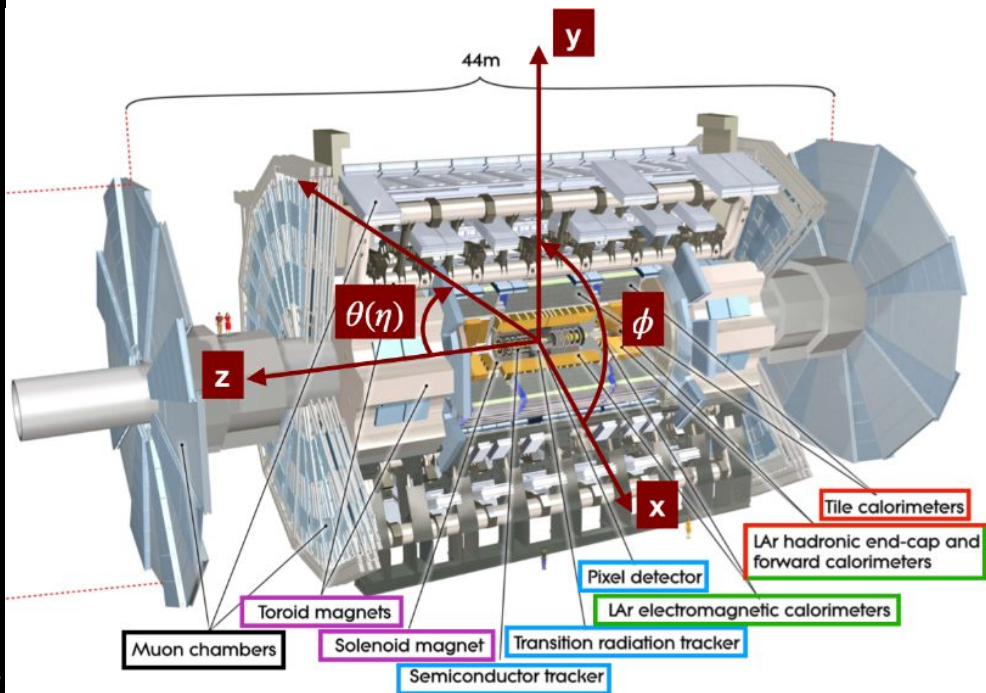
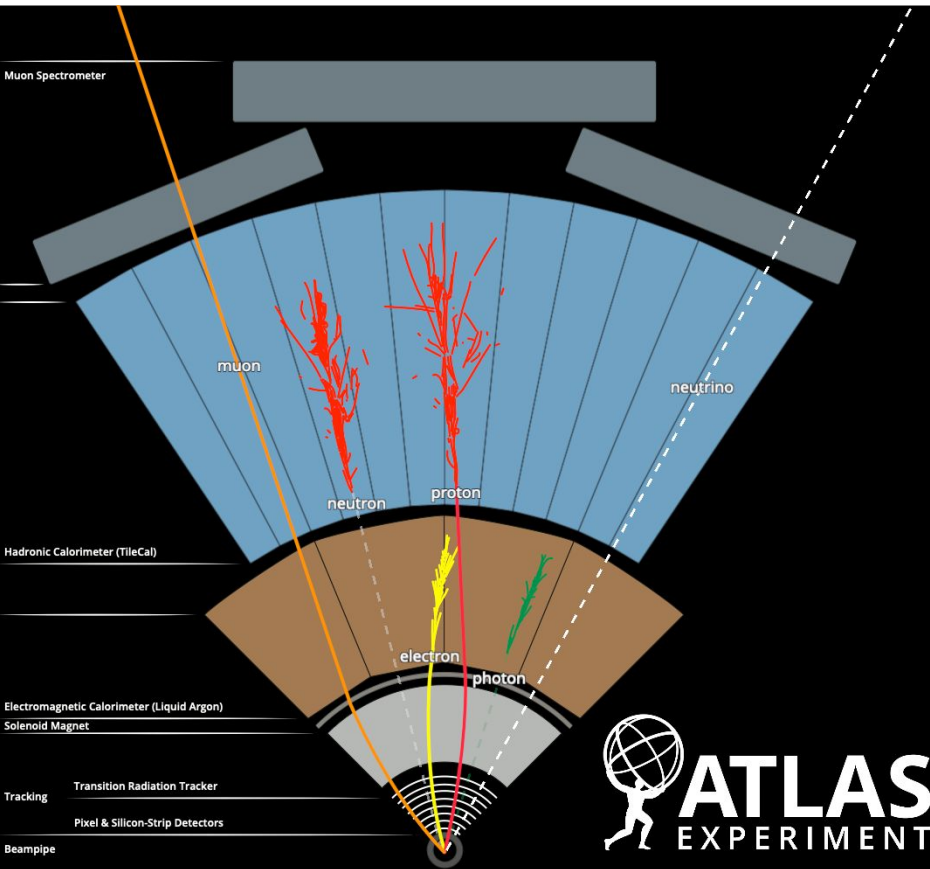


# Boosted W and H Tagging using Lund Jet Plane

**Rafael Andrei Vinasco Soler**

Supervisors: Reina Camacho Toro, Carlos Sandoval.

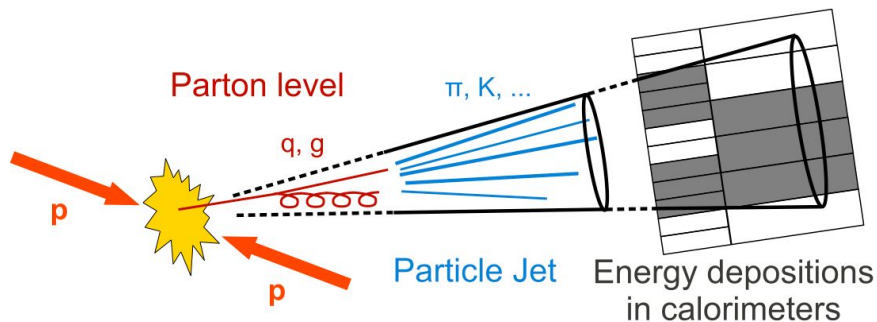
And thanks to Mykola Khandoga and Jad Mathieu Sardain for their full support



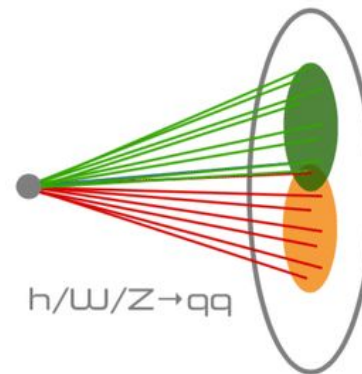
Use Lund plane variables as input for machine learning methods to develop a new tagging methods for boosted **W** and **Higgs bosons**.

**Jet:** A set of collimated particles produced in the hadronization of a quark or gluon.

## Background



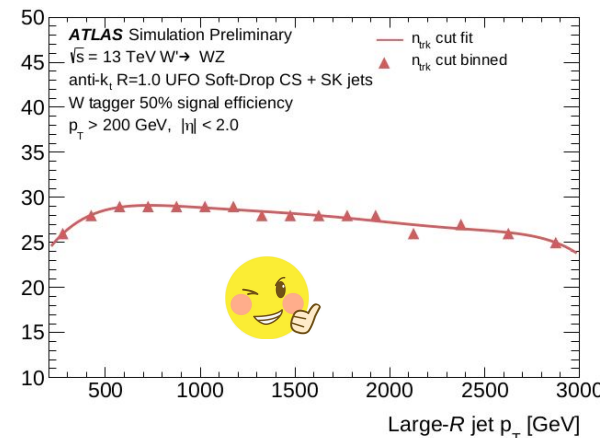
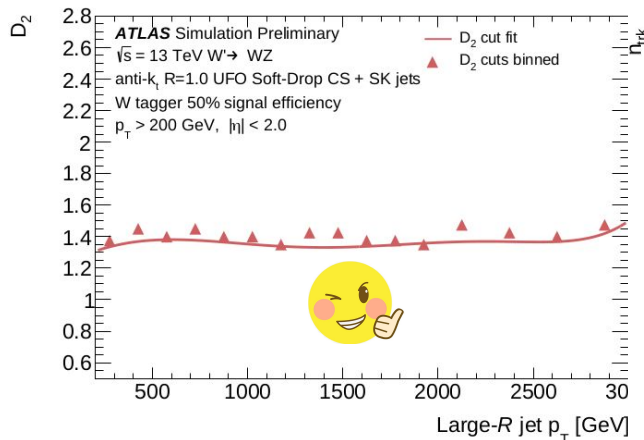
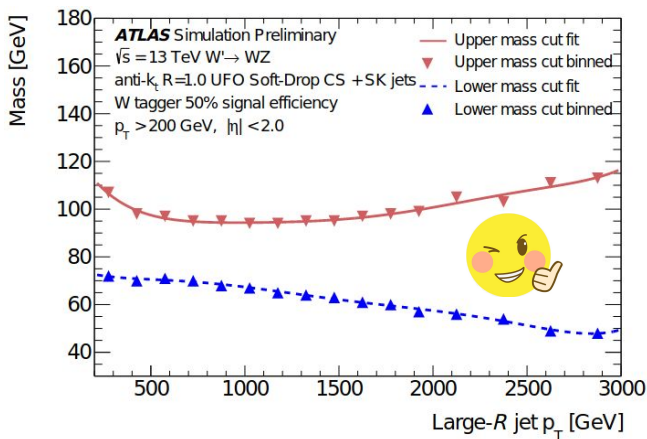
## Signal





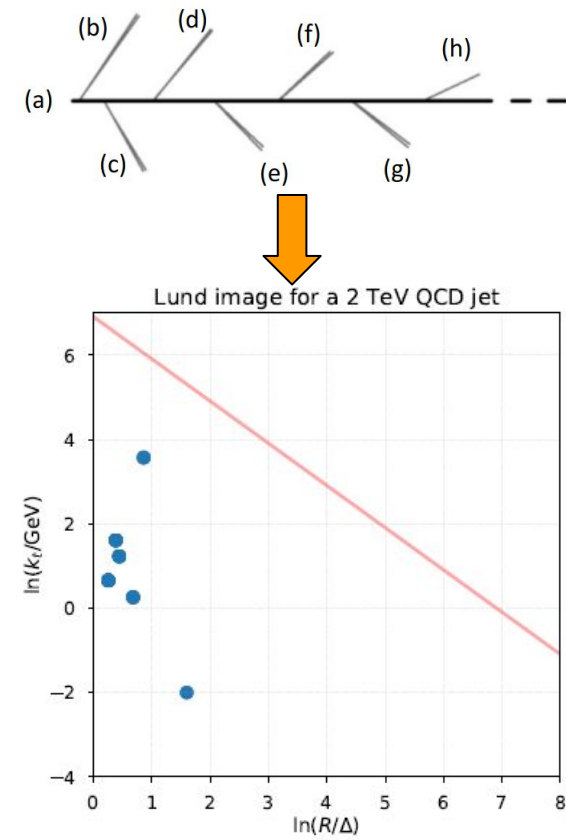
# How we identify W Boosted boson now?

Currently is used a tagger that perform cuts on **3 Jet substructure variables**.  
These cuts are made according to the Jet transverse momentum (**p<sub>T</sub>**).



Plots taken from: **Performance of W/Z taggers using UFO jets in ATLAS**  
<https://cds.cern.ch/record/2777009/files/ATL-PHYS-PUB-2021-029.pdf>

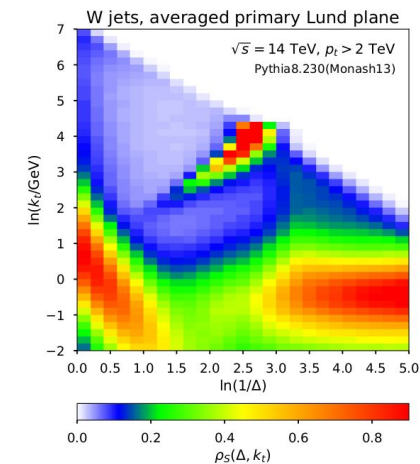
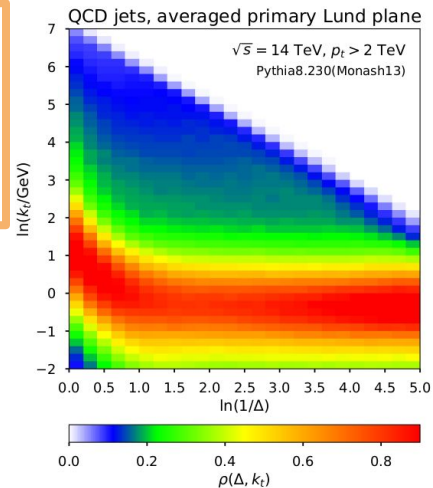
**Lund plane:** Is a way to represent the phase space of jet constituents reconstructed by reversing jet clustering sequence.



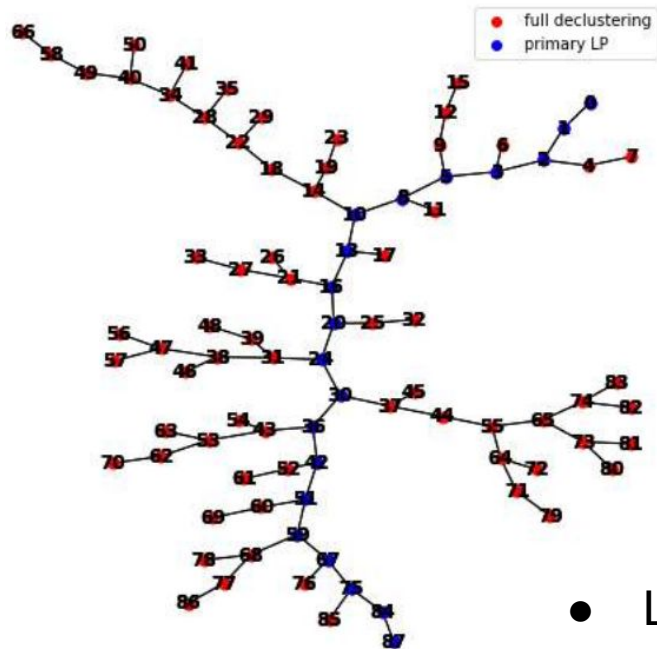
- **Great to separate QCD and W-jets**

- **Lund plane variables:**

- **$k_T$**  : Transverse momentum of the emission.
- **$\Delta$**  : Emission angle
- **$Z$**  : Momentum fraction of branching

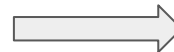


Plots taken from: **Dreyer, F.A., Salam, G.P. and Soyez, G. (2018).**  
**The Lund jet plane.** <https://arxiv.org/pdf/1807.04758.pdf>



- Using the Lund Plane we are going inside the hadronization history. Every single emission is represented!
- If is used the information of each emission instead of using jet global variables we can do a better background discrimination

**More information  
used**



**Better performance**


- Lund planes is made up as a set of vertices and their connection edge, so this is an ideal input for Graph Neural Networks!



# Models (GNN architectures) tested

Traditional Neural Networks require input to be of fixed length whilst Graph Neural Networks do not have this limitation, whether the input graph has 2 nodes or 20, the GNN model can handle it!

## GNN architectures

- LundNet (<https://arxiv.org/pdf/2012.08526.pdf>)  **our inspiration**
- Graph Isomorphism Network (GINConv)
- Graph Attention Network (GATConv)
- Gated Graph Sequence Neural Network (GatedGraphConv)

All documented as GINConv, GATConv, GatedGraphConv, and PNAConv, respectively, at :

<https://pytorch-geometric.readthedocs.io/en/latest/modules/nn.html#convolutional-l>



Events were generated using Monte Carlo simulations in Powheg and Pythia 8 and the detector is simulated using Geant4. Precisely, this is the data used:

- **Dijets:**  
mc16\_13TeV.3647[03,09].Pythia8EvtGen\_A14NNPDF23LO\_jetjet\_JZ[03,09]With  
SW.deriv.DAOD\_JETM8.e7142\_s3126\_r10201\_p4355
- **W prime** (only channel W' to WZ is included):  
mc16\_13TeV.426347.Pythia8EvtGen\_A14NNPDF23LO\_WprimeWZ\_flatpT.deriv.  
DAOD\_JETM8.e6880\_s3126\_r10201\_p4355

### Train size:

2% of dijet background and 10% of W signal.





## Signal and Background cuts:

Ungroomed Jet\_pt > 200 GeV,

Jet\_pt > 200 GeV,

Jet\_pt < 3000 GeV,

Jet\_mass > 40 GeV,

Jet\_mass < 300 GeV,

Jet\_D2 > 0,

## Signal definition

Jet truth match with W boson

Ungroomed Jet\_mass > 50 GeV

Number of b Hadrons = 0



**Background rejection:** How many Background is discarded for the classifier

$$\frac{1}{\epsilon_{\text{background}}} = \frac{N_{\text{background}}^{\text{identified}}}{N_{\text{background}}^{\text{total}}} \longrightarrow \text{“Background rejection”}$$

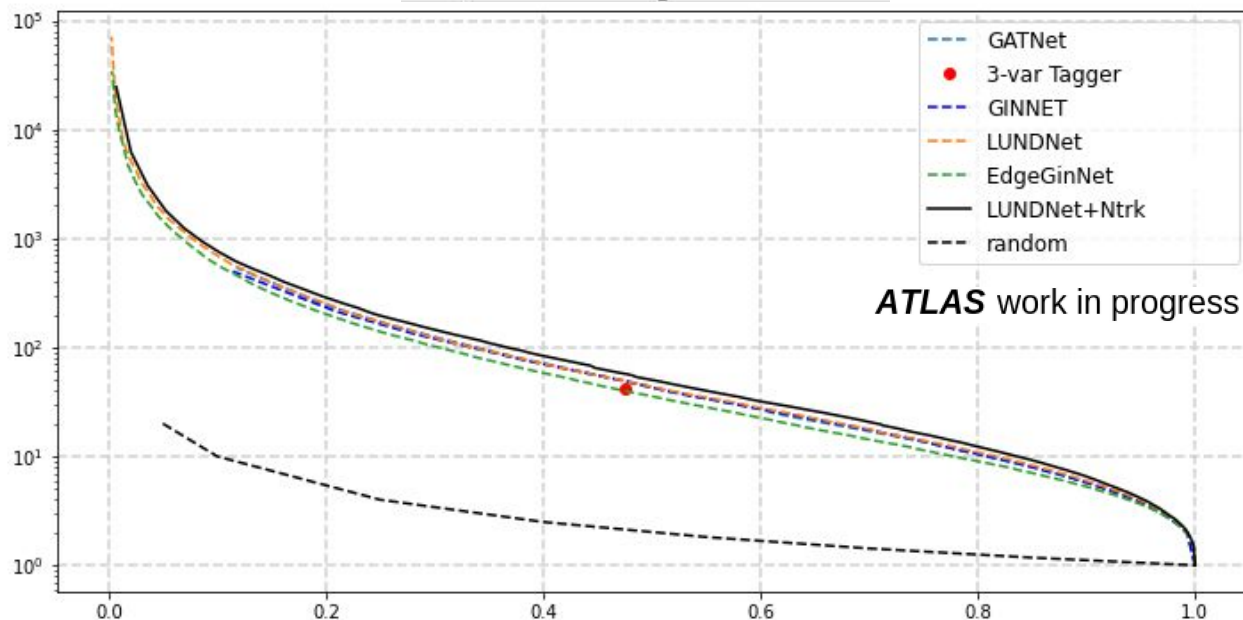
**Background rejection=200** ➡ 1 of 200 background jets pass the selection

**Signal efficiency:** How many signal remain after the selection

$$\epsilon_{\text{signal}} = \frac{N_{\text{signal}}^{\text{identified}}}{N_{\text{signal}}^{\text{total}}} \longrightarrow \text{“Signal efficiency”}$$

Four different GNN structures have been tested.

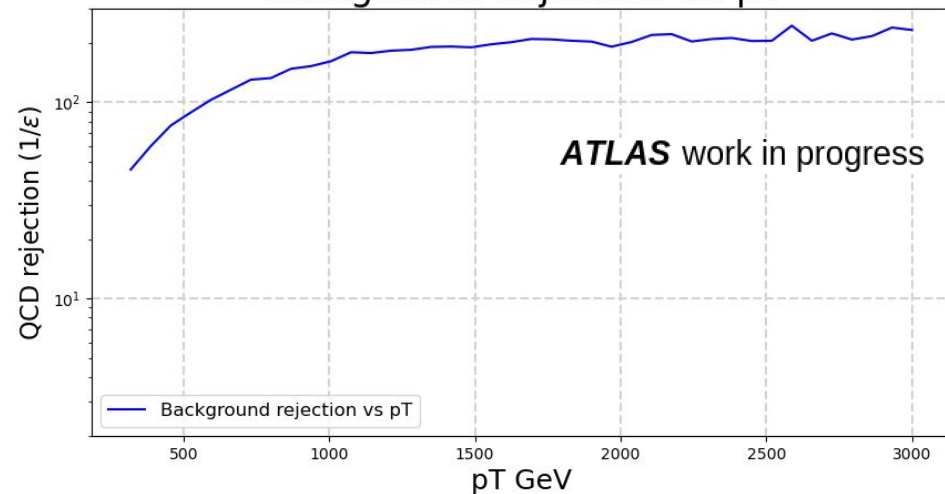
## QCD Rejection



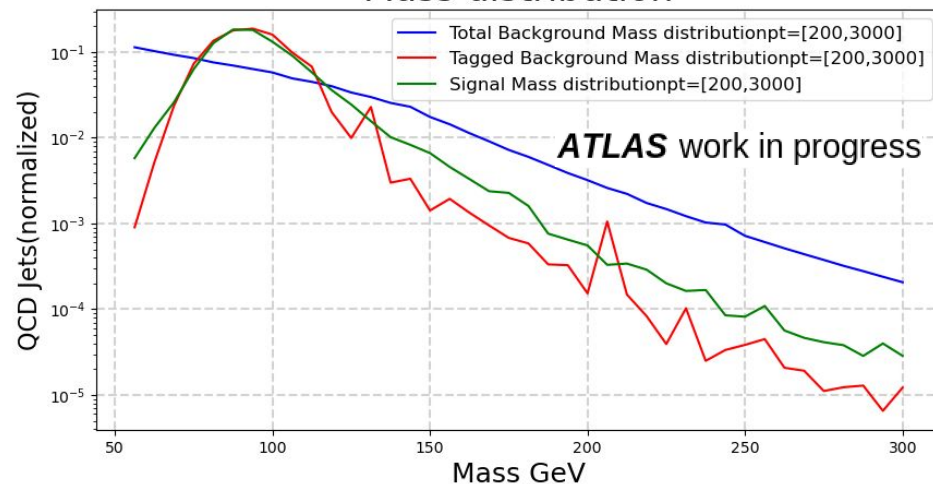
- $50 \text{ GeV} < \text{Jet mass} < 300 \text{ GeV}$
- $|\text{Jet eta}| < 2$
- Jet truth match with W boson
- Number of b Hadrons = 0

## LUNDNet + Number of tracks ( Ntrk )

### Background Rejection VS pT



### Mass distribution



- $50 \text{ GeV} < \text{Jet mass} < 300 \text{ GeV}$
- $|\text{Jet eta}| < 2$
- Jet truth match with W boson
- Number of b Hadrons = 0



In order to mass decorrelated the tagger an Adversarial Neural Network is added, this network is a Mixture gaussian model that learn how is the mass of the Jet using the output score of the classifier.

A new loss function is used: ( f=classifier , r=adversarial )

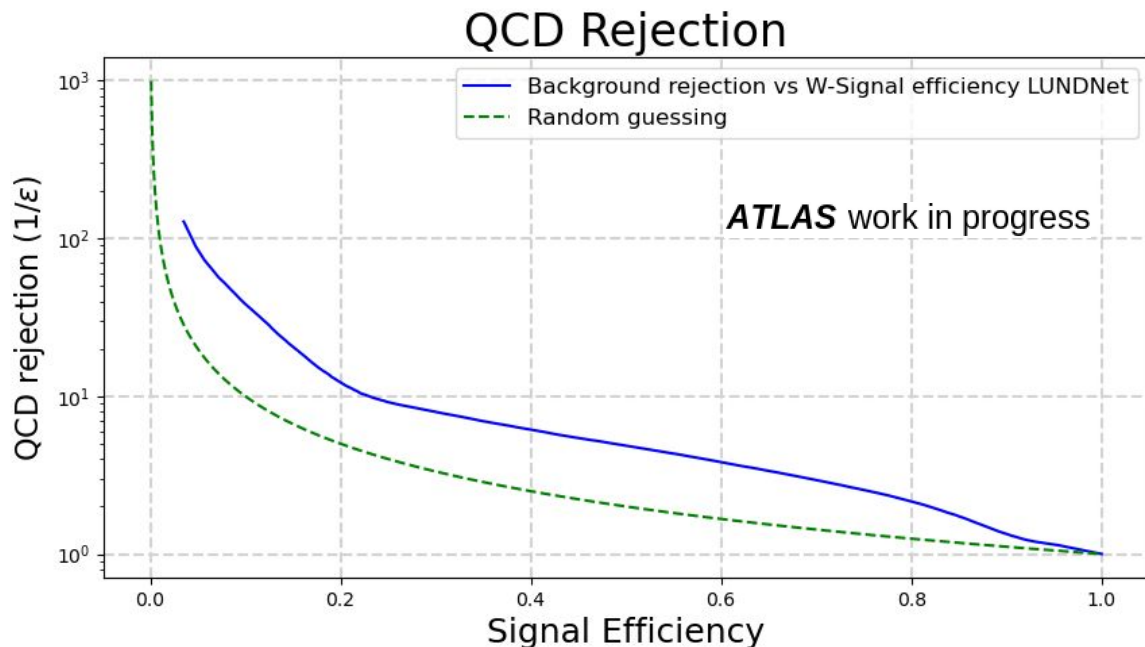
$$E(\theta_f, \theta_r) = \mathcal{L}_f(\theta_f) - \mathcal{L}_r(\theta_f, \theta_r)$$

Where the purpose of the algorithm is:

$$\hat{\theta}_f, \hat{\theta}_r = \arg \min_{\theta_f} \max_{\theta_r} E(\theta_f, \theta_r).$$

# Classifier + adversarial results

## GATNet results (the best one)

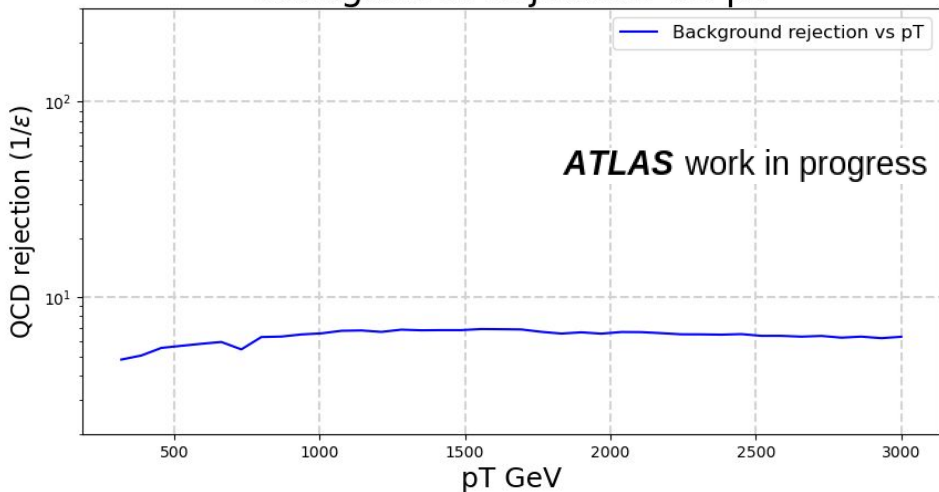


- $50 \text{ GeV} < \text{Jet mass} < 300 \text{ GeV}$
- $|\text{Jet eta}| < 2$
- Jet truth match with W boson
- Number of b Hadrons = 0

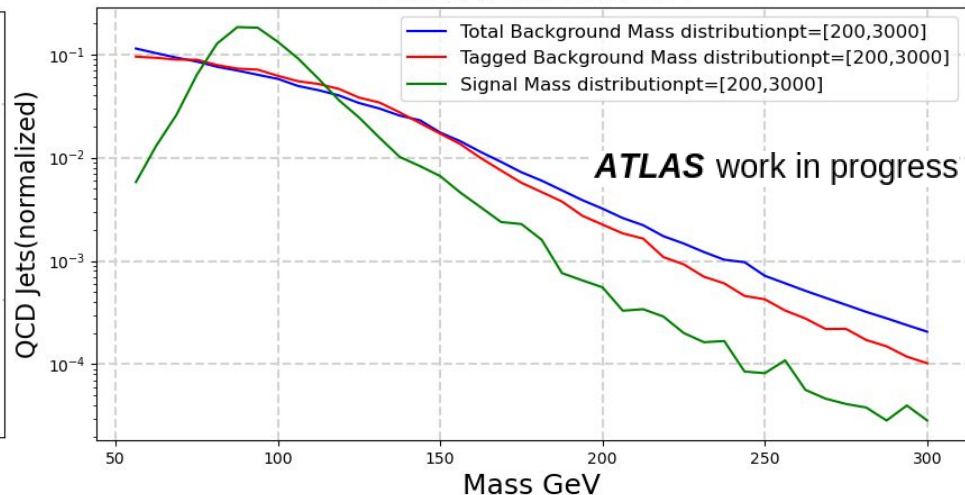
# Classifier + adversarial results

## GATNet result (the best one)

Background Rejection VS pT



Mass distribution



- 50 GeV < Jet mass < 300 GeV
- Jet truth match with W boson
- | Jet eta | < 2
- Number of b Hadrons = 0



Is expected that the emissions coming from parton shower processes and not from Hard processes have lower momentum, so this is the idea to do a Cut off in the emissions used.

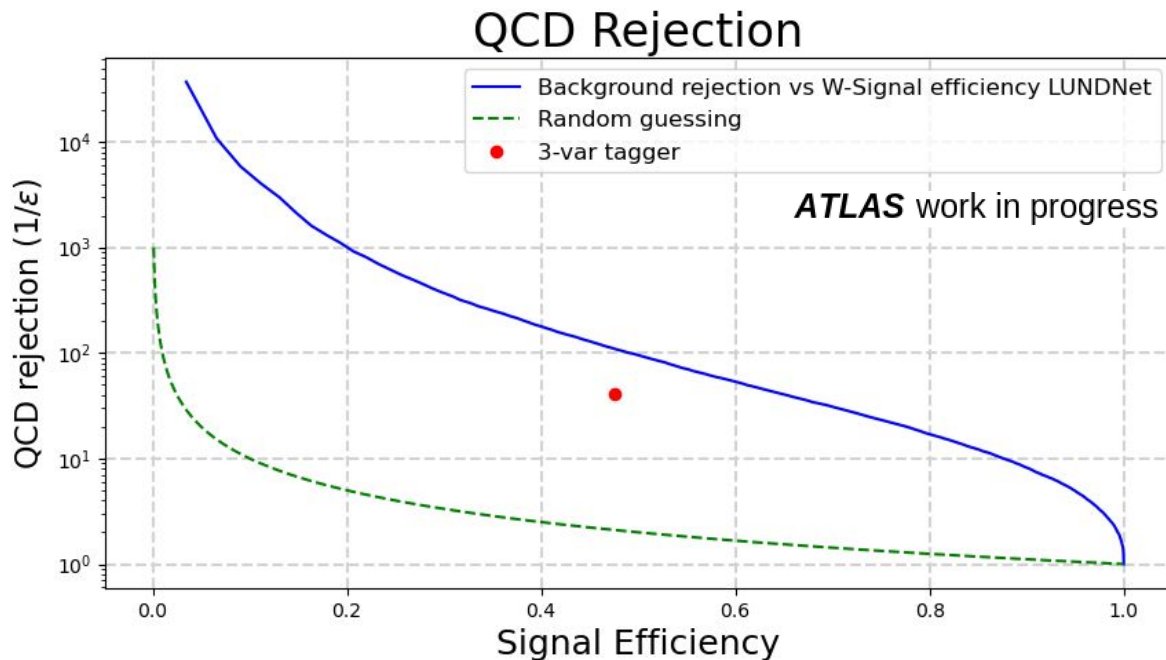
**Only the 9 emissions with highest  $p_T$  are taken.**

**Parton shower ( QCD emissions)  Expected Lower energy**

This let us use more events and remove possible undesired emissions in the training

# Tagger using first 9 emissions

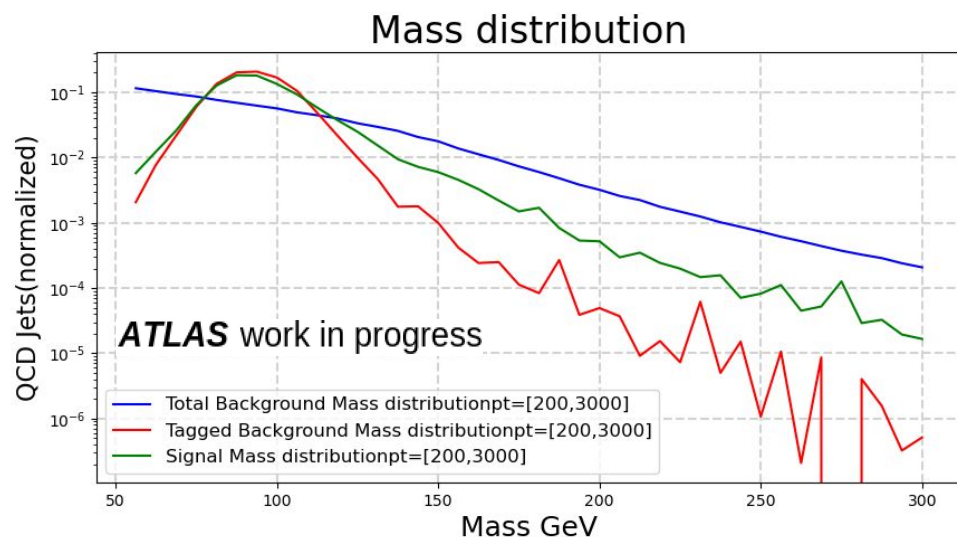
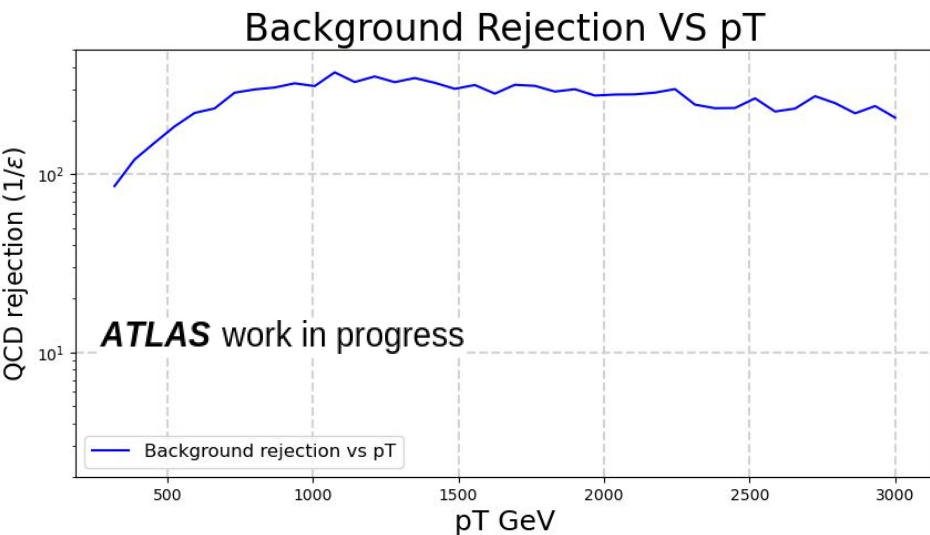
**Train size:** 5% of dijet background and 5% of W signal. Results for LUNDNet + Ntrk



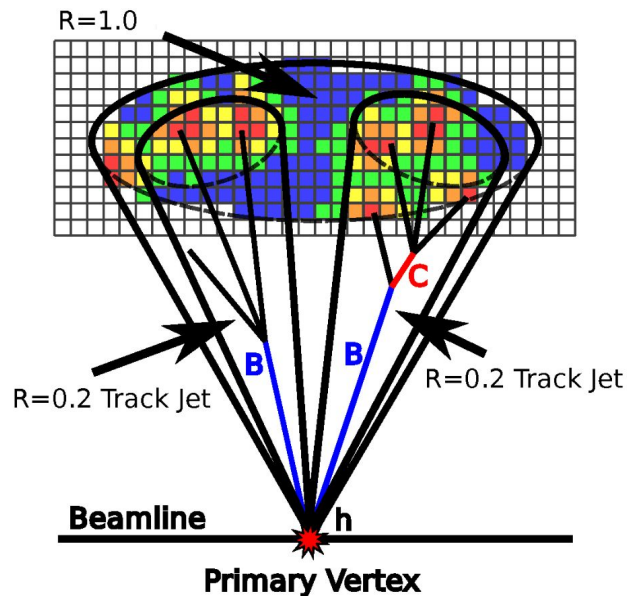
- |  |                                |
|--|--------------------------------|
| ○ $50 \text{ GeV} < \text{Jet mass} < 300 \text{ GeV}$ | ○ Jet truth match with W boson |
| ○ $ \text{Jet eta}  < 2$                               | ○ Number of b Hadrons = 0      |

# Tagger using first 9 emissions

**Train size:** 5% of dijet background and 5% of W signal. Results for LUNDNet + Ntrk



**Classifier + Adversarial result are not done yet!**



**Current Tagger:** Use as input global variables for the large Jet  $R=1.0$  and the output of a NN flavor tagger for small jets  $R=0.2\sim 0.4$  inside the jet.

**Monte Carlo data samples used:**  $G' \rightarrow HH \rightarrow bbbb$  samples.

The mass of  $G'$  is in the range of [400,6000] GeV.

## Signal definition:

$$250 \text{ GeV} < p_T < 2800 \text{ GeV}$$

$$|\eta| < 2$$

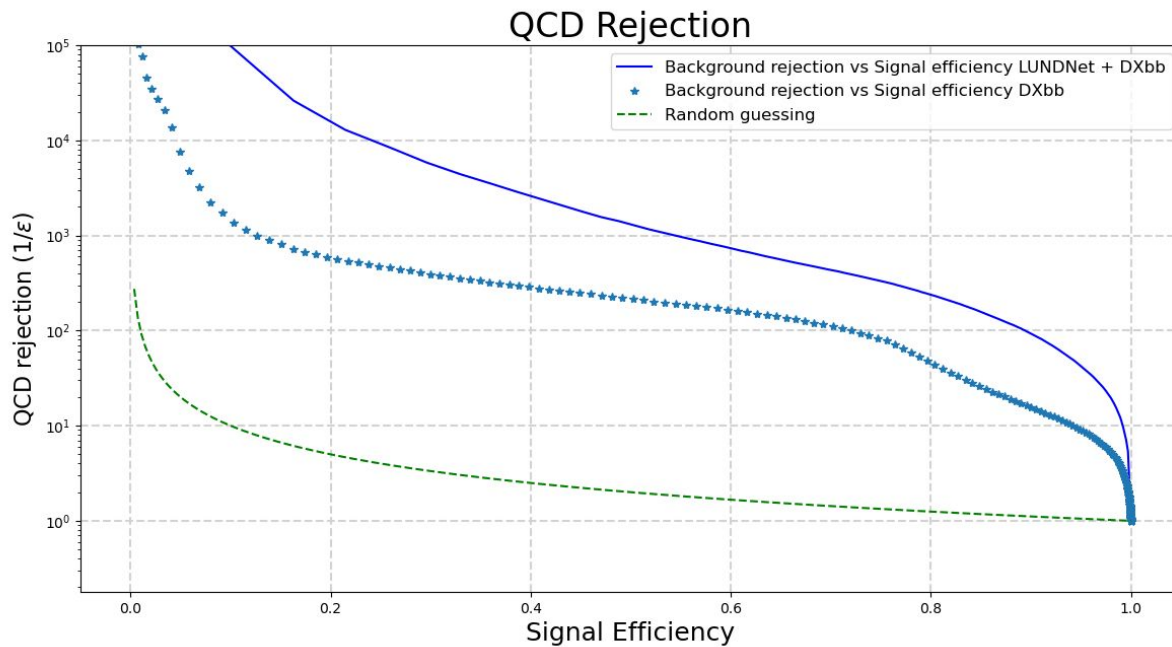
$$76 < M_J / [\text{GeV}] > 146$$

## Signal definition

Jet truth match with H boson

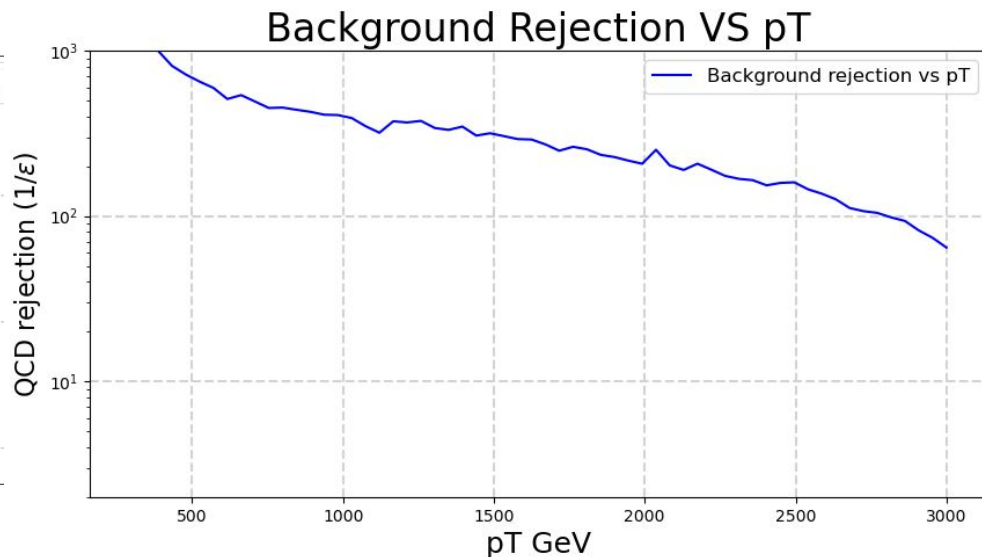
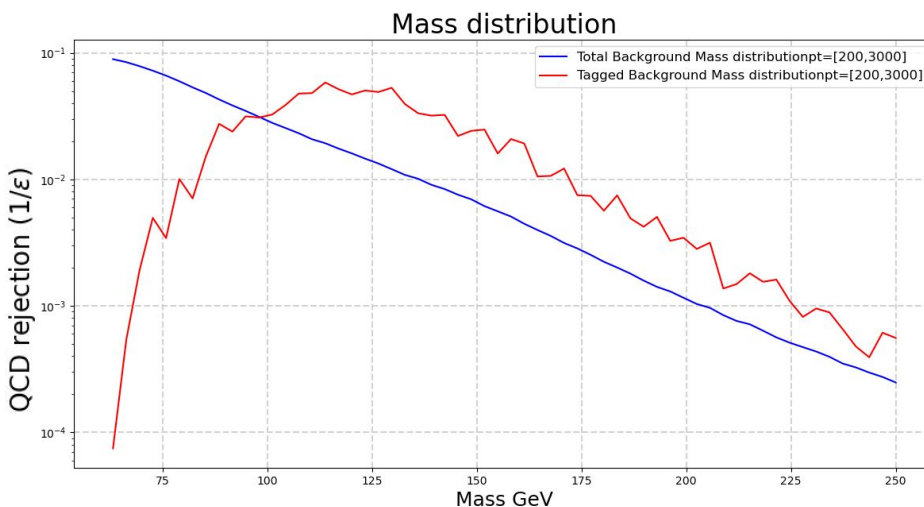
Number of b Hadrons  $> 1$

**Train size:** 2% of dijet background and 40% of H to bb signal. Results for LUNDNet + DXbb tagger



- |                               |                                |
|-------------------------------|--------------------------------|
| ○ 76 GeV < Jet mass < 146 GeV | ○ Jet truth match with H boson |
| ○   Jet eta   < 2             | ○ Number of b Hadrons > 1      |

**Train size:** 2% of dijet background and 40% of H to bb signal. Results for LUNDNet + DXbb tagger

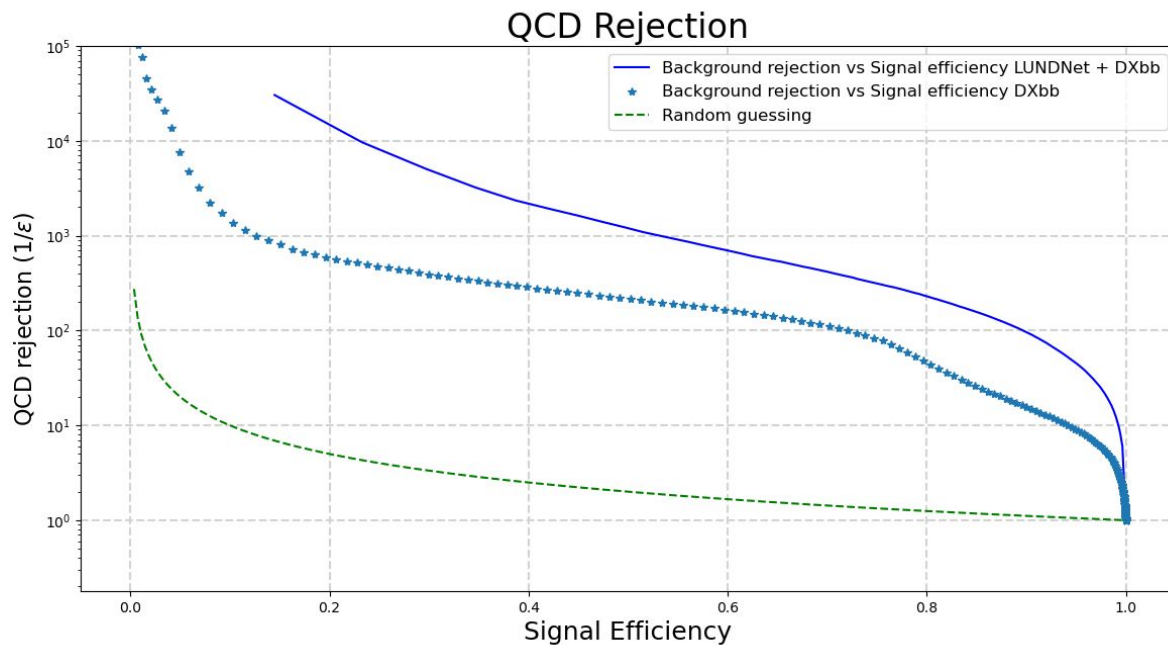


- $76 \text{ GeV} < \text{Jet mass} < 146 \text{ GeV}$
- $|\text{Jet eta}| < 2$
- Jet truth match with H boson
- Number of b Hadrons  $> 1$



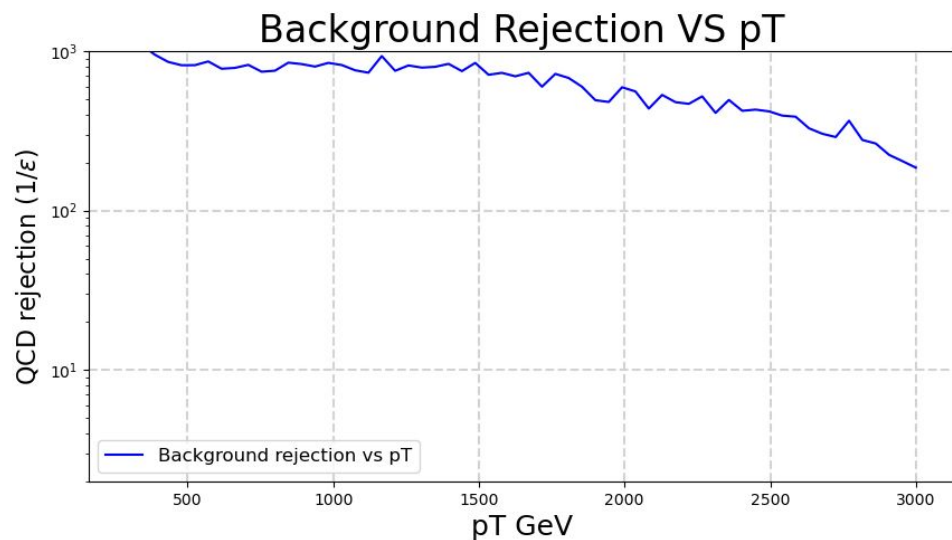
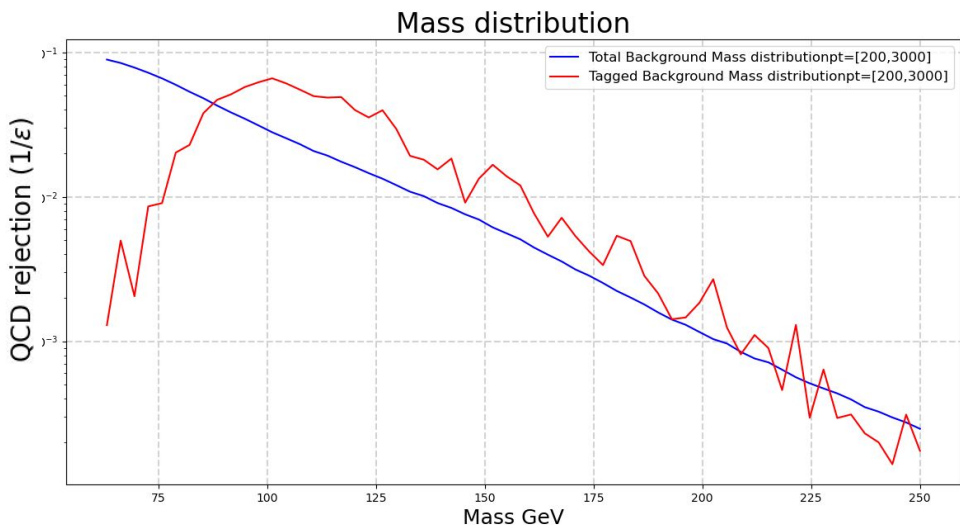
# Higgs to bb: Adversarial Results

**Train size:** 2% of dijet background and 40% of H to bb signal. Results for LUNDNet + DXbb tagger



- 76 GeV < Jet mass < 146 GeV
- Jet truth match with H boson
- | Jet eta | < 2
- Number of b Hadrons > 1

# Higgs to bb: Adversarial Results



- $76 \text{ GeV} < \text{Jet mass} < 146 \text{ GeV}$
- $|\text{Jet eta}| < 2$
- Jet truth match with H boson
- Number of b Hadrons  $> 1$

## W tagger:

- Presented 4 GNN architectures with improved performance over the currently boosted W boson taggers.
- Optimized methods outperform current methods by around 50%, however further improvements could be applied.
- Algorithm improvements are still needed to increase the background rejection of the mass decorrelated taggers.

## H to bb tagger:

- Using Lund Plane variables to improve the current tagger gives a tagger which it's around  $\sim 10$  times better.
- It's necessary to improve Adversarial + classifier algorithm in order to improve the mass decorrelation of the model.



UNIVERSIDAD  
NACIONAL  
DE COLOMBIA



*Thanks for your attention :)*





UNIVERSIDAD  
NACIONAL  
DE COLOMBIA

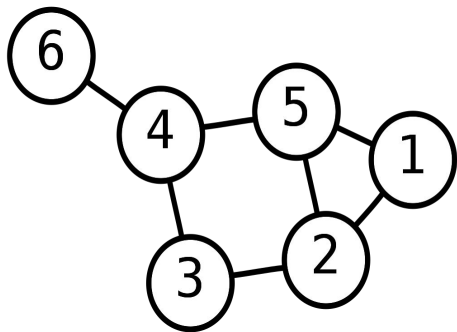


**BACKUP ;)**

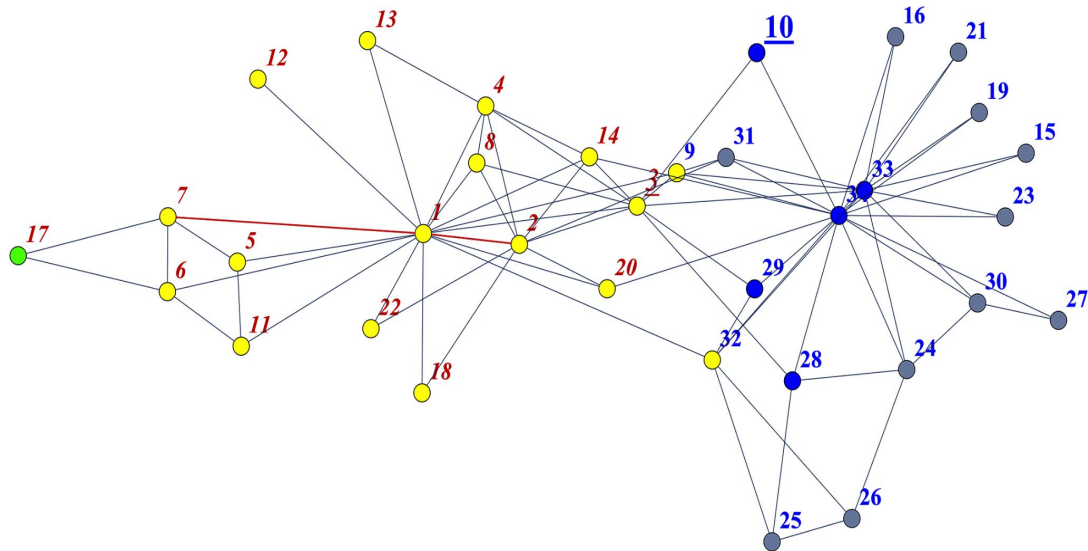


# Graph Neural Networks

**Garphs:** “mathematical structures used to model pairwise relations between objects. A graph in this context is made up of **vertices** (also called *nodes* or *points*) which are connected by **edges** (also called *links* or *lines*)”

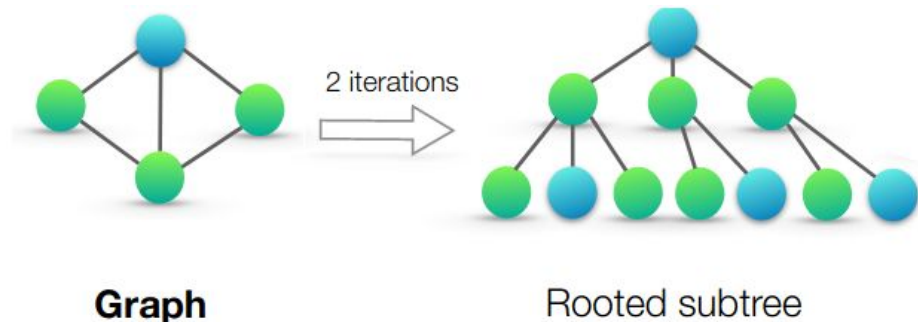


A graph with six vertices and seven edges.



# Graph Neural Networks

We begin by summarizing some of the most common GNN models and, along the way, introduce our notation. Let  $G = (V, E)$  denote a graph with node feature vectors  $X_v$  for  $v \in V$ . There are two tasks of interest: (1) *Node classification*, where each node  $v \in V$  has an associated label  $y_v$  and the goal is to learn a representation vector  $h_v$  of  $v$  such that  $v$ 's label can be predicted as  $y_v = f(h_v)$ ; (2) *Graph classification*, where, given a set of graphs  $\{G_1, \dots, G_N\} \subseteq \mathcal{G}$  and their labels  $\{y_1, \dots, y_N\} \subseteq \mathcal{Y}$ , we aim to learn a representation vector  $h_G$  that helps predict the label of an entire graph,  $y_G = g(h_G)$ .



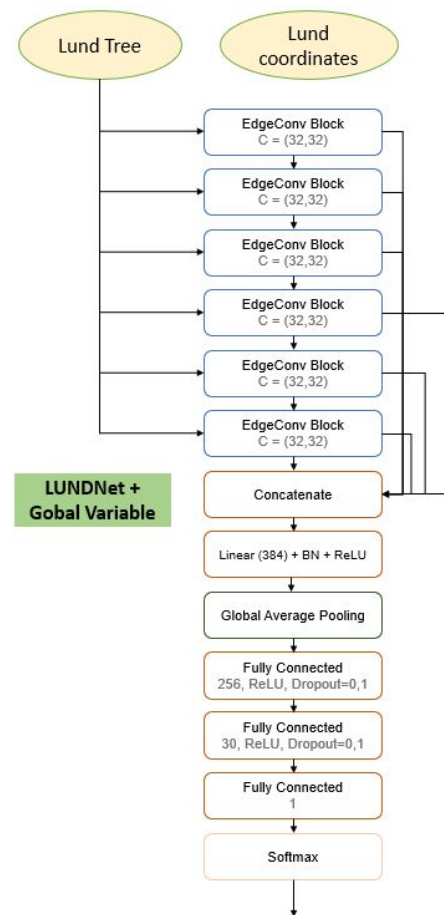
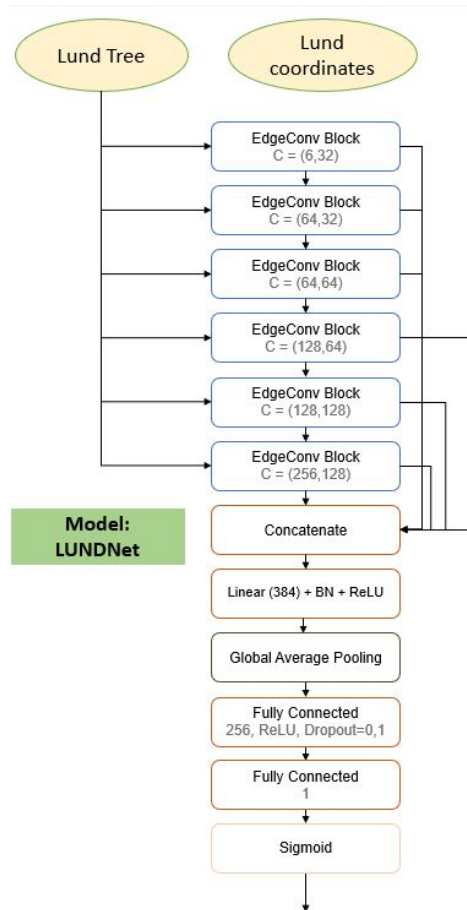
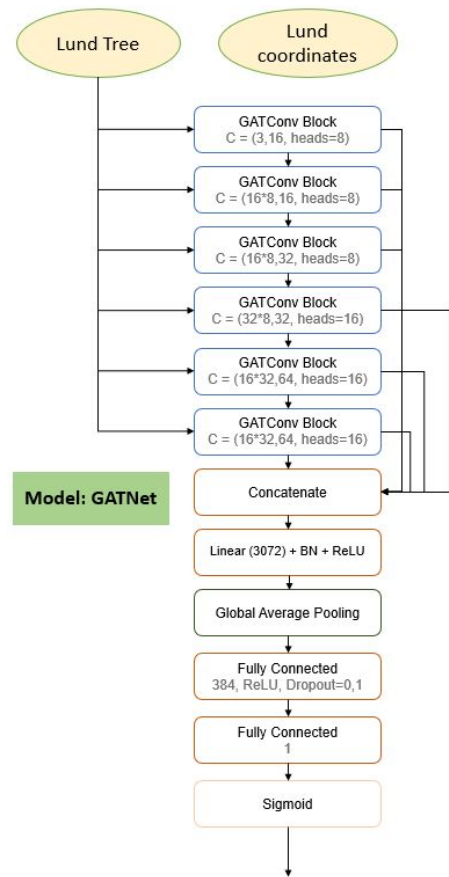
After  $k$  iterations of aggregation, a node is represented by its transformed feature vector, which captures the structural information

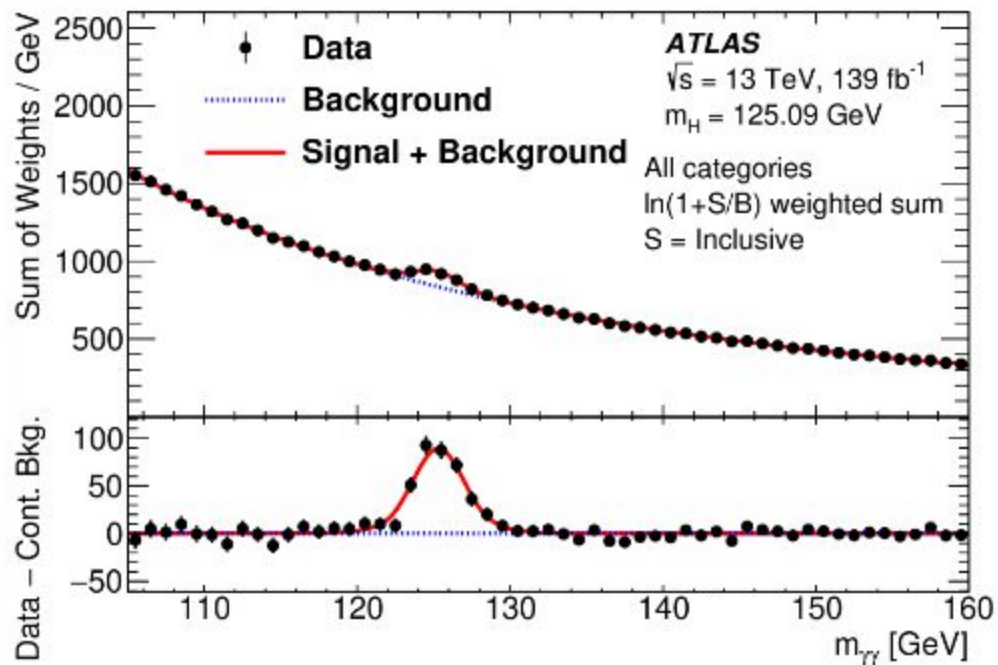
$$h_G = \text{READOUT}(\{h_v^{(K)} \mid v \in G\}).$$

Plots and definitions taken from: **HOW POWERFUL ARE GRAPH NEURAL NETWORKS?**

<https://arxiv.org/pdf/1810.00826.pdf>

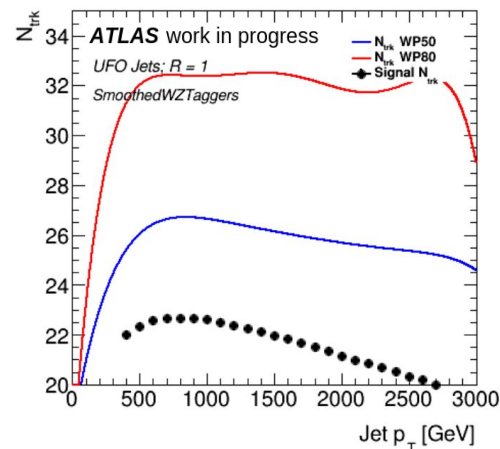
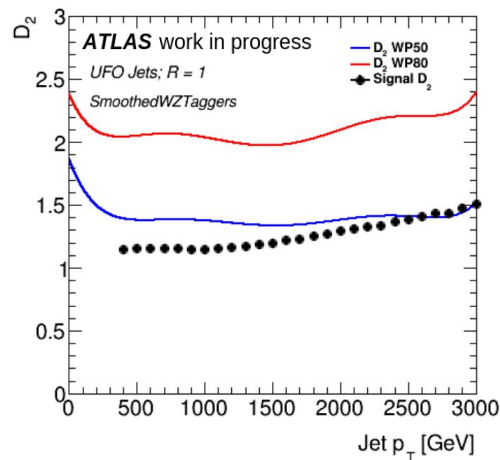




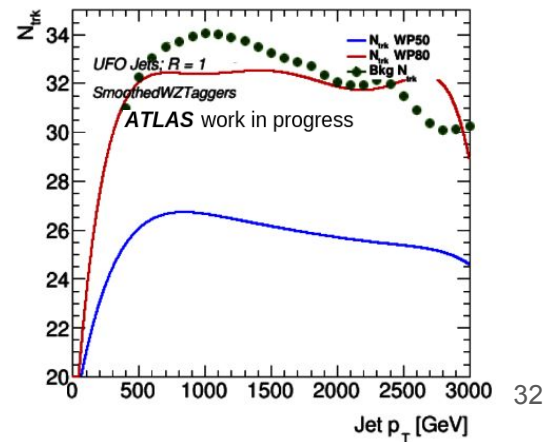
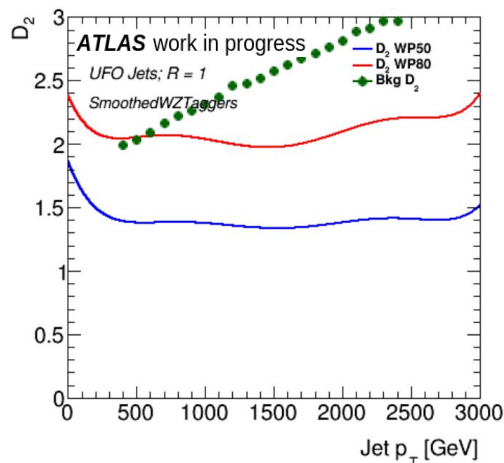


# Standard Tagger performance

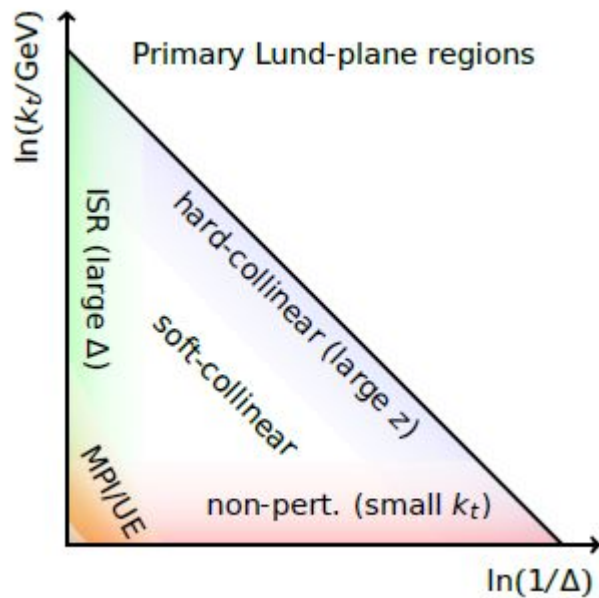
## Signal performance



## Background performance

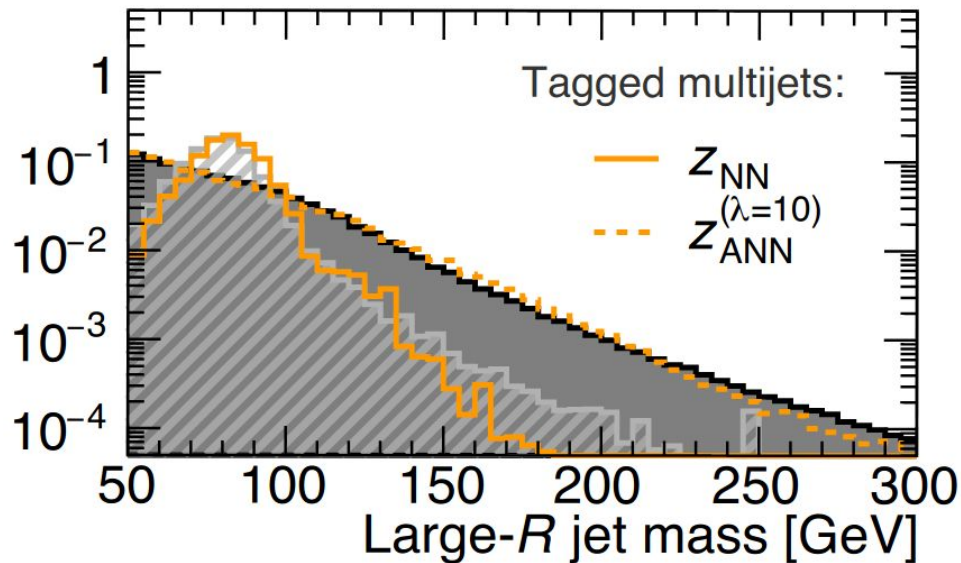


# Lund Plane regions



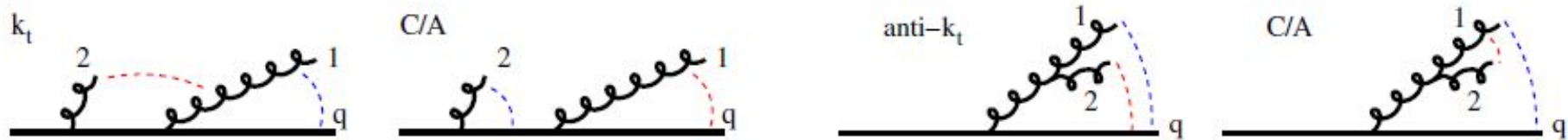
Using  $\ln(Kt)$  and  $\ln(1/\Delta)$  is easy to identify different regions.

## Mass sculpting



After the selection the mass profile of the background signal changed! To avoid that we could use an Adversarial Neural Network!

## Declustering algorithms



- The Declustering algorithms tries to go inside the hadronization history in order to determine where each emission is coming from.

### Contribuciones a NLO:

$$\bar{\rho}_2^{(k_t)}(\Delta, \kappa) \simeq -4C_F^2 \ln^2 \frac{\Delta}{\kappa} + \mathcal{O}(L) . \quad \longrightarrow \quad \text{Kt algorithm}$$

$$\bar{\rho}_2^{(\text{anti-}k_t)}(\Delta, \kappa) \simeq +8C_F C_A \ln^2 \frac{\Delta}{\kappa} + \mathcal{O}(L) . \quad \longrightarrow \quad \text{Anti-Kt algorithm}$$

$$\bar{\rho}_{2,\text{rc}}^{(\text{C/A})}(\Delta, \kappa) = \bar{\rho}_1(\Delta, \kappa) 4\pi b_0 \ln \frac{1}{\kappa} + \mathcal{O}(1) . \quad \longrightarrow \quad \text{C/A algorithm}$$