

Equivariant Point Cloud Generation for Particle Jets

Erik Buhmann^{*}, Gregor Kasieczka, Jesse Thaler

Very popular: Generative Models

DALL·E 2



↖
Text prompt:
"artificial intelligence solving
particle physics equations,
digital art, written A I"

INSIDER Log in Subscribe

HOME > TECH

Artists say AI image generators are copying their style to make thousands of new images — and it's completely out of their control

Beatrice Nolan Oct 17, 2022, 3:22 PM

A collage of various digital art styles. It features a central figure of a person's face, a tiger, and several abstract patterns and shapes. The colors are primarily red, black, and white, with some blue and purple accents. The style is reminiscent of digital art or generative art.

Very popular: Generative Models

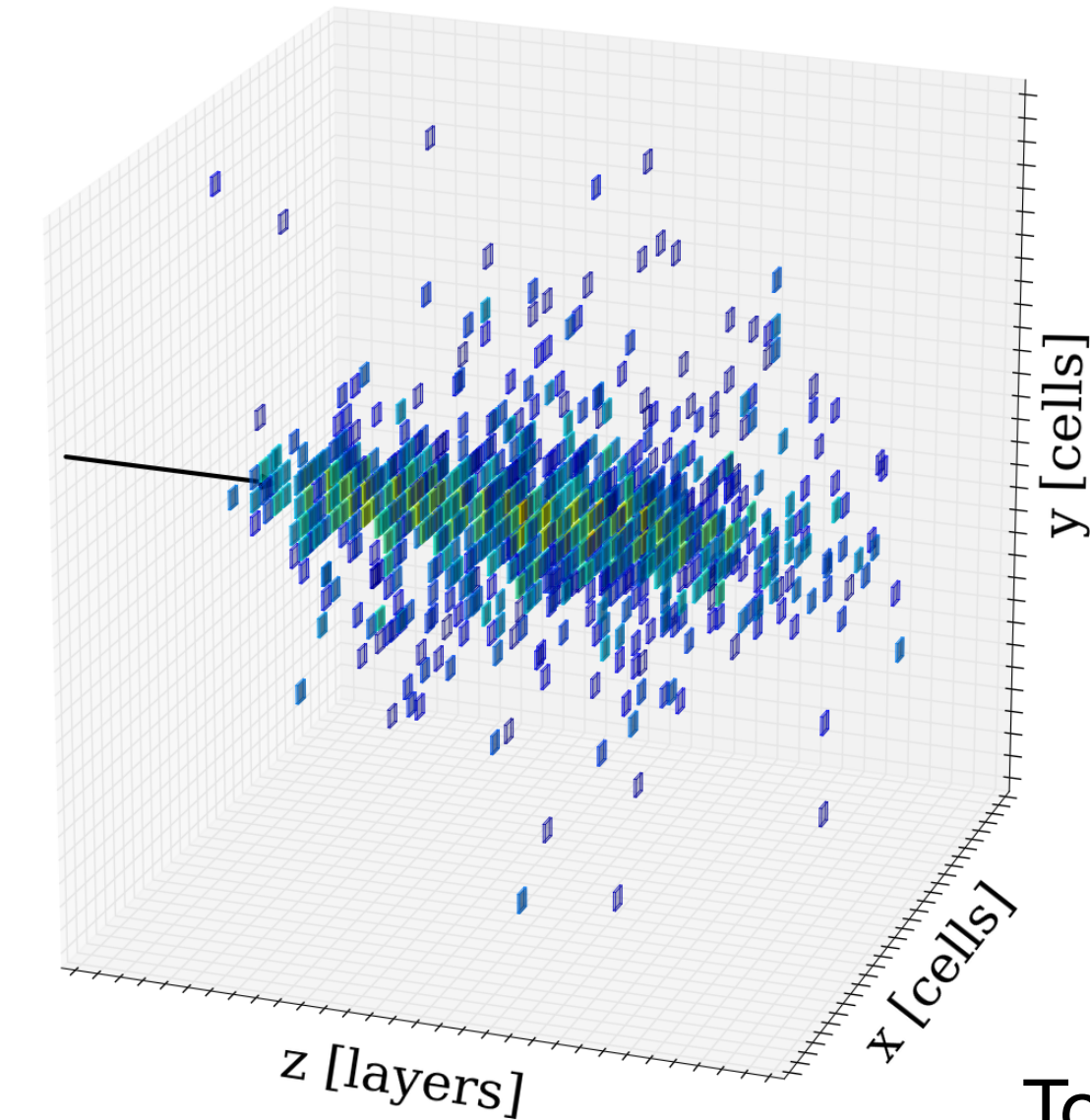
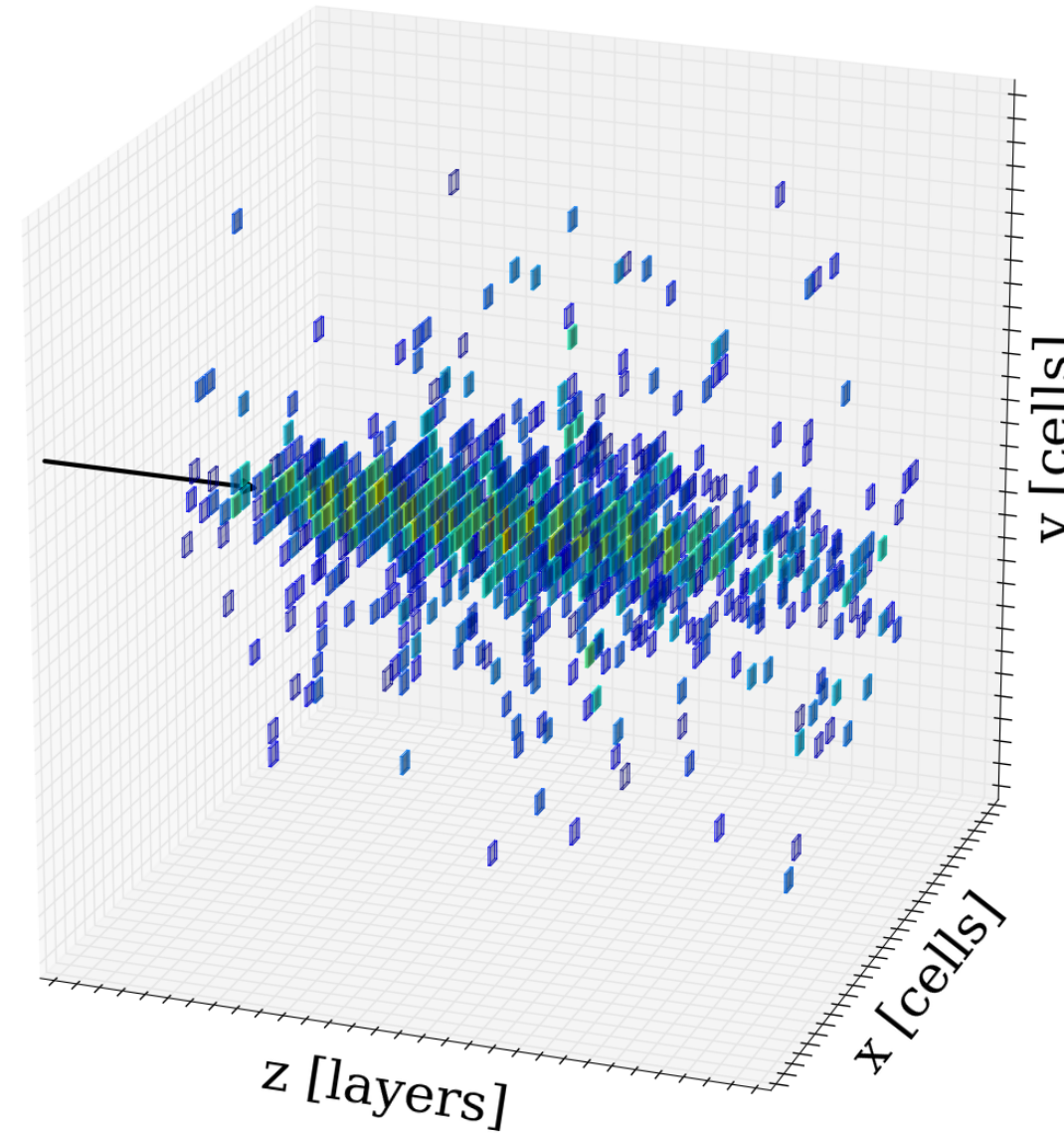
DALL·E 2



Photon shower in high-granularity electromagnetic calorimeter

Simulation with Geant4

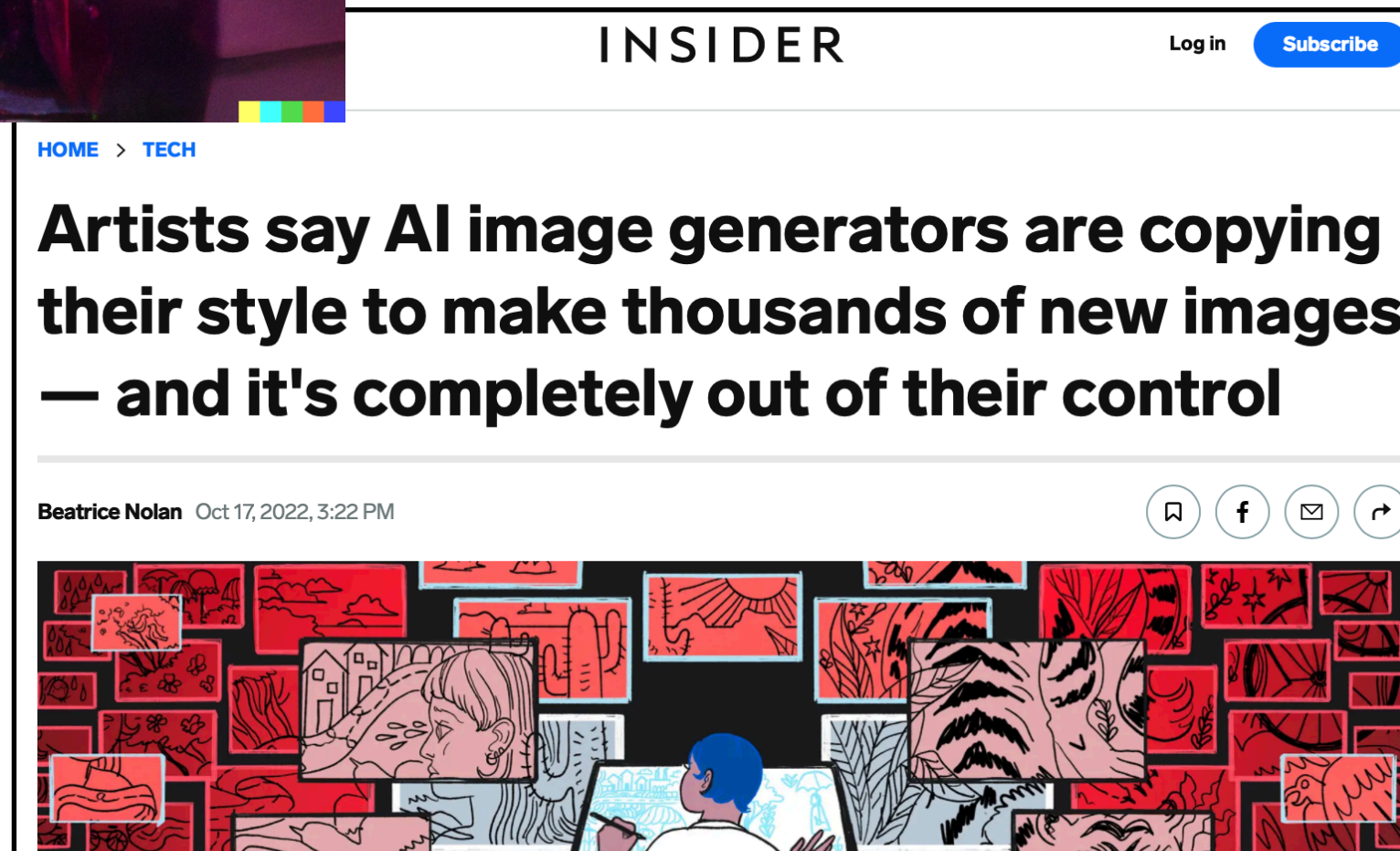
Generation with BIB-AE



[EB, Sascha Diefenbacher et al: Getting High: High Fidelity Simulation of High Granularity Calorimeters with High Speeds](#)

[Learn more: Sascha's talk, Tomorrow 4:15pm](#)

↖
Text prompt:
"artificial intelligence solving particle physics equations, digital art, written A I"



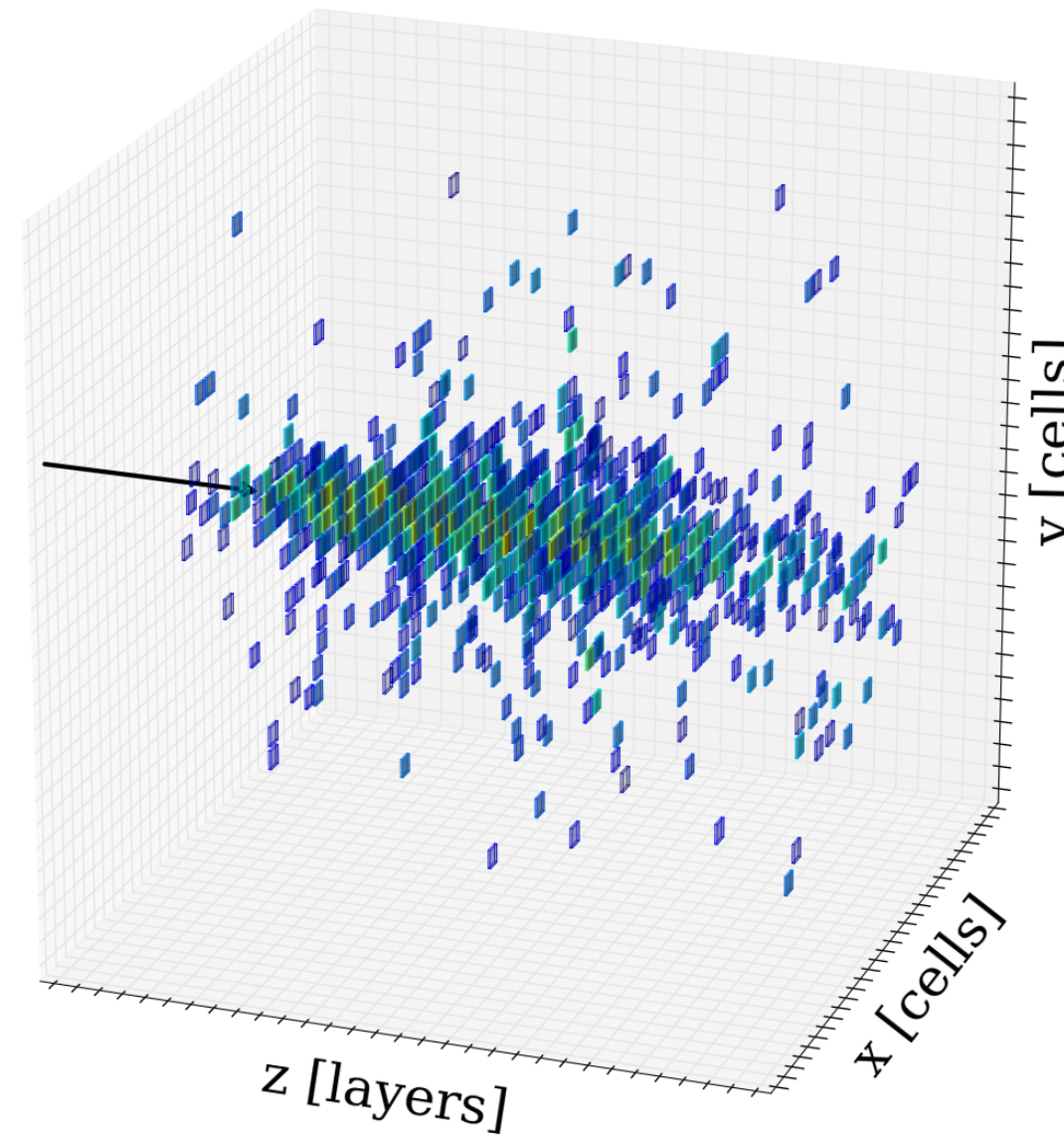
Very popular: Generative Models

DALL·E 2

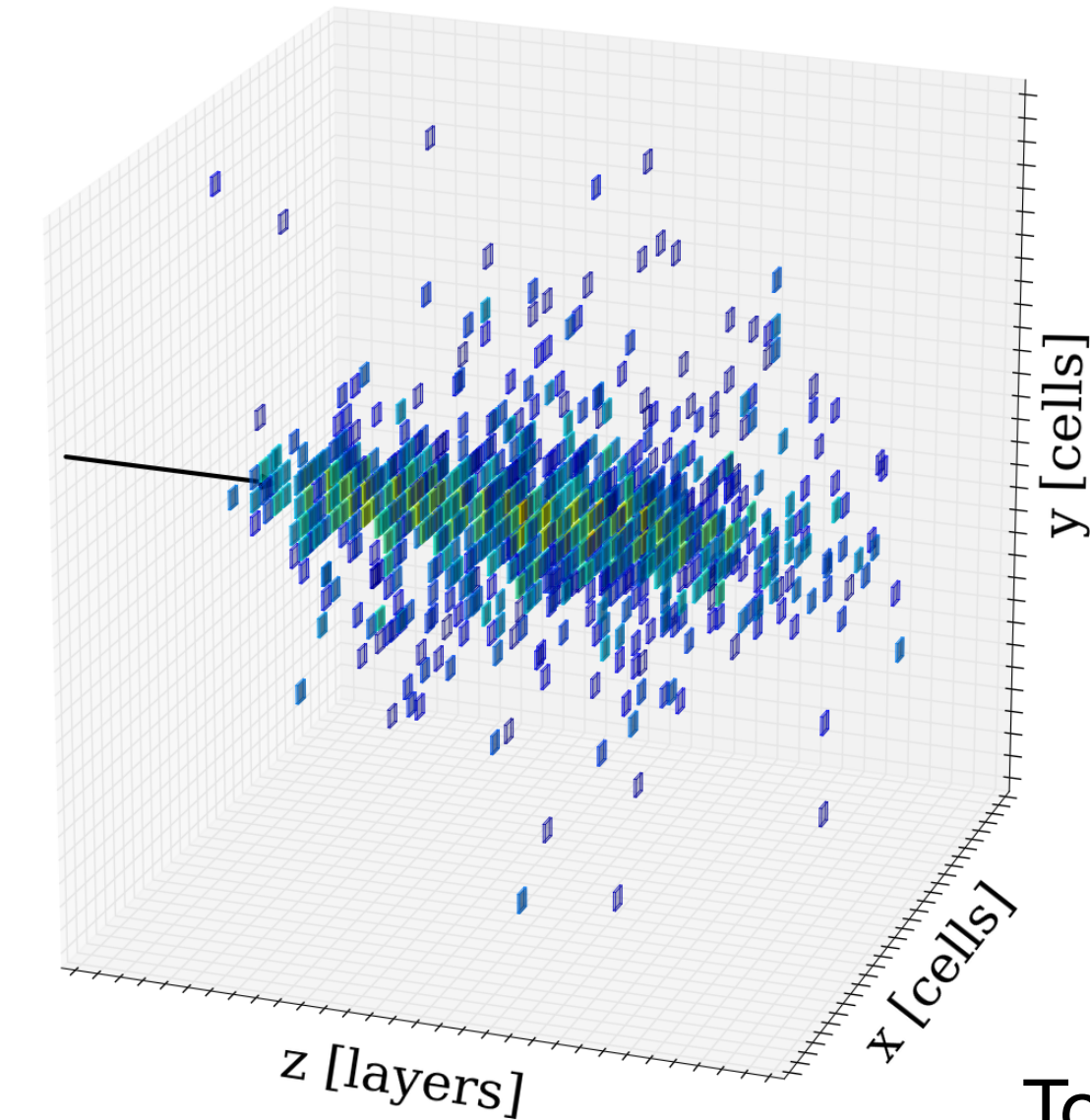


Photon shower in high-granularity electromagnetic calorimeter

Simulation with Geant4



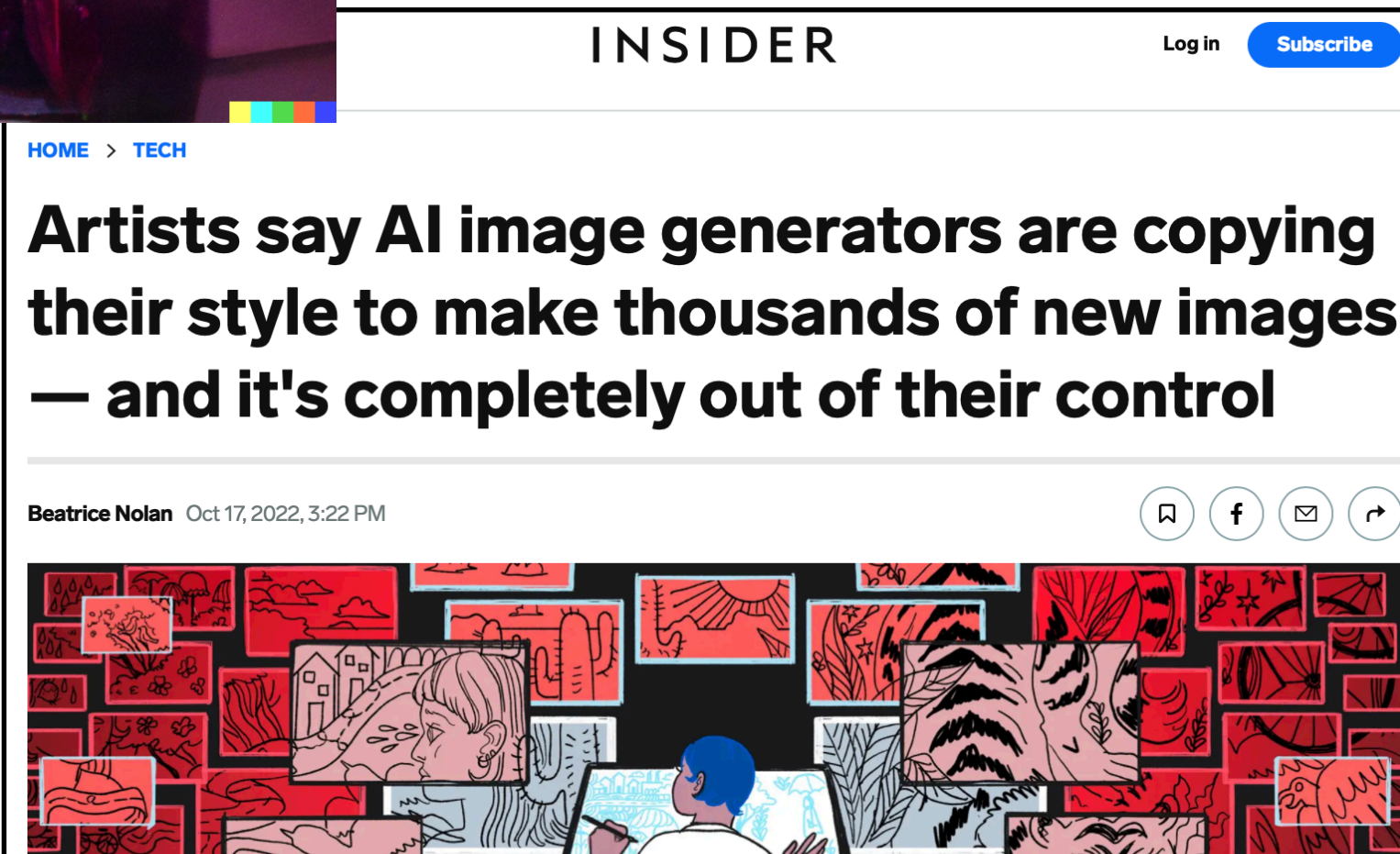
Generation with BIB-AE



[EB, Sascha Diefenbacher et al: Getting High: High Fidelity Simulation of High Granularity Calorimeters with High Speeds](#)

[Learn more: Sascha's talk, Tomorrow 4:15pm](#)

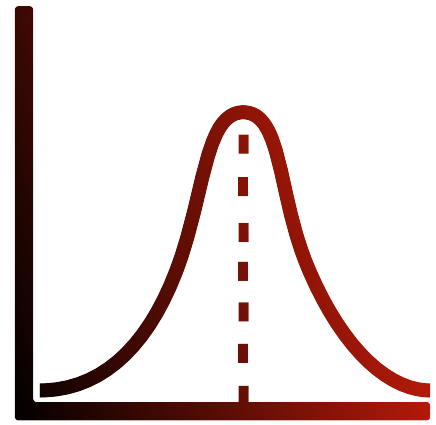
↖
Text prompt:
"artificial intelligence solving particle physics equations, digital art, written A I"



"If generative models recreate what they have learned, what's the point of training on simulation?"

Generative Models: Use cases in HEP research

Amplification of statistics



- Strong inductive bias of architectures help models to learn underlying distribution
- Powerful data augmentation technique

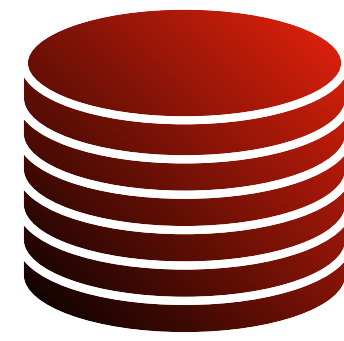
[S Bieringer et al: Calomplification - The Power of Generative Calorimeter Models](#)

[A Butter et al: GANplifying Event Samples](#)

[J Kummer et al: Radio Galaxy Classification with wGAN-Supported Augmentation](#)

[...]

Amortised computation



- Minimisation of local computing resources by upfront central model training
- Storing model weights instead of data

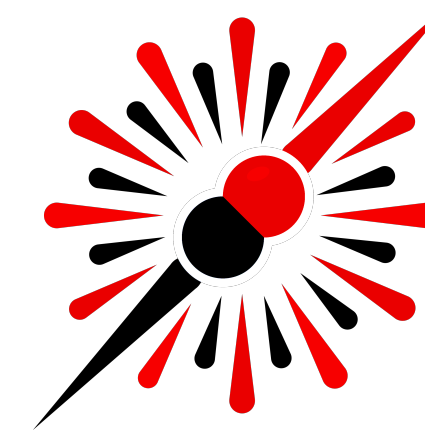
[M Paganini et al: CaloGAN: Simulating 3D High Energy Particle Showers in Multi-Layer Electromagnetic Calorimeters with Generative Adversarial Networks](#)

[EB, Sascha Diefenbacher et al: Getting High: High Fidelity Simulation of High Granularity Calorimeters with High Speeds](#)

[A Butter et al: Machine Learning and LHC Event Generation](#)

[...]

Generation from detector data



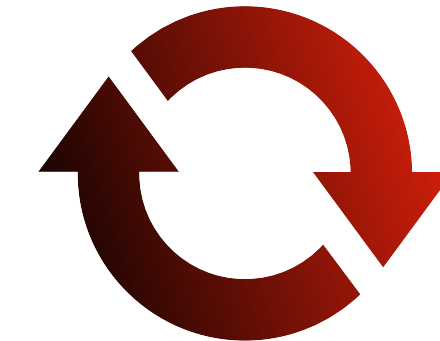
- Unsupervised training on real events instead of tuning Monte Carlo simulations
- I.e. for estimation of background densities

[JN Howad et al: Learning to Simulate High Energy Particle Collisions from Unlabeled Data](#)

[A Hallin et al: Classifying Anomalies THrough Outer Density Estimation \(CATHODE\)](#)

[...]

Differentiable models



- Optimisation of experimental setup based on explicit data likelihood
- Backpropagation through analysis chain

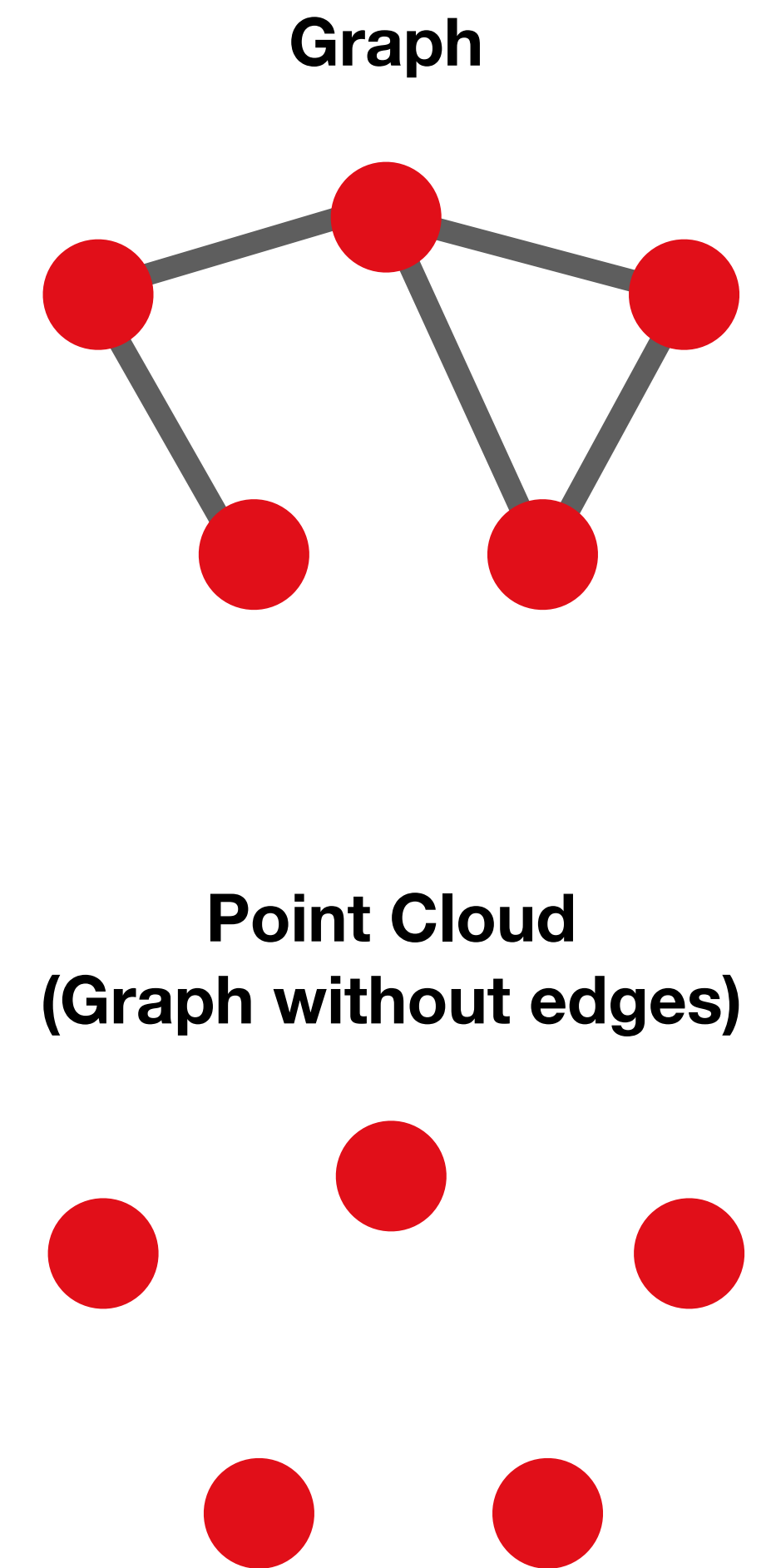
[T Dorigo et al: Toward the End-to-End Optimization of Particle Physics Instruments with Differentiable Programming: a White Paper](#)

[A Adelmann et al: New directions for surrogate models and differentiable programming for High Energy Physics detector simulation](#)

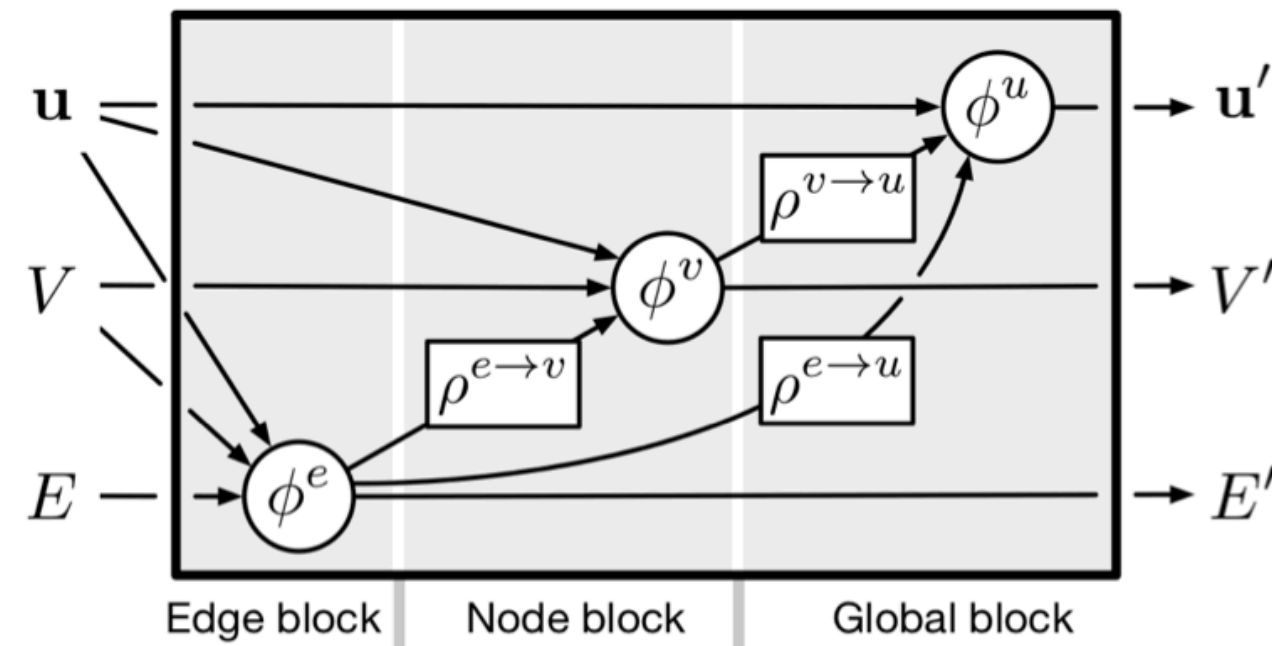
[...]

Generative Modelling of Point Clouds

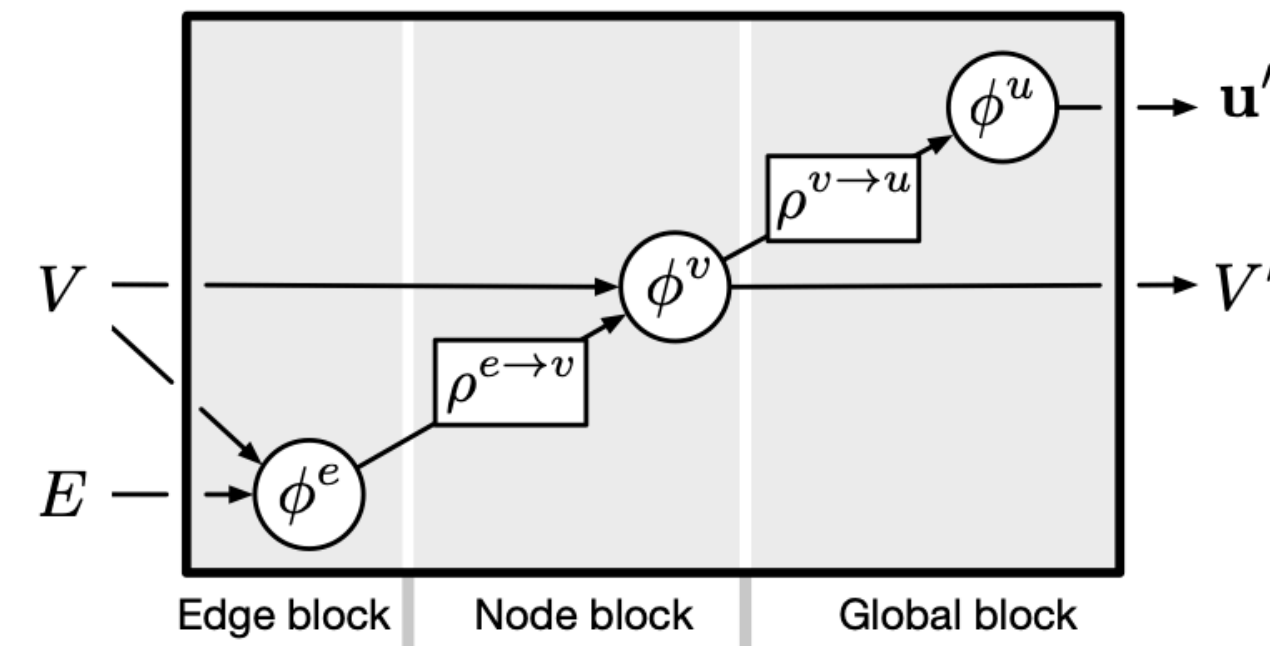
- Particle jets are **variable-length, unordered sets** of particles
 - Natural representation as “point cloud”
- Requirements for generative model:
 - A. Variable particle multiplicity N
 - B. Permutation equivariance
 - C. Fast generation for large multiplicities (ideally $\mathcal{O}(N)$)
- Current approaches using graph & transformer models
- Our simple Deep Sets-based generative model is **equally performant, yet less complex and significantly faster**



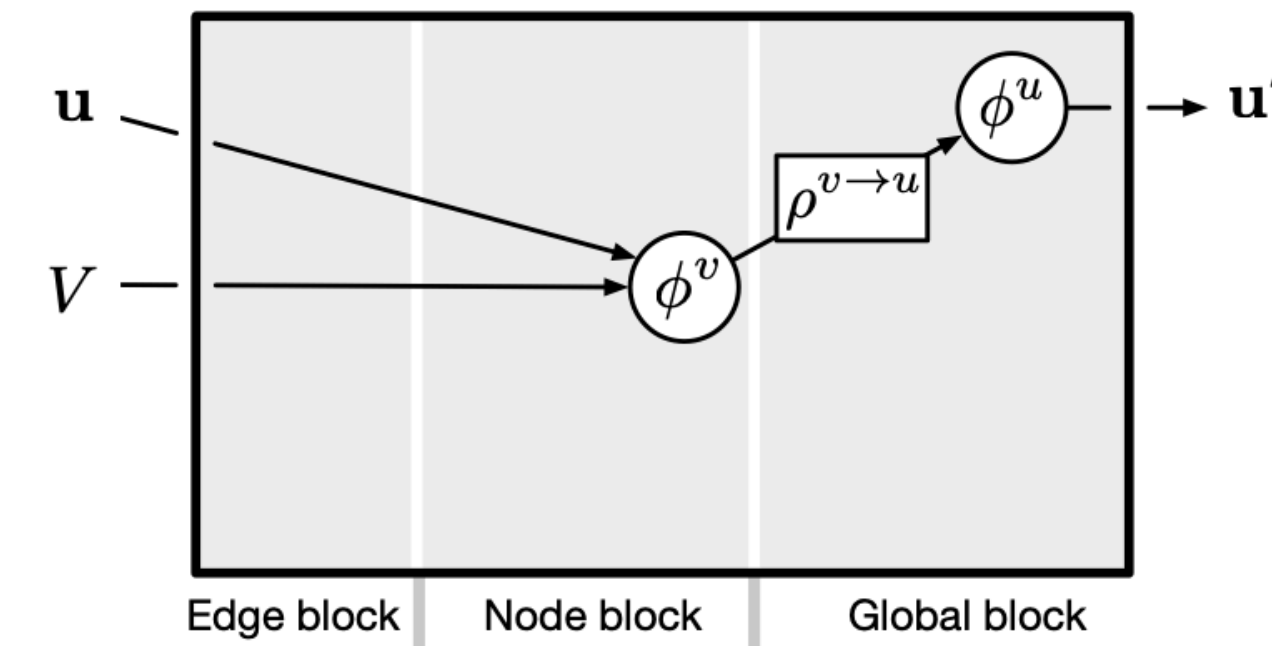
Graph and Deep Sets Architectures



Full graph network block



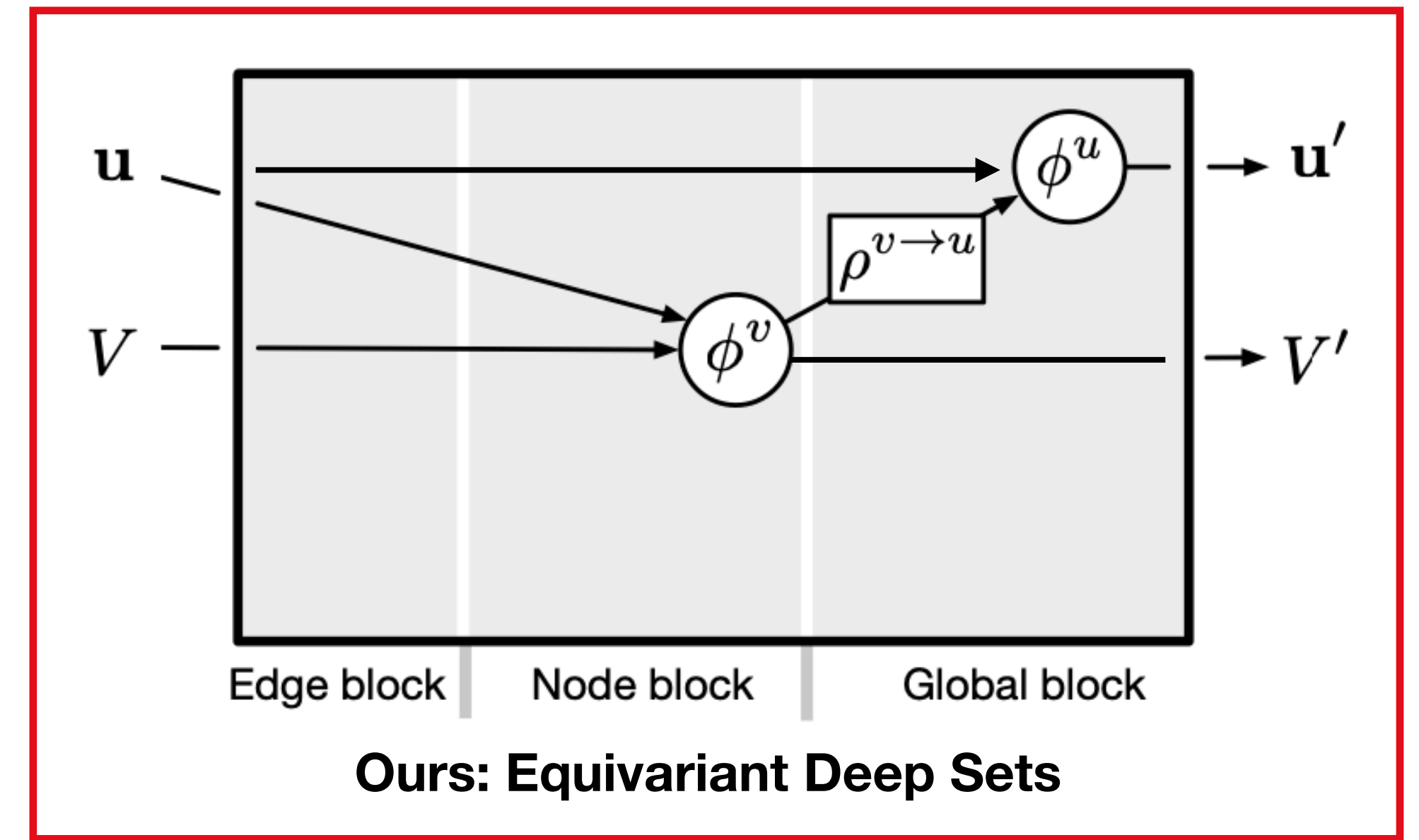
Message-passing neural network
(Without u' : (Self-)attention network)



Invariant Deep Sets

Graph: $G = (u, V, E)$
 u : Global attribute
 V : Node's attributes
 E : Edge's attributes

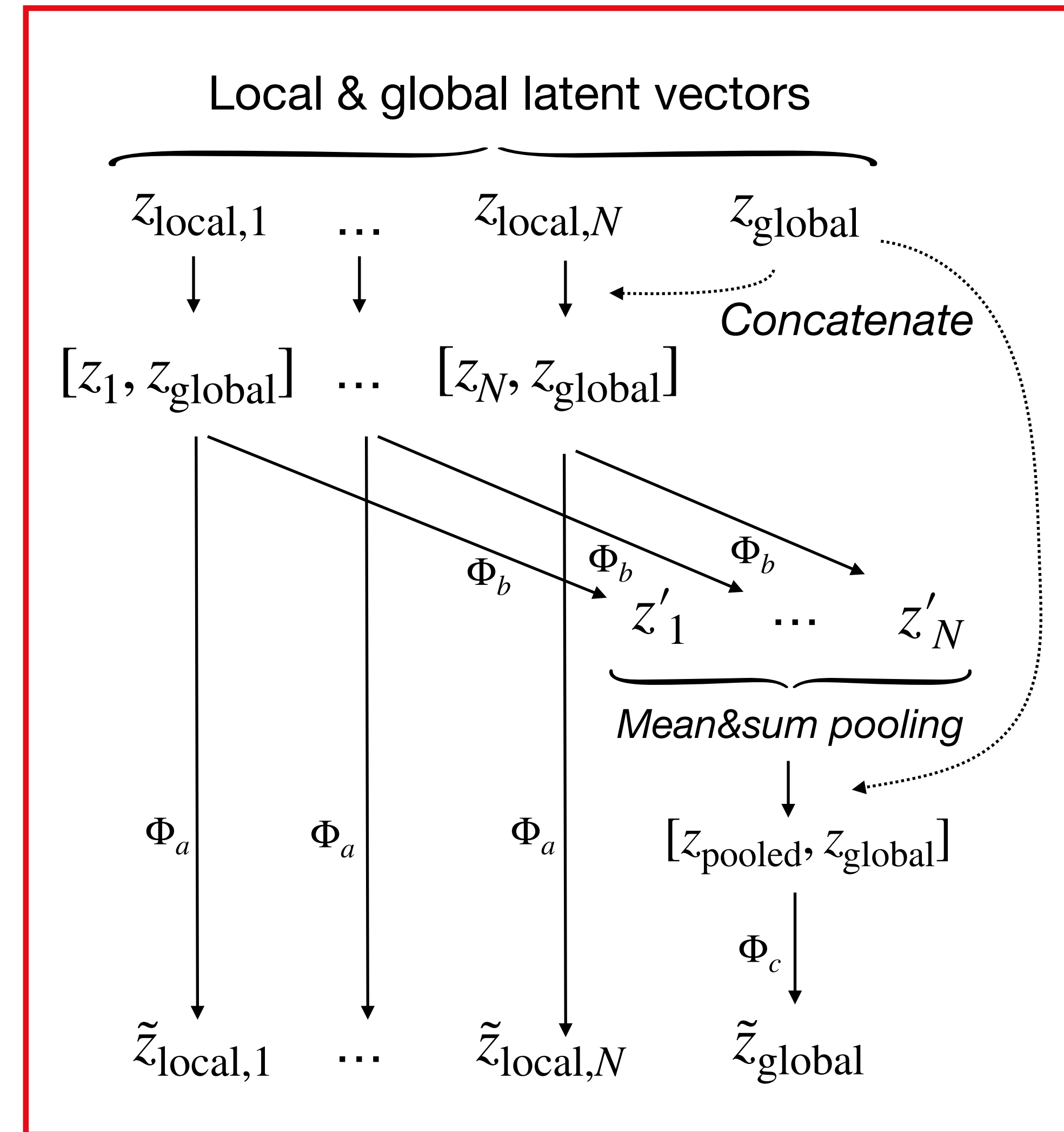
- Advantage of Equivariant Deep Sets:
Very simple model and fast generation (scaling $\mathcal{O}(N)$)
- Generative modelling via Generative Adversarial Network (GAN), Autoencoder, Flow, etc. frameworks



Ours: Equivariant Deep Sets

Equivariant Point Cloud (EPiC) Layer

- Particle-wise vectors z_{local} are updated with global vector z_{global} , and vice-versa
- Both mean & sum pooling necessary for variable particle multiplicity
- Control of communication between local vectors via:
 1. Length of global vector z_{global}
 2. Number of stacked EPiC layers R
- Optimisation of these two hyperparameters to develop minimal generative model

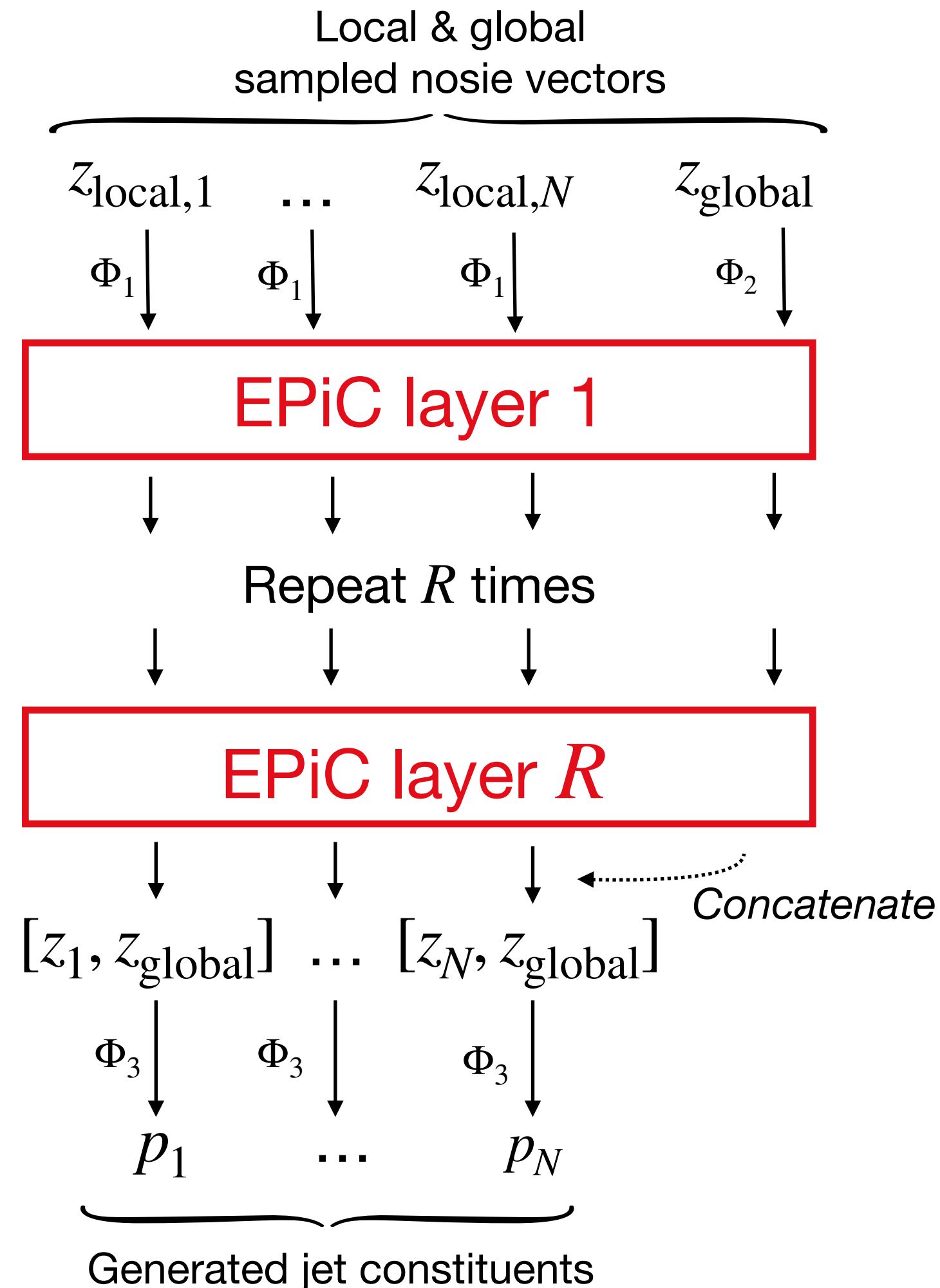


Φ : Fully Connected Network

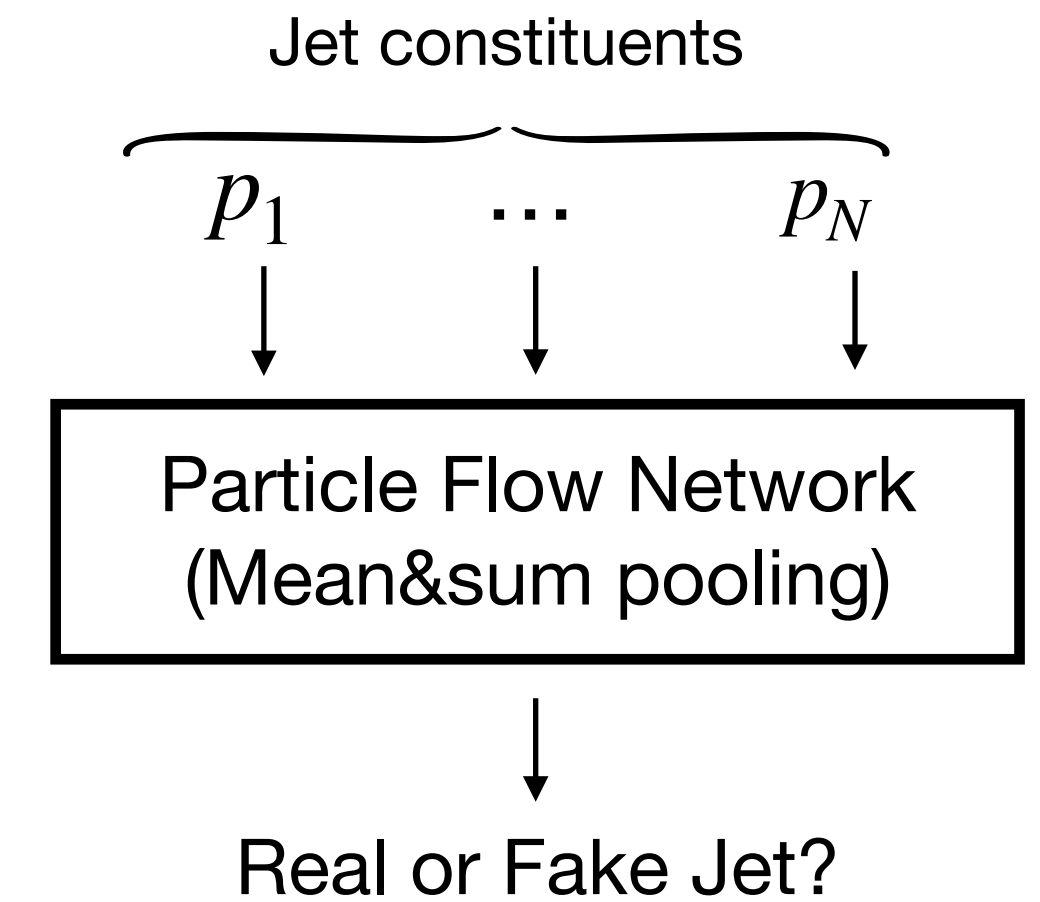
Equivariant Point Cloud (EPIc) GAN

- Generator (90k parameters):
 - Multiple R Equivariant Point Cloud layer stacked
 - With $R = 0$ equivalent to “Point Cloud GAN (PC-GAN)” generator
- Discriminator (25k parameters):
 - Invariant Deep Sets structure
- Particle multiplicity defined when sampling

Generator G :



Discriminator D :



PT Komiske, et al: Energy Flow Networks: Deep Sets for Particle Jets

LSGAN loss objective:

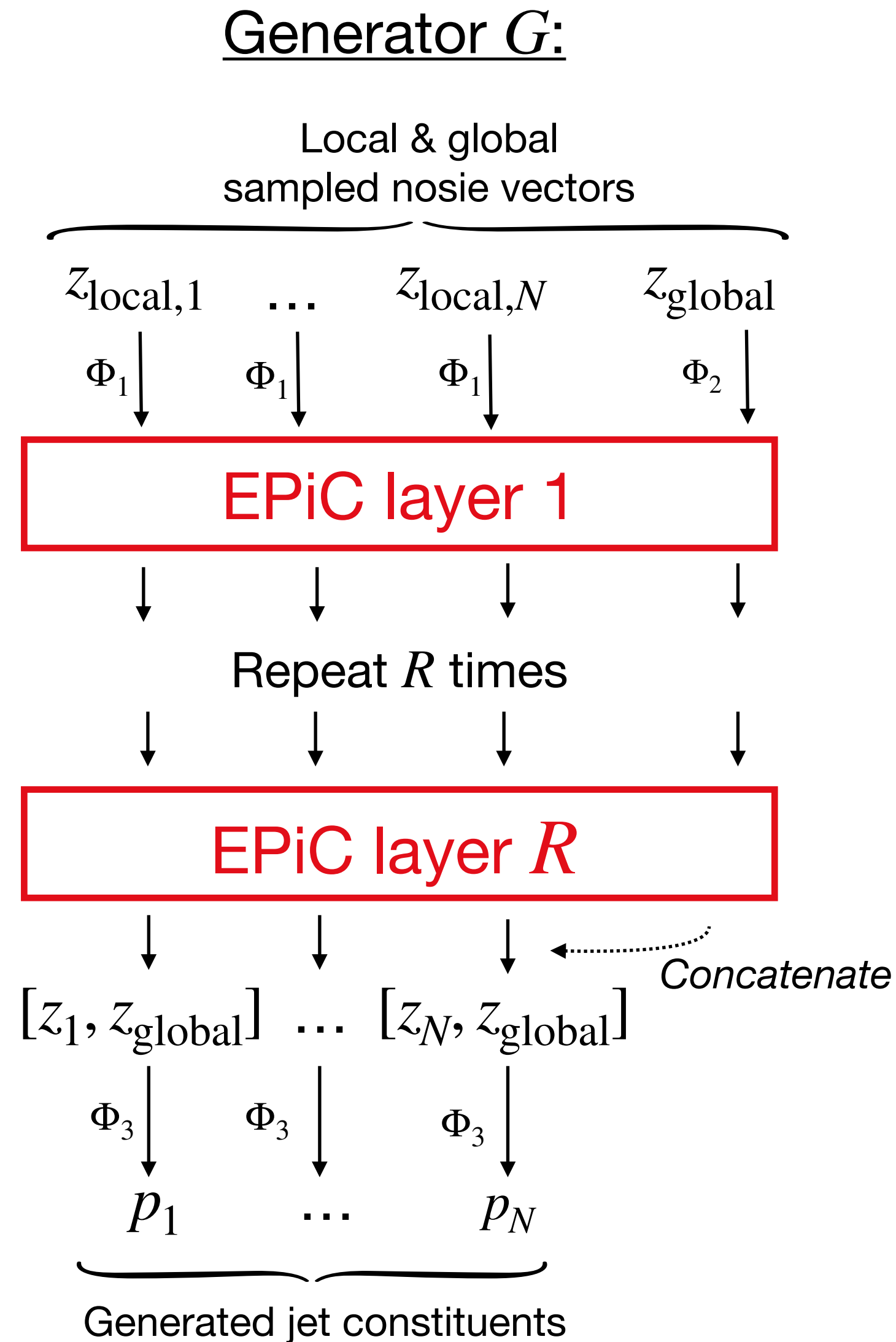
$$\min_D L(D) = \frac{1}{2} \mathbb{E}[(D(x) - 1)^2] + \frac{1}{2} \mathbb{E}[(D(G(z)))^2]$$

$$\min_D L(D) = \frac{1}{2} \mathbb{E}[(D(G(z)) - 1)^2]$$

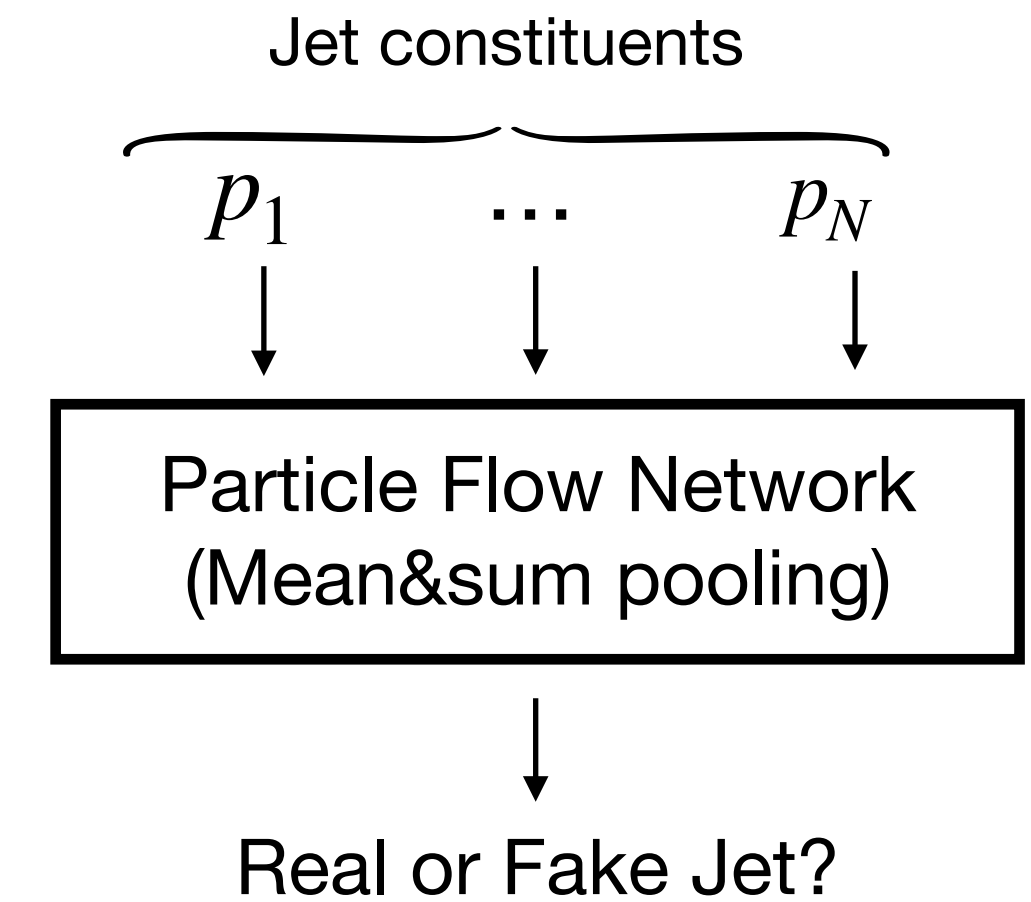
X Mao et al: Least Squares Generative Adversarial Networks

Equivariant Point Cloud (EPIc) GAN

- Avoiding zero-padding by batching jets with same particle multiplicity
- Generation: Particle multiplicity sampled via kernel density estimation
- Trained for 500 epochs, best epoch chosen based on mass distribution on validation set
- $z_{\text{global}} = 5$ global latent variables
- $z_{\text{local}} = 10$ global latent variables



Discriminator D :



PT Komiske, et al: Energy Flow Networks: Deep Sets for Particle Jets

LSGAN loss objective:

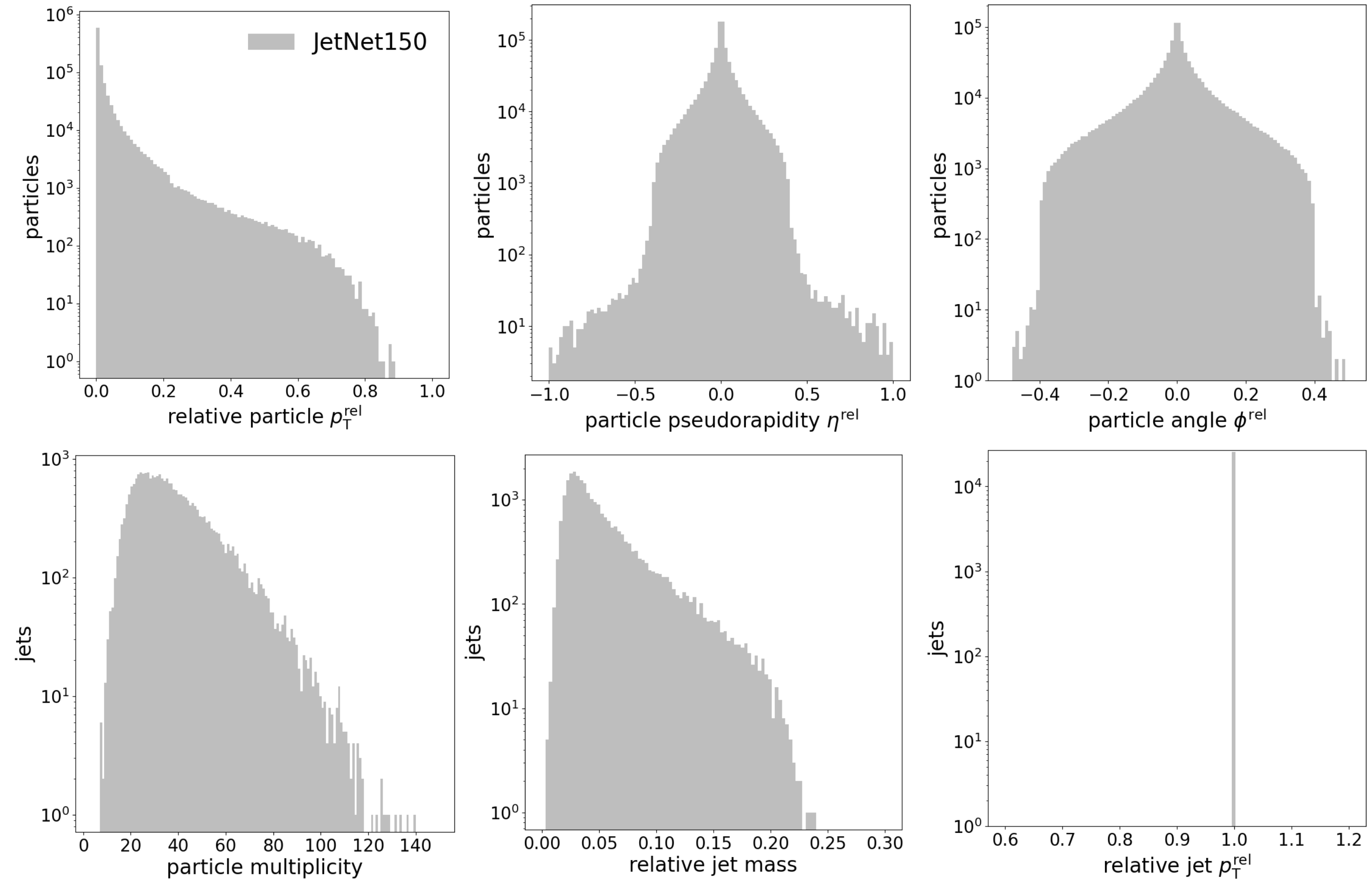
$$\min_D L(D) = \frac{1}{2} \mathbb{E}[(D(x) - 1)^2] + \frac{1}{2} \mathbb{E}[(D(G(z)))^2]$$

$$\min_D L(D) = \frac{1}{2} \mathbb{E}[(D(G(z)) - 1)^2]$$

X Mao et al: Least Squares Generative Adversarial Networks

Point Cloud Data: JetNet150 Dataset

- Benchmark dataset: JetNet150 [1]
- Pythia simulated jets from proton-proton collisions
- Anti- k_T clustered with $R = 0.8$ and maximum particle multiplicity $N = 150$
- Particle collider coordinates normalised and centred
 - $p_T^{\text{rel}} = p_T^{\text{particle}} / p_T^{\text{jet}}$
 - $\eta^{\text{rel}} = \eta^{\text{particle}} - \eta^{\text{jet}}$
 - $\phi^{\text{rel}} = \phi^{\text{particle}} - \phi^{\text{jet}}$
- Today: Only light quark jets dataset

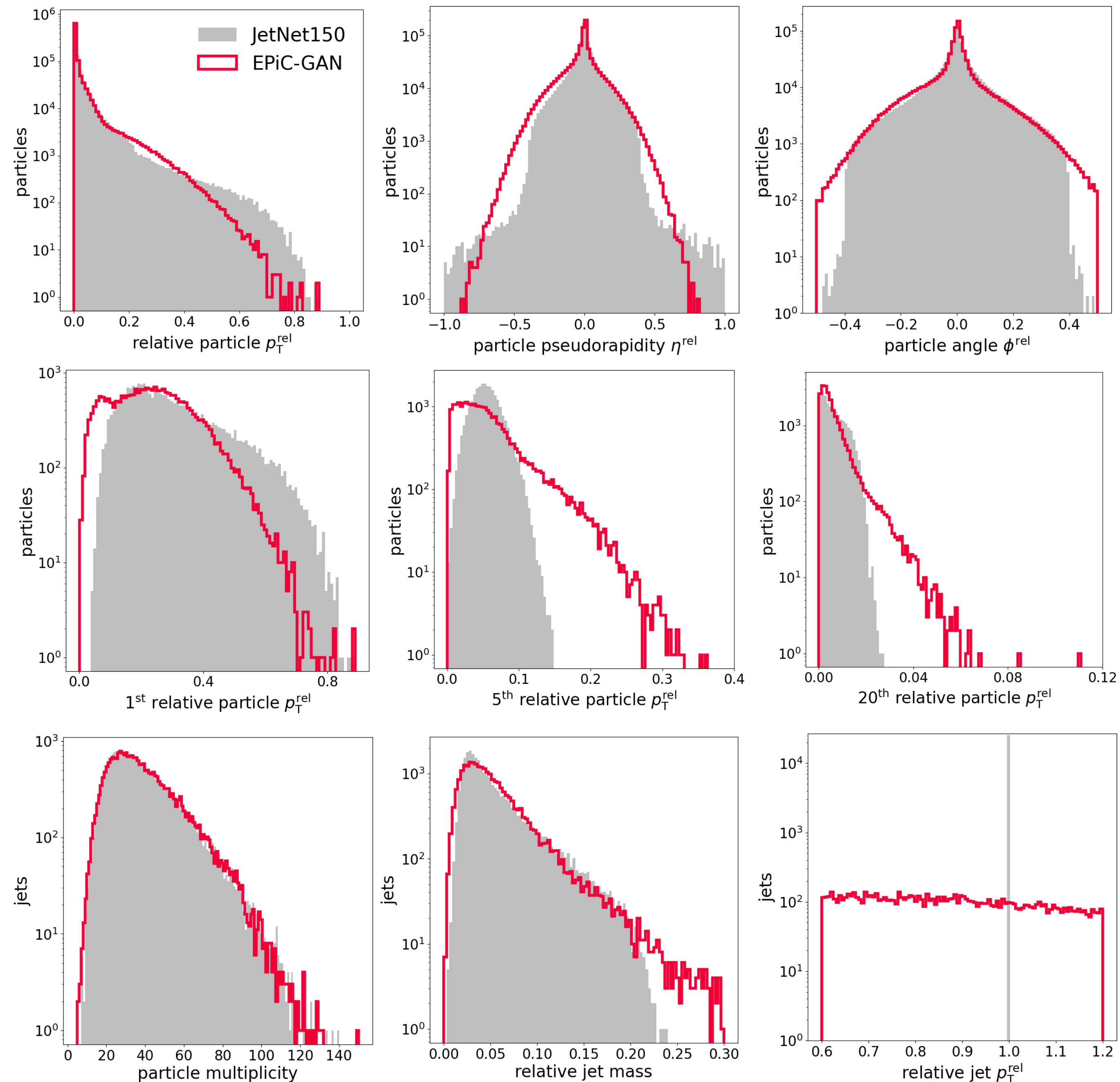


[R Kansal, et al: Particle Cloud Generation with Message Passing Generative Adversarial Networks](#)

[1] [R Kansal, et al: JetNet150 \(2.0.0\) \[Data set\]. Zenodo](#)

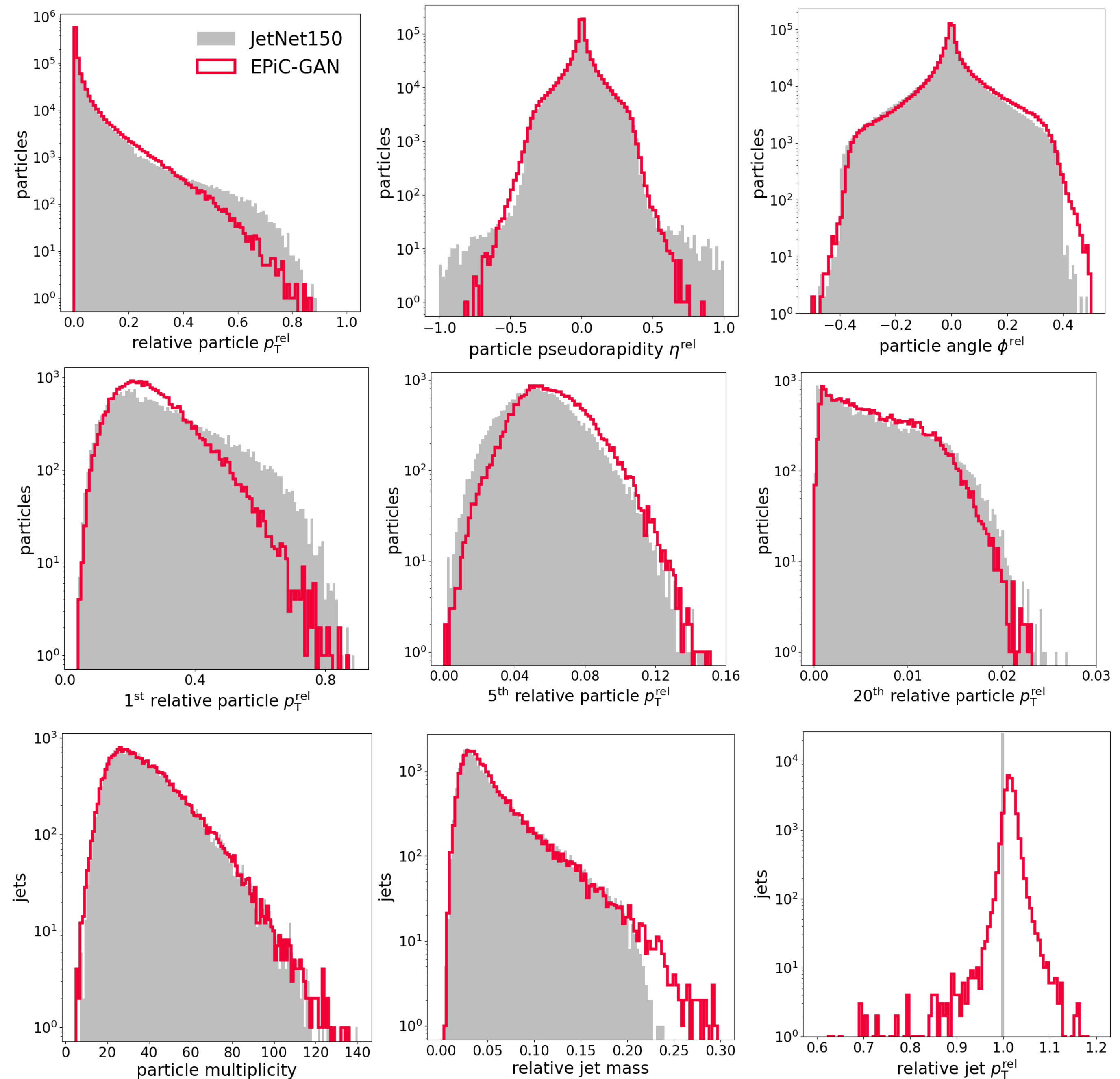
Results on JetNet150 quarks

- EPiC-GAN setup:
 - $R = 0$ equivariant layers
 - Equivalent to PC-GAN generator
- No communication between points possible
- Particle and jet p_T distributions badly represented



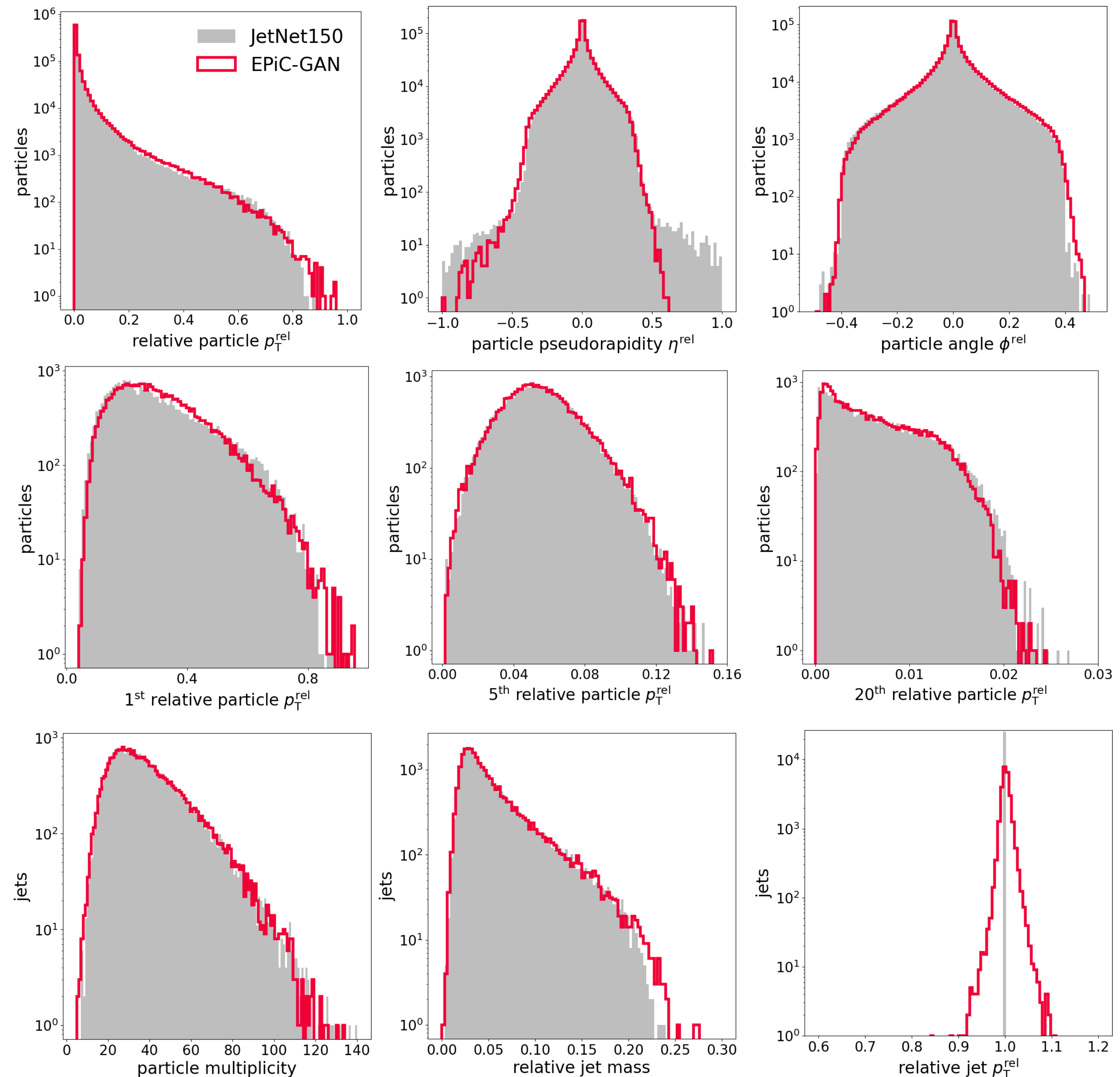
Results on JetNet150 quarks

- EPiC-GAN setup:
 - $R = 1$ equivariant layers
- Points communicate once via global latent vector
- Improves particle and jet p_T distributions significantly
- Improves jet mass distributions as well (correlates with geometric structure of jets)



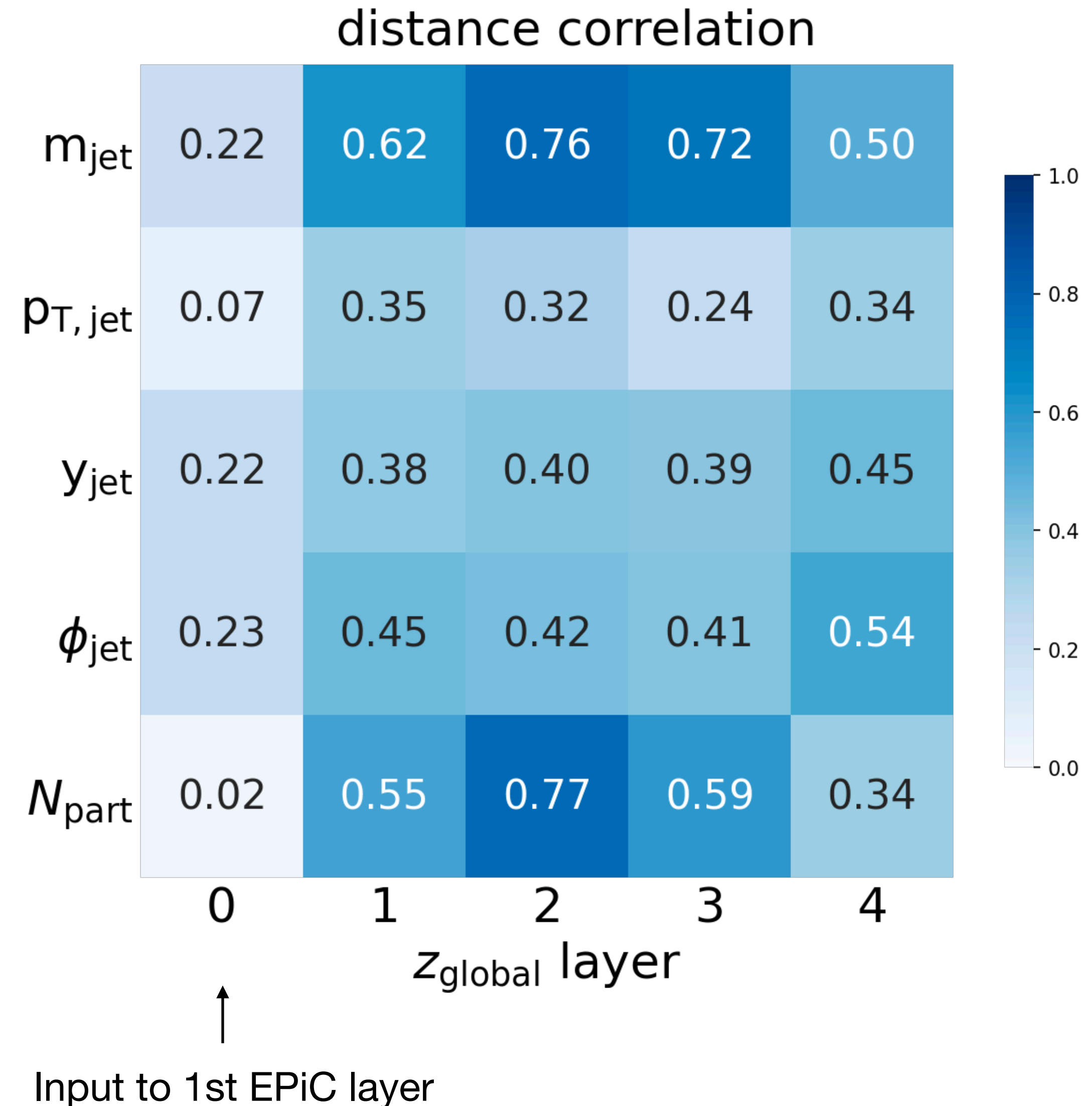
Results on JetNet150 quarks

- EPiC-GAN setup:
 - $R = 4$ equivariant layers
- High generative fidelity after only four communication steps
- Distributions well represented by EPiC-GAN
- Sharp relative jet p_T distribution challenging; can be resolved by calibration



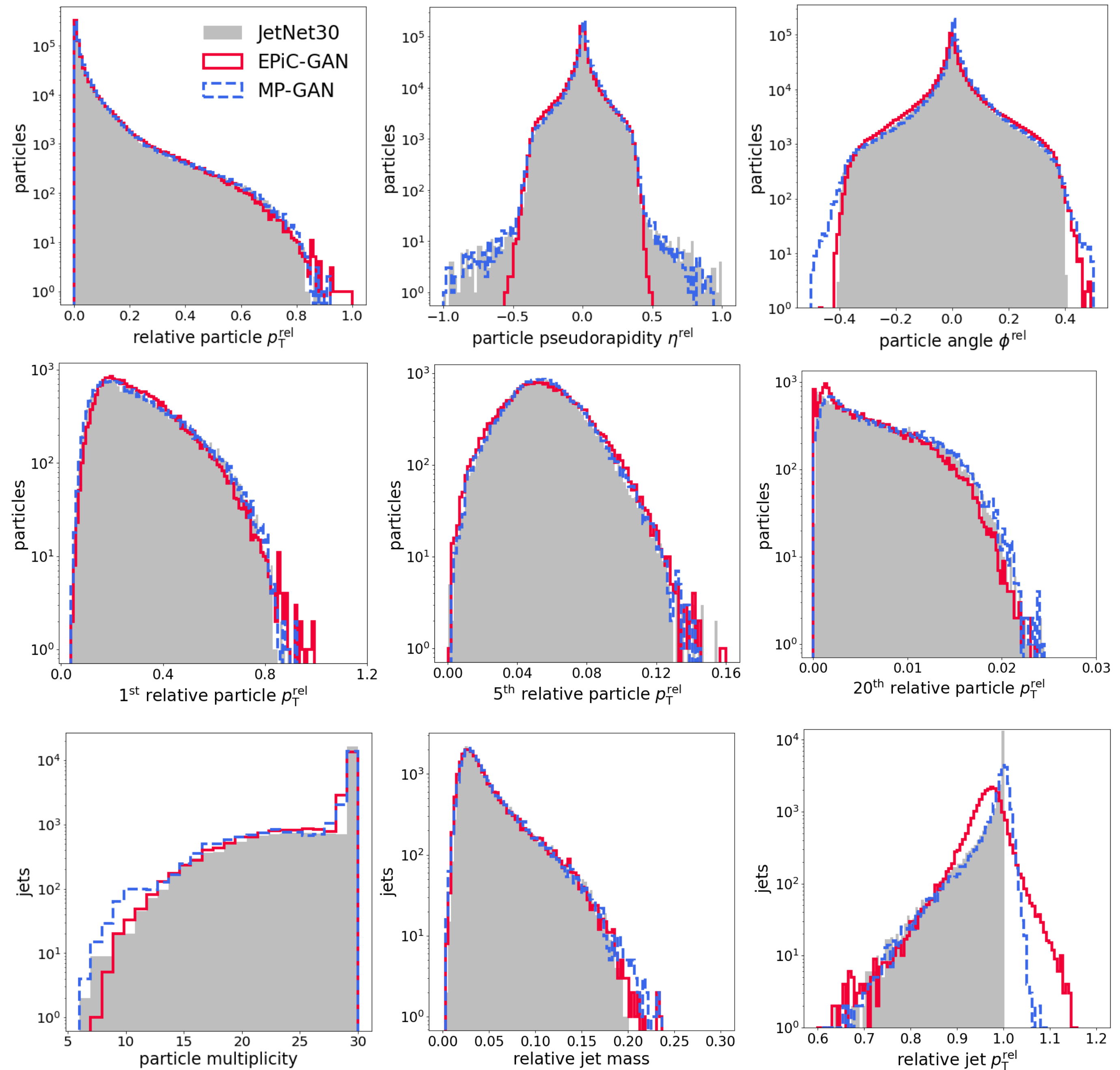
Interpretability: Distance Correlations

- Short global vector allows interpretability
- z_{global} before and after every R equivariant layer
- Distance correlation between physics observables and global vectors
- **Jet features encoded in global vector,** in particular the jet mass & particle multiplicity



Results on JetNet30 quarks

- EPiC-GAN setup:
 - $R = 4$ equivariant layers
 - $z_{\text{global}} = 10$
- Comparison to Message-Passing GAN implementation & trained weights from [1]
- Cut on particle multiplicity for maximum $N = 30$



Similar performance in metrics from [1]:

Metric	W_1^{M} ($\times 10^3$)	W_1^{P} ($\times 10^3$)	W_1^{EFP} ($\times 10^5$)	FPND	COV \uparrow	MMD
MP-GAN	0.6 ± 0.2	4.9 ± 0.5	0.7 ± 0.4	0.35	0.50	0.026
EPiC-GAN	0.8 ± 0.2	2.9 ± 0.5	1.0 ± 0.5	0.93	0.36	0.025

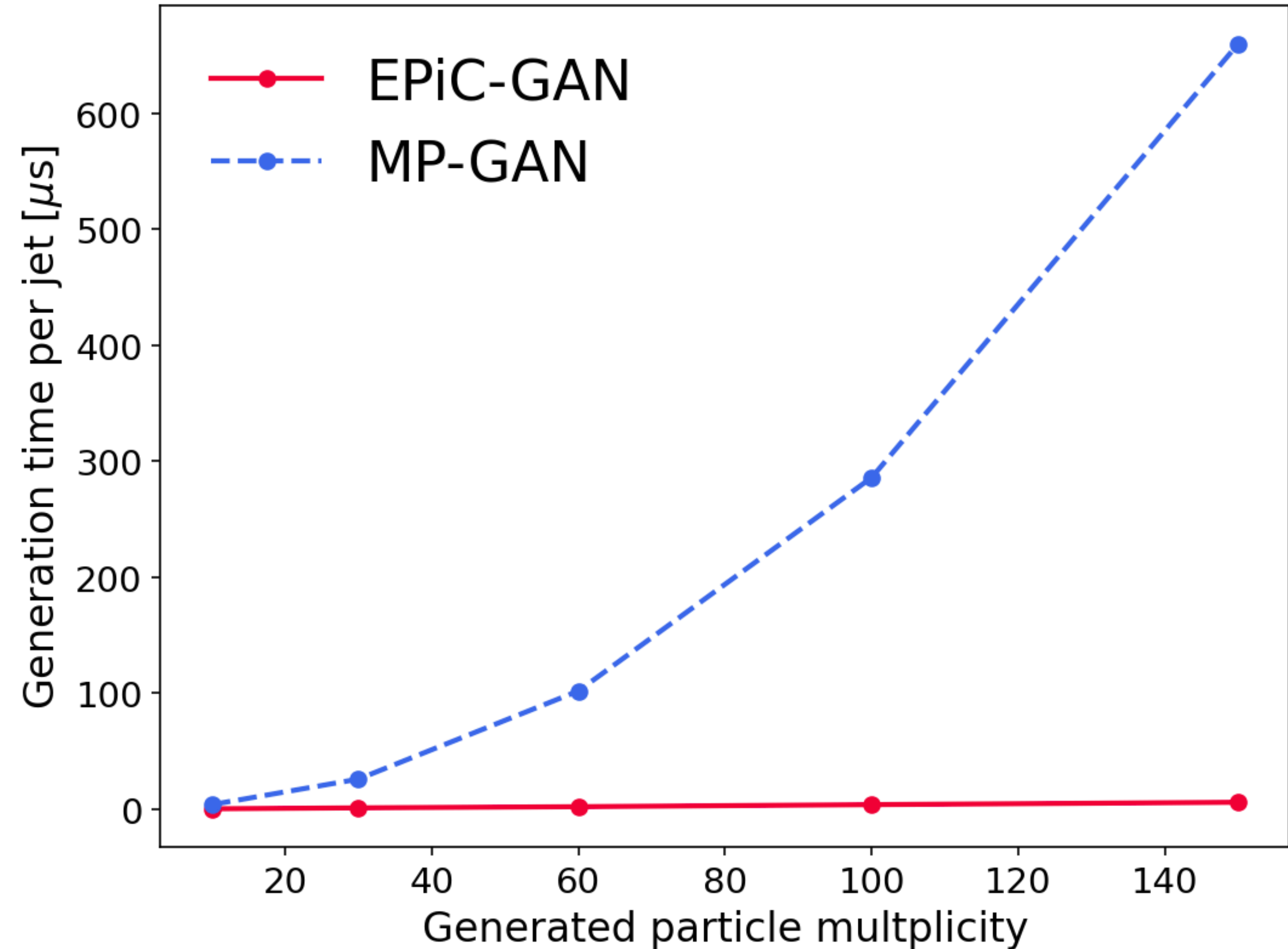
[1] R Kansal, et al: Particle Cloud Generation with Message Passing Generative Adversarial Networks

Scaling of generation time

- Deep Sets scales $\approx \mathcal{O}(N)$
- Message-Passing scales $\approx \mathcal{O}(N^2)$
- Batch size was adjusted for optimal generation speed

Generation time per jet:

Particles	Pythia ^[1]	MP-GAN*	EPiC-GAN*
$N = 30$	46 ms	26 μs	1 μs
$N = 150$	46 ms	660 μs	6 μs

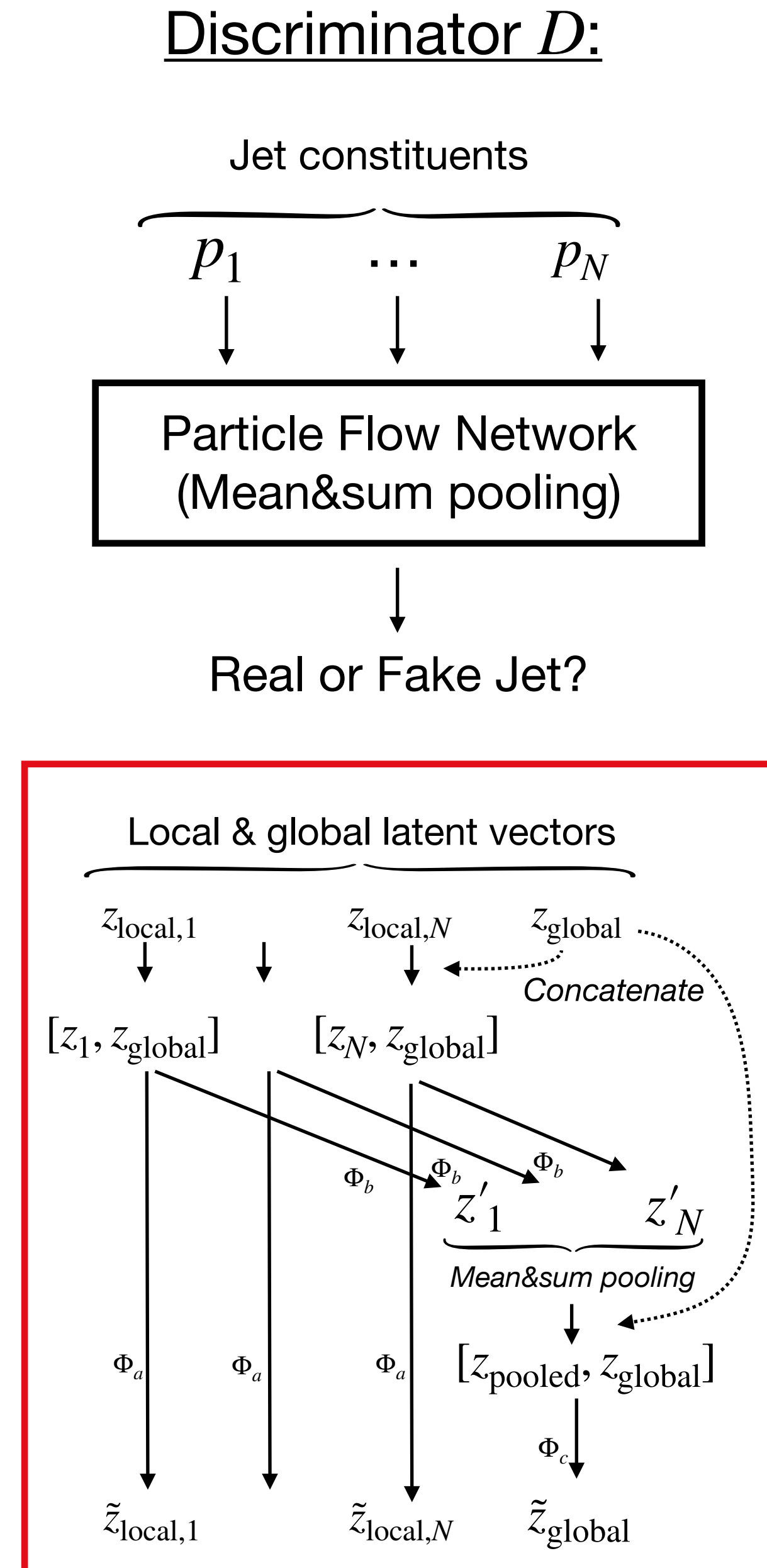
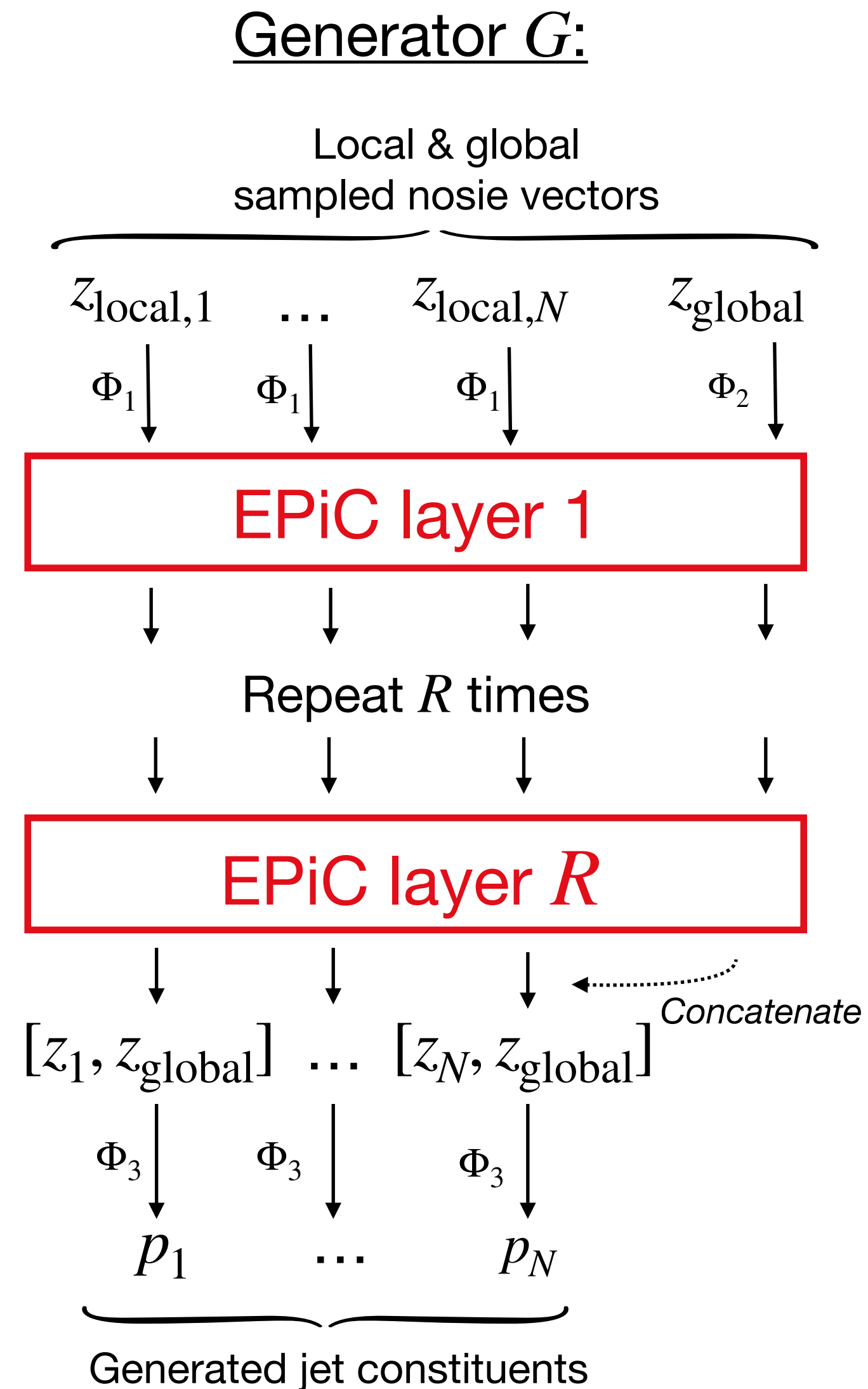


* 500k jets generated on hardware:
Intel Gold-5218 (64 CPUs @ 2.3 Ghz), 384GB RAM, Nvidia A100-40GB

[1] R Kansal, et al: Particle Cloud Generation with Message Passing Generative Adversarial Networks

Summary

- Generative modelling of point clouds usually done with graph and transformer-based models
- Equivariant Point Cloud (EPIc) GAN offers a **simple and fast alternative**
- Model generates realistic particle jets with **variable particle multiplicity**
- Fine-tuning possible for **minimal global information & model complexity**



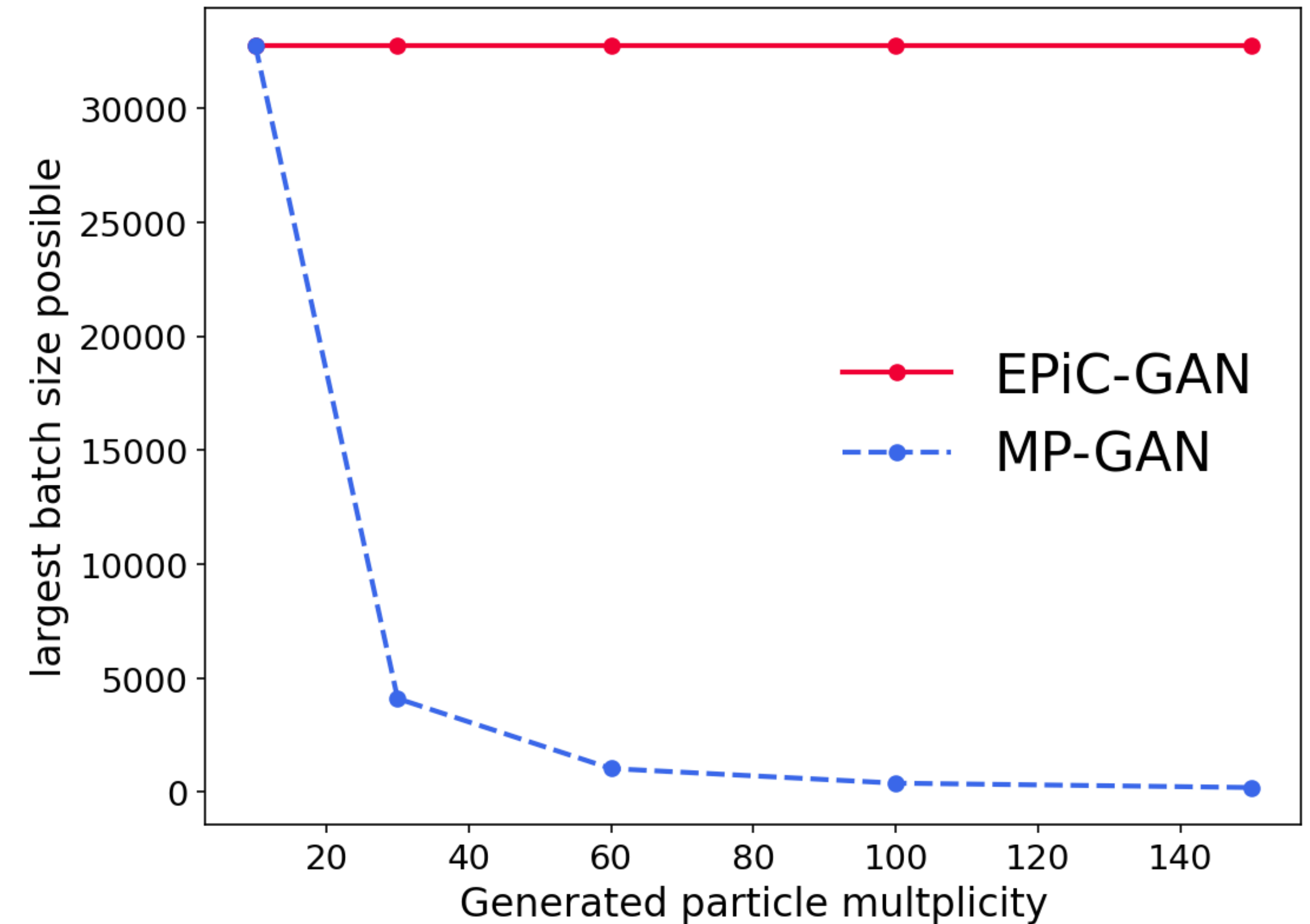
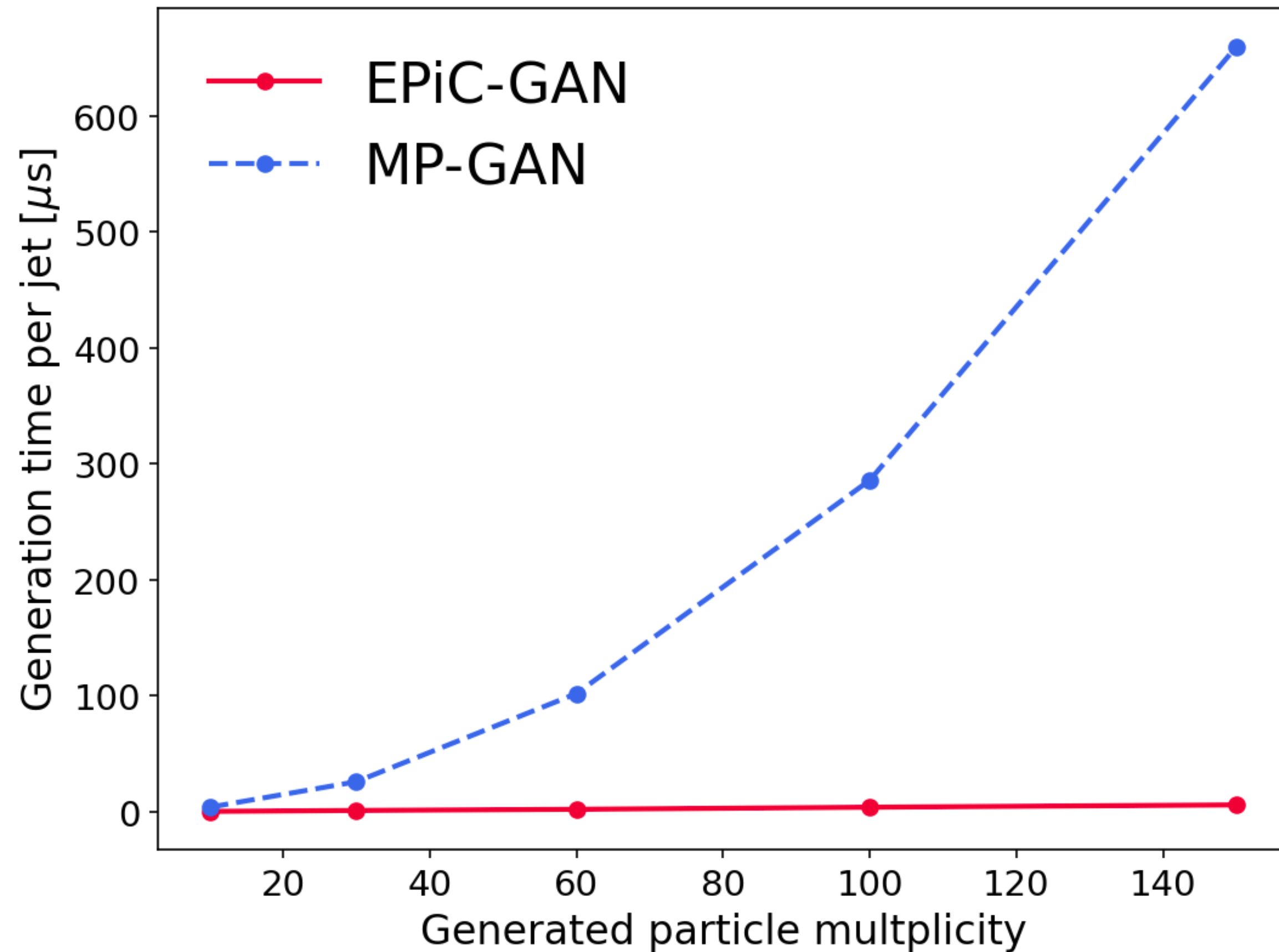
Stay tuned for the paper!

Bonus slides

EPiC-GAN Hyperparameter

- Trained for 500 epochs
- Learning rate of Adam optimiser: $1e-4$
- Maximum batch size = 128
- Pre-processing: Each feature standardised to $\mathcal{N}(0,5\sigma)$
- Generator: 90k parameters (with $R = 4$ & $z_{\text{global}} = 5$)
- Discriminator: 25k parameters
- All fully connected layer size = 64
- z_{local} : For each particle one local noise vector of length 10
- Training / validation / test set: 127k / 26k / 26k
- Shown plots from test set with 26k events

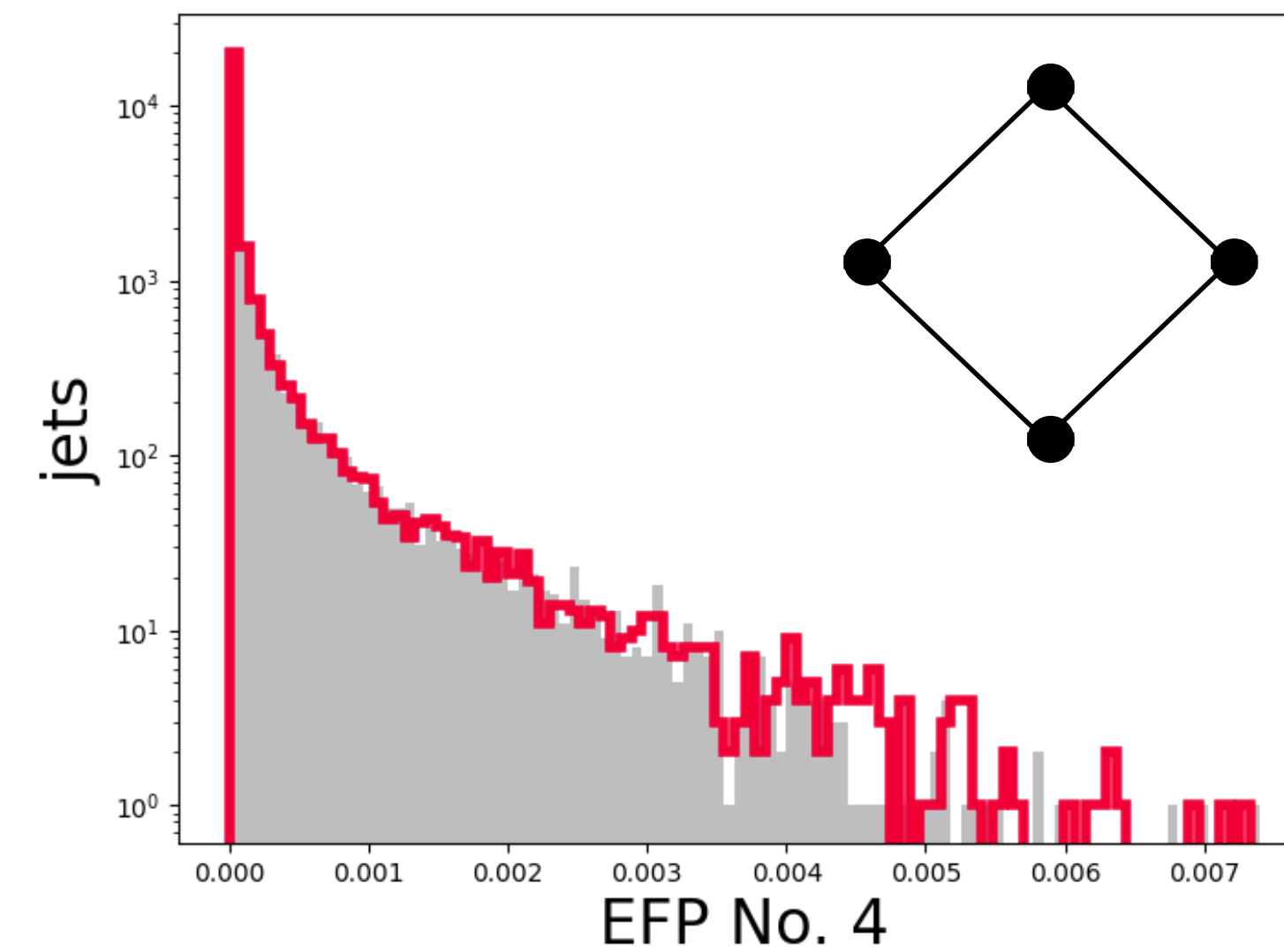
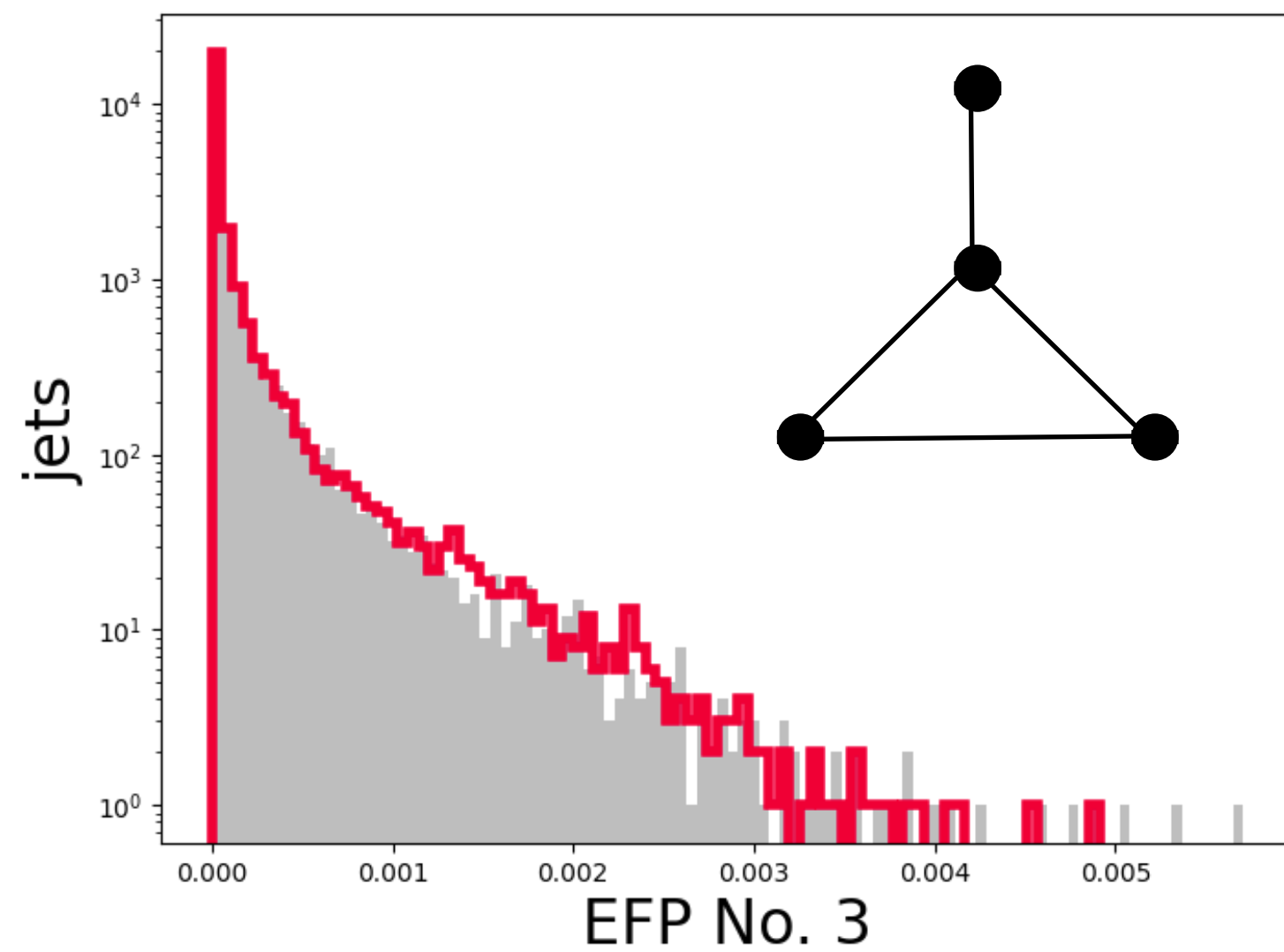
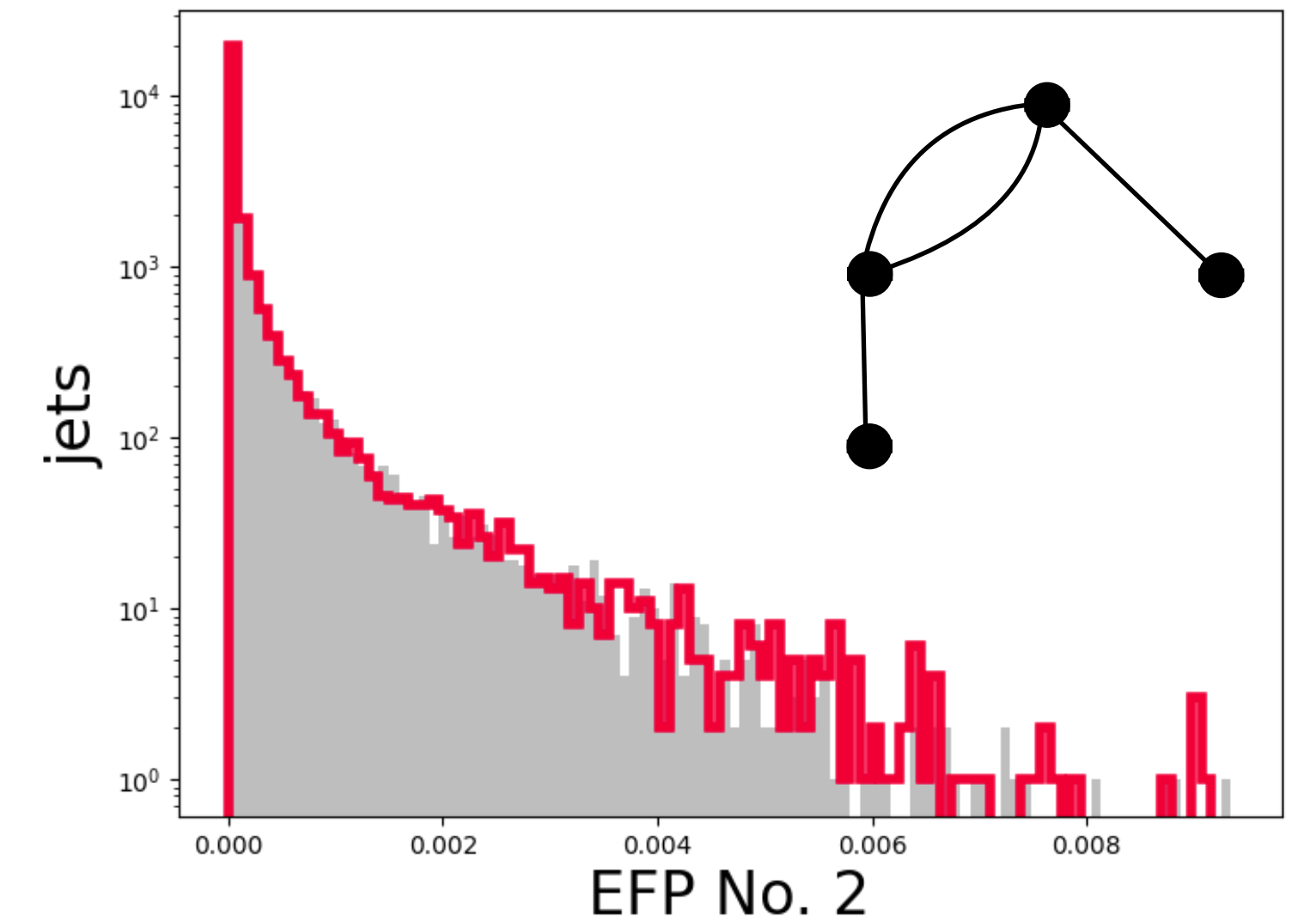
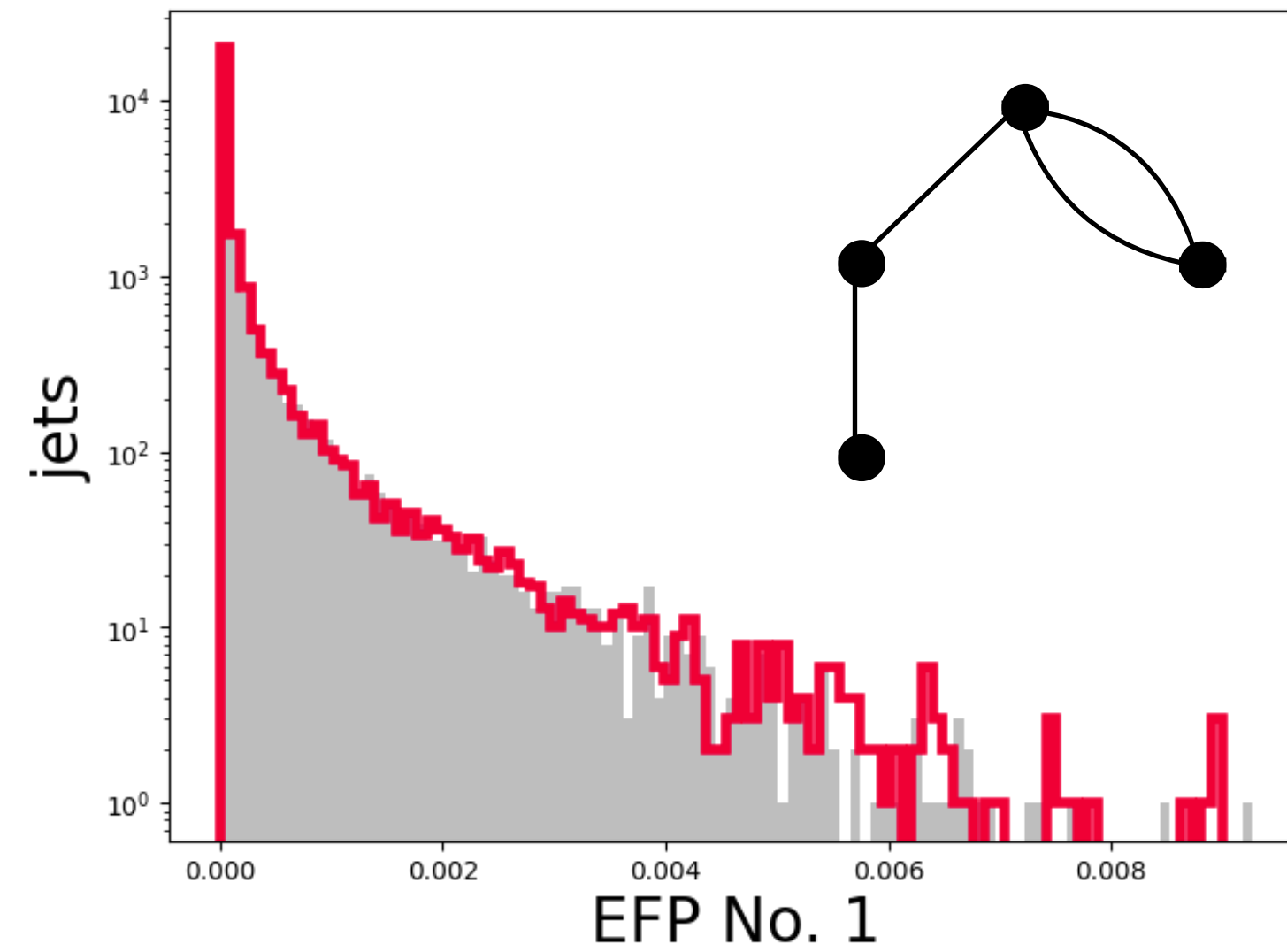
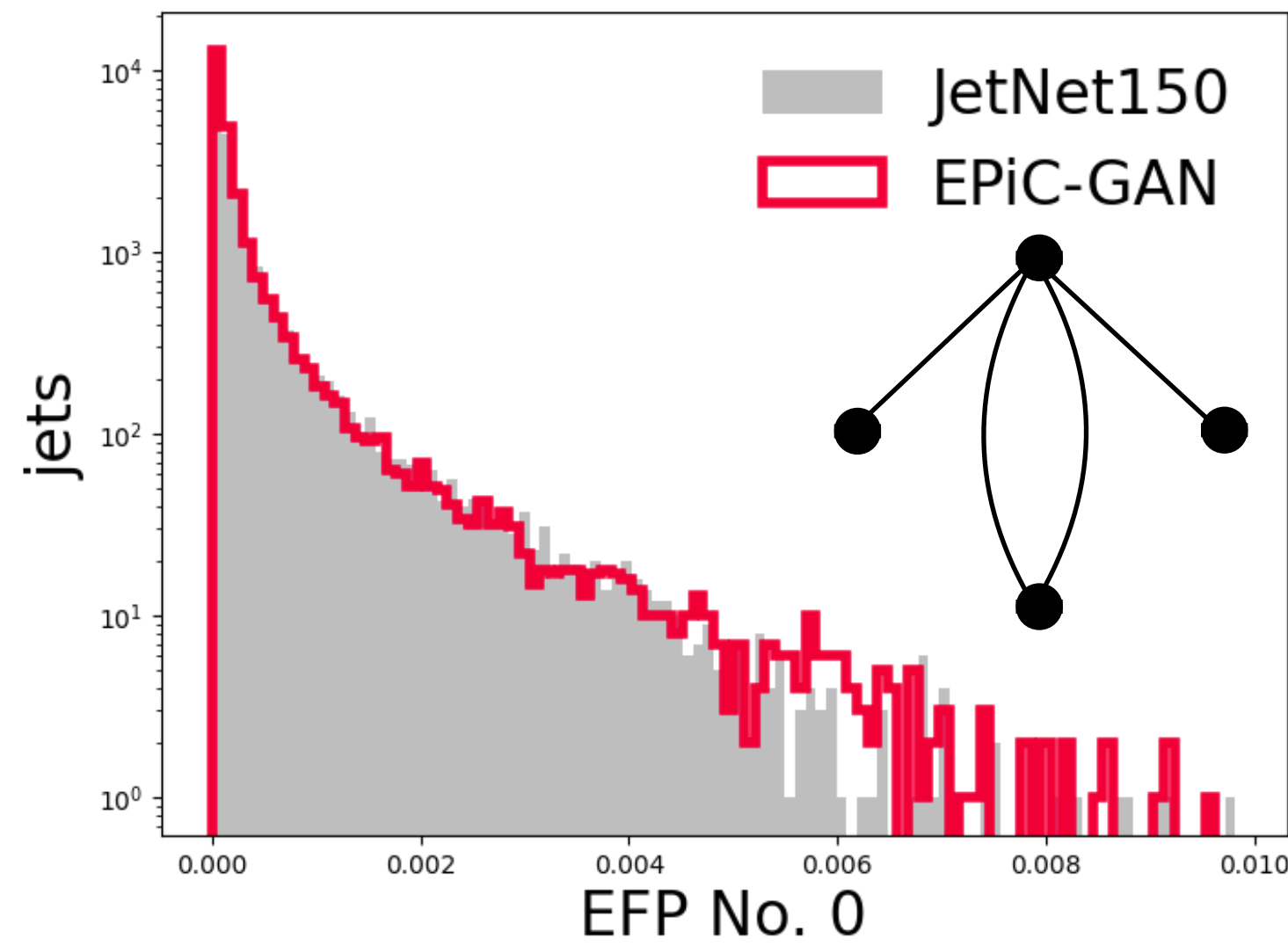
Timing & optimal batch size



Hardware constraints:

Intel Gold-5218 (64 CPUs @ 2.3 Ghz), 384GB RAM, Nvidia A100-40GB

Results: A few energy flow polynomials

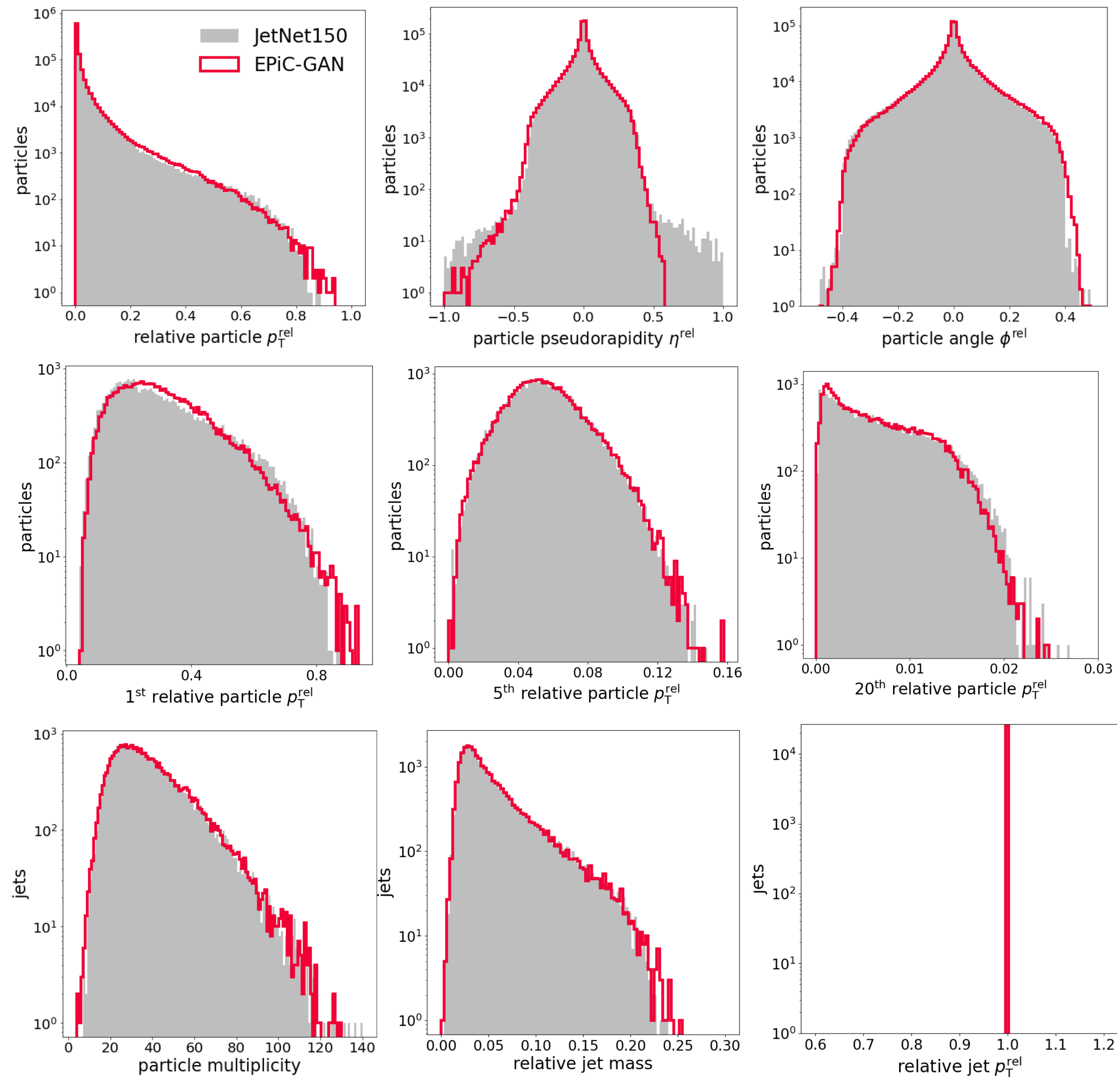


PT Komiske et al: Energy flow polynomials: A complete linear basis for jet substructure

Calibrated Results on JetNet150 quarks

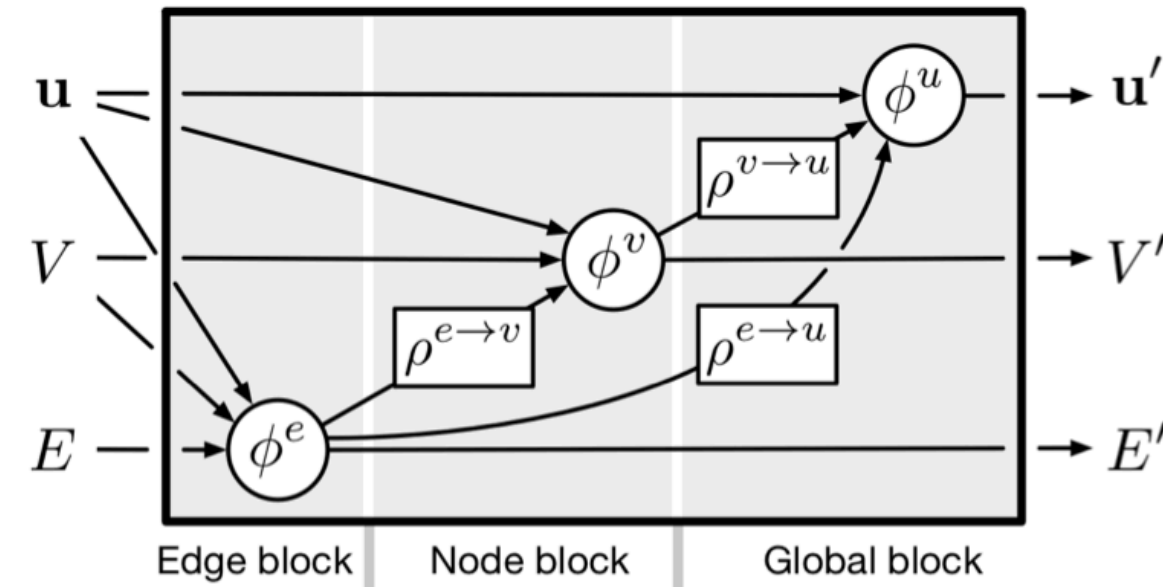
- EPiC-GAN setup:
 - $R = 4$ equivariant layers

- Generation calibrated
for relative jet $p_T = 1$

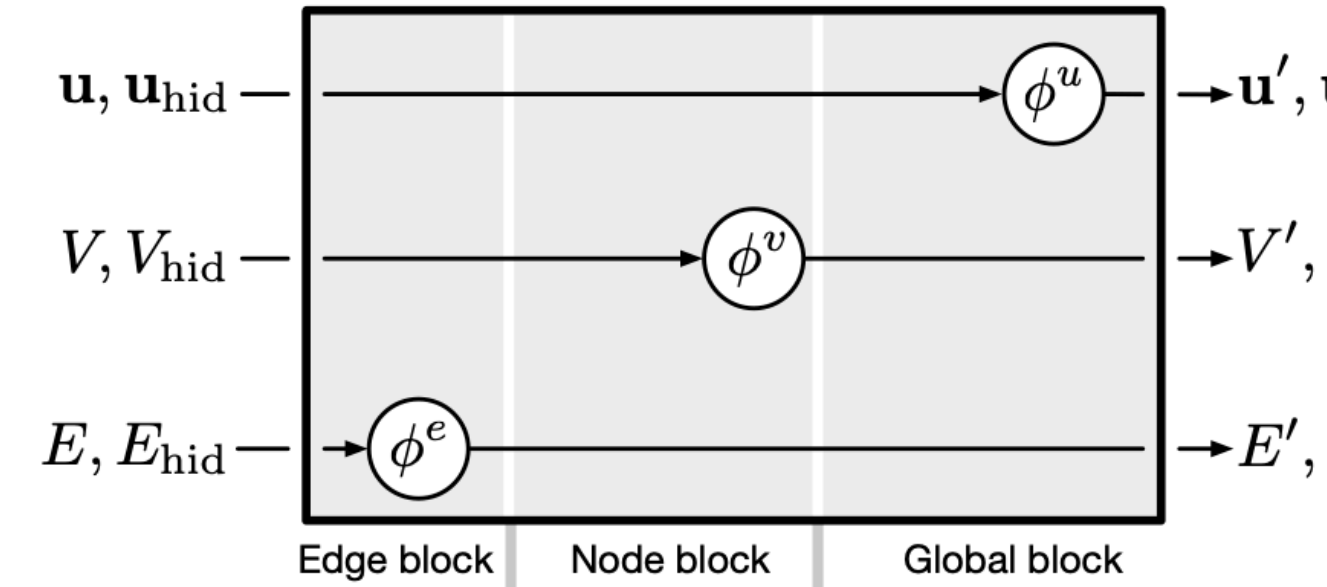


Graph Architectures

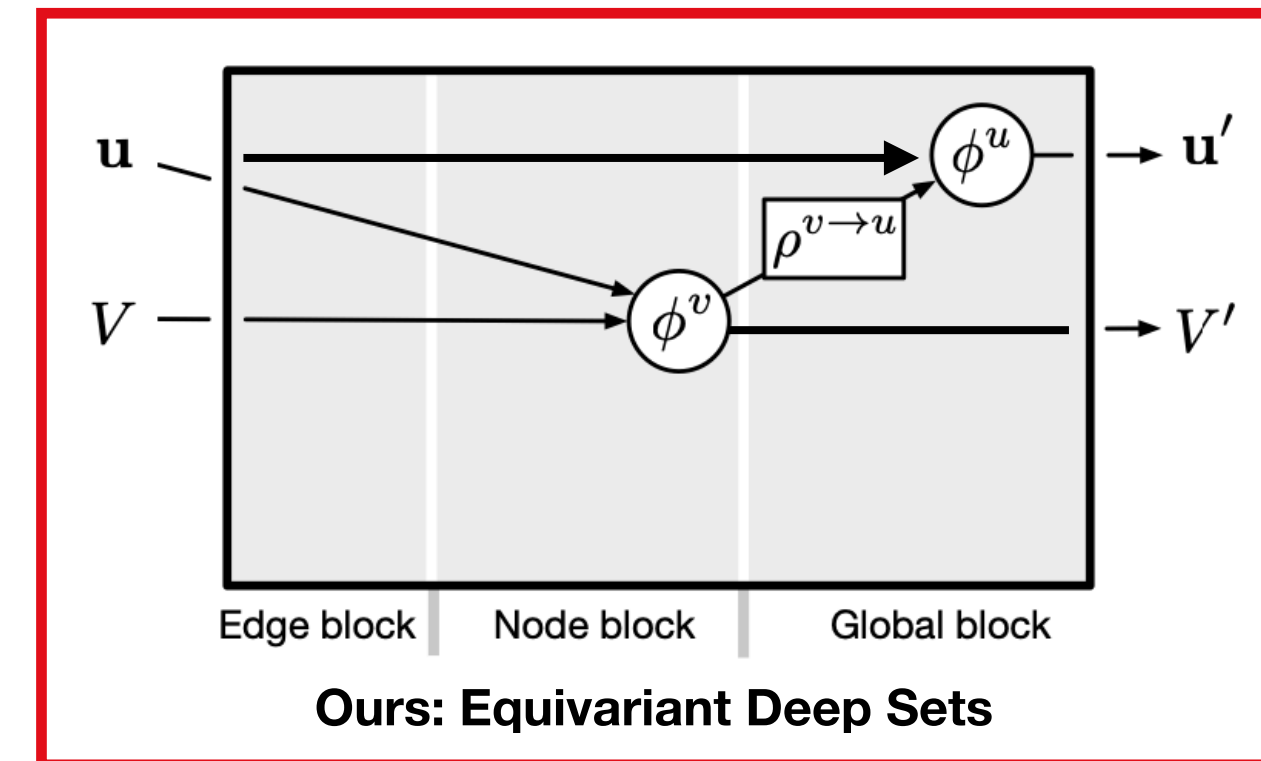
M Zaheer et al: Deep Sets



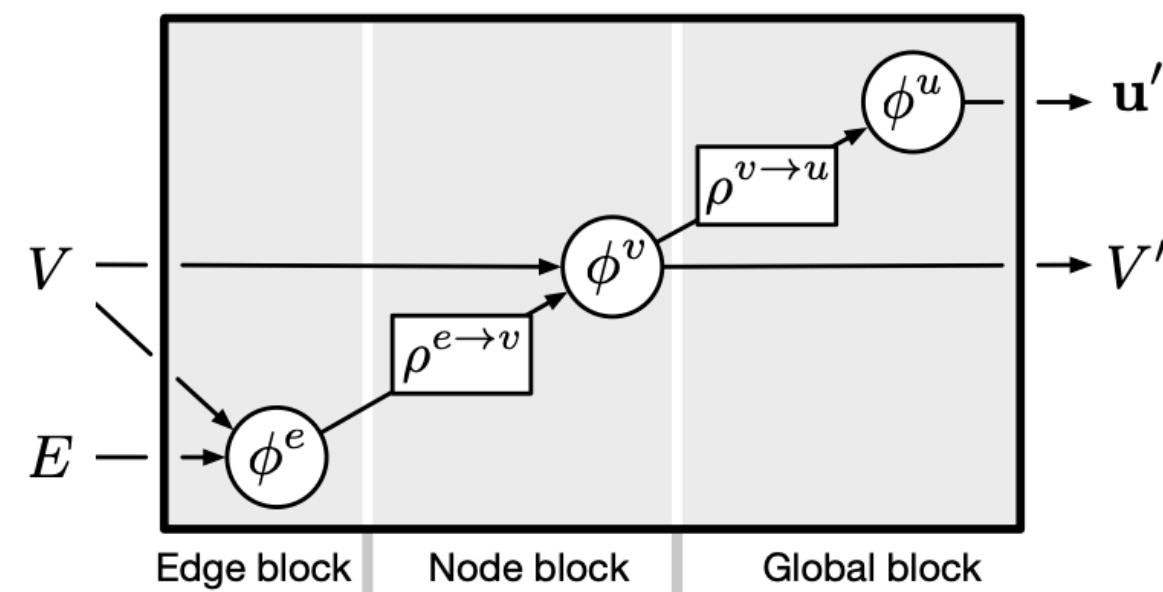
(a) Full GN block



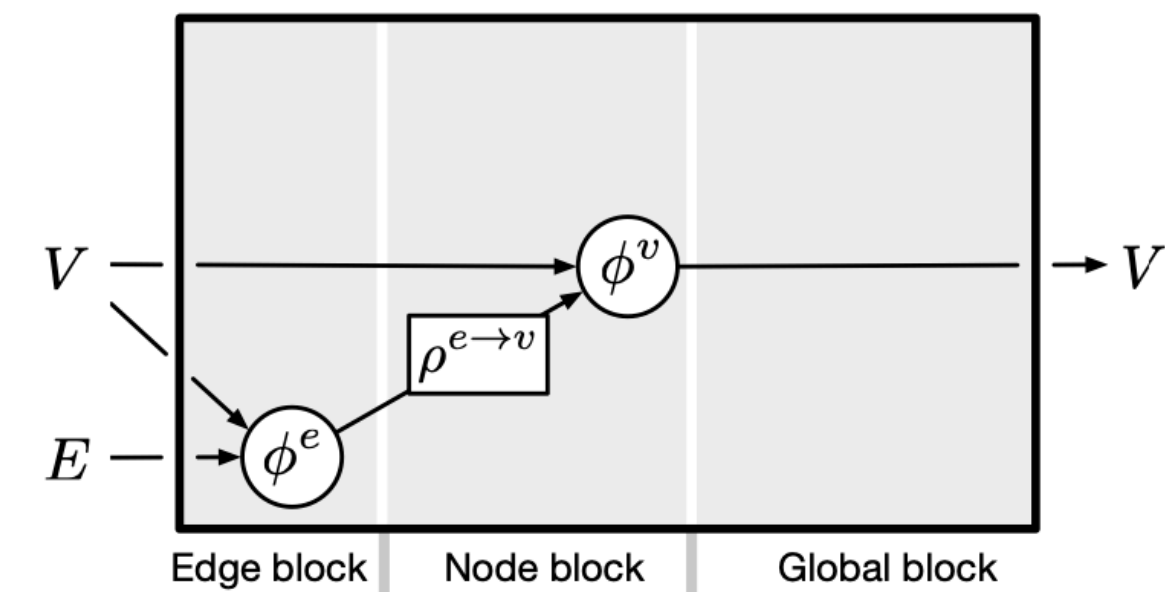
(b) Independent recurrent block



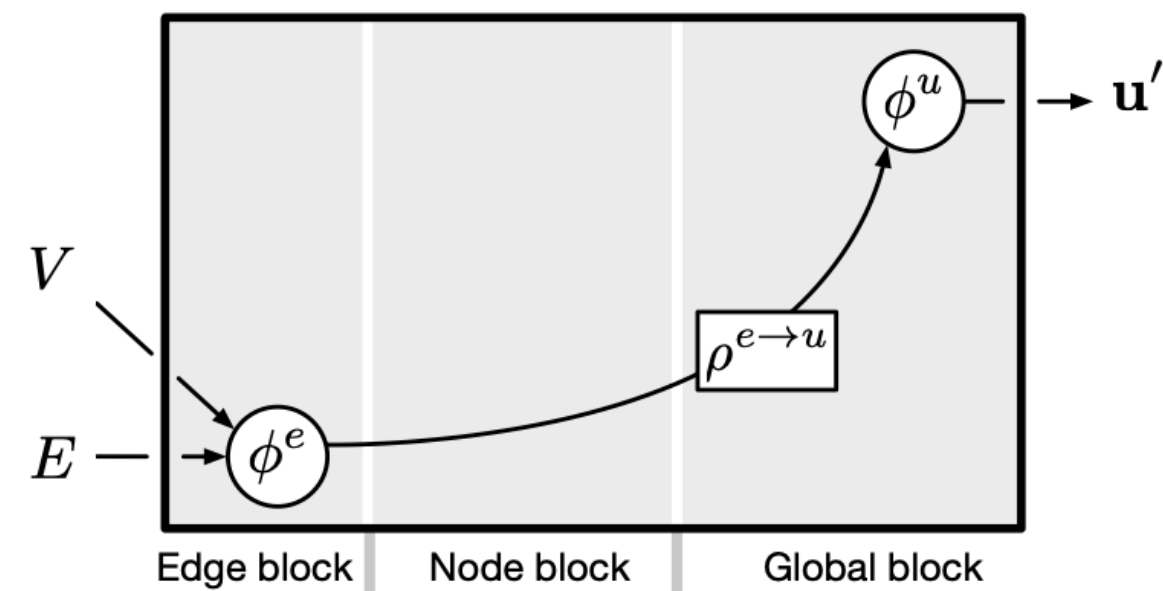
Ours: Equivariant Deep Sets



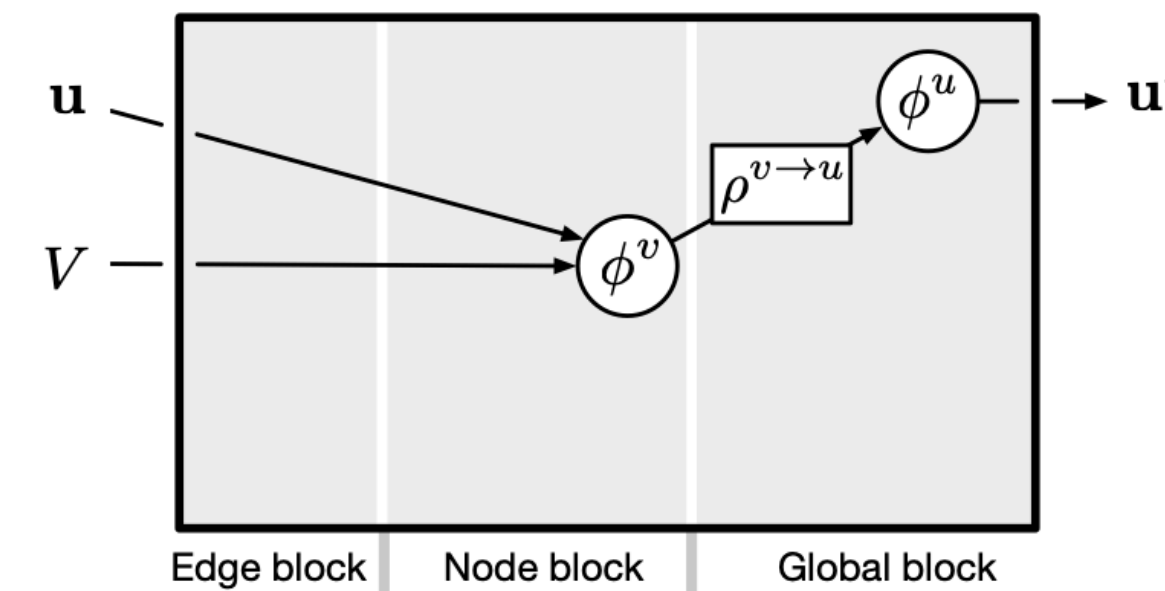
(c) Message-passing neural network



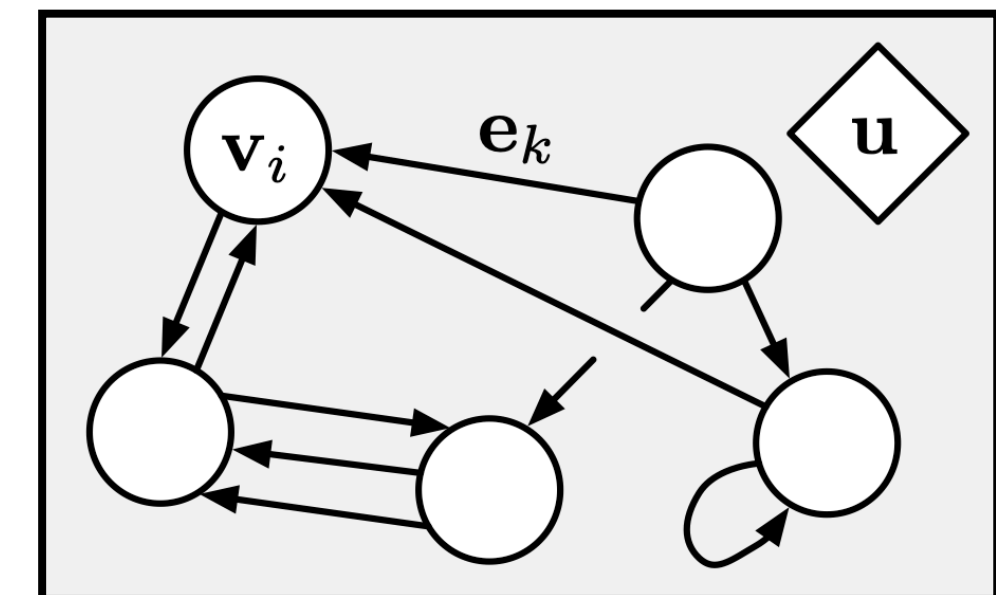
(d) Non-local neural network



(e) Relation network



(f) Deep set



Graph: $G = (u, V, E)$
 u : Global attribute
 V : Node's attributes v_i
 E : Edge's attributes e_i

PW Battaglia et al: Relational inductive biases, deep learning, and graph networks