The impact of dimension-8 operators on the 2HDM

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Motivation 2HDM EFT Results Conclusion	Motivation	2HDM	EFT	Results	Conclusions
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- Although the Standard Model (SM) is extremely powerful, there is physics beyond it (BSM)
- The SM Effective Field Theory **SMEFT** is a very convenient description of BSM physics:
 - It configures a consistent and general description of deviations from the SM

$$\mathcal{L} = \mathcal{L}_{\rm SM} + \Sigma_{n,i} \frac{C_i^n O_i^n}{\Lambda^{n-4}}$$

- Conversion between experimental data and theory has to be done only once
- Ultimate goal of the SMEFT framework:
 - Find a pattern of non-zero deviations in the SMEFT coefficients C_i^n
 - Associate that pattern with a particular BSM model
- How *good* is such association?
 - This can be investigated by looking at particular BSM models
 - Usually, one truncates the SMEFT expansion with dimension-6 operators [Englert et al, 1403.7191] [Brehmer et al, 1510.03443]
 - But is that *good enough*?

[Perez, Toscano, Wudka, 9506457]

[Gorbahn, No, Sanz, 1502.07352]

[Bélusca-Maïto et al, 1611.01112]

[Dawson, Murphy, 1704.07851]

[Dawson, Homiller, Lane, 2007.01296]

heavy

- There are some scenarios in which dimension-6 operators are expected to be insufficient [Contino et al, 1604.06444]
- Considering dimension-6 squared (without dimension-8) effects is formally inconsistent

• For an amplitude
$$\mathcal{A} \propto a_0 g_{\rm SM} + a_1 \frac{C^{(6)}}{\Lambda^2} + a_2 \frac{C^{(6)}}{\Lambda^4} + \cdots$$
, we have:

$$\mathcal{A}|^2 \propto |a_0 g_{\rm SM}|^2 + \frac{2}{\Lambda^2} \operatorname{Re}[a_0 a_1 g_{\rm SM} C^{(6)}] + \frac{1}{\Lambda^4} \left\{ |a_1 C^{(6)}|^2 + 2 \operatorname{Re}[a_0 a_2 g_{\rm SM} C^{(8)}] \right\} + \dots$$

- (()

 \sim (0)

- Effects of dimension-8 operators have been considered in very few cases...
 [Hays et al, 1808.00442] [Corbett, 2102.02819] [Dawson, Homiller, Sullivan, 2110.06929]
 ... and the results turn out to be very model dependent
- Those effects are expected to be interesting in the 2 Higgs Doublet Model (2HDM):
 - Dimension-6 operators cannot capture the Higgs-gauge interactions of the 2HDM

[Bélusca-Maïto et al, 1611.01112]

- It provides a sufficiently rich description, without being too cumbersome
- I shall investigate LHC Higgs signals at leading order (LO)

Motivation	2HDM	EFT	Results	Conclusions
• 2HDM in a nuts	hell:			

- take the SM, with its scalar doublet (Φ_1) , and add an extra one (Φ_2)
- impose a Z_2 symmetry, according to which $\Phi_1 \rightarrow \Phi_1, \quad \Phi_2 \rightarrow -\Phi_2$
- both Φ_1 and Φ_2 have vevs: $\frac{v_1}{\sqrt{2}}$ and $\frac{v_2}{\sqrt{2}}$; then, define β such that $\tan \beta = v_2/v_1$
- rotate to the Higgs basis:

$$\left(\begin{array}{c}H_1\\H_2\end{array}\right) = \left(\begin{array}{cc}c_\beta & s_\beta\\-s_\beta & c_\beta\end{array}\right) \left(\begin{array}{c}\Phi_1\\\Phi_2\end{array}\right)$$

• in that basis, where only H_1 has vev,

$$\mathcal{L}_{2\mathrm{HDM}} \ni \mathcal{L}_{\mathrm{kin}} + \mathcal{L}_{Y} - V_{Y}$$

 $\mathcal{L}_{\rm kin} = (D_{\mu}H_1)^{\dagger} (D^{\mu}H_1) + (D_{\mu}H_2)^{\dagger} (D^{\mu}H_2)$

$$V = Y_{1}H_{1}^{\dagger}H_{1} + Y_{2}H_{2}^{\dagger}H_{2} + \left(Y_{3}H_{1}^{\dagger}H_{2} + \text{h.c.}\right) + \frac{Z_{1}}{2}\left(H_{1}^{\dagger}H_{1}\right)^{2} + \frac{Z_{2}}{2}\left(H_{2}^{\dagger}H_{2}\right)^{2} + Z_{3}\left(H_{1}^{\dagger}H_{1}\right)\left(H_{2}^{\dagger}H_{2}\right) + Z_{4}\left(H_{1}^{\dagger}H_{2}\right)\left(H_{2}^{\dagger}H_{1}\right) + \left\{\frac{Z_{5}}{2}\left(H_{1}^{\dagger}H_{2}\right)^{2} + Z_{6}\left(H_{1}^{\dagger}H_{1}\right)\left(H_{1}^{\dagger}H_{2}\right) + Z_{7}\left(H_{2}^{\dagger}H_{2}\right)\left(H_{1}^{\dagger}H_{2}\right) + \text{h.c.}\right\} + Z_{7}\left(H_{2}^{\dagger}H_{2}\right)\left(H_{1}^{\dagger}H_{2}\right) + \text{h.c.}\right\} + \mathcal{L}_{Y} = -\lambda_{u}^{(1)*}H_{1}^{\dagger}\hat{q}_{L}u_{R} - \lambda_{u}^{(2)*}H_{2}^{\dagger}\hat{q}_{L}u_{R} - \lambda_{d}^{(1)}\bar{d}_{R}H_{1}^{\dagger}q_{L} - \lambda_{d}^{(2)}\bar{d}_{R}H_{2}^{\dagger}q_{L} - \lambda_{l}^{(1)}\bar{e}_{R}H_{1}^{\dagger}l_{L} - \lambda_{l}^{(2)}\bar{e}_{R}H_{2}^{\dagger}l_{L} + \text{h.c.}$$

$$\downarrow \dots \Rightarrow \hat{q}_{L} \equiv -i\sigma_{2}(\bar{q}_{L})^{\mathrm{T}}, \text{ such that } H_{j}^{\dagger}\hat{q}_{L} = \bar{q}_{L}\tilde{H}_{j}$$

Motivation

• extend Z_2 to the fermions \longrightarrow 4 types of 2HDM: Type-I, Type-II, Type-L, Type-F

EFT

• the Yukawa parameters read:
$$\lambda_f^{(1)} = \frac{\sqrt{2}}{v} m_f$$
, $\lambda_f^{(2)} = \frac{\eta_f}{\tan\beta} \lambda_f^{(1)}$

	Type-I	Type-II	Type-L	Type-F
η_u	1	1	1	1
η_d	1	$-\tan^2\beta$	1	$-\tan^2\beta$
η_l	1	$-\tan^2\beta$	$-\tan^2\beta$	1

consider the particular scenario where Y_3, Z_5, Z_6, Z_7 all take real values. Then: $H_1 = \begin{pmatrix} G^+ \\ \frac{1}{\sqrt{2}}(v+h_1^{\rm H}+iG_0) \end{pmatrix}, \quad H_2 = \begin{pmatrix} H^+ \\ \frac{1}{\sqrt{2}}(h_2^{\rm H}+iA) \end{pmatrix}$

N.B.: this is *not* a model, but simply one solution of the generally CP violating model

where all states are mass eigenstates but $h_1^{\rm H}, h_2^{\rm H}.$ By introducing α , we find:

$$H_{1} = \begin{pmatrix} G^{+} & H^{+} \\ \frac{1}{\sqrt{2}} \left(v + s_{\beta - \alpha} h_{125} + c_{\beta - \alpha} H_{0} + iG_{0} \right) \end{pmatrix}, \quad H_{2} = \begin{pmatrix} H^{+} & H^{+} \\ \frac{1}{\sqrt{2}} \left(c_{\beta - \alpha} h_{125} - s_{\beta - \alpha} H_{0} + iA \right) \end{pmatrix}$$

where h_{125} is the scalar found at the LHC, and H_0, A, H^+ are new scalars

write the Z's of the potential in terms of more convenient parameters:

$$Z_{1} = \frac{\left[m_{h_{125}}^{2} + m_{H_{0}}^{2} \cot(\beta - \alpha)^{2}\right] \sin(\beta - \alpha)^{2}}{v^{2}},$$

$$Z_{3} = \frac{2(m_{H^{\pm}}^{2} - Y_{2})}{v^{2}},$$

$$Z_{4} = \frac{2m_{A}^{2} + m_{h_{125}}^{2} + m_{H_{0}}^{2} - 4m_{H^{\pm}}^{2} + (m_{h_{125}}^{2} - m_{H_{0}}^{2}) \cos\left[2(\beta - \alpha)\right]}{2v^{2}},$$

$$Z_{5} = \frac{-2m_{A}^{2} + m_{h_{125}}^{2} + m_{H_{0}}^{2} + (m_{h_{125}}^{2} - m_{H_{0}}^{2}) \cos\left[2(\beta - \alpha)\right]}{2v^{2}},$$

$$Z_{6} = \frac{(m_{h_{125}}^{2} - m_{H_{0}}^{2}) \sin\left[2(\beta - \alpha)\right]}{2v^{2}}$$

take some of the parameters as independent:

2HDM

$$\beta - \alpha, m_{h_{125}}, Y_2, m_{H_0}, m_A, m_{H^{\pm}}, \beta, m_f$$

Results

	Motivation	2HDM	EFT	Results	Conclusions		
	A complexe II +	- h- h	internets it and		$\bullet Y_2 \equiv \Lambda^2 \gg v^2$		
•	• Assuming H_2 to be heavy, we want to <i>integrate</i> it <i>out</i>						
	• write the equation of motion (EoM) for H_2						
	 assume 	a solution of the form I	$H_{2c} = H_{2c}^{(0)} + \frac{H_{2c}}{4}$	$\frac{F_{2c}^{(1)}}{Y_2} + \frac{H_{2c}^{(2)}}{Y_2^2}$			

- (the different $H_{2c}^{(i)}$ can be determined by solving the EoM order by order)
- replace H_2 by H_{2c} in the Lagrangian
- The effective Lagrangian reads:

$$\mathcal{L}_{\text{eff}} = F_4 + \frac{F_6}{Y_2} + \frac{F_8}{Y_2^2} + \mathcal{O}\left(\frac{1}{Y_2^3}\right)$$

or canonical

and we label both the absolute dimension and the effective dimension

[Egana-Ugrinovic, Thomas, 1512.00144]

example:
$$\frac{F_{\tilde{8}\underline{4}\underline{4}}}{Y_2^2} \ni \underbrace{\left(\frac{Y_3^2}{Y_2^2}\right)}_{\text{eff dim. 8}} \underbrace{\left(D_{\mu}H_1\right)^{\dagger} \left(D^{\mu}H_1\right)}_{\text{abs. dim. 4}}$$

then, we have:

$$F_4 = F_{4,2} + F_{4,4},$$

$$F_6 = F_{6,2} + F_{6,4} + F_{6,6},$$

$$F_8 = F_{8,4} + F_{8,6} + F_{8,8},$$



$$H_1 = \mathcal{H}\left(1 - \frac{\left|Y_3\right|^2}{2Y_2^2}\right)$$

• The SMEFT Lagrangian is then:

$$\mathcal{L}_{\mathrm{SMEFT}} = \mathcal{L}_{\mathrm{SM}} + rac{S_{\mathrm{all},6}}{\Lambda^2} + rac{S_{\mathrm{all},8}}{\Lambda^4} + \mathcal{O}\left(rac{1}{\Lambda^6}
ight),$$

$$\begin{split} S_{\text{all},6} &= C_{\mathcal{H}}(\mathcal{H}^{\dagger}\mathcal{H})^{3} + \left\{ C_{u\mathcal{H}}\left(\mathcal{H}^{\dagger}\mathcal{H}\right) \bar{q}_{L}u_{R}\tilde{\mathcal{H}} + C_{d\mathcal{H}}\left(\mathcal{H}^{\dagger}\mathcal{H}\right) \bar{q}_{L}d_{R}\mathcal{H} + \text{h.c.} \right\} + 4\text{F} \\ S_{\text{all},8} &= C_{\mathcal{H}^{8}}(\mathcal{H}^{\dagger}\mathcal{H})^{4} + C_{\mathcal{H}^{6}}^{(1)}(\mathcal{H}^{\dagger}\mathcal{H})^{2}\left(D_{\mu}\mathcal{H}\right)^{\dagger}\left(D^{\mu}\mathcal{H}\right) + \left\{ C_{qu\mathcal{H}^{5}}(\mathcal{H}^{\dagger}\mathcal{H})^{2}\bar{q}_{L}u_{R}\tilde{\mathcal{H}} \right. \\ &+ C_{qu\mathcal{H}^{3}D^{2}}^{(1)}\left(D_{\mu}\mathcal{H}\right)^{\dagger}\left(D^{\mu}\mathcal{H}\right)\bar{q}_{L}u_{R}\tilde{\mathcal{H}} + C_{qu\mathcal{H}^{3}D^{2}}^{(2)}\left[\left(D_{\mu}\mathcal{H}\right)^{\dagger}\tau^{I}\left(D^{\mu}\mathcal{H}\right)\right]\left[\bar{q}_{L}u_{R}\tau^{I}\tilde{\mathcal{H}}\right] \\ &+ C_{qu\mathcal{H}^{3}D^{2}}^{(5)}\left[\left(D_{\mu}\mathcal{H}\right)^{\dagger}\mathcal{H}\right]\left[\bar{q}_{L}u_{R}\tilde{D^{\mu}}\mathcal{H}\right] + C_{qd\mathcal{H}^{5}}(\mathcal{H}^{\dagger}\mathcal{H})^{2}\bar{q}_{L}d_{R}\mathcal{H} \\ &+ C_{qd\mathcal{H}^{3}D^{2}}^{(1)}\left(D_{\mu}\mathcal{H}\right)\bar{q}_{L}d_{R}\mathcal{H} + C_{qd\mathcal{H}^{3}D^{2}}^{(2)}\left[\left(D_{\mu}\mathcal{H}\right)^{\dagger}\tau^{I}\left(D^{\mu}\mathcal{H}\right)\right]\left[\bar{q}_{L}d_{R}\tau^{I}\mathcal{H}\right] \\ &+ C_{qd\mathcal{H}^{3}D^{2}}^{(5)}\left(\mathcal{H}^{\dagger}D_{\mu}\mathcal{H}\right)\left(\bar{q}_{L}d_{R}D^{\mu}\mathcal{H}\right) + \text{h.c.}\right\} + 4\text{F}, \end{split}$$

• The explicit matching is:

$$C_{\mathcal{H}} = C_{\mathcal{H}}^{[6]} + \frac{C_{\mathcal{H}}^{[8]}}{\Lambda^2} = |Z_6|^2 + \frac{1}{\Lambda^2} \left(Y_3 Z_1 Z_6^* + Y_3^* Z_1 Z_6 - Y_3 Z_{34} Z_6^* - Y_3^* Z_{34} Z_6 - Y_3 Z_5^* Z_6 - Y_3^* Z_5 Z_6^* + 2Y_1 |Z_6|^2 \right)$$

$$C_{u\mathcal{H}} = C_{u\mathcal{H}}^{[6]} + \frac{C_{u\mathcal{H}}^{[8]}}{\Lambda^2} = Z_6 \lambda_u^{(2)*} + \frac{1}{\Lambda^2} \left(Y_3^* Z_6 \lambda_u^{(1)} + Y_3 Z_1 \lambda_u^{(2)*} - Y_3 Z_{34} \lambda_u^{(2)*} - Y_3^* Z_5 \lambda_u^{(2)*} + 3Y_1 Z_6 \lambda_u^{(2)*} \right)$$

$$C_{d\mathcal{H}} = C_{d\mathcal{H}}^{[6]} + \frac{C_{d\mathcal{H}}^{[8]}}{\Lambda^2} = Z_6^* \lambda_d^{(2)*} + \frac{1}{\Lambda^2} \left(Y_3 Z_6^* \lambda_d^{(1)} + Y_3^* Z_1 \lambda_d^{(2)*} - Y_3^* Z_{34} \lambda_d^{(2)*} - Y_3 Z_5 \lambda_d^{(2)*} + 3Y_1 Z_6 \lambda_d^{(2)*} \right)$$

and

$$\begin{split} C_{\mathcal{H}^8} &= -Z_{34} |Z_6|^2 - \frac{1}{2} Z_5^* Z_6^2 - \frac{1}{2} Z_5 (Z_6^*)^2 + 2Z_1 |Z_6|^2, \\ C_{\mathcal{H}^6}^{(1)} &= -|Z_6|^2, \\ C_{qu\mathcal{H}^5} &= -Z_{34} Z_6 \lambda_u^{(2)*} - Z_5 Z_6^* \lambda_u^{(2)*} + |Z_6|^2 \lambda_u^{(1)} + 3Z_1 Z_6 \lambda_u^{(2)*}, \\ C_{qu\mathcal{H}^3 D^2}^{(1)} &= -3Z_6 \lambda_u^{(2)*}, \\ C_{qu\mathcal{H}^3 D^2}^{(2)} &= Z_6 \lambda_u^{(2)*}, \\ C_{qd\mathcal{H}^3 D^2}^{(5)} &= -2Z_6 \lambda_u^{(2)*}, \\ C_{qd\mathcal{H}^5} &= -Z_{34} Z_6^* \lambda_d^{(2)*} - Z_5^* Z_6 \lambda_d^{(2)*} + |Z_6|^2 \lambda_d^{(1)} + 3Z_1 Z_6^* \lambda_d^{(2)*}, \\ C_{qd\mathcal{H}^3 D^2}^{(1)} &= -3Z_6^* \lambda_d^{(2)*}, \\ C_{qd\mathcal{H}^3 D^2}^{(2)} &= -Z_6^* \lambda_d^{(2)*}, \\ C_{qd\mathcal{H}^3 D^2}^{(5)} &= -Z_6^* \lambda_d^{(2)*}, \\ C_{qd\mathcal{H}^3 D^2}^{(5)} &= -Z_6^* \lambda_d^{(2)*}. \end{split}$$

EFT

$$\begin{array}{c|cccc} \hline \text{Motivation} & \underline{2\text{HDM}} & \underline{\text{EFT}} & \underline{\text{Results}} & \underline{\text{Conclusions}} \\ \hline \text{The validity of the EFT approach requires decoupling:} \\ \bullet & m_A^2 \sim m_{H_0}^2 \sim m_{H^{\pm}}^2 \sim Y_2 \equiv \Lambda^2 \gg v^2, \qquad m_{h_{125}}^2 \simeq v^2, \\ \bullet & |\cos(\beta - \alpha)| \propto \frac{v^2}{\Lambda^2} & \hline & \text{decoupling thus implies alignment, } \cos(\beta - \alpha) \rightarrow 0 \\ \hline & \text{Hence, we expand the results to quadratic order in } \cos(\beta - \alpha). \text{ Examples:} \\ \bullet & \frac{C_{uH}}{\Lambda^2} = -\frac{2}{\sqrt{2}} (\sqrt{2}G_F)^{3/2} \frac{\cos(\beta - \alpha)}{\tan\beta} \eta_u m_u - \frac{\cos(\beta - \alpha) m_u (\sqrt{2}G_F)^{3/2}}{\sqrt{2}\Lambda^2} \left[\cos(\beta - \alpha) \Lambda^2 - \frac{6 m_h^2 \eta_u}{\tan\beta} \right] \\ \bullet & \frac{C_{H^8}}{\Lambda^4} = 2 \cos(\beta - \alpha)^2 m_h^2 (\sqrt{2}G_F)^3 \end{array}$$

• To calculate in SMEFT, we define as independent parameters the set:

 $G_F, M_W, M_Z, m_h, m_f \hspace{0.2cm} ext{(and WCs)}$

and we rewrite the dependent parameters in terms of them:

$$\begin{split} \overline{g}_2 &= (\sqrt{2}G_F)^{1/2} \, 2\, M_W, \\ Y_f &= \sqrt{2}(\sqrt{2}G_F)^{1/2} \, m_f + \frac{C_{f\mathcal{H}}}{2\sqrt{2}G_F\Lambda^2} + \frac{C_{qf\mathcal{H}^5}}{8\,G_F^2\Lambda^4} + \frac{C_{\mathcal{H}^6}^{(1)}m_f}{4\sqrt{2}\,(\sqrt{2}G_F)^{3/2}\Lambda^4} \\ \lambda &= \frac{G_F m_h^2}{\sqrt{2}} + \frac{3C_{\mathcal{H}}}{2\sqrt{2}G_F\Lambda^2} + \frac{3C_{\mathcal{H}^8}}{4G_F^2\Lambda^4} + \frac{C_{\mathcal{H}^6}^{(1)}m_h^2}{4\sqrt{2}G_F\Lambda^4} \end{split}$$

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• Higgs signal strengths:

$$\mu_{pp\to h\to f}^{P} = \frac{\sigma_{pp\to h}^{\widehat{P}}(pp\to h)}{\sigma^{P}(pp\to h)_{\rm SM}} \times \frac{\mathrm{BR}(h\to f)}{\mathrm{BR}(h\to \widehat{f})_{\rm SM}}$$

$$\lim_{U\to \mathrm{final\ states:\ }\gamma\gamma,\ b\overline{b},\ \tau^{+}\tau^{-},\ W^{+}W^{-},\ ZZ}$$

• Pure SMEFT results:



• The inclusion of $\frac{1}{\Lambda^4}$ effects adds an extra solution in some WCs: the *wrong-sign* solution

Motivation	2HDM	EFT	Results	Conclusions
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• Two-parameter limits on WCs:



- Again, two solutions: the SM one and the wrong-sign solution (non-SM)
- There is a large correlation between the two WC
- $C_{t\mathcal{H}}$ is less contrained than in the single-fit parameters



insufficient for some regions



- In these models, there is at least one $|\eta_f| \propto an^2 eta$
- Therefore, even the dim-6 Yukawa operators are constrained for high $\tan \beta$
- The dim-8 operators are thus irrelevant in these models





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Motivation 2HDM EFT	Results	Conclu	sions
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- SMEFT is very convenient; but *how good* is the usual truncation with dimension-6 operators?
- I considered the 2HDM, and described an EFT for it up to **dimension-8** operators
- After integrating out the heavy doublet, I used several conversions to obtain SMEFT
- There are very few dimension-6 WCs for LO LHC Higgs physics: C_{uH}, C_{dH}, C_{lH}
- The gauge-Higgs interactions appear only with the **dimension-8** operator $(\mathcal{H}^{\dagger}\mathcal{H})^2 (D_{\mu}\mathcal{H})^{\dagger} (D^{\mu}\mathcal{H})$
- They turn out to be crucial for the Type-I 2HDM for high $\tan \beta$, where C_{fH} are suppressed
- Dimension-8 operators are also relevant for the wrong-sign solution in Type-L
- For other regions and types, dimension-8 operators are irrelevant
- SMEFT NLO Higgs trilinear contributions are quite restrictive

• A note about expansions in power of $1/\Lambda$:

• When truncating
$$BR(h \to b\bar{b}) = \frac{\Gamma(h \to b\bar{b})}{\Gamma(h \to all)}$$
, one can:
 $\begin{cases}
expand num. and dent separately or expand quotient as whole
\end{cases}$

 $\mathrm{BR}(h \to b\bar{b}); \Gamma(h \to b\bar{b}), \Gamma(h \to \mathrm{all}) \text{ expanded separately } \mathrm{BR}(h \to b\bar{b}); [\Gamma(h \to b\bar{b})/\Gamma(h \to \mathrm{all})] \text{ expanded}$



• When higher order operators are relevant for $\Gamma(h \to \text{all})$, then $\frac{1}{\Gamma(h \to \text{all})}$ does not converge

- The correct way is thus to expand $\Gamma(h \to b\bar{b})$ and $\Gamma(h \to all)$ separately
- Neglecting squared effects leads to unreasonable results; but:
 - that is a general consequence of a consistent SMEFT truncation
 - the regions at stake are experimentally excluded anyway

avand num and dan concretely