

# **CPV and mixing** in the B and D system





1.6.2023 **Alexander Lenz** Siegen







- Intro: Meson decays and Mixing
- Intro: 3 Kinds of CPV violation
- Status Quo: Mixing & CPV in mixing
  - Non-perturbative determination of bag parameter
  - Newest results for  $\Delta\Gamma$ ,  $\Delta M$  and  $a_{fs}$
  - Peculiarities of Charm mixing
  - Alternative Renormalisation scale setting changes for  $a_{fs}$
- Status Quo: CPV in interference
  - Penguin pollution
  - Relation to CPV in mixing
- Status Quo: Direct CPV
  - $\Delta A_{CP}$
  - QCD factorisation for non-leptonic B decays a new anomaly?
  - Flavour Specific CP asymmetries

# Outline



**Experimental aspects: Justin Skorupa** Valeria Lukashenko **Alexander Thaler Ramon Angel Ruiz Fernandez Jake Bennett** Serena Maccolini



### see e.g. Eleftheria Somonidi

For a recent comprehensive review of CPV results see e.g. Gershon, Nir in PDG







# t,c,u W t,c,u

 $|M_{12}|$ ,  $|\Gamma_{12}|$  and  $\phi = \arg(-M_{12}/\Gamma_{12})$  can be related to three observables:

• Mass difference:  $\Delta M := M_H - M_L \approx 2 |M_{12}|$  (off-shell)  $|M_{12}|$ : heavy internal particles: t, SUSY, ...

• Decay rate difference:  $\Delta \Gamma := \Gamma_L - \Gamma_H \approx 2 |\Gamma_{12}| \cos \phi$  (on-shell)  $|\Gamma_{12}|$ : light internal particles: u, c, ... (almost) no NP!!!

$$\begin{array}{c} \mathbf{g} \\ |B_{q,L}\rangle &= p|B_{q}\rangle + q|\bar{B}_{q}\rangle \\ |B_{q,H}\rangle &= p|B_{q}\rangle - q|\bar{B}_{q}\rangle \end{array}$$

$$\begin{array}{c} \mathbf{d} \\ \mathbf{b} \\ \mathbf{b} \\ \mathbf{d} \\ \mathbf{b} \\ \mathbf{d} \\ \mathbf{d$$







$$\Gamma\left[\bar{B}_{q}(t) \to f\right] = N_{f} \left|\mathcal{A}_{f}\right|^{2} \frac{\left(1+|\lambda_{f}|^{2}\right)}{2} \left(1+a_{\mathrm{fs}}^{q}\right) e^{-\Gamma_{q}t} \left\{\cosh\left(\frac{\Delta\Gamma_{q}t}{2}\right) - \frac{1-|\lambda_{f}|^{2}}{1+|\lambda_{f}|^{2}}\cos\left(\Delta M_{q}t\right) - \frac{2\operatorname{Re}(\lambda_{f})}{1+|\lambda_{f}|^{2}}\sin\left(\frac{\Delta\Gamma_{q}t}{2}\right) + \frac{2\operatorname{Im}(\lambda_{f})}{1+|\lambda_{f}|^{2}}\sin\left(\Delta M_{q}t\right)\right\},$$

With

$$\mathcal{A}_f = \langle f | \mathcal{H}_{ ext{eff}} | B_q 
angle \,, \qquad ar{\mathcal{A}}_f = \langle f | \mathcal{H}_{ ext{eff}} | ar{B}_q 
angle \,, \qquad egin{array}{c} \lambda_f = rac{q}{p} rac{ar{\mathcal{A}}_f}{\mathcal{A}_f} \,, \ p \mid egin{array}{c} \lambda_f = \langle f | \mathcal{H}_{ ext{eff}} | ar{B}_q 
angle \,, \ egin{array}{c} \lambda_f = rac{q}{p} rac{ar{\mathcal{A}}_f}{\mathcal{A}_f} \,, \ egin{array}{c} \lambda_f = \langle f | \mathcal{H}_{ ext{eff}} | ar{B}_q 
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angle \,, \ egin{array}{c} \lambda_f = rac{q}{p} rac{ar{\mathcal{A}}_f}{\mathcal{A}_f} \,, \ egin{array}{c} \lambda_f = rac{A}{p} \,, \ egin{array}{c} \lambda_f \,, \ egin{array}{c} \lambda_f = rac{A}{p} \,, \ egin{array}{c} \lambda_f \,, \$$

and the tiny quantity  $a_{fs}^q$  to be defined below

# Mixing



Time evolution of neutral B mesons (quantum mechanics on a macroscopic scale)











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Status Quo: CPV in interference

Status Quo: Direct CPV

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$$A_{\rm fs}^q = \frac{\Gamma\left(\bar{B}_q(t) \to f\right) - \Gamma\left(B_q(t) \to \bar{f}\right)}{\Gamma\left(\bar{B}_q(t) \to f\right) + \Gamma\left(B_q(t) \to \bar{f}\right)} \xrightarrow[\text{Priod}{P}]{A_{\bar{f}} = A_f} = a_{\rm fs}^q \approx \frac{|\Gamma_{12}^q|}{|M_{12}^q|} \sin\phi_{12}^q$$

2. CP violation in interference of mixing and decay

$$A_{\text{ind}}^{q} = \frac{\Gamma\left(\bar{B}_{q}(t) \to f\right) - \Gamma\left(B_{q}(t) \to f\right)}{\Gamma\left(\bar{B}_{q}(t) \to f\right) + \Gamma\left(B_{q}(t) \to f\right)} \qquad \begin{array}{c} \text{e.g. } B_{s} \to J/\Psi\phi \\ \text{or } B_{d} \to J/\Psi K_{s} \end{array} \qquad \begin{array}{c} \text{See also} \\ \text{1511.094} \\ \text{hep-ph/020} \end{array}$$

## 3. CP violation in decay

$$A_{\rm dir}^q = \frac{\Gamma\left(\bar{B}_q(t) \to \bar{f}\right) - \Gamma\left(B_q(t) \to f\right)}{\Gamma\left(\bar{B}_q(t) \to \bar{f}\right) + \Gamma\left(B_q(t) \to f\right)} = \frac{\left|\bar{\mathcal{A}}_{\bar{f}}\right|^2 - \left|\mathcal{A}_f\right|^2}{\left|\bar{\mathcal{A}}_{\bar{f}}\right|^2 + \left|\mathcal{A}_f\right|^2}$$

# **CP** Violation



## 1. CP violation in Mixing: Consider a flavour specific ( $A_{\bar{f}} = 0 = \bar{A}_f$ ) decay $B \to f$

e.g. 
$$B \to X l \nu$$
  
or  $\bar{B}_s \to D_s^+ \pi^-$   
or  $\bar{B}_d \to D^+ K^-$ 

e.g.  $\Delta A_{CP}$ or  $D^0 \rightarrow \pi^- \pi^+, K^- K^+$ 









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# Status Quo: Mixing

 $\Delta M_s = 2 |M_{12}^s|$ 



Significant CKM dependence

Ł 3 6

### **2-loop: Buras, Jamin, Weisz** 3-loop: Gorbahn, Stamou,.....

$$Q = \bar{s}^{\alpha} \gamma_{\mu} (1 - \gamma_5) b^{\alpha} \times \bar{s}^{\beta} \gamma^{\mu} (1 - \gamma_5) b^{\beta}$$

$$\langle Q \rangle \equiv \langle B_s^0 | Q | \bar{B}_s^0 \rangle = \frac{8}{3} M_{B_s}^2 f_{B_s}^2 B(\mu)$$



### By far dominant uncertainty



### **HQET-sum rules: 3-loop + part of NNLO matching:**

\* $B_{A}$  mixing: Siegen: Grozin, Klein, Mannel, Pivovarov 1606.06054, 1706.05910, 1806.00253 \* $B_d$  and D mixing,  $D^0$ ,  $D^+$ ,  $B_d$  and  $B^+$  lifetimes Durham: Kirk (Rome), AL, Rauh (Bern) 1711.02100  $*B_{\rm s}$  mixing Durham: King, AL, Rauh (Bern) 1904.00940 \* $B_{\rm s}$  and  $D_{\rm s}^+$  lifetimes Siegen: King (Durham), AL, Rauh (Bern) 2112.03691

### See also talk by Stefan Meinel







 $\Delta M_d = (0.5065 \pm 0.0019) \,\mathrm{ps}^{-1}$ 

 $\Delta M_s = (17.765 \pm 0.006) \,\mathrm{ps}^{-1}$ 

 $\Delta M_d = (0.533^{+0.022}_{-0.036}) \text{ ps}^{-1}$  $\Delta M_s = (18.4^{+0.7}_{-1.2}) \text{ ps}^{-1}$ 



 $\Delta M_s [ps^{-1}]$ 

# Status Quo: Mixing

![](_page_8_Picture_7.jpeg)

### $\delta$ (Theo.)/ $\delta$ (Exp.) $\approx 140$

 $\delta$ (Theo.)/ $\delta$ (Exp.)  $\approx 15$ 

### 12 April 2021: Fascinating quantum mechanics.

Precise determination of the  $B_s^0 - \overline{B}_s^0$  oscillation frequency.

### "A phenomenon in which quantum mechanics gives a most remarkable prediction" - Richard Feynman

Today, the LHCb Collaboration submitted a paper for publication that reports a precise determination of the  $B_s^0 - \overline{B}_s^0$  oscillation frequency. This result is presented also today at the joint annual conference of the UK Institute of Physics (IOP), organized by the University of Edinburgh. The  $B_s^0 - \overline{B}_s^0$  oscillation is a spectacular and fascinating feature of quantum mechanics. The strange beauty particle  $B_{s}^{0}$  composed of a <u>beauty</u> antiquark ( $\overline{b}$ ) bound with a <u>strange</u> quark s turns into its antiparticle partner  $\overline{B}_{s}^{0}$ composed of a b quark and an s antiquark ( $\bar{s}$ ) about 3 million million times per second (3\*10<sup>12</sup>) as seen in the image below.

![](_page_8_Figure_14.jpeg)

http://lhcb-public.web.cern.ch

![](_page_8_Picture_17.jpeg)

![](_page_8_Picture_18.jpeg)

![](_page_9_Picture_0.jpeg)

# Status Quo: Mixing

![](_page_9_Picture_2.jpeg)

- 2035:

 $\Delta M_{c}^{\mathrm{EXP},2035} = (17.750 \pm 0.002) \,\mathrm{ps}^{-1}$ 

**Discovery of BSM with 5 standard deviations** For slides, see: https://indico.cern.ch/event/1186057/

![](_page_9_Picture_10.jpeg)

 Lattice values for dim 6 matrix elements converge •  $V_{ch}$  inclusive vs exclusive converges and direct measurement as FCC-ee

3-loop corrections known and confirmed

## $\Delta M_s^{\text{SM},2035} = (19.20 \pm 0.29) \, \text{ps}^{-1}$

![](_page_9_Picture_14.jpeg)

![](_page_10_Picture_0.jpeg)

![](_page_10_Picture_2.jpeg)

$ ilde{\Gamma}_{6}^{(1)}$	with $\langle \tilde{Q}_6 \rangle \propto f_B^2 B_{1,2,3}$ and $\langle \tilde{Q}_7 \rangle \propto f_B^2 R_{0,2,3}$ • 1998 Beneke, Buchalla, Greub, AL, Nierste • 2003 Franco, Lubicz, Mescia, Tarantino • 2003 Beneke, Buchalla, AL, Nierste • 2006 AL, Nierste				
$\tilde{\Gamma}_{6}^{(2)}$ $\tilde{\Gamma}_{7}^{(0)}$	<ul> <li>2017 partly: Asatrian, Hovhannisyan, Nierste, Yeghiazaryan</li> <li>2020 partly: Asatrian, Asatryan, Hovhannisyan, Nierste, Tumasyan</li> <li>2021 partly: Gerlach, Nierste, Shtabovenko, Steinhauser</li> <li>2022 Gerlach, Nierste, Shtabovenko, Steinhauser</li> <li>1996 Beneke, Buchalla, Dunietz</li> </ul>				
$\tilde{\Gamma}_7^{(1)}$ $ ilde{\Gamma}^{(0)}$	<ul> <li>2001 Dighe, Hurth, Kim</li> <li>202x Nierste and friends</li> <li>2007 Radin, Cabbiani, Potrov</li> </ul>				
8	$\Delta \Gamma_{s}^{HQE} = (0.091 \pm 0.013) \mathrm{ps}^{-1} \qquad \Delta \Gamma_{s}^{HFLAV} = (0.0000000000000000000000000000000000$				
	1912.07621 HFLAV,				

# Status Quo: Mixing

![](_page_10_Picture_5.jpeg)

$$_{6}\rangle + \frac{\Lambda^{4}}{m_{b}^{4}}\tilde{\Gamma}_{7}\langle \tilde{Q}_{7}\rangle + \dots$$

$$J_{3}, m_{s}/m_{b}f_{B}^{2}B_{4,5}$$
 and  $\tilde{\Gamma}_{i} = \tilde{\Gamma}_{i}^{(0)} + \frac{\alpha}{4\pi}\tilde{\Gamma}_{i}^{(1)} + \dots$ 

- $B_1$  the same as for  $\Delta M$ ,  $B_{2,3,4,5}$  new
- 2016 FNAL/MILC
- $\langle \tilde{Q}_6 \rangle$ • 2016-18 Grozin, Klein, Mannel, Pivovarov  $B_d$ 
  - 2017 Kirk, AL, Rauh  $B_d$
  - 2019 King, AL, Rauh  $B_s$
  - · 2019 HPQCD 19007.01025

$$R_2 = \frac{1}{m_b^2} (\bar{b}^{\alpha} \overleftarrow{D}_{\rho} \gamma^{\mu} (1 - \gamma^5) D^{\rho} s^{\alpha}) (\bar{b}^{\beta} \gamma_{\mu} (1 - \gamma^5) s^{\beta}$$
$$R_3 = \frac{1}{m_b^2} (\bar{b}^{\alpha} \overleftarrow{D}_{\rho} (1 - \gamma^5) D^{\rho} s^{\alpha}) (\bar{b}^{\beta} (1 - \gamma^5) s^{\beta})$$

• So far only Vacuum insertion approximation • 2019 HPQCD 1910.00970

 $(0.082 \pm 0.005) \,\mathrm{ps}^{-1}$  $(-1.3 \pm 6.6) \cdot 10^{-3} \,\mathrm{ps}^{-1}$ 

ATLAS 1605.07485

 $\langle \tilde{Q}_7 \rangle$ 

## **!FPCP2023: New LHCb**

 $\Delta \Gamma_s^{LHCB} = (0.0846 \pm 0.0050) \,\mathrm{ps}^{-1}$ 

$$\delta$$
(Theo.)/ $\delta$ (Exp.)  $\approx 2.6$ 

![](_page_10_Picture_21.jpeg)

![](_page_10_Picture_22.jpeg)

## $\Delta \Gamma_s^{\text{HQE, LYON2023}} = (0.0895 \pm 0.0131) \,\text{ps}^{-1}$

![](_page_11_Picture_1.jpeg)

# ling

![](_page_11_Picture_3.jpeg)

$$= \tilde{\Gamma}_i^{(0)} + \frac{\alpha}{4\pi} \tilde{\Gamma}_i^{(1)} + \dots$$

or  $\Delta M$ ,  $B_{2,3,4,5}$  new

Klein, Mannel, Pivovarov  $B_d$ uh  $B_d$ uh  $B_s$ D7.01025  $R_2 = \frac{1}{m_b^2} (\bar{b}^{\alpha} \overset{\leftarrow}{D}_{\rho} \gamma^{\mu} (1 - \gamma^5) D^{\rho} s^{\alpha}) (\bar{b}^{\beta} \gamma_{\mu} (1 - \gamma^5) s^{\beta})$  $R_3 = \frac{1}{m_b^2} (\bar{b}^{\alpha} \overset{\leftarrow}{D}_{\rho} (1 - \gamma^5) D^{\rho} s^{\alpha}) (\bar{b}^{\beta} (1 - \gamma^5) s^{\beta})$ 

m insertion approximation 0.00970

## **!FPCP2023: New LHCb**

 $\Delta \Gamma_s^{LHCB} = (0.0846 \pm 0.0050) \, \mathrm{ps}^{-1}$ 

 $\delta$ (Theo.)/ $\delta$ (Exp.)  $\approx 2.6$ 

![](_page_11_Picture_11.jpeg)

![](_page_11_Picture_12.jpeg)

![](_page_12_Picture_0.jpeg)

![](_page_12_Picture_1.jpeg)

![](_page_12_Figure_2.jpeg)

# Status Quo: Mixing

![](_page_12_Picture_4.jpeg)

Slide from **Ramon Angel Ruiz Fernandez** 

![](_page_13_Picture_0.jpeg)

![](_page_13_Picture_1.jpeg)

![](_page_13_Picture_2.jpeg)

### • 2035:

- •
- •

### Amazing confirmation of HQE framework

For slides, see: https://indico.cern.ch/event/1186057/

# Status Quo: Mixing

![](_page_13_Picture_11.jpeg)

Lattice and sum rule values for dim 7 matrix elements Better understanding of quark masses •  $\alpha_s/m_b$  corrections determined Lattice values for dim 6 matrix elements converge

$$\Delta \Gamma_s^{\text{SM2035}} = (0.085 \pm 0.005) \,\text{ps}^{-1}$$

 $\Delta \Gamma_{c}^{\text{HFLAV2035}} = (0.080 \pm 0.002) \, \text{ps}^{-1}$ 

![](_page_14_Picture_0.jpeg)

The charm system is theoretically more difficult than the b system since

• 
$$\alpha_s(m_c) \approx 0.34$$

$$\frac{\Lambda_{QCD}}{m_c} \approx 3 \frac{\Lambda_{QCD}}{m_b}$$

Nevertheless the Heavy Quark Expansion might still converge in the charm system

Mixing and *CP* violation in the charm system Alexander Lenz (Siegen U.), Guy Wilkinson (Oxford U.) (Nov 9, 2020) e-Print: 2011.04443 [hep-ph]

## But for mixing it gets much worse

# Status Quo: Charm Mixing

![](_page_14_Picture_8.jpeg)

### HQE seems to work for charm lifetimes

Revisiting inclusive decay widths of charmed mesons

Daniel King (Durham U., IPPP and Durham U.), Alexander Lenz (Siegen U.), Maria Laura Piscopo (Siegen U.), Thomas Rauh (U. Bern, AEC), Aleksey V. Rusov (Siegen U.) et al. (Sep 27, 2021)

Published in: *JHEP* 08 (2022) 241 • e-Print: 2109.13219 [hep-ph]

![](_page_14_Figure_13.jpeg)

Lifetimes of singly charmed hadrons James Gratrex (Boskovic Inst., Zagreb), Blaženka Melić (Boskovic Inst., Zagreb), Ivan Nišandžić (Boskovic Inst., Zagreb) (Apr 25, 2022) Published in: JHEP 07 (2022) 058, JHEP 07 (2022) 058 • e-Print: 2204.11935 [hep-ph]

### See talk by Jake Bennett

![](_page_15_Picture_0.jpeg)

## **B**-mixing

![](_page_15_Figure_3.jpeg)

![](_page_15_Picture_4.jpeg)

## D-mixing

![](_page_15_Figure_6.jpeg)

![](_page_15_Figure_7.jpeg)

![](_page_16_Picture_0.jpeg)

**B**-mixing

30

![](_page_16_Picture_2.jpeg)

CKM dominant  $\equiv$  GIM dominant CKM suppressed  $\equiv$  GIM suppressed

# Status Quo: Charm Mixing

![](_page_16_Picture_5.jpeg)

D-mixing

![](_page_16_Picture_7.jpeg)

CKM suppressed  $\equiv$  GIM dominant CKM dominant  $\equiv$  GIM suppressed

![](_page_16_Picture_9.jpeg)

![](_page_17_Picture_0.jpeg)

![](_page_17_Figure_2.jpeg)

![](_page_17_Picture_3.jpeg)

![](_page_18_Picture_0.jpeg)

pert. calculation: Bobrowski et al 1002.4794 lattice input: ETM 1403.7302; 1505.06639; FNAL/MILC 1706.04622 **HQET** sum rules: Kirk, AL, Rauh 1711.02100

![](_page_18_Picture_9.jpeg)

- The HQE is successful in the B system and for D meson lifetimes => apply it for D-mixing
  - $y_D^{\text{HQE}} \approx \lambda_s^2 \left( \Gamma_{12}^{ss} 2\Gamma_{12}^{sd} + \Gamma_{12}^{dd} \right) \approx 10^{-5} y_D^{\text{Exp.}}$ 
    - How can this be?
    - Look only at a single diagram:
    - $y_D^{\text{HQE}} \neq \lambda_s^2 \Gamma_{12}^{ss} \tau_D = 3.7 \cdot 10^{-2} \approx 5.6 y_D^{\text{Exp.}}$
  - The problem seems to originate in the extreme GIM cancellations

![](_page_19_Picture_0.jpeg)

1. Du	ality violations -	break down of HQE		1
$\Gamma_{12}^{ss}$	$\rightarrow \Gamma_{12}^{ss}(1+\delta^{ss})$ ,	20% of duality violation is sufficient to explain		3
$\Gamma_{12}^{sd}$	$\rightarrow \Gamma_{12}^{sd}(1+\delta^{sd})$ ,	experiment	$\delta^{\rm sd}$	
$\Gamma^{dd}_{12}$	$\rightarrow \Gamma_{12}^{dd}(1+\delta^{dd})$ ,	Jubb, Kirk, AL, Tetlalmatzi-Xolocotzi 2016		T
				-

**Higher dimensions** Georgi 9209291; Ohl, Ricciardi, Simmons 9301212; Bigi, Uraltsev 0005089

Idea: GIM cancellation is lifted by higher orders in the HQE overcompensating the 1/mc suppression.

Partial calculation of D=9 yields an enhancement - but not to the experimental value Bobrowski, AL, Rauh 2012

- Renormalisation scale setting: AL, Piscopo, Vlahos 2020  $\mu_x^{ss} = \mu_x^{sd} = \mu_x^{dd}$ Implicitly assumes a precision of 10^-5!
- **New Physics is present and we cannot prove it yet:-)**

![](_page_19_Picture_8.jpeg)

![](_page_19_Figure_9.jpeg)

![](_page_19_Figure_15.jpeg)

XXXXXXXXXXXX XXXXXXXXXXXX XXXXXXXXXXX

1) Vary  $\mu^{ss,dd}$  and  $\mu^{ds}$ independently between 1 GeV and 2  $m_c$  $\Rightarrow$  uncertainty increases and exp. value is covered 2) Choose scales somehow

phase space inspired as

$$\mu^{ss} = m_c - 2\epsilon$$
$$\mu^{sd} = m_c - \epsilon$$
$$\mu^{dd} = m_c$$

exp. value is covered

**Exclusive and inclusive** approaches can over the experimental regions

No precision determination possible

![](_page_19_Figure_23.jpeg)

![](_page_20_Picture_0.jpeg)

![](_page_20_Picture_1.jpeg)

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Status Quo: Direct CPV

# Outline

![](_page_20_Picture_8.jpeg)

![](_page_21_Picture_0.jpeg)

## In the ratio $\Gamma_{12}/M_{12}$ theory uncertainties are cancelling

![](_page_21_Figure_2.jpeg)

$$a_{sl}^{s,\text{Exp}} = \left(60 \pm 280\right) \cdot 10^{-10}$$
$$a_{sl}^{d,\text{Exp}} = \left(-21 \pm 17\right) \cdot 10^{-10}$$

**HFLAV 1970?** 

# Status Quo: CPV in Mixing

![](_page_21_Picture_6.jpeg)

$$\operatorname{Re}\left(\frac{\Gamma_{12}^s}{M_{12}^s}\right) = -\frac{\Delta\Gamma_s}{\Delta M_s}$$

$${\rm Im}\left(\frac{\Gamma_{12}^s}{M_{12}^s}\right) =$$

$$\frac{\Gamma_{12}^{s,uc}}{\Gamma_{12}^{s}} + \left(\frac{\lambda_u}{\lambda_t}\right)^2 \frac{\Gamma_{12}^{s,cc} - 2\Gamma_{12}^{s,uc} + \Gamma_{12}^{s,uu}}{\tilde{M}_{12}^s}$$

Imaginary part via CKM Leading contribution to  $a_{fs}$ Tiny contribution to  $\Delta\Gamma$ 

$$\frac{V_{ub}V_{ud}}{V_{tb}V_{td}} = \lambda^{0.8}$$
$$\frac{V_{ub}V_{us}}{V_{ub}V_{us}} = \lambda^{2.8}$$

**Stronger CKM suppression** Very strong GIM suppression **Imaginary part via CKM** Subleading contribution to  $a_{fs}$  and  $\Delta\Gamma$ 

$$a_{sl}^{s,\text{SM}} = \left(2.06 \pm 0.18
ight) \cdot 10^{-5}, \ a_{sl}^{d,\text{SM}} = \left(-4.73 \pm 0.42
ight) \cdot 10^{-4}.$$

### 1912.07621

![](_page_21_Picture_16.jpeg)

![](_page_22_Picture_0.jpeg)

![](_page_22_Picture_1.jpeg)

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![](_page_22_Picture_8.jpeg)

![](_page_23_Picture_0.jpeg)

$$A_{CP,f}(t) = \frac{\Gamma\left(\bar{B}_{s}^{0}(t) \to f\right) - \Gamma\left(B_{s}^{0}(t) \to f\right)}{\Gamma\left(\bar{B}_{s}^{0}(t) \to f\right) + \Gamma\left(B_{s}^{0}(t) \to f\right)} = -\frac{\mathcal{A}_{CP}^{dir}\cos(\Delta M_{s}t) + \mathcal{A}_{CP}^{mix}\sin(\Delta M_{s}t)}{\cosh\left(\frac{\Delta\Gamma_{s}t}{2}\right) + \mathcal{A}_{\Delta\Gamma}\sinh\left(\frac{\Delta\Gamma_{s}t}{2}\right)}$$

![](_page_23_Figure_3.jpeg)

If there is only one decay topology contributing to the decay

$$\mathcal{A}_{f} = \left| \mathcal{A}_{f}^{ ext{Tree}} 
ight| e^{i \left[ \phi_{ ext{Tree}}^{ ext{QCD}} + rg(\lambda_{c}) 
ight]}$$

$$ar{\mathcal{A}}_{ar{f}} = \left| \mathcal{A}_{f}^{\mathrm{Tree}} \right| e^{i \left[ \phi_{\mathrm{Tree}}^{\mathrm{QCD}} - \mathrm{arg}(\lambda_{c}) 
ight]}$$

## All hadronic uncertainties are cancelling exactly in the CP asymmetry! **Gold-plated modes**

## **PV in Interference**

![](_page_23_Picture_9.jpeg)

$$\frac{b}{b} \frac{\bar{A}_f}{A_f} \left[ 1 - \frac{a_{\mathrm{fs}}^s}{2} \right]$$

$$\mathcal{A}_f = \langle f | \mathcal{H}_{eff} | B_s^0 
angle$$
  
 $ar{\mathcal{A}}_f = \langle f | \mathcal{H}_{eff} | ar{B}_s^0 
angle$ 

CP violation in the  $B_s^0$  system

Marina Artuso (Syracuse U.), Guennadi Borissov (Lancaster U.), Alexander Lenz (Durham U., IPPP) (Nov 30, 2015) Published in: Rev.Mod.Phys. 88 (2016) 4, 045002, Rev.Mod.Phys. 91 (2019) 4, 049901 (addendum) · e-Print 1511.09466 [hep-ph]

$$\frac{\bar{\mathcal{A}}_{f_{\mathrm{CP}}}}{\mathcal{A}_{f_{\mathrm{CP}}}} = -\eta_{\mathrm{CP}} e^{-2i\phi_{j}^{\mathrm{CKM}}}$$

![](_page_23_Picture_16.jpeg)

![](_page_24_Picture_0.jpeg)

# **Status Quo: CPV in Interference**

## If there are two decay topologies contributing to the decay

$$\begin{split} \mathcal{A}_{f} &= \left|\mathcal{A}_{f}^{\mathrm{Tree}}\right| e^{i\left[\phi_{\mathrm{Tree}}^{\mathrm{QCD}} + \arg\left(\lambda_{c}\right)\right]} + \left|\mathcal{A}_{f}^{\mathrm{Pen}}\right| \\ \bar{\mathcal{A}}_{\bar{f}} &= \left|\mathcal{A}_{f}^{\mathrm{Tree}}\right| e^{i\left[\phi_{\mathrm{Tree}}^{\mathrm{QCD}} - \arg\left(\lambda_{c}\right)\right]} + \left|\mathcal{A}_{f}^{\mathrm{Peng}}\right| \\ \end{split}$$

Then the CP asymmetry depends on

$$ar{\mathcal{A}}_{ar{f}} = -e^{-2i rg(\lambda_c)} \left[ rac{1+re^{-i rg(\lambda_c)}}{1+re^{+i rg(\lambda_c)}} 
ight]$$

with 
$$r = |\mathscr{A}_{f}^{\text{Peng}}| / |\mathscr{A}_{f}^{\text{Tre}}$$

![](_page_24_Picture_8.jpeg)

![](_page_24_Figure_9.jpeg)

## 20

## If penguins are small compared to tree-level, the hadronic corrections are cancelling to leading order and there is a correction proportional to r **Penguin pollution**

![](_page_24_Picture_12.jpeg)

![](_page_25_Picture_0.jpeg)

# **Status Quo: CPV in Interference**

![](_page_25_Figure_3.jpeg)

### **Neglect penguins:**

CP asymmetry in  $B_s \to J/\Psi \phi$  is directly proportional to sin (2 $\beta_s$ ) with  $\phi_s = -2\beta_s^{\text{CKMFitter}}$ 

CP asymmetry in  $B_d \rightarrow J/\Psi K_s$  is directly proportional to sin (2 $\beta$ ) **Bigi, Sanda 1981,...** 

Since there is only one amplitude, all hadronic effects cancel exactly!

# Fleischer,... (2010.14423), Ciuchini et al, Faller et al, Jung, Ligeti et al, Frings, Nierste and Wiebusch,...

![](_page_25_Picture_9.jpeg)

CP violation in the  $B^0_s$  system

Marina Artuso (Syracuse U.), Guennadi Borissov (Lancaster U.), Alexander Lenz (Durham U., Published in: *Rev.Mod.Phy*s. 88 (2016) 4, 045002, *Rev.Mod.Phys*. 91 (2019) 4, 049901 (addendum) • e-Print

Within the SM penguins are expected to give contributions of the order of  $\pm 1^{\circ} \approx \pm 0.017$ Now the hadronic ratio of penguin/tree has to be known - extremely challenging

![](_page_25_Picture_16.jpeg)

![](_page_25_Picture_17.jpeg)

![](_page_26_Picture_0.jpeg)

# **Status Quo: CPV in Interference**

Golden plated modes:  $B_{\rm s} \to J/\Psi \phi$ 

![](_page_26_Figure_3.jpeg)

![](_page_26_Picture_4.jpeg)

![](_page_26_Figure_5.jpeg)

![](_page_26_Figure_6.jpeg)

 $a_{fs}^{s}$ 

0.3

**Slide from Ramon Angel Ruiz Fernandez** 

not really constrained by  $\phi_{
m c}^{ccs}$ 

![](_page_26_Picture_12.jpeg)

# **LHCb-PAPER-2023-013** $sin(2\beta) = 0.716(15) \approx \pm 0.6^{\circ}$ UNIVERSITÄT Valeria Lukashenko, e+e-:Justin Skorupa Status Quo: CPV in Interference UNIVERSITÄT SIEGEN

Golden plated modes:  $B_{s} \rightarrow J/\Psi \phi$ 

![](_page_27_Figure_2.jpeg)

![](_page_27_Picture_3.jpeg)

**HFLAV** Preliminary

 $\phi_{s,Prelim.}^{c\bar{c}s} = -0.039 \pm 0.016 \text{ mrad} \approx \pm 0.9^{\circ}$ 

Modification due to **New Physics**  $M_{12}^{s} = M_{12}^{s, \text{SM}} |\Delta_{s}| e^{i\phi_{s}^{\Delta}}$  $\Gamma_{12}^{s} = \Gamma_{12}^{s, \text{SM}} \left| \tilde{\Delta} \right| e^{-i\phi_{s}^{\tilde{\Delta}}}$ See 1106.3200  $B_s \to J/\Psi \phi$  $-2\beta_s^{\mathrm{Exp}} \ = \ -2\beta_{s,\mathrm{Tree}}^{\mathrm{SM}} + \phi_s^{\Delta} + \beta_{s,\mathrm{Peng}}^{\mathrm{SM}} + \beta_{s,\mathrm{Peng}}^{\mathrm{BSM}},$  $\phi_{12}^{s,\mathrm{Exp}} = \phi_{12}^{s,\mathrm{SM}} + \phi_s^\Delta + \tilde{\phi}_s^\Delta,$ 

**Slide from Ramon Angel Ruiz Fernandez** 

not really constrained by  $\phi_{
m c}^{ccs}$ 

 $a_{fs}^{s}$ 

![](_page_27_Picture_10.jpeg)

![](_page_27_Picture_11.jpeg)

![](_page_28_Picture_0.jpeg)

![](_page_28_Picture_1.jpeg)

- Intro: Meson decays and Mixing
- Intro: 3 Kinds of CPV violation
- Status Quo: Mixing & CPV in mixing

Status Quo: CPV in interference

## Status Quo: Direct CPV

# Outline

![](_page_28_Picture_8.jpeg)

![](_page_29_Picture_0.jpeg)

$$A_{\mathrm{dir.CP},f}(t) = \frac{\Gamma\left(\bar{B}_{s}^{0}(t) \to \bar{f}\right) - \Gamma\left(B_{s}^{0}(t) \to f\right)}{\Gamma\left(\bar{B}_{s}^{0}(t) \to \bar{f}\right) + \Gamma\left(B_{s}^{0}(t) \to f\right)} = \frac{\left|\bar{\mathcal{A}}_{\bar{f}}\right|^{2} - \left|\mathcal{A}_{f}\right|^{2}}{\left|\bar{\mathcal{A}}_{\bar{f}}\right|^{2} + \left|\mathcal{A}_{f}\right|^{2}} = \frac{2|r|\sin\left(\phi_{\mathrm{Peng}}^{\mathrm{QCD}} - \phi_{\mathrm{Tree}}^{\mathrm{QCD}}\right)\sin\left[\arg(\lambda_{u}) - \arg(\lambda_{u}) - \arg(\lambda_{u})\right]}{1 + |r|^{2} + 2|r|\cos\left(\phi_{\mathrm{Peng}}^{\mathrm{QCD}} - \phi_{\mathrm{Tree}}^{\mathrm{QCD}}\right)\cos\left[\arg(\lambda_{u}) - \arg(\lambda_{u})\right]}$$

## **Extremely hard to predict!**

(In the case of CPV in interference the leading term was free of hadronic uncertainties and only the penguin corrections depended on r)

# **Status Quo: CPV in Decay**

![](_page_29_Picture_6.jpeg)

$$\mathcal{A}_{f} = \left|\mathcal{A}_{f}^{\mathrm{Tree}}\right| e^{i\left[\phi_{\mathrm{Tree}}^{\mathrm{QCD}} + \arg(\lambda_{c})\right]} + \left|\mathcal{A}_{f}^{\mathrm{Peng}}\right| e^{i\left[\phi_{\mathrm{Peng}}^{\mathrm{QCD}} + \arg(\lambda_{c})\right]}$$
$$\bar{\mathcal{A}}_{\bar{f}} = \left|\mathcal{A}_{f}^{\mathrm{Tree}}\right| e^{i\left[\phi_{\mathrm{Tree}}^{\mathrm{QCD}} - \arg(\lambda_{c})\right]} + \left|\mathcal{A}_{f}^{\mathrm{Peng}}\right| e^{i\left[\phi_{\mathrm{Peng}}^{\mathrm{QCD}} - \arg(\lambda_{c})\right]}$$

The leading contribution to the CP asymmetry is proportional to  $r = |\mathscr{A}_{f}^{\text{Peng}}| / |\mathscr{A}_{f}^{\text{Tree}}|$ 

![](_page_29_Picture_9.jpeg)

![](_page_29_Figure_10.jpeg)

![](_page_29_Picture_11.jpeg)

![](_page_29_Picture_12.jpeg)

![](_page_30_Picture_0.jpeg)

## 3 $\sigma$ to 7 $\sigma$ deviation of experiment from QCDf predictions with standard error estimates

## **Colour-allowed Tree-level Decays**

![](_page_30_Picture_4.jpeg)

- CKM leading decays
- The are no annihilation, penguins,...
- QCDf should work at its best!

Beneke, Buchalla, Neubert, Sachrajda 1999...

$$egin{aligned} &\langle D_q^{(*)+}L^- | \, \mathcal{Q}_i \, | ar{B}_q^0 
angle = \sum_j F_j^{ar{B}_q o D_q^{(*)}}(M_L^2) \ & imes \int_0^1 du \, T_{ij}(u) \phi_L(u) + \mathcal{O}\left(rac{\Lambda_{ ext{QCD}}}{m_b}
ight), \end{aligned}$$

![](_page_30_Figure_10.jpeg)

![](_page_30_Picture_11.jpeg)

![](_page_30_Figure_12.jpeg)

![](_page_31_Picture_0.jpeg)

## What could go wrong?

![](_page_31_Picture_3.jpeg)

Alexander Lenz @alexlenz42

According to the new Belle measurement in sigma of the QCD factorisation prediction in

**QCD** factorisation 90.9% 9.1% **New Physics** 0% Experiment 33 votes · Final results 9:47 AM · Nov 10, 2021 · Twitter Web App

![](_page_31_Picture_11.jpeg)

2111.04978, the decay barB\_d to D+ K- is around 7 2007.10338. Where is this discrepancy rooted?

...

![](_page_32_Picture_0.jpeg)

## What could go wrong?

![](_page_32_Picture_3.jpeg)

Alexander Lenz @alexlenz42

According to the new Belle measurement in sigma of the QCD factorisation prediction in

**QCD** factorisation 90.9% 9.1% **New Physics** 0% Experiment 33 votes · Final results 9:47 AM · Nov 10, 2021 · Twitter Web App

- Huber, Kränkl 1606.02888
- Bordone, Gubernari, Huber, Jung, vanDyk 2007.10338
- Iguro, Kitahara 2008.01086
- Cai, Deng, Li, Yang 2103.04138
- Bordone, Greljo, Maryocca 2103.10332
- Beneke, Böer, Finauro, Vos 2107.03819

Similar for  $B_s \to D_s^{\mp} K^{\pm}$ 

• Fleischer, Malami 2110.04240, 2109.04950

![](_page_32_Picture_19.jpeg)

2111.04978, the decay barB\_d to D+ K- is around 7 2007.10338. Where is this discrepancy rooted?

...

![](_page_33_Picture_0.jpeg)

## What could go wrong?

![](_page_33_Picture_3.jpeg)

Alexander Lenz @alexlenz42

According to the new Belle measurement in 2111.04978, the decay barB\_d to D+ K- is around 7 sigma of the QCD factorisation prediction in 2007.10338. Where is this discrepancy rooted?

### **QCD** factorisation

**New Physics** 

Experiment

33 votes · Final results

9:47 AM · Nov 10, 2021 · Twitter Web App

### In progress: Piscopo, Rusov

- Huber, Kränkl 1606.02888
- Bordone, Gubernari, Huber, Jung, vanDyk 2007.10338
- Iguro, Kitahara 2008.01086
- Cai, Deng, Li, Yang 2103.04138
- Bordone, Greljo, Maryocca 2103.10332
- Beneke, Böer, Finauro, Vos 2107.03819

Similar for  $B_s \to D_s^{\mp} K^{\pm}$ 

• Fleischer, Malami 2110.04240, 2109.04950

![](_page_33_Picture_20.jpeg)

...

90.9% 9.1% 0%

### In the SM the determination of $\gamma$ is super precise

The ultimate theoretical error on  $\gamma$  from  $B \rightarrow DK$  decays

Joachim  $\operatorname{Brod}^{1,*}$  and  $\operatorname{Jure} \operatorname{Zupan}^{1,\dagger}$ 

<sup>1</sup>Department of Physics, University of Cincinnati, Cincinnati, Ohio 45221, USA

### Abstract

The angle  $\gamma$  of the standard CKM unitarity triangle can be determined from  $B \to DK$  decays with a very small irreducible theoretical error, which is only due to second-order electroweak corrections. We study these contributions and estimate that their impact on the  $\gamma$  determination is to introduce a shift  $|\delta\gamma| \leq \mathcal{O}(10^{-7})$ , well below any present or planned future experiment.

### If there are BSM effects in nonleptonic decays, the determination of $\gamma$ can be modified by $\mathcal{O}(5^{\circ})$

PHYSICAL REVIEW D 92, 033002 (2015)

New physics effects in tree-level decays and the precision in the determination of the quark mixing angle  $\gamma$ 

Joachim Brod

PRISMA Cluster of Excellence and Mainz Institute for Theoretical Physics, Johannes Gutenberg University, 55099 Mainz, Germany

Alexander Lenz, Gilberto Tetlalmatzi-Xolocotzi, and Martin Wiebusch Institute for Particle Physics Phenomenology, Department of Physics, Durham University, South Road, Durham DH1 3LE, United Kingdom

update AL, Tetlalmatzi-Xolocotzi 1912.07621

![](_page_33_Figure_36.jpeg)

![](_page_33_Figure_37.jpeg)

![](_page_33_Figure_38.jpeg)

![](_page_33_Figure_39.jpeg)

![](_page_33_Figure_40.jpeg)

![](_page_33_Figure_41.jpeg)

## **Direct CP asymmetries**

•  $B \rightarrow K\pi$  puzzle still present, see. e.g. 1507.03700 Updates: **2002.03262** complete 2-loop penguins 2107.03819 QED corrections **2104.14871**  $A_{CP}(B^0 \rightarrow \pi^0 \bar{K}^0)$  Belle II SU(3) symmetry e.g. **1806.08783**, **2111.06418**,... comprehensive phenomenological study missing

• Experiment: LHCb 03/2019

See talk by Eleftheria Solomonidi **Theory: SM or not SM?** E.g. 1903.10952,1909.03063 vs. 1903.10490, 1909.11242

We need 
$$r = |\mathscr{A}_{f}^{\text{Peng}}| / |\mathscr{A}_{f}^{\text{Tree}}|$$

![](_page_34_Picture_5.jpeg)

![](_page_34_Picture_7.jpeg)

## $\Delta A_{CP}$ : direct CP violation in the charm system $D^0 \to K^+ K^-$ vs. $D^0 \to \pi^+ \pi^-$

![](_page_34_Picture_9.jpeg)

![](_page_34_Picture_10.jpeg)

![](_page_34_Figure_11.jpeg)

![](_page_34_Picture_12.jpeg)

![](_page_35_Picture_0.jpeg)

**Experimental news:** •

$$a^d_{K^-K^+} = (7.7 \pm 5.7) \times 10$$
  
 $a^d_{\pi^-\pi^+} = (23.2 \pm 6.1) \times 10$   
with  $ho(a^d_{KK}, a^d_{\pi\pi}) = 88\%$ 

**Theoretical news:** •

![](_page_35_Figure_5.jpeg)

![](_page_35_Picture_9.jpeg)

![](_page_35_Picture_10.jpeg)

### See talk by Serena Maccolini

![](_page_35_Figure_12.jpeg)

### See talk by Eleftheria Solomonidi

 Confirms small SM value, as LCSR a la Khodjamirian, Petrov Contains nearby resonances Found inconsistencies in predictions obtaining large SM values

## hep-ph/2305.11951

![](_page_36_Picture_0.jpeg)

![](_page_36_Picture_1.jpeg)

## • $a_{fs}^q$ is typically measured with semi-lept

## One could also use the flavour specific

12 April 2021: Fascinating quantum mechanics.

Precise determination of the  $B_s^0 - \overline{B}_s^0$  oscillation frequency.

"A phenomenon in which quantum mechanics gives a most remarkable prediction" - Richard Feynman

Today, the LHCb Collaboration submitted a paper for publication that reports a precise determination of the  $B_s^0 - \overline{B}_s^0$  oscillation frequency. This result is presented also today at the joint <u>annual conference</u> of the UK Institute of Physics (IOP), organized by the University of Edinburgh. The  $B_s^0 - \overline{B}_s^0$  oscillation is a spectacular and fascinating feature of quantum mechanics. The strange beauty particle  $B_s^0$  composed of a <u>beauty</u> antiquark ( $\overline{b}$ ) bound with a <u>strange</u> quark s turns into its antiparticle partner  $\overline{B}_s^0$ composed of a b quark and an s antiquark ( $\overline{s}$ ) about 3 million million times per second (3\*10<sup>12</sup>) as seen in the image below.

![](_page_37_Figure_7.jpeg)

![](_page_37_Picture_8.jpeg)

tonic 
$$B_q$$
 decays  $\bar{B}_s \to D_s^+ \pi^-$  decay

![](_page_37_Figure_10.jpeg)

- $a_{fs}^q$  is typically measured with semi-leptonic  $B_q$  decays
- $\bullet$  One could also use the flavour specific  $\bar{B}_s \to D_s^+ \pi^-$  decay
- Assume: there is new physics in these decays, potentially CP violating

$$egin{aligned} \mathcal{A}_f &= & \left|\mathcal{A}_f^{ ext{SM}}
ight|e^{i\phi^{ ext{SM}}}e^{iarphi^{ ext{SM}}}+ \left|\mathcal{A}_f^{ ext{BSM}}
ight|e^{i\phi^{ ext{BSM}}}e^{iarphi^{ ext{BSM}}} \end{aligned} \ &=: & \left|\mathcal{A}_f^{ ext{SM}}
ight|e^{i\phi^{ ext{SM}}}e^{iarphi^{ ext{SM}}}\left(1+re^{i\phi}e^{iarphi}
ight)
ight, \end{aligned}$$

Discrepancy QCDf vs Exp. sug

![](_page_38_Picture_6.jpeg)

ggests 
$$r \approx 0.1 - 0.2$$

- $a_{fs}^q$  is typically measured with semi-lep
- One could also use the flavour specific
- Assume: there is new physics in these
- Derive CP asymmetry

$$A_{\rm fs}^{q} = \frac{a_{\rm fs}^{q} - 2r\sin\phi\sin\varphi + 2a_{\rm fs}^{q}r\cos\phi\cos\varphi + a_{\rm fs}^{q}r^{2}}{1 + 2r\cos\phi\cos\varphi + r^{2} - 2a_{\rm fs}^{q}r\sin\phi\sin\varphi} \approx a_{\rm fs}^{q} - A_{\rm dir}^{q}$$

$$Constrained by$$

$$semi-leptonic$$

$$Measurements$$

$$a_{sl}^{s,\rm Exp} = (60 \pm 280) \cdot 10^{-5},$$

$$a_{sl}^{d,\rm Exp} = (-21 \pm 17) \cdot 10^{-4}.$$
HFLAV 1970?

![](_page_39_Picture_6.jpeg)

otonic 
$$B_q$$
 decays  
c  $\bar{B}_s \rightarrow D_s^+ \pi^-$  decay  
e decays, potentially CP violating

![](_page_39_Picture_8.jpeg)

- $a^q_{fs}$  is typically measured with semi-leptonic  $B_q$  decays
- One could also use the flavour specific  $\bar{B}_s 
  ightarrow D_s^+ \pi^-$  decay
- Assume: there is new physics in these decays, potentially CP violating
- Derive CP asymmetry

$$A_{\mathrm{fs}}^q \;=\; rac{oldsymbol{a_{\mathrm{fs}}}^q - 2r\sin\phi\sinarphi + 2a_{\mathrm{fs}}^q r}{1 + 2r\cos\phi\cosarphi + r^2 - 2r}$$

Significant exp. deviation of  $A_{fs}^q$  from  $a_{sl}^q$ = unambiguous and theory independent signal for BSM

![](_page_40_Picture_7.jpeg)

![](_page_40_Figure_8.jpeg)

![](_page_41_Picture_0.jpeg)

# Conclusions

- Continuous progress in experiment and theory for mixing observables SM model and theory tools seem to work very well
- SM Penguin pollution is crucial now
- Interesting developments in hadronic decays  $B_s \rightarrow D_s^+ \pi^-$ ,  $\Delta A_{CP}$ ,... • QCD independent strategies to identify BSM effects!
- We want  $a_{fs}^{q}$

![](_page_41_Picture_8.jpeg)

![](_page_42_Picture_0.jpeg)

![](_page_42_Picture_1.jpeg)

## https://indico.tp.nt.uni-siegen.de/event/1/

## Follow us on Instagram

![](_page_42_Picture_4.jpeg)

![](_page_42_Picture_5.jpeg)