



Is The Muon A Third Family Lepton ?

Shahram Vatani
with Giacomo Cacciapaglia and Aldo Deandra
arXiv:2212.08691

Quick Look On The SM

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Gauge :

$$SU(3)_c \times SU(2) \times U(1)_Y$$

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Fermions :

Up, Down, Electron, Neutrino
« Family »

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ElectroWeak Symmetry Breaking :

H

Quick Look On The SM

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Fermi Theory + Mass

Quick Look On The SM

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Construction based on Gauge Principle

Quick Look On The SM

Fermions :
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Muon

Strange

Charm

Tau

Construction based on Gauge Principle

Quick Look On The SM

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× 3 = Flavor

Construction based on Gauge Principle

Quick Look On The SM

Only aspect that does not derive
from Gauge Principle

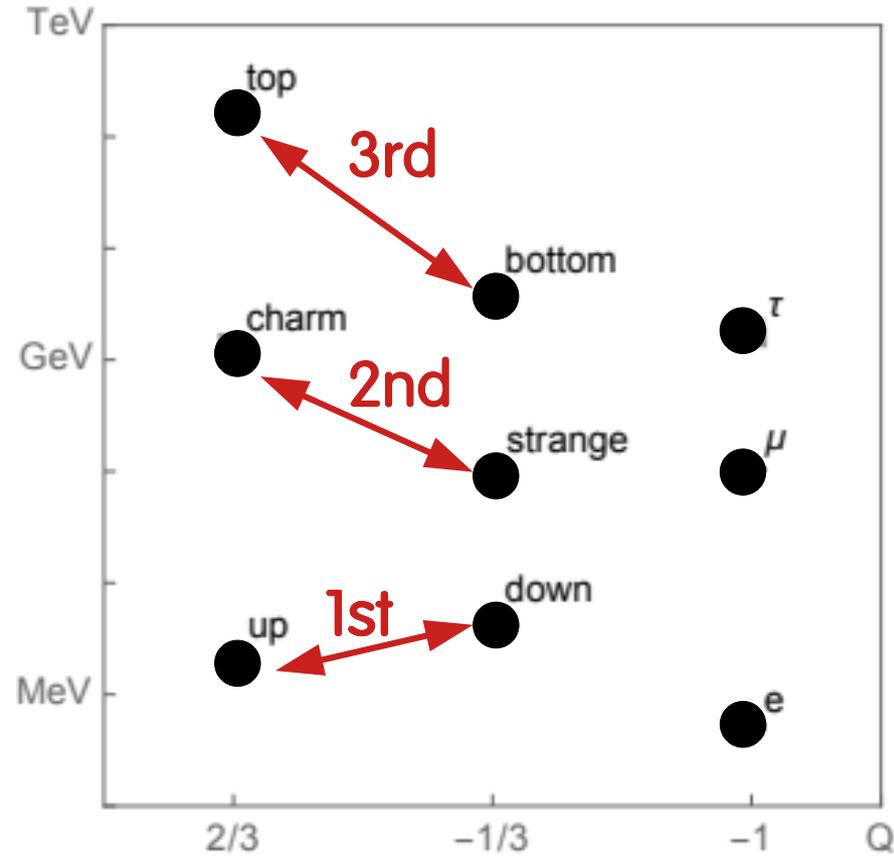
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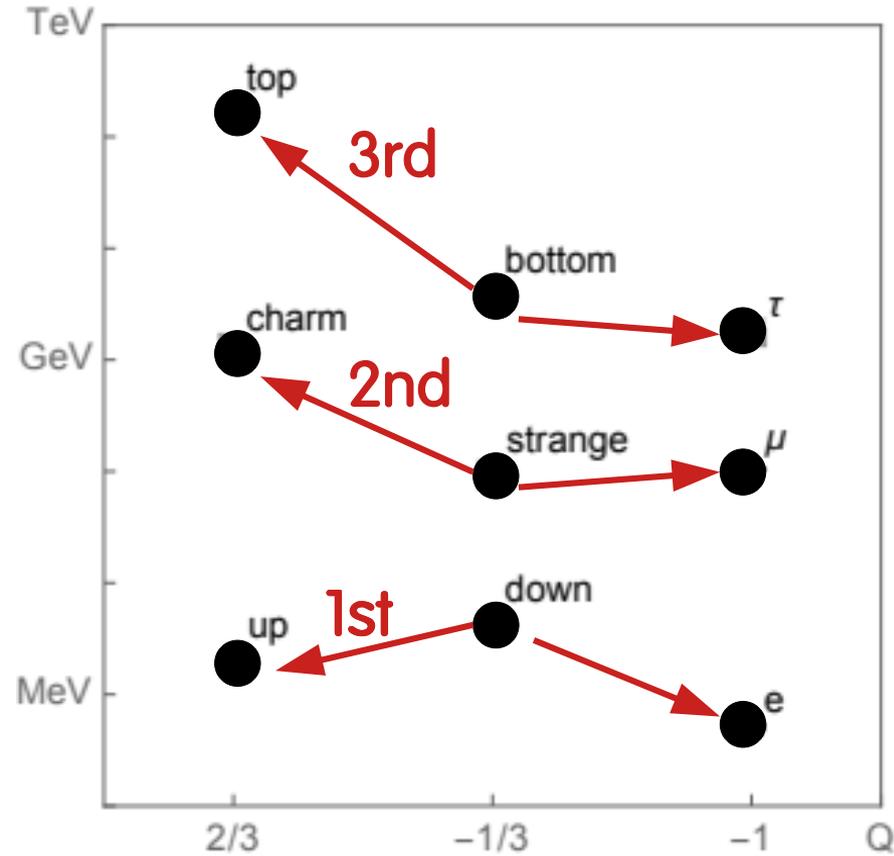


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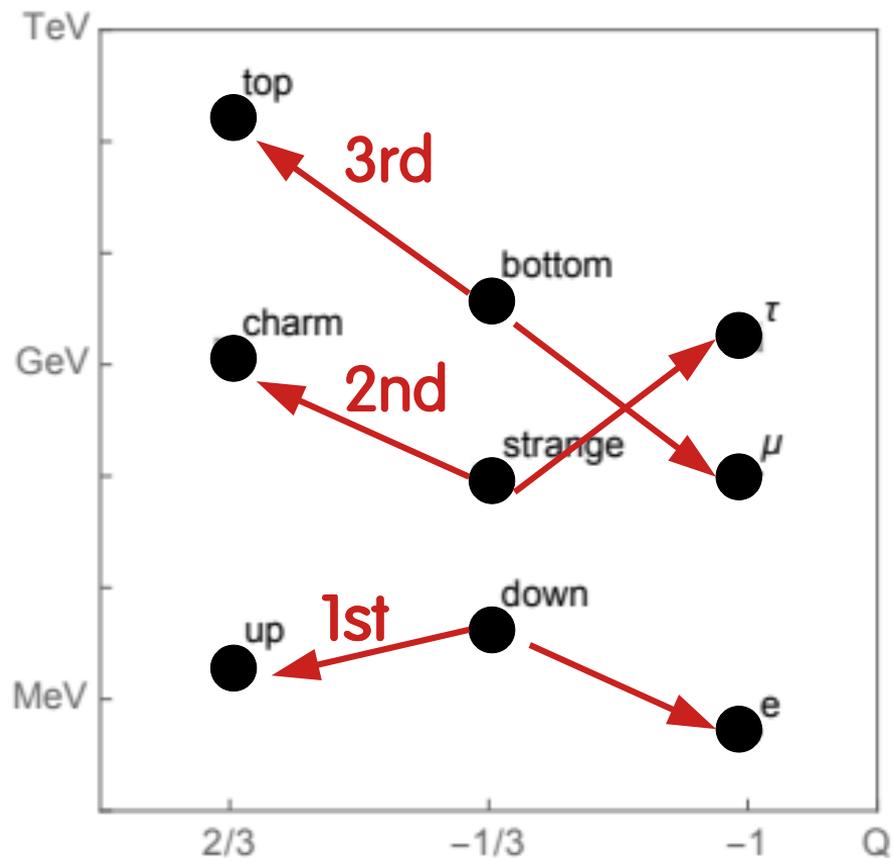
SM Family Assignment



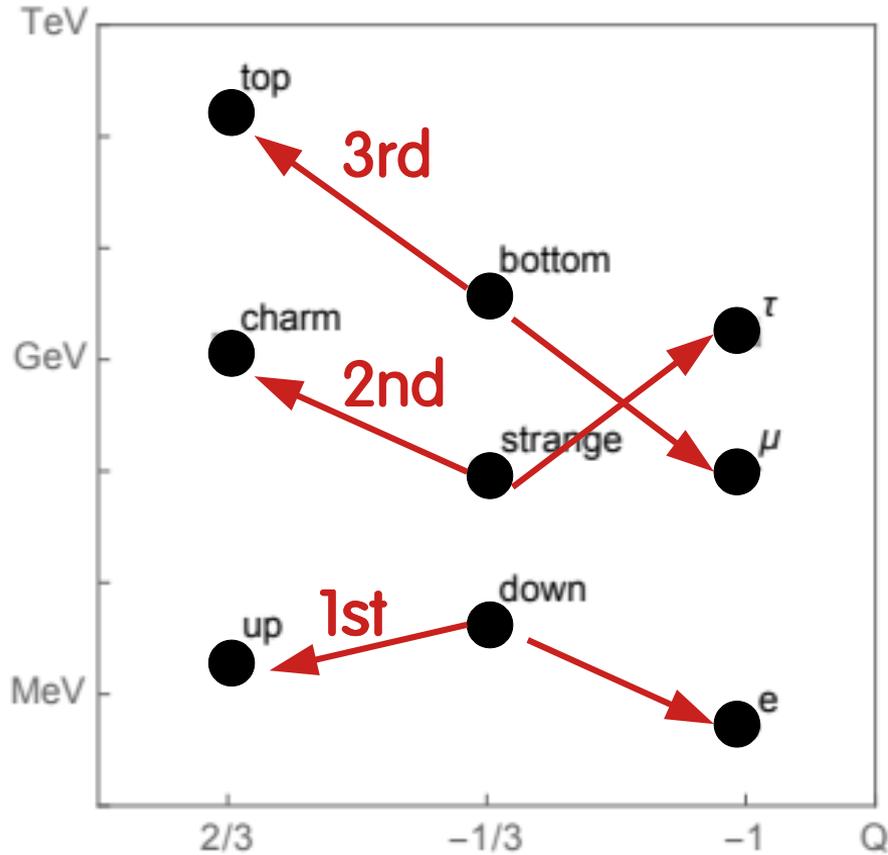
SM Family Assignment



New Family Assignment ?

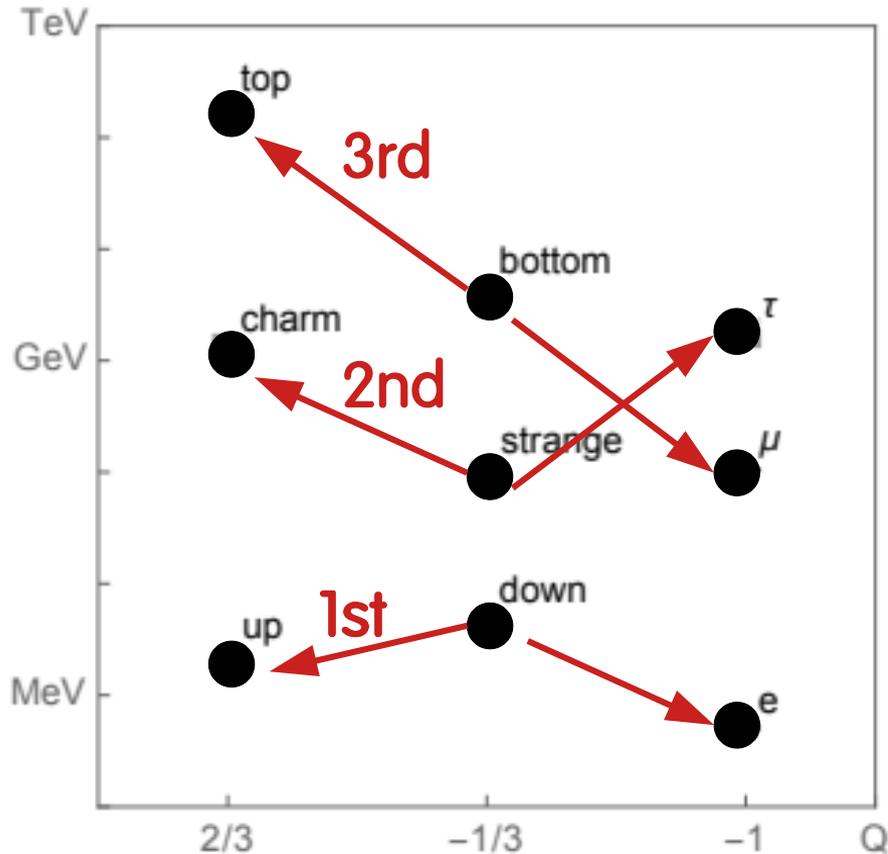


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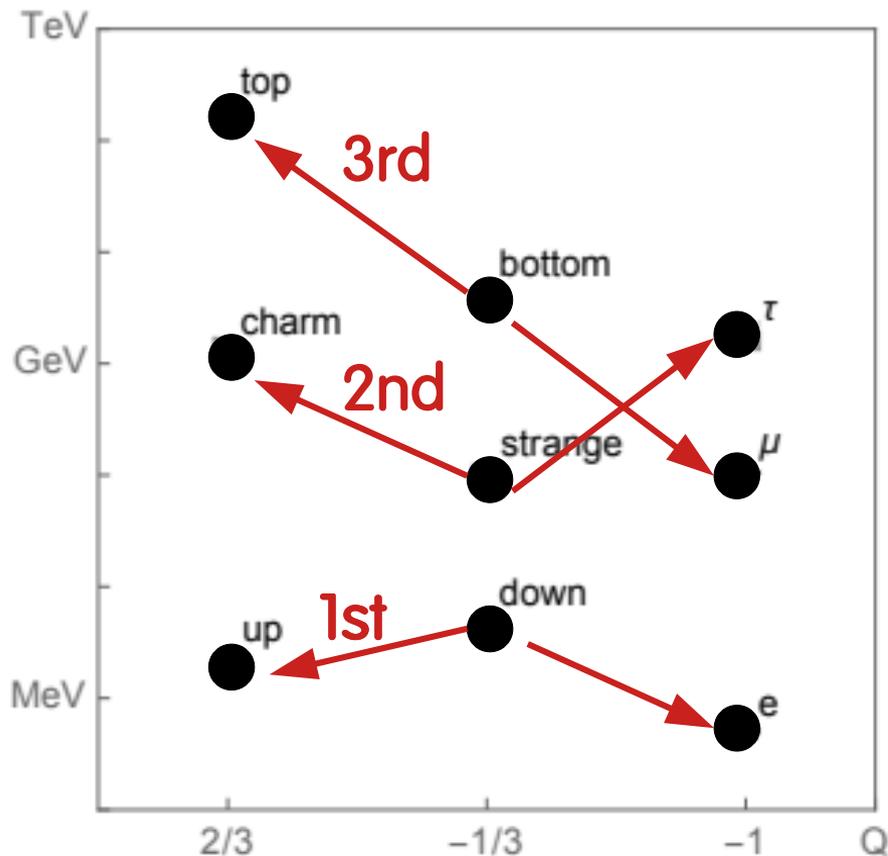
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New Family Assignment ?



- Relevant in BSM :
Pati-Salam Unification

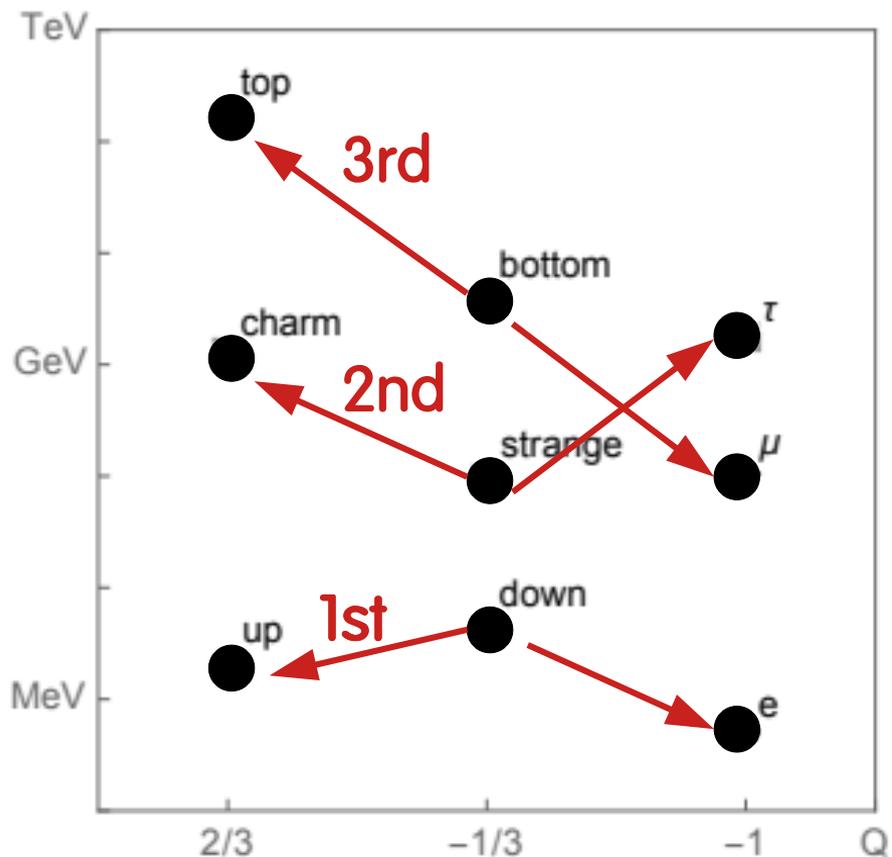
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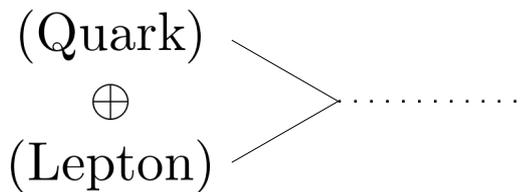
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$$\begin{pmatrix} \text{Quark} \\ \text{Lepton} \end{pmatrix} \Leftrightarrow \text{New Physics}$$

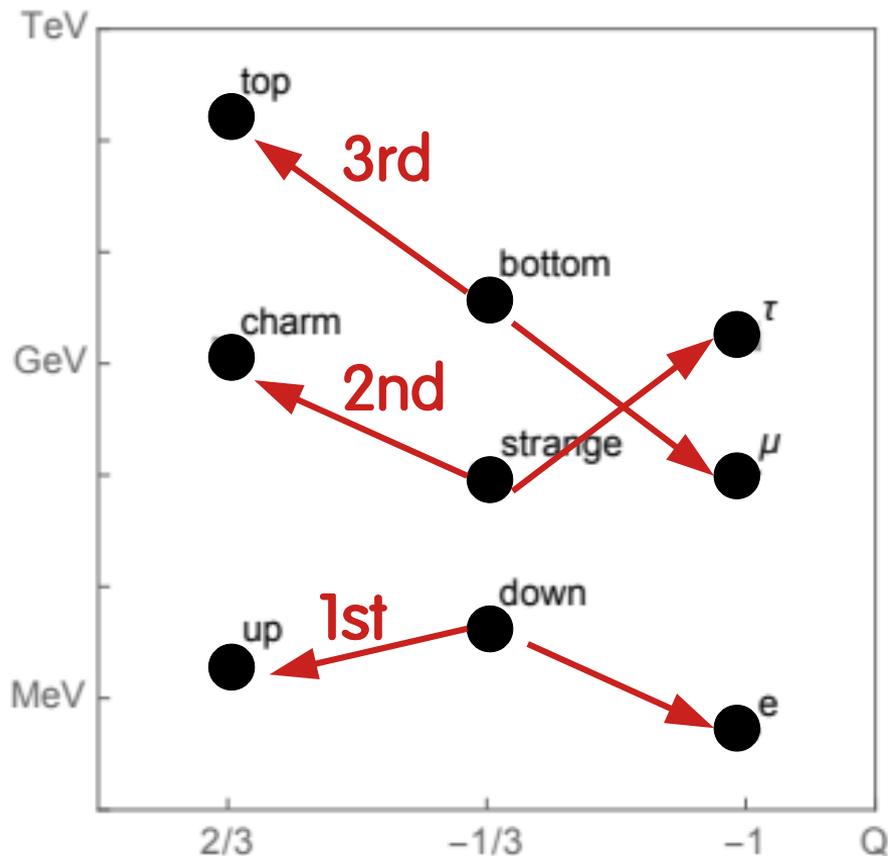
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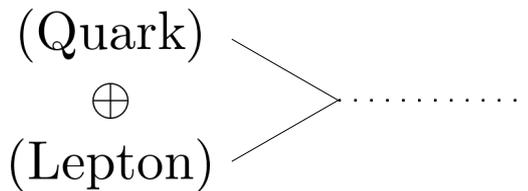
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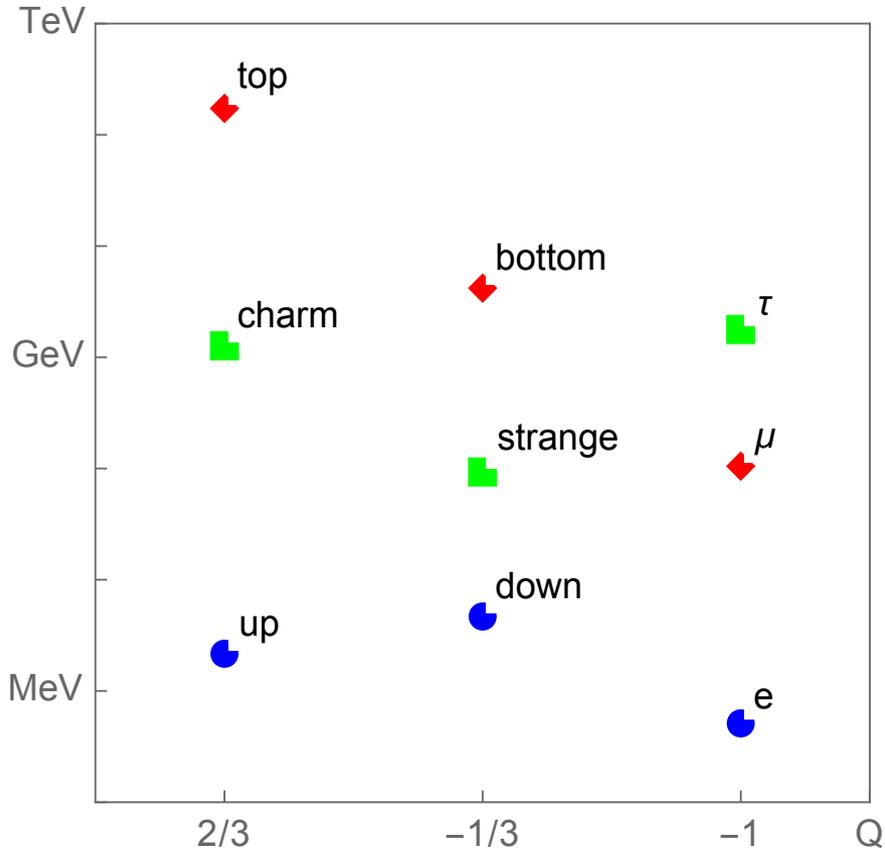


- A new mass structure :
New origin for Yukawa pattern

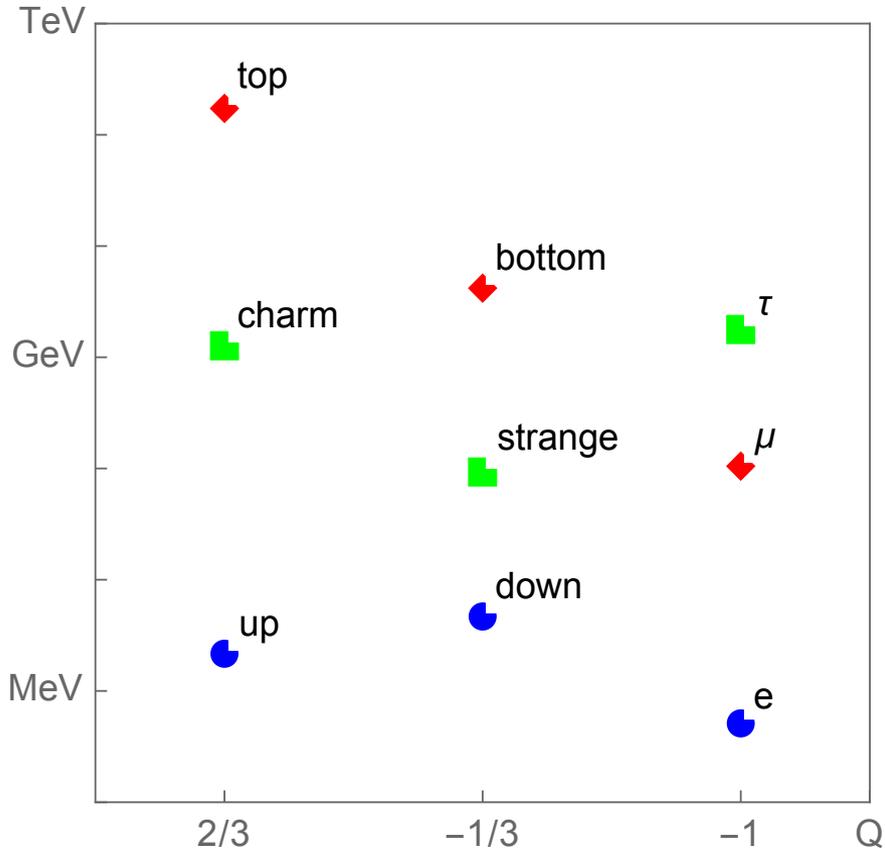
- 1) Loop Model for Masses

- 2) B Anomalies

New Family Assignment ?

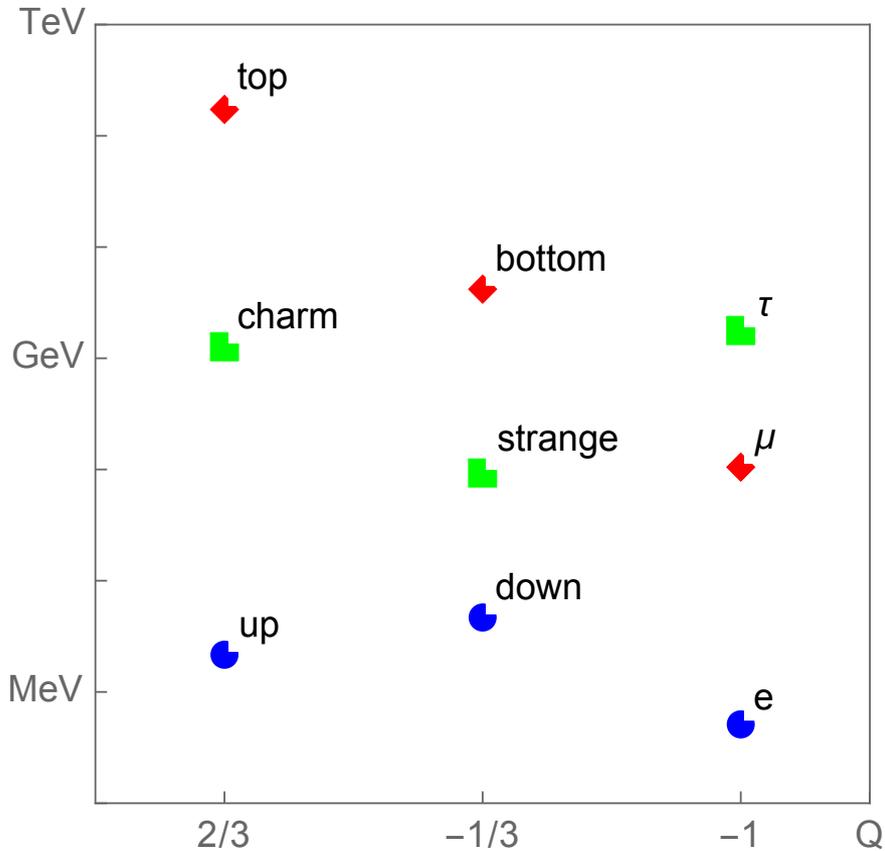


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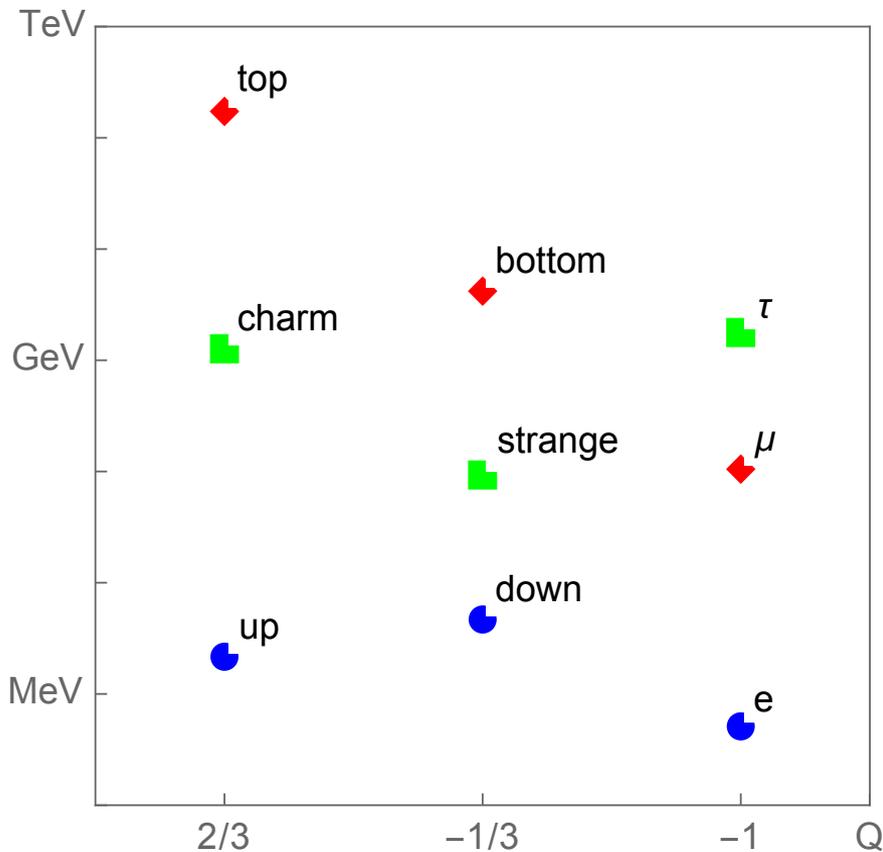
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New Family Assignment ?



- 1st ~ MeV
- 2nd ~ GeV

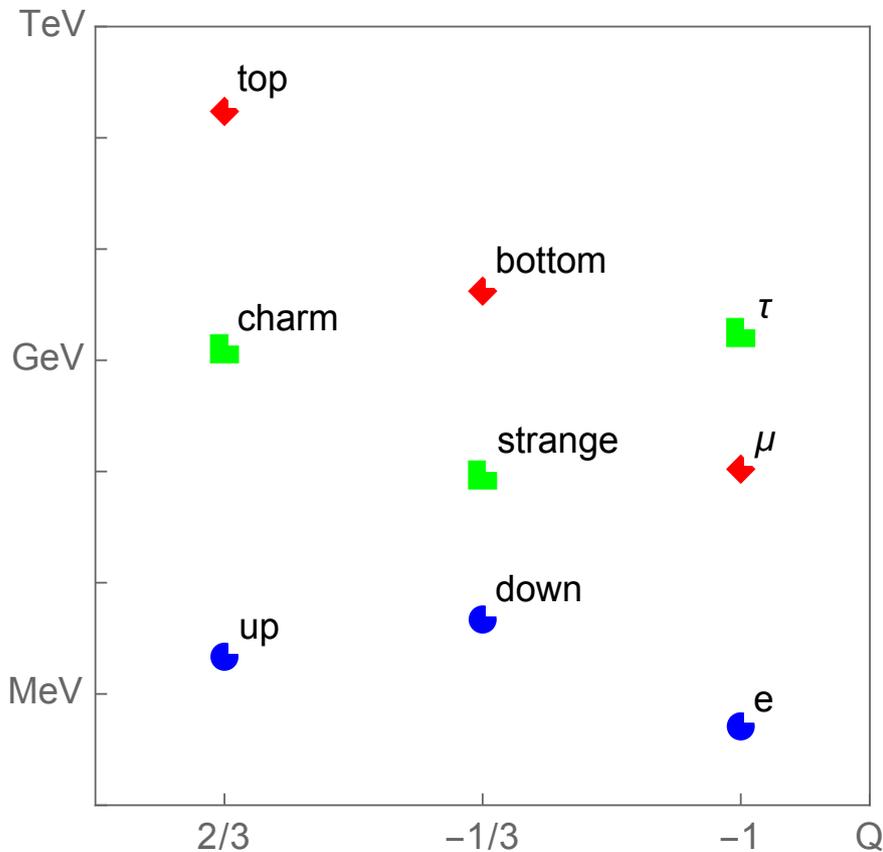
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$$X_{tb} = \frac{m_t}{m_b} = 41.31^{+0.31}_{-0.21}$$
$$X_{b\mu} = \frac{m_b}{m_\mu} = 39.56^{+0.28}_{-0.19}$$

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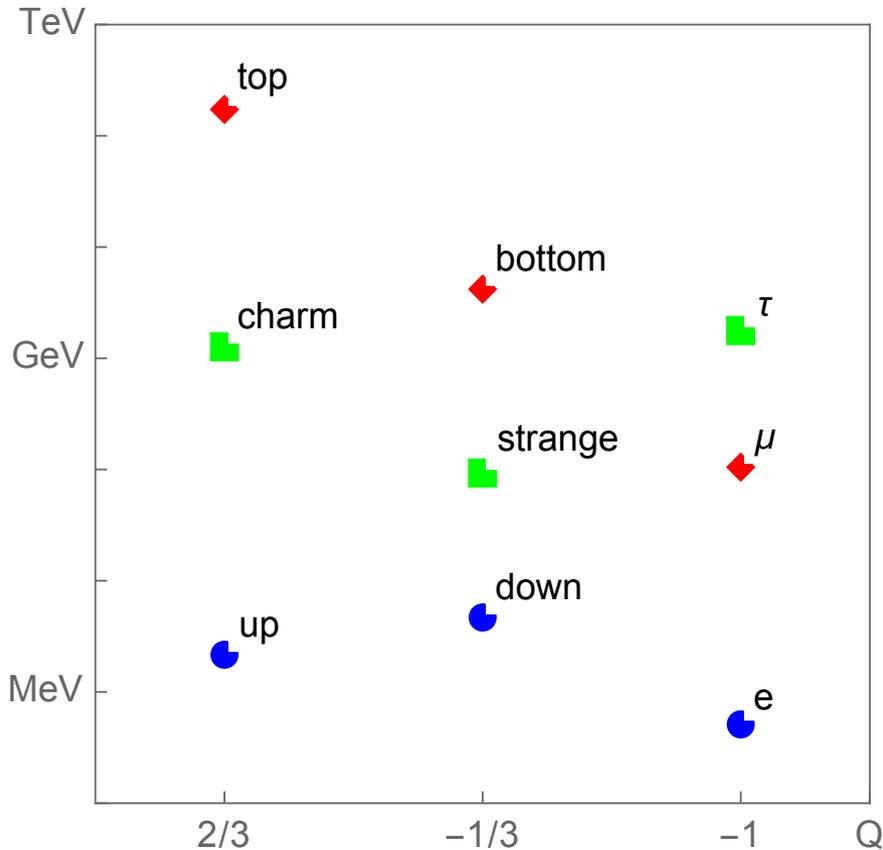
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$$\frac{X_{b\mu}}{X_{tb}} = 0.958^{+0.014}_{-0.009}$$

New Family Assignment ?



- Family Symmetry on 1st and 2nd Generations, broken by effective Yukawa (10^{-2} & 10^{-5})
- 3rd generation has tree level yukawa coupling
- Only top-Yukawa is allow (rest by Loop / Froggatt-Nielsen)

Loop Generation

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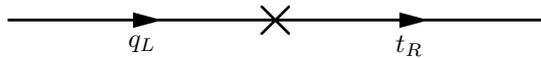
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$$m_t = y_t \langle H \rangle$$

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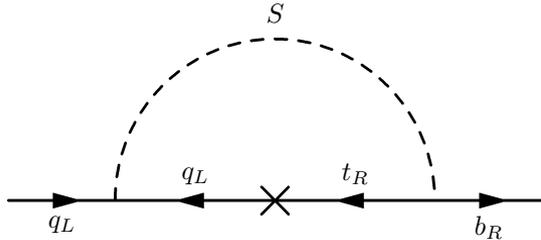
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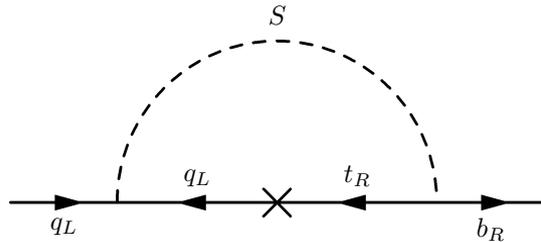


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$$\frac{m_b}{m_t} = \frac{\lambda_S^2 c_{qq} c_{tb}}{8\pi^2} N_c \ln \frac{\Lambda}{M_S}$$

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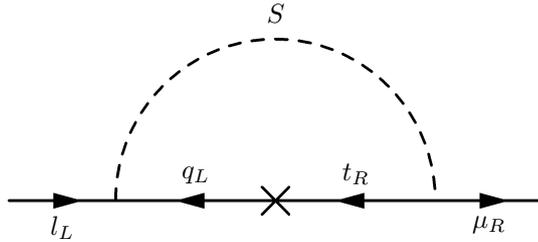
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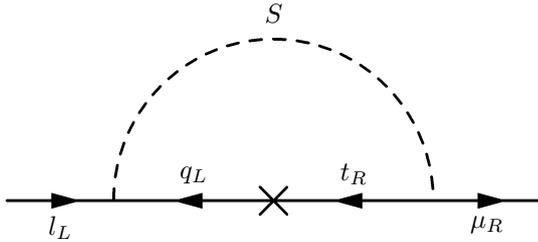


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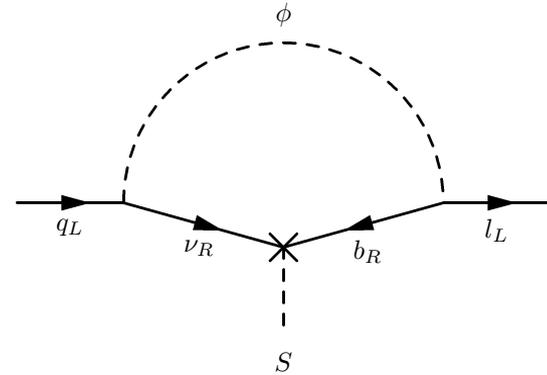
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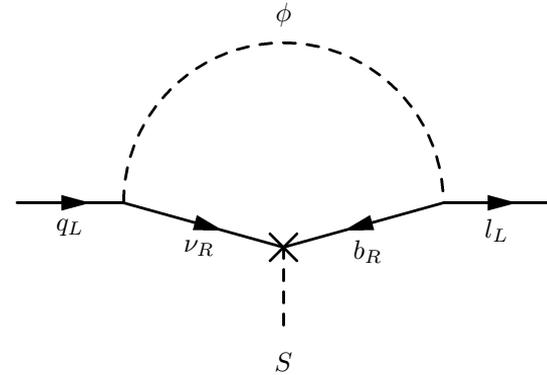
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$$M_R < M_{S/\phi}$$

$$M_R = 1.3 \cdot 10^7 \text{ GeV} \quad , \quad \frac{M_S}{M_\phi} = 1150 \quad , \quad \frac{\Lambda}{M_S} = 490$$

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- LFV is strongly constrained by experiments at levels well beyond the constraints on LFUV
- If the μ is assigned to 3rd generation, anomalies involving μ could be explained without LFV signatures

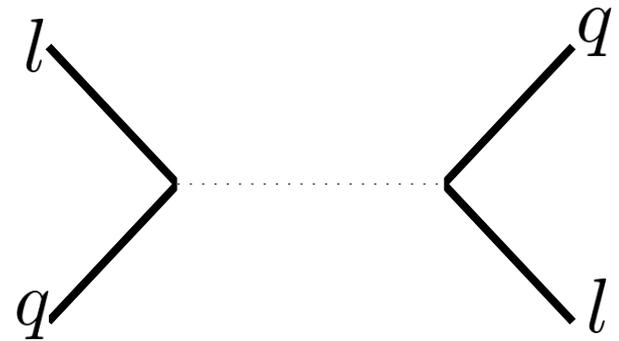
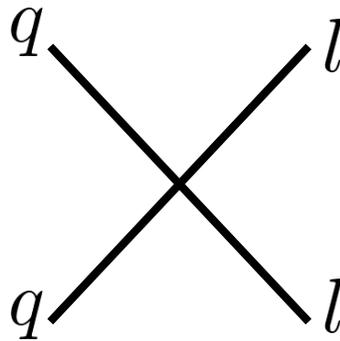
B Anomalies

- The LEFT highlight a specific set of 4-Fermion interactions

$$\mathcal{O}_{9(10)} = \frac{\alpha}{4\pi} [\bar{s}\gamma_\mu P_L b] [\bar{\mu}\gamma^\mu (\gamma_5)\mu]$$

How to generate them ?

- New Physics (LeptoQuark)



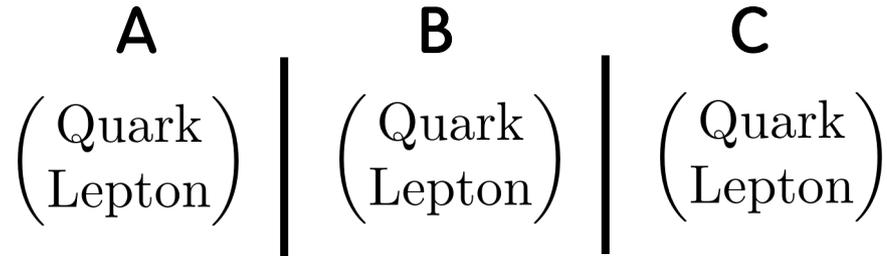
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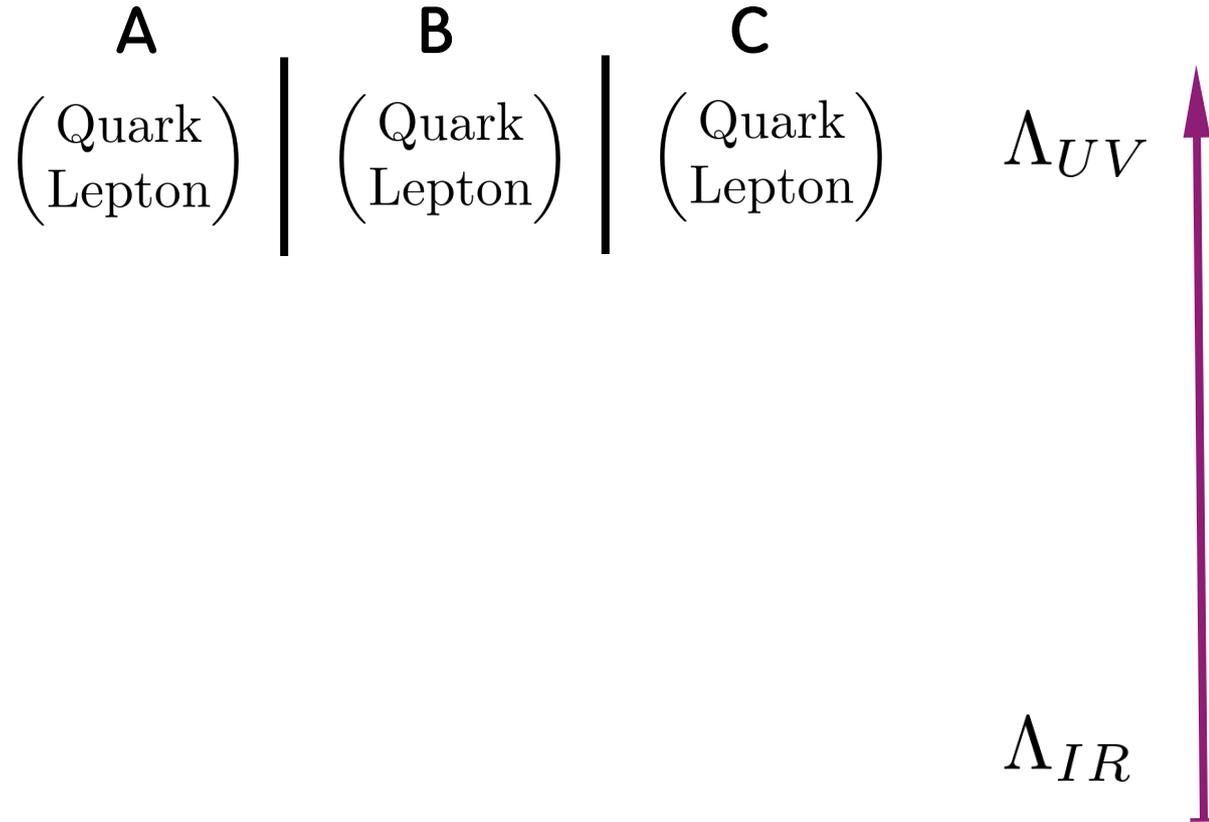
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3 SM-like unified families « à la Pati-Salam »

$$\begin{array}{c} \mathbf{A} \\ \left(\begin{array}{c} \text{Quark} \\ \text{Lepton} \end{array} \right) \end{array} \left| \begin{array}{c} \mathbf{B} \\ \left(\begin{array}{c} \text{Quark} \\ \text{Lepton} \end{array} \right) \end{array} \right| \begin{array}{c} \mathbf{C} \\ \left(\begin{array}{c} \text{Quark} \\ \text{Lepton} \end{array} \right) \end{array} \Lambda_{UV}$$

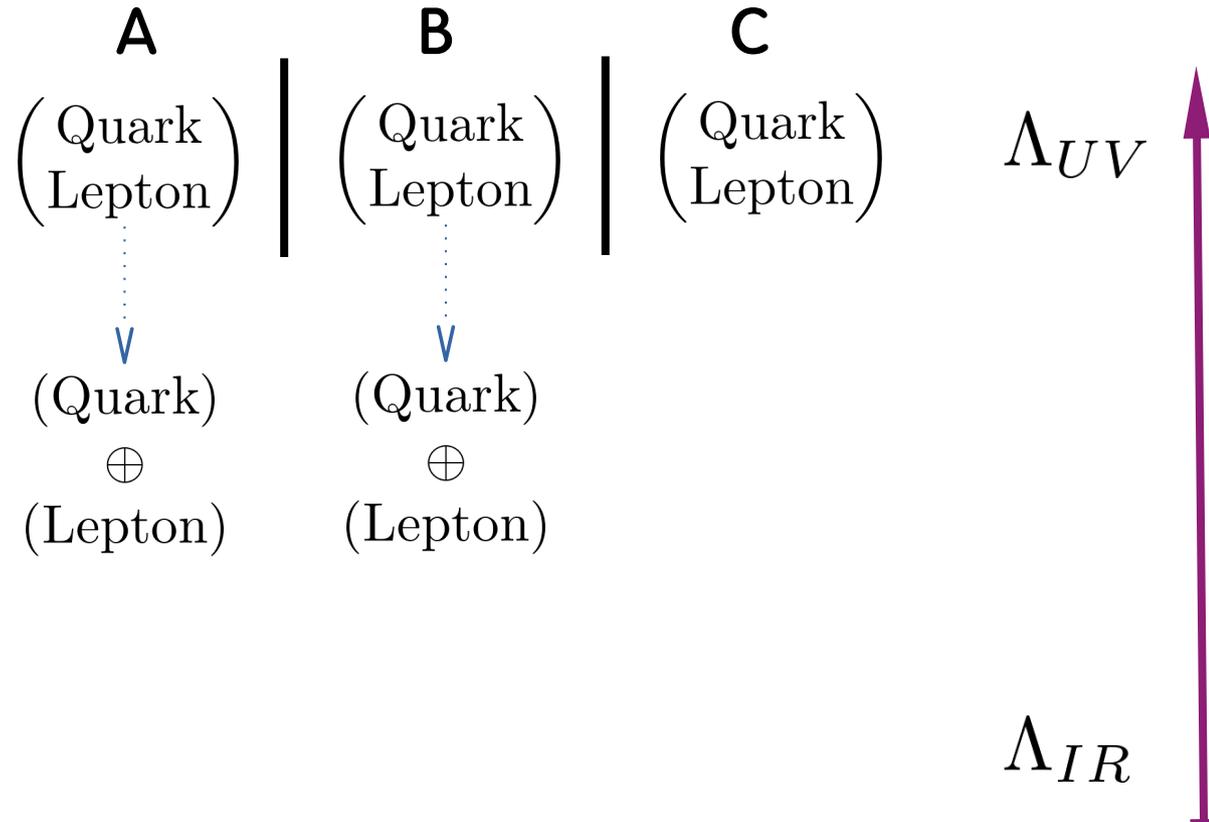
B Anomalies

3 SM-like unified families « à la Pati-Salam »



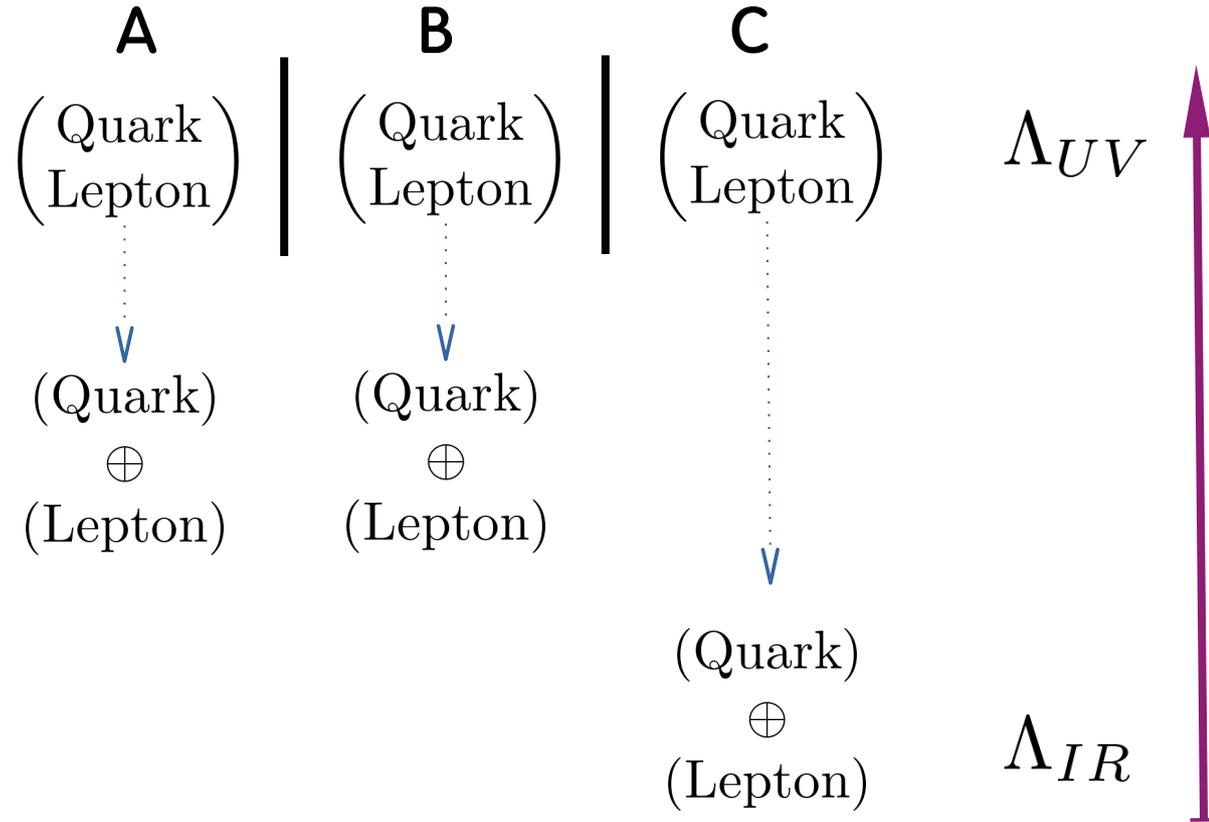
B Anomalies

3 SM-like unified families « à la Pati-Salam »



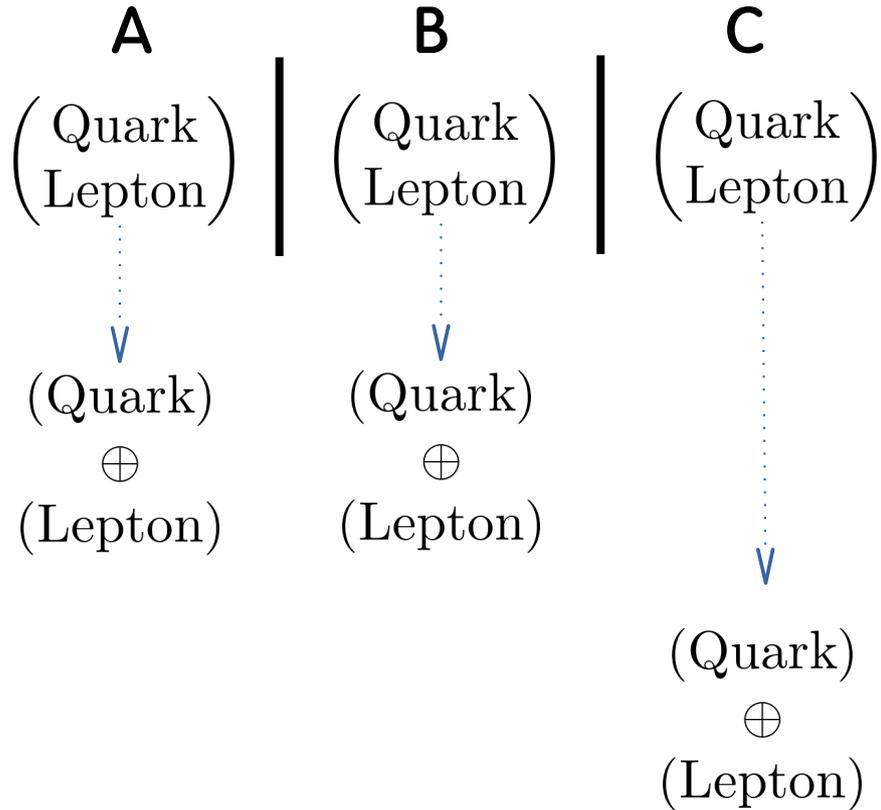
B Anomalies

3 SM-like unified families « à la Pati-Salam »



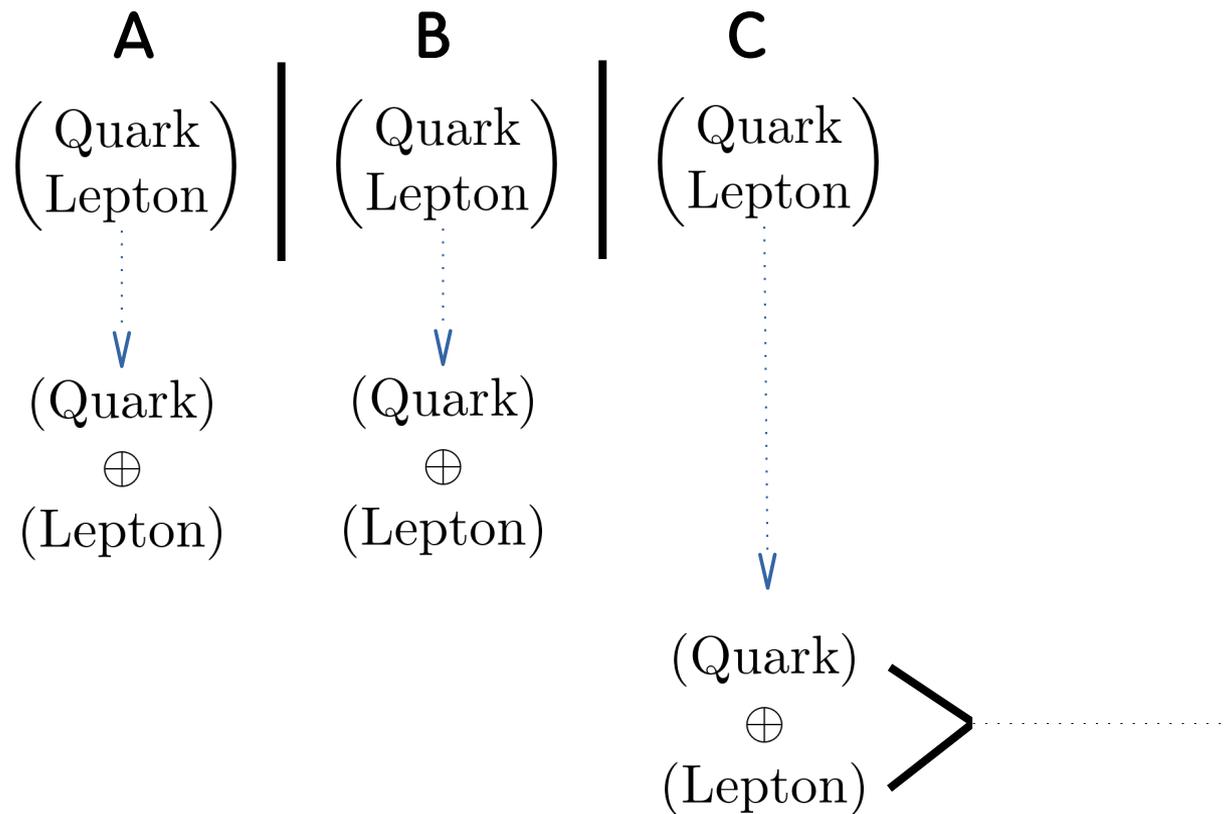
B Anomalies

3 SM-like unified families « à la Pati-Salam »



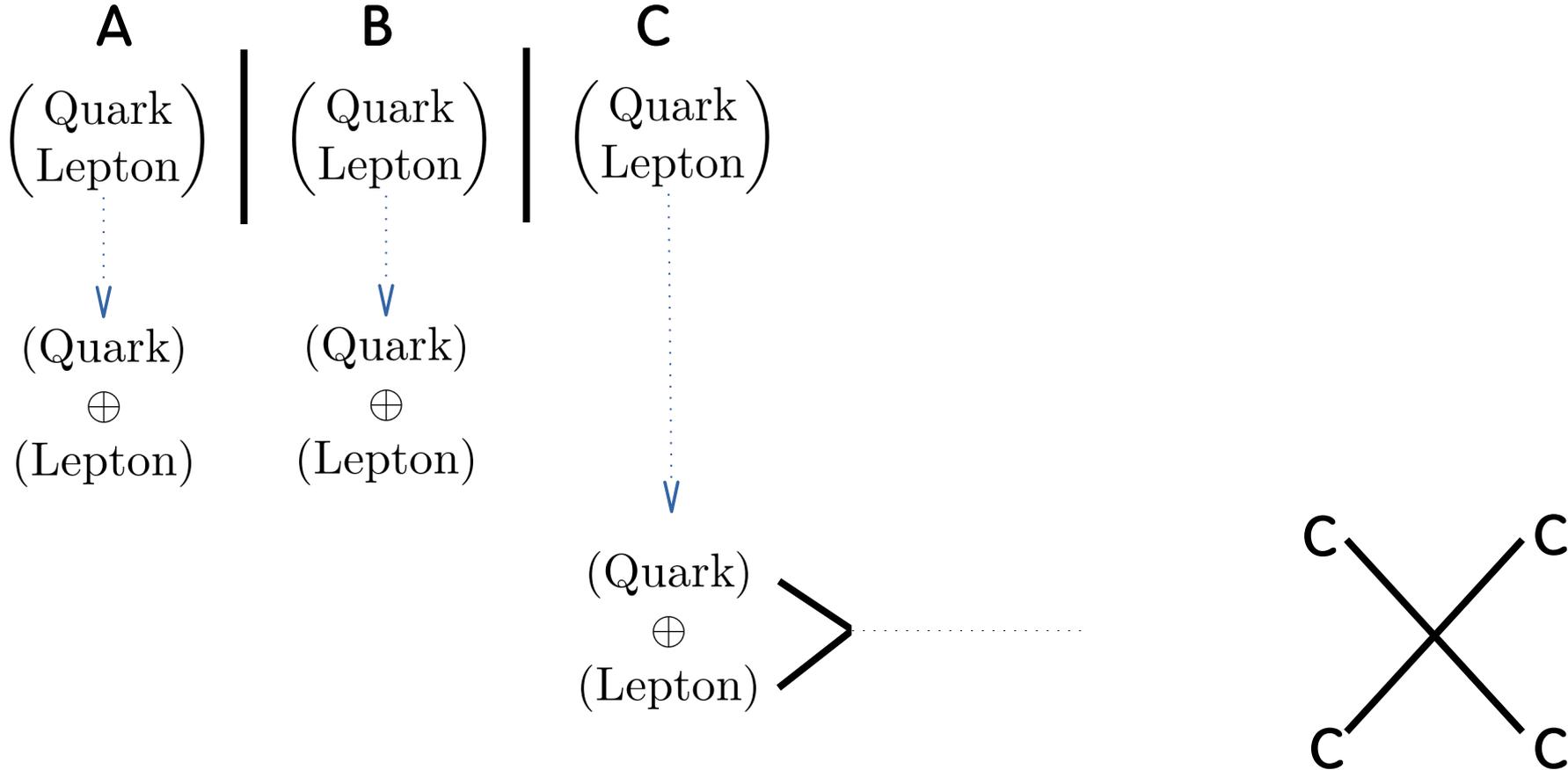
B Anomalies

3 SM-like unified families « à la Pati-Salam »



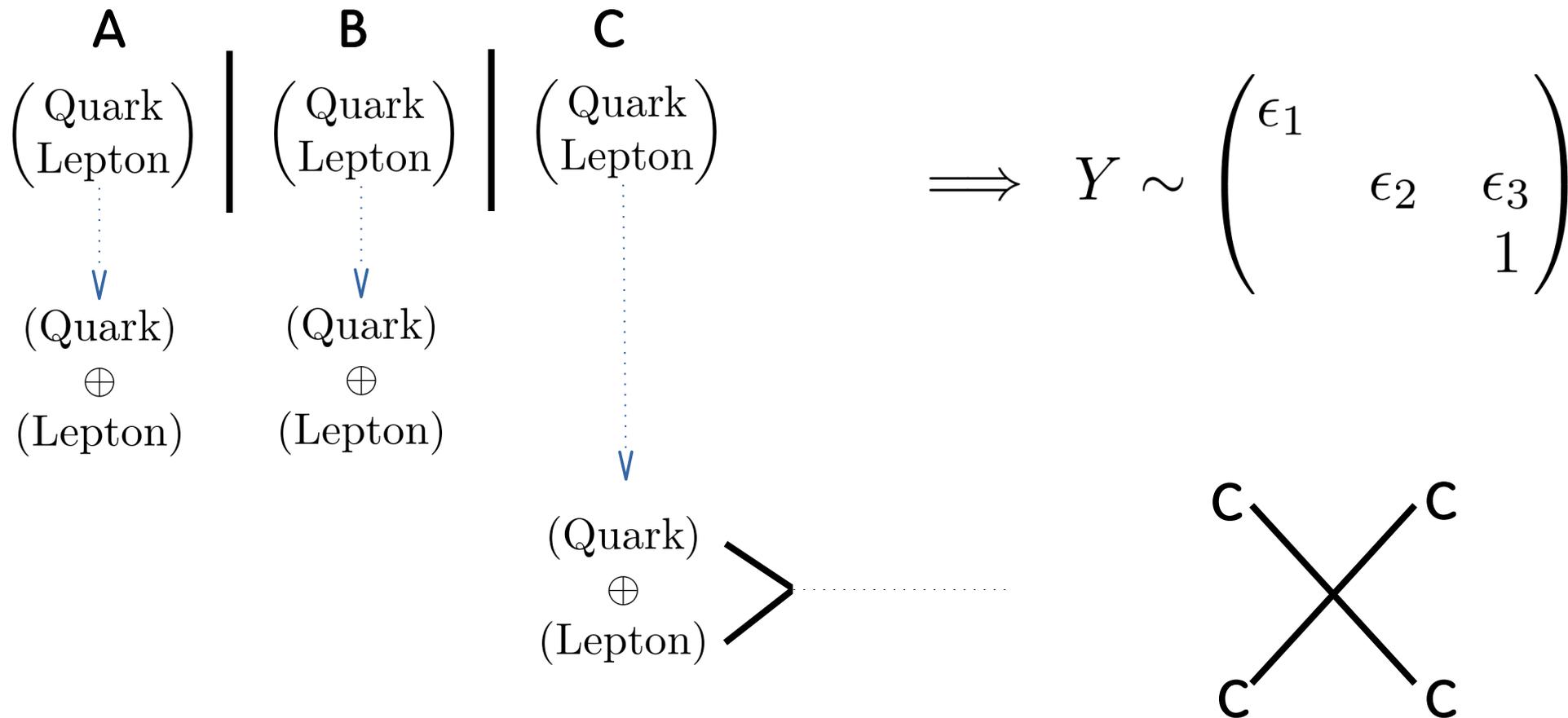
B Anomalies

3 SM-like unified families « à la Pati-Salam »



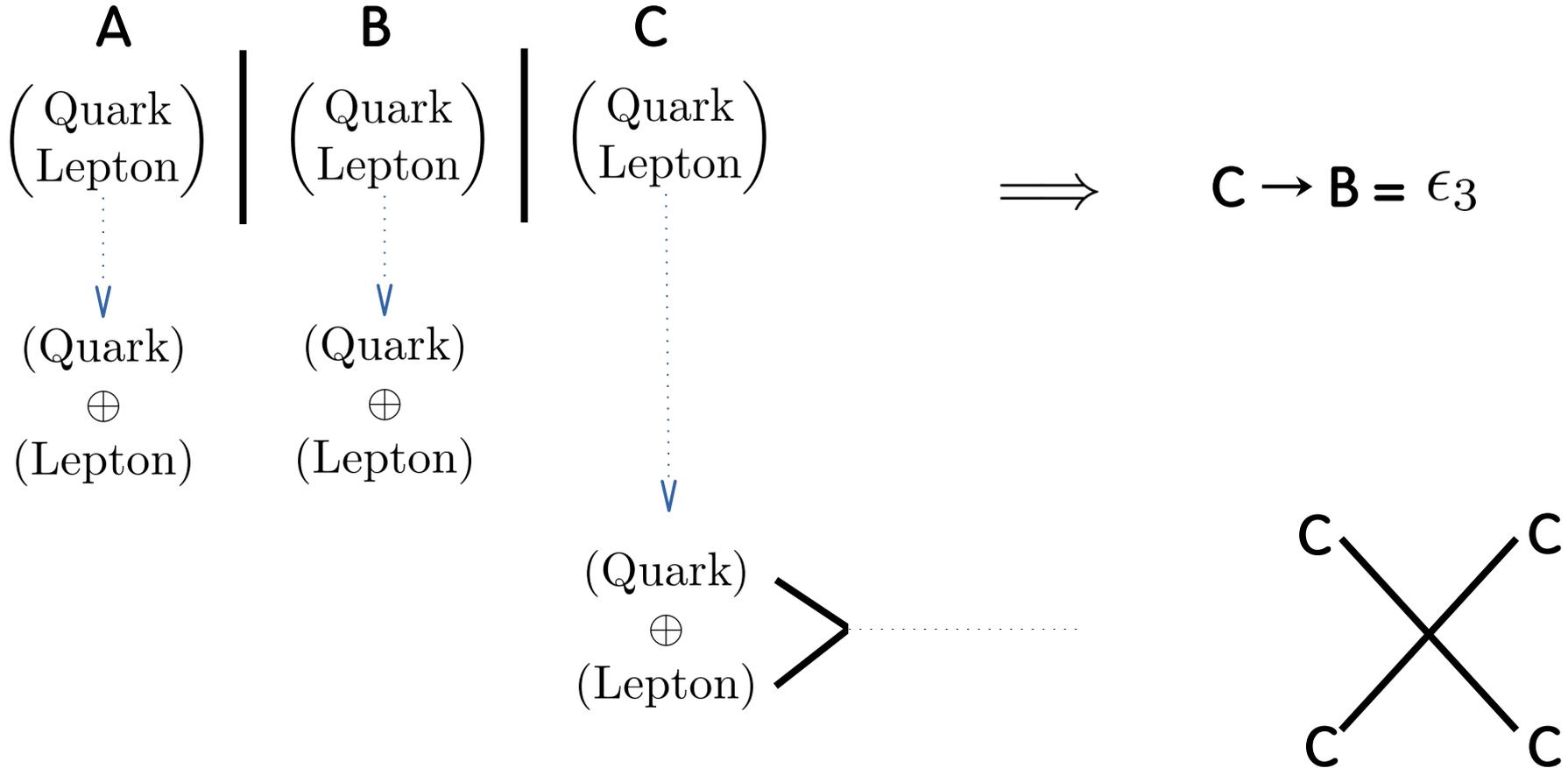
B Anomalies

3 SM-like unified families « à la Pati-Salam »

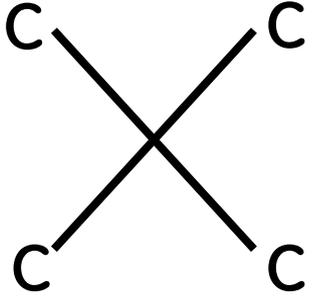


B Anomalies

3 SM-like unified families « à la Pati-Salam »

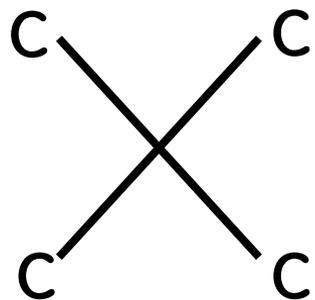


B Anomalies

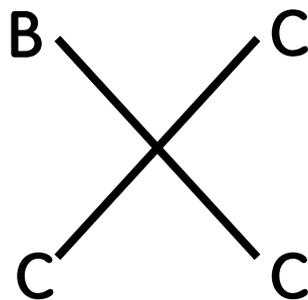


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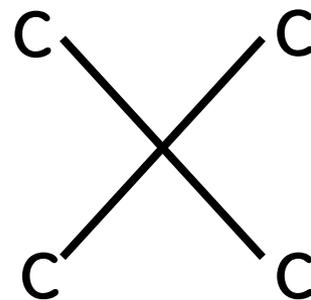
B Anomalies



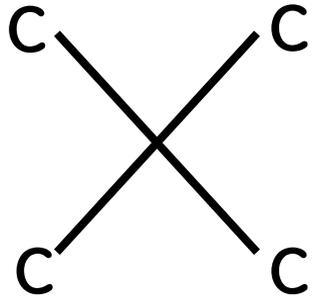
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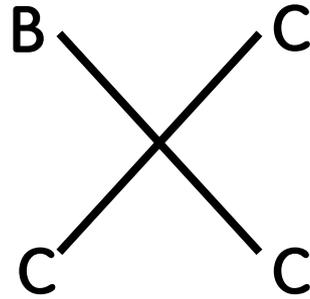
= ϵ_3



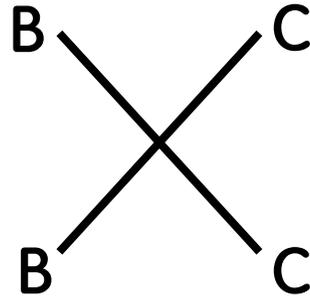
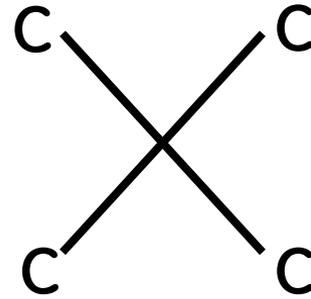
B Anomalies



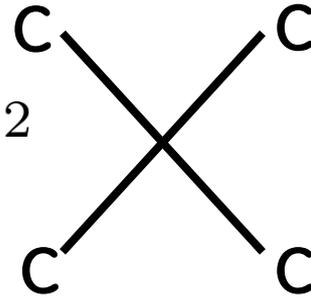
;



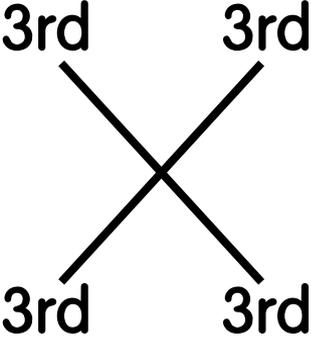
= ϵ_3



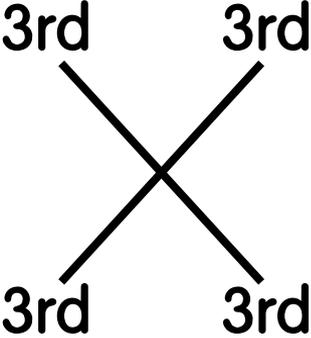
= ϵ_3^2



B Anomalies

$$\mathcal{O}_{9(10)} = \frac{\alpha}{4\pi} [\bar{s}\gamma_\mu P_L b] [\bar{\mu}\gamma^\mu (\gamma_5)\mu] = \epsilon_3^3$$
A diagram representing the Levi-Civita symbol ϵ_3^3 . It consists of four '3rd' labels arranged in a square. Two diagonal lines cross each other in the center, connecting the top-left '3rd' to the bottom-right '3rd' and the top-right '3rd' to the bottom-left '3rd'.

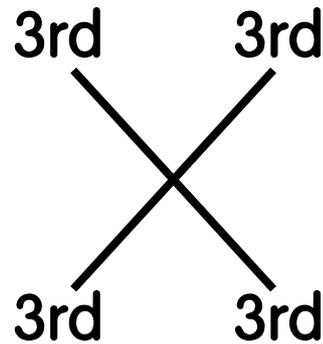
B Anomalies

$$\mathcal{O}_{9(10)} = \frac{\alpha}{4\pi} [\bar{s}\gamma_\mu P_L b] [\bar{\mu}\gamma^\mu (\gamma_5)\mu] = \epsilon_3^3$$


The diagram consists of two intersecting diagonal lines forming an 'X' shape. The four endpoints of the lines are labeled '3rd'. The top-left and bottom-right endpoints are on the left side of the diagram, while the top-right and bottom-left endpoints are on the right side. This represents a crossing of two 3rd-order terms.

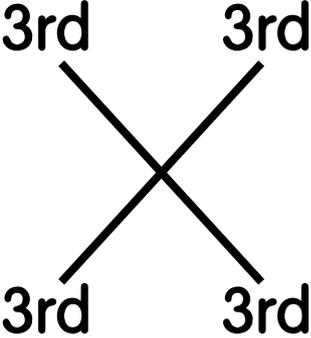
B Anomalies

$$\mathcal{O}_{9(10)} = \frac{\alpha}{4\pi} [\bar{s}\gamma_\mu P_L b] [\bar{\mu}\gamma^\mu (\gamma_5)\mu] = \epsilon_3^3$$



$$Y \sim \begin{pmatrix} \epsilon_1 & & \\ & \epsilon_2 & \\ & & \epsilon_3 \\ & & & 1 \end{pmatrix}$$

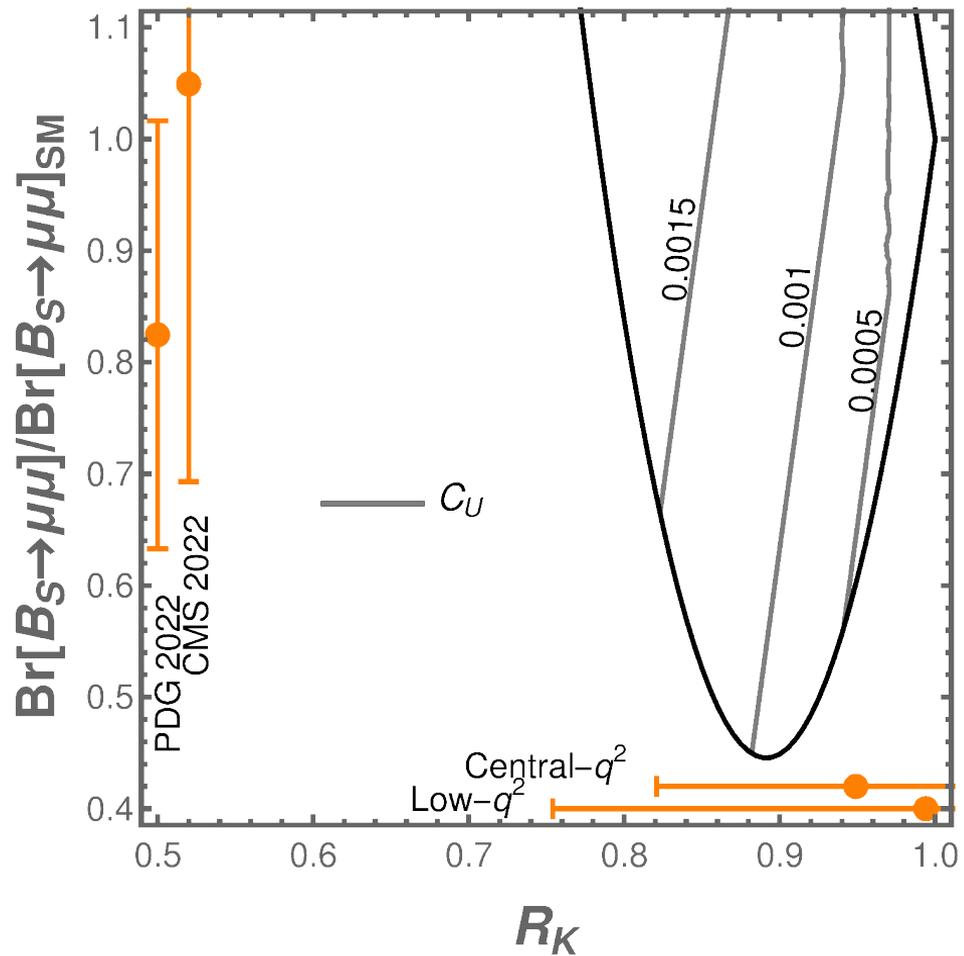
B Anomalies

$$\mathcal{O}_{9(10)} = \frac{\alpha}{4\pi} [\bar{s}\gamma_\mu P_L b] [\bar{\mu}\gamma^\mu (\gamma_5)\mu] = \epsilon_3^3$$


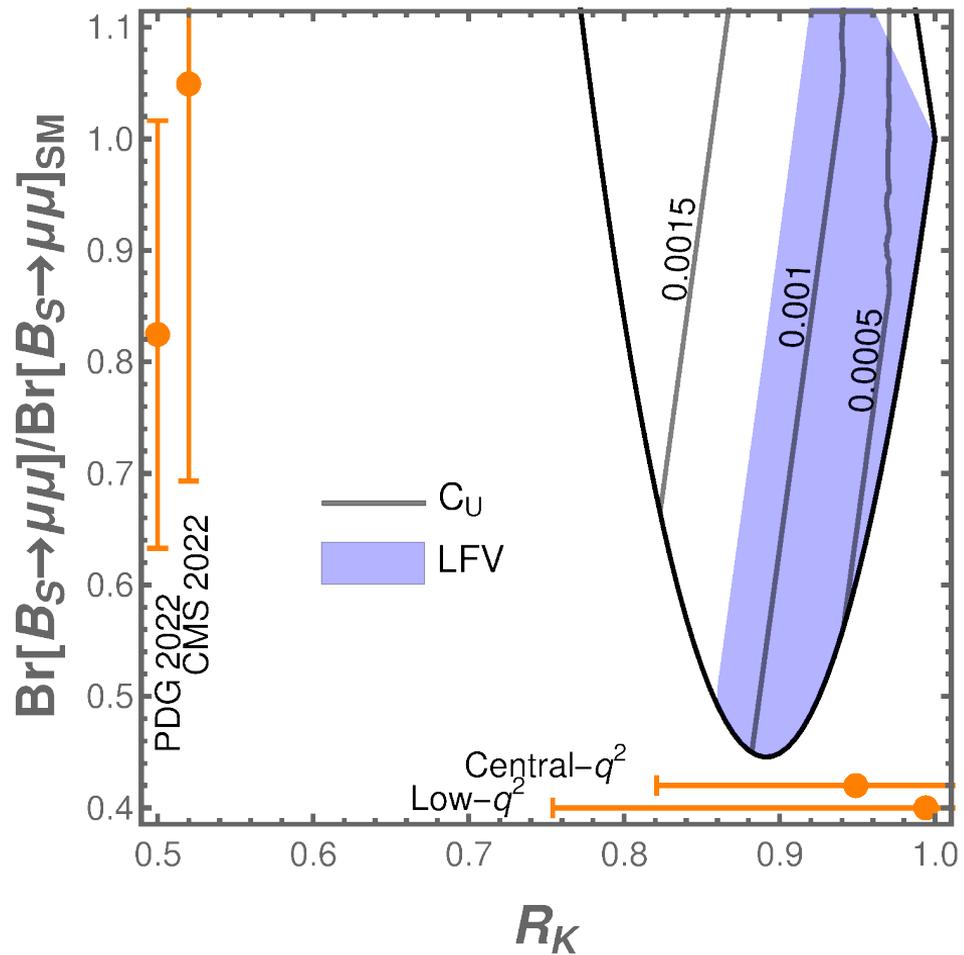
$$Y \sim \begin{pmatrix} \epsilon_1 & & \\ & \epsilon_2 & \\ & & \epsilon_3 \\ & & & 1 \end{pmatrix} \implies \begin{pmatrix} \epsilon_1 & & \\ & \epsilon_2 & \\ & & 1 \\ & & & \epsilon_3 \end{pmatrix}$$

Results

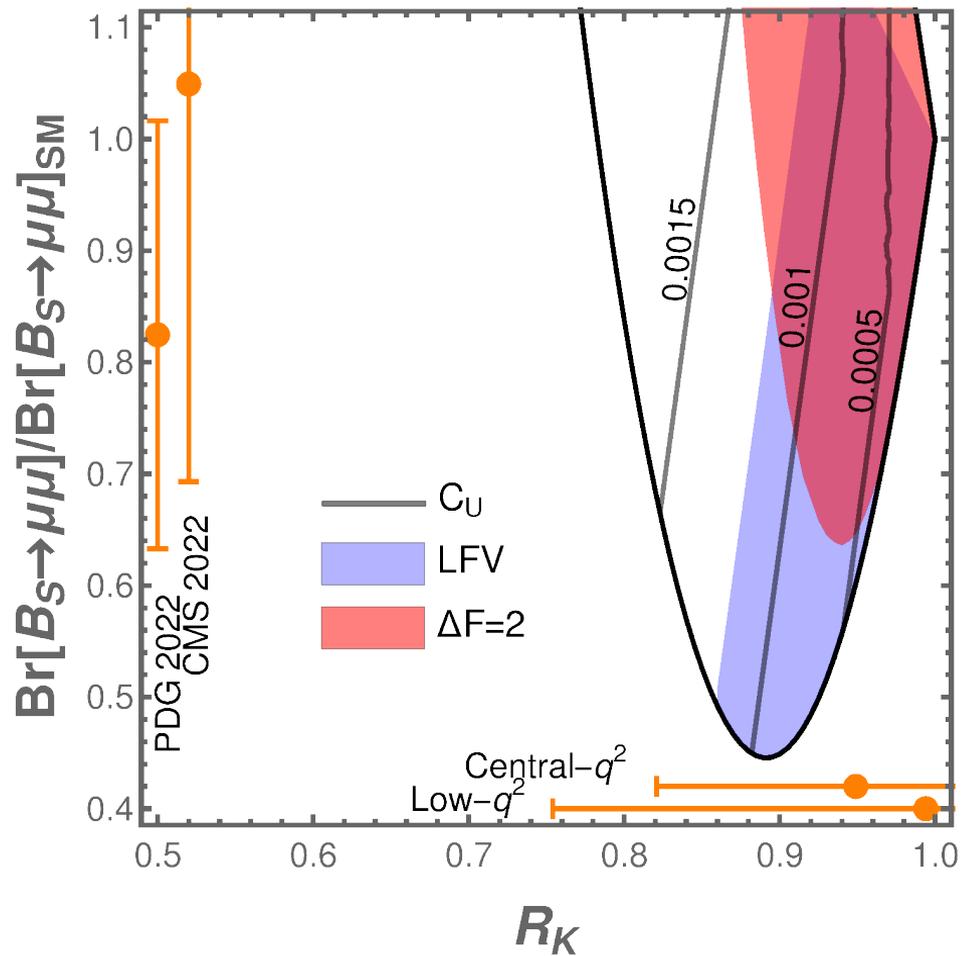
Results



Results



Results



Thank You !