
Jet Energy Resolution and Improvements

Ariel Schwartzman
SLAC, Stanford University

SLAC ATLAS Forum, 24-Jan-2007

Introduction (I)

Jet energy resolution has three main contributions:

$$\frac{\sigma(E)}{E} \sim \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$$

Given a particle-jet energy, what is the distribution of the jet energy measured in the calorimeter. Does not include the contribution of particles outside the cone at particle-level.

Resolution must be *measured* in the data, where there is no access to particle-jets: investigate data-driven techniques.

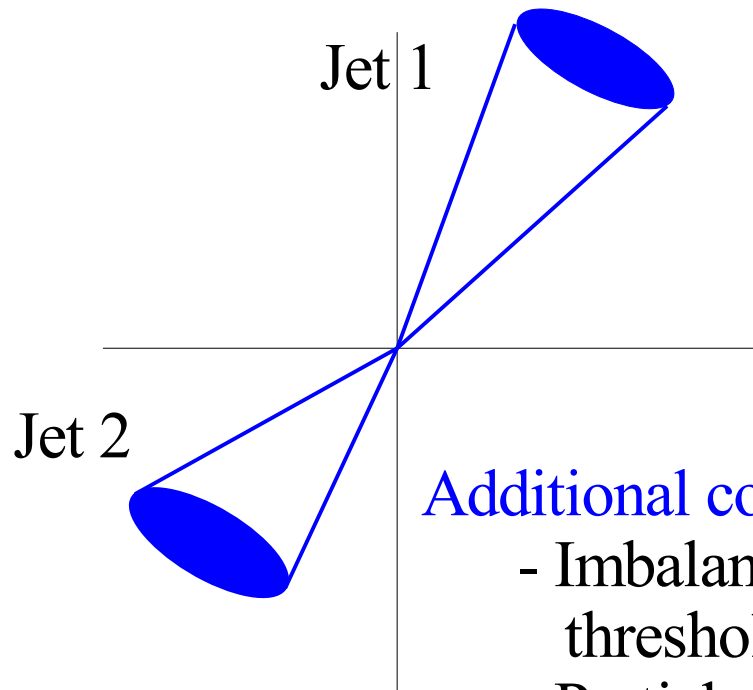
Jet resolution is crucial in many physics analysis and searches: investigate ways to *improve* it.

- **Stochastic response:**
Jet fragmentation
Sampling fluctuations,
EM fraction fluctuations per hadron.
- **Electronic noise term**
- **Constant term:**
Dead material, magnetic field,
calorimeter non-compensation.
- **Absolute jet energy scale:**
denominator in $\sigma(E)/E$.

Jet Energy Resolution (Dijet balance)

Determination of the jet E_T resolution based on energy conservation in the transverse plane.

- 1 primary vertex.
- 2 back-to-back leading jets ($\Delta\Phi < 2.8$)
- No other reconstructed jet with $E_T > 10$ GeV.
- Both jets in the *same* η region.



$$A = \frac{E_{T,1} - E_{T,2}}{E_{T,1} + E_{T,2}}$$

$$\sigma_A^2 = \left| \frac{\partial A}{\partial E_{T,1}} \right|^2 \sigma_{E_{T,1}}^2 + \left| \frac{\partial A}{\partial E_{T,2}} \right|^2 \sigma_{E_{T,2}}^2$$

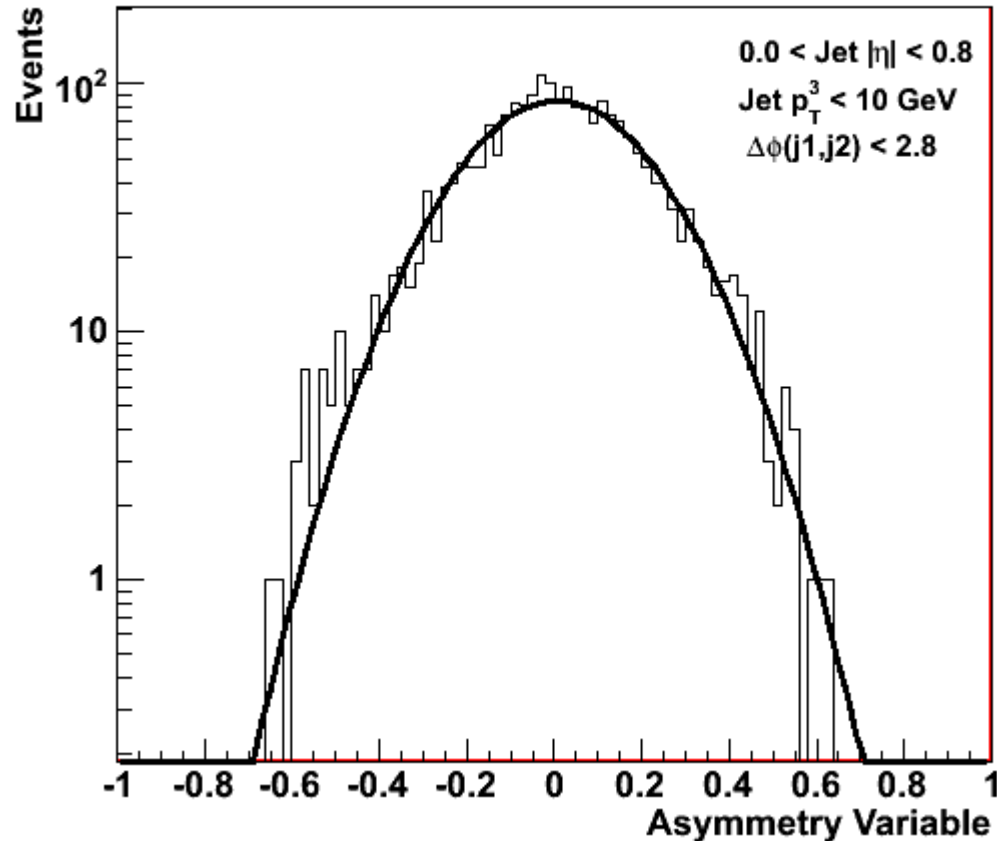
$$\left(\frac{\sigma_{E_T}}{E_T} \right) = \sqrt{2} \sigma_A$$

Additional corrections:

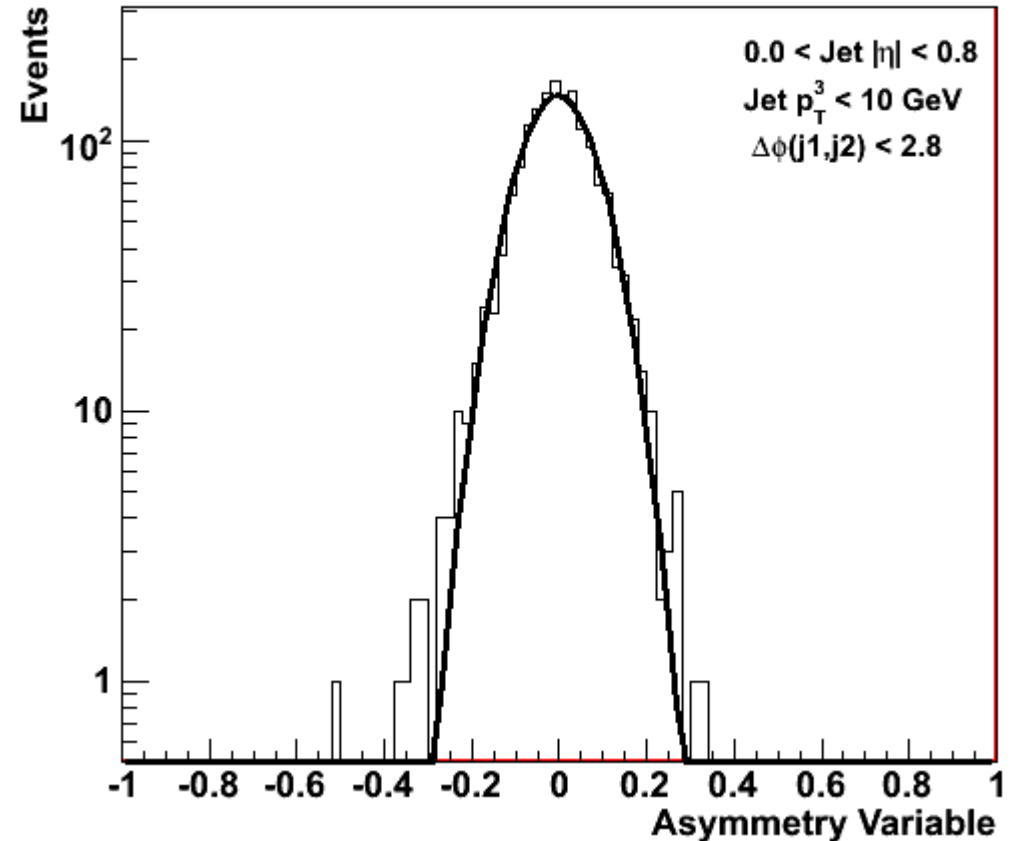
- Imbalance due to additional jets below the 10 GeV threshold and soft radiation in the event.
- Particle jet imbalance contribution.

Dijet balance: Asymmetry Distributions

25 GeV < Jet p_T < 40 GeV



80 GeV < Jet p_T < 100 GeV

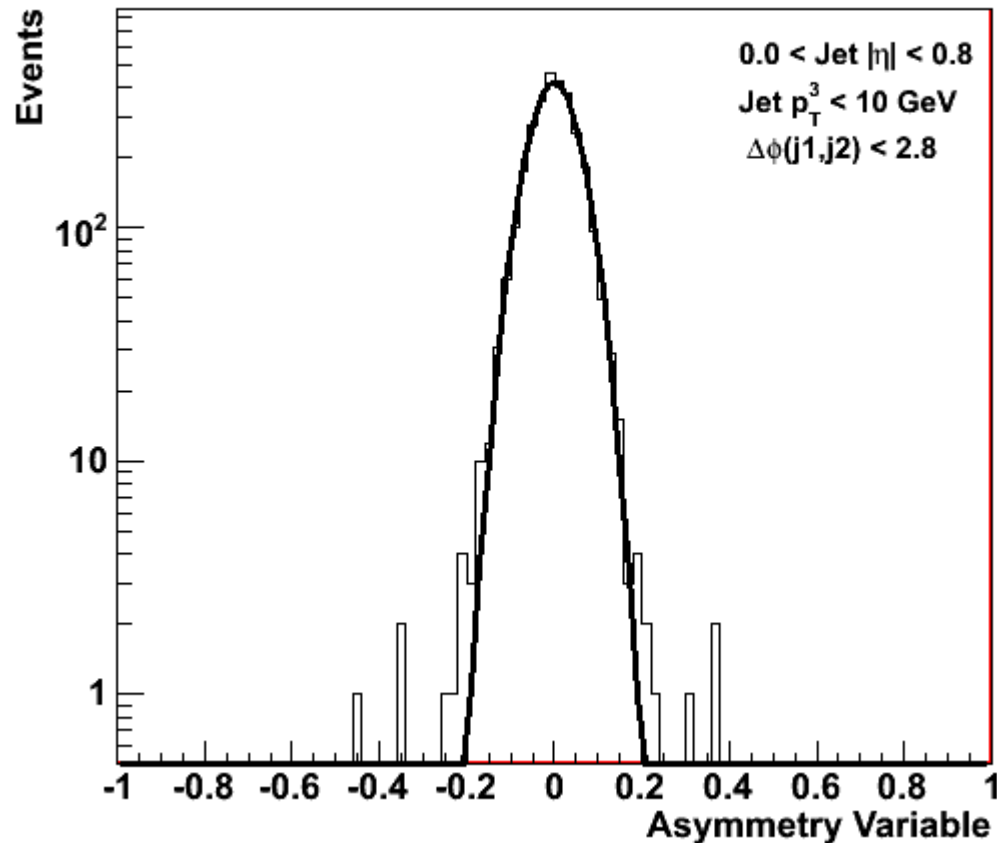


Data sample divided in 4 p_T regions, and 4 eta regions.

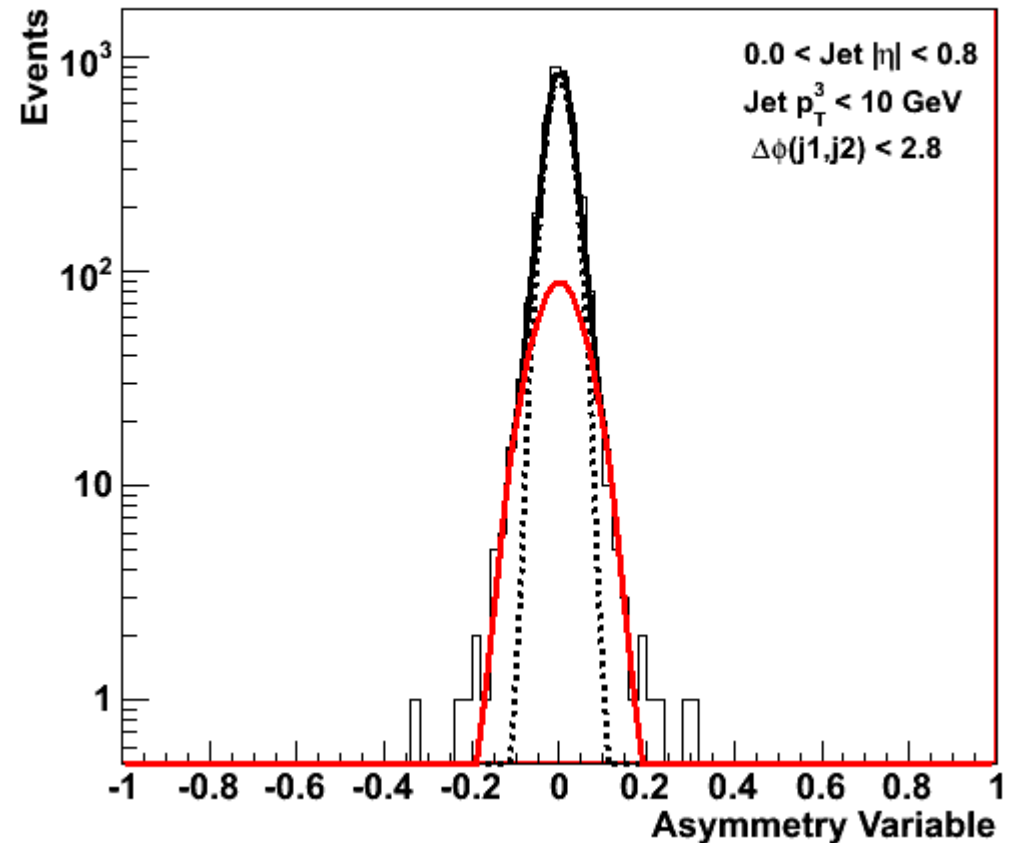
Asymmetry variables fitted with single Gaussians.

Dijet balance: Asymmetry Distributions

160 GeV < Jet p_T < 200 GeV

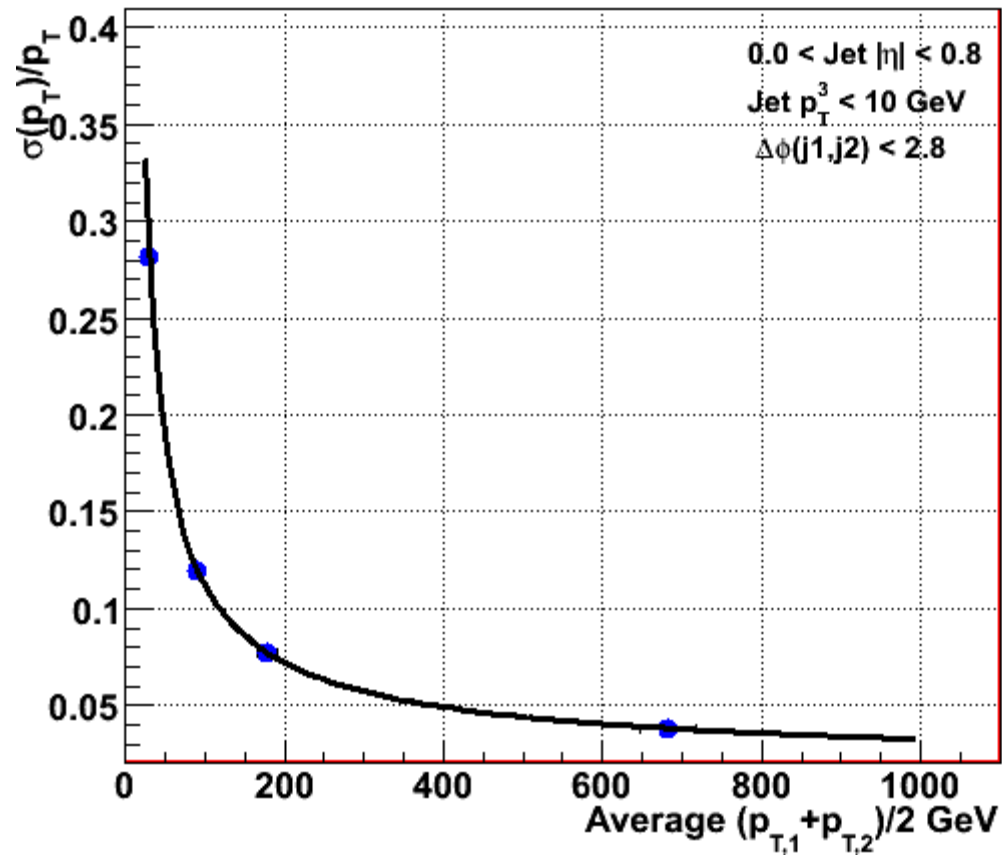


630 GeV < Jet p_T < 750 GeV



Non Gaussian tails in the highest p_T bin.

Dijet balance Resolution ($\text{Eta} < 0.8$)

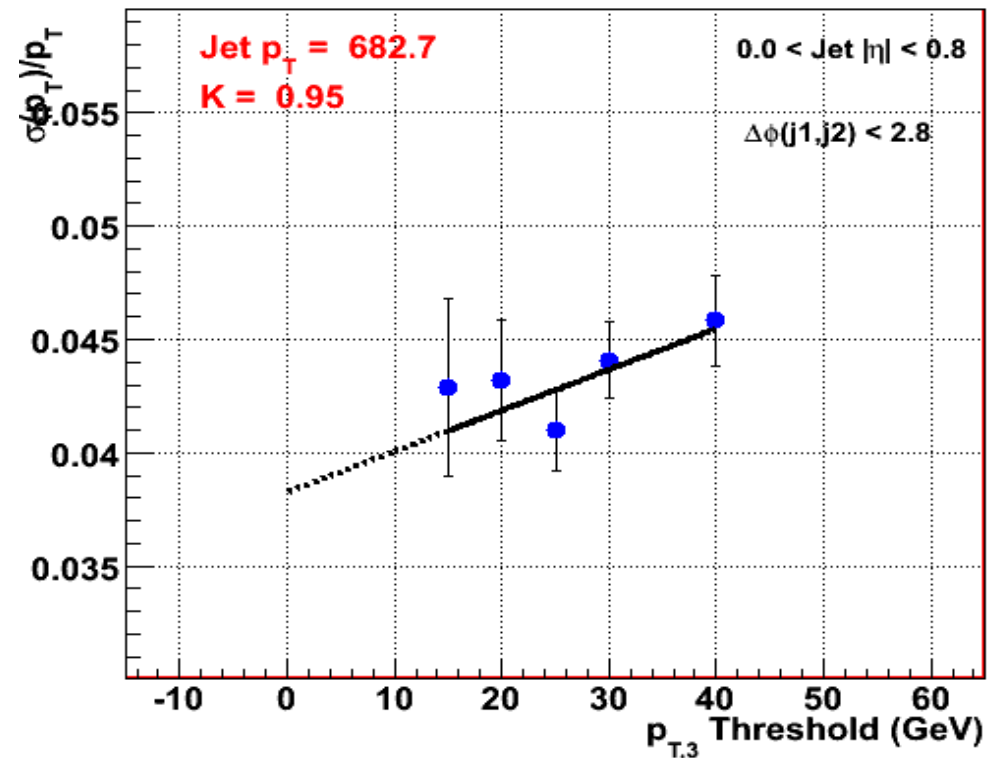
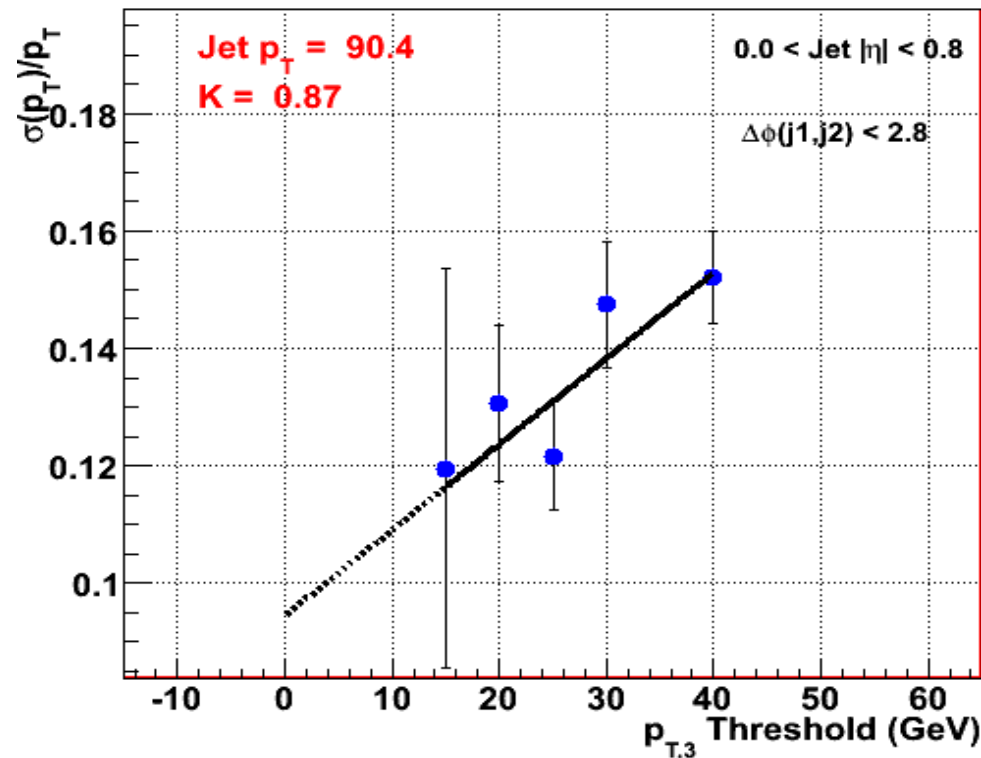


$$\frac{\sigma p_T}{p_T} = \frac{0.86}{\sqrt{p_T}} \oplus \frac{7.08}{p_T} \oplus 0.017$$

Soft Radiation Correction (I)

Events with soft radiation prevent the two leading jets from balancing in the transverse plane.

Compute resolutions in samples with different third jet cuts: 15,20,25,30,40 GeV
Extrapolate to $p_T=0$ (ideal Dijet sample)



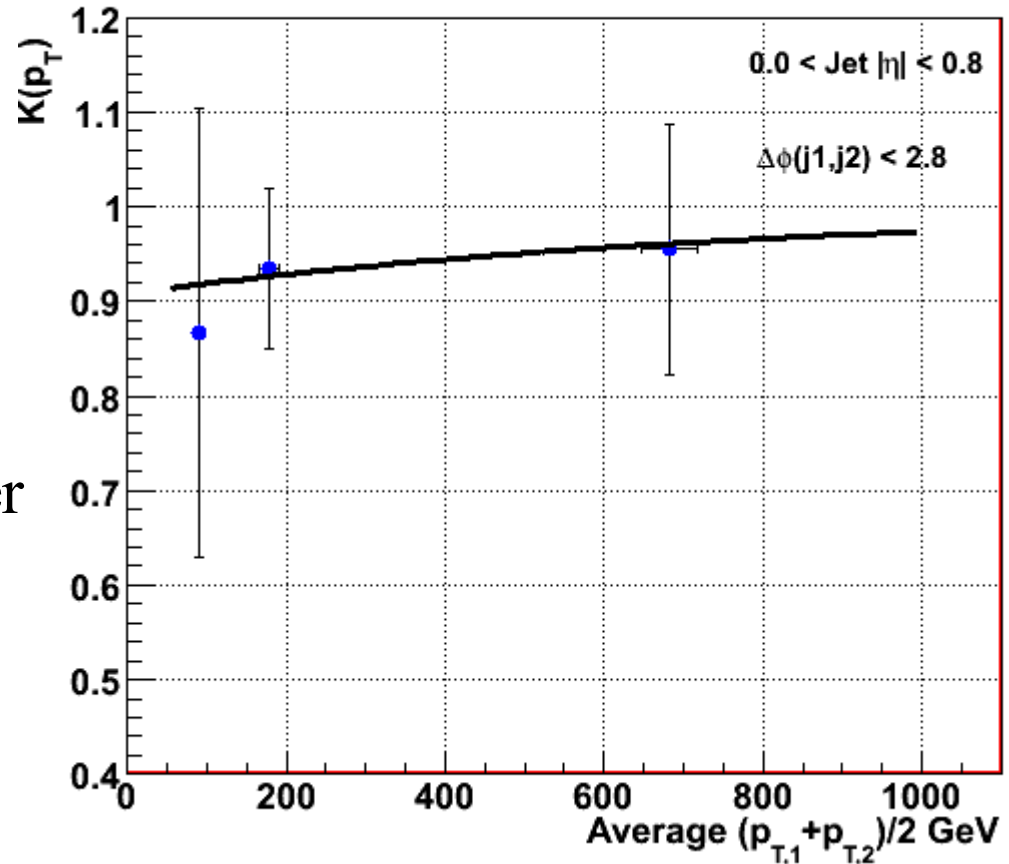
Soft Radiation Correction (II)

$$K(P_T) = \left(\frac{\sigma p_T}{p_T} \right)^{th=0 GeV} / \left(\frac{\sigma p_T}{p_T} \right)^{th=10 GeV}$$

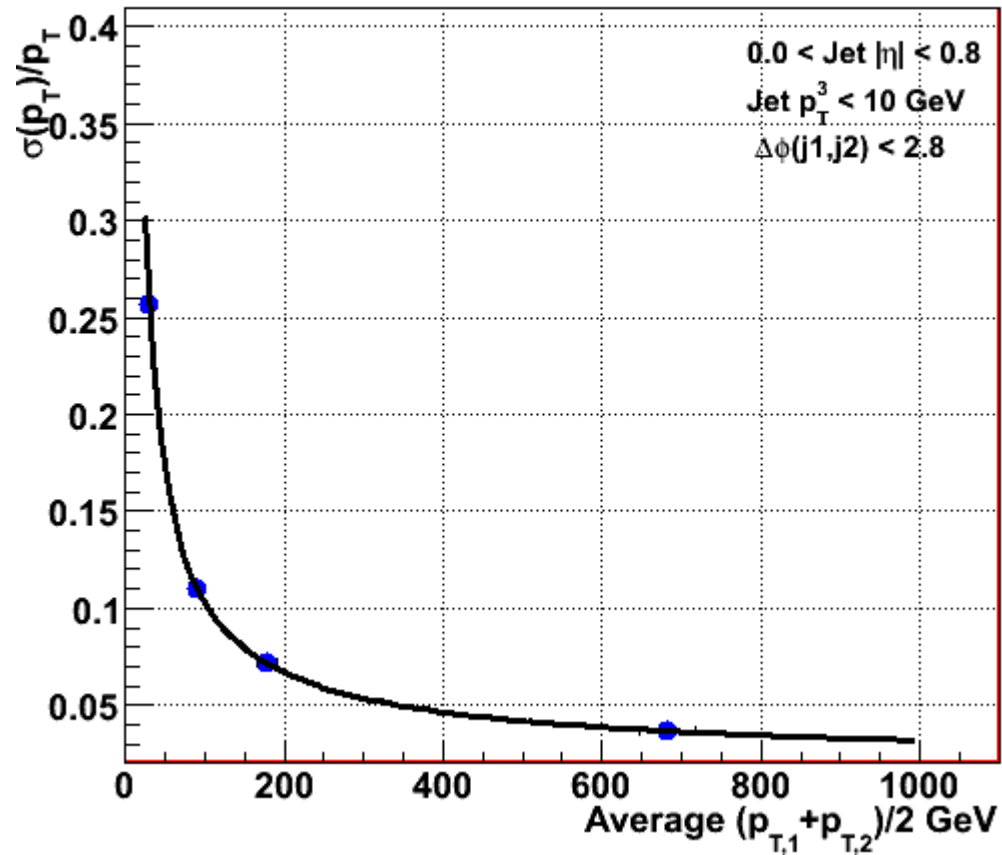
$$\left(\frac{\sigma p_T}{p_T} \right)^{th=10 GeV} = K \times \left(\frac{\sigma p_T}{p_T} \right)^{th=0 GeV}$$

Soft radiation bias should be larger at small transverse energies, and negligible at high p_T :

$$K(P_T) = 1 - \exp^{-a - b p_T}$$



Resolution after Soft Radiation Correction



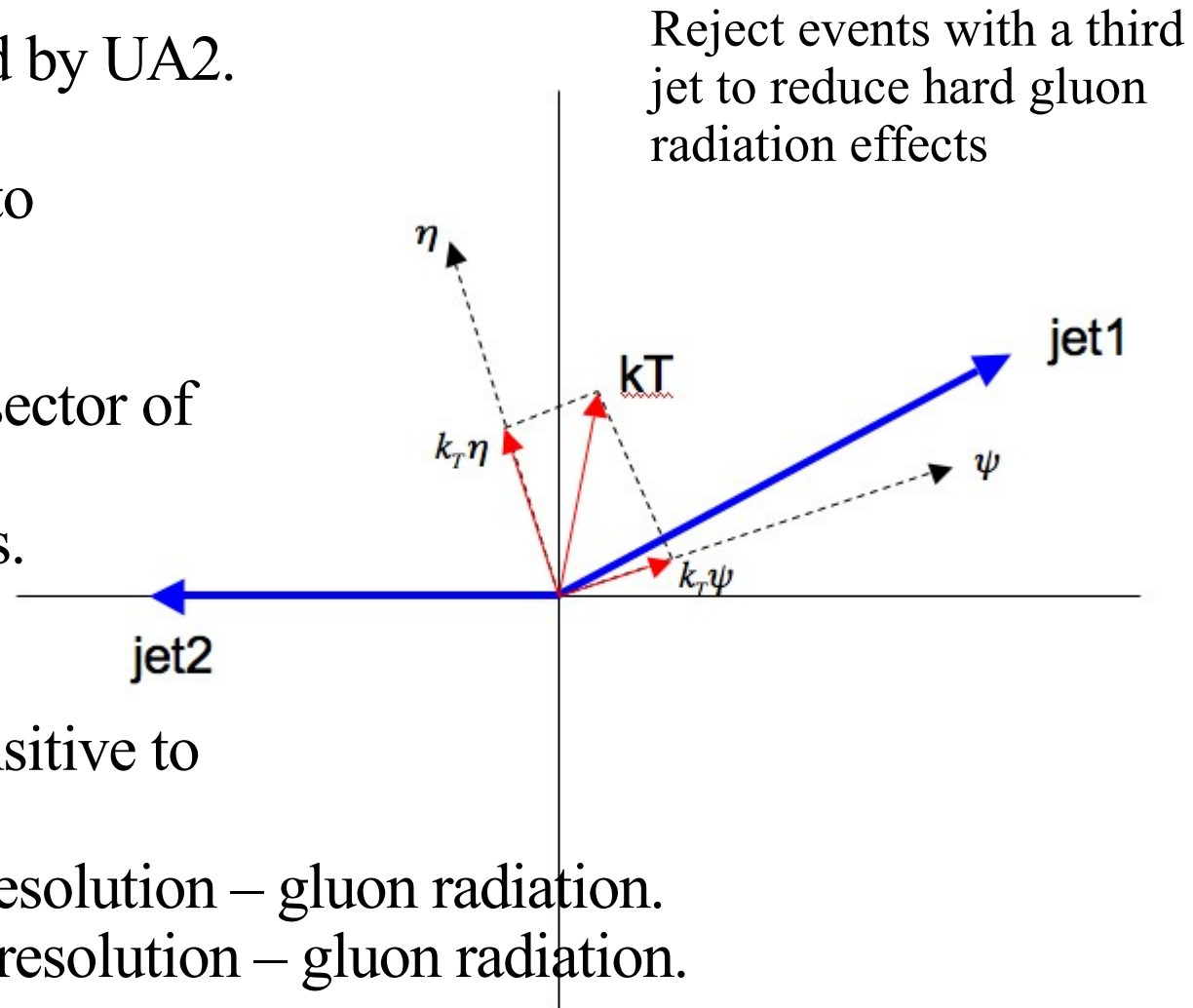
$$\frac{\sigma p_T}{p_T} = \frac{0.79}{\sqrt{p_T}} \oplus \frac{6.41}{p_T} \oplus 0.019$$

Kt Balance Technique

Method used in CDF, developed by UA2.

Project Imbalance vector k_T onto
2 components (ψ , η)

- Eta axis: azimuthal angular bisector of the dijet system.
- Psi axis: orthogonal to Eta axis.



ψ , and η components are sensitive to different effects:

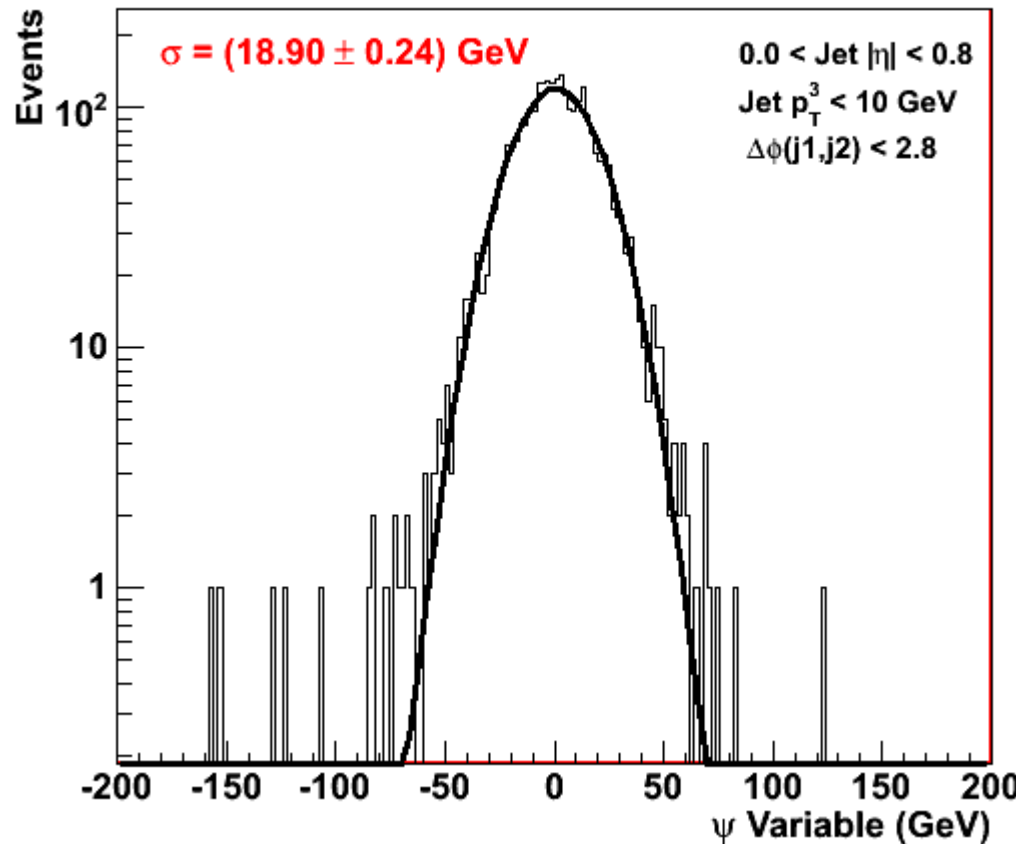
ψ distribution: jet energy resolution – gluon radiation.

η distribution: jet angular resolution – gluon radiation.

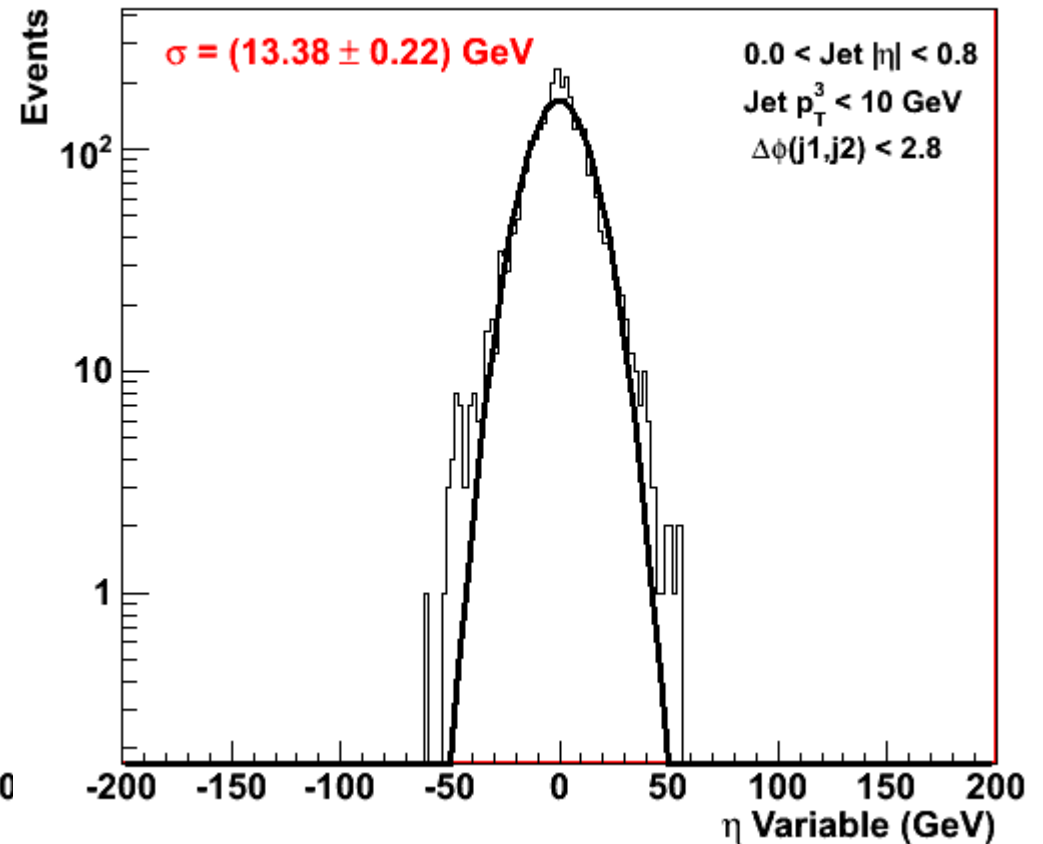
Remove soft radiation contribution by subtracting in quadrature $\sigma(\eta)$ from $\sigma(\psi)$

Distributions of the 2 kT Components

160 GeV < Jet p_T < 200 GeV



160 GeV < Jet p_T < 200 GeV

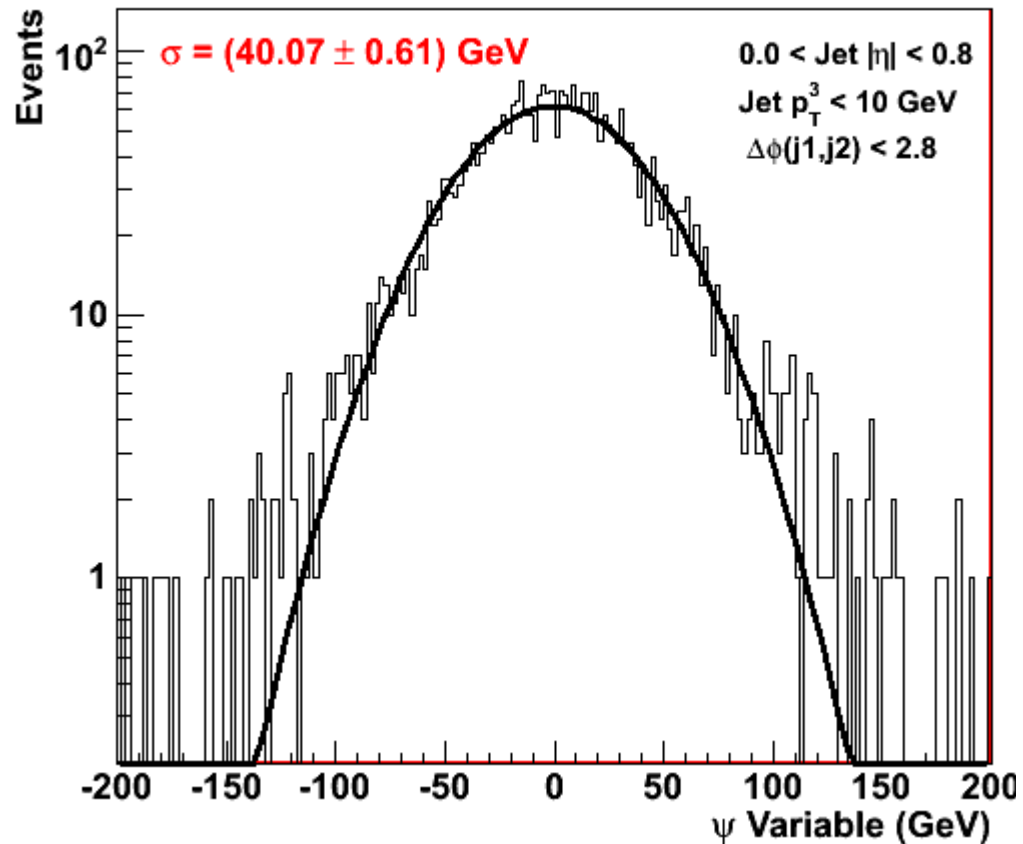


Data sample divided in 4 p_T regions, and 4 eta regions.

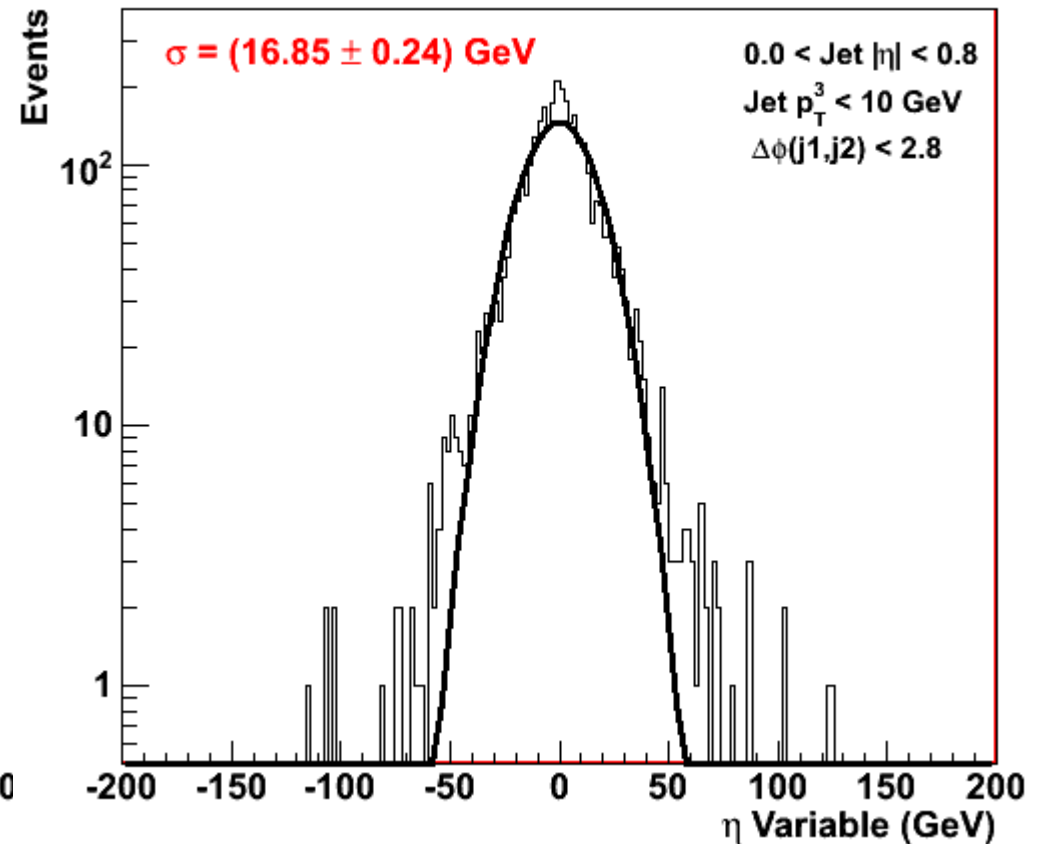
Psi and Eta variables fitted with single Gaussians.

Distributions of the 2 kT Components

630 GeV < Jet p_T < 750 GeV

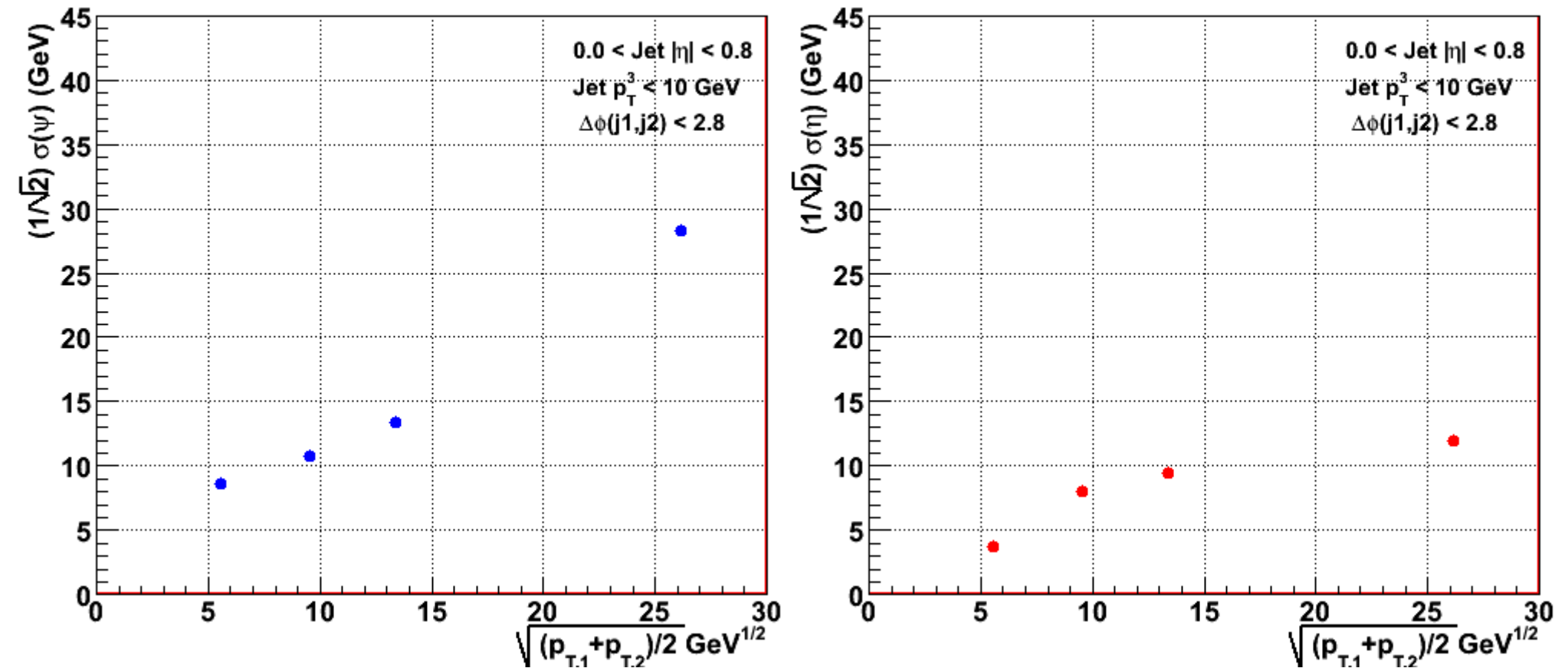


630 GeV < Jet p_T < 750 GeV



Eta resolution has weaker dependence with energy, as expected.

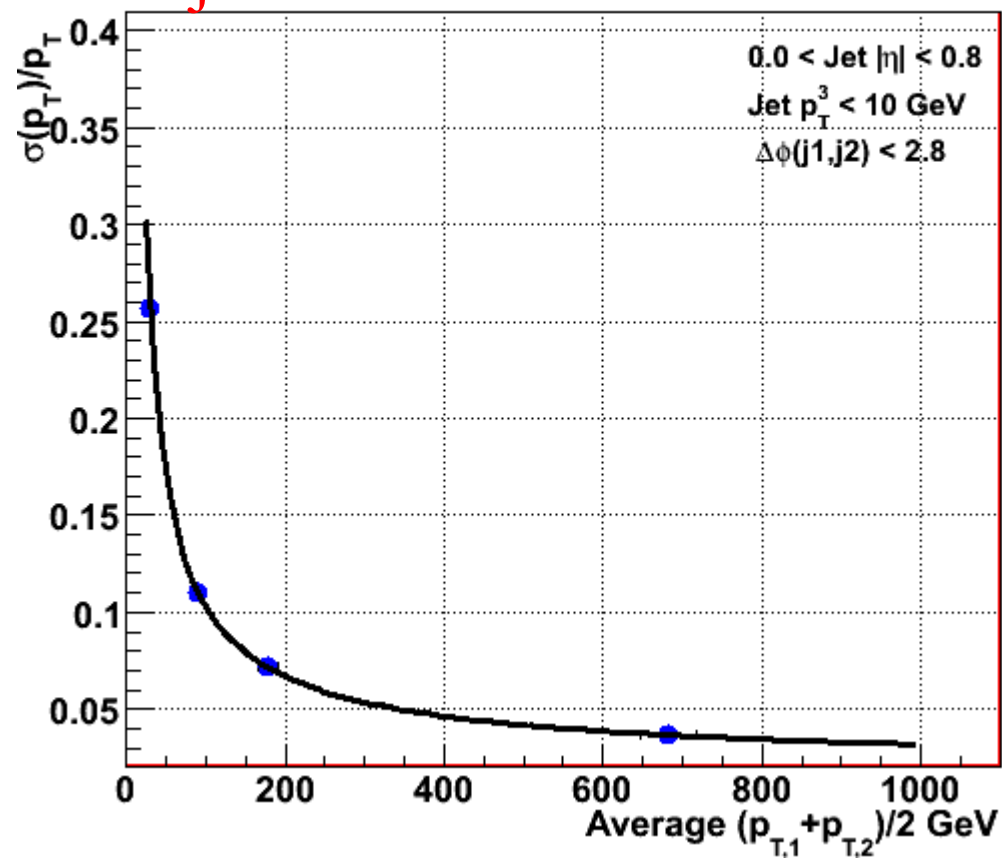
Resolution of the 2 kT components



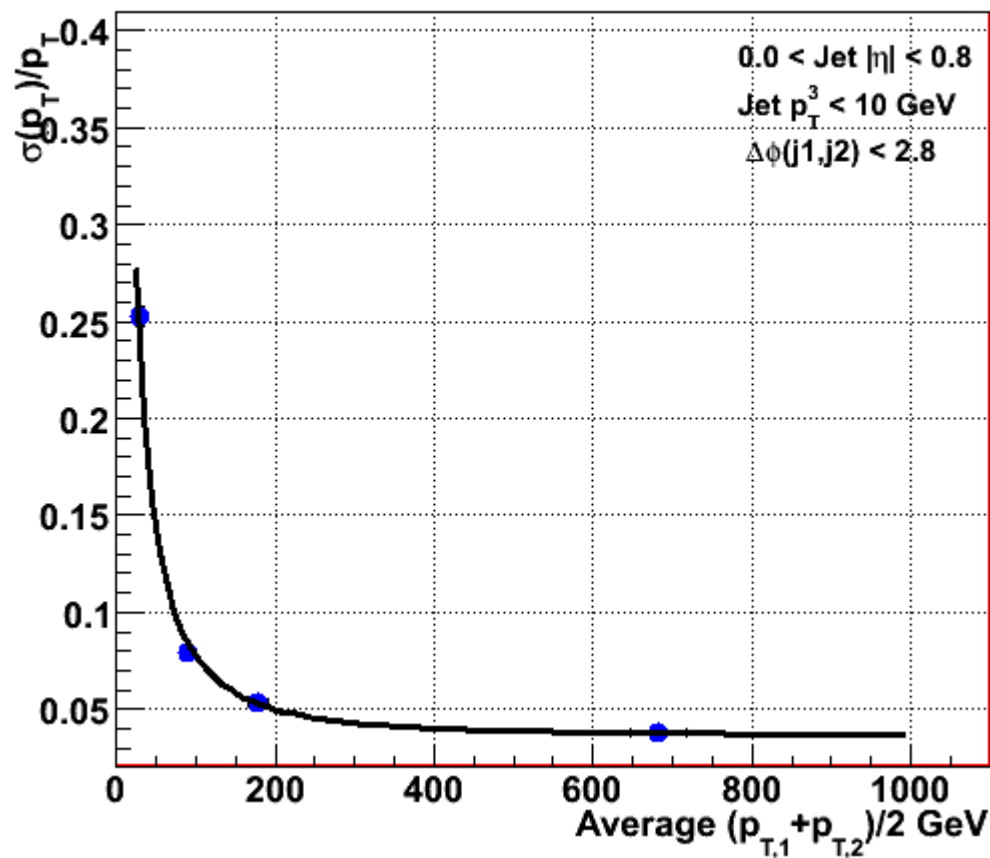
Width of Psi component has an approximately linear dependence with $\sqrt{p_T}$
Width of Eta component is more flat, specially at high p_T .

Comparison of Dijet and Kt Balance Methods

Dijet balance



kT

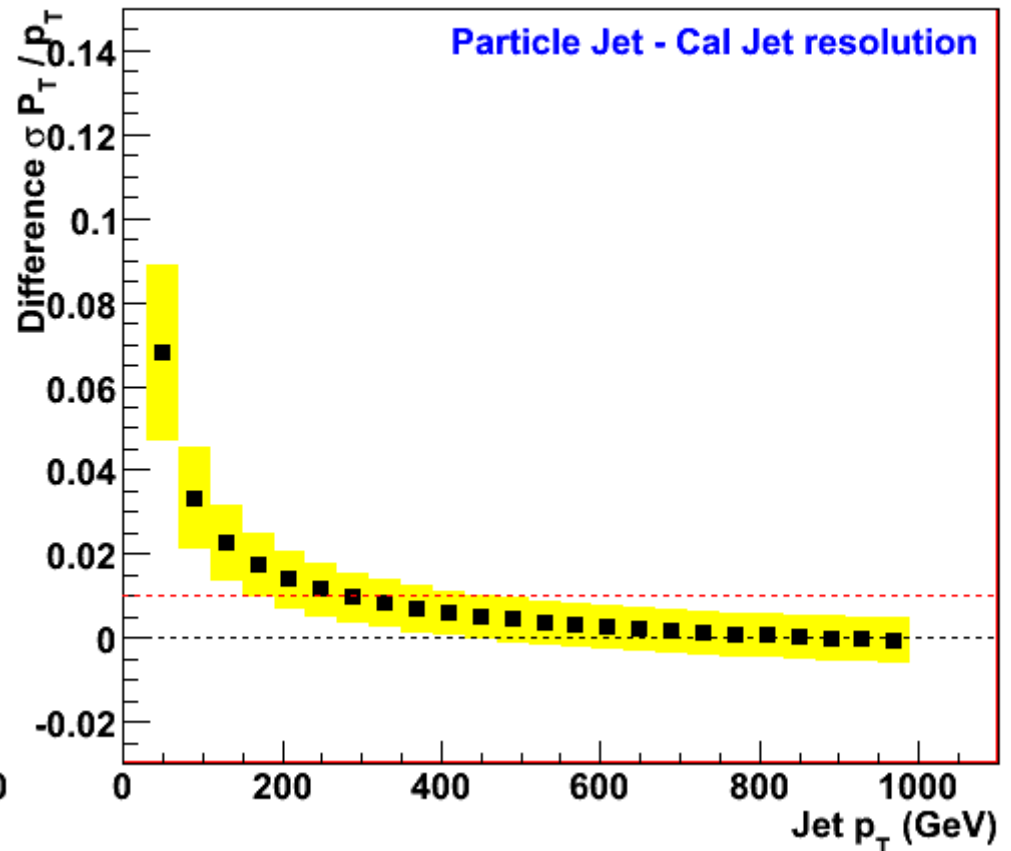
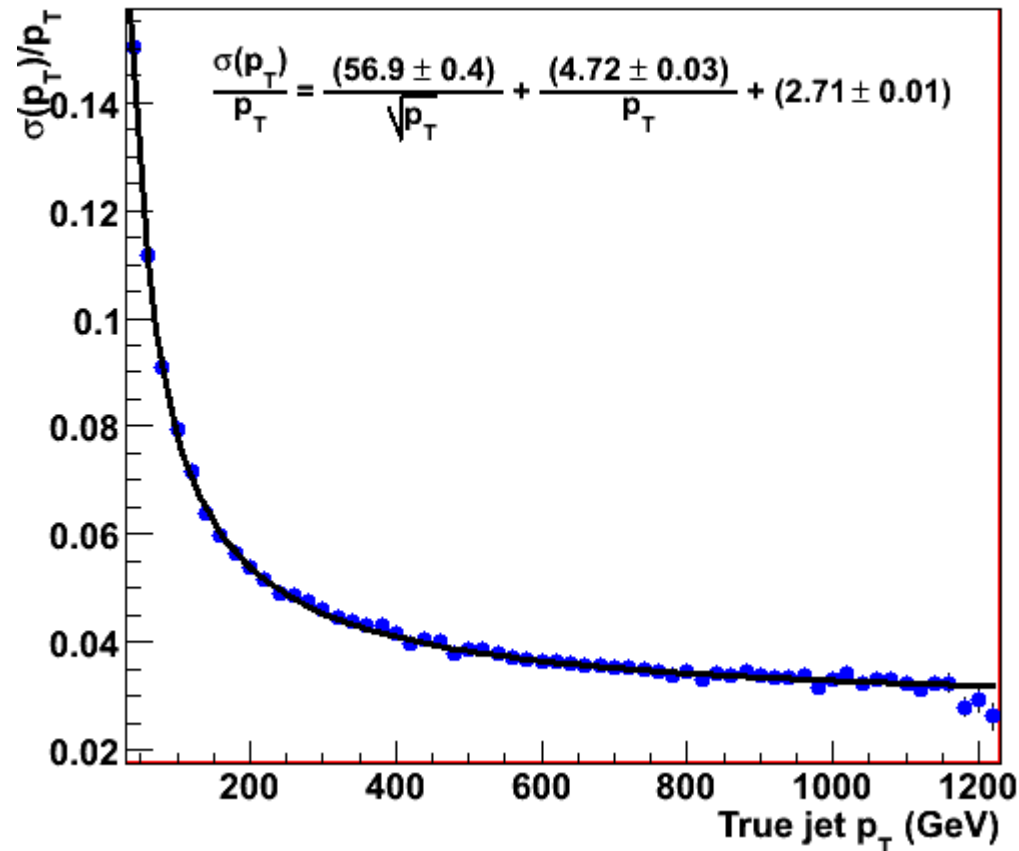


Very preliminary.

Kt technique gives smaller resolution at low p_T .

Monte Carlo Closure Test

$0.0 < |\eta| < 0.8$



Compare calorimeter jets with particle jets (straight resolution)

$\Delta R(\text{jet}, \text{particle}) < 0.1$

Within 1% for $p_T > 200$ GeV. Large discrepancies at low p_T .

Improving Jet Resolution using Tracks

Tracking provides an independent measurement of energy that can be used to improve the energy resolution.

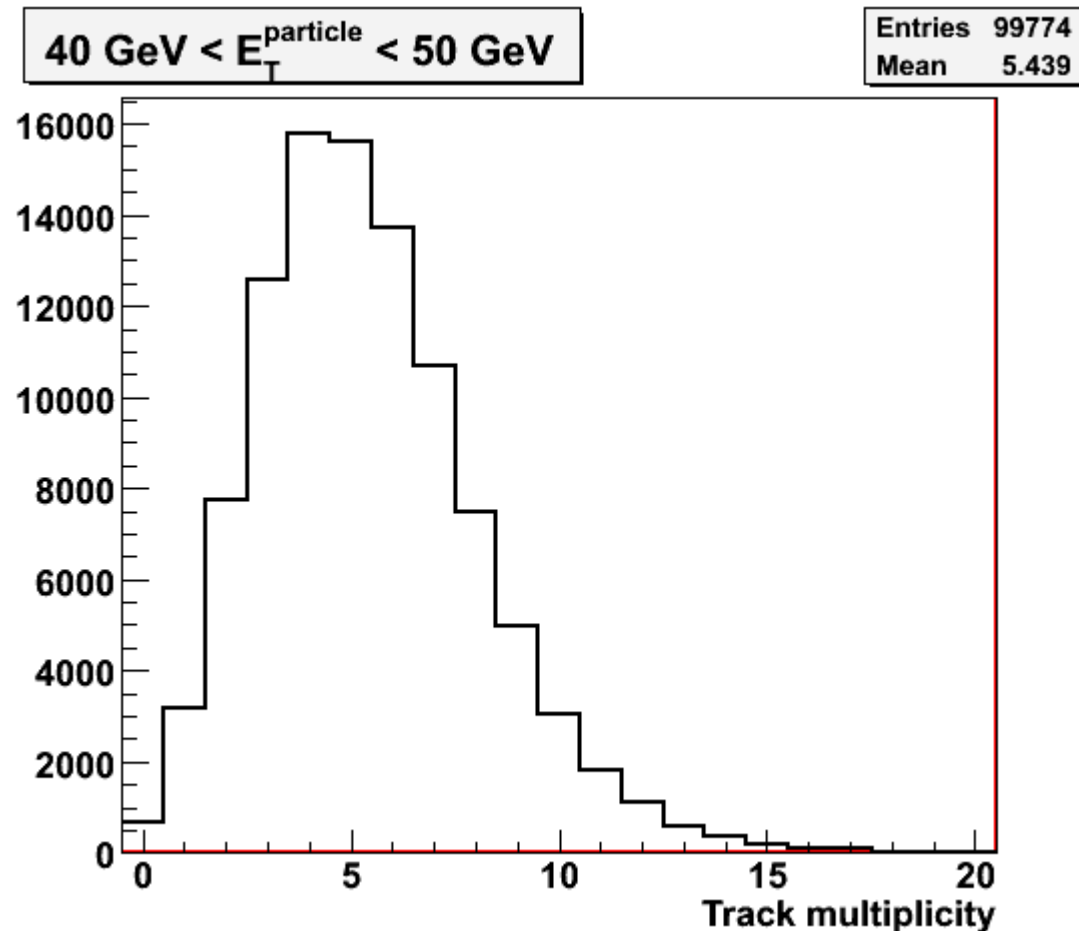
Match Cone 0.4 calorimeter jets with reconstructed tracks:

$$\begin{aligned} \Delta R(PV) &< 0.4 \\ p_T &> 0.5 \text{ GeV} \end{aligned}$$

Consider the fraction of charged transverse momentum in jets:

$$f_{trk} = \frac{E_T^{trk}}{E_T^{cal}}$$

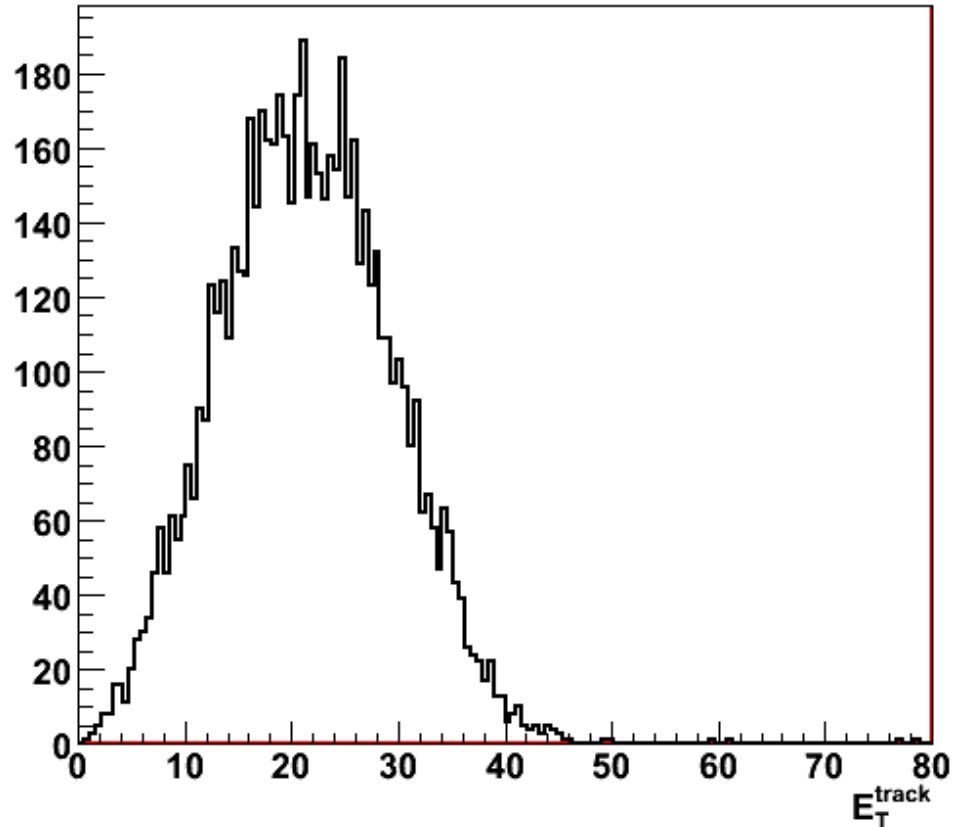
Look at the energy scale of cal-jets as a function of the charged particle composition, and “correct” for differences in scale.



Track Distributions in Jets

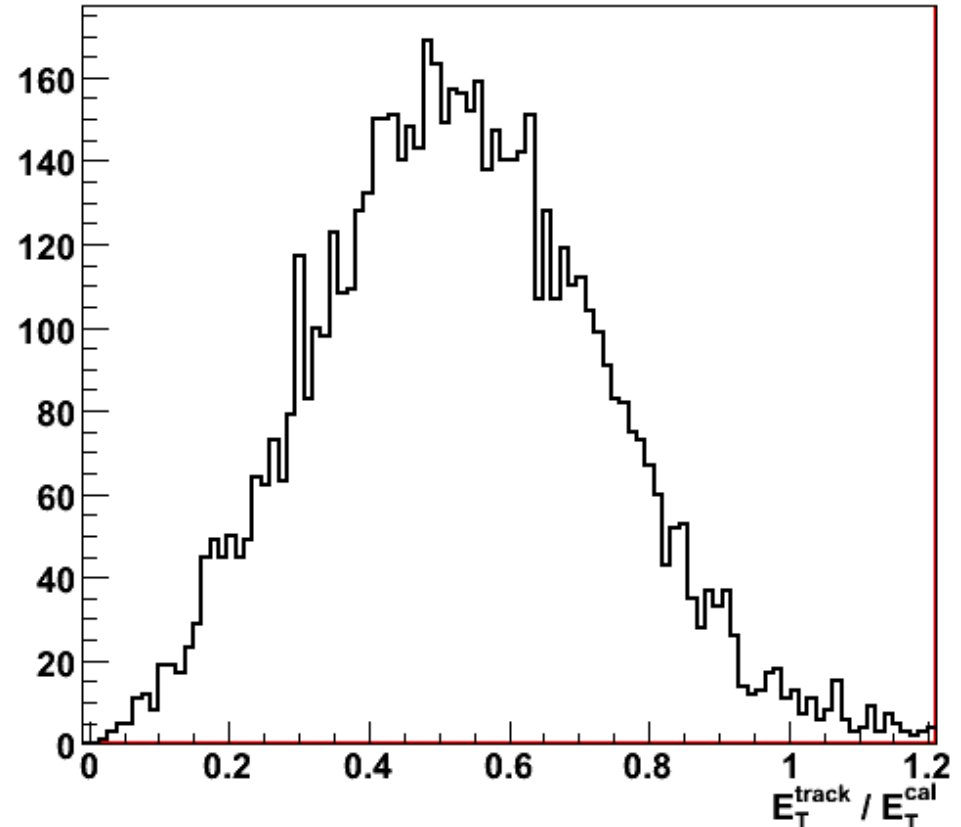
40 GeV < E_T^{particle} < 50 GeV

Entries 6595
Mean 21.46



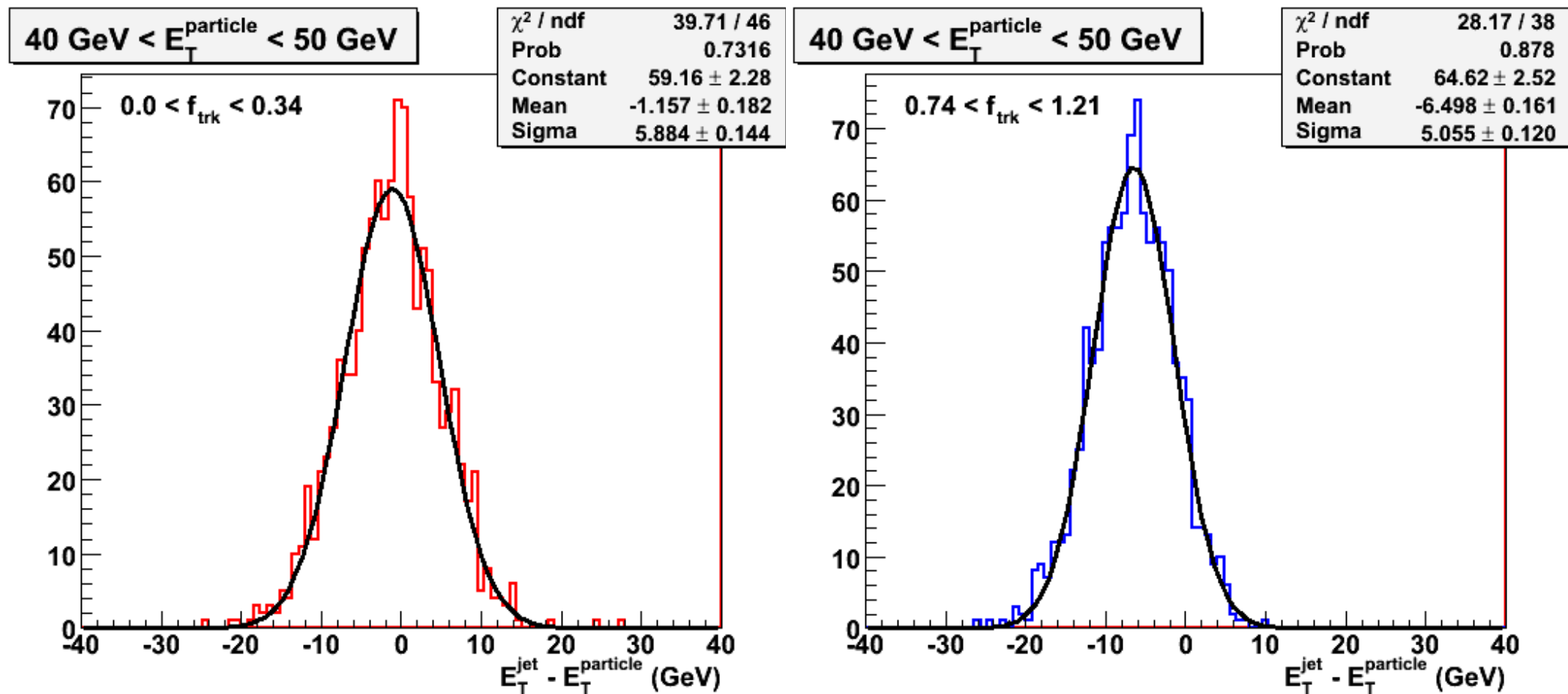
40 GeV < E_T^{particle} < 50 GeV

Entries 6595
Mean 0.5341



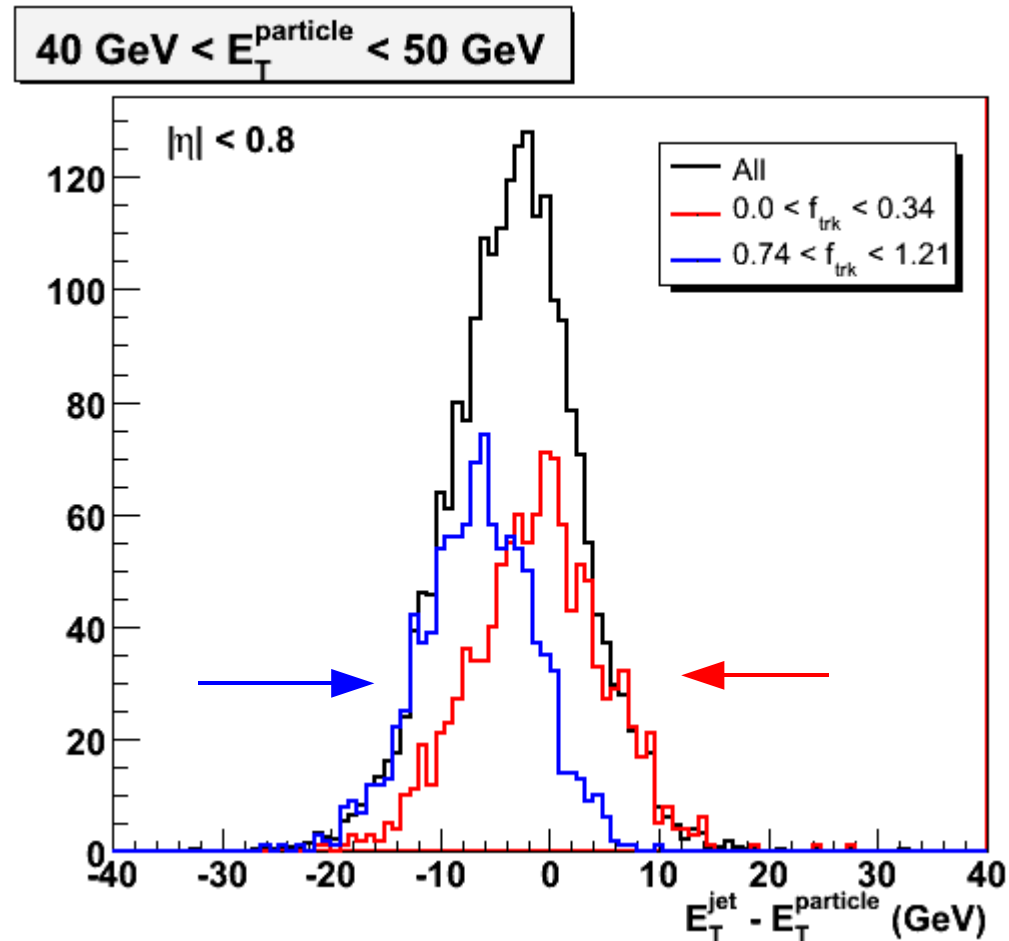
Track selection studies in progress: remove poorly measured and high E tracks

Jet Resolution vs Charged ET fraction



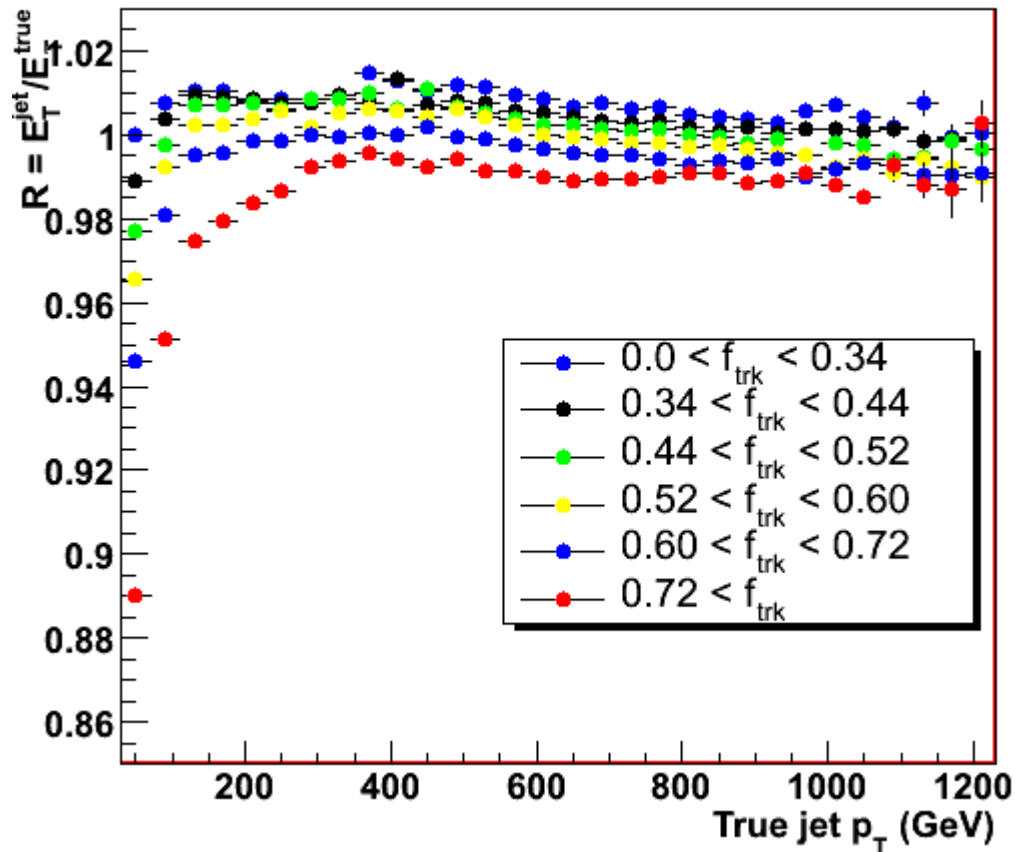
Significant Cal-Jet *energy scale* differences as a function of ET fraction.

Jet Resolution vs Charged ET fraction



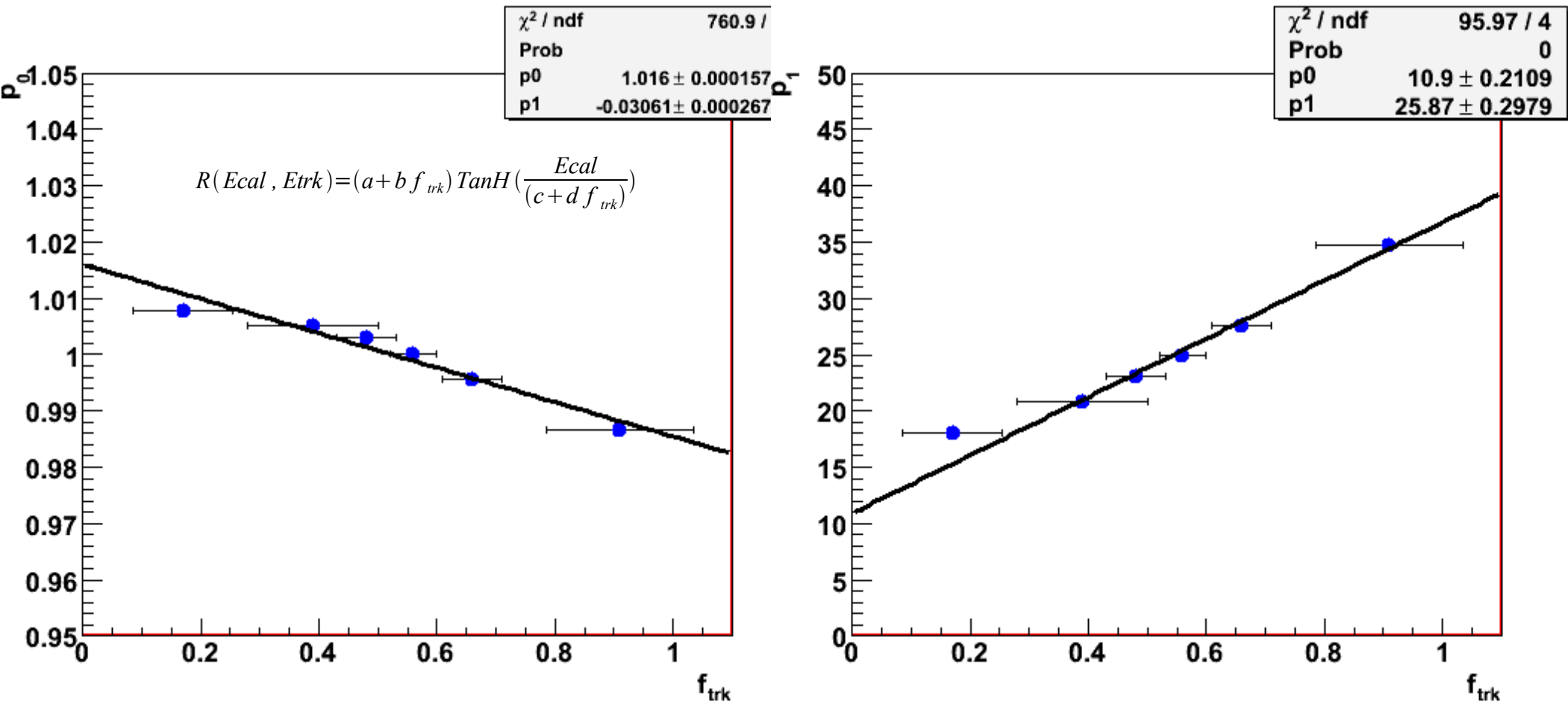
The Cal Jet resolution width can be improved if jets with different f_{trk} are calibrated such that they have the same energy scale.

Jet Response vs. Charged ET fraction



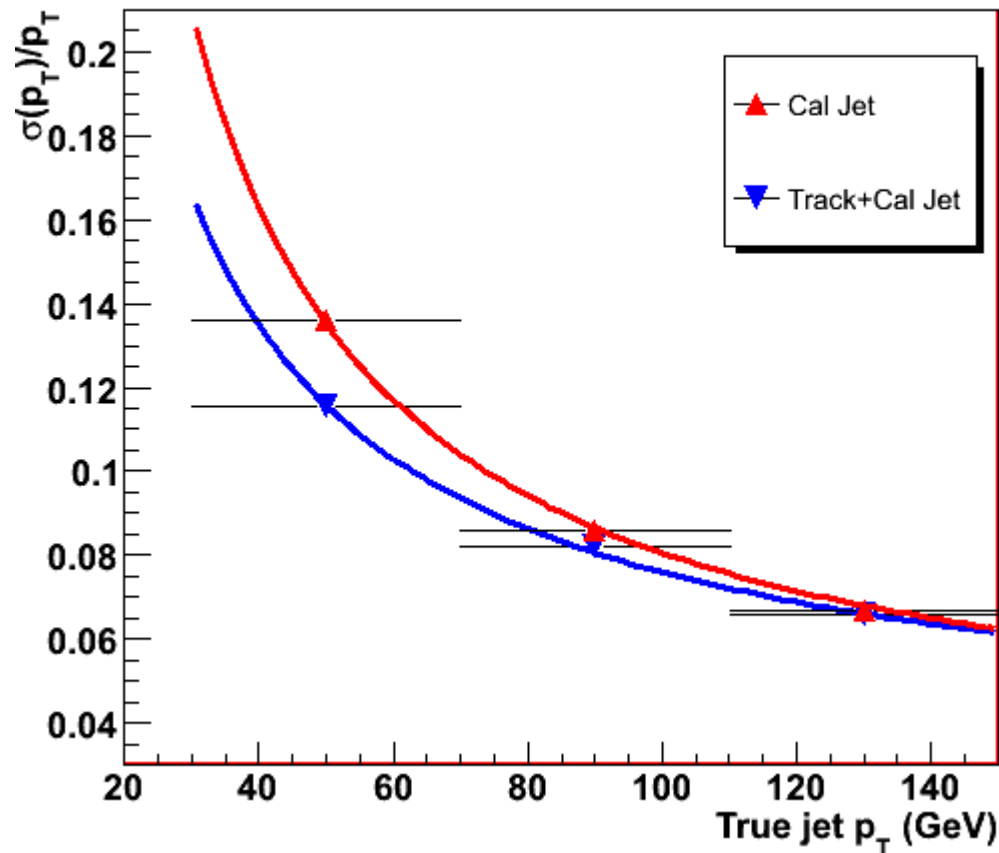
Significant energy scale dependence at low ET (<150 GeV)
Most of the energy shift comes from $f_{\text{trk}} > 0.5$

Jet Energy Scale Correction using Tracks



Fit Jet Energy Response for each f_{trk} , and derive a track-based response correction: $R(E_{\text{cal}}, E_{\text{trk}})$

Track+Jet Energy Resolution Improvement



Jet Resolution is improved because jets with different charged fraction are corrected to the same energy scale, reducing the overall width.

More than 15% relative improvement at 50 GeV.

Summary and Plans

- First look at 2 data-driven techniques to determine jet energy resolutions: Dijet balance, kT.

Differences between both methods at low transverse energy.

Closure test shows that the application of both methods over-estimate the jet resolution at low transverse energy (under investigation)

- Developed an algorithm to improve the jet energy resolution using track information.

The gain is due to the proper calibration of jets as a function of its charged particle energy content, measured with the tracker (15% @ 50 GeV)

The next step is to explore the use of correlations between different track variables (to account for jet fragmentation fluctuations) and to optimize the track selection.