

tracklength
projections
precision
recall
track
smoothness
signal
clustering
decision_trees
detector
ROC
diffractive
on-shell
time_residuals
PMTs
Feynman
Z-boson
XGBOOST
DOMs
coherent
SVD
neutrinos
validation
CCFR
testing
PCA
waveforms
MC
IceCube
training
AUC
confusion_matrix
tridents
strings
Kmeans
background
muons
data
Cherenkov
SM
DIS



SEARCH FOR RIDENT EVENTS WITH

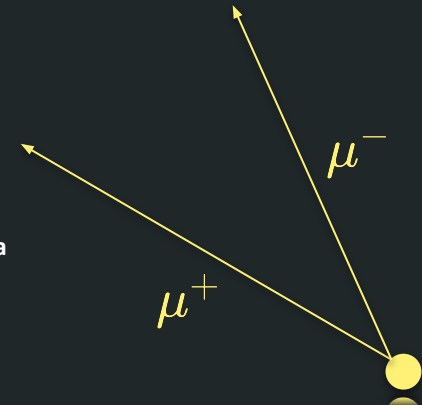


Nakul Aggarwal

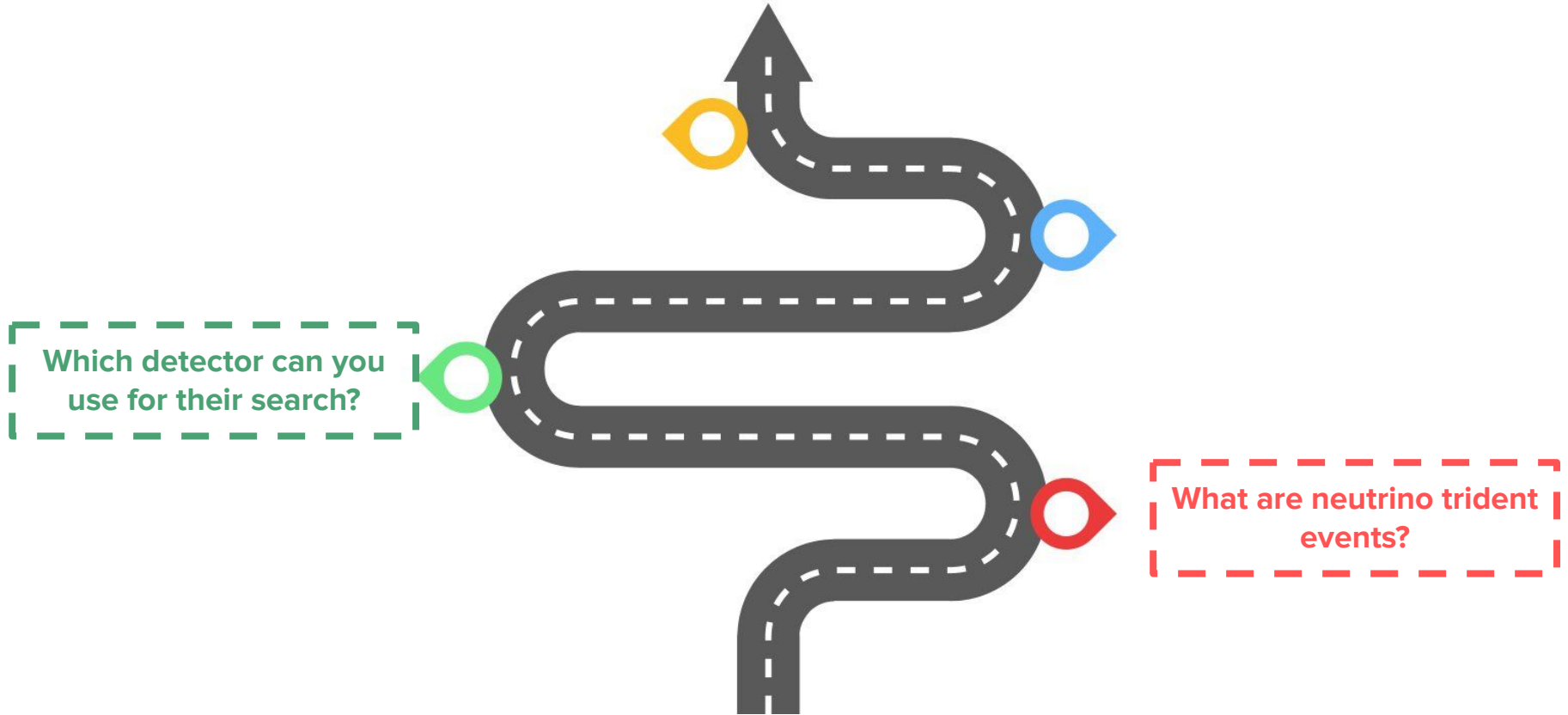
Department of Physics, University of Alberta, Edmonton, Alberta

NOV 3, 2022

SUPERVISOR: JUAN PABLO YÁÑEZ GARZA



ROADMAP [2/4]



ROADMAP [3/4]



ROADMAP [4/4]

Can you use a ML technique using the features extracted from the previous step?

Which detector can you use for their search?

What features can you use for signal and background separation?

What are neutrino trident events?

SHALL WE BEGIN?

NEUTRINO TRIDENT PRODUCTION

DEEP INELASTIC SCATTERING (DIS): MUONIC CHANNEL

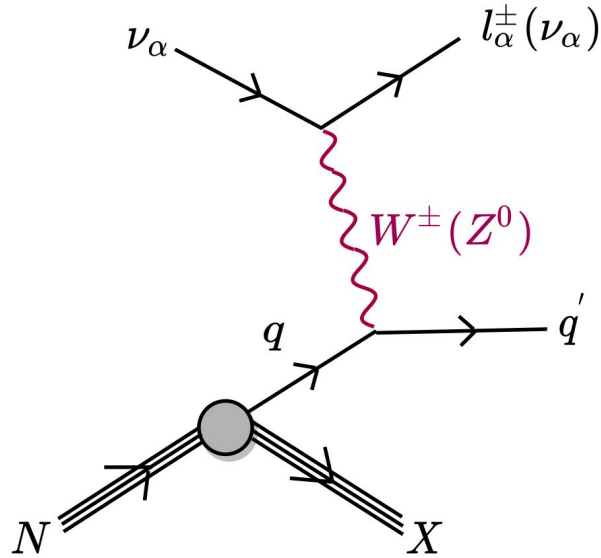


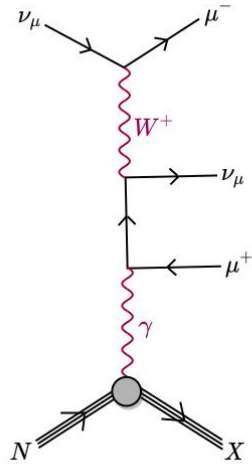
Fig: Feynman diagram for DIS: The dominant interaction involves one outgoing lepton.

- ❖ **Lepton-hadron scattering:** An incoming neutrino interacts with a nucleus N and produces a charged lepton.
- ❖ If the energy of the neutrino is very high, nucleus is shattered and emits many new particles, a process called hadronization.
- ❖ **Single Muon Channel:** If the incoming neutrino is muon neutrino, then the outgoing lepton is a muon.
- ❖ **Dominant Process.**

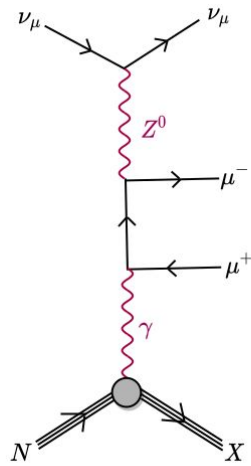
Charged Current DIS (CC-DIS): If the exchange is via a W boson.

Neutral Current DIS (NC-DIS): If the exchange is via a Z boson.

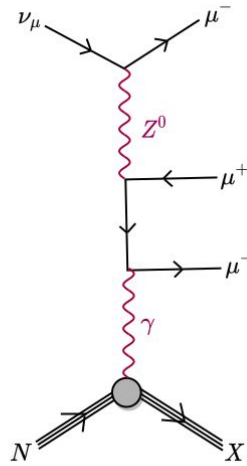
NEUTRINO TRIDENT EVENTS: MUONIC CHANNEL



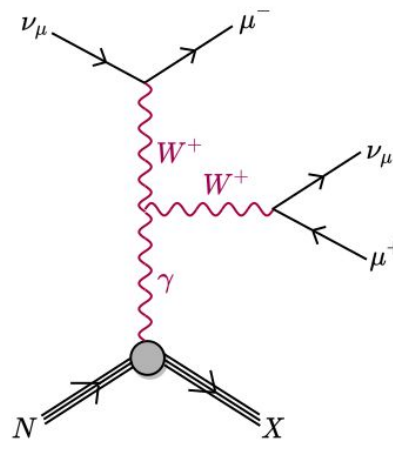
(a)



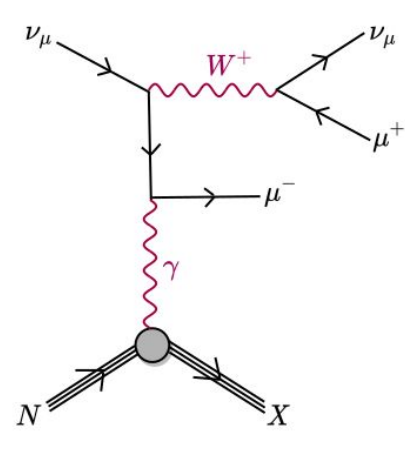
(b)



(c)



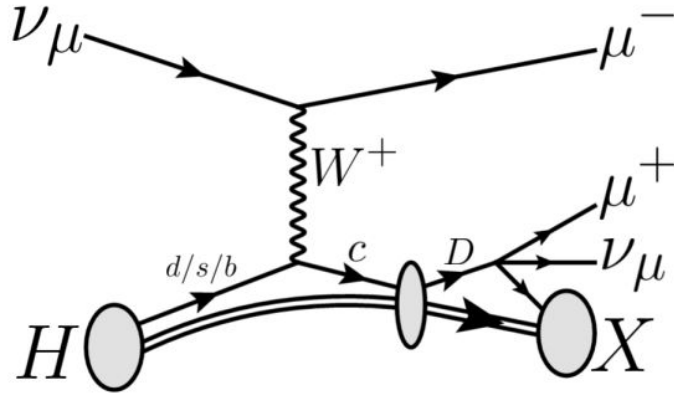
(d)



(e)

- ❖ **NTP: 3 leptons are produced (2 charged and 1 neutral). Hence, the name trident.**
- ❖ **If the incoming neutrino is a muon, and the outgoing leptons are 2 muons and a muon neutrino, then this channel is called muonic channel.**
- ❖ **Sub-dominant electroweak process due to addition of more vertices.**

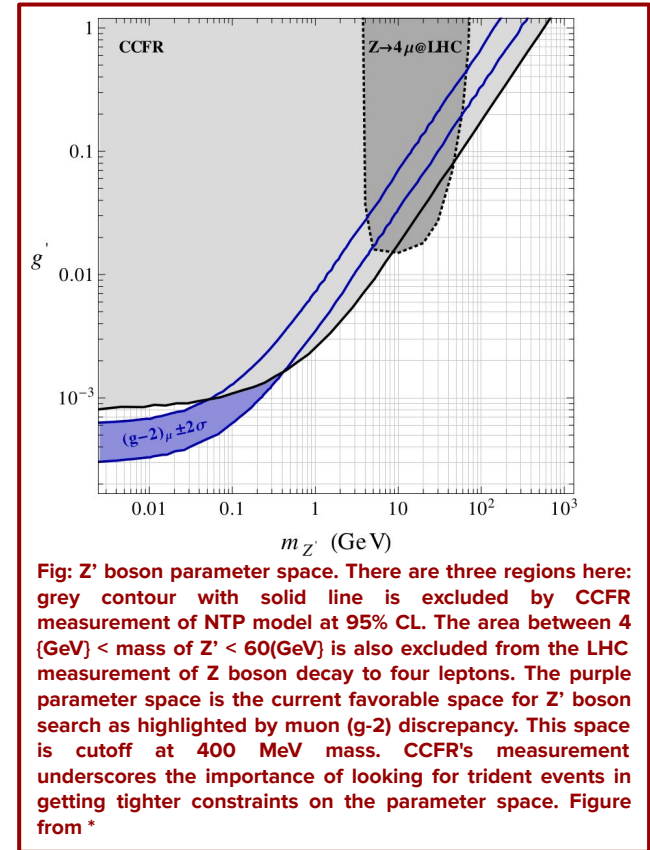
CHARM MUONS



- ❖ Charm decays into a secondary muon. This is also a 2 muon signature.
- ❖ This cross-section is higher than the trident cross-section as this is a subset of CC-DIS interaction.

WHY SHOULD WE LOOK FOR DIMUONS?

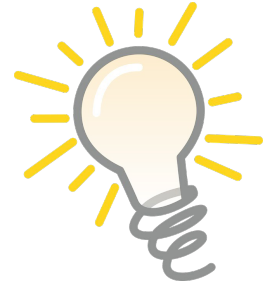
- ❖ The event rate of this process is a powerful probe to a well-motivated parameter space of new physics beyond the Standard Model.
- ❖ A deviation from the event rate predicted by the SM could be an indication of new interactions mediated by new gauge bosons
- ❖ **EXTRA CONTRIBUTIONS:** In particular, BSM (Beyond Standard Model) processes like supersymmetry can look for additional supersymmetric particles like Z' etc. in place of W/Z bosons.
- ❖ Thus, it serves as a powerful electroweak test for Standard Model and physics beyond Standard Model.



* W. Altmannshofer, S. Gori, M. Pospelov, and I. Yavin, "Neutrino trident production: A powerful probe of new physics with neutrino beams," Physical Review Letters, vol. 113, no. 9, p. 091 801, 2014.

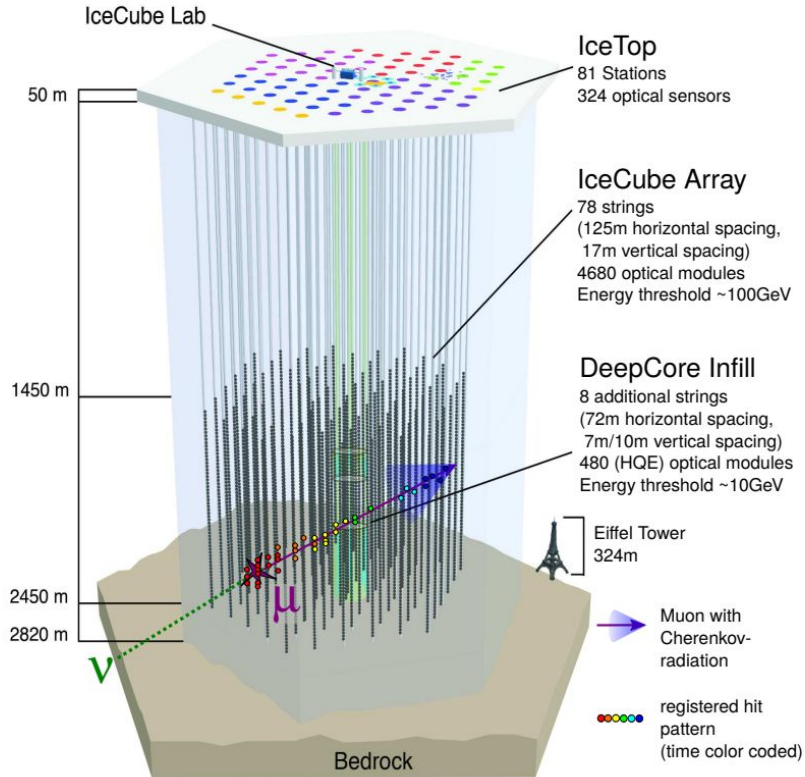
WHERE TO LOOK FOR TRIDENTS?

- ❖ **Dimuon events in the high energy regime (100 GeV ~ 10 PeV) [2] where increase in the cross-section can lead to the observation of trident events in neutrino telescope detectors like IceCube, Antares etc.**
- ❖ **The detections of TeV–PeV neutrinos by IceCube have already been a breakthrough.**
- ❖ **High instrumented volume of IceCube (1km³)**
- ❖ **IceCube has 10 years of data.**



ICECUBE DETECTOR

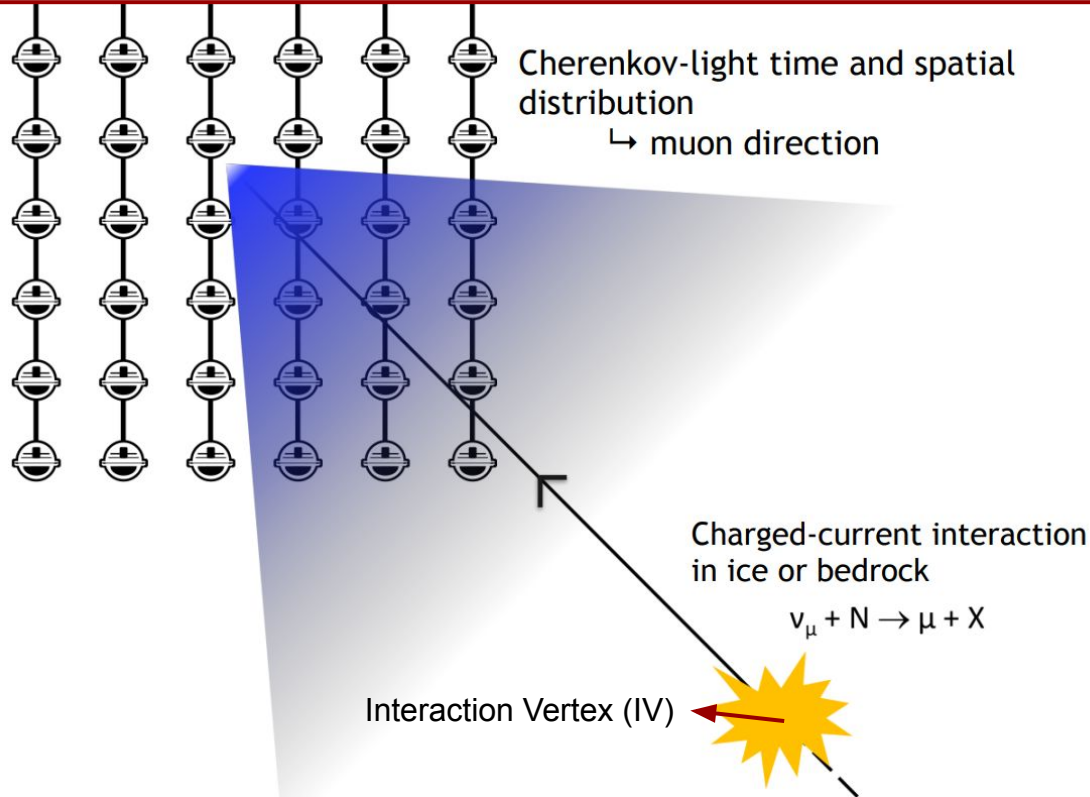
ICECUBE DETECTOR



- ❖ **Neutrino Telescope at the geographical South Pole**
- ❖ **Optical sensors (Digital Optical Modules: DOMs) deployed in a 3-D hexagonal lattice along cables ('strings'), starting from 1.5 km below Earth's surface to minimize atmospheric background from cosmic rays.**

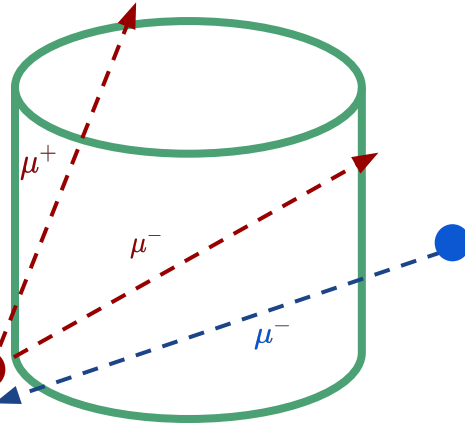
Figure from:
<https://user-web.icecube.wisc.edu/~mda65/talks/thesis.pdf>

CHERENKOV CONE: OPTICAL EQUIVALENT TO A SONIC BOOM



- ❖ A charged particle in ice can travel faster than speed of light and emit Cherenkov radiation.
- ❖ It is this light that is measured by DOMs and quantized into discrete hits. Hence the prefix: digital

CLASSIFICATION



DIMUONS



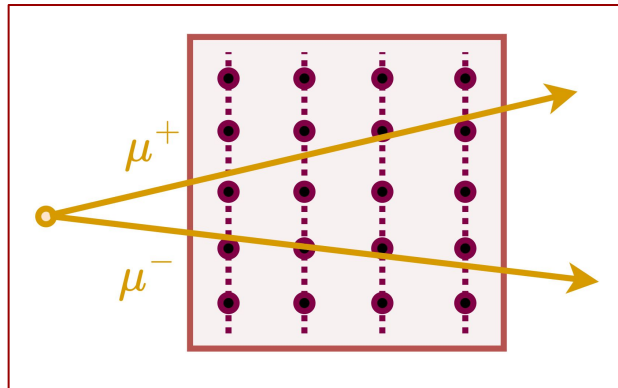
SINGLE MUON

SEARCH FOR TRIDENT EVENTS

DIMUON CLASSES

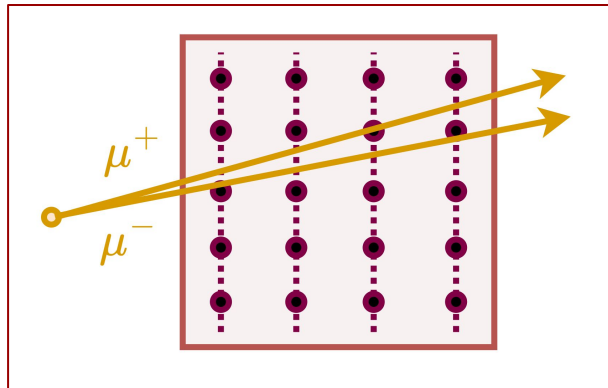


CLASS-A



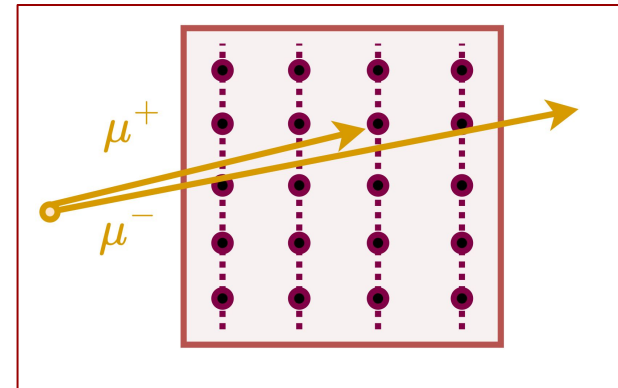
- ◆ Track_length: Both $\geq 200\text{m}$
- ◆ Separation: $\geq 25\text{m}$

CLASS-B



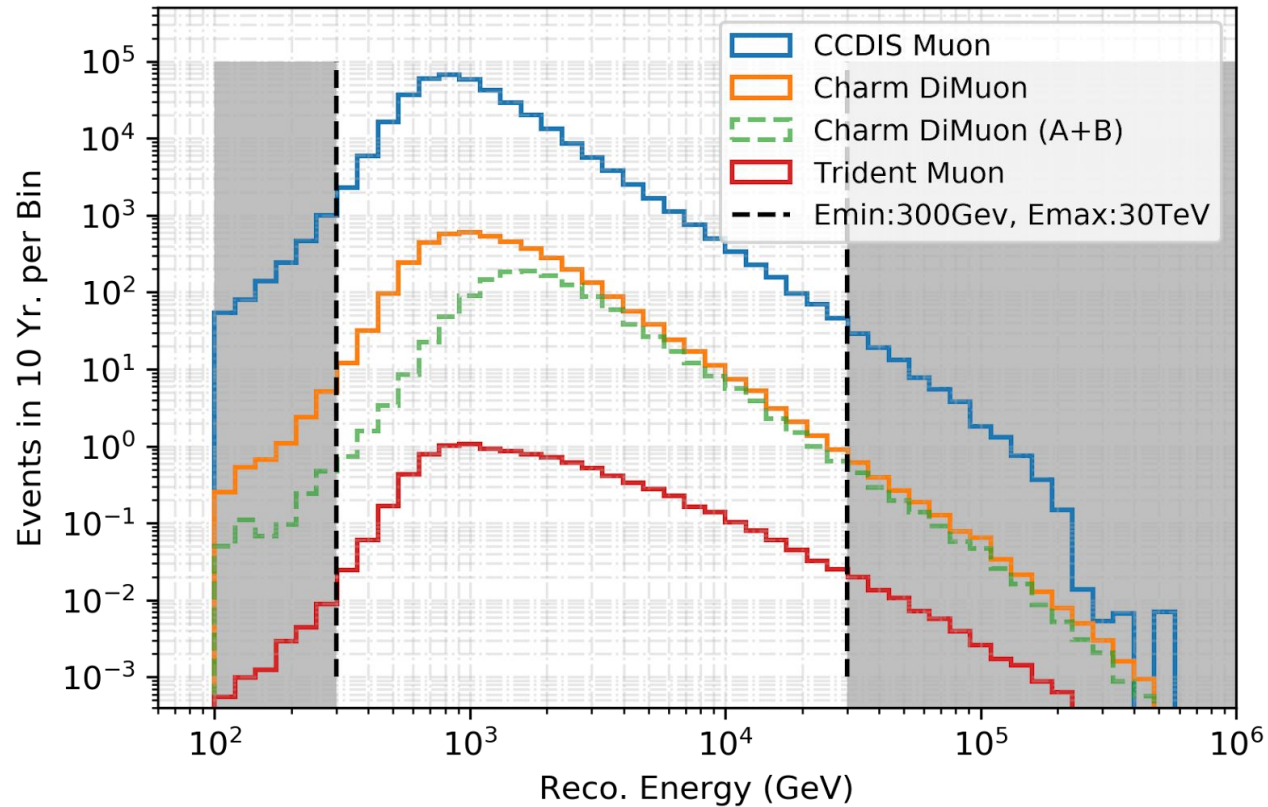
- ◆ Track_length: Both $\geq 200\text{m}$

CLASS-C

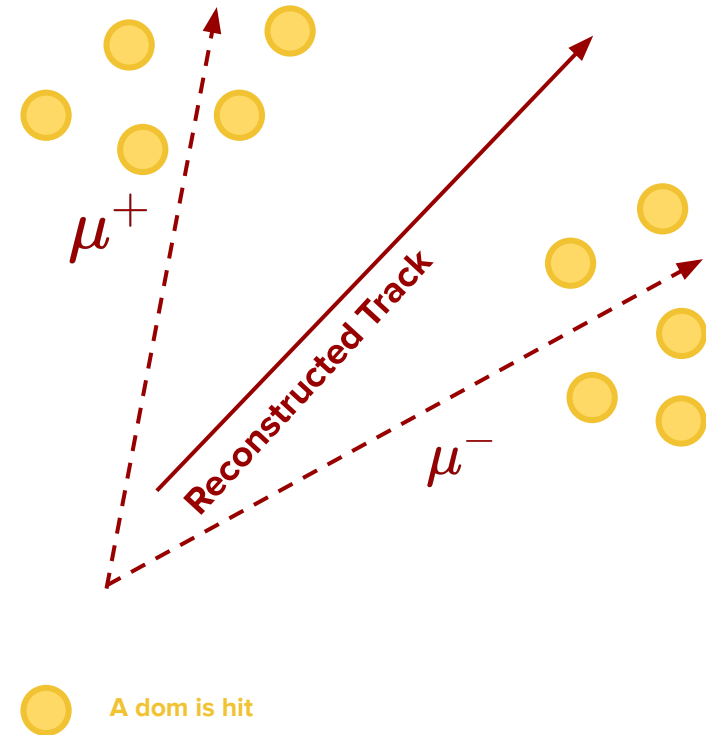
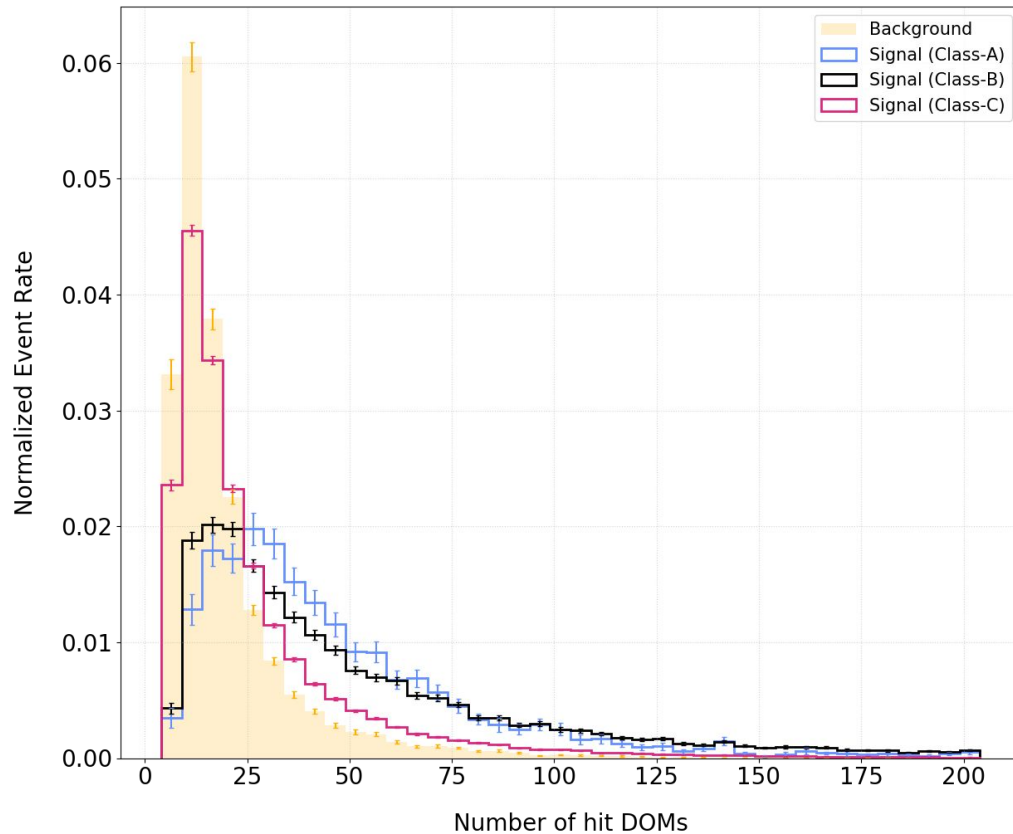


- ◆ Track_length: At least one $< 200\text{m}$

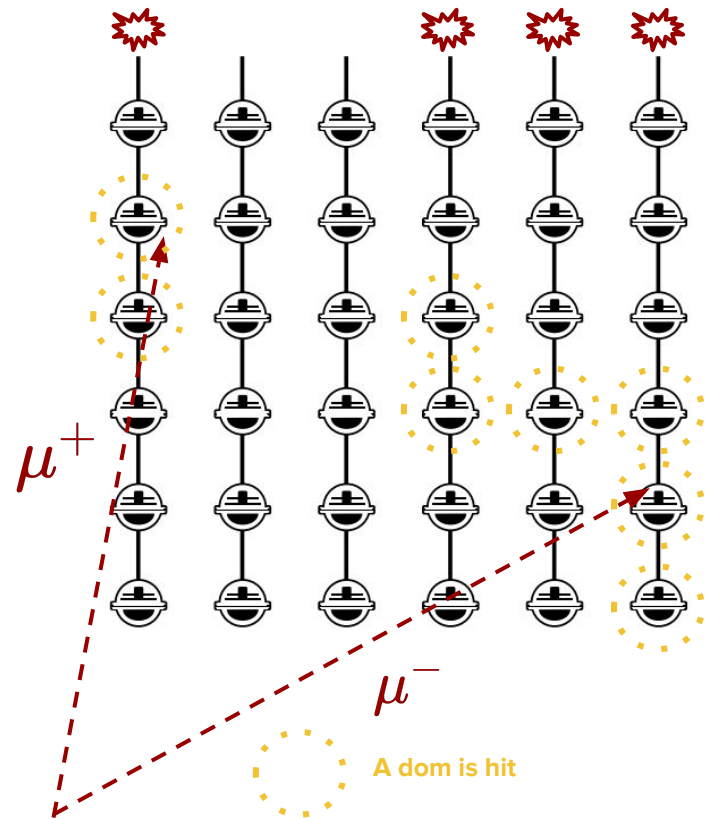
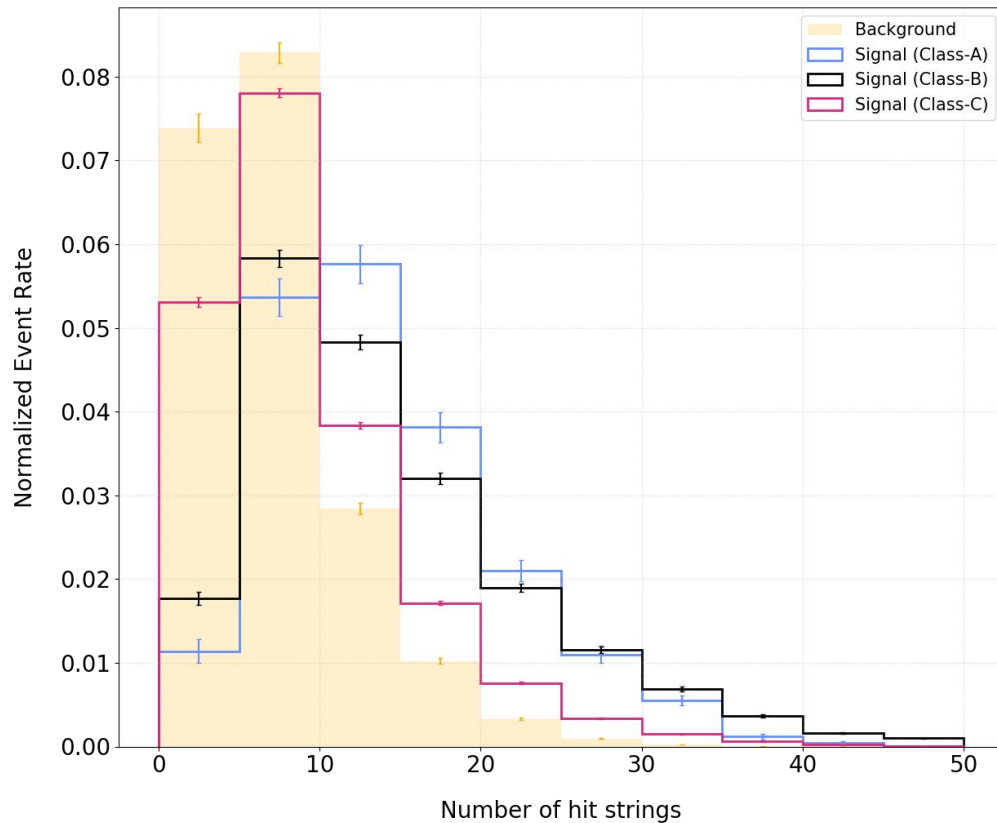
EVENT RATE



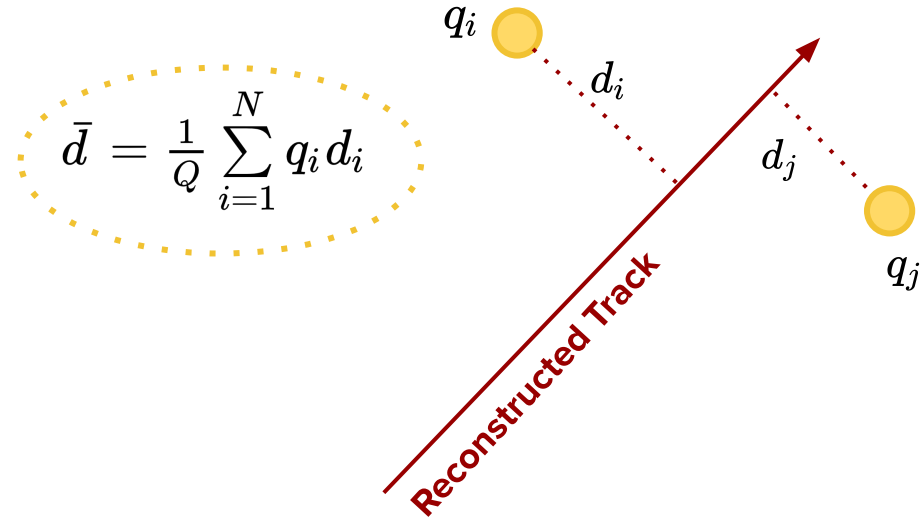
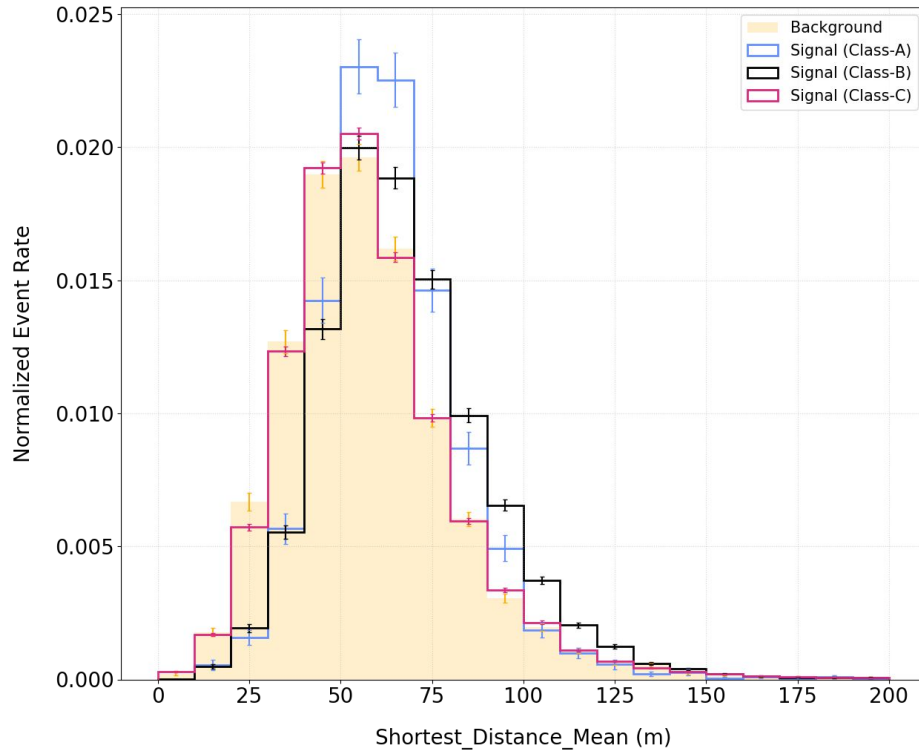
FEATURES: NUMBER OF HIT DOMs



FEATURES: NUMBER OF HIT STRINGS



FEATURES: SHORTEST DISTANCE MEAN



N : Number of hit DOMS

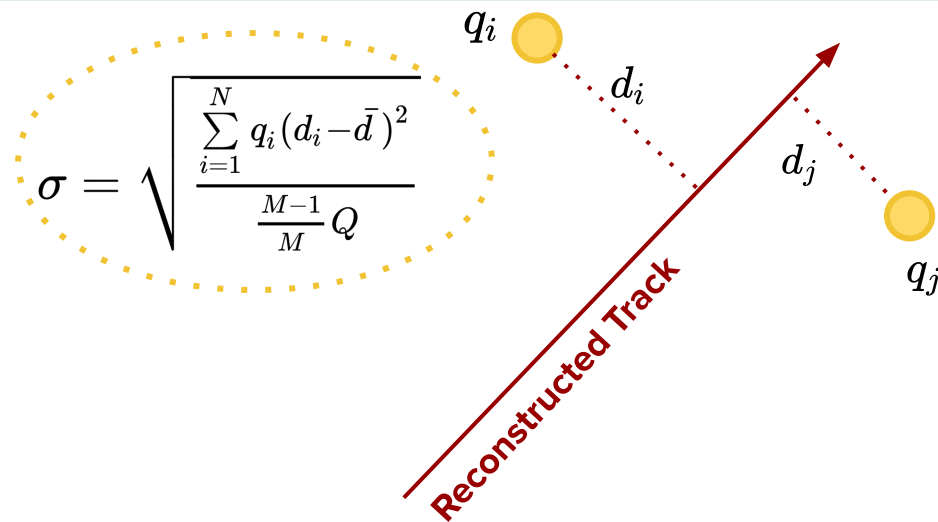
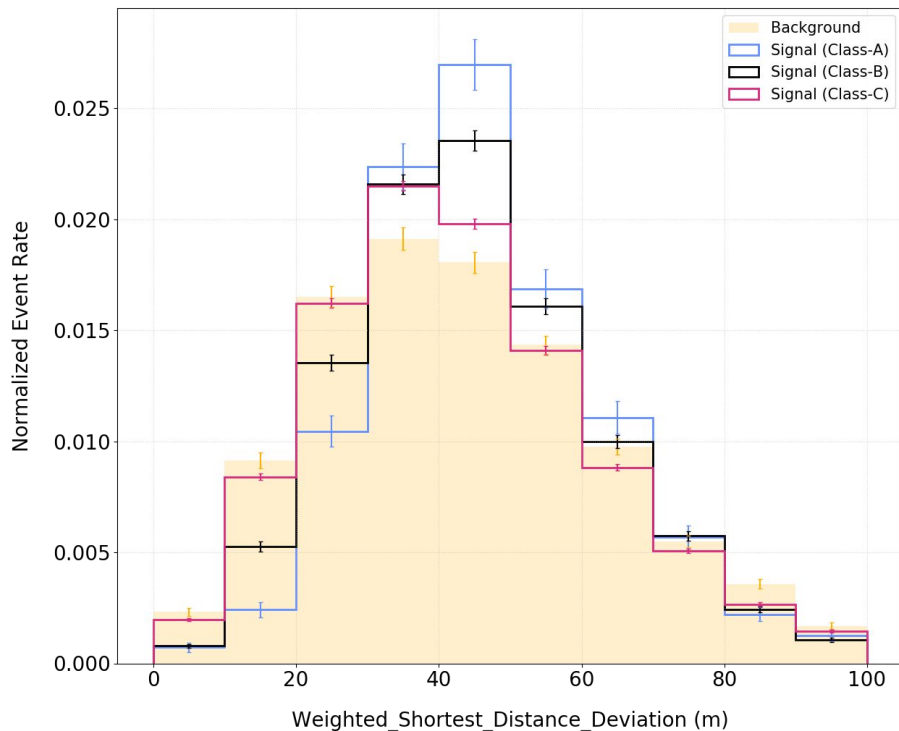
Q : Total charge (light) of all hit DOMS

d_i : Distance of closest approach of the i th hit DOM from the track.

q_i : Total light seen by i th hit DOM.

\bar{d} : Average separation of hit DOMs from the track.

FEATURES: WEIGHTED SHORTEST DISTANCE DEVIATION



M : Number of non-zero charge values

σ : Weighted standard deviation of the distance of closest approach.

FEATURES: CLUSTERING [1/2]

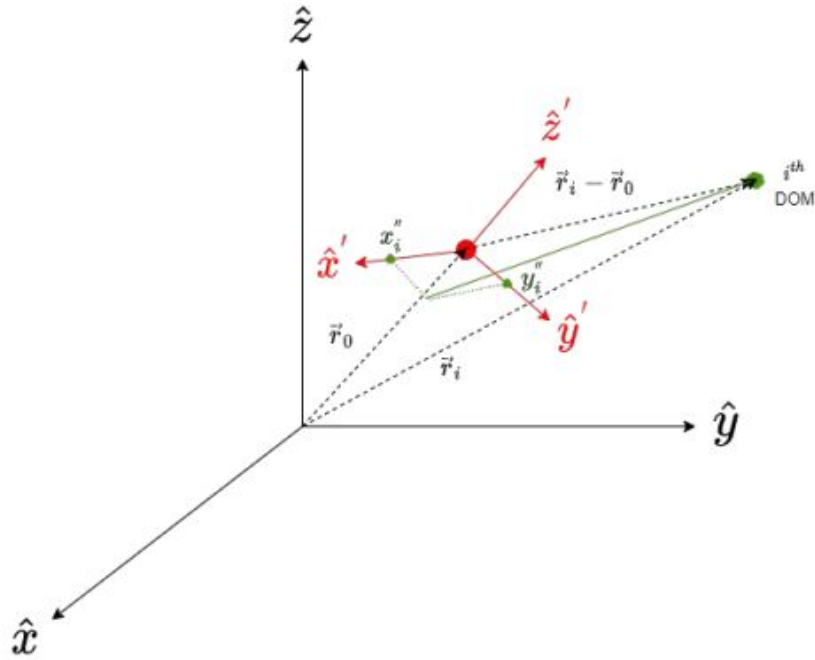
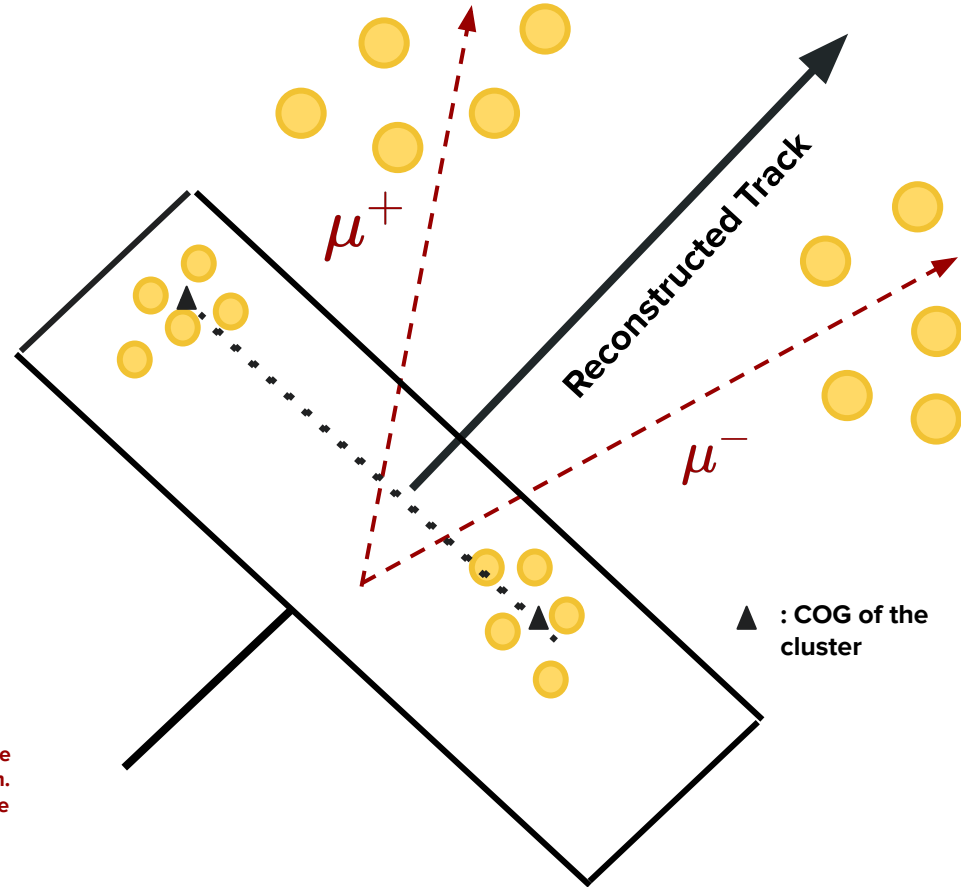
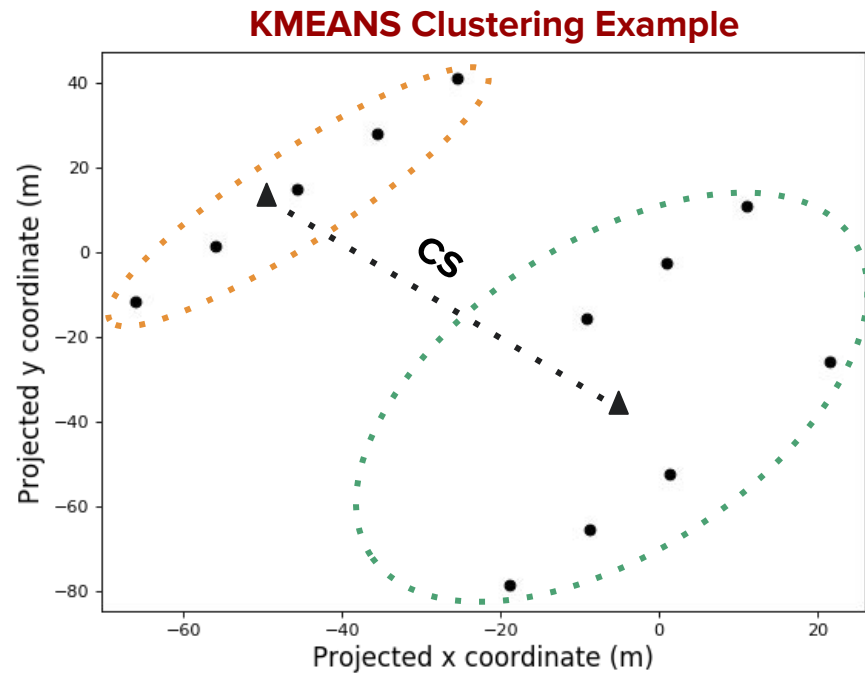
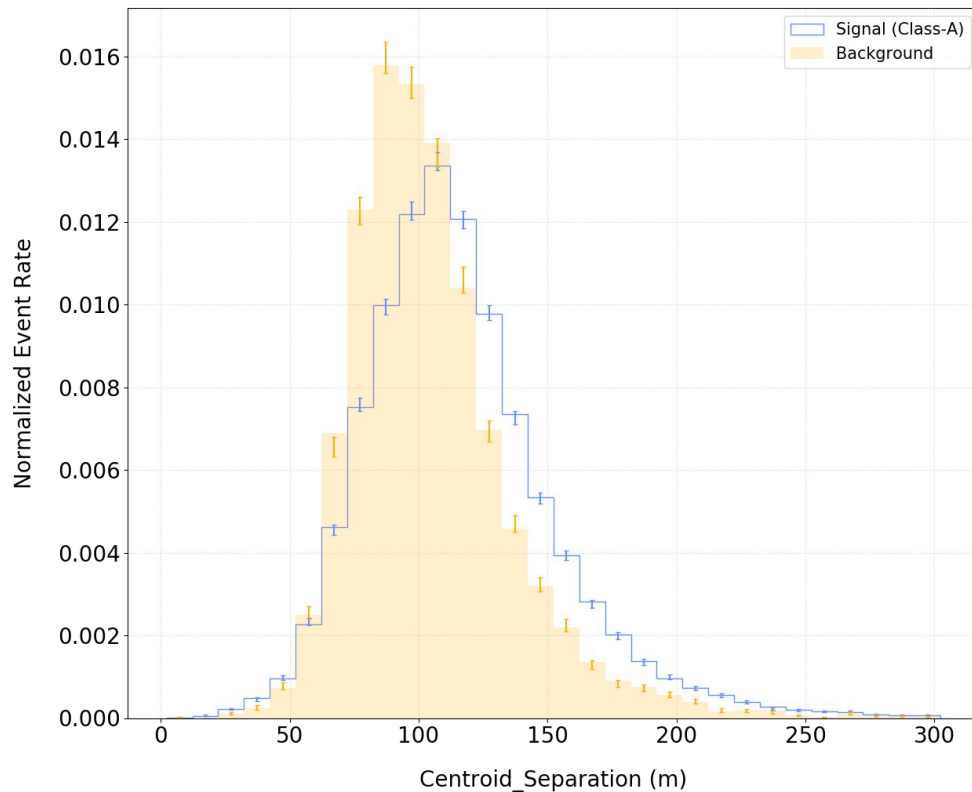


Fig: This figure depicts two coordinate systems. The unprimed coordinate system is the detector coordinate system. The primed coordinate system is the track's coordinate system. The primed x-y plane contains the track's starting point. The track's direction forms the primed z axis. All the hit DOMs are projected into the primed x-y plane.



▲ : COG of the cluster

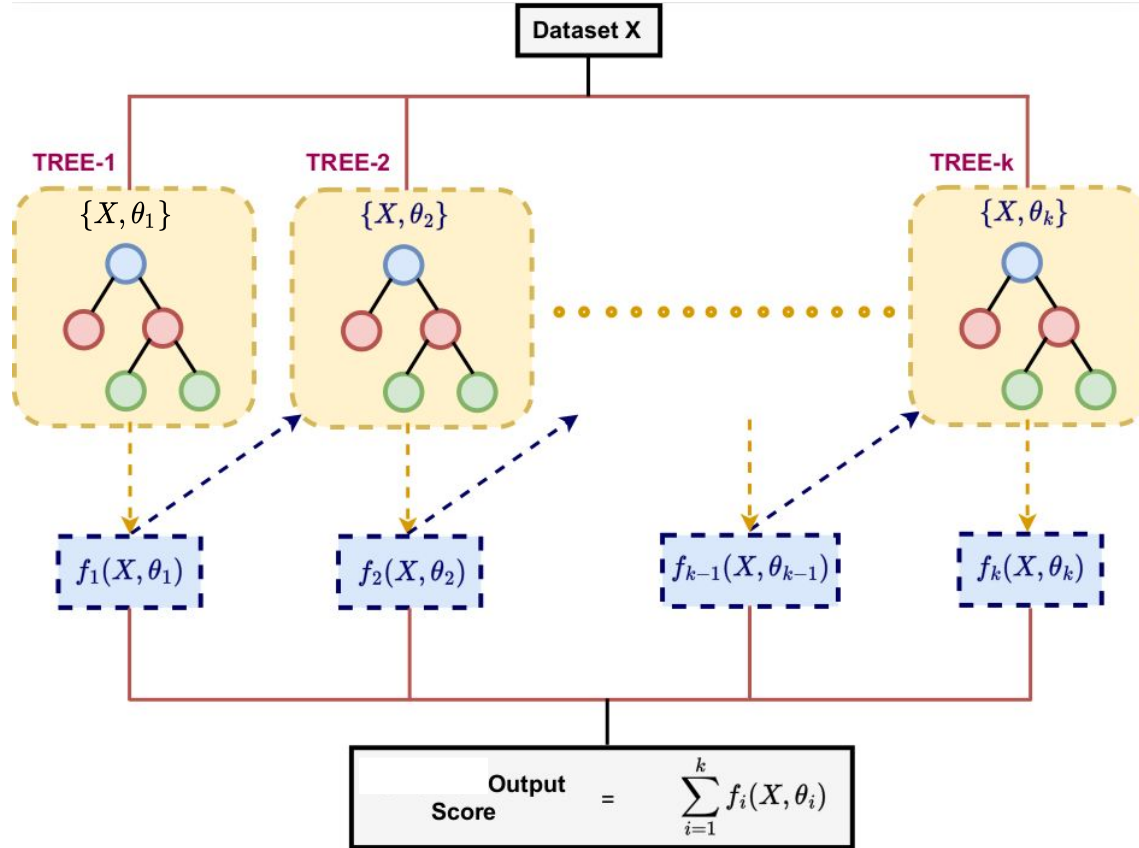
FEATURES: CLUSTERING [2/2]



CS : Centroid Separation

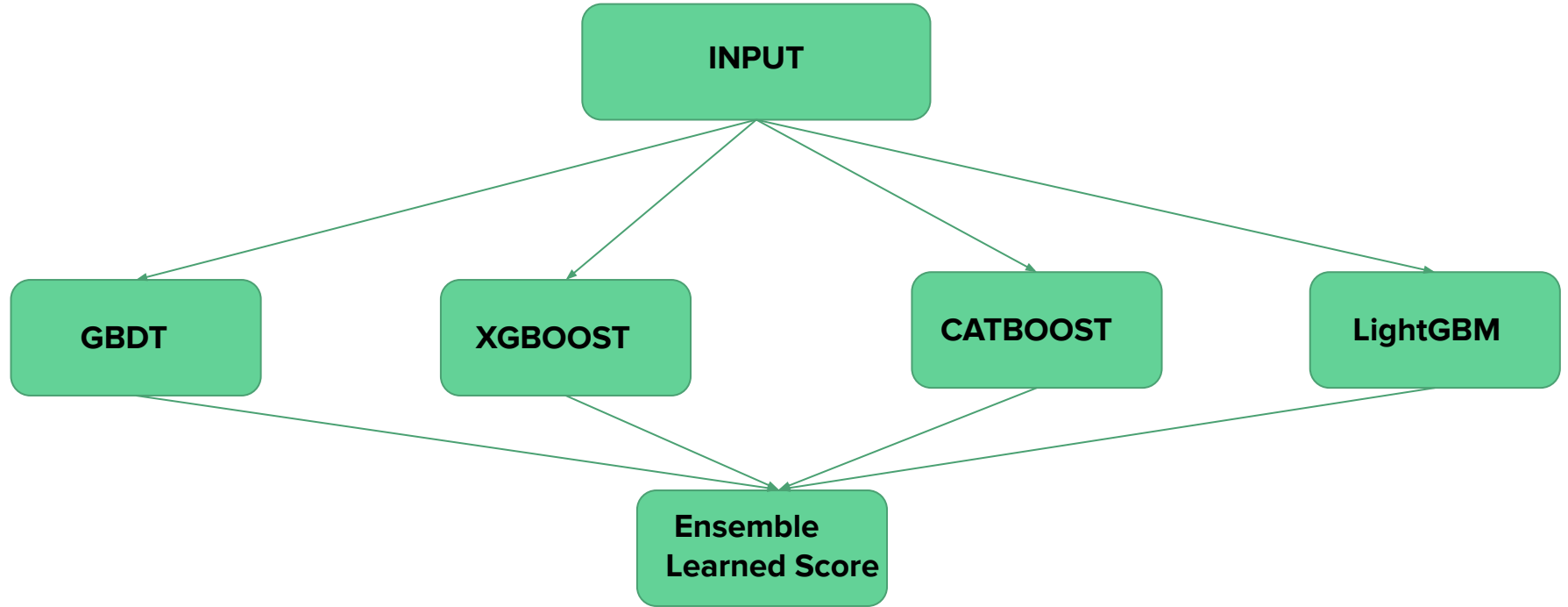
MACHINE-LEARNING ANALYSIS

BOOSTed decision tree



- ◆ Together we learn from the mistakes of our past.
- ◆ Start with a decision tree and get its output
- ◆ Compare this output with the actual output.
- ◆ If they are not the same, those events are assigned incorrectly.
- ◆ Correct for these mistakes in the next tree.
- ◆ Repeat until the stopping condition.

Ensemble Learning



RESULTS: TRAINING AND VALIDATION [1/3]

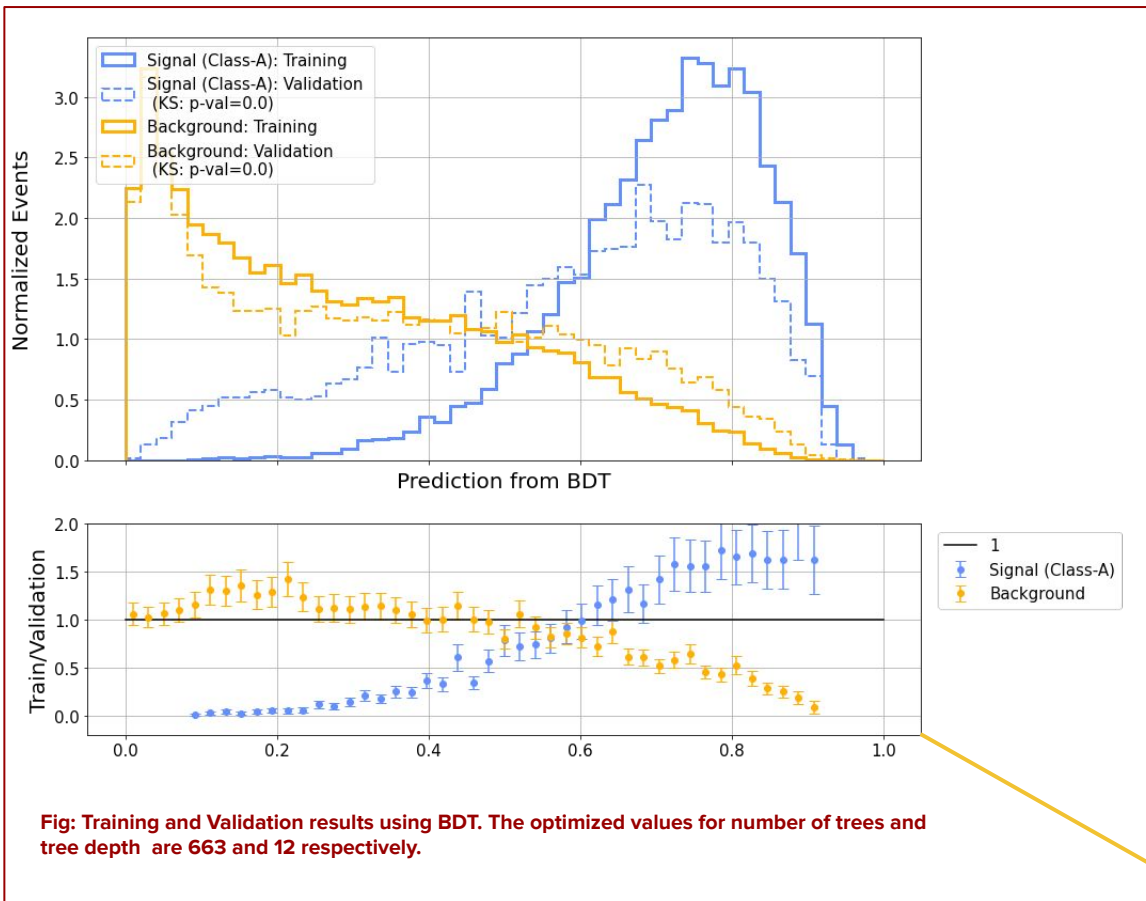


Fig: Training and Validation results using BDT. The optimized values for number of trees and tree depth are 663 and 12 respectively.

- ◆ **BDT Score: 1 means signal and 0 is background.**
- ◆ **Train on only Class-A events.**
- ◆ **Split the training sample into training and validation (80-20).**

68%

RESULTS: TRAINING AND VALIDATION [2/3]

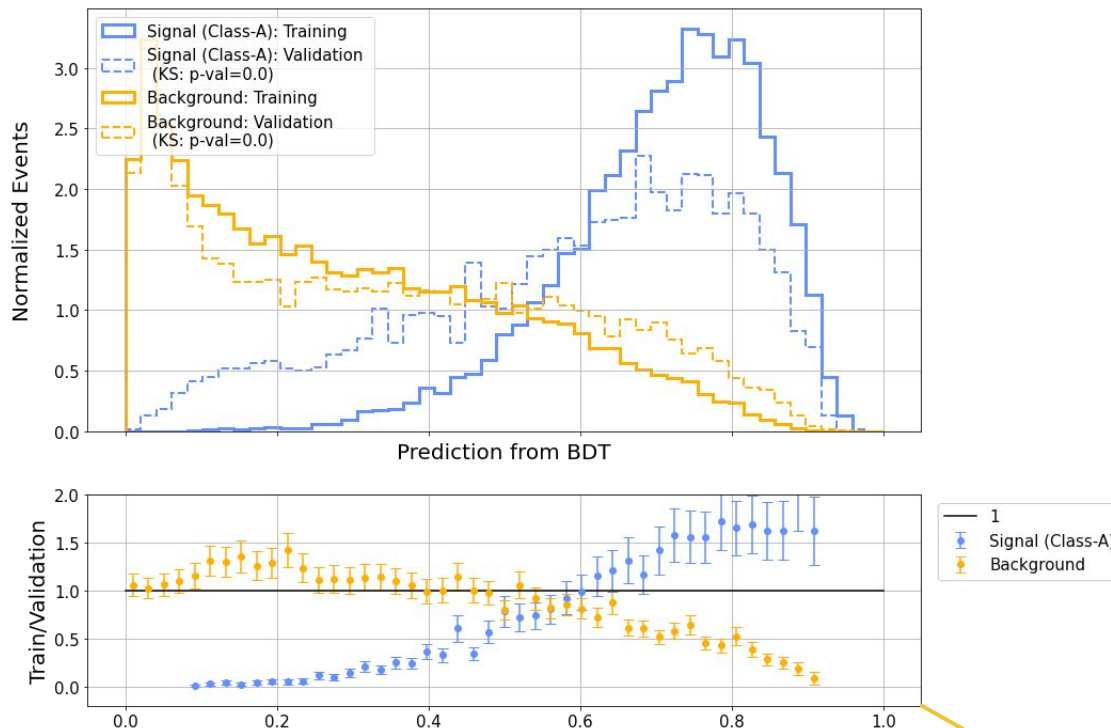


Fig: Training and Validation results using BDT. The optimized values for number of trees and tree depth are 663 and 12 respectively.

- ◆ Train on only Class-A events.
- ◆ Split the training sample into training and validation (80-20).
- ◆ Optimize the hyperparameter values like tree depth, number of trees etc.
- ◆ Test the validation.
- ◆ Use Kolmogorov-Smirnov Test (KS) to check if the two-distributions are identical.
- ◆ If not, there is overtraining.
- ◆ By decreasing the tree depth and the number of trees, reduce overtraining.

68%

RESULTS: TRAINING AND VALIDATION [3/3]

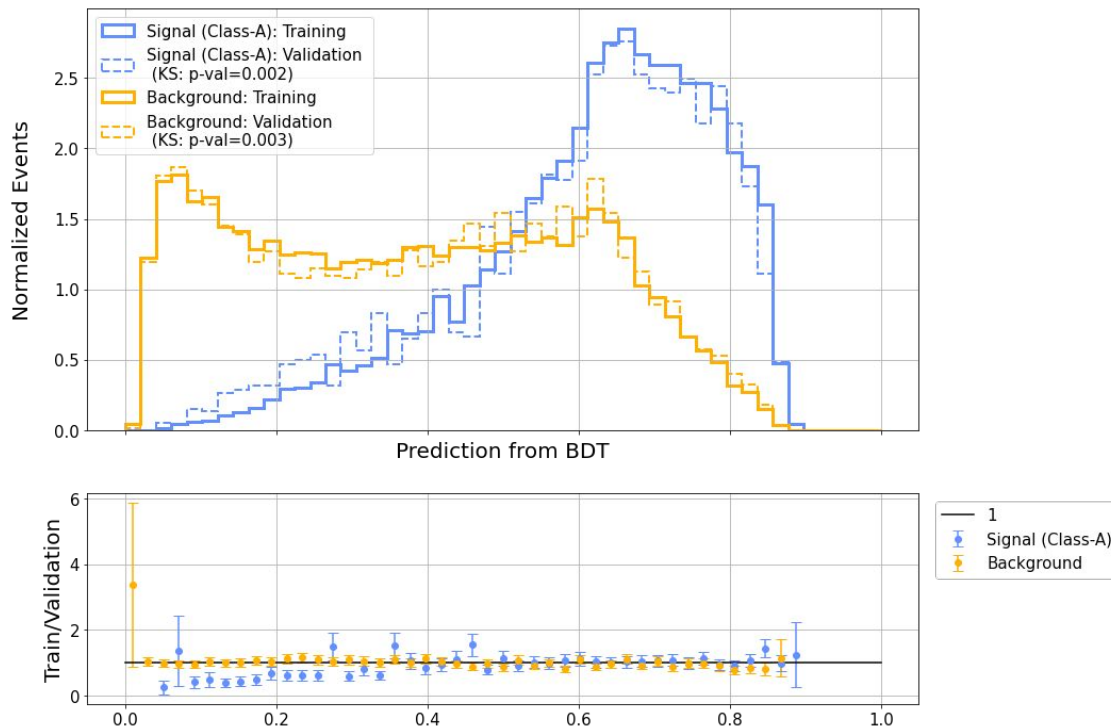


Fig: Training and Validation results using BDT. The optimized values for number of trees and tree depth are 200 and 5 respectively.

- ◆ This is the final selection. The KS-values for both signal background are more than 0.001 (decided cut).
- ◆ Cannot get rid of overtraining completely.
- ◆ Accept some.

RESULTS: TESTING

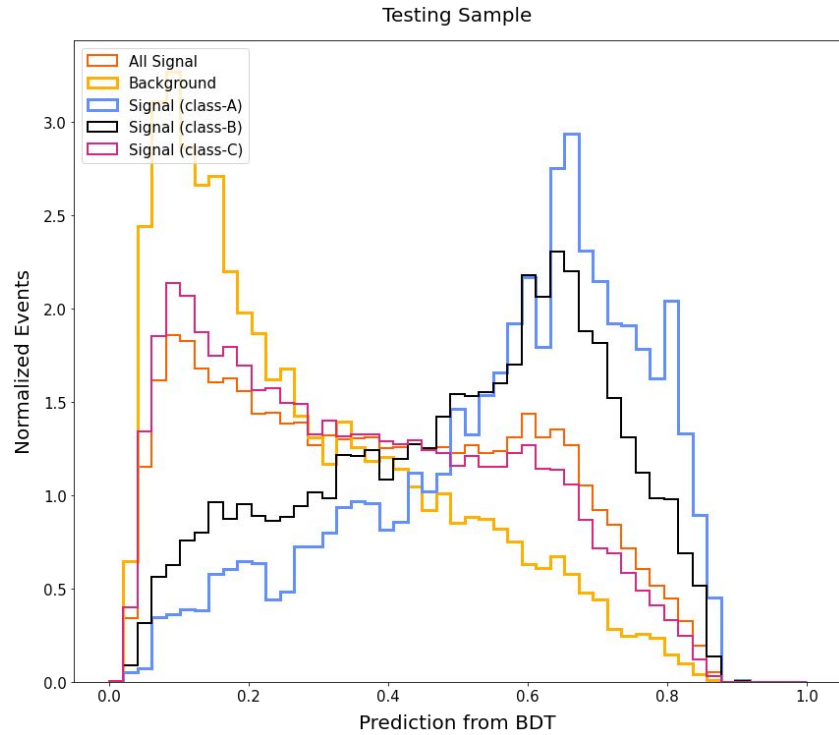


Fig: Testing Results. There is significant improvement over signal to background separation using XGBOOST.

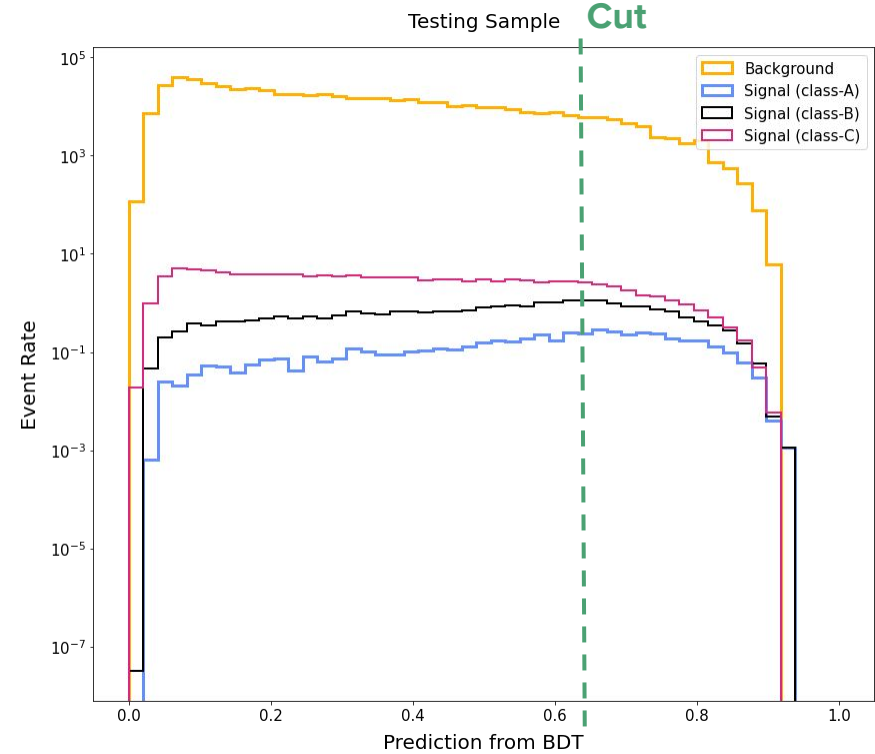


Fig: Testing Results. Non-normalized actual Event Rate in log scale.

RESULTS: ROC-AUC

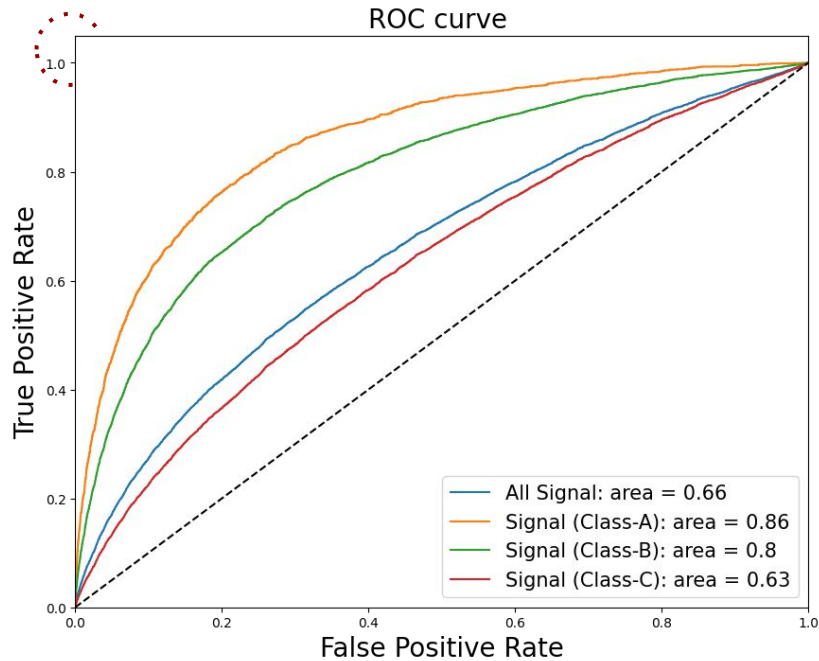


Fig: ROC-AUC Curve. Class-A with background has the maximum area in this curve (Around 0.86).

	Actual Positive	Actual Negative
Predicted Positive	True Positive (TP)	False Positive (FP)
Predicted Negative	False Negative (FN)	True Negative (TN)

$$\text{True Positive Rate} = \frac{TP}{TP+FN}$$

$$\text{False Positive Rate} = \frac{FP}{FP+TN}$$

RESULTS: Approximate Median Significance (AMS)

Approximate Median Significance Plot

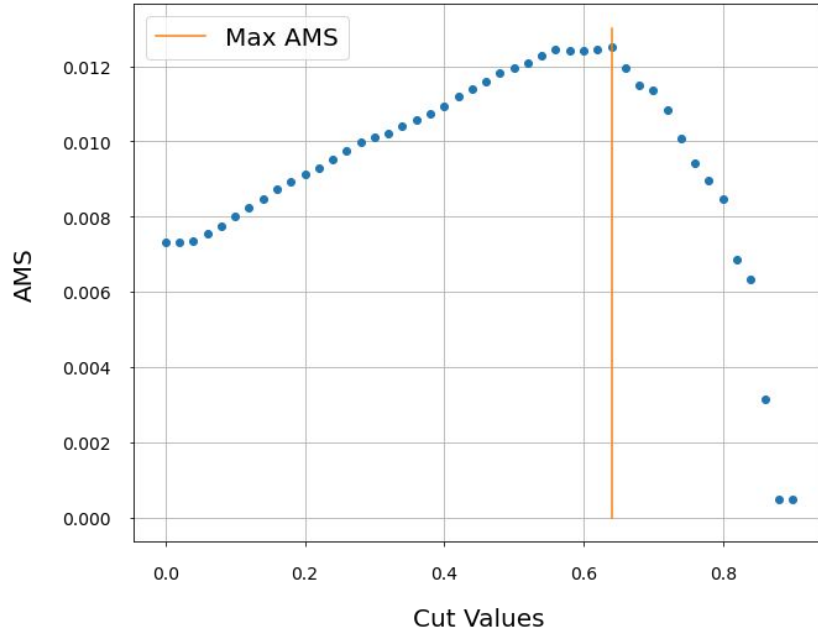


Fig: AMS Plot. The max value of AMS happens at the cut threshold of 0.64.

$$AMS = \sqrt{2(N_s + N_b) \log\left(1 + \frac{N_s}{N_b}\right) - N_s}$$

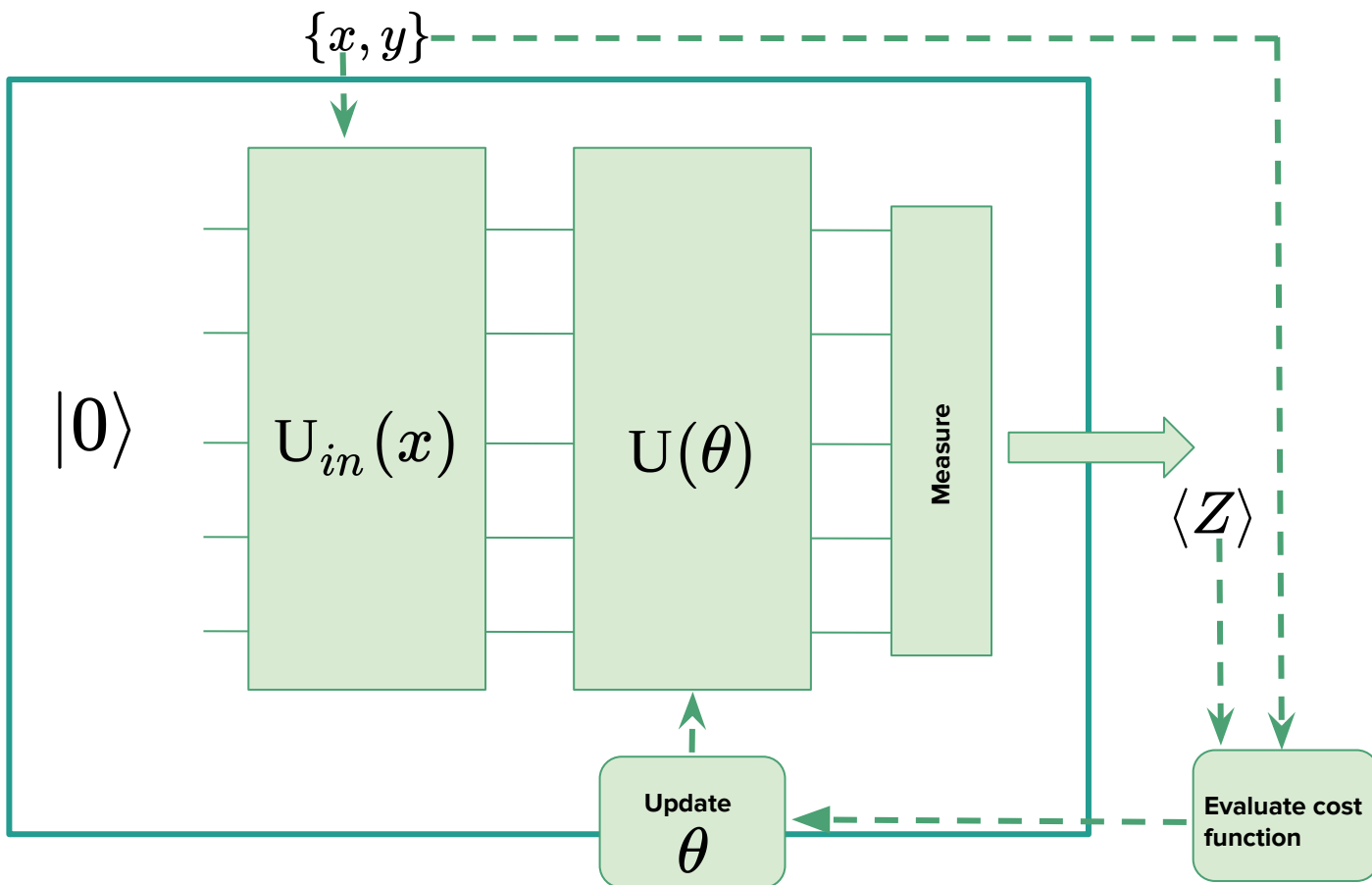
N_s : Number of signal events

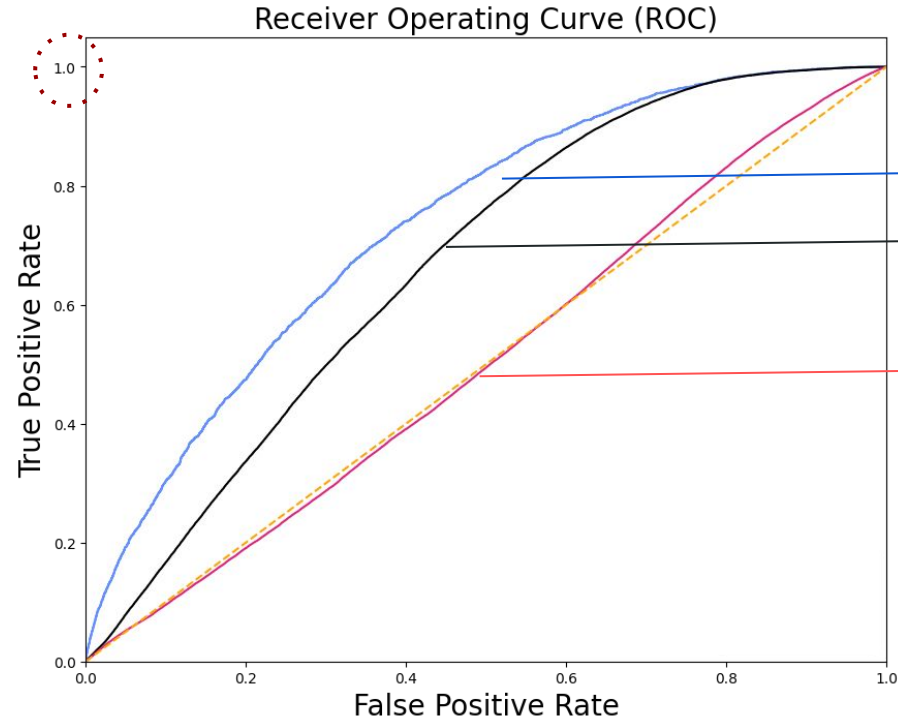
N_b : Number of background events

◆ In case of high background, AMS is asymptotically equal to

$$\frac{N_s}{\sqrt{N_b}}$$

QUANTUM MACHINE LEARNING ARCHITECTURES





Classical Ensemble-Decision Trees (Class-A)
(0.75)

Quantum Variational Algorithm (Class-A)
(0.7)

Classical Ensemble-Decision Trees (Class-C)
(0.51)

Fig: The blue curve represents the ensemble learning and the black curve represents the roc-auc for the quantum algorithm using IBMQ

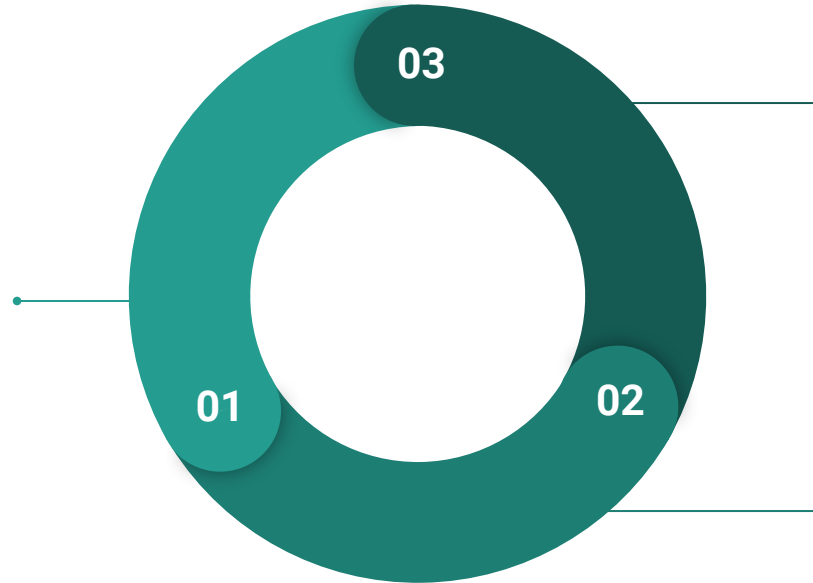
CONCLUSIONS

CONCLUSIONS

NEUTRINO TRIDENT EVENTS

Production of three outgoing leptons

Powerful probe into search for BSM bosons.



ML-Decision Trees

They amplified the difference between signal and background by looking into the higher-dimensional sub-spaces of the features.

IceCube detector

Features based on detector resolution and geometry properties, Cherenkov light distribution: Used for signal/background separation.

NEXT STEPS

GET PLOTS FOR CHARM DIMUONS

See how the BDT distribution looks like for charm dimuons



Decide Cuts

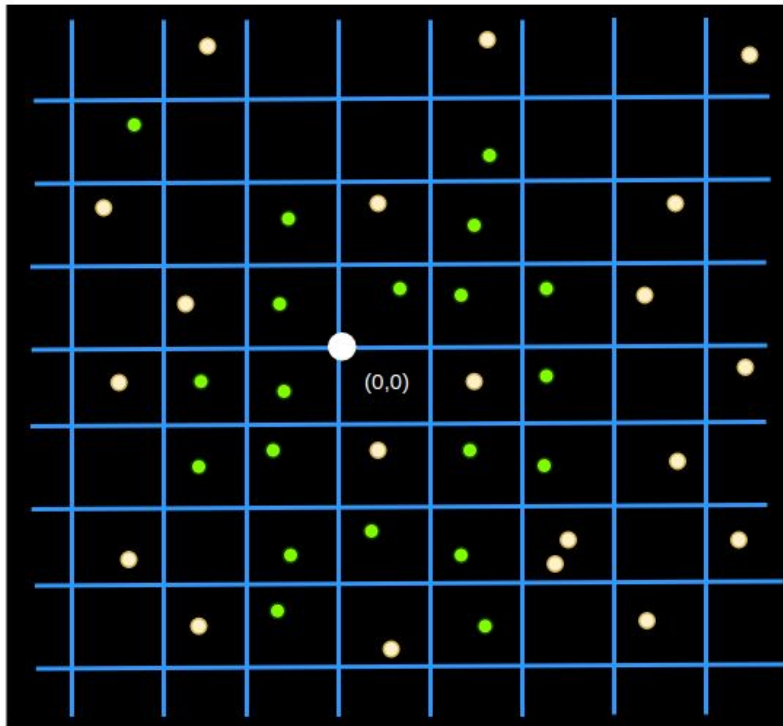
What cut can be used beyond which one can say that there is signal?

IceCube Data

Check how is the real data performing on XGBOOST.

THANK-YOU

BACKUP-SLIDES

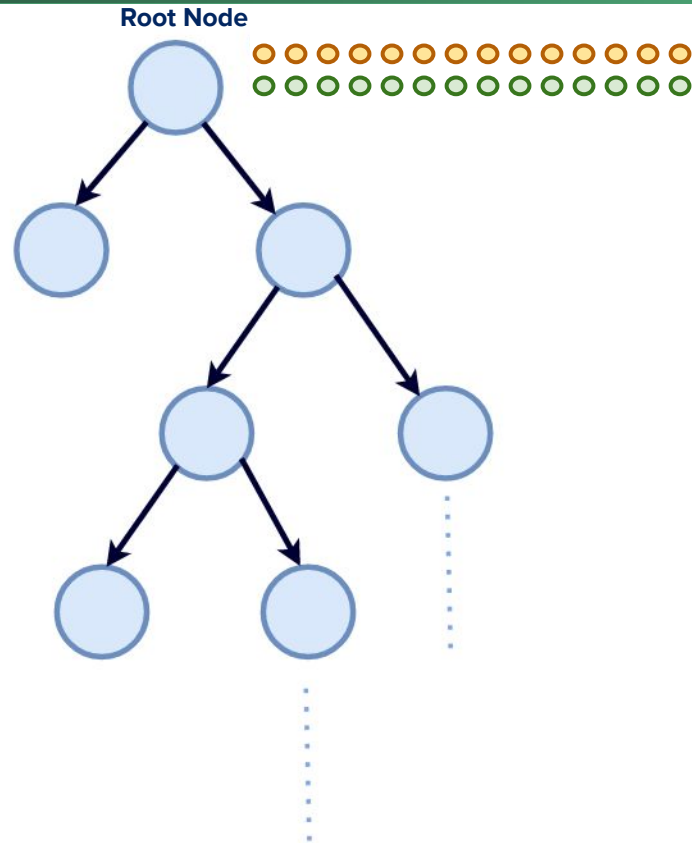
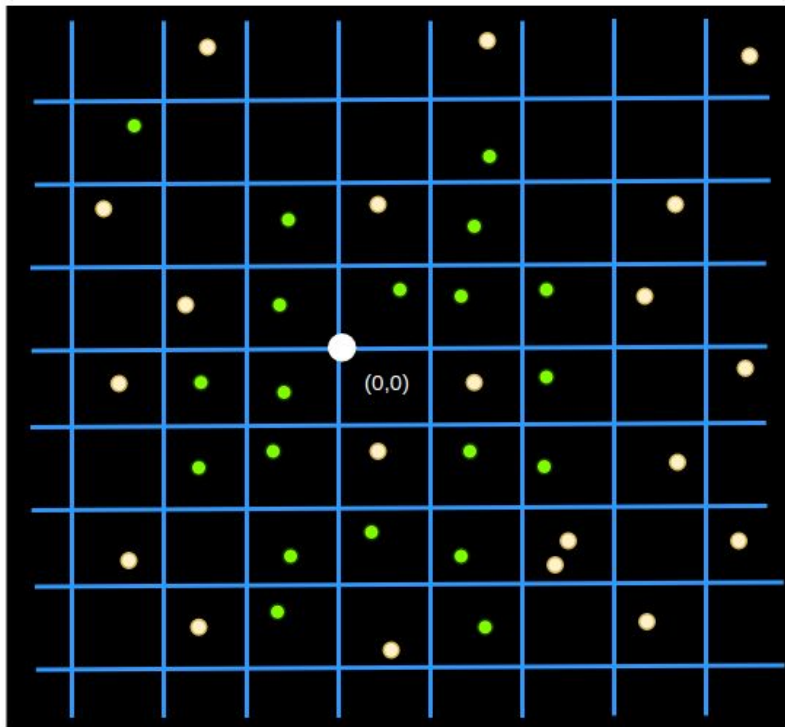


Feature_1

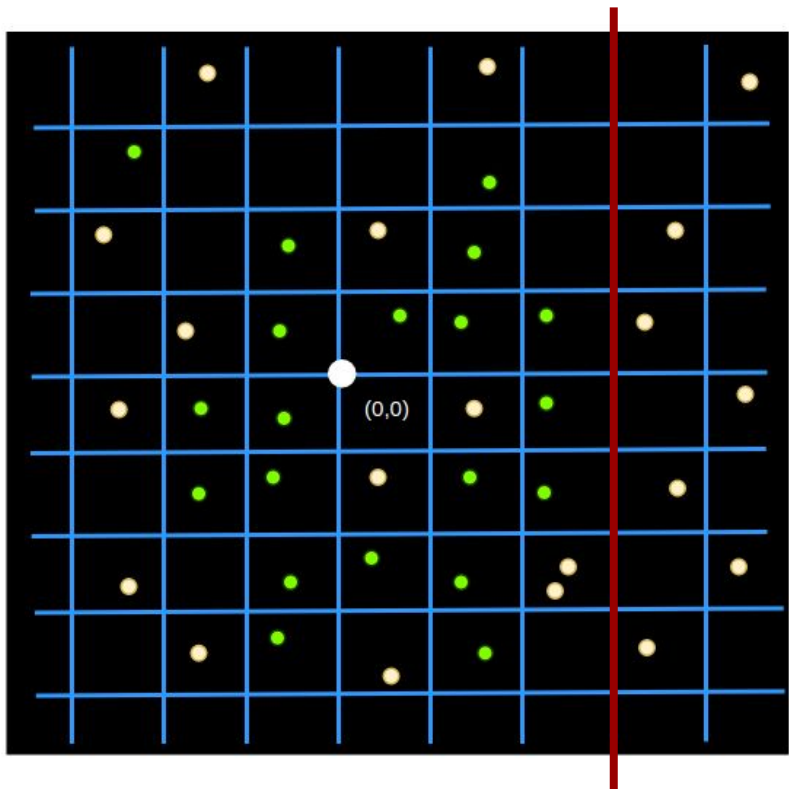
Feature_2

Can you use a line to separate one class events from the other?

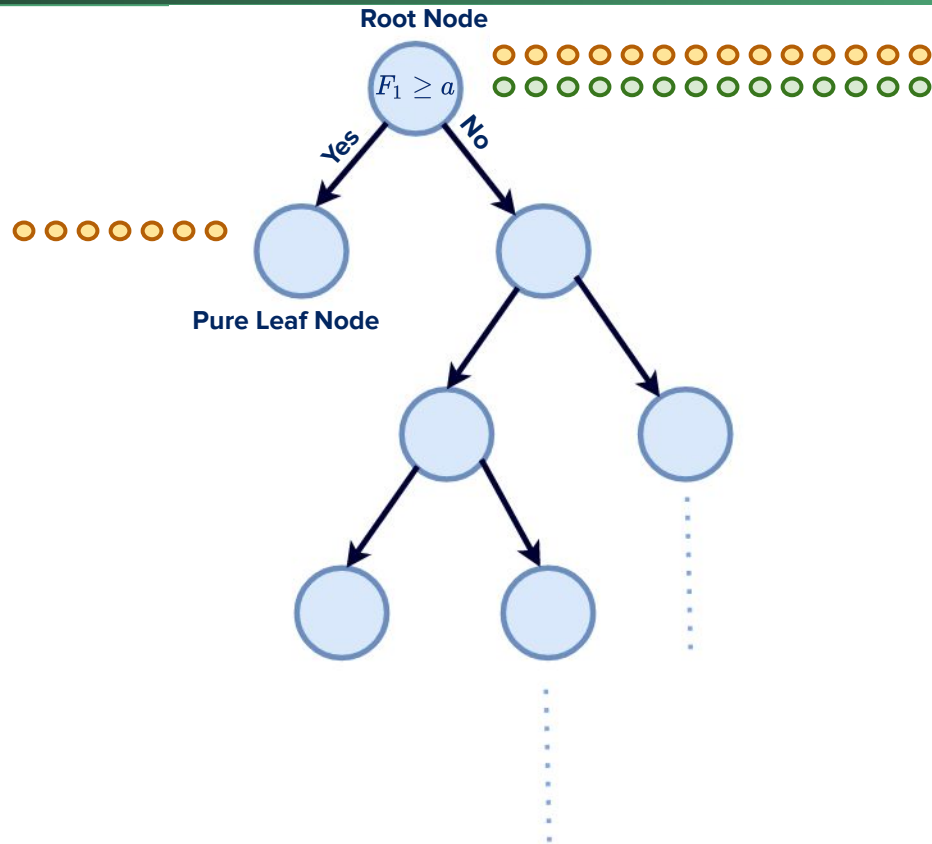
DECISION TREES: CLASSIFY FOR US [2/9]



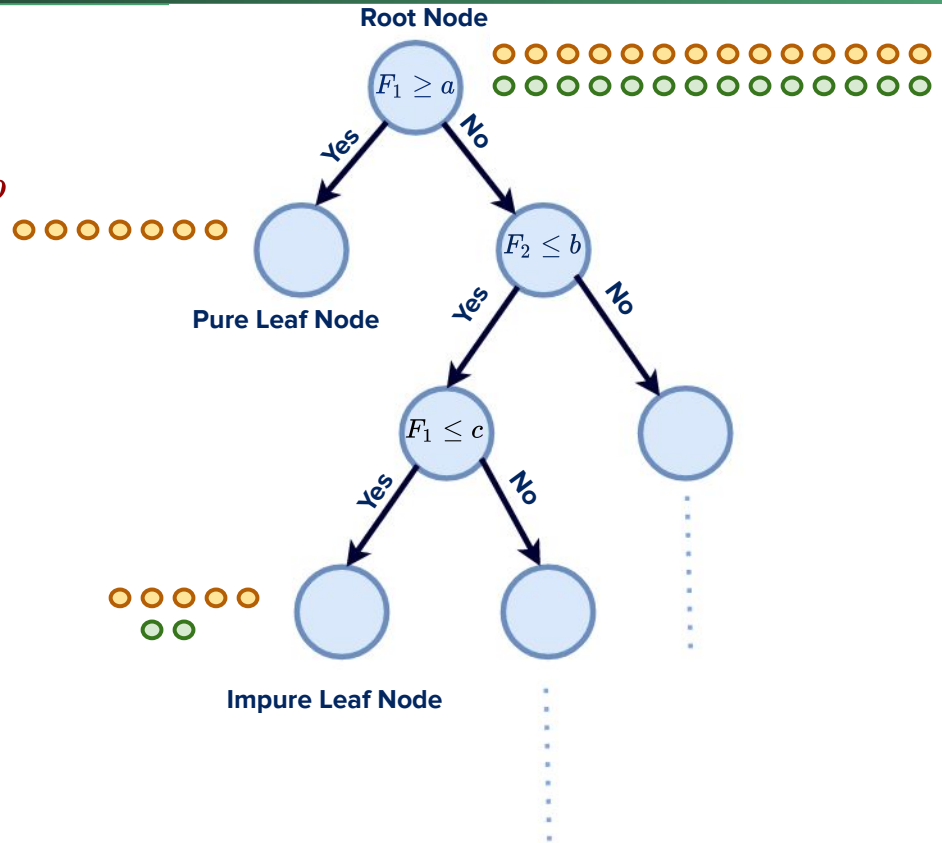
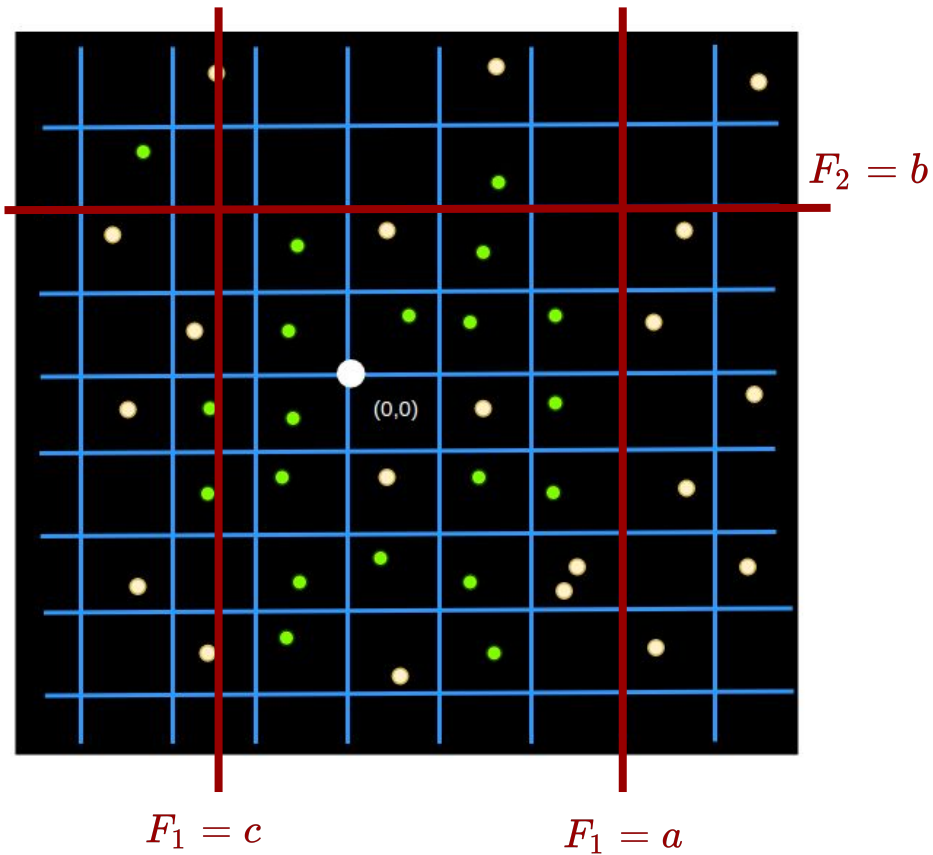
DECISION TREES: CLASSIFY FOR US [3/9]



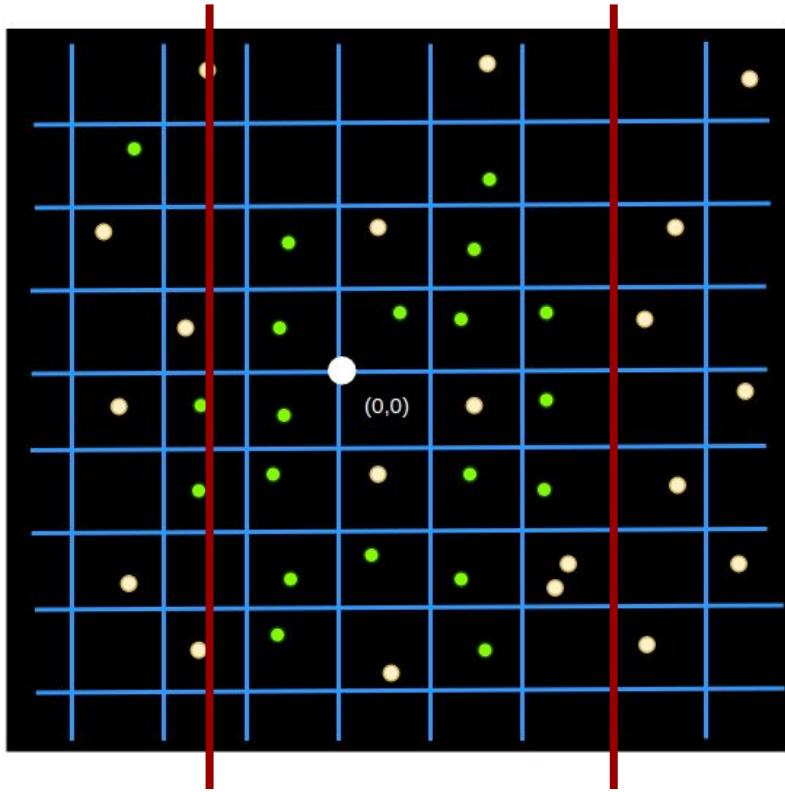
$$F_1 = a$$



DECISION TREES: CLASSIFY FOR US [4/9]



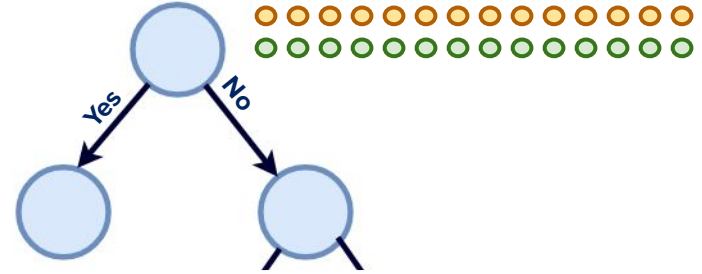
DECISION TREES: CLASSIFY FOR US [5/9]



$F_1 = c$

$F_1 = a$

Root Node

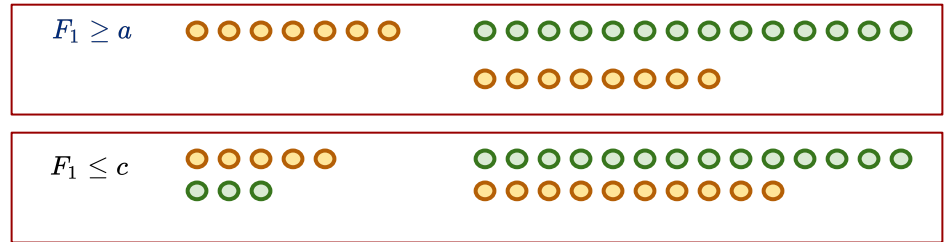
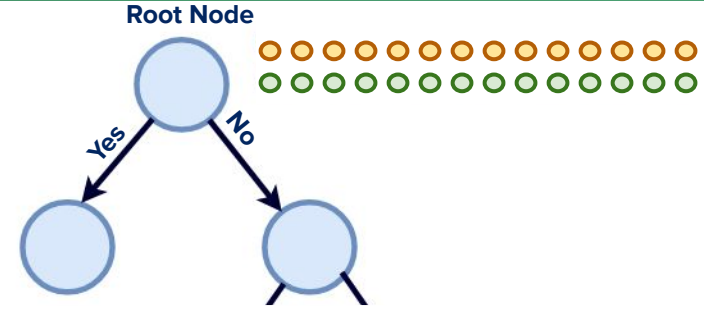
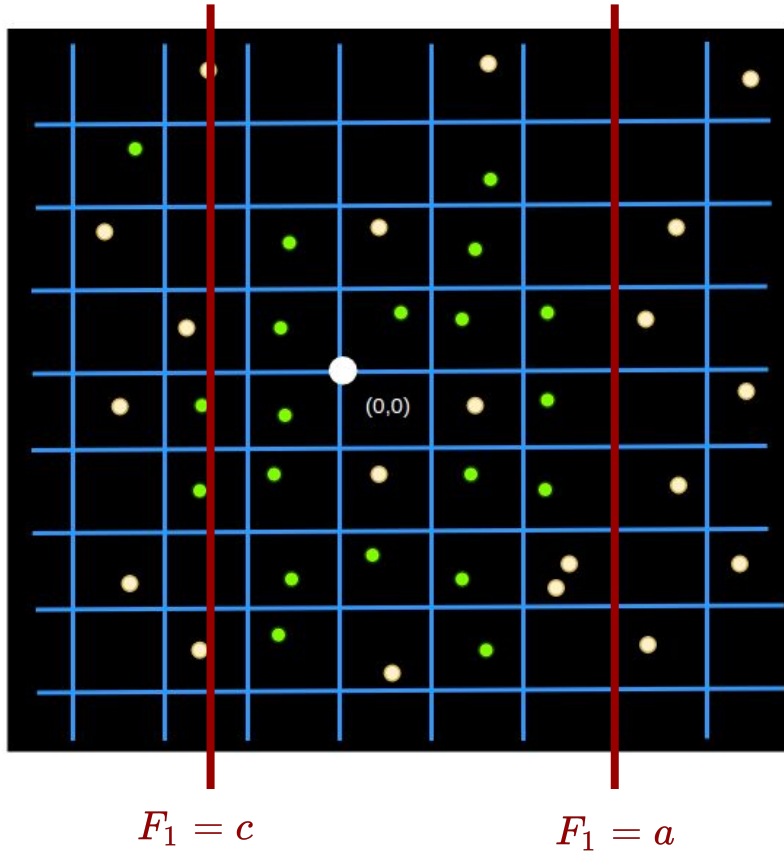


$F_1 \geq a$



$F_1 \leq c$

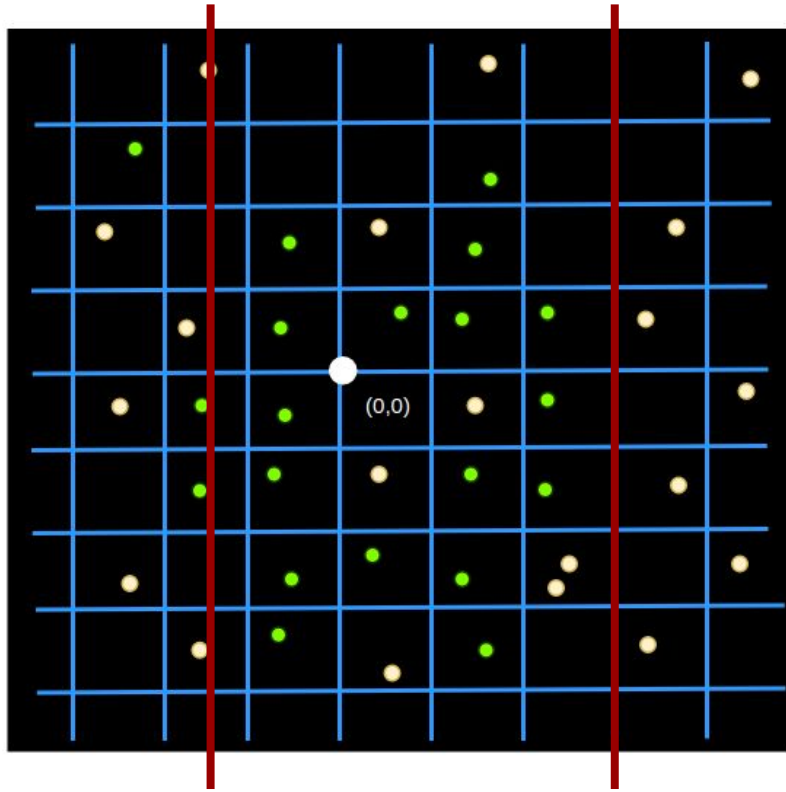
DECISION TREES: CLASSIFY FOR US [6/9]



$$\text{Entropy}_{\text{node}} = - \sum_{i=1}^2 p_i \log_2 p_i$$

p_i : probability of each class (signal and bkg.)

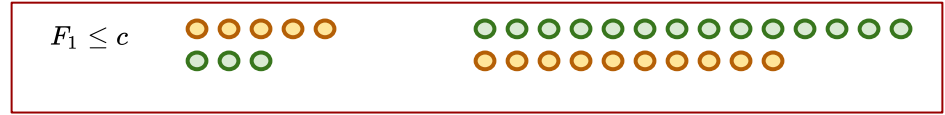
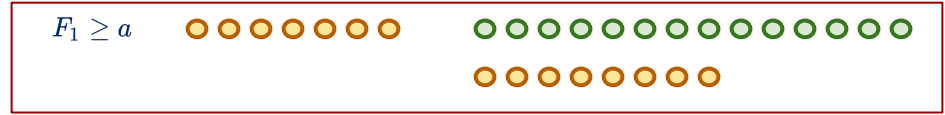
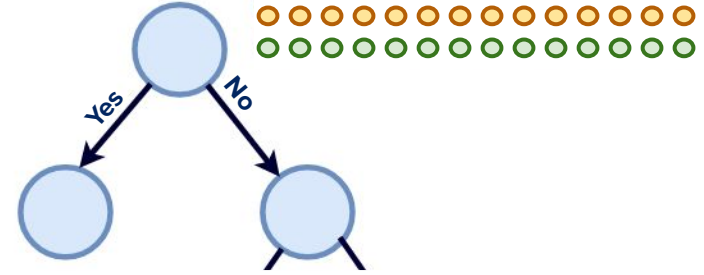
DECISION TREES: CLASSIFY FOR US [7/9]



$$F_1 = c$$

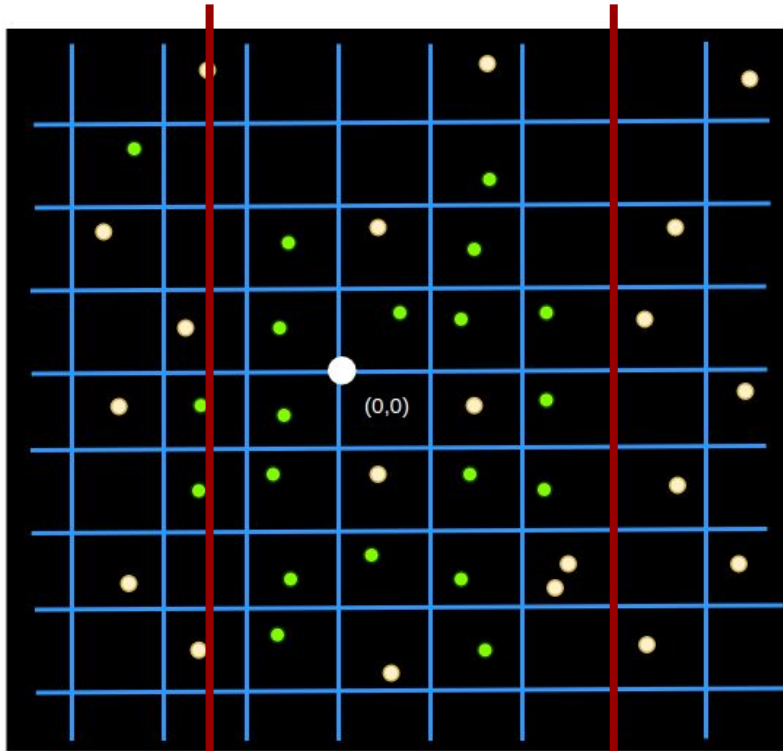
$$F_1 = a$$

Root Node



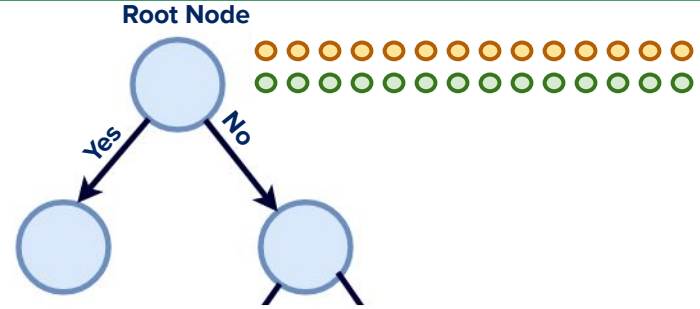
◆ Clearly entropy of root node is 1 (max. value).

DECISION TREES: CLASSIFY FOR US [8/9]



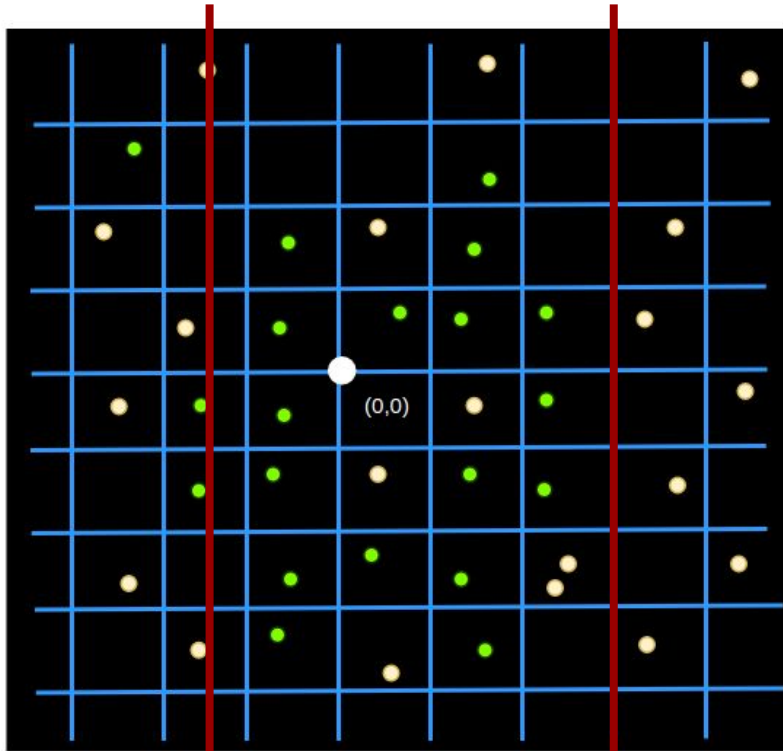
$F_1 = c$

$F_1 = a$



- ❖ Clearly entropy of root node is 1 (max. value).
- ❖ Entropy for is 0 (Pure leaf node).

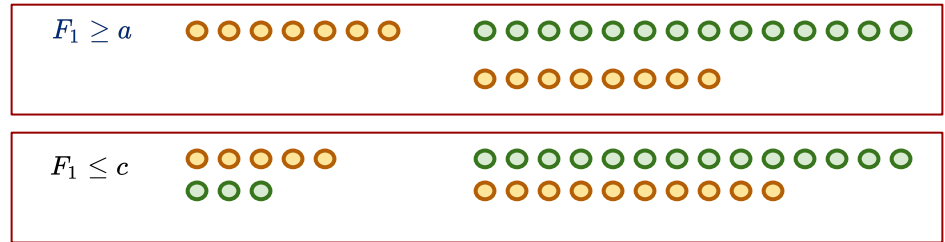
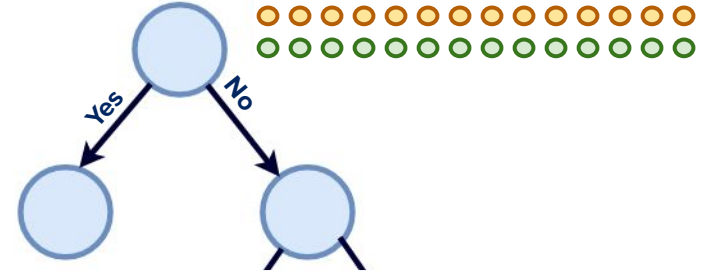
DECISION TREES: CLASSIFY FOR US [9/9]



$F_1 = c$

$F_1 = a$

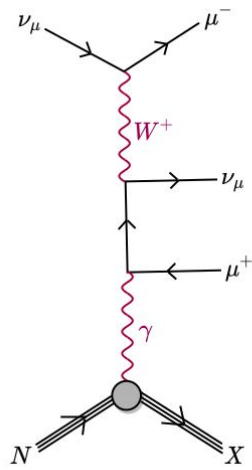
Root Node



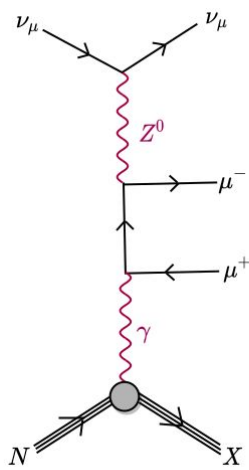
$$\text{Information Gain} = \text{Entropy}_{\text{parent}} - \sum_j \alpha_j \text{Entropy}_{\text{daughter}_j}$$

$$\alpha_j : \frac{\text{Total points in } j^{\text{th}} \text{ daughter node}}{\text{Total points in parent node}}$$

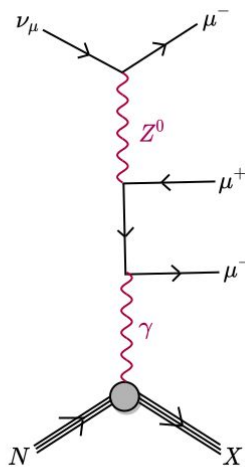
NEUTRINO TRIDENT EVENTS: MUONIC CHANNEL



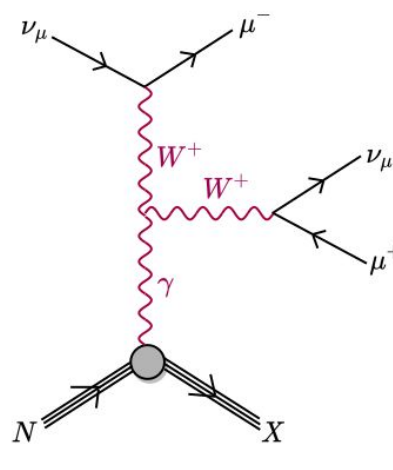
(a)



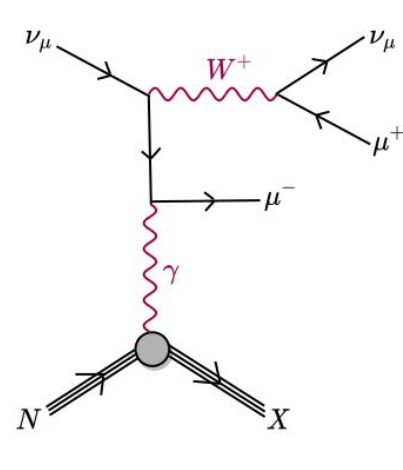
(b)



(c)



(d)



(e)

❖ **Diagrams d and e: W-Bosons are ON-SHELL. High energy neutrinos (above $\sim 3\text{TeV}$) [1] can produce on-shell W boson via these diagrams and enhance the eventrate at the detectors.**

CROSS-SECTION

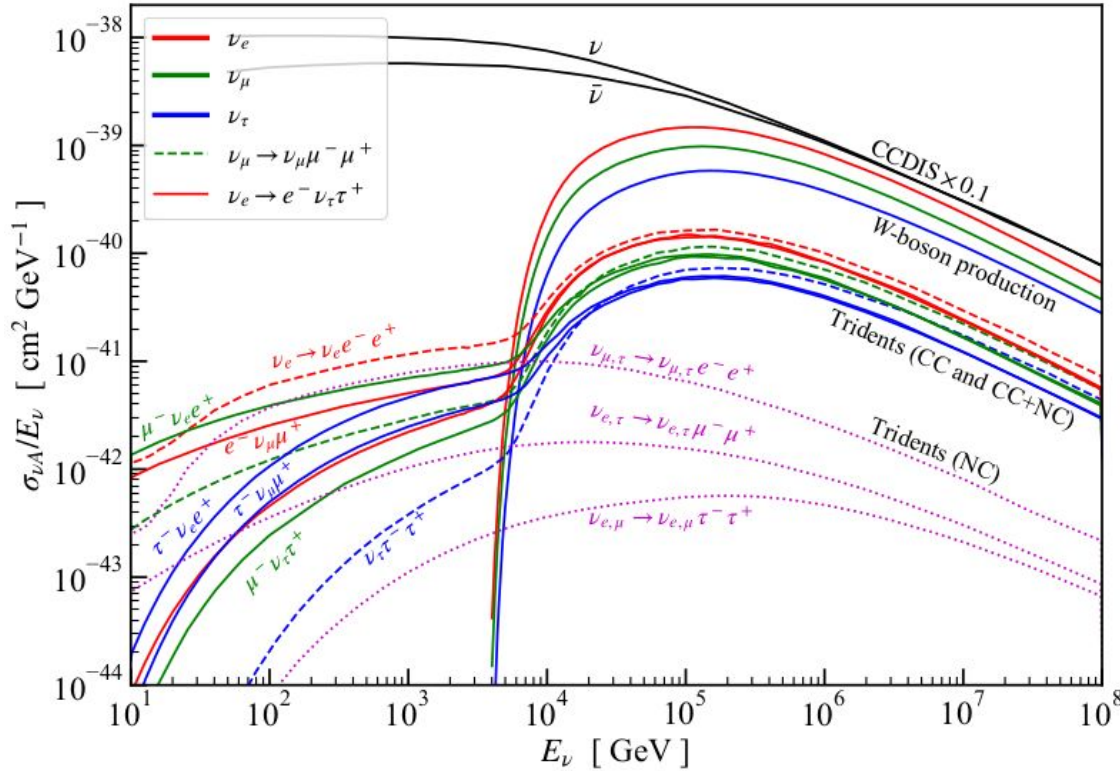
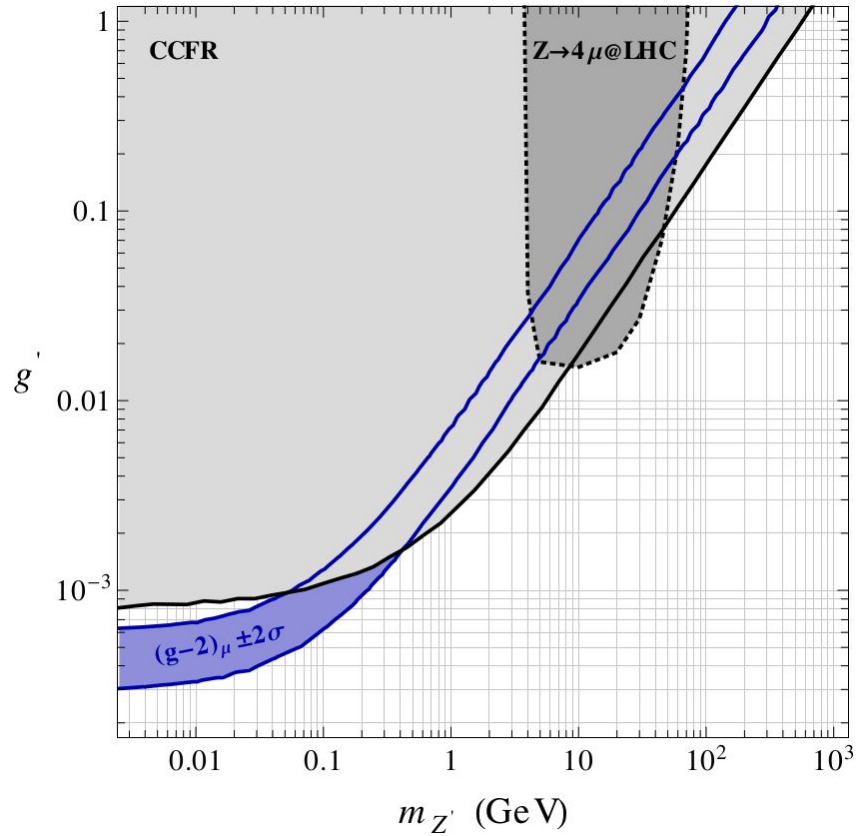
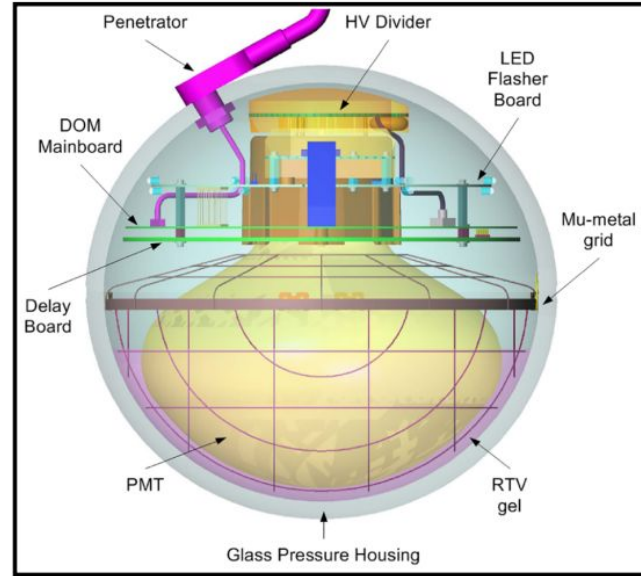
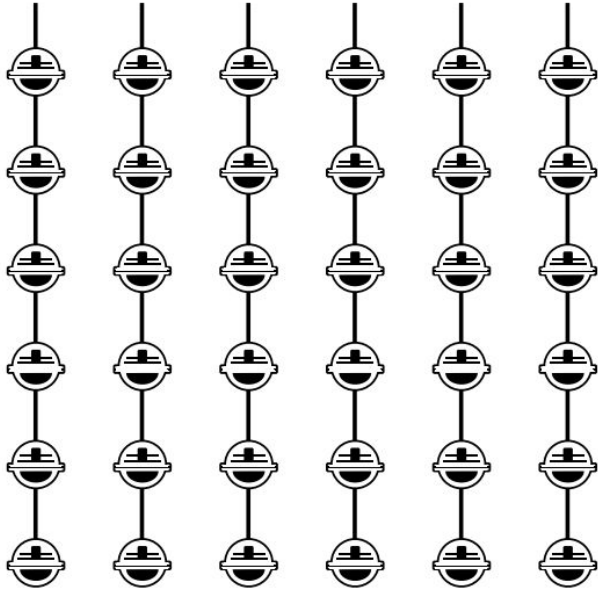


Fig: Total cross-section for simuons and dimuons against incoming neutrino energy. Figure from [1]

- ◆ In the energy range [10 GeV - 3 TeV], the ordinary CC-DIS cross-section is roughly 10000 orders of magnitude higher than the trident cross section.
- ◆ At roughly 3 TeV range, trident cross-section jumps due to the resonance effect from the on-shell W-boson channels.
- ◆ Beyond 100 TeV, the trident cross-section starts to decrease.

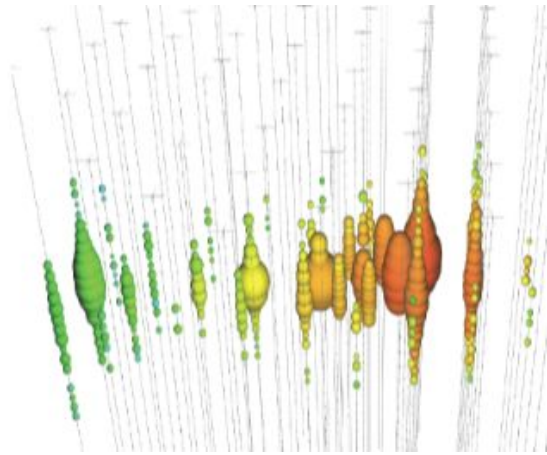


DIGITAL OPTICAL MODULE (DOM): DATA ACQUISITION MODULES

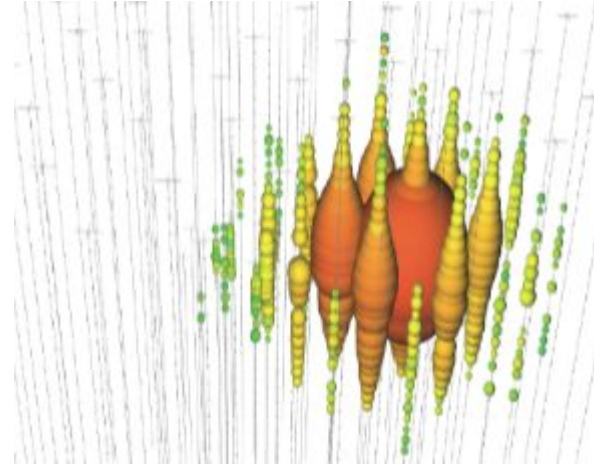


- ❖ **13 mm thick glass sphere containing a Photo-Multiplier Tube (PMT) to measure light.**

PARTICLE SIGNATURES IN ICECUBE



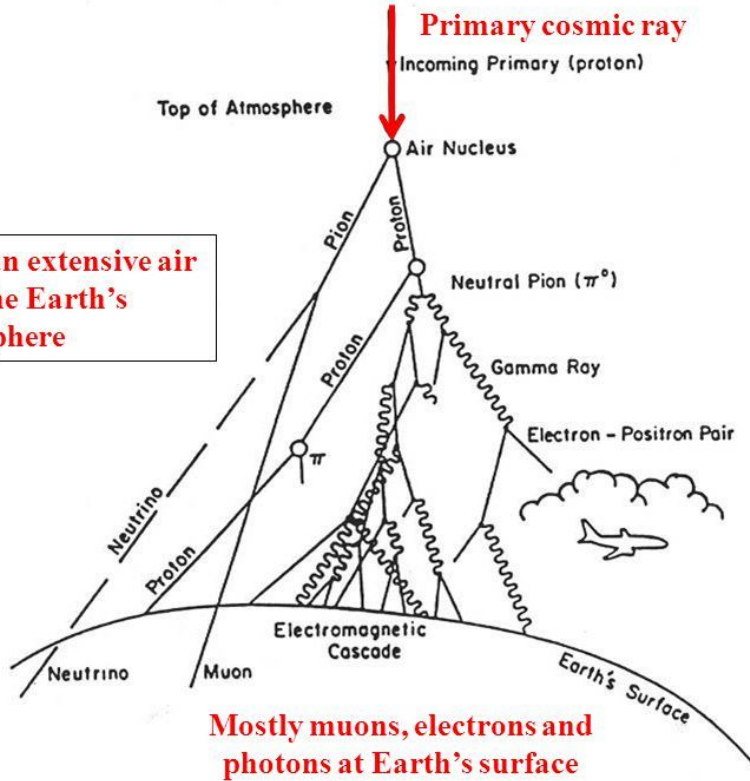
**MUON
(TRACK)**



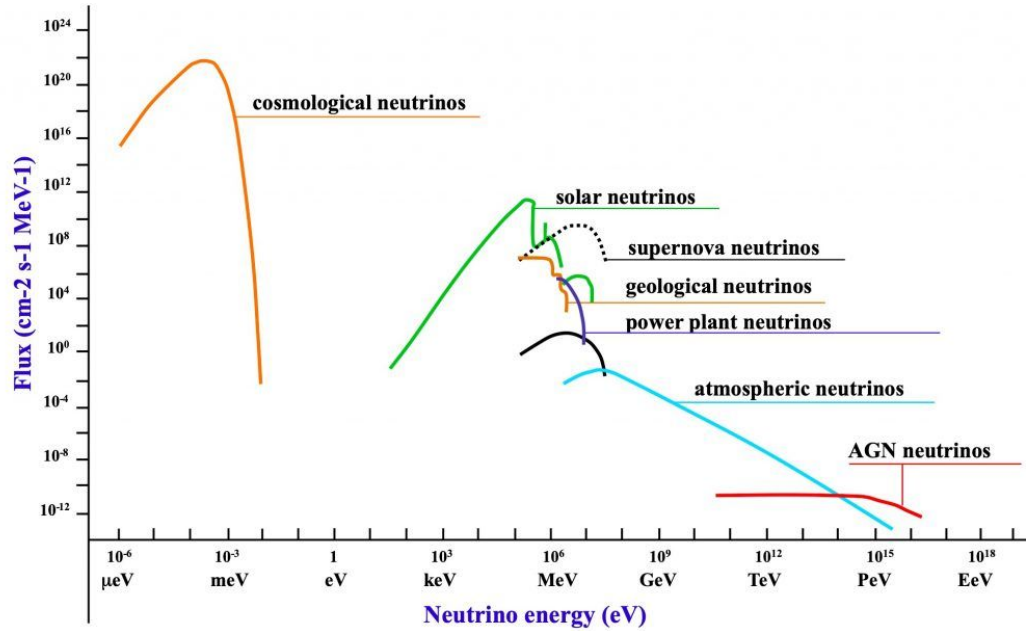
**ELECTRON
(CASCADE)**

EXTENSIVE AIR SHOWERS

Development of an extensive air shower in the Earth's atmosphere

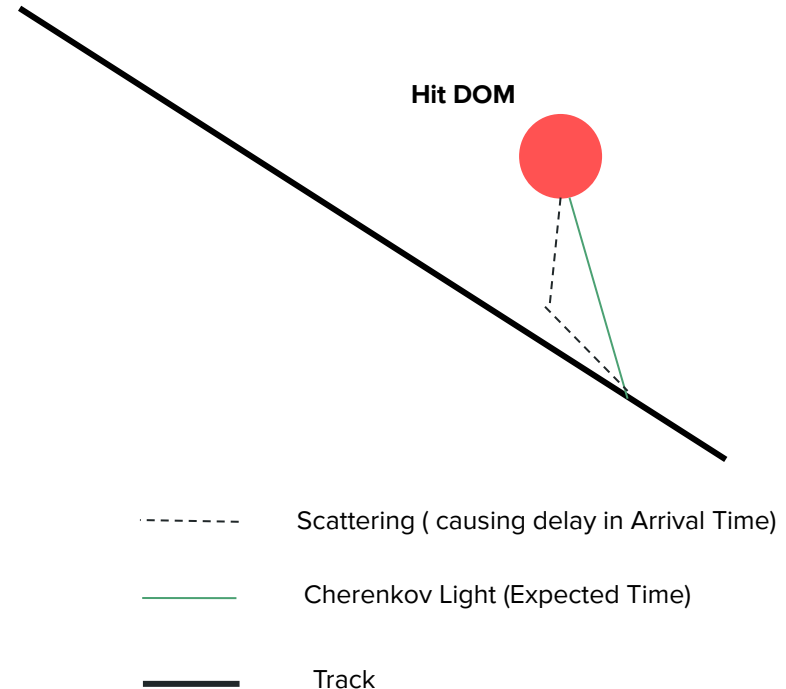


FLUX SOURCES

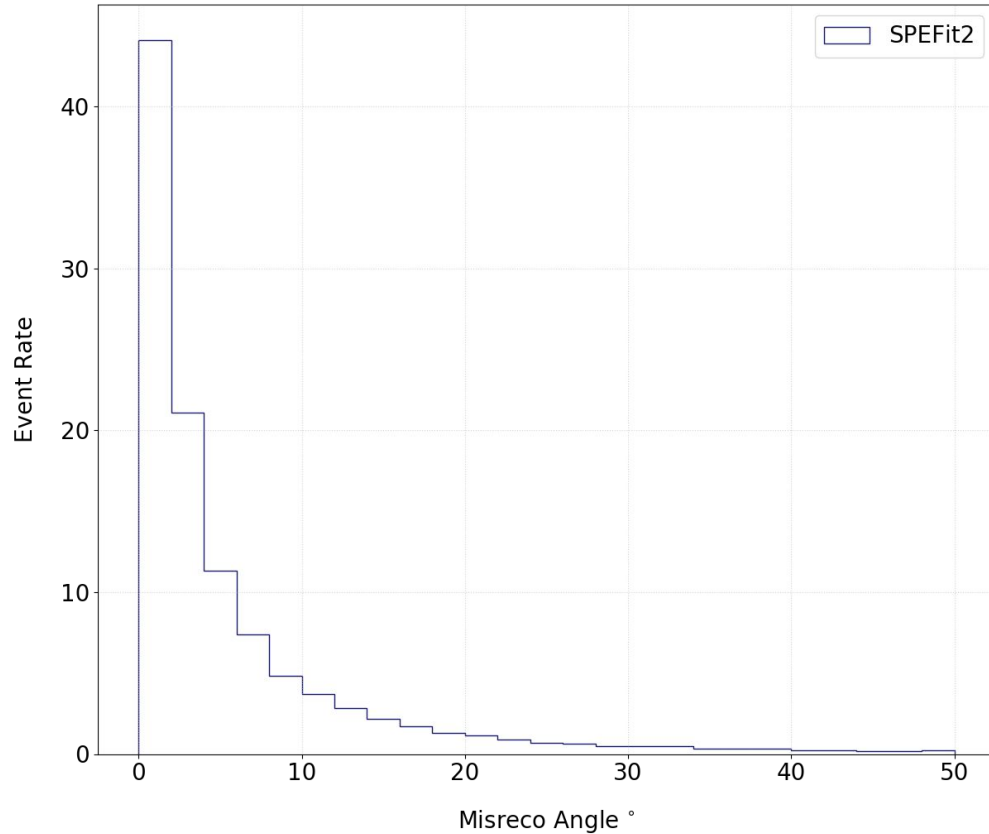


TRACK RECONSTRUCTION

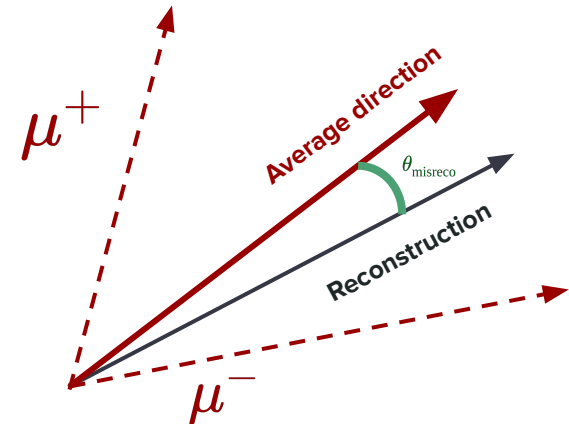
- Track reconstruction problem: Given a set of observations, the goal is to recover the track of a muon
- Challenges: Light propagating through the ice is affected by scattering and absorption. As a result, the Cherenkov light radiated by a muon can arrive early or late than the expected time on a DOM due to ice scattering. Therefore, we measure the quantity called time residual= geometric time-arrival time.
- Hypothesis: Single Muon



TRACK RECONSTRUCTION



- ◆ **SPEFIT2: minimization of time residuals gives a reconstructed track almost in the middle of the double muon tracks.**



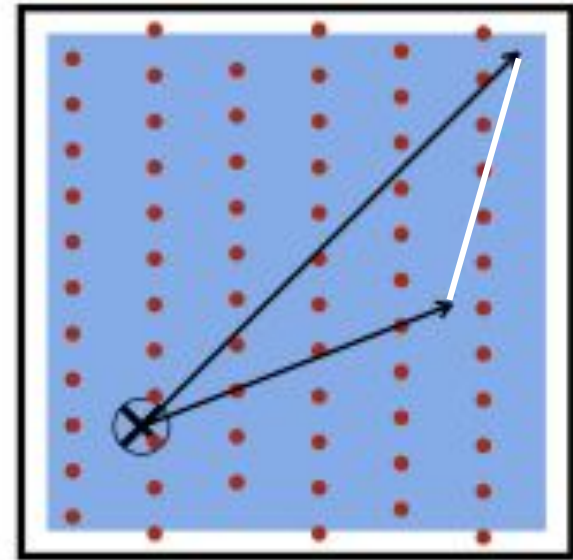
EVENT-RATE ESTIMATION FOR TRIDENT EVENTS AT ICECUBE

Selection

Criteria:

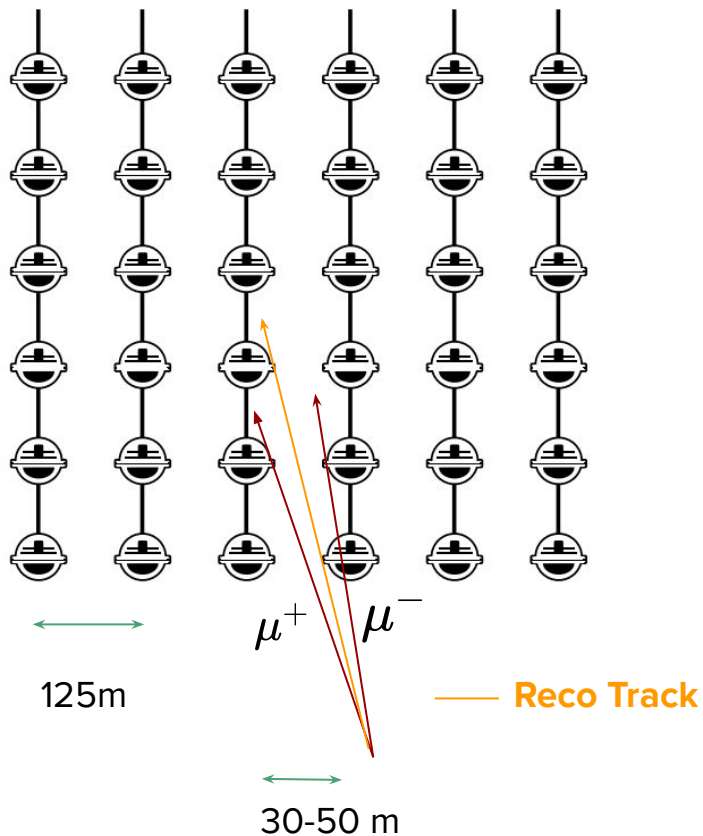
1. Neutrino sources: Atmospheric showers and astrophysical neutrino flux.
2. Highest track separation (white line) of the dimuons inside the IceCube detector is greater than 20m.

Event Rate Prediction: A total of 41 events is predicted to satisfy the selection criterion as double-track trident events in 10 years of IceCube data.



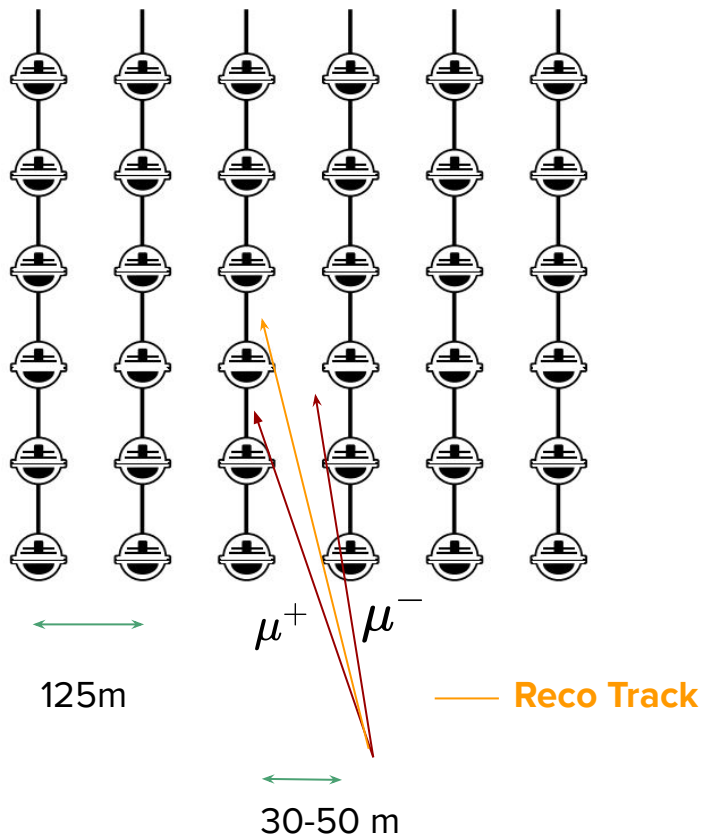
[3] D. E. Groom, N. V. Mokhov and S. I. Striganov, *Atom. Data Nucl. Data Tabl.* 78, 183-356 (2001) doi:10.1006/adnd.2001.0861

SEARCH CHALLENGES WITH ICECUBE [1/2]



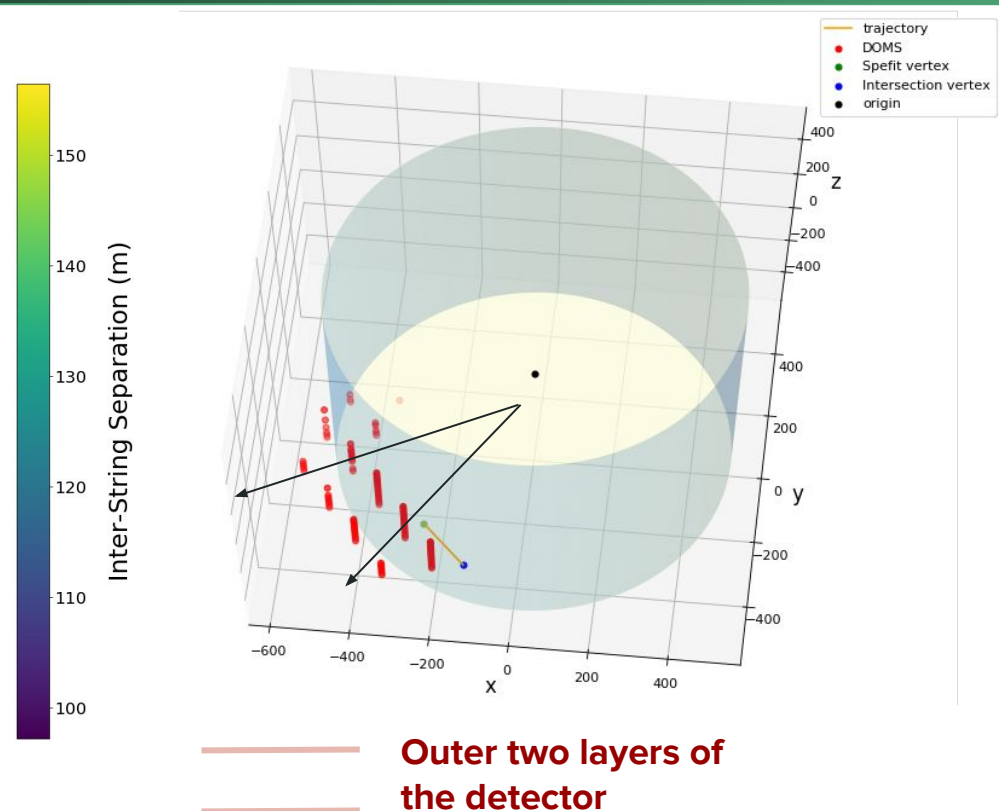
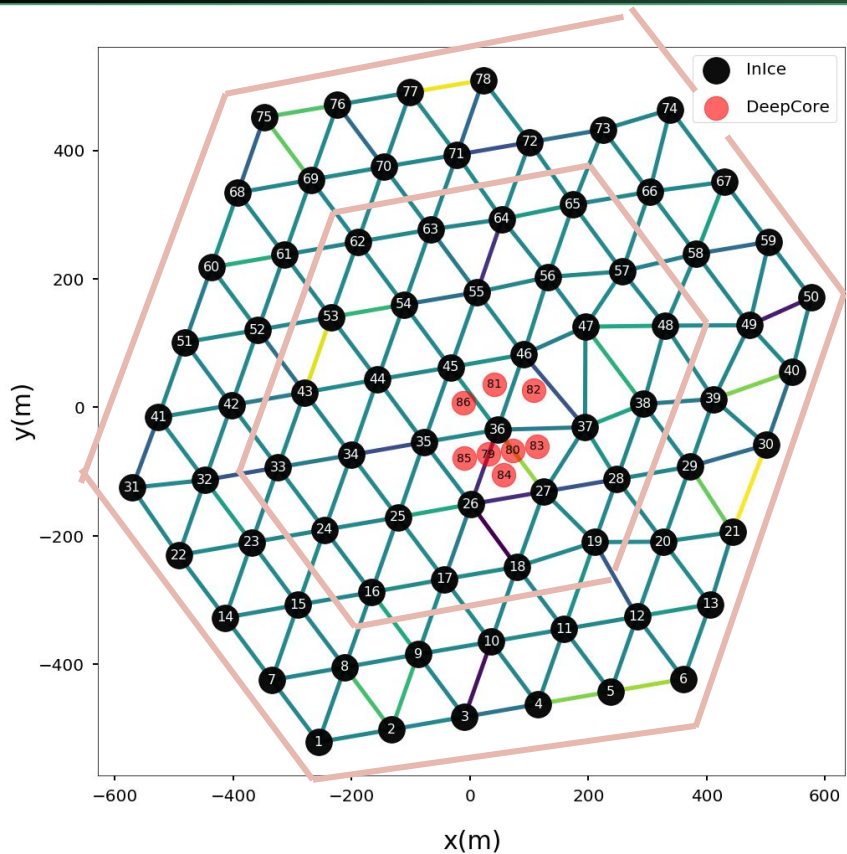
- ❖ Typical separation between the muons \sim O(30-50 m).
- ❖ Inter-string distance is 125 m.
- ❖ The two muons pass between two strings.

SEARCH CHALLENGES WITH ICECUBE [2/2]



- ❖ Typical separation between the muons $\sim O(30-50 \text{ m})$.
- ❖ Inter-string distance is 125 m.
- ❖ The two muons pass between two strings.
- ❖ They almost mimic the behavior of a single muon.
- ❖ Since IceCube's medium is ice, there is light scattering.

DETECTOR TOP VIEW: GEOMETRY OPTIMIZATION



Outer two layers of the detector