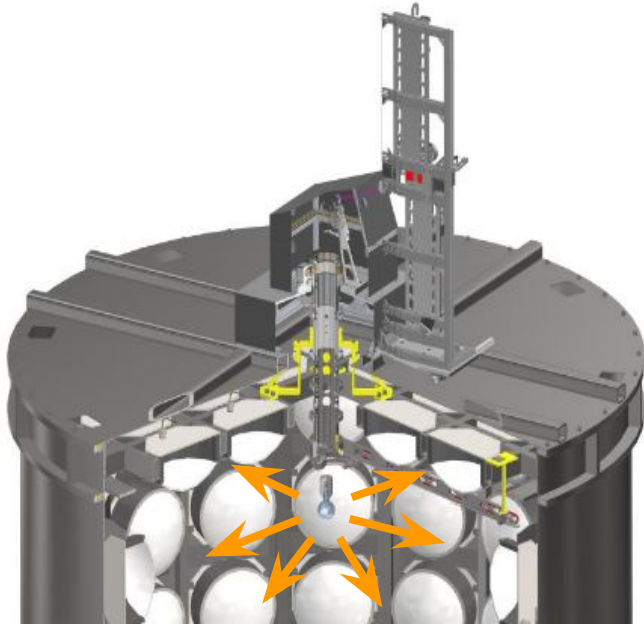


# PMT in-situ calibration with the laser diffuser for WCTE

---

Alie Craplet (alie.craplet17@imperial.ac.uk)

# The calibration process

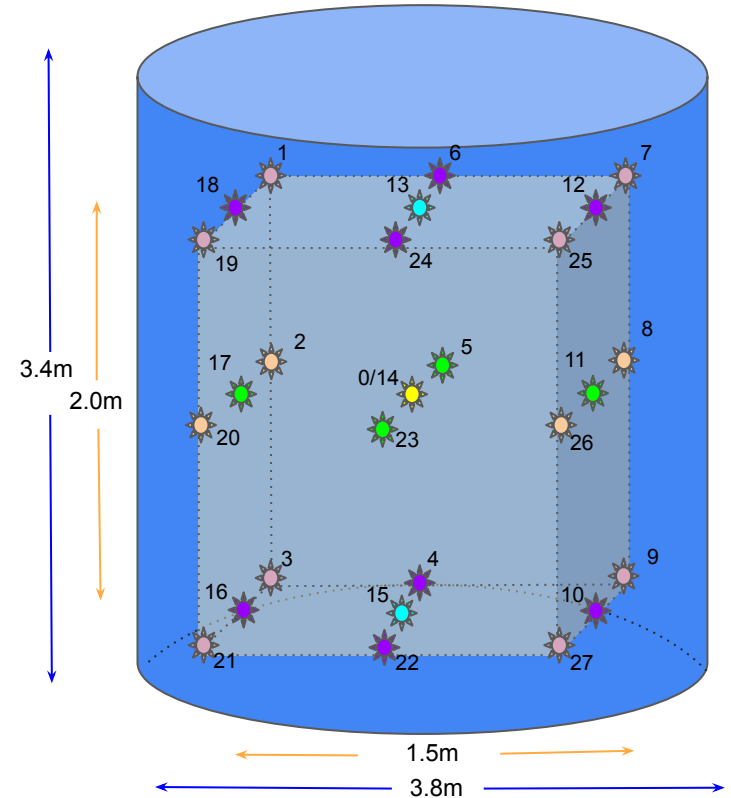


- Laser diffuser and calibration deployment system (CDS) build and tested at Imperial
- Source displaced at key positions within the tank, short light bursts shot.
- Hit times used for **timing** calibration.
- Number of photo-electron recorded used for PMT **angular response** calibration and **water attenuation length** estimation

# Simulated datasets

- Datasets simulated with WCSim and the WCTE 16cShort (16c4r) geometry (without CDS arm)
- Source simulated as a **/gps/particle opticalphoton** at different positions
- 3k events (10k photons per event) simulated.
- Uniform light emission in phi 0-360° and theta 20-180°.
- Photon energy: 3.505eV (353.7 nm) or 3.089eV(401.9nm)
- Studies done with either the 4 mPMT masked or not.

Source positions simulated in WCSim



# Timing calibration

---

Use the hit times of each PMT to figure out the required timing offset

# Timing calibration - method

## 1. Time of flight correction of the digitised hit times

$$t_c = t_{\text{raw}} - t_{\text{trig}} - R/c_w$$

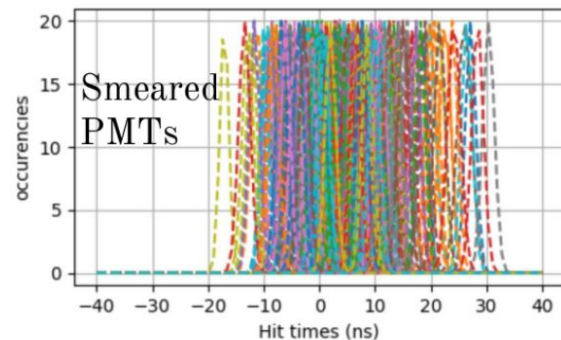
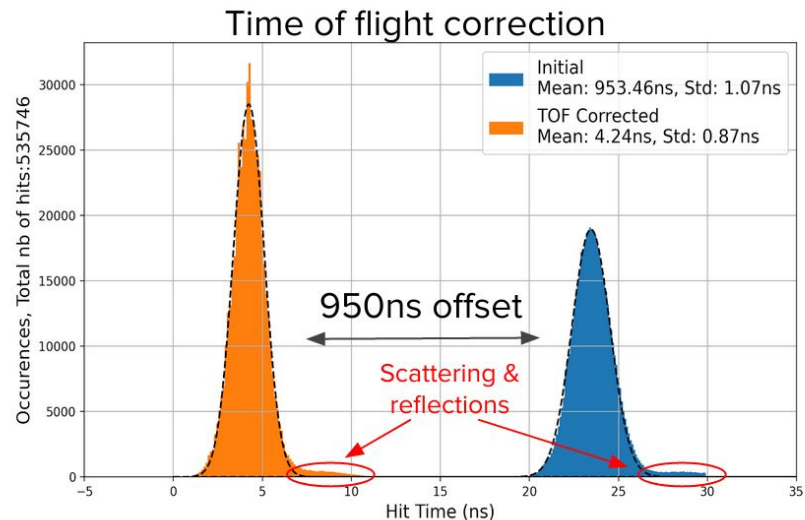
TOF-corrected hit time ←  $t_c$  ← Light velocity in water  
Digitised hit time ←  $t_{\text{raw}}$  ←  
DAQ triggering time ←  $t_{\text{trig}}$  ←  
Source - PMT distance ←  $R$  ←

## 2. Add to TOF-corrected hit time a PMT-dependent smearing drawn from a Gaussian $t_s \sim G(\mu_s, \sigma_s)$

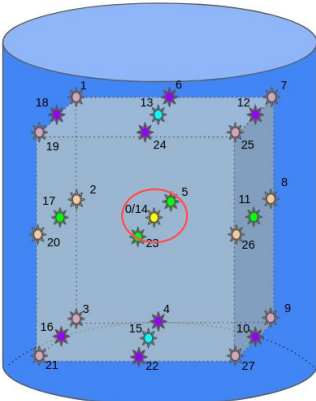
$$t_D = t_c + t_s$$

Smearred and TOF-corrected hit time ←  $t_D$  ←

## 3. Gaussian fit to $t_D$ giving best fit parameters $t_D \sim G(\mu_D, \sigma_D)$ Comparison of $\mu_D$ to $t_s$ to check accuracy of the calibration

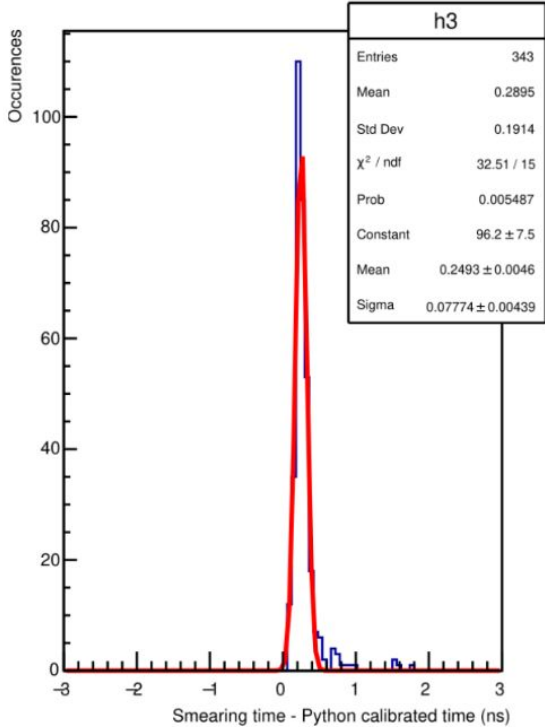


# Timing calibration - Results for source at centre



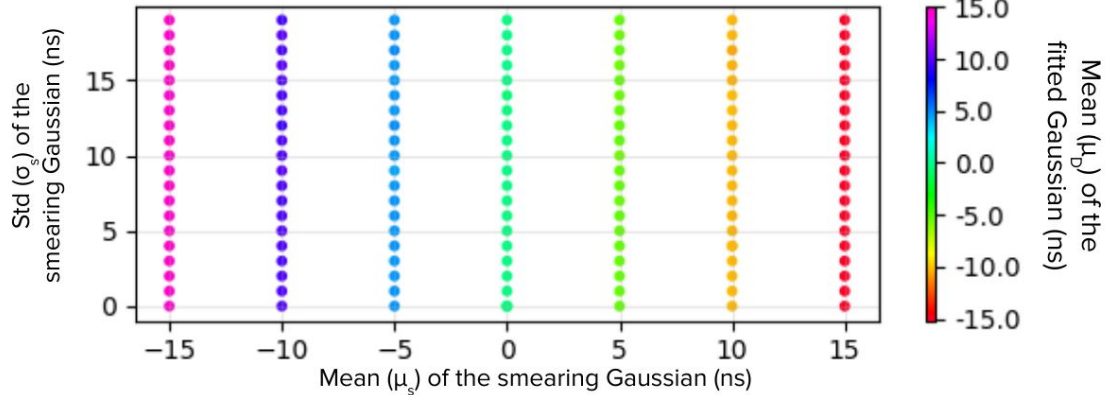
Source at [0, 0, 0]

Python calib. wscim\_1kphat\_3eV\_16Short\_pos0\_CherenkovDigiHits\_cal301.root



The  $t_s - \mu_D$  distribution is centered at +0.29ns with a standard deviation of  $\sim 0.2$ ns.

The accuracy of the calibration doesn't depend on the value of the smearing parameters.



$$t_s - \mu_D$$

# Angular response and attenuation length

---

Fit the number of photoelectron to extract  $A(\cos(\theta))$  and  $\alpha$

# The wcsim\_hybrid\_attenuation\_fit code

Written and adapted to run with WCTE-geometry wcsim-made files by Ka Ming Tsui (Liverpool):

[https://github.com/kmtsui/wcsim\\_hybrid\\_attenuation\\_fit/tree/feature\\_wcte](https://github.com/kmtsui/wcsim_hybrid_attenuation_fit/tree/feature_wcte)

This method uses a set of multiplicative factors and a Minuit minimisation to fit the number of P.E. in the data using:

$$\text{PE}_{\text{predicted}} = \text{Norm} \times \underbrace{\exp\{-R/\alpha\}}_{\text{Attenuation factor}} \times \underbrace{\omega}_{\text{Solid angle subtended by the PMT}} \times \underbrace{\text{Angular Response}(\cos(\theta))}_{\text{Fitted in bins of } \cos(\theta) \text{ or as a polynomial function of } \theta}$$

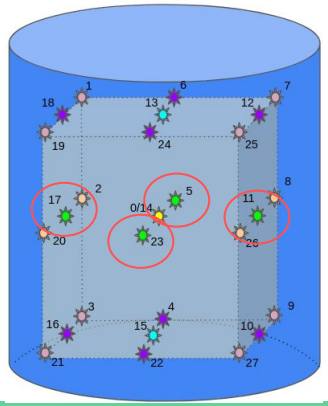
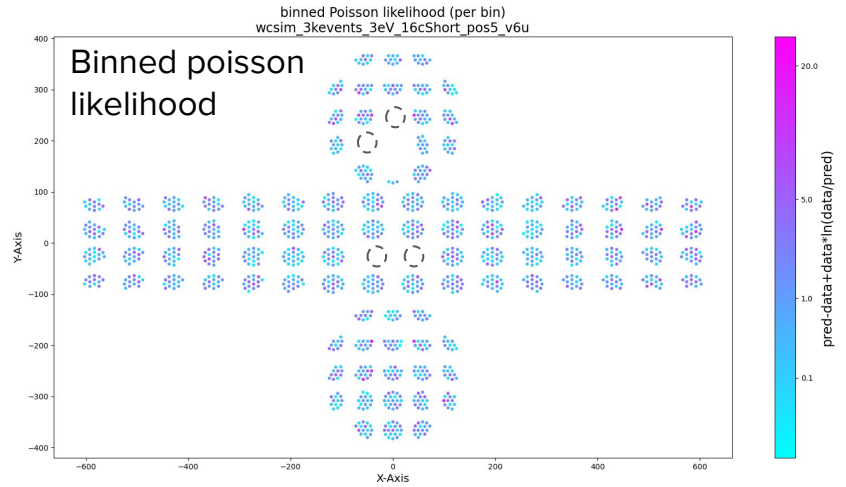
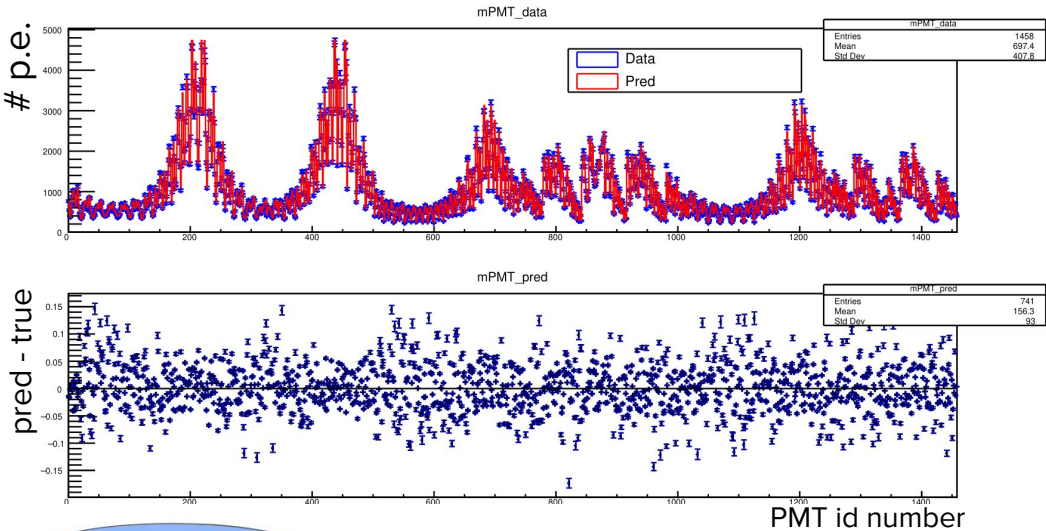
Fixed
Fitted factors

Before the fit, the PMTs can either be distributed in bins of  $\cos(\theta)$  and distance  $R$  from the light source (100 bins total) or, if the fit is unbinned, each bin holds the data from one PMT.

The code extracts the attenuation length in the water  $\alpha$  and the angular response of the PMTs.



# P.E. fit for attenuation length and pmt angular response extraction

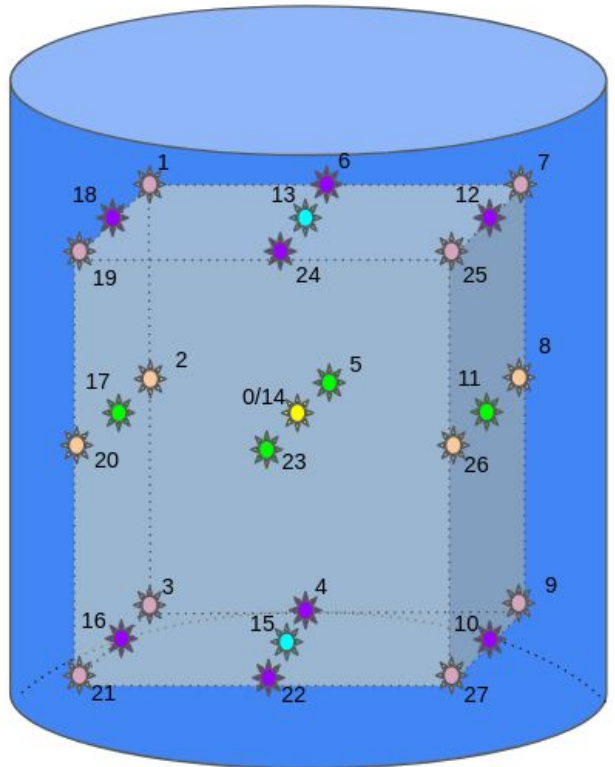
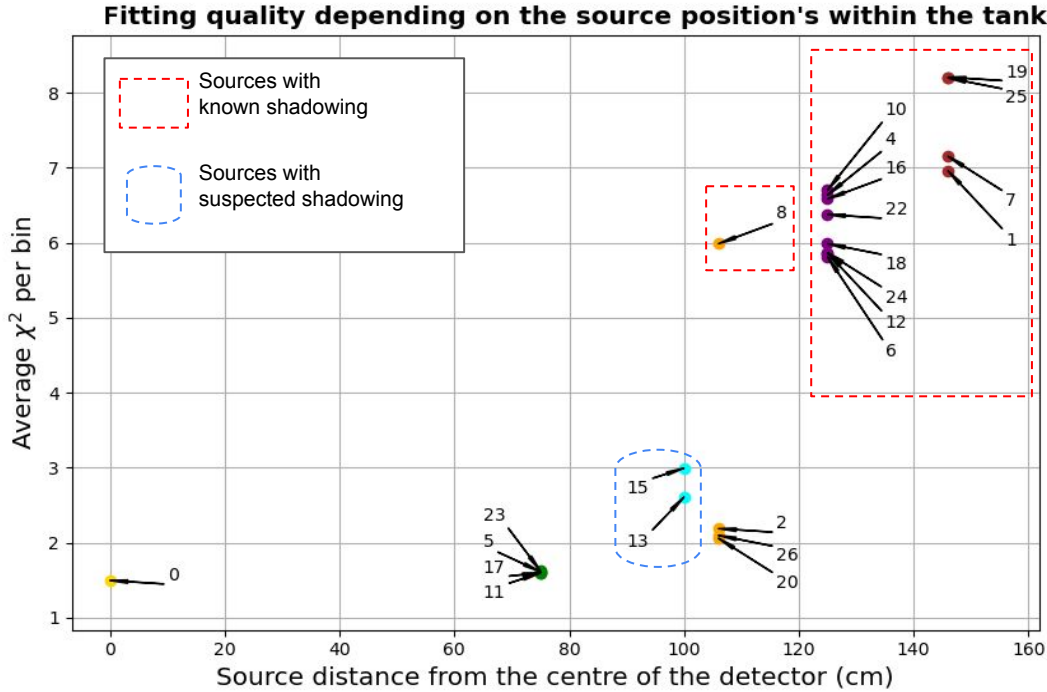


Source dist from 0	75cm
Source positions	5, 17, 11, 23
Chi2/non empty bin (approximately)	~1.5

The number of photo-electron is in general very accurately fitted by the program with a  $\chi^2$  value between 1 and 2.

The fit quality seems to be uniform across the tank - no significant reflections/shadowing.

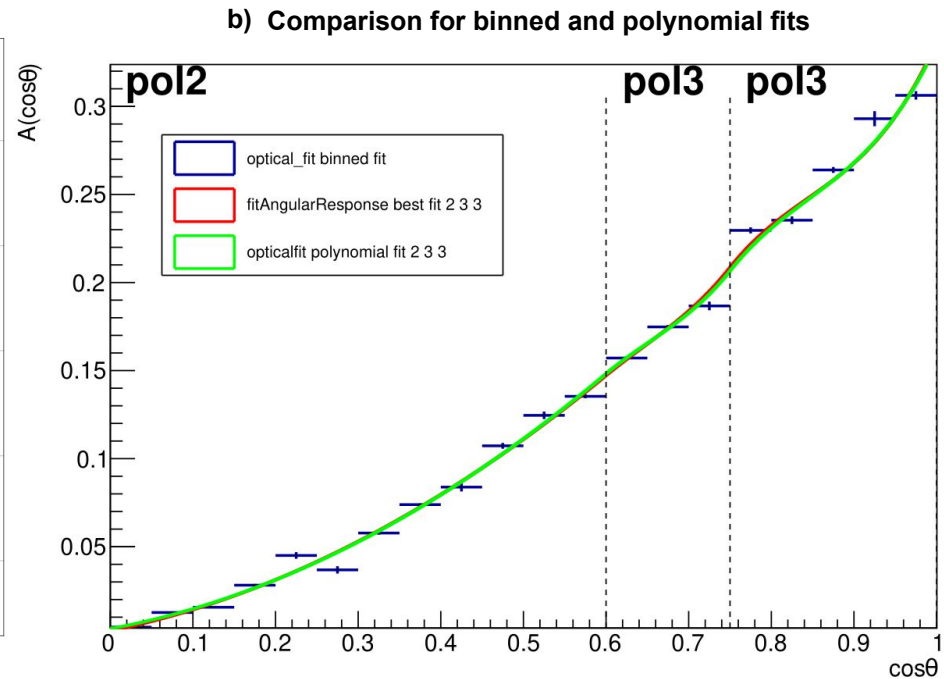
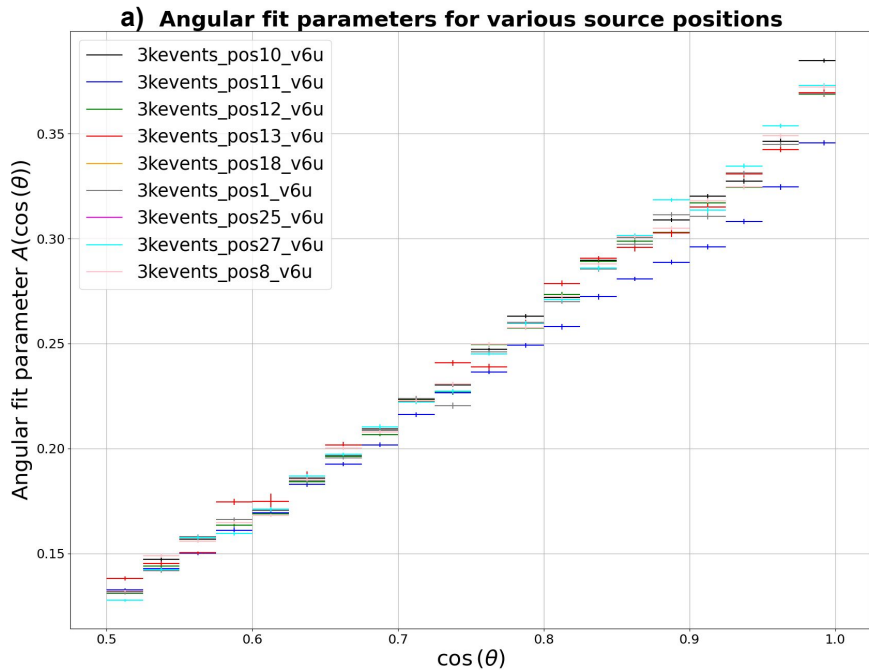
# Effect of shadowing on fitting quality



Source positions further away from the centre of the detector are worsely fitted, shadowing plays a very important role on the fitting quality.

# Angular response

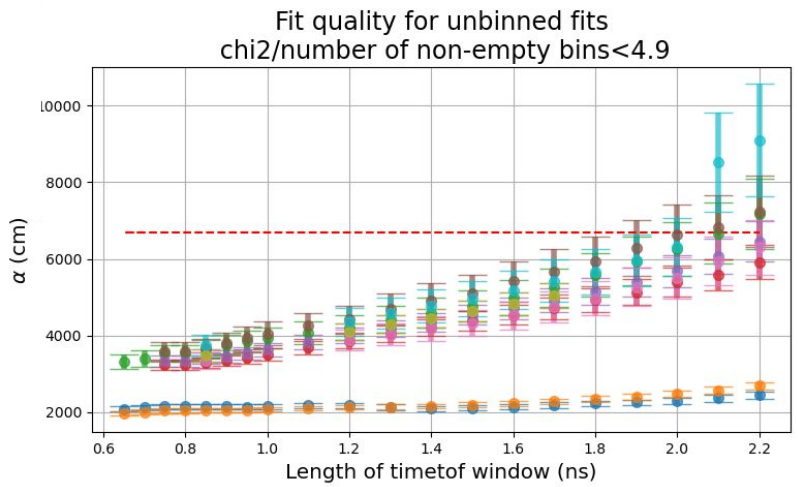
$$PE_{\text{predicted}} = \text{Norm} \times \exp\{-R/\alpha\} \times \omega \times \text{Angular Response}(\cos(\theta))$$



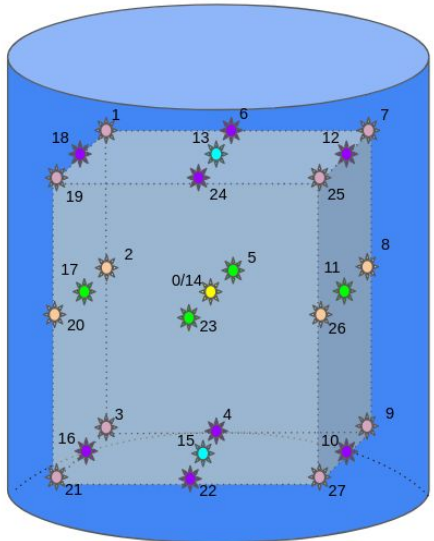
Consistent angular response across source positions, both the binned and polynomial response agree.

# Attenuation length

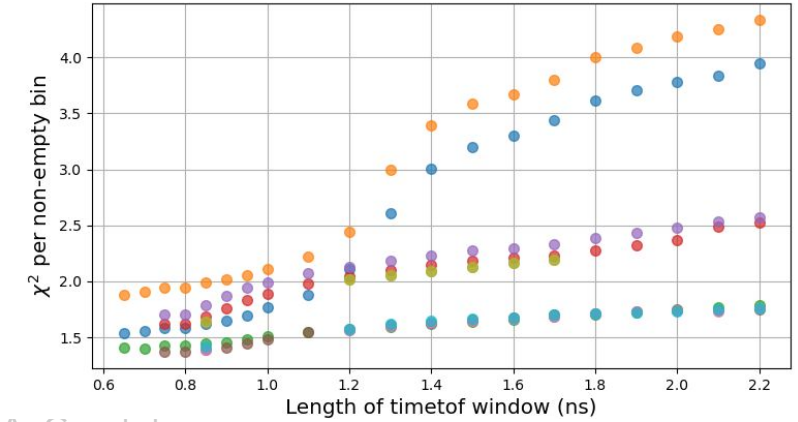
$$PE\_predicted = \text{Norm} \times \exp\{-R/\alpha\} \times \omega \times \text{Angular Response}(\cos(\theta))$$



- True  $\alpha = 6677.84\text{cm}$
- pos 13: [0, 100, 0]
- pos 15: [0, -100, 0]
- pos 11: [75, 0, 0]
- pos 26: [75, 0, 75]
- pos 2: [-75, 0, -75]
- pos 5: [0, 0, -75]
- pos 17: [-75, 0, 0]
- pos 20: [-75, 0, 75]
- pos 21: [-75, -100, 75]
- pos 23: [0, 0, 75]



**Simulated attenuation length: 66m**



The estimate of the attenuation length depends mainly on:

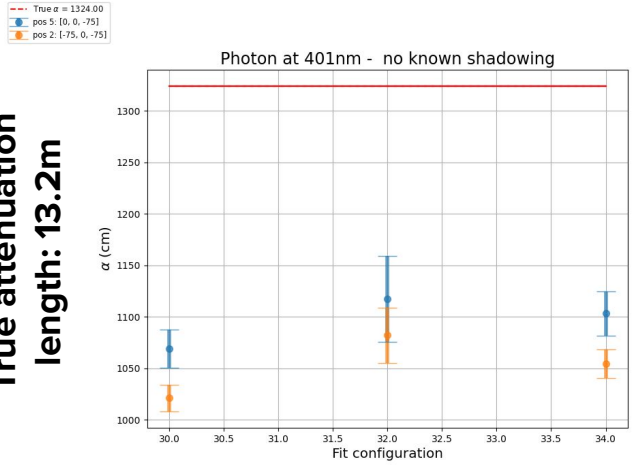
- The source position
- The length of the the TOF-corrected window

Some issues probably remain - we expect a smaller error than what we see.

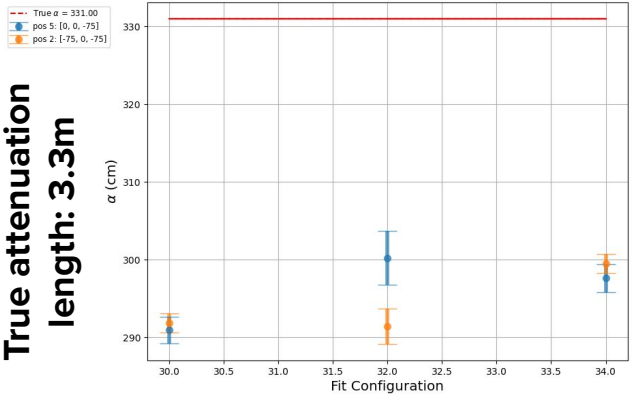
# Attenuation length without shadowing

$$PE\_predicted = \text{Norm} \times \exp\{-R/\alpha\} \times \omega \times \text{Angular Response}(\cos(\theta))$$

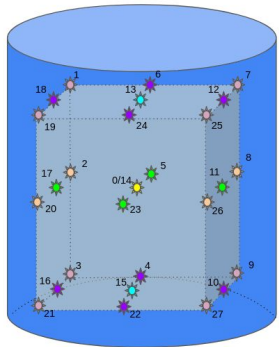
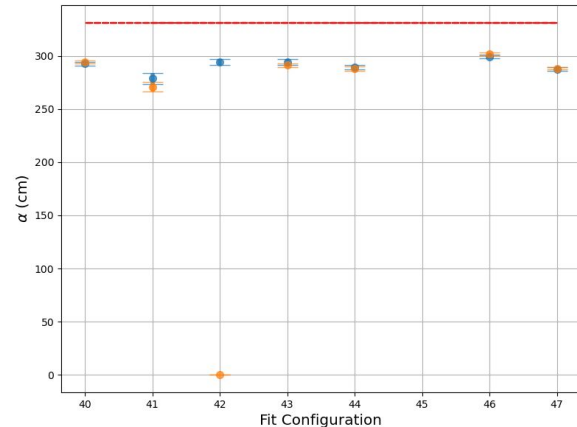
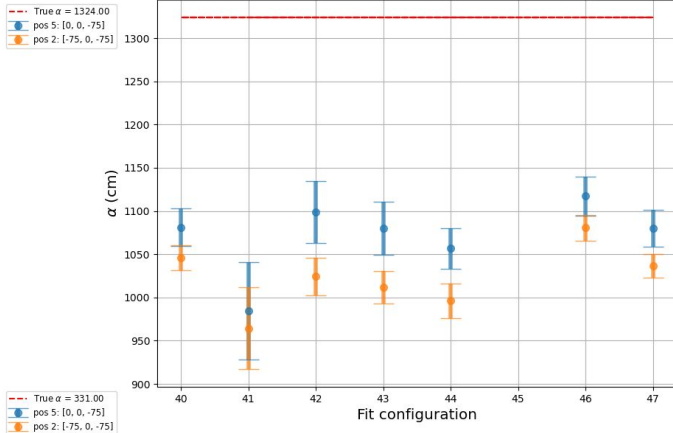
True attenuation length: 13.2m



True attenuation length: 3.3m



Photon at 401nm - no known shadowing



## Configurations:

- 30: Unbinned PMT, polynomial A.R.  
 timetof < 0.15ns, 0.5 < costh
- 32: 30 (0.6 < costh < 0.8)
- 34: 30 (timetof < 0.25ns)
- 40: Unbinned PMT, binned A.R.  
 timetof < 0.15ns, costh > 0.5
- 41: 40 (only central PMT)
- 42: 40 (first ring of PMTs)
- 43: 40 (second ring of PMTs)
- 44: 40 (R > 100cm)
- 46: 40 (timetof < 0.25ns)
- 47: 40 (timetof < 0.05ns)

# Conclusion

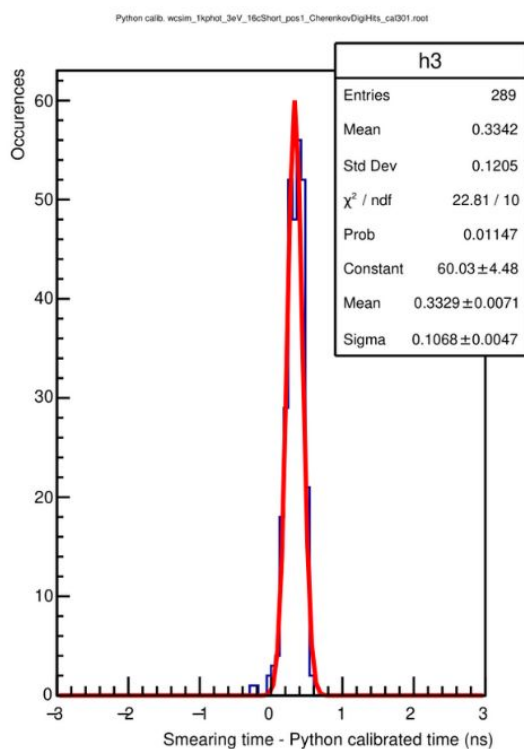
- The possibility of using the laser diffuser and the CDS for in-situ PMT timing and angular response calibration is demonstrated
- Any (simple) time smearing can be calibrated to within about 0.2ns, well below the PMT transient time spread
- The angular response of the PMT is found to be consistent and can be used as a benchmark for the calibration
- Some work is required to make sure the attenuation length estimate is optimal
- The CAD model of the CDS will next be added to the simulation to verify the impact of shadowing and light reflection

# Back-up slides

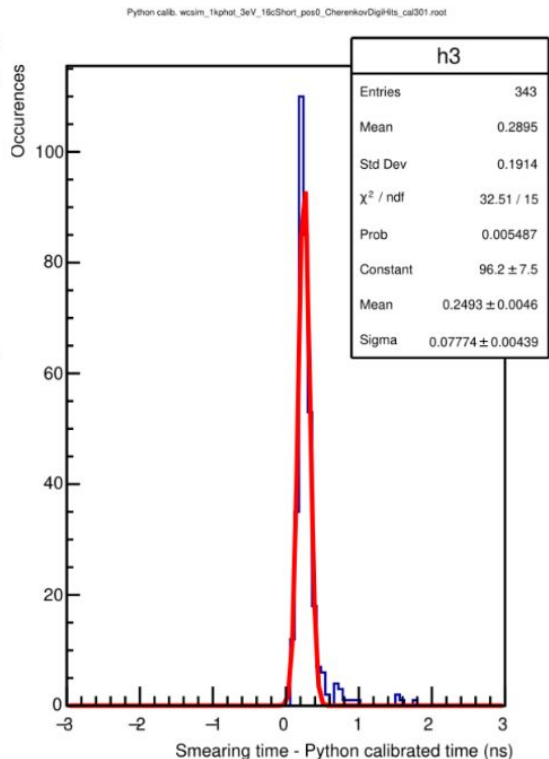
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# Timing calibration - Results

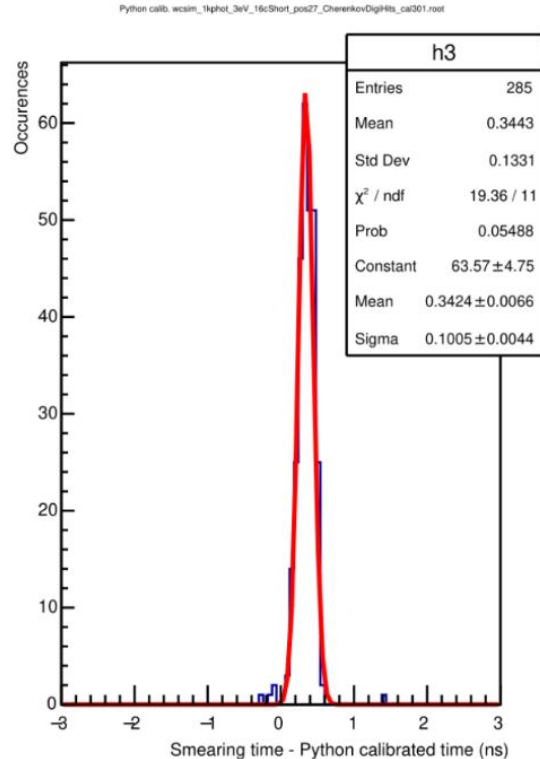
Source at [-75, -75, 100]



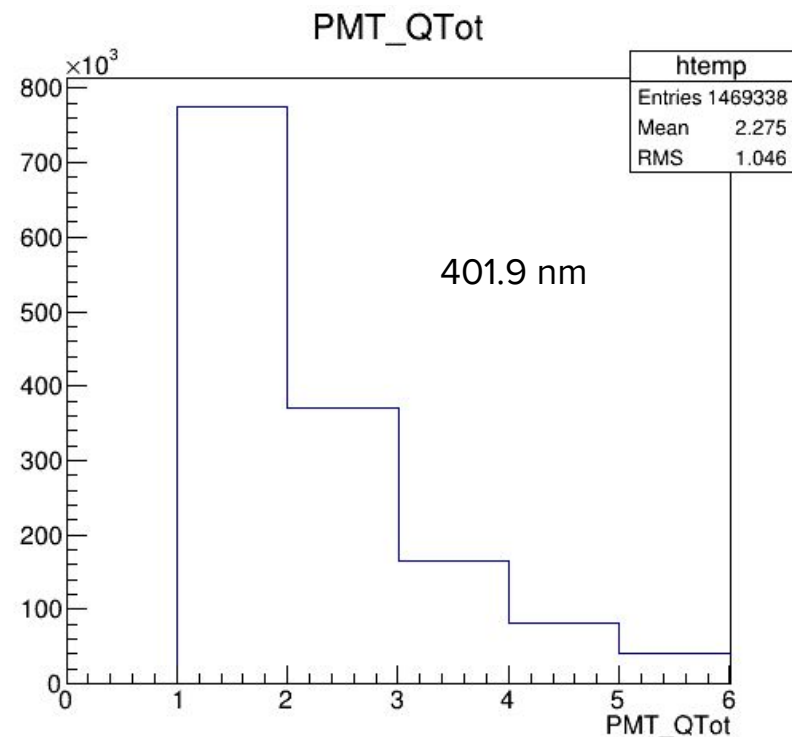
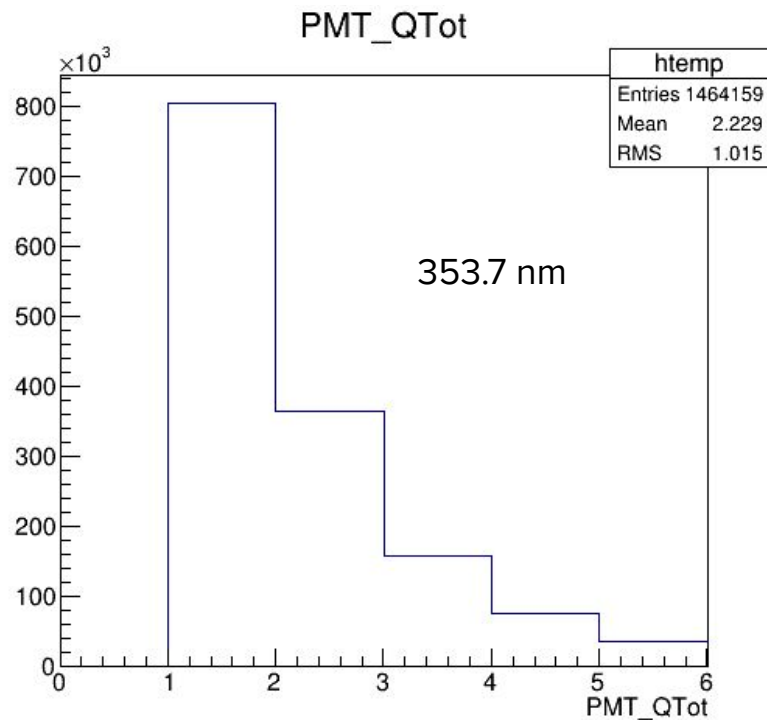
Source at [0, 0, 0]



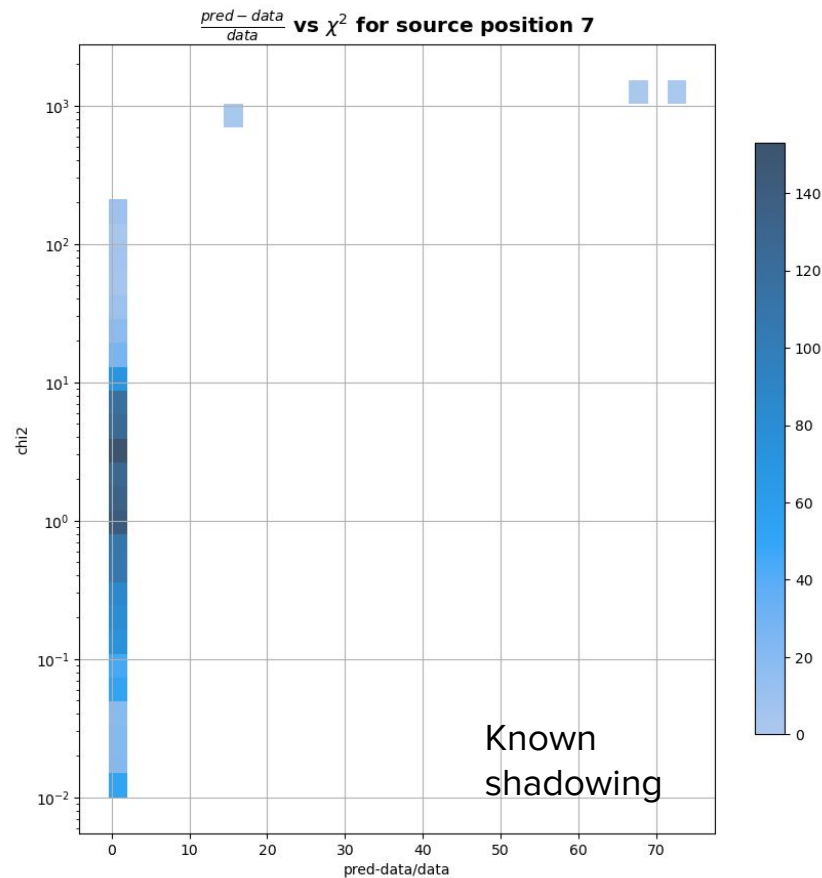
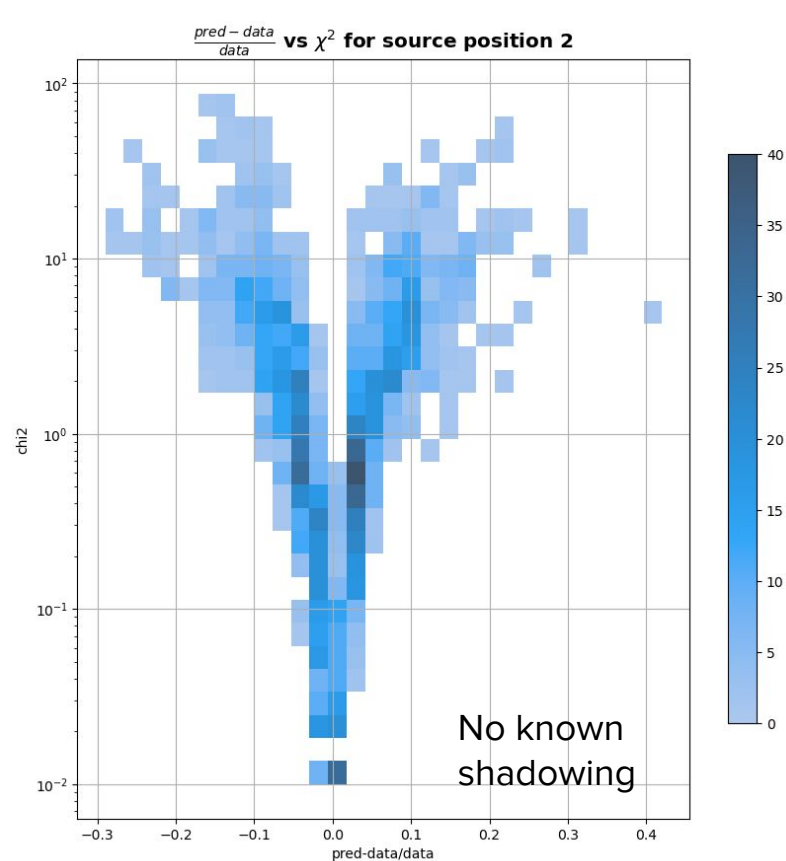
Source at [75, 75, -100]



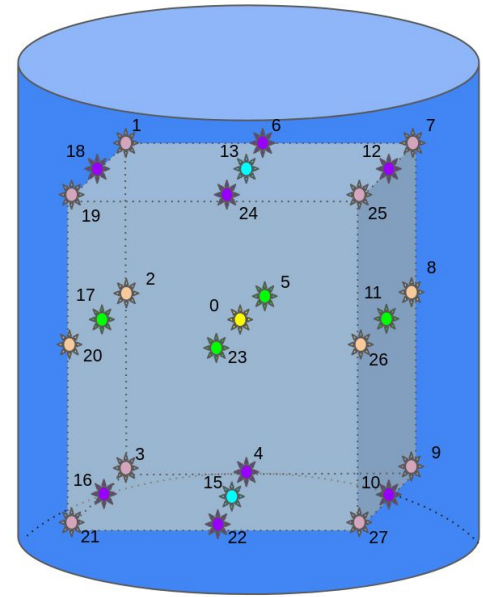
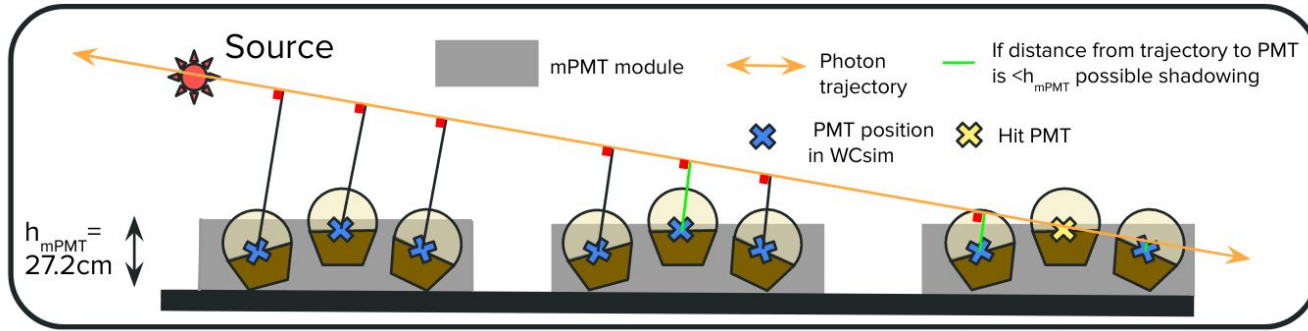




# Scattering or absorption?



# Geometrical checks



Check the distance of closest approach between a given photon trajectory (associated with a hit PMT) and the other PMT as a function of the  $\chi^2$  of the hit PMT.

Hope that if there is PMT-induced shadowing we will see that a lot of mPMT and/or PMT will cross the line of sight.

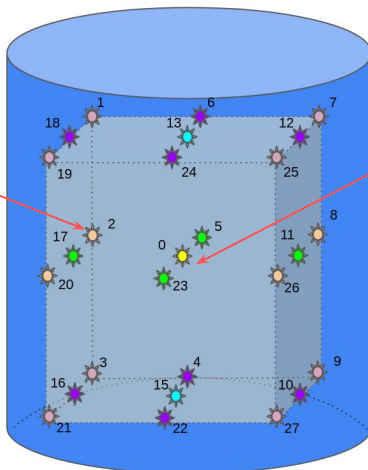
All geometrical checks were made with a cut on the timetof (raw) at 0.25ns

# Geometrical checks

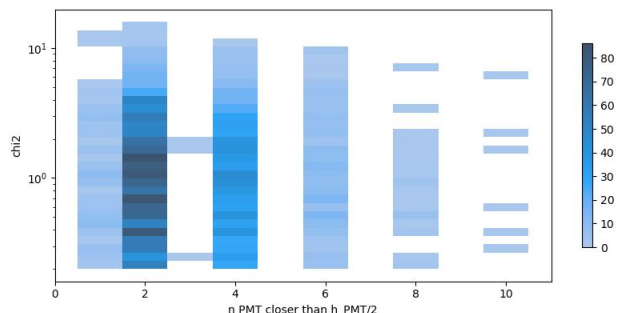
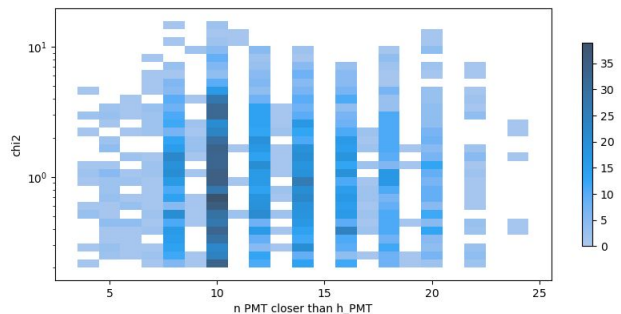
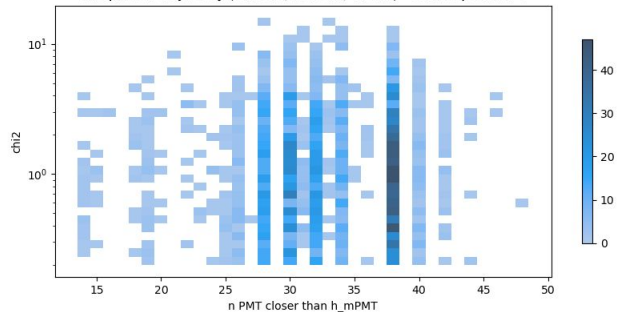
Top: total number of PMTs closer to the line of sight than  $h_{\text{mPMT}}(27.2\text{cm})$

Middle: total number of PMTs closer to the line of sight than  $h_{\text{PMT}}(13.8\text{cm})$

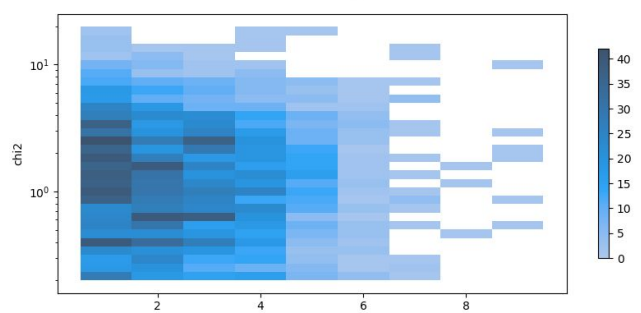
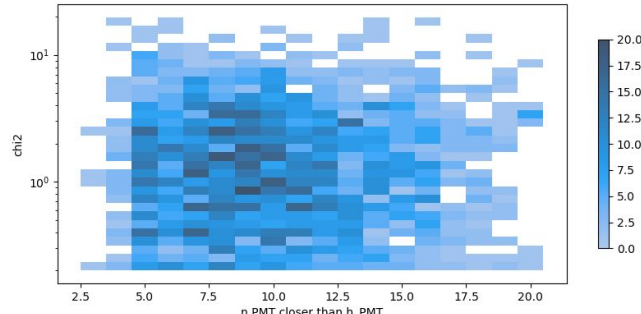
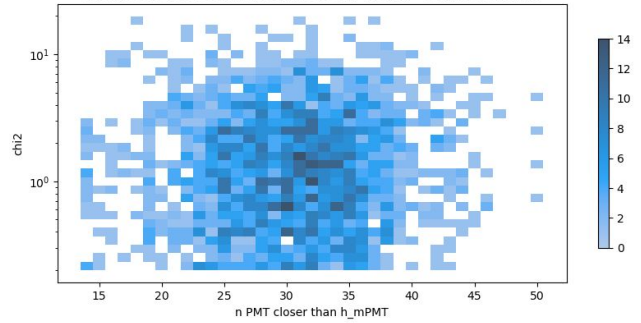
Bottom: total number of PMTs closer to the line of sight than  $h_{\text{PMT}}/2 (7.9\text{cm})$



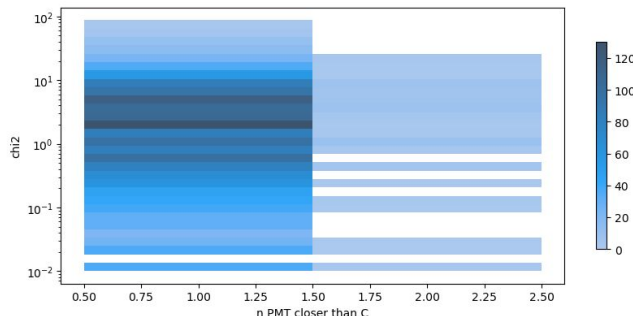
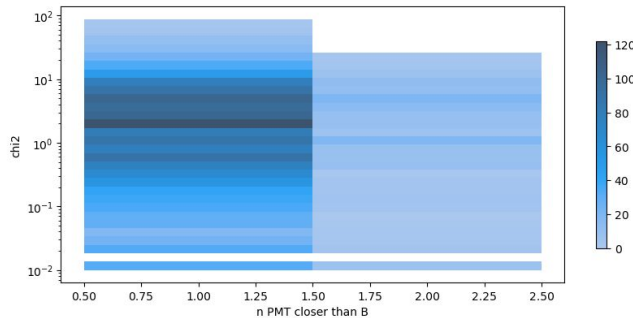
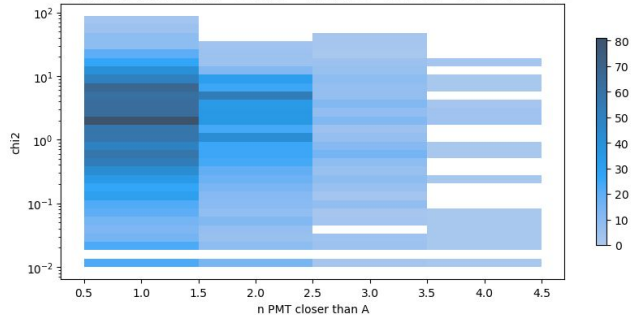
$\chi^2$  per PMT as a function of how many PMTs are within a certain range of the photon trajectory (27.2cm, 13.8cm, 7.9cm) - Source position 0



$\chi^2$  per PMT as a function of how many PMTs are within a certain range of the photon trajectory (27.2cm, 13.8cm, 7.9cm) - Source position 2



$\chi^2$  per PMT as a function of how many PMTs are within a certain range of the photon trajectory (A = 5cm, B = 2.5cm, C = 1.25cm) - Source position 2

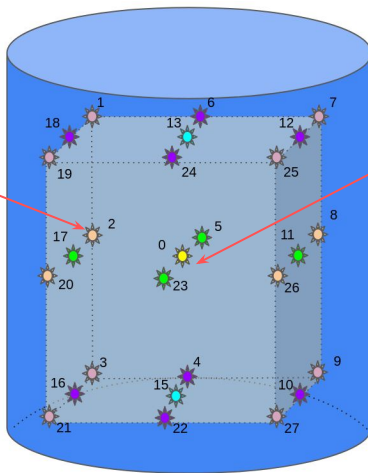


# Geometrical checks

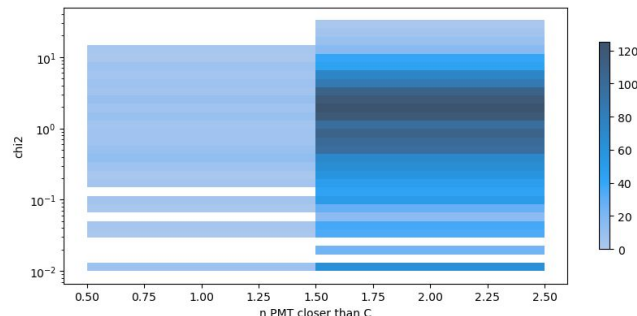
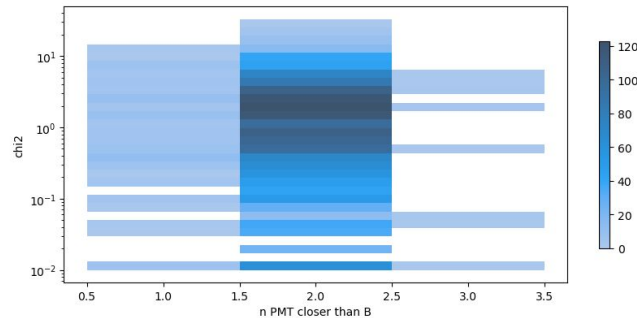
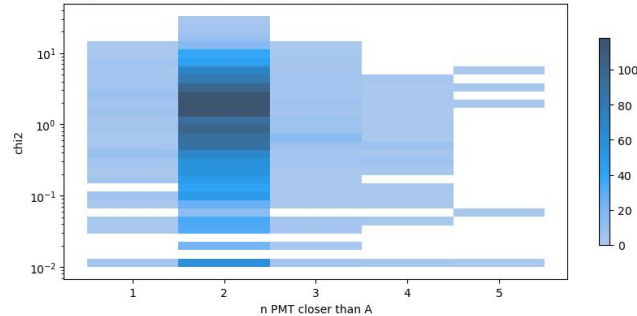
Top: total number of PMTs closer to the line of sight than  $h_{\text{mPMT}}(27.2\text{cm})$

Middle: total number of PMTs closer to the line of sight than  $h_{\text{PMT}}(13.8\text{cm})$

Bottom: total number of PMTs closer to the line of sight than  $h_{\text{PMT}}/2 (7.9\text{cm})$

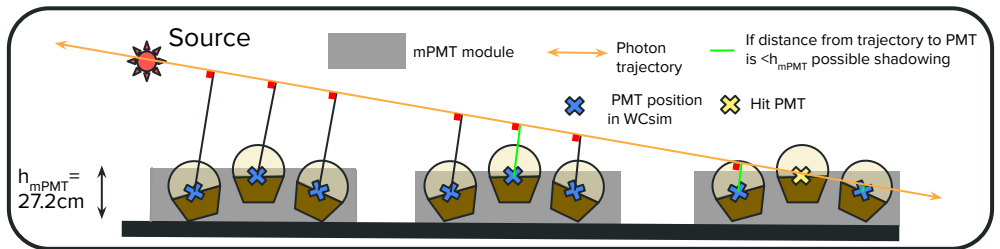
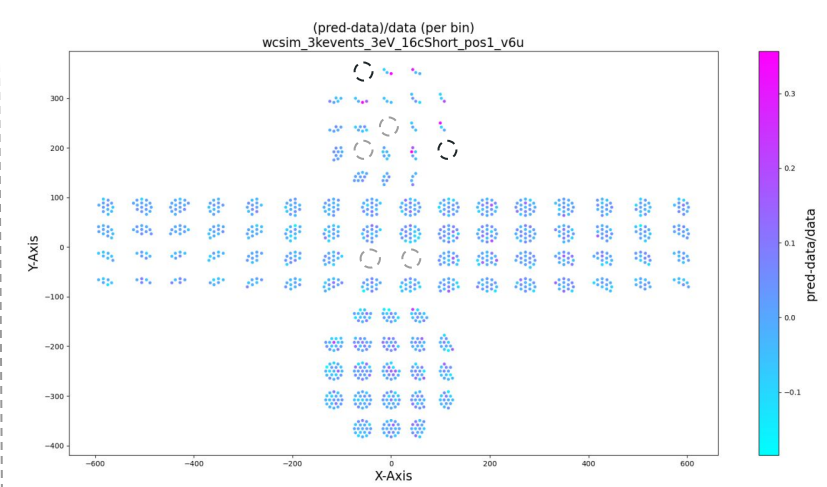
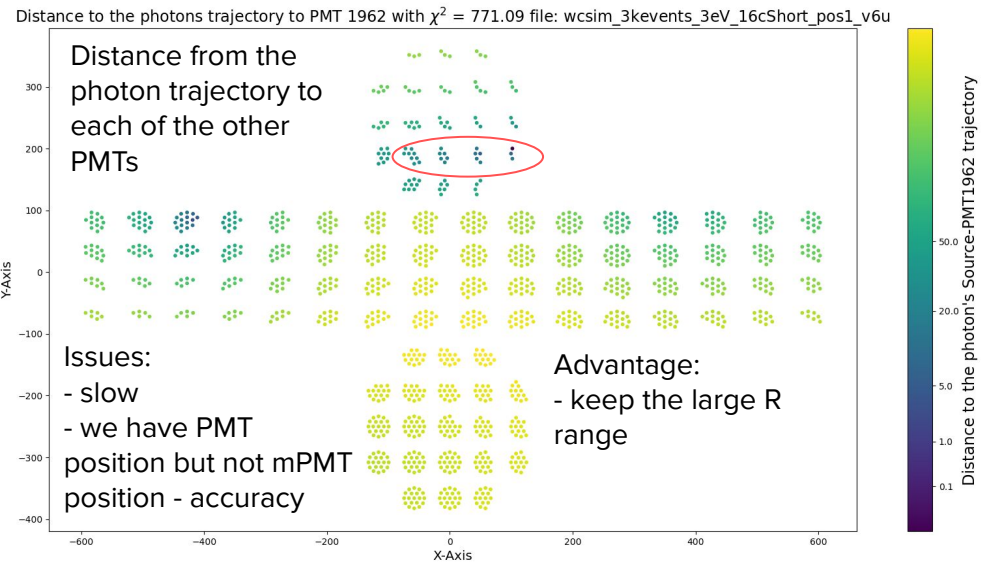


$\chi^2$  per PMT as a function of how many PMTs are within a certain range of the photon trajectory (A = 5cm, B = 2.5cm, C = 1.25cm) - Source position 5



# Possible other fixes: **Option 2: mask (m)PMT as required**

For each source-PMT trajectory -> check the distance between the trajectory and each PMT -> if dist to any PMT is < thresh: mask

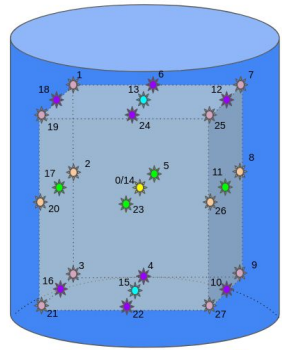
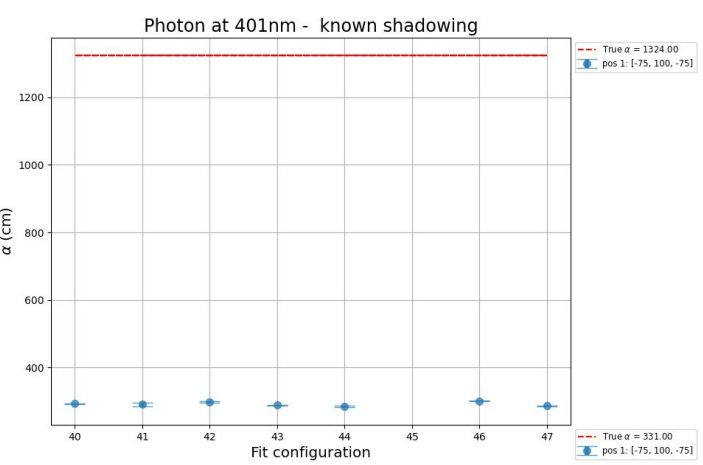
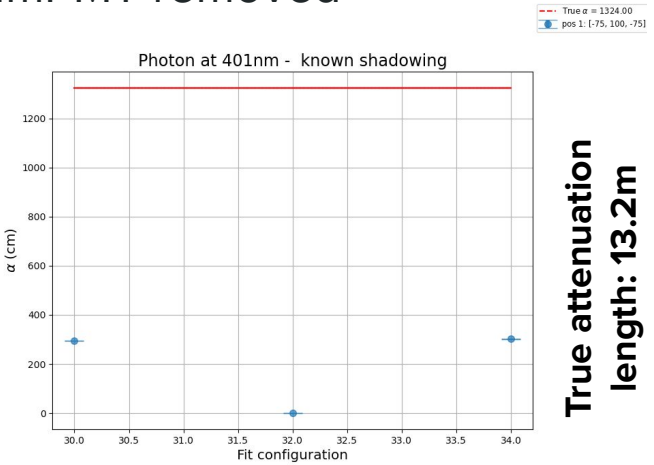


Above: simply removed the two most problematic mPMTs.  
Less accurate than simply displacing the source

# Attenuation length with shadowing

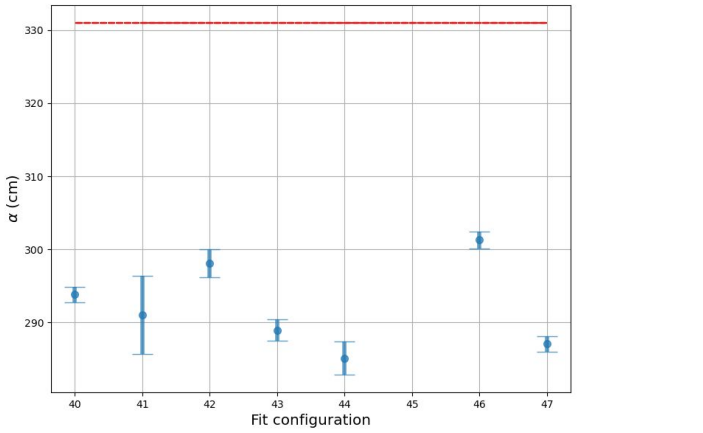
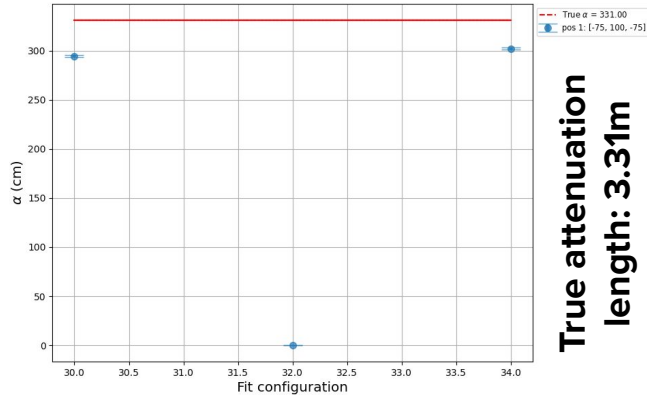
## 2mPMT removed

$$PE_{\text{predicted}} = \text{Norm} \times \exp\{-R/\alpha\} \times \omega \times \text{Angular Response}(\cos(\theta))$$



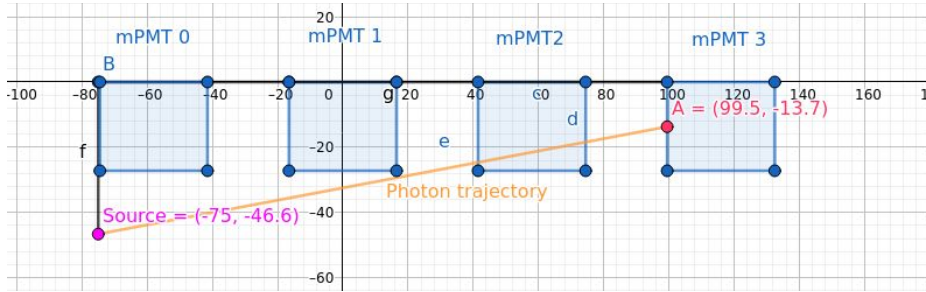
Configurations:

- 30: Unbinned PMT, polynomial A.R. timetof < 0.15ns, 0.5 < costh
- 32: 30 (0.6 < costh < 0.8)
- 34: 30 (timetof < 0.25ns)



- 40: Unbinned PMT, binned A.R. timetof < 0.15ns, costh>0.5
- 41: 40 (only central PMT)
- 42: 40 (first ring of PMTs)
- 43: 40 (second ring of PMTs)
- 44: 40 (R>100cm)
- 46: 40 (timetof < 0.25ns)
- 47: 40 (timetof < 0.05ns)

# Geometrical check where there is known shadowing

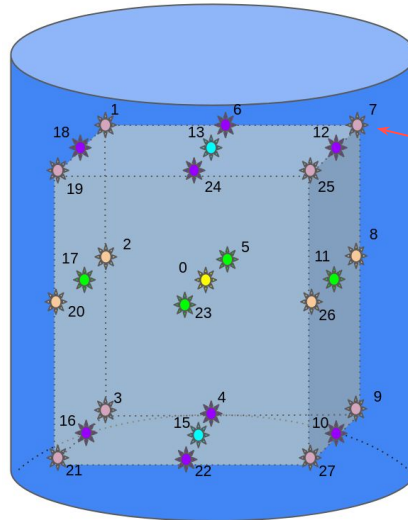


Top: total number of PMTs closer to the line of sight than  $h_{\text{mPMT}}$  (27.2cm)

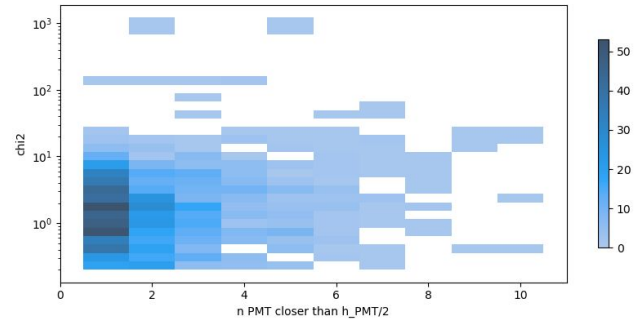
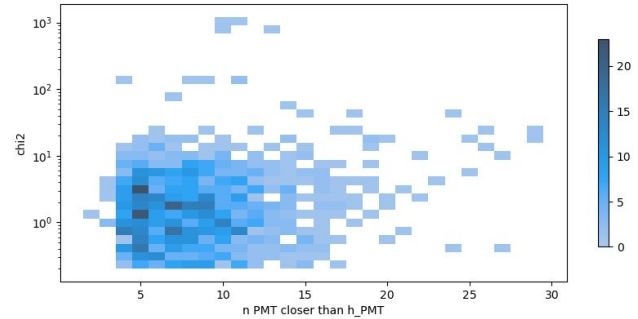
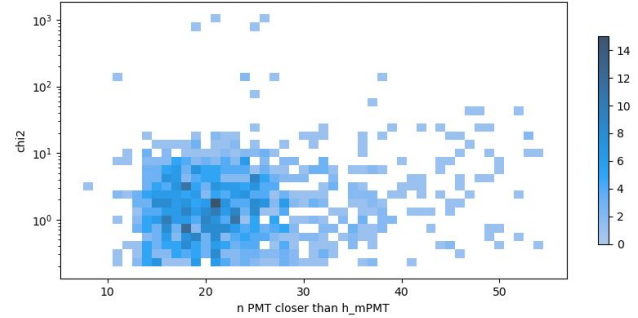
Middle: total number of PMTs closer to the line of sight than  $h_{\text{PMT}}$  (13.8cm)

Bottom: total number of PMTs closer to the line of sight than  $h_{\text{PMT}}/2$  (7.9cm)

Nothing very obvious is coming out of this...

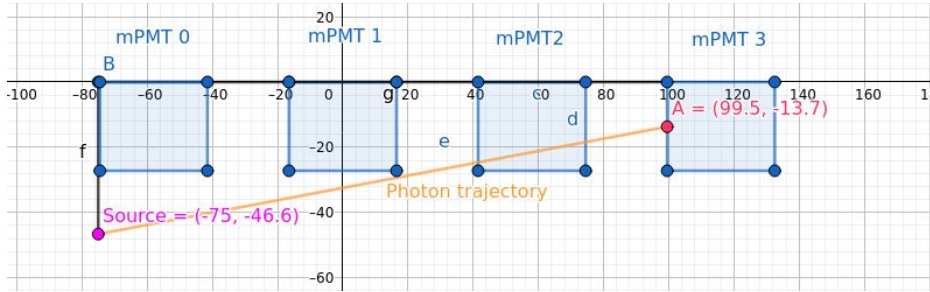


$\chi^2$  per PMT as a function of how many PMTs are within a certain range of the photon trajectory (27.2cm, 13.8cm, 7.9cm) - Source position 7





# Geometrical check where there is known shadowing

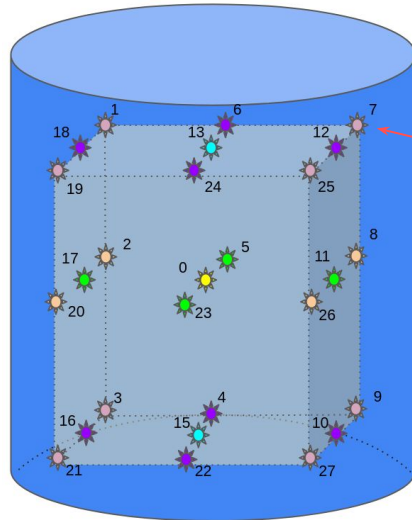


Top: total number of PMTs closer to the line of sight than  $h_{\text{mPMT}}$  (27.2cm)

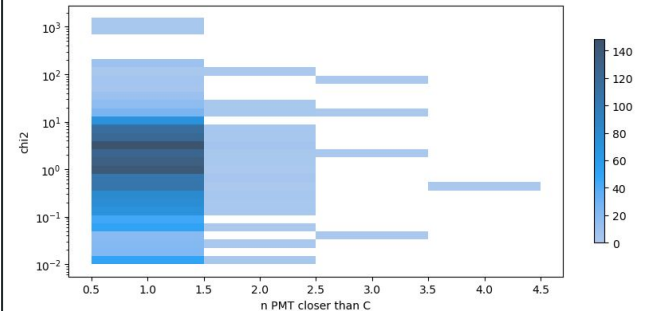
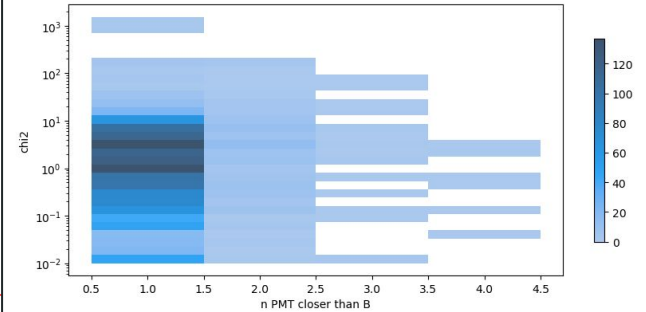
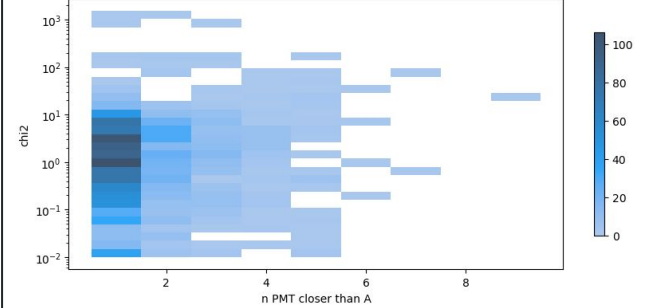
Middle: total number of PMTs closer to the line of sight than  $h_{\text{PMT}}$  (13.8cm)

Bottom: total number of PMTs closer to the line of sight than  $h_{\text{PMT}}/2$  (7.9cm)

Nothing very obvious is coming out of this...



$\chi^2$  per PMT as a function of how many PMTs are within a certain range of the photon trajectory ( $A = 5\text{cm}$ ,  $B = 2.5\text{cm}$ ,  $C = 1.25\text{cm}$ ) - Source position 7



# Investigation of alpha estimate

$\Delta\alpha = \alpha_{\text{alpha fixed at true value, norm fitted}} - \alpha_{\text{alpha fitted, norm fixed @ best fit value obtained from previous fit where } \alpha \text{ was fixed @ its true value}}$

$\Delta\chi^2 = \chi^2_{\text{alpha fixed at true value, norm fitted}} - \chi^2_{\text{alpha fitted, norm fixed @ best fit value obtained from previous fit where } \alpha \text{ was fixed @ its true value}}$

Unibinned fit (1333 bins) Source in pos 2	$\Delta\alpha$	$\Delta\chi^2$
10 bins in costh [0.5, 1.01]	6677.84 - 4103.64 = 2574.20 cm	3369- 3266 = 103
20 bins in costh [0.5, 1.01]	6677.84 - 3758.36 = 2919.48 cm	2224- 2101 = 123

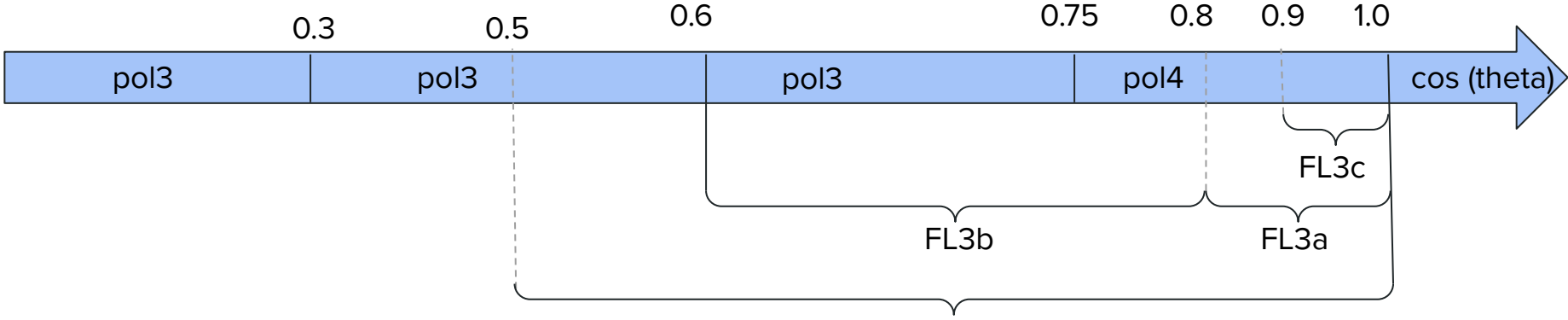
It looks like more freedom in the angular response fits the distribution better but biases against  $\alpha$  which is then fitted further away from its true value. Too many  $\Theta$ -dependant fit parameters?

In this case the three rings parameterization was used.

Best fit norm (alpha fixed) is quite far from the calculated value (~70% smaller -> did I forget Q.E.?)

# Other investigations - cos(theta) portions @ 401.9nm

Fit PMTs: unbinned, Angular response: polynomial



pos 2

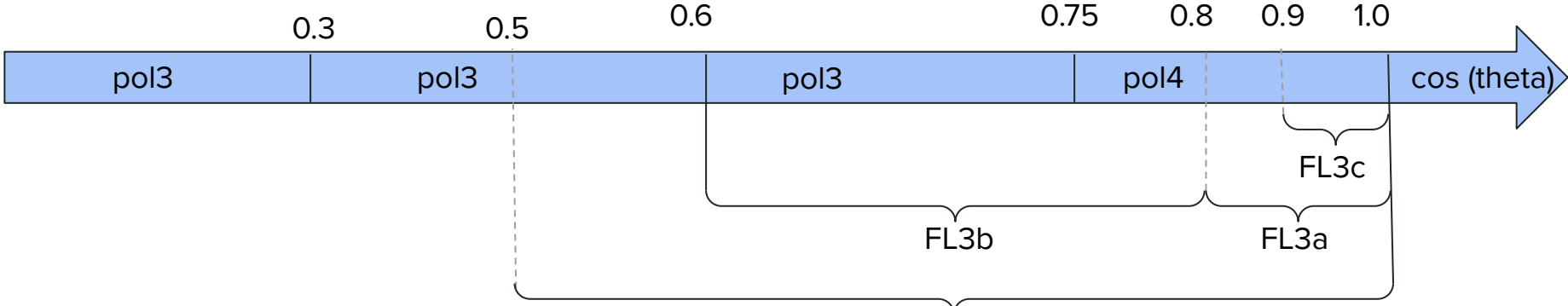
No DN		FL3	FL3a	FL3b	FL3c
401nm-pos2 alpha = 107m	chi2 alpha	Inf 0.02 +/- 0	1.53 37.9 +/- 2.2	1.40 44.5 +/- 4.3	1.43 35.4 +/- 2.5
401nm-pos2 alpha = 3.31m	chi2 alpha	1.43 2.9 +/- 0.01	Inf 0.02 +/- 0	1.28 2.9 +/- 0.02	10.8 9.8 +/- 0.2
401nm-pos2 alpha = 13.24m	chi2 alpha	1.53 10.2 +/- 0.1	1.62 9.8 +/- 0.2	1.31 10.8 +/- 0.3	1.48 9.5 +/- 0.2

pos 5

No DN		FL3	FL3a	FL3b	FL3c
401nm-pos5 alpha = 107m	chi2 alpha	1.20 51.3 +/- 4.5	1.16 41.0 +/- 3.6	1.23 74.3 +/- 17	1.21 40.4 +/- 4.8
401nm-pos5 alpha = 3.31m	chi2 alpha	1.39 3.1 +/- 0.01	40.6 100 +/- inf	1.44 3.1 +/- 0.03	1.44 3.1 +/- 0.03
401nm-pos5 alpha = 13.24m	chi2 alpha	1.36 13.9 +/- 0.3	1.40 13.7 +/- 0.4	1.25 14.3 +/- 0.6	

# Other investigations - cos(theta) portions @ 353.7nm

Fit PMTs: unbinned, Angular response: polynomial



pos 2

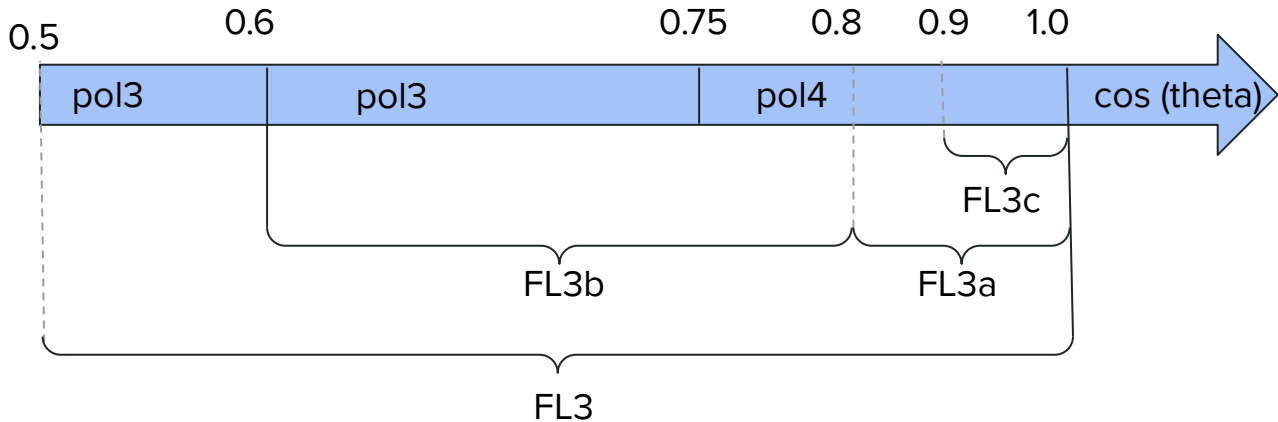
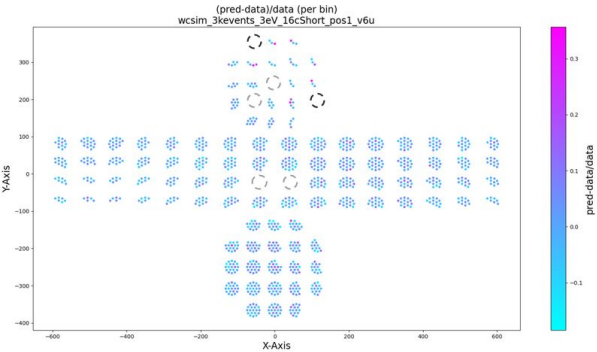
No DN		FL3	FL3a	FL3b	FL3c
353nm-pos2 alpha = 66.8m	chi2 alpha				
353nm-pos2 alpha = 2.5m	chi2 alpha				
353nm-pos2 alpha = 10.0m	chi2 alpha				

pos 5

No DN		FL3	FL3a	FL3b	FL3c
353nm-pos5 alpha = 66.8m	chi2 alpha				
353nm-pos5 alpha = 2.5m	chi2 alpha				
353nm-pos5 alpha = 10.0m	chi2 alpha				

# Other investigations - cos(theta) portions pos 1 with 2 mPMTs removed

## Fit PMTs: unbinned, Angular response: polynomial



pos 1 - 353.7nm

No DN		FL3	FL3a	FL3b	FL3c
353nm-pos2 alpha = 66.8m	chi2 alpha				
353nm-pos2 alpha = 2.5m	chi2 alpha				
353nm-pos2 alpha = 10.0m	chi2 alpha				

pos 1 - 401.9nm

No DN		FL3	FL3a	FL3b	FL3c
401nm-pos5 alpha = 66.8m	chi2 alpha				
401nm-pos5 alpha = 2.5m	chi2 alpha				
401nm-pos5 alpha = 10.0m	chi2 alpha				

# Other investigations - ring selection @ 401.9nm

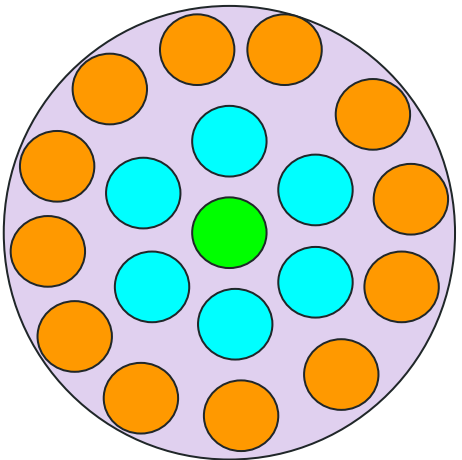
mPMT module

pos 2

No DN		FL4	FL4a	FL4b	FL4c
401nm-pos2 alpha = 66.8m	chi2 alpha				
401nm-pos2 alpha = 2.5m	chi2 alpha				
401nm-pos2 alpha = 10.0m	chi2 alpha				

**Fit:**

Unbinned PMTs  
Binned angular response (20 bins)  
 $0.5 < \text{costh} < 1.01$



pos 5

No DN		FL4	FL4a	FL4b	FL4c
401nm-pos2 alpha = 66.8m	chi2 alpha				
401nm-pos2 alpha = 2.5m	chi2 alpha				
401nm-pos2 alpha = 10.0m	chi2 alpha				

pos 1 - 2mPMT masked

No DN		FL4	FL4a	FL4b	FL4c
401nm-pos2 alpha = 66.8m	chi2 alpha				
401nm-pos2 alpha = 2.5m	chi2 alpha				
401nm-pos2 alpha = 10.0m	chi2 alpha				

# Other Investigations - Timetof cuts @ 401.9nm

pos 5

No DN		FL3	FL3d	FL3e	FL4	FL4f	FL4g
401nm-pos5 alpha = 66.8m	chi2 alpha						
401nm-pos5 alpha = 2.5m	chi2 alpha						
401nm-pos5 alpha = 10.0m	chi2 alpha						

pos 2

No DN		FL3	FL3d	FL3e	FL4	FL4f	FL4g
401nm-pos2 alpha = 66.8m	chi2 alpha						
401nm-pos2 alpha = 2.5m	chi2 alpha						
401nm-pos2 alpha = 10.0m	chi2 alpha						

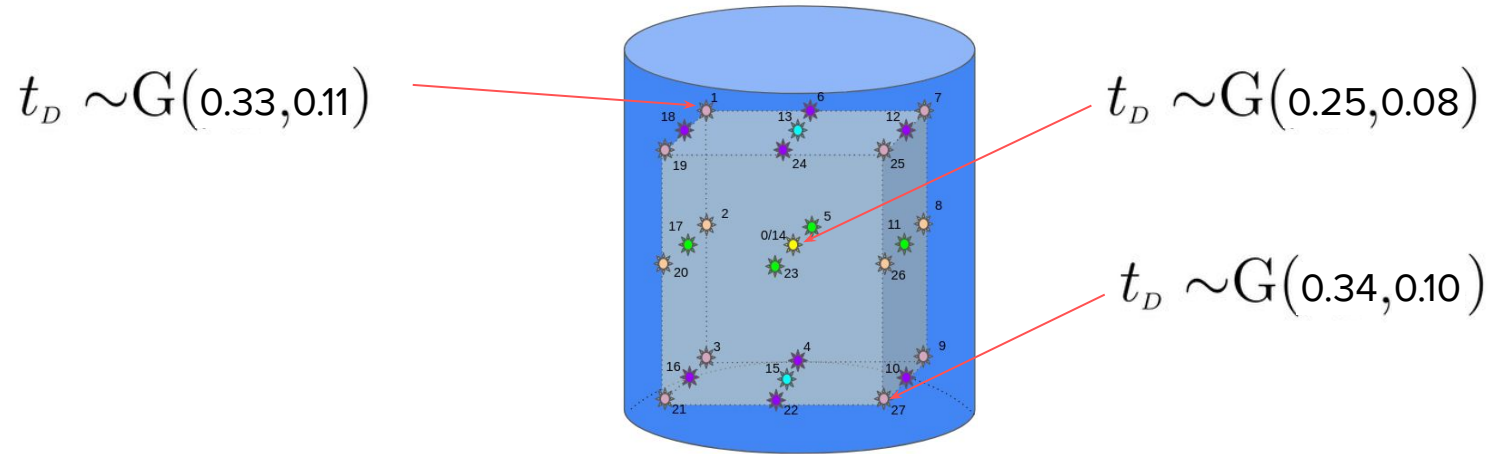
PMT: unbinned	0.05ns	0.15ns	0.25ns
Angular response polynomial	FL3e	FL3	FL3d
Angular response binned	FL4g	FL4	FL4f

pos 1 - 401.9nm

No DN		FL3	FL3d	FL3e	FL4	FL4f	FL4g
401nm-pos5 alpha = 66.8m	chi2 alpha						
401nm-pos5 alpha = 2.5m	chi2 alpha						
401nm-pos5 alpha = 10.0m	chi2 alpha						

# Timing calibration - Results

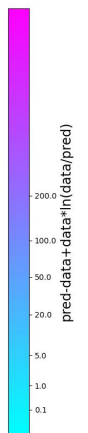
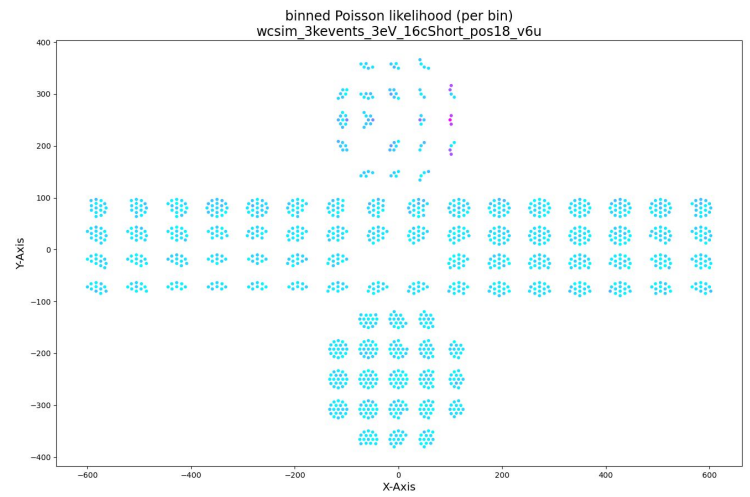
The source at centre of the detector provides better calibration than when on more extreme positions.



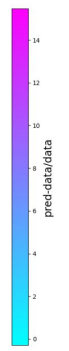
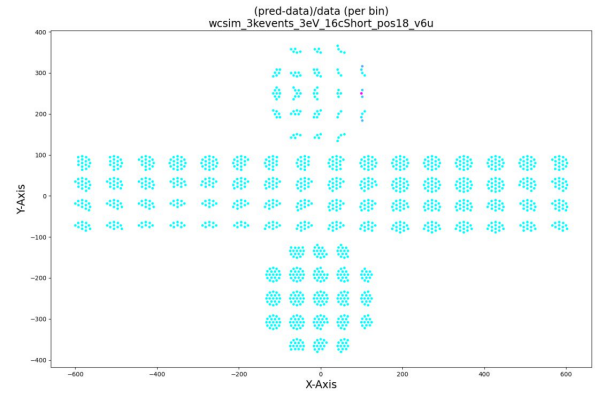
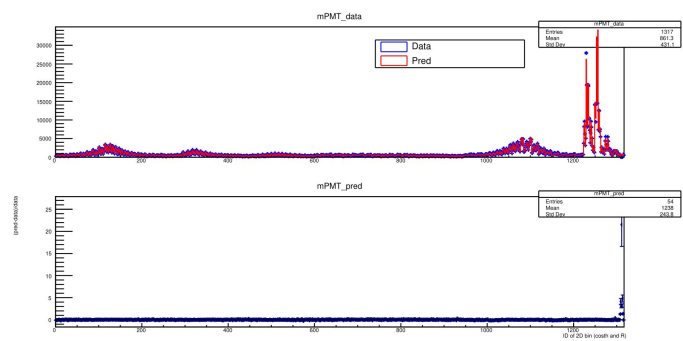
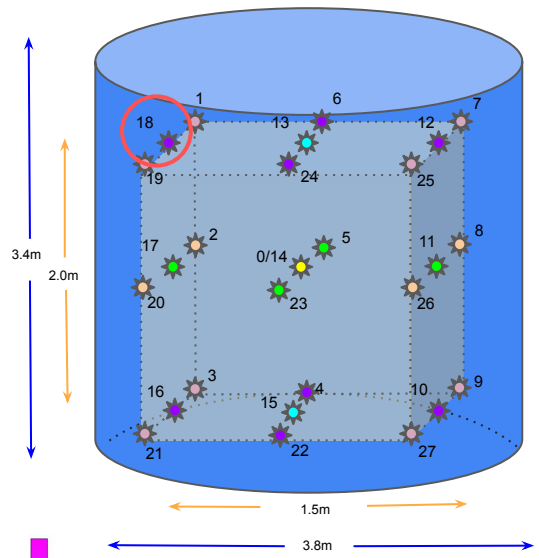
Geometry comparison -  ${}^{16}\text{C}4\text{r}$   $t_D \sim G(0.25, 0.08)$  similar to  ${}^{16}\text{C}5\text{r}$   $t_D \sim G(0.25, 0.06)$  for source at the centre of the tank.



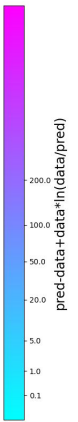
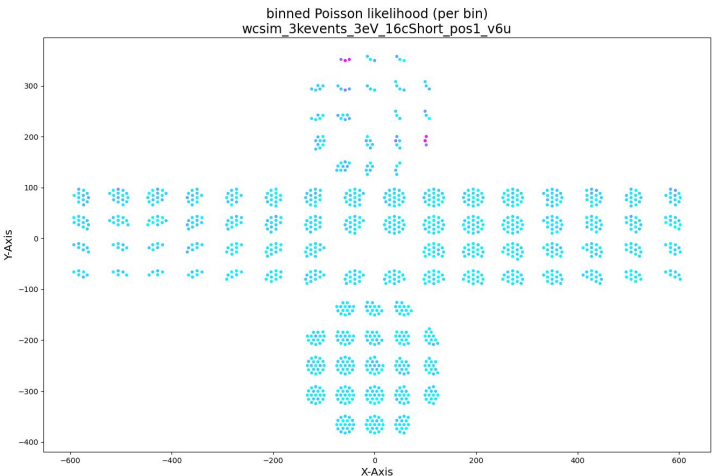
# Fit failures - 125 cm away from centre of the tank



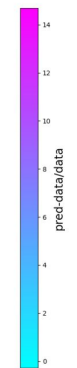
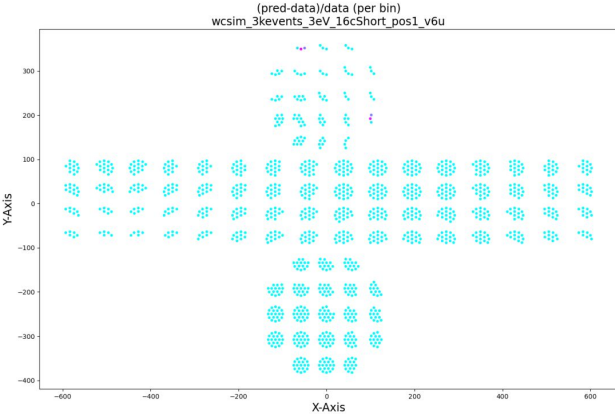
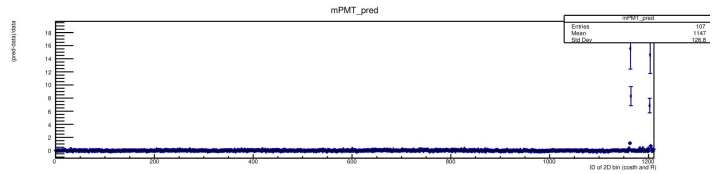
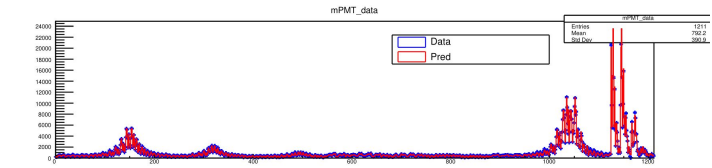
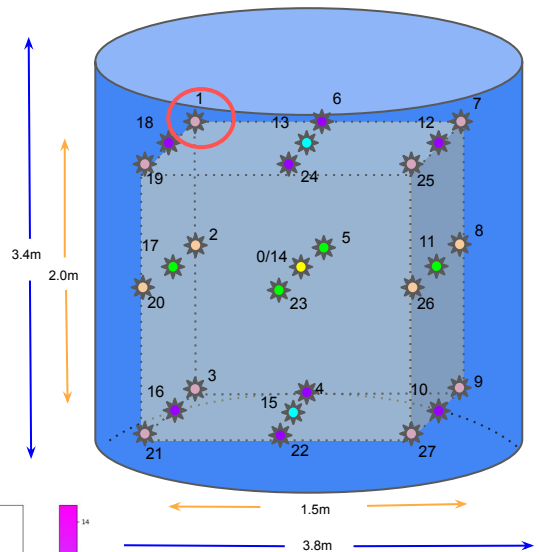
~10 times more hits predicted compared to observed.



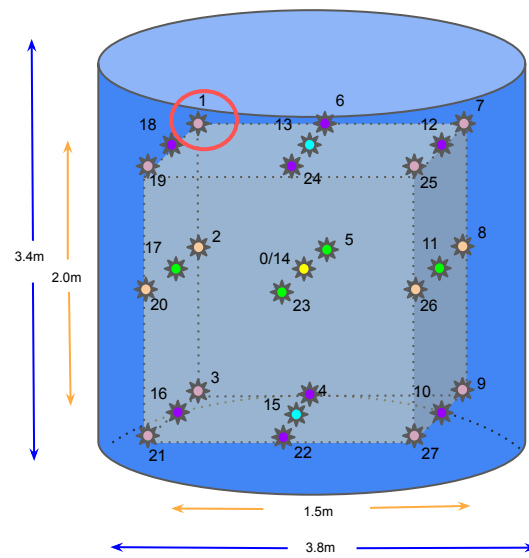
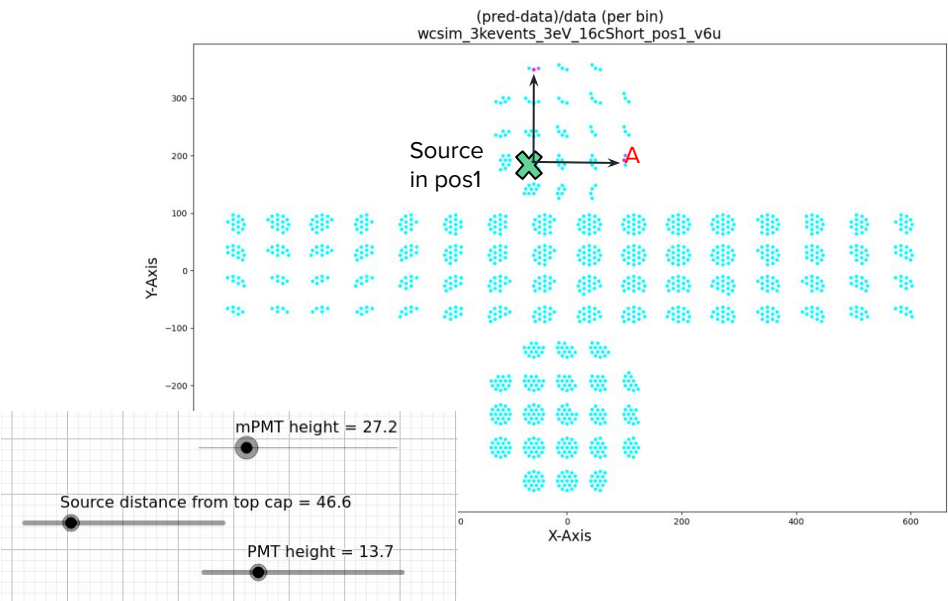
# Fit failures - 146 cm away from centre of the tank



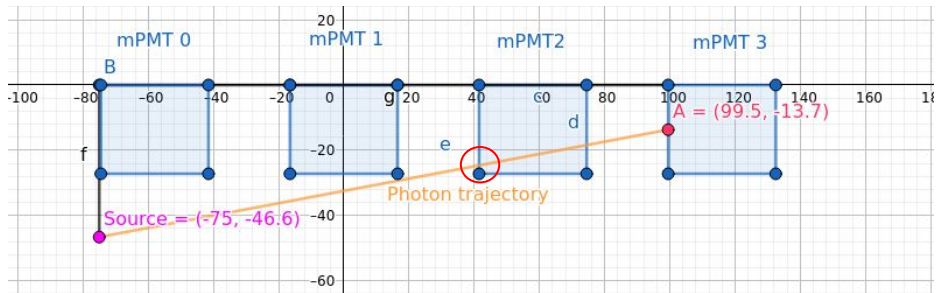
~10 times more hits predicted compared to observed.



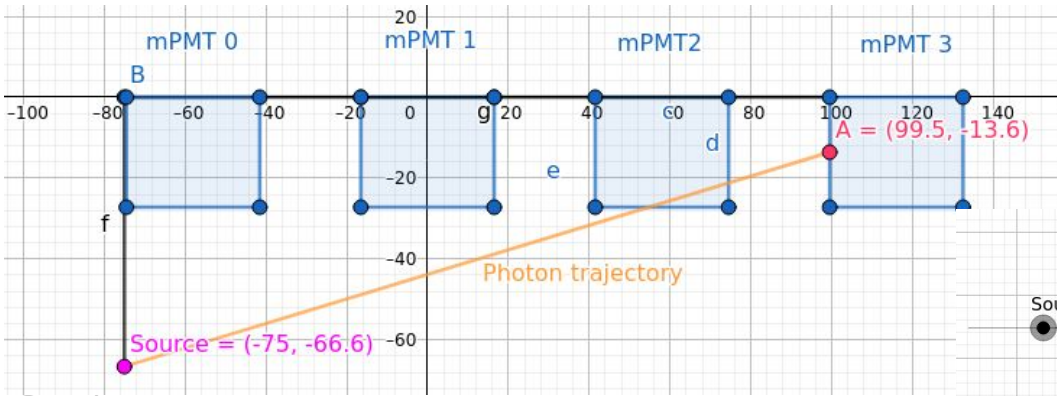
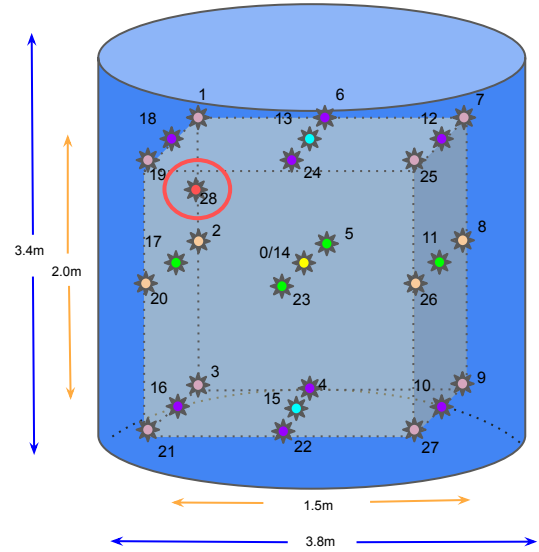
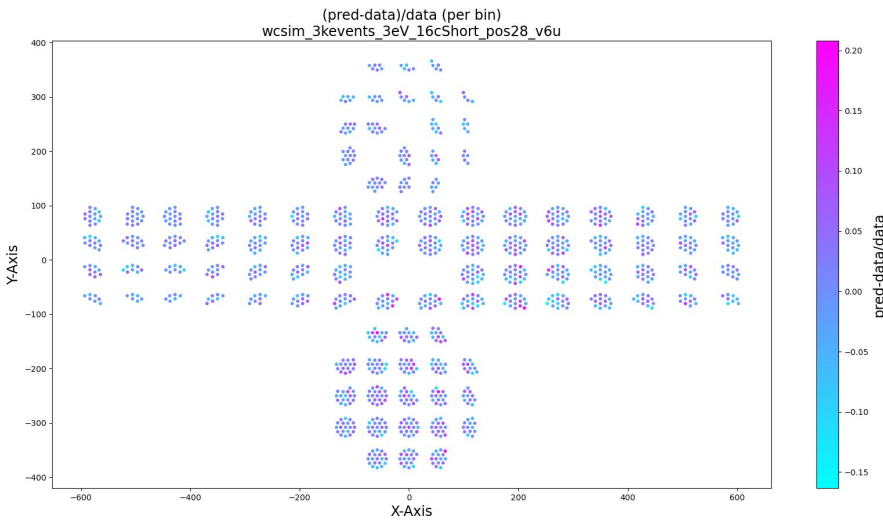
# Explanation: shadowing by the mPMT surface



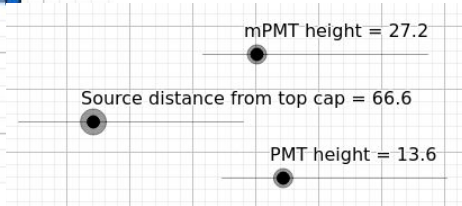
- **Assumed** that the PMT point in WCSim is at the centre of the height of the mPMT module
- Light absorption by outside mPMT surface
- No excess p.e. recorded at mPMT2 - expect that the light is absorbed by outer cover and not detected by the mPMT2 module's PMTs



# Fix1: lowering the source

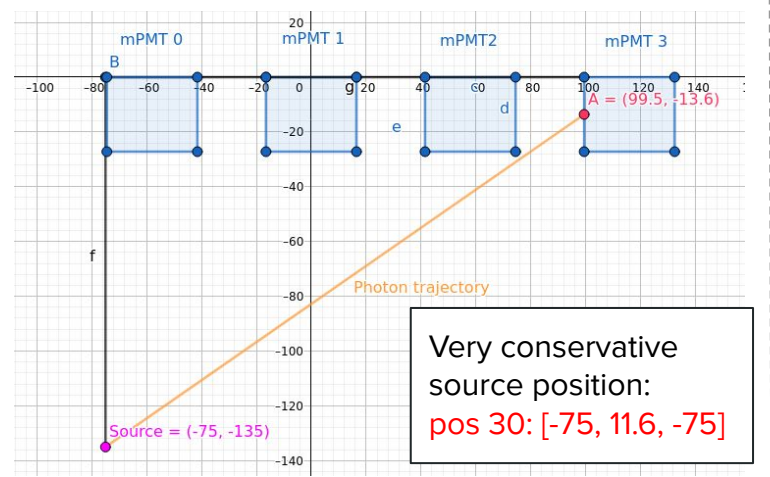


Instead of pos1: [-75, 100, -75]  
 Have source at pos 28: [-75, 80, -75]

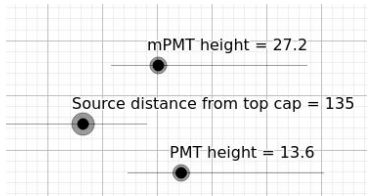


Also improves the PMT coverage!

# Long term fix: Option 1: very conservative source position

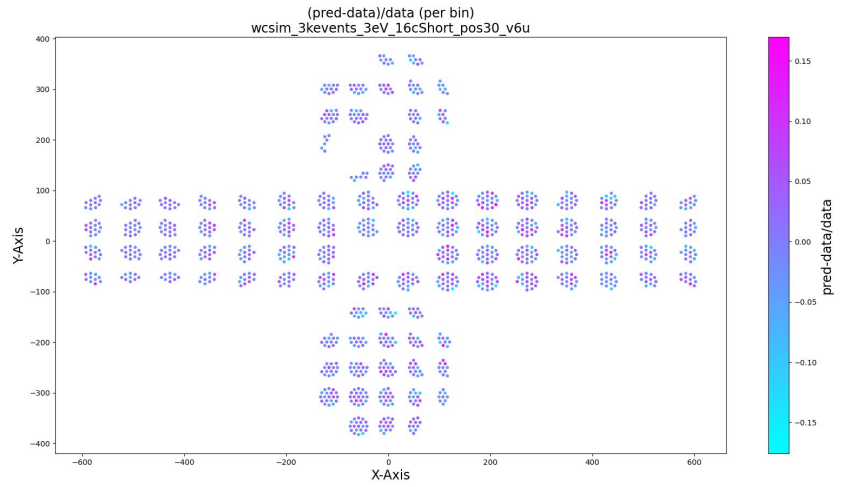
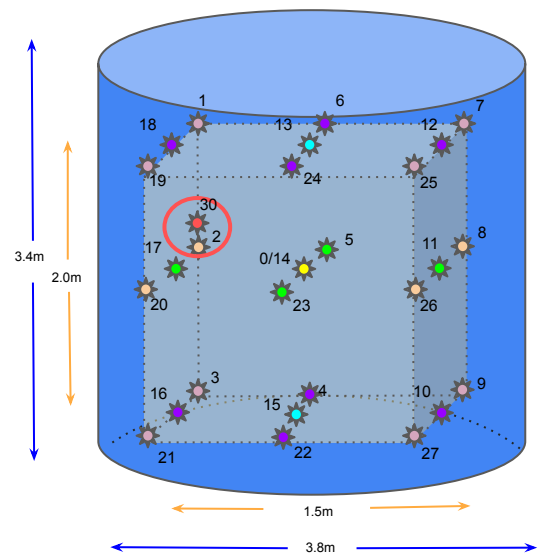


Very conservative source position:  
 pos 30: [-75, 11.6, -75]

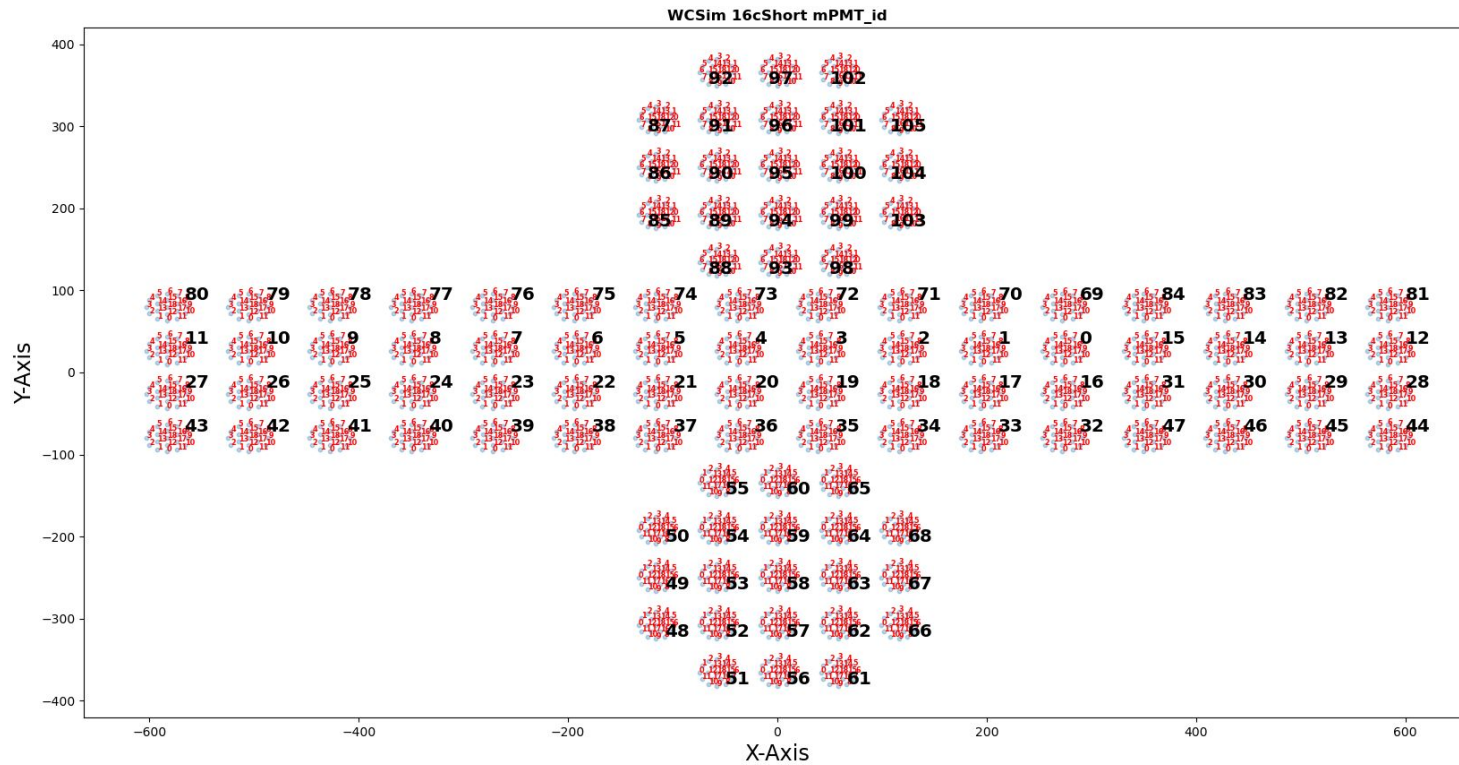


Issues:  
 - reduces our R range

Advantage:  
 - faster calibration procedure



# Geometry



# Time of

