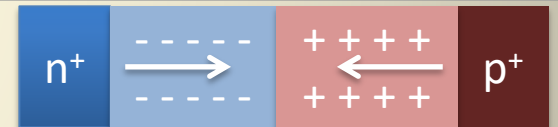
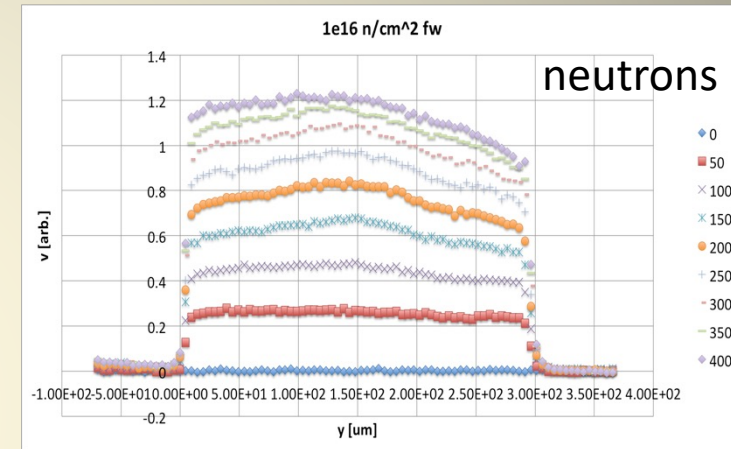


- For forward bias can extract  $v(E)$  up to a scale factor
- Observe less saturation than predicted
- Model with

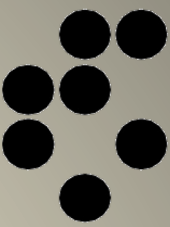
$$v_{sum}(E) = \frac{\mu_{0,e}E}{1 + \frac{\mu_{0,e}E}{v_{e,sat}}} + \frac{\mu_{0,h}E}{1 + \frac{\mu_{0,h}E}{v_{h,sat}}}$$

- keep saturation velocities at nominal values @-20°C ( $v_{e,sat} = 107 \mu\text{m/ns}$ ;  $v_{h,sat} = 83 \mu\text{m/ns}$ )
- float (common) zero field mobility degradation
- fit  $v(E)$  for  $\phi_n \geq 5 \times 10^{15}$  and  $\phi_p \geq 3 \times 10^{15}$

n.b. FW profiles less uniform for lower fluences & protons; departures from average field still small, corrections  $O(\%)$

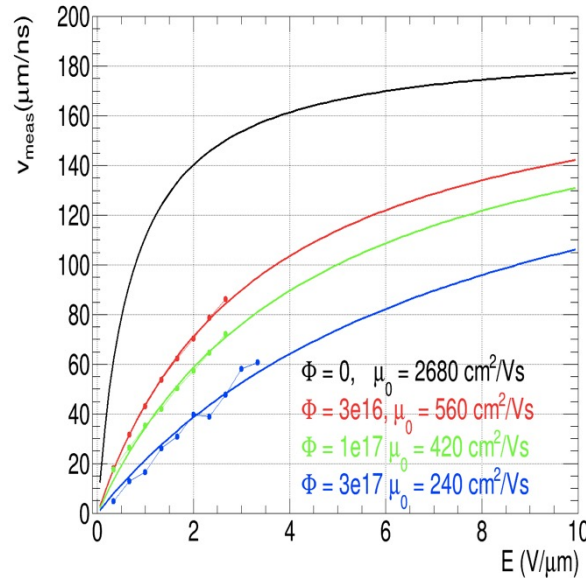
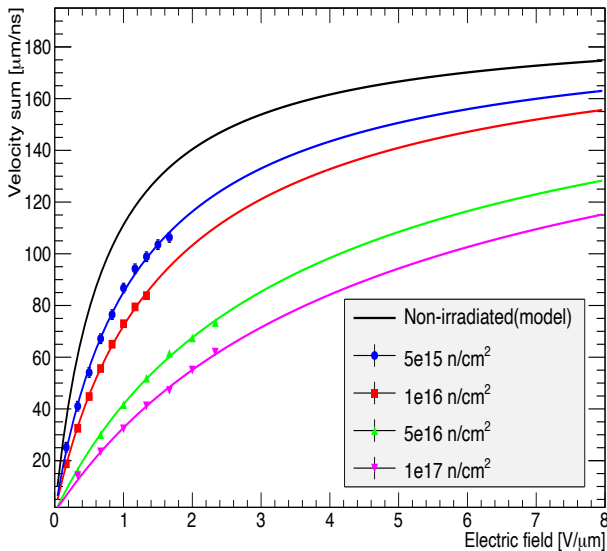


# Mobility Fits

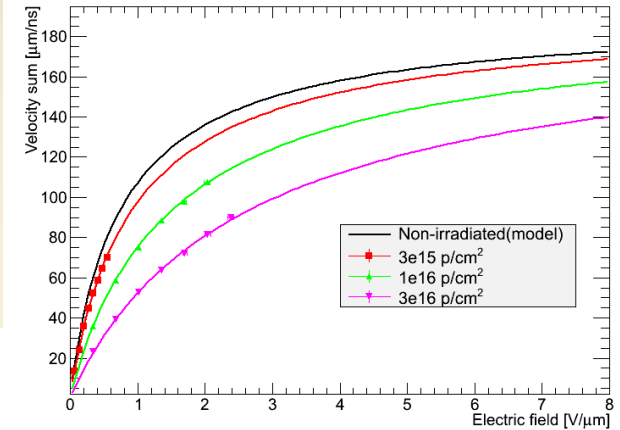


- Data fits model almost perfectly
  - $\mu_0$  degradation the only free parameter, scale fixed by  $v_{sum,sat}$
  - At  $3e17$  E range too limited ( $v(E)$  linear), regard result as upper limit

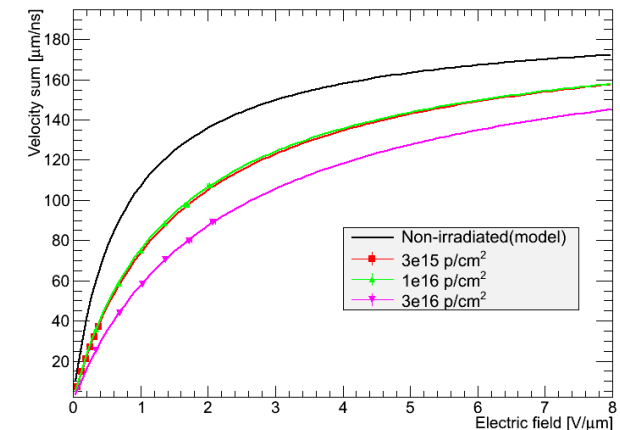
Mobility neutrons



Mobility protons A

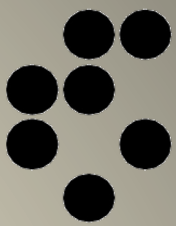


Mobility protons B





# Mobility Results

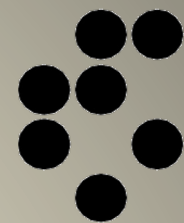


- Fit to  $v_e + v_h$  with common mobility degradation factor
  - factor of **2** at  $10^{16} n_{eq}/cm^2$ , **6** at  $10^{17} n_{eq}/cm^2$ , **>10** at  $3 \times 10^{17} n_{eq}/cm^2$
  - need **2x/6x/>10** higher  $E$  to saturate  $v$  !
- ☠ correspondingly higher  $E$  for charge multiplication !

$\Phi_n$	$\mu_{0,sum}$	$\Phi_p$	$\mu_{0,sum}$
[ $10^{15} n_{eq}/cm^2$ ]	[ $cm^2/Vs$ ]	[ $10^{15} n_{eq}/cm^2$ ]	[ $cm^2/Vs$ ]
non-irr (model)		2680	
5	$1661 \pm 134$	1.6	$2063 \pm 188$
10	$1238 \pm 131$	6.1	$1337 \pm 47$
30	560	15.4	$817 \pm 42$
50	$555 \pm 32$		
100	$407 \pm 40$		
100	420	<b>T=-20°C</b>	
300	<240		



# Mobility Analysis



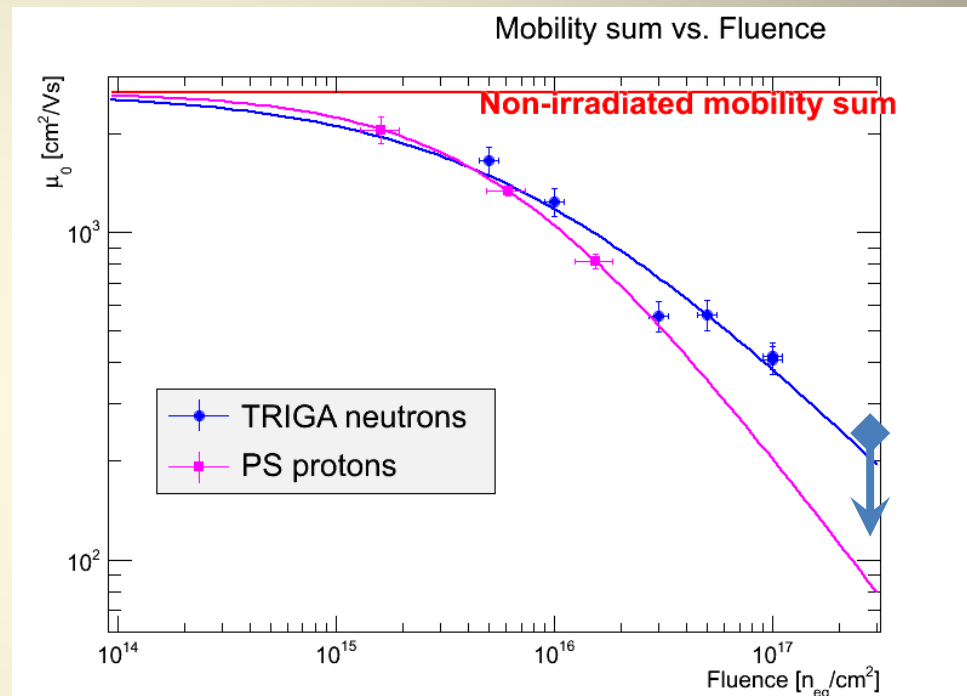
- Mobility governed by hard scattering on acoustic phonons and traps

$$\frac{1}{\tau} = \frac{1}{\tau_{ph}} + \frac{1}{\tau_{trap}}$$

- Fit mobility dependence on fluence with a power law

$$\mu_{0,sum}(\Phi) = \frac{\mu_{0,sum,phonon}}{1 + \left(\frac{\Phi}{\Phi_{1/2}}\right)^a}$$

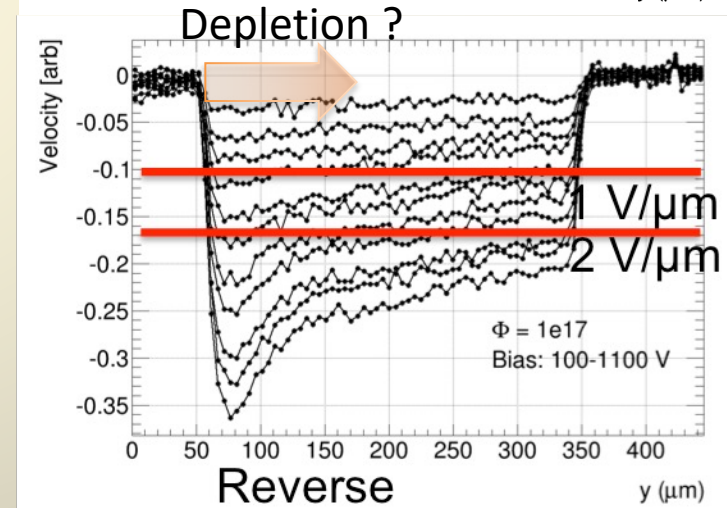
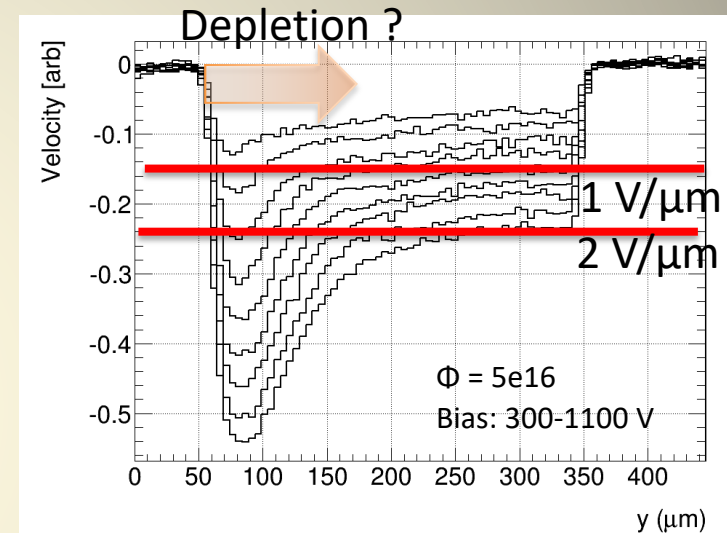
- Fits perfectly, value of  $a$  close to linear
  - 10% error assumed for all neutron data
- At same NIEL, mobility decrease worse for protons
  - NIEL violation? Large errors?



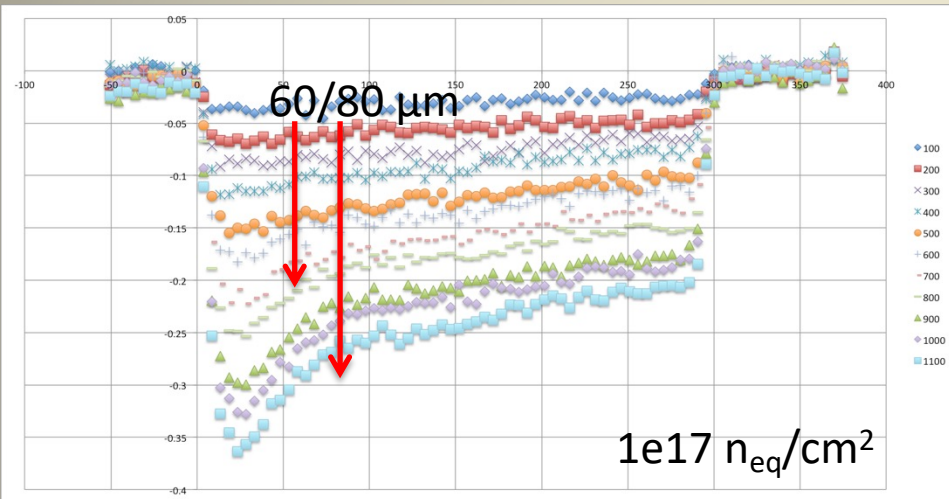
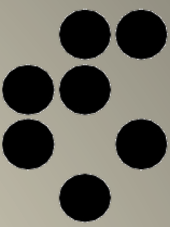
Irradiation particle	$a$	$\sigma_a$	$\Phi_{1/2} / 10^{15}$	$\sigma_{\Phi_{1/2}} / 10^{15}$
Reactor neutrons	-0.68	0.08	6.9	1.7
PS protons	-0.90	0.19	6.1	1.0

# Reverse Bias Field Profile

- Two distinct regions at high biases
  - Large region from backplane with (small) slope in the field
    - constant (small, negative) space-charge
    - $E = j \cdot \rho$  at junction ? like “ENB” ?
    - indication of thermal (quasi)equilibrium:  $np = n_i^2$  ?
    - thus no current generation ?
  - Small region at junction building up with bias
    - depleted space-charge region ?
    - source of generation current ?



# SCR Consistency

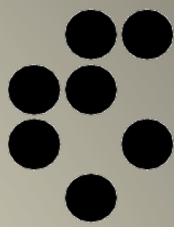


- Hard to estimate SCR extent, especially at lower bias and highest fluence
- A crude estimate
  - $5 \times 10^{16} n_{eq}/\text{cm}^2$  :  
~80  $\mu\text{m}$  @ 600 V; ~120  $\mu\text{m}$  @ 1000 V
  - $10^{17} n_{eq}/\text{cm}^2$  :  
~60  $\mu\text{m}$  @ 600 V; ~80  $\mu\text{m}$  @ 1000 V

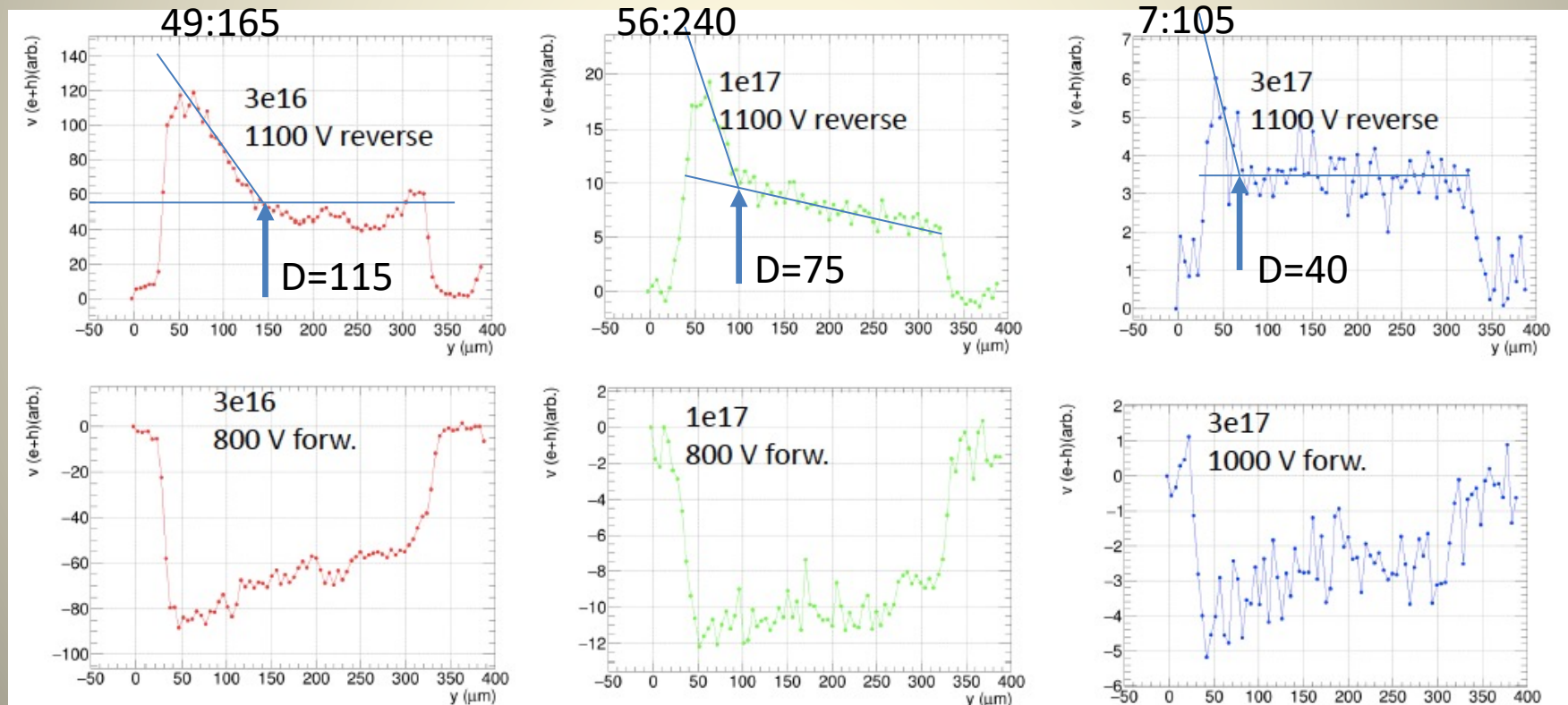
- Predicted/measured currents
  - $5 \times 10^{16} n_{eq}/\text{cm}^2$ : 300/300  $\mu\text{A}$  @ 600 V; 400/500  $\mu\text{A}$  @ 1000 V
  - $10^{17} n_{eq}/\text{cm}^2$ : 400/300  $\mu\text{A}$  @ 600 V; 500/600  $\mu\text{A}$  @ 1000 V
  - Not compatible with linear  $I$ - $V$  at  $3$  &  $4.6 \times 10^{17}$  – pure resistor ?
- Reasonable agreement with current generated exclusively in SCR
  - n.b. - current “saturation” observed @1000V in *JINST 8 P08004 (2013)*
- Acceptor introduction rates:  $g_c \approx 6/4 \times 10^{-4} \text{ cm}^{-1}$ 
  - substantial part (up to 80 %) of voltage drop “spent” in “ENB”
  - matches well data in *JINST 9 P10016(2014)* (up to  $10^{16}$ )



# ATL12 up to $3e17$

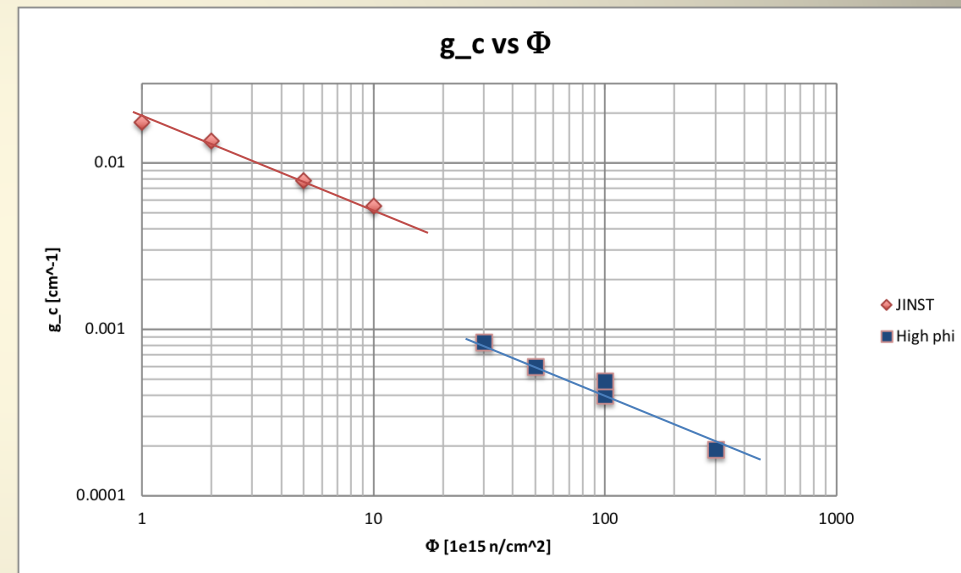


- Estimate of SCR width 115  $\rightarrow$  75  $\rightarrow$  40  $\mu\text{m}$
- $V_{drop}$  in SCR only 23  $\rightarrow$  19  $\rightarrow$  6 % of 1100 V

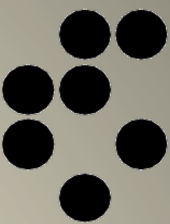


# Acceptor introduction in SCR

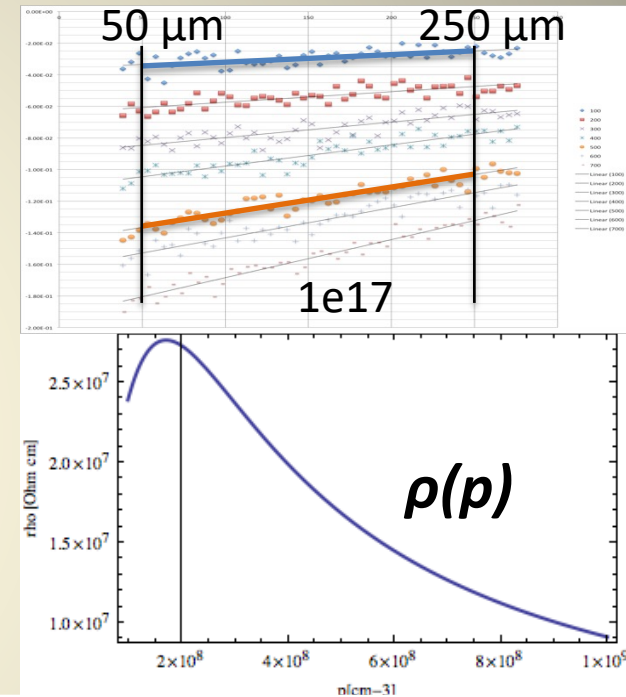
- Stable acceptor introduction rate  $g_c$  drops by nearly two orders of magnitude from low fluences to  $3 \times 10^{17}$ 
  - Observed up to  $10^{16}$  in *JINST 9 P10016(2014)*
  - Looks like a power law
    - $g_c$  in JINST not taking into account voltage drop out of SCR – higher values of  $g_c$



# “ENB” Consistency



- Space charge in “ENB” rising with bias, e.g. for  $10^{17} n_{eq}/cm^2$ 
  - $1.6 \times 10^{11}$  @ 100 V,  $9.2 \times 10^{11} cm^{-3}$  @ 500V
  - c.f.  $\sim 4 \times 10^{13} cm^{-3}$  in SCR
  - negative space charge, like in SCR
- Resistivity from  $\rho = j/E$  @ 100 V
  - maximum  $\rho(p) \approx 2.8 \times 10^7 \Omega cm$  using nominal mobilities @  $p \sim 2 \times 10^8 cm^{-3}$ 
    - all measured values exceed this limit
  - compatible with measured mobility sum and  $p \sim O(10^9) cm^{-3}$
  - Compatible also with  $\rho$  from  $I-V$  for 3 & 4.6e17



$\Phi$	$\rho$	$p$
$[n_{eq}/cm^2]$	$[10^7 \Omega cm]$	$[10^9 cm^{-3}]$
1e16	3.3	0.5
5e16	3.0	1.5
1e17	2.8	2.1

# Trapping analysis

- From *I. Mandić et al., JINST 15 P11018 (2020)*

– FW bias CCE estimated by

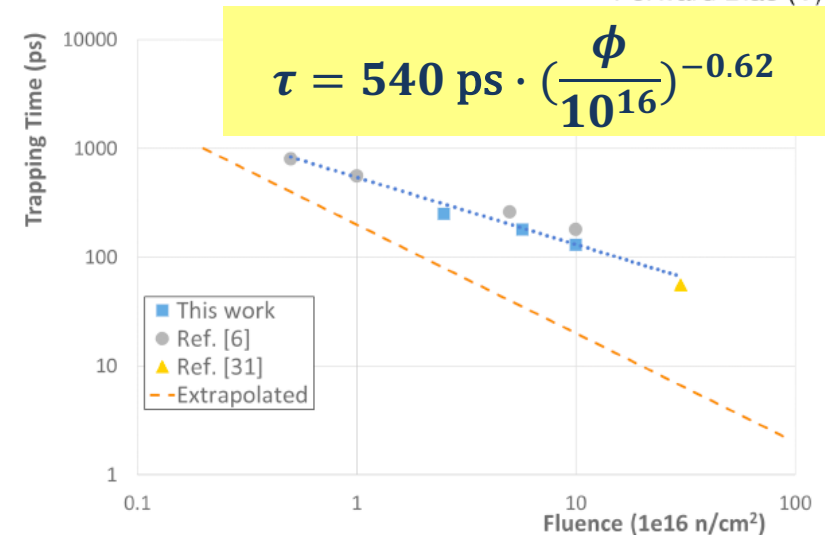
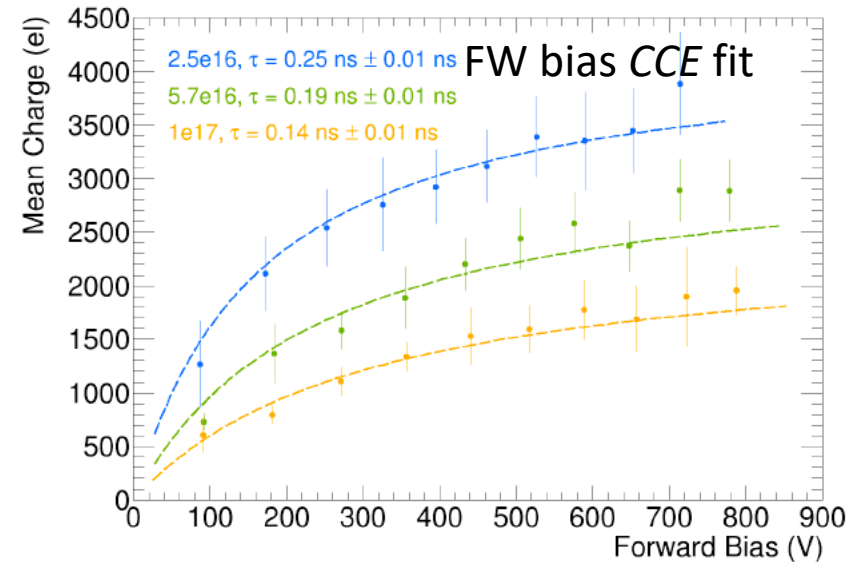
$$Q = \frac{\Delta Q}{\Delta x} \cdot v \cdot \tau$$

- $v(E)$  with fluence dependent  $\mu$
- constant  $E=V/D$  (FW)

😊 Order of magnitude smaller than extrapolated !

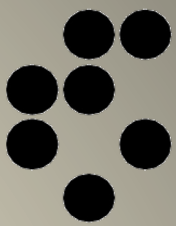
😊 Agrees with estimates from reverse bias CCE (backup)

- Trapping independent of bias, seen in wave-forms





# Summary

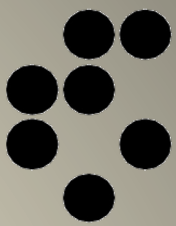


- Measurements performed on Si detectors irradiated to extreme fluences
  - Neutrons from  $10^{15}$  to  $4.6 \times 10^{17}$   $n_{\text{eq}}/\text{cm}^2$ , PS protons from  $5 \times 10^{14}$  to  $3 \times 10^{16}$   $\text{p}/\text{cm}^2$
  - Velocity vs. electric field impact observed and interpreted as reduction of zero field mobility
    - Zero field mobility follows power law with  $|a| \leq 1$ ,  $\Phi_{1/2} \approx 10^{16}$   $\text{n}/\text{cm}^2$
    - Protons degrade mobility more than neutrons
    - Induces resistivity increase in-line with measured  $I$ - $V$
    - Exhibits adverse effect on charge multiplication !
  - Simple field profile for very high neutron fluences
    - Diminishing SCR and highly resistive ENB
    - Effective acceptor introduction rates reduced by factor  $\sim 100$  wrt low fluences
    - Current much lower than anticipated. Generated in SCR only ? Ohmic at highest fluences...
  - Trapping estimates for very high neutron fluences
    - from charge collection in FW and reverse bias
    - from waveforms
    - All estimates point to severe non-linearity of trapping with fluence, 10x lower at  $10^{17}$
    - Trapping appears independent of electric field
- Conclusion: ***Low fluence extrapolations do not work at all !***  
... go out and ***measure*** to get anything working at ***extreme*** fluences !!!



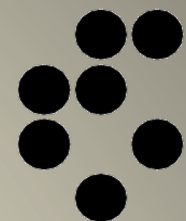


# Implications for TF3



- Basic bulk silicon properties in the fluence range to master are the prerequisite to any inner tracking detector design for FCC-hh
- They need to be *measured*
  - Only pioneering consistency checks done so far
- Need resources far beyond current ones
  - Facilities
  - Measurement techniques
  - Peopleat least for the first ~5 of the 20 years
- New RD or additional RD50 research line essential for achieving the goal
  - EU funding would help to rise funds at national level

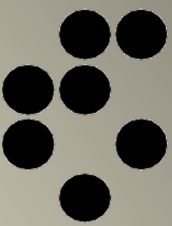
# Conclusion



NOTHING IS  
**IMPOSSIBLE,**  
THE WORD  
ITSELF SAYS  
**“I’M POSSIBLE”!**  
- AUDREY HEPBURN

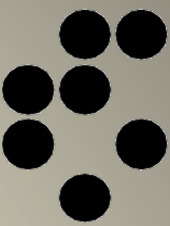


# Backup Slides



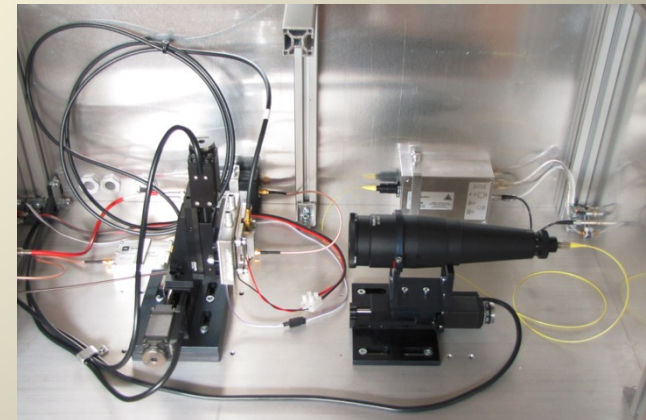
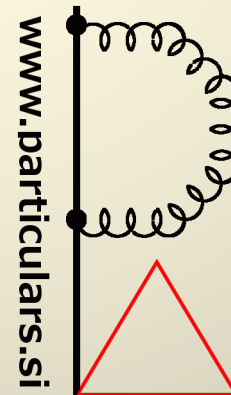
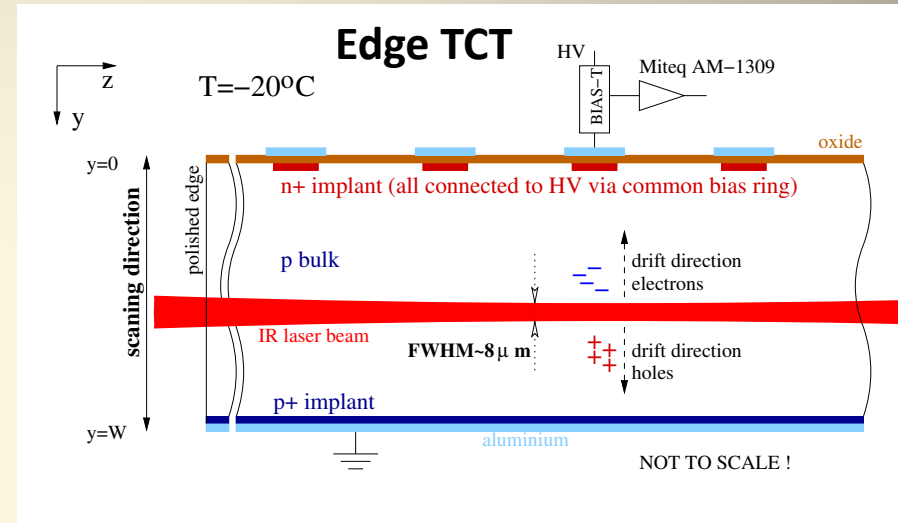


# Edge TCT



## • Edge-TCT

- Generate charges by edge-on IR laser perpendicular to strips, detector edge polished
- Focus laser under the strip to be measured, move detector to scan
- Measure induced signal with fast amplifier with sub-ns rise-time (Transient Current Technique)
- Laser beam width  $8\ \mu\text{m}$  FWHM under the chosen strip, fast (40 ps) and powerful laser
  - Caveat – injecting charge under all strips effectively results in constant weighting (albeit not electric !) field

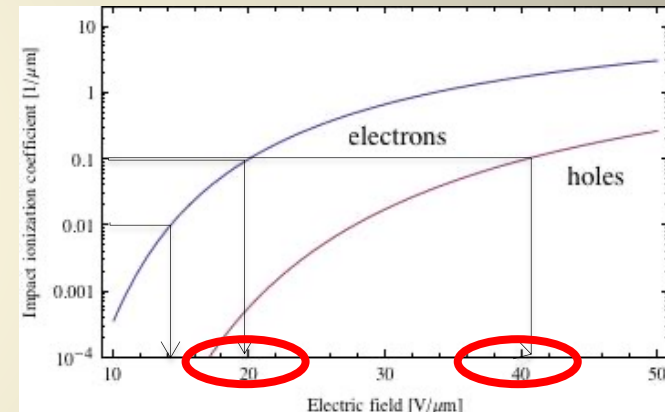


# Charge Multiplication

- Multiplication is textbook physics
  - e.g. S.M. Sze, Physics of Semiconductor Devices, Wiley, New York, 1981
    - Ch 1.6.4 High-Field Property
      - Velocity saturation, impact ionization
    - Ch 2.5.3 Avalanche Multiplication
      - Junction break-down
- Measured impact ionization
  - Electrons create 1 pair in 10  $\mu\text{m}$  at  $E \sim 20 \text{ V}/\mu\text{m}$  (100  $\mu\text{m}$  at 14  $\text{V}/\mu\text{m}$ ), holes need  $E \sim 40 \text{ V}/\mu\text{m}$
  - Holes need  $\sim 1 \text{ mm}$  for pair creation at  $E \sim 20 \text{ V}/\mu\text{m}$ 
    - Neglect hole multiplication in signal creation altogether
    - Need to invoke hole multiplication for junction breakdown
- $\alpha_e \gg \alpha_h$  - Nature gentle to us (in silicon)
  - Large range in  $E$  where electrons multiply without inducing breakdown
  - But beware of (too) high electric fields !

$$\alpha_{e,h}(E) = \alpha_{e,h}^{\infty} e^{-b_{e,h}/E}$$

A. G. Chynoweth, Phys. Rev. 109, 1537(1958).



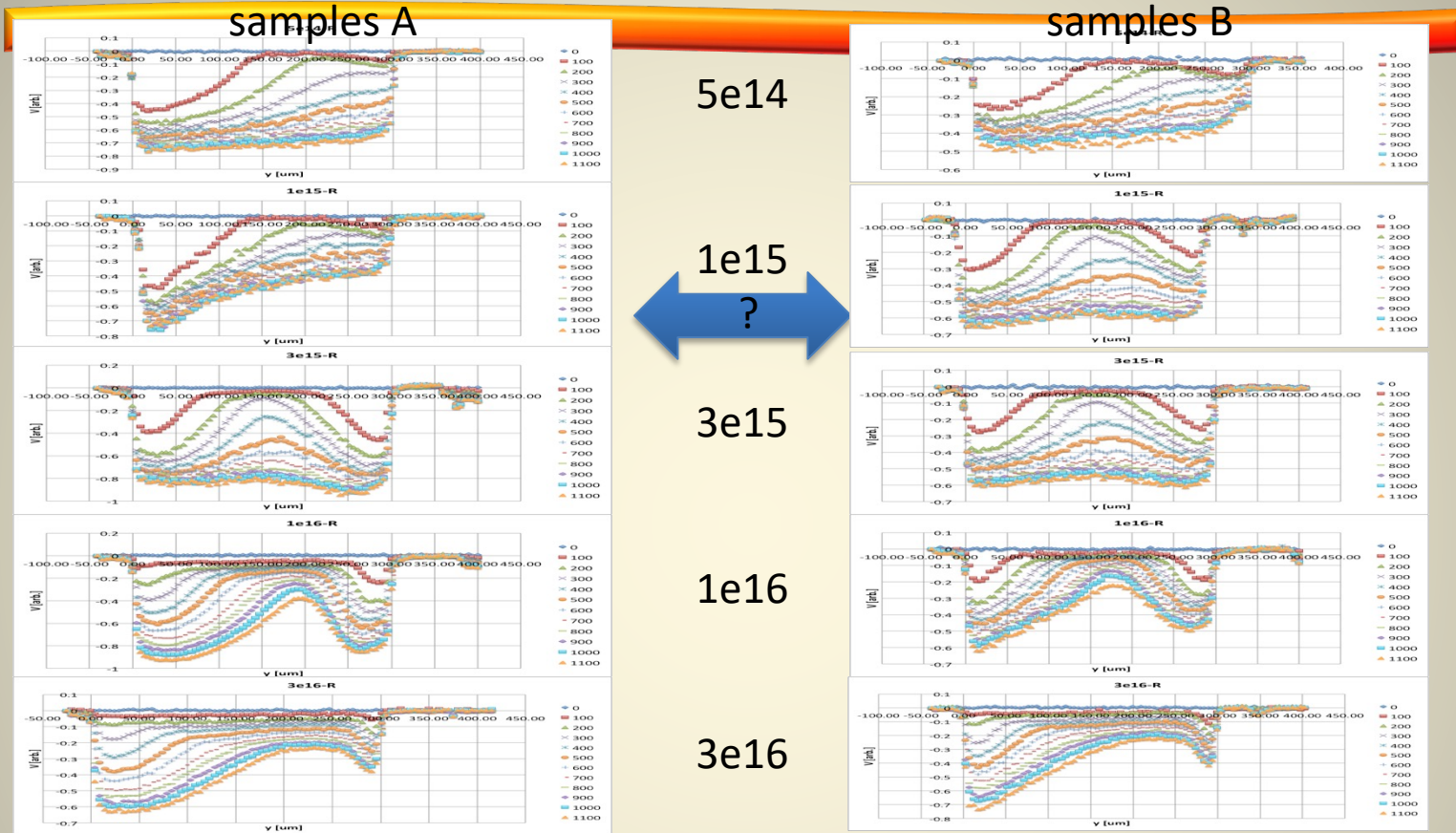
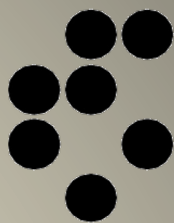
R.VAN OVERSTRAETEN and H.DE MAN, Solid-State Electronics 13(1970),583-608.  
 W.MAES, K.DE MEYER, R.VAN OVERSTRAETEN, Solid-State Electronics 33(1990),705-718.

$$\int_0^w dx \alpha_e(x) e^{-\int_0^x (\alpha_e(x') - \alpha_h(x')) dx'} = 1$$

Breakdown condition, can swap  $\alpha_e$  with  $\alpha_h$



# Reverse velocity profiles



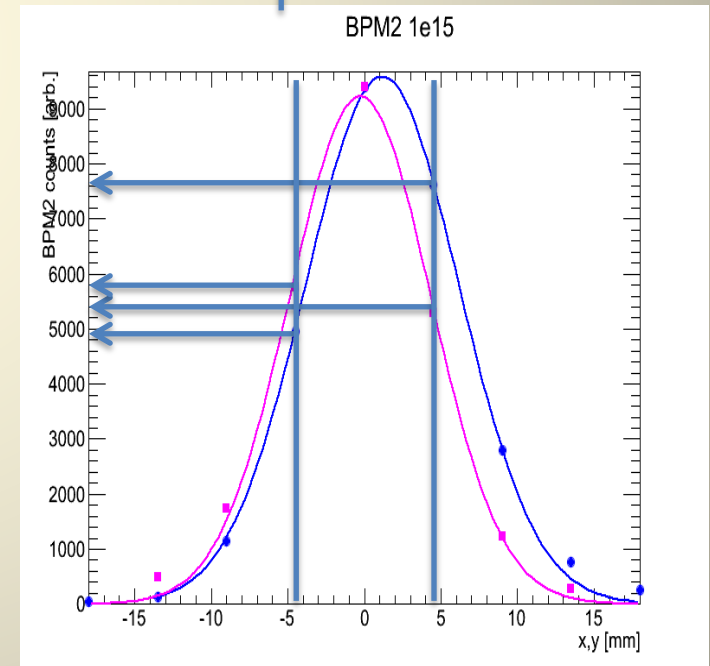
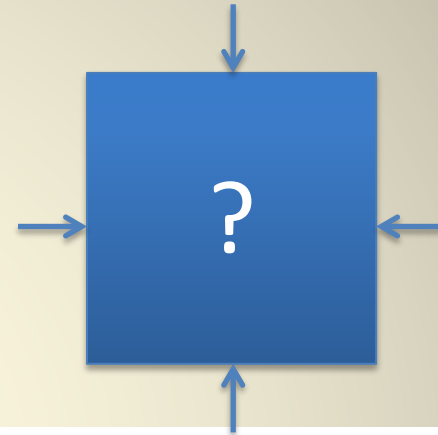
Something's fishy... never repeat experiments ?!



Explained by PS beam profile variation on sample edges

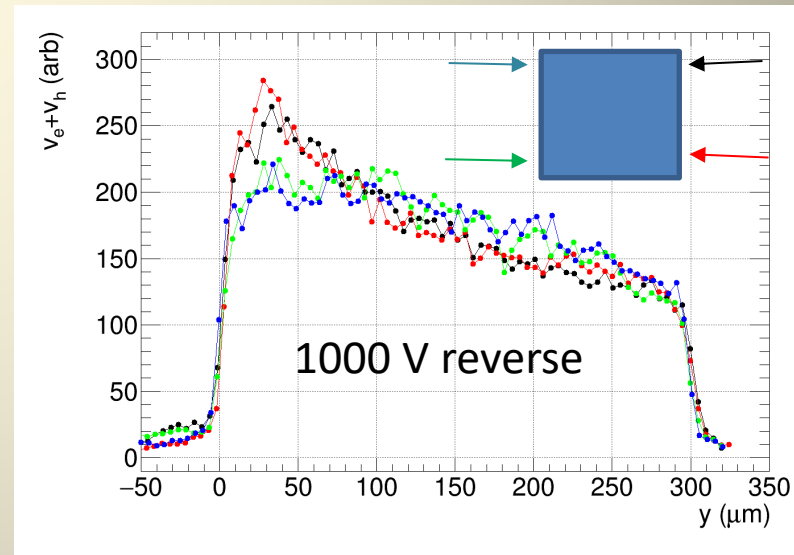
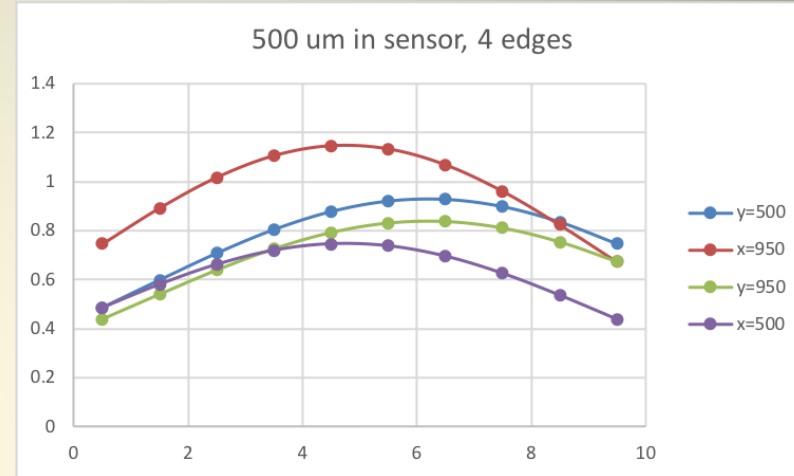
# Proton irradiations - details

- Samples irradiated in PS in pairs
  - in series in same sample holder
- Same leakage current in both samples
  - ⇒ same *average* fluence received
- Beam profile asymmetric
  - monitored by BPM2
- Which side did we pick up ?



# Protons revisited

- BPM2 results for the 1e15 sample, 0.5 mm in sensor
- 10x10 mm<sup>2</sup> average to peak: 0.7
  - Values rescaled
- Mid-side to average:
  - 1.17, 0.88, 0.82, 0.74
    - Must be the larger difference
  - Correct fluences by -10 %
  - Assign 20 % error
- Re-measured one sample from both sides, match with BPM2 data – still in progress
  - Looks like explaining the issue





# Mobility Comparison

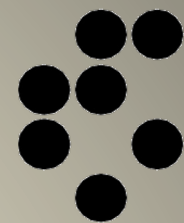


Table 3. Best-fitting parameters for the impurity dependence of electron and hole Ohmic mobilities at room temperature, as given in eqn (6)

	Electrons	Holes	Units
$\mu_{min}$	92	47.7	$\text{cm}^2 \text{V}^{-1} \text{sec}^{-1}$
$\mu_{max}$	1360	495	$\text{cm}^2 \text{V}^{-1} \text{sec}^{-1}$
$N_{ref}$	$1.3 \times 10^{17}$	$6.3 \times 10^{16}$	$\text{cm}^{-3}$
$\alpha$	0.91	0.76	—

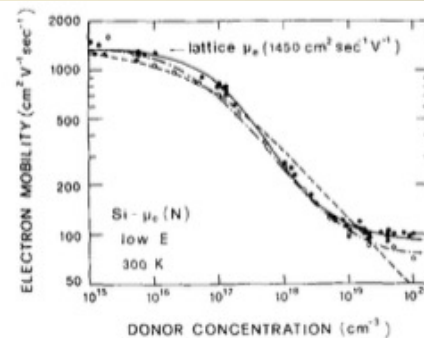


Fig. 5. Electron mobility,  $\mu_e$ , in silicon at 300 K as a function of impurity concentration. Open and closed circles are the experimental results reported by Irvin[55] and of Mousty *et al.*[56], respectively. The continuous line is the phenomenological best fit (eqn (6)) of Baccarani and Ostoia[53] the broken line the best fit (eqn (7)) of Hilsun[54] the dot-dashed line (eqn (8)) of Scharfetter and Gummel[57] (see Tables 3 and 4).

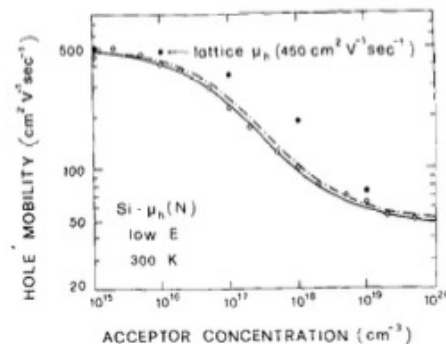


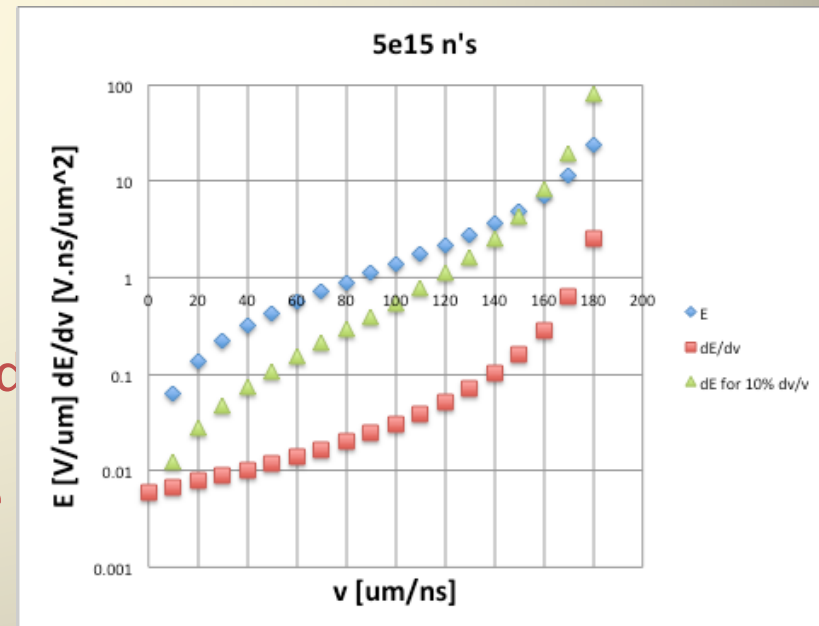
Fig. 6. Hole mobility,  $\mu_h$ , in silicon at 300 K as a function of impurity concentration. Open circles are experimental results reported by Irvin[55]. Continuous and dot-dashed lines represent the best fitting curves of Caughey and Thomas[58] (eqn (6)) and of Scharfetter and Gummel[57] (eqn (8)), respectively (see Tables 3 and 4).

**A REVIEW OF SOME CHARGE TRANSPORT PROPERTIES OF SILICON†**  
 C. JACOBONI, C. CANALI, G. OTTAVIANI AND A. ALBERICI QUARANTA  
 Istituto di Fisicadell'Universitadi Modena, 41100Modena, Italy  
 (Received 18 March 1976; in revised form 12 July 1976)

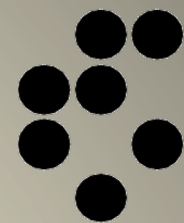
- Dependence on *shallow* dopant concentration
  - Measured in the roaring 60's
- Characteristic trap concentration  $N \sim 10^{17} \text{ cm}^{-3}$ 
  - looks out of reach for typical  $g=0(10^{-2})$
- But  $g$  refers to  $N_{eff} = |N_a - N_d|$
- While  $N$  is more like  $N_a + N_d$ 
  - *x-sections for deep and shallow?*
- Power law looks compatible:  $\alpha \leq 1$

# Velocity and Field Profiles

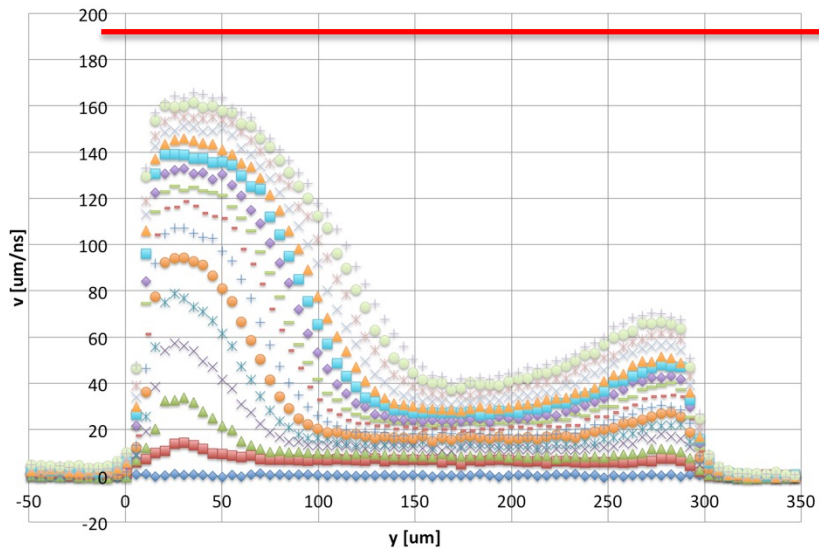
- Knowing  $v(E)$  can set scale to velocity profiles
  - assumption: same scale on FW and reverse bias
    - protons: for  $5 \times 10^{14}$  and  $10^{15}$  use same scale, fixed by average field for  $5 \times 10^{14}$  at 1100 V (no good FW data)
- Invert  $E(v)$  to get electric field profiles
  - big errors when approaching  $v_{sat}$  i.e. at high  $E$ 
    - exaggerated by CM in high field regions
    - $v > v_{sat}$  not physical, but can be faked by CM



# Velocity Profiles Neutrons



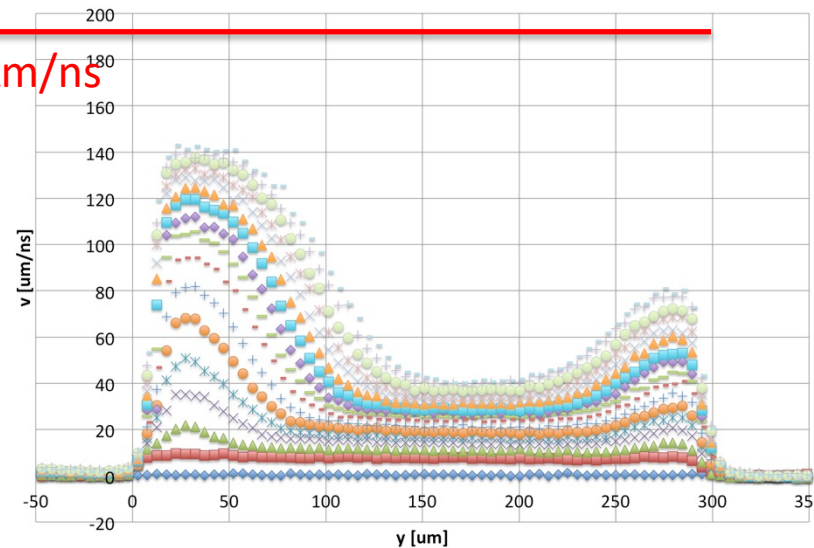
Velocity profile 5e15



$v_{50} = 190 \mu\text{m/ns}$

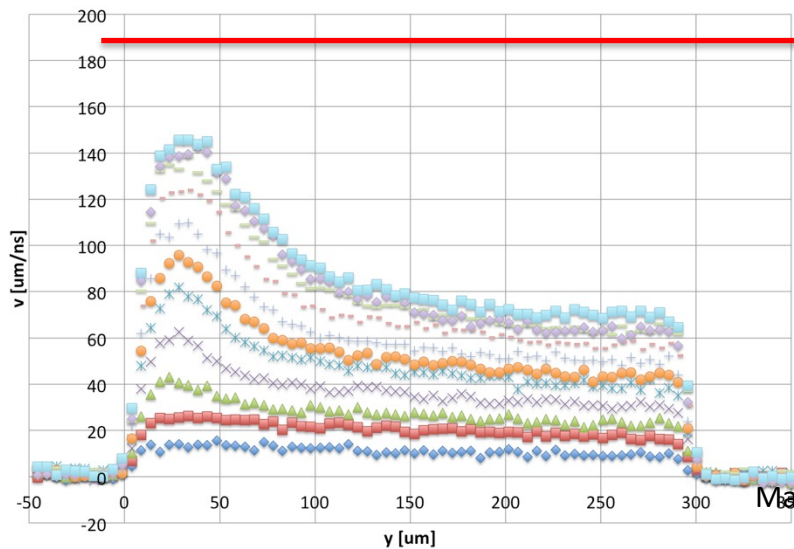
- 0
- 100
- 150
- 200
- 250
- 300
- 350
- 400
- 450
- 500
- 550
- 600
- 650
- 700
- 750

Velocity profile 1e16



- 0
- 50
- 100
- 150
- 200
- 250
- 300
- 350
- 400
- 450
- 500
- 550
- 600
- 650
- 700
- 750
- 800

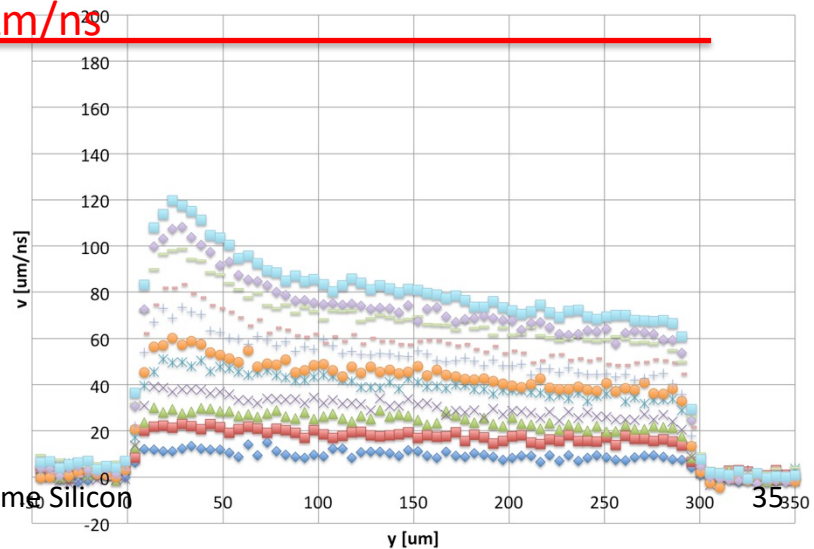
Velocity profile 5e16



$v = 190 \mu\text{m/ns}$

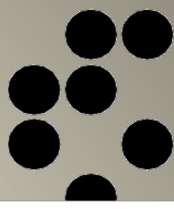
- 100
- 200
- 300
- 400
- 500
- 600
- 700
- 800
- 900
- 1000
- 1100

Velocity profile 1e17

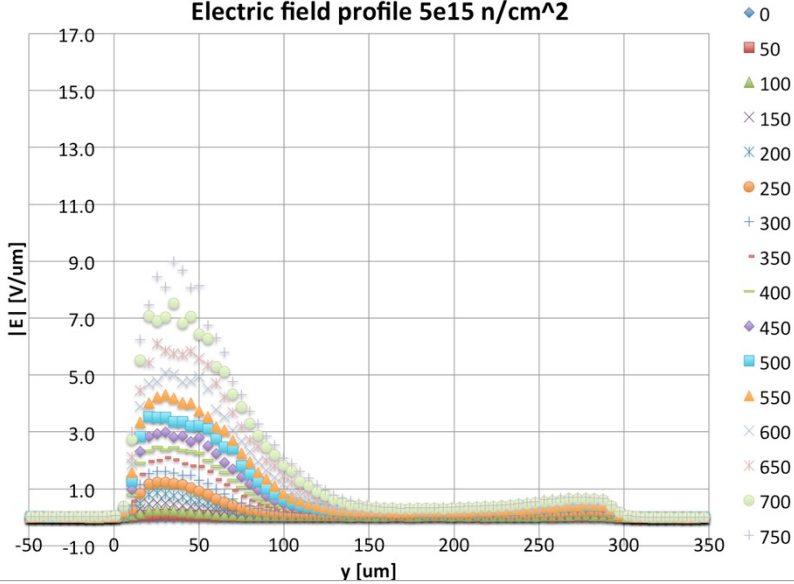


- 100
- 200
- 300
- 400
- 500
- 600
- 700
- 800
- 900
- 1000
- 1100

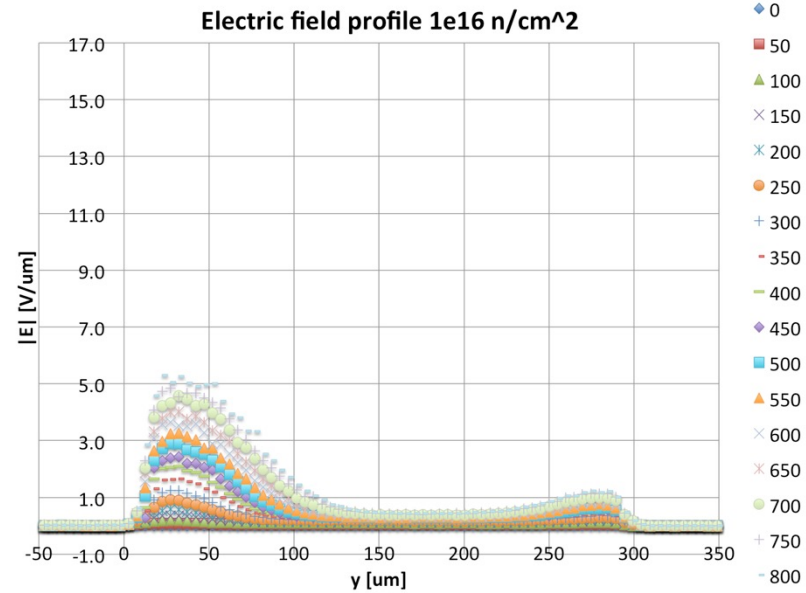
# Field Profiles Neutrons



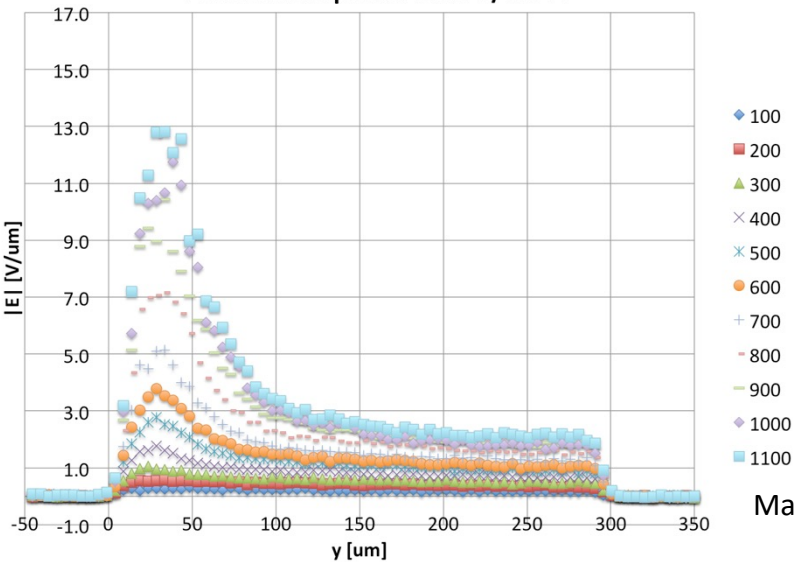
Electric field profile 5e15 n/cm<sup>2</sup>



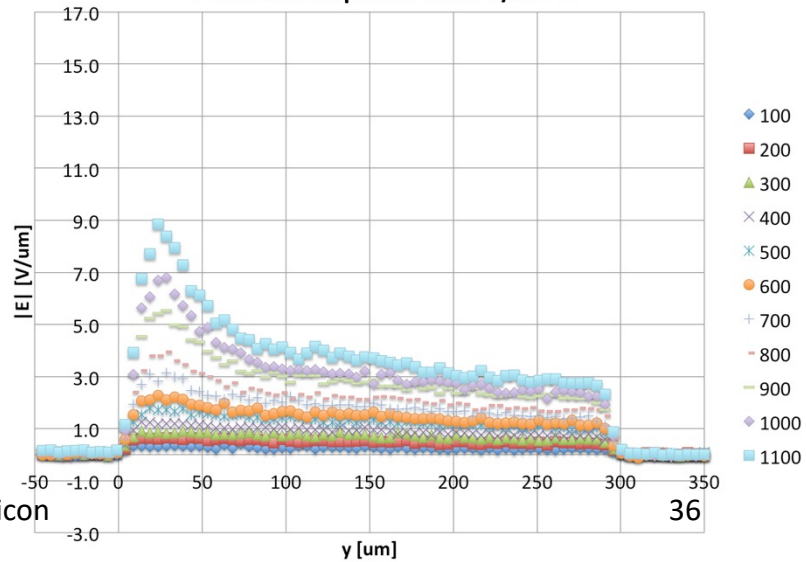
Electric field profile 1e16 n/cm<sup>2</sup>



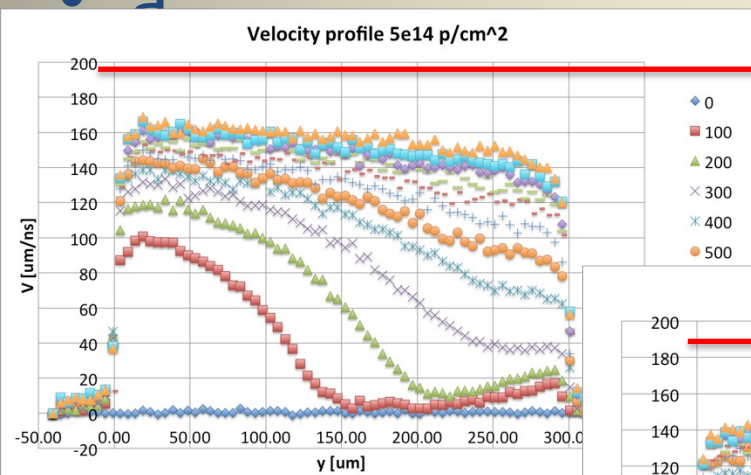
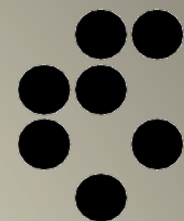
Electric field profile 5e16 n/cm<sup>2</sup>



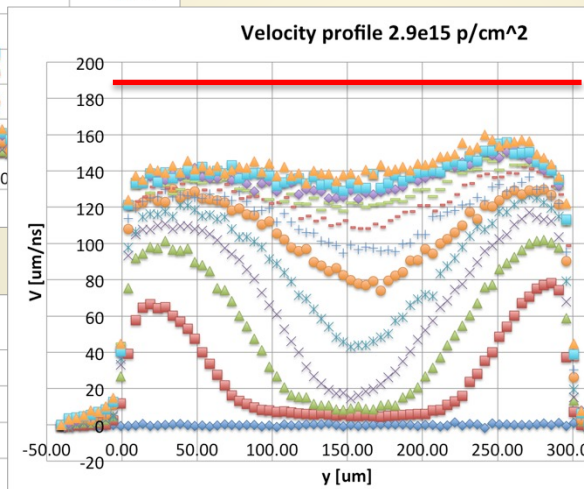
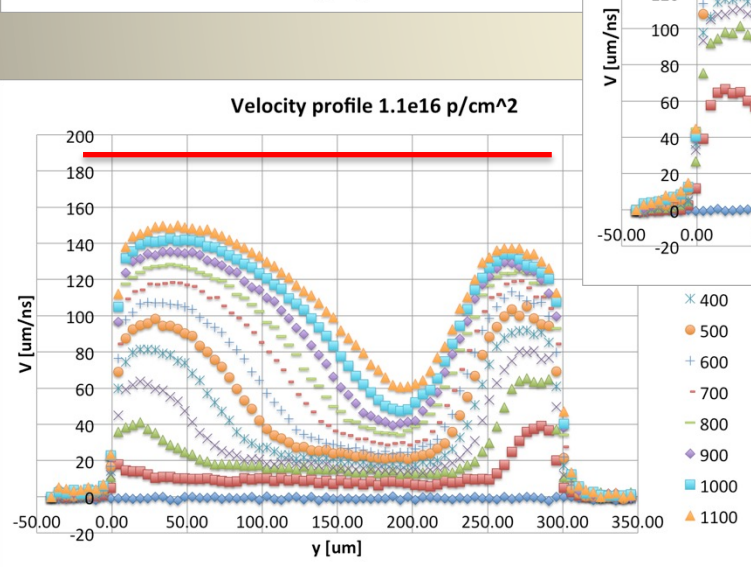
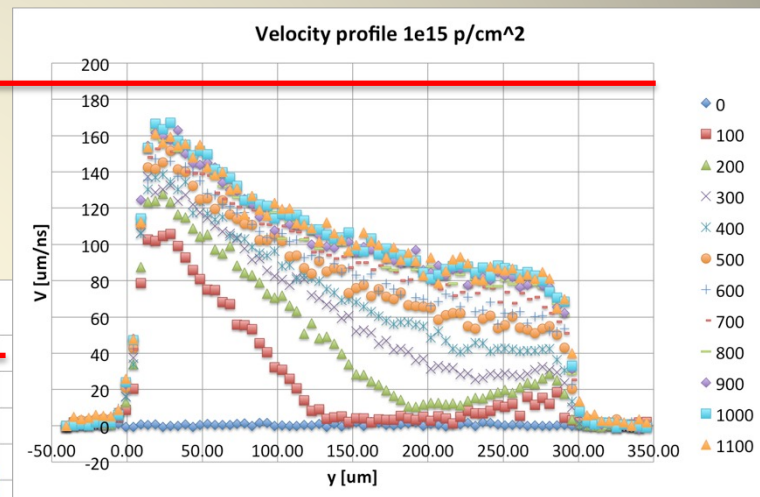
Electric field profile 1e17 n/cm<sup>2</sup>



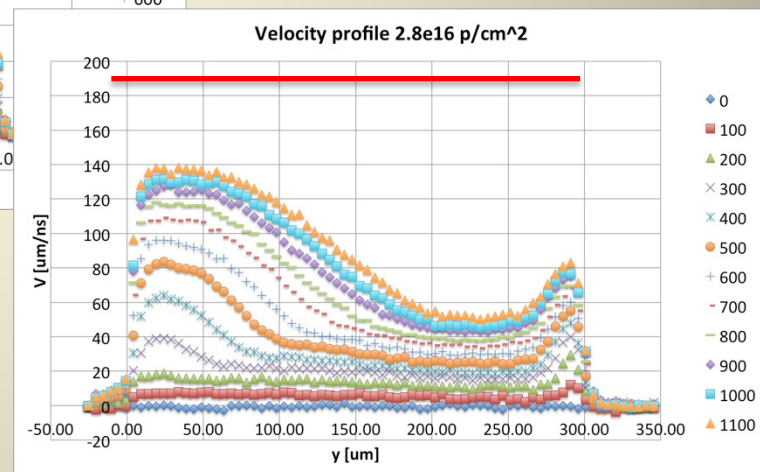
# Velocity Profiles Protons



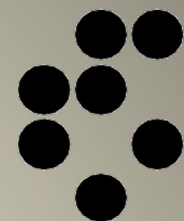
$v = 190 \mu\text{m/ns}$



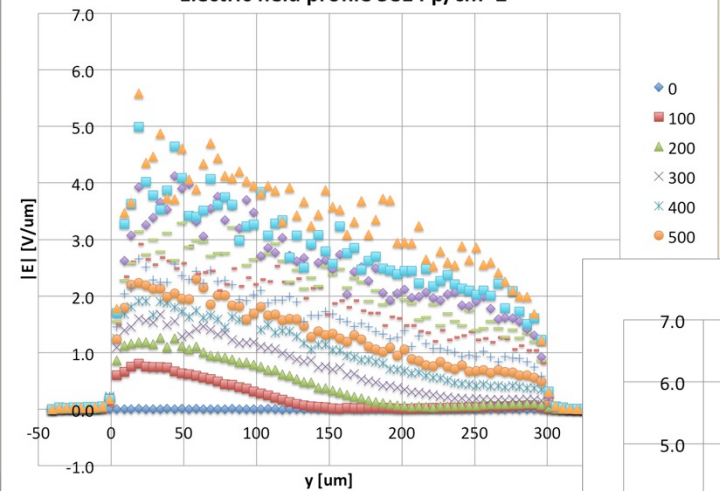
Same scale as  
for neutrons



# Field Profiles Protons

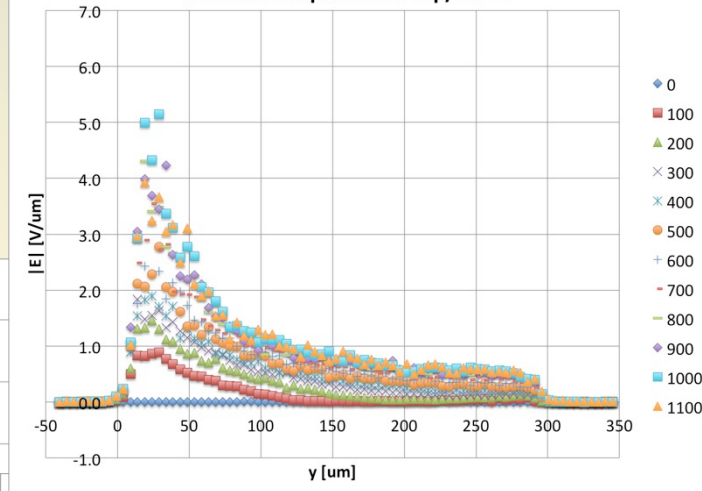


Electric field profile  $5e14 \text{ p/cm}^2$

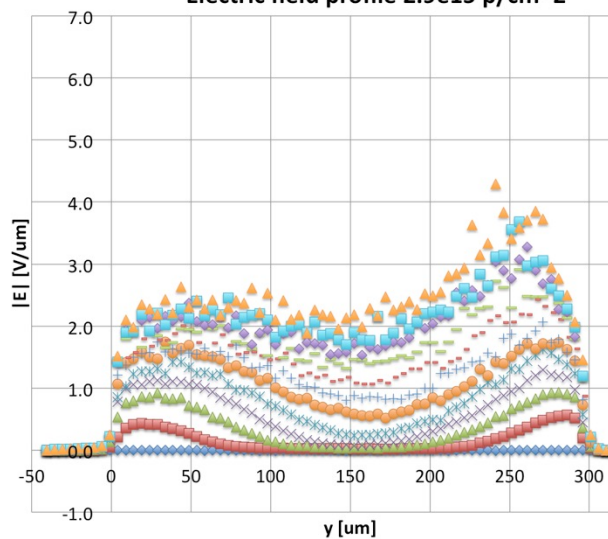


Smaller peak fields  
than for neutrons  
Scale 0-7 V/ $\mu\text{m}$

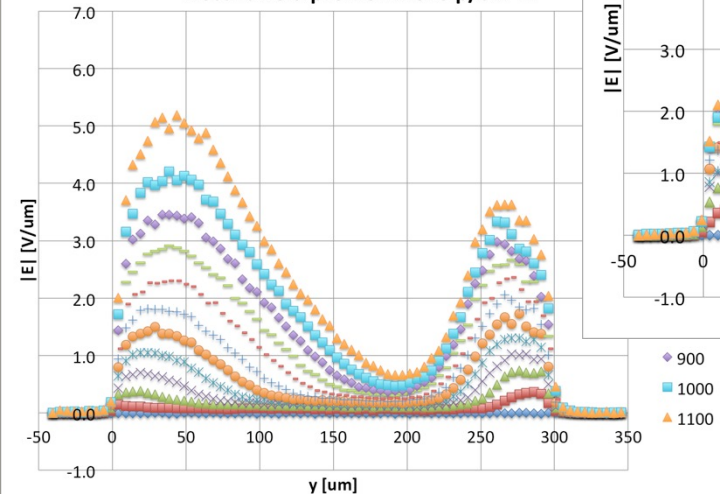
Electric field profile  $1e15 \text{ p/cm}^2$



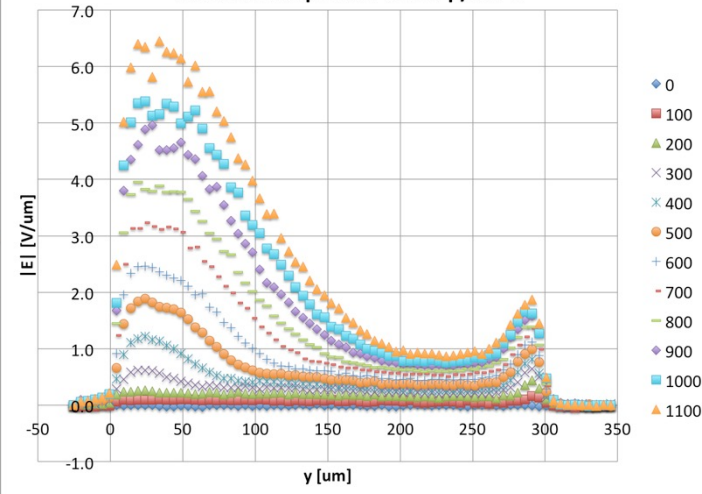
Electric field profile  $2.9e15 \text{ p/cm}^2$



Electric field profile  $1.1e16 \text{ p/cm}^2$

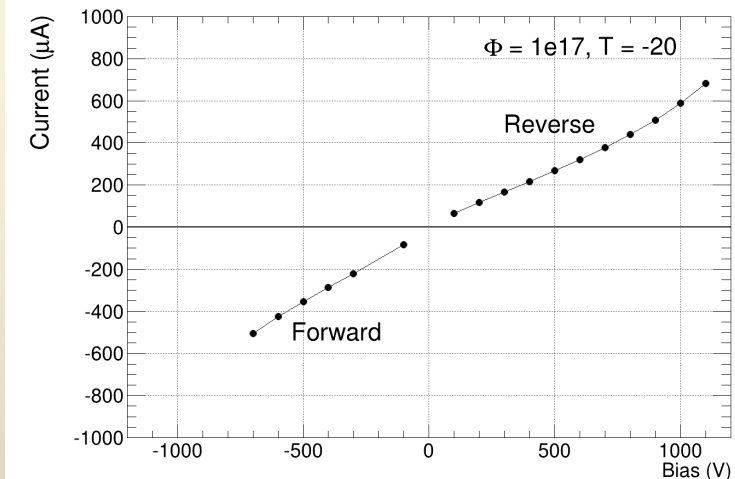
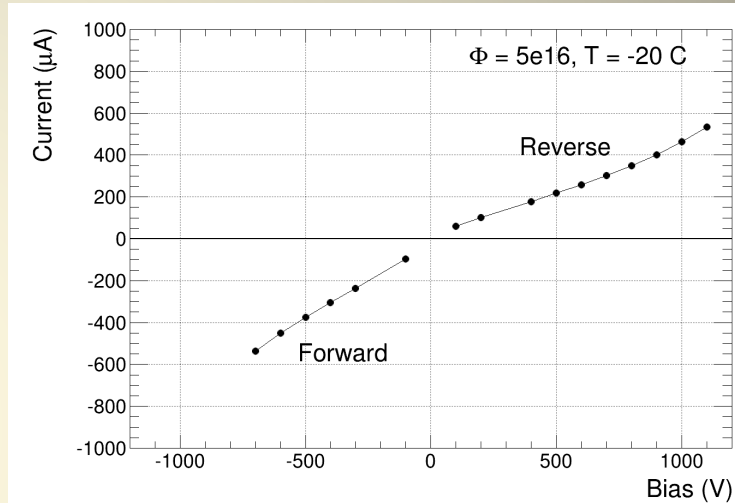


Electric field profile  $2.8e16 \text{ p/cm}^2$

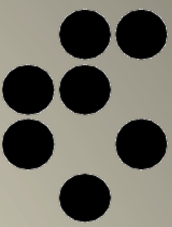


# Current Characteristics

- Smooth behaviour in both directions
  - Highly resistive Si limits FW injection
- Reverse current smaller than predicted by an order of magnitude
- Both currents rising  $\sim$ linear with bias
  - Slopes FW/reverse more compatible at higher fluences
- Consistent with recent measurements at highest fluences



# Trapping Considerations



- Extrapolation from low fluence data with  $\beta_{e,h}(-20^\circ\text{C})=4.4, 5.8 \times 10^{-16} \text{ cm}^2/\text{ns}$ ;  $1/\tau = \beta \Phi$

$\Phi$ [1e15]	5	10	50	100
$\tau$ [ps]	400	200	40	20
$mfp@v_{sat}$ [ $\mu\text{m}$ ]	95	48	9.5	4.8
MPV [ $e_0$ ]	7600	3800	760	380
MPV@1000 V	8900	5500	1800	1150
CCD <sub>1000 V</sub> [ $\mu\text{m}$ ]	110	70	23	14

From "magic formula"  
JINST 9 P10016(2014)



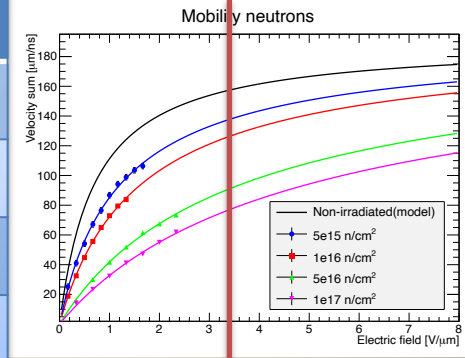
- Measured data exceeds (by far) linear extrapolation of trapping
  - n.b.1:  $E \sim 3 \text{ V}/\mu\text{m}$  by far not enough to saturate velocity
  - n.b.2: little sign of CM at highest fluences



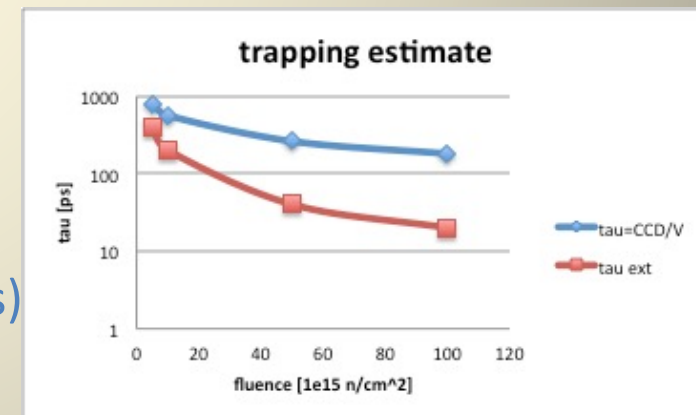
# More Considerations

- More realistic: take  $v_{sum}$  at average  $E = 3.3 \text{ V}/\mu\text{m}$

$\Phi$ [ $1e15$ ]	5	10	50	100
$v_{sum}(3.3 \text{ V}/\mu\text{m})$	137	126	90	77
$CCD_{1000 \text{ V}}$ [ $\mu\text{m}$ ]	110	70	23	14
$\tau \approx CCD/v$ [ps]	800	560	260	180
$\tau_{ext}$ [ps]	400	200	40	20

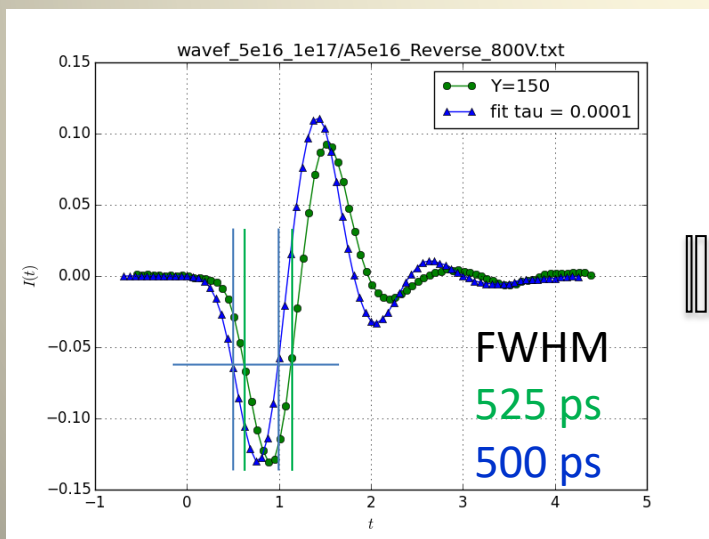


- Implies factor of 6-9 less trapping at highest fluences
  - lowest fluence still x2 from extrapolation
  - weak dependence on fluence as anticipated
  - CM would effectively shorten trapping times
  - not good when large  $E$  variations ( $v(E)$  saturates)
  - not good when  $CCD \approx$  thickness (less signal at same  $\tau$ )

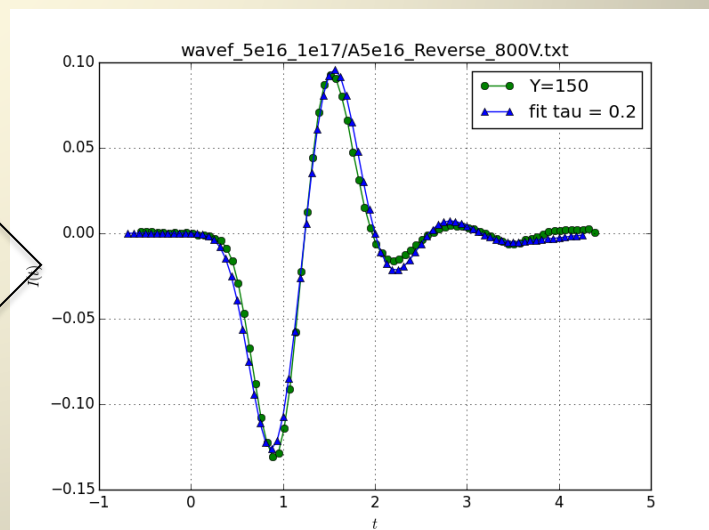


# Exploiting TCT Waveforms

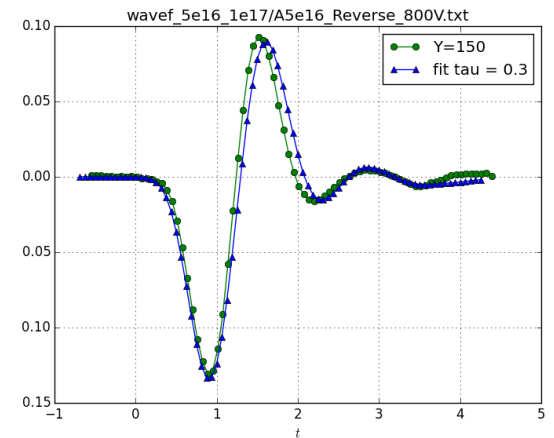
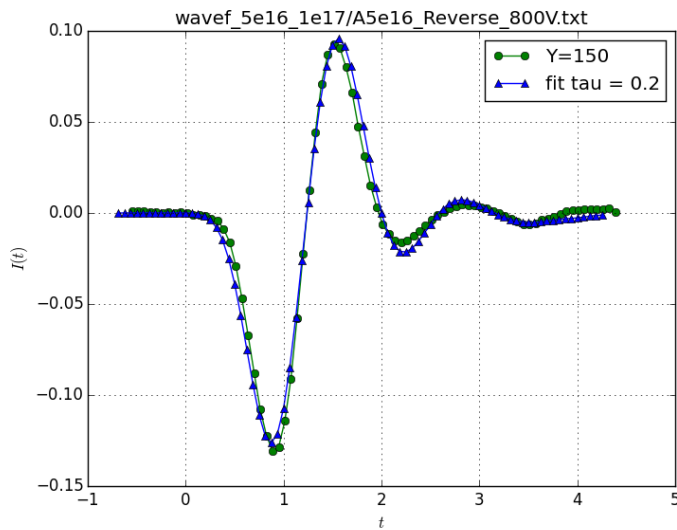
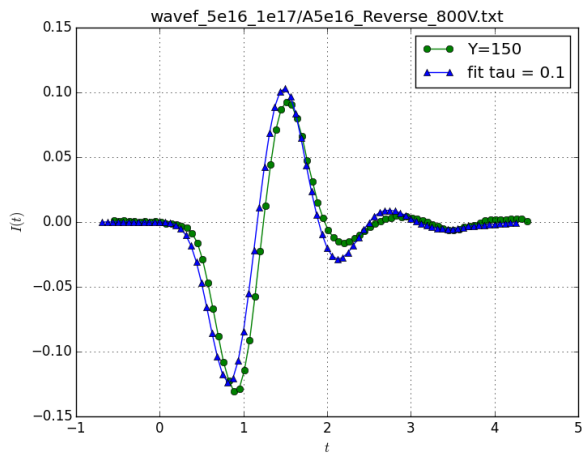
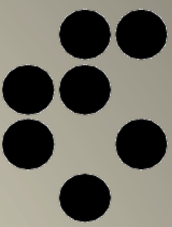
- Waveforms at  $y=100 \mu\text{m}$ , 800 V,  $5 \times 10^{16}$  and  $10^{17}$ 
  - $E \approx 3 \text{ V}/\mu\text{m}$ , CCD/2 implies signal within  $\sim 10 \mu\text{m}$  or  $< 0.2 \text{ ns}$ 
    - the rest you see is the transfer function of the system
- Still distinct signals from the two fluences
  - treat  $10^{17}$  waveform as transfer function of the system
    - convolute with  $e^{-t/\tau}$  to match  $5 \times 10^{16}$  response
    - $\tau = 0.2 \text{ ns}$  provides a good match
- In fact, measure  $\sim \Delta\tau$ , as “transfer” already convoluted with  $e^{-t/\tau(1e17)}$  !



$\tau = 0.2 \text{ ns}$



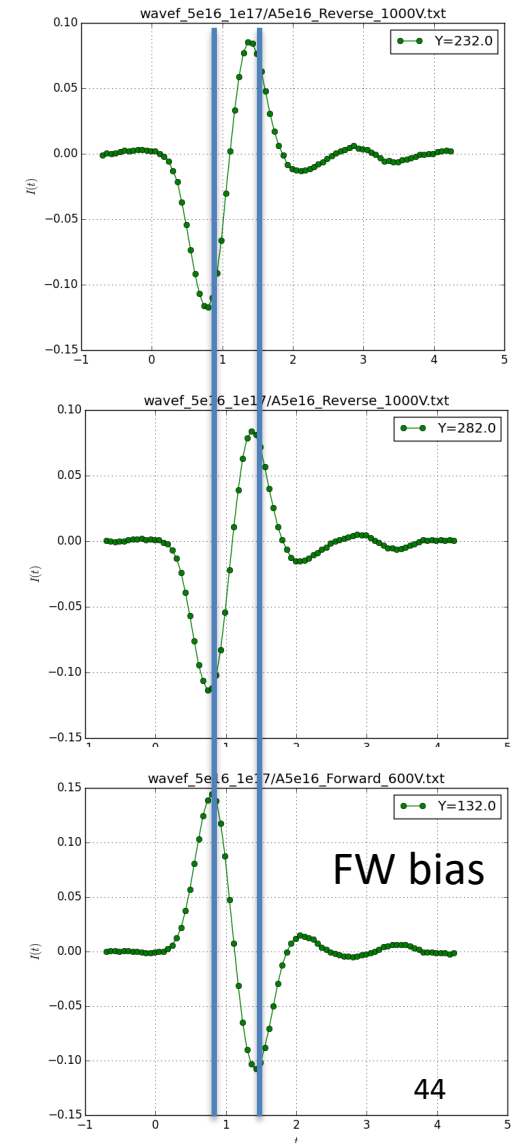
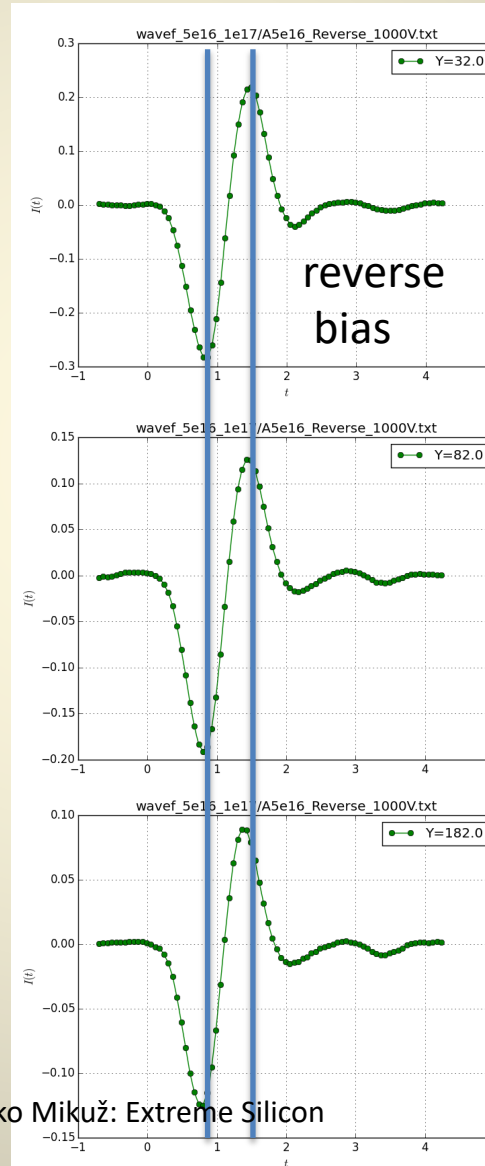
# Waveforms: How sensitive ?



- $\Delta\tau = 0.2$  ns certainly best fit, 0.1 too narrow, 0.3 too broad
- precision  $\sim 50$  ps

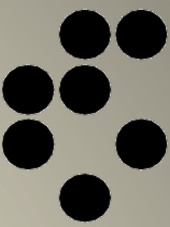
# Trapping – position dependence ?

- Waveforms plotted every 50  $\mu\text{m}$  in detector depth for reverse bias at 1000 V
- Forward bias in middle of detector added at 600 V
- Very little, if any, wf dependence on position observed
- Trapping not position dependent !?





# Trapping @3e17



- Moved to another setup – different waveforms
  - Widths of reverse and FW similar
  - With decreases 1- $\rightarrow$ 3e17
  - Irregular waveforms with small signal @3e17
  - Hard to state something more quantitative

