

Progress in Electroweak Baryogenesis



Daniel J. H. Chung

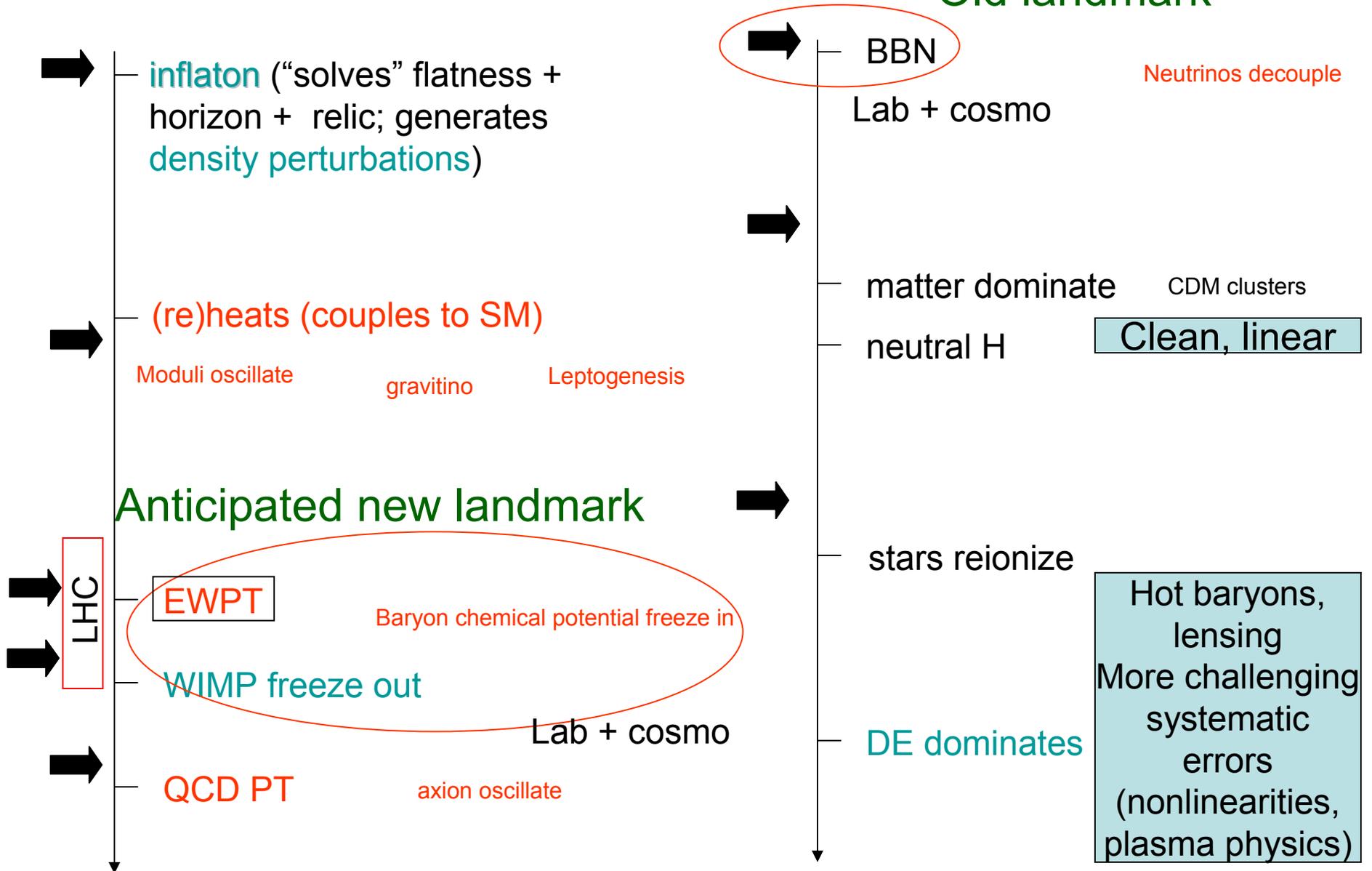
Electroweak Baryogenesis References

- Incomplete list of ewbgenesis people:

Ambjorn, Arnold, Ashoorion, Baek, Blum, Bochkarev, Bodeker, Brhlik, Carena, Chang, Cirigliano, Cline, Cohen, Davies, Davoudiasl, de Carlos, Dine, Dolan, Elmfors, Enqvist, Espinosa, Farrar, Froggatt, Gavela, Garbrecht, Giudice, Good, Grasso, Grinstein, Grojean, Hernandez, Huet, Huber, Jakiw, Jansen, Joyce, Kane, Kainulainen, Kajantie, Kaplan, Keung, Khlebnikov, Klinkhamer, Ko, Kolb, Konstandin, **Kuzmin**, Laine, Langacker, Lee, Linde, Liu, Losada, Menon, Moore, Moorhouse, Moreno, Morrissey, Multamaki, Murayama, Nelson, Nir, No, Olive, Orloff, Oaknin, Pietroni, Quimbay, Quiros, Pene, Pierce, Pilaftsis, Prokopec, Profumo, Rajagopal, Ramsey-Musolf, Ringwald, Riotto, **Rubakov**, Rummukainen, Sather, Schmidt, Seco, Senaha, Servant, **Shaposhnikov**, Shaughnessy, Singleton, Thomas, Tkachev, Trodden, Trott, Tsypin, Tulin, Turok, Vilja, Vischer, Wagner, Westphal, Weinstock, Wells, Worah, Yaffe...

- Some overview references
 - [hep-ph/0609145](#)
 - [hep-ph/0312378](#)
 - [hep-ph/0303065](#)
 - [hep-ph/0208043](#)
 - [hep-ph/0006119](#)
 - [hep-ph/9901362](#)
 - [hep-ph/9901312](#)
 - [hep-ph/9802240](#)

(Lack of) Rigidity Old landmark

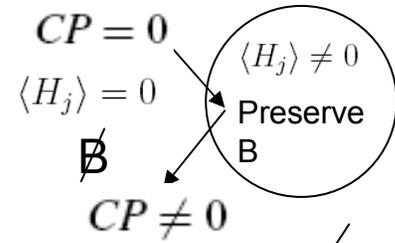


Implications of EWPT?

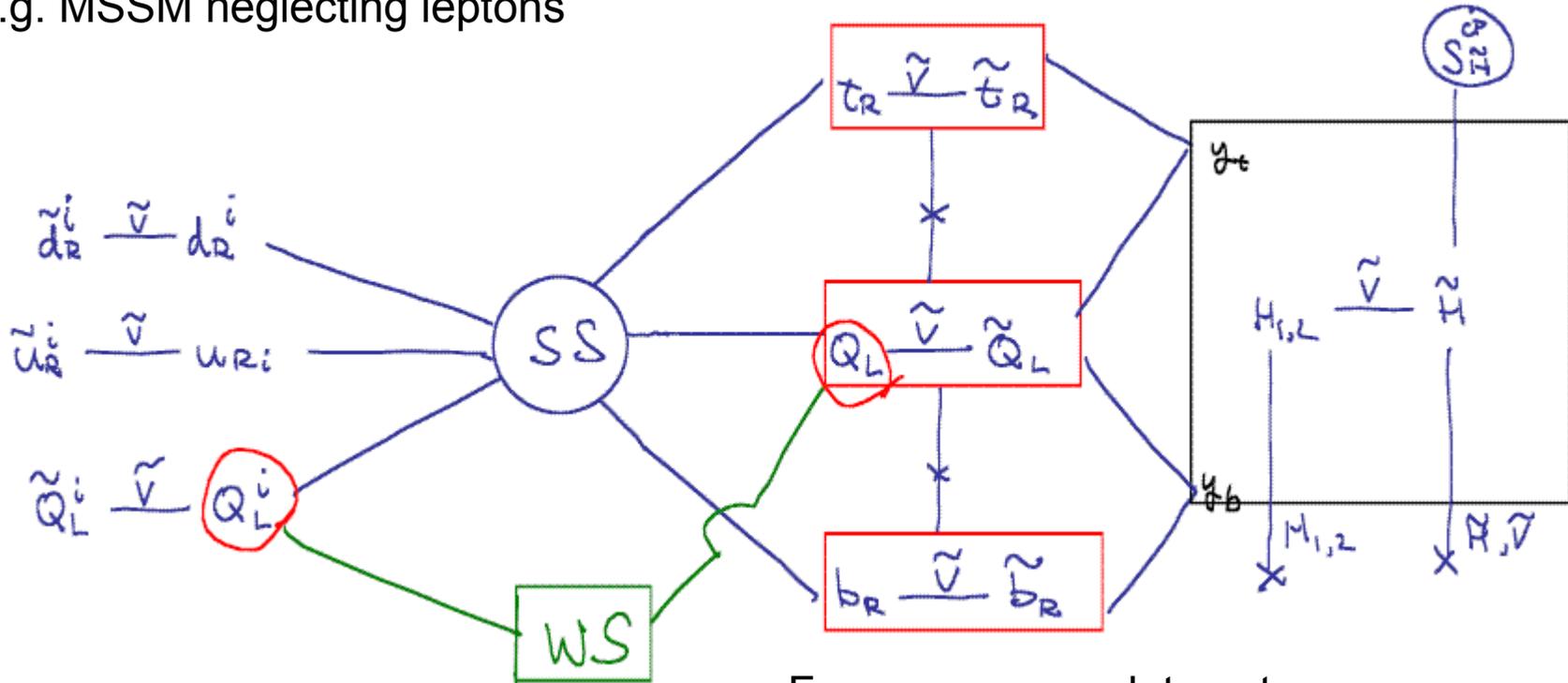
- **Electroweak Baryogenesis:** Bubble plasma dynamics
 - Good: Overconstraint possible
 - Bad: 1 number, mild tuning of parameters
- **Leptogenesis: B-L to B conversion**
 - Good: Connection to a lot of “natural” UV physics
 - Bad: Overconstraint unlikely
- **Gravity Waves: Bubble stirs up fluid**
 - Good: Overconstraint possible
 - Bad: Measurability is uncertain
- **DM: Freeze out physics can be affected**
 - Good: Overconstraint possible
 - Bad: narrow parametric window
- **CC: IR contribution**
 - Good: Overconstraint possible
 - Bad: narrow parametric window, and dependence on multiple discoveries
- **Clustering: too small scale and effects easily washed out**

Electroweak Bgenesis

[Kuzmin, Rubakov, Shaposhnikov 85]



- 1) Bubble nucleate ← 1st order PT
 - 2) CP violating scattering in bubble → source of CP asymmetry ← CP
 - 3) CP charge diffuse out in front of bubble generating B through sphalerons
 - 4) True vacuum phase captures the B-asymmetry created ← 1st order EWSB
- e.g. MSSM neglecting leptons

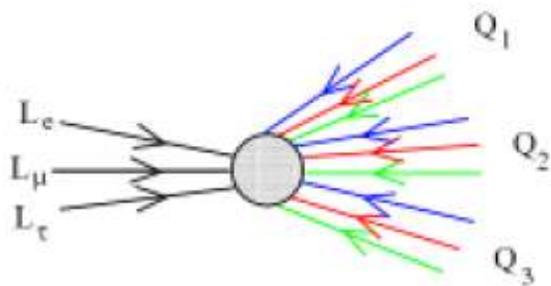


For a more complete set, see
 [DC, Garbrecht, Ramsey-Musolf, Tulin 09]

Ingredient 1

- Universe reheats to a high enough temperature such that B-violating sphalerons are unsuppressed:

[Kuzmin, Rubakov, Shaposhnikov 85; Arnold, McLerran 87; Bodeker, Moore, Rummukainen 00]



$$\Gamma_{\text{WS } v=0} \sim 10^{-5} T$$

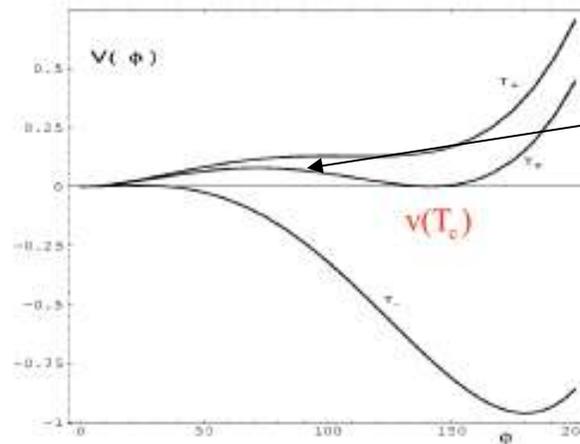
↑
 $O(10) \alpha_W^5$

Plausible since low scale inflationary models are more fine tuned.

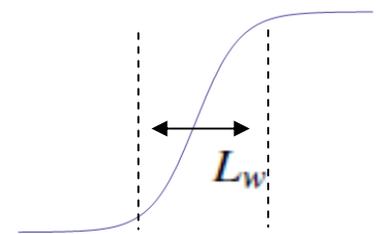
Note the smallness of baryon number comes partly from 10^{-5}

Ingredient 2

- Bubble nucleation from EWSB sector or concurrently from another sector as long as bubble percolation completes nearly simultaneously:
e.g. [Moreno, Quiros, Seco 98; John, Schmidt 00; Moore 00; Csikor, Fodor, Hegedus, Jakovac, Katz, Piroth 00]



Barrier determines L_w



Bubble action not monotonic.

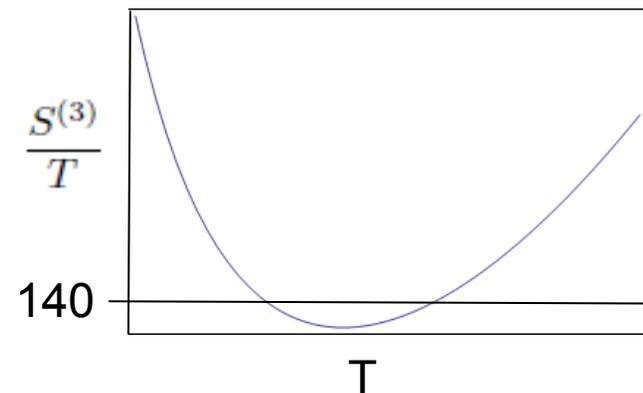
[Dine, Leigh, Huet, Linde, Linde 92]

$$\frac{S^{(3)}}{T} \approx 13.7 \frac{\mathcal{E}}{T} \left(\frac{\alpha}{\lambda}\right)^{3/2} f(\alpha)$$

$$f(\alpha) \equiv 1 + \frac{\alpha}{4} \left(1 + \frac{2.4}{1-\alpha} + \frac{0.26}{(1-\alpha)^2} \right)$$

$$\alpha(T) = \alpha_0 (1 - T^2/T_0^2)$$

$$T_0 = \sqrt{\frac{-M^2}{2c}} \quad \alpha_0 \equiv \lambda M^2 / 2\mathcal{E}^2$$



Ingredient 3

- Unsuppressed bubble (i.e. $\phi = v(t, \vec{x})$) coupling to CP violating physics.

e.g. one popularly considered source in MSSM

Physics: local mass eigenstates do not remain mass eigenstates over L_w

VEV insertion approx [Riotto 96; Carena, Quiros, Riotto, Vilja, Wagner 97]

$$V(x) \equiv v_2(x) - \frac{M}{|M|} v_1(x)$$

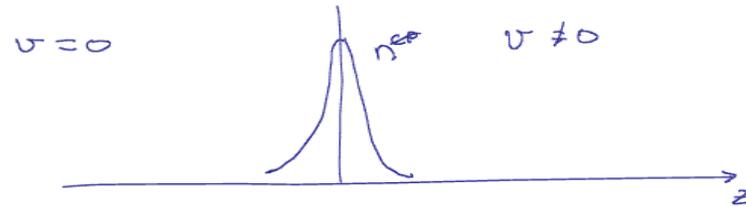
$$\begin{array}{c}
 \left| \begin{array}{c} \tilde{H} \\ \hline \tilde{H} \end{array} \right. \text{---} \left| \begin{array}{c} \tilde{H} \\ \hline \tilde{H} \end{array} \right. + \left| \begin{array}{c} \tilde{H} \\ \hline \tilde{H} \end{array} \right. \begin{array}{c} v(x) \\ \times \\ \tilde{\chi}_i \end{array} \begin{array}{c} v^*(y) \\ \times \\ \tilde{\chi}_i \end{array} \left| \begin{array}{c} \tilde{H} \\ \hline \tilde{H} \end{array} \right|^2 \\
 \text{---} \left| \begin{array}{c} \tilde{H} \\ \hline \tilde{H} \end{array} \right. \text{---} \left| \begin{array}{c} \tilde{H} \\ \hline \tilde{H} \end{array} \right. + \left| \begin{array}{c} \tilde{H} \\ \hline \tilde{H} \end{array} \right. \begin{array}{c} v^*(x) \\ \times \\ \tilde{\chi}_i \end{array} \begin{array}{c} v(y) \\ \times \\ \tilde{\chi}_i \end{array} \left| \begin{array}{c} \tilde{H} \\ \hline \tilde{H} \end{array} \right|^2
 \end{array}$$

$$\propto \alpha_i \text{Im}(m M_i) \underbrace{[v_1(y)v_2(x) - v_1(x)v_2(y)]}_{v_w \beta'(z) v^2(x)}$$

CP asymmetry carriers must be thermally populated.

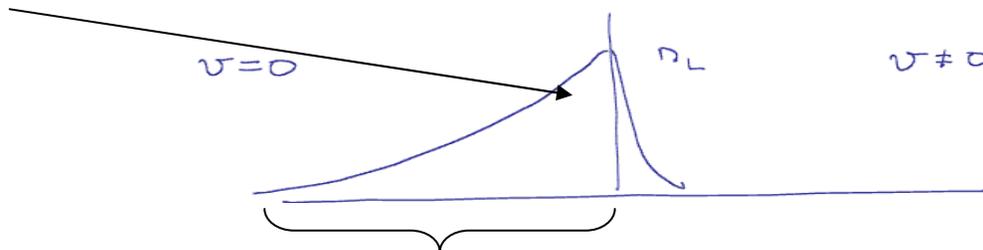
Ingredient 4

- Efficient diffusion is useful [Cohen et al 94; Joyce, Prokopec, Turok 94]



↓ Diffusion

More charge gets out with less damping



$$\frac{D_i}{v_w}$$

$$D_i \sim \frac{1}{\Gamma_i} \frac{\langle \frac{p_z^2}{E^2} \frac{\partial f_0}{\partial E} \rangle}{\langle \frac{\partial f_0}{\partial E} \rangle} \longrightarrow$$

Weakly interacting CP asymmetry carrier.
(Higgs compared to quarks)

Ingredients 5 & 6

- Efficient transfer of CP asymmetry to the B-violating sector
e.g. MSSM and similar scenarios: top Yukawa

also y_b for $\tan\beta \gtrsim 5$
even y_τ for $\tan\beta \gtrsim 15$

[DC, Garbrecht, Ramsey-Musolf, Tulin, 08,09]

- Strong enough phase transition to prevent wash-out

$$\Gamma = A(T) \exp \left[-E^{sph}(T)/T \right] \longrightarrow$$

$$\frac{v(T_c)}{T_c} \gtrsim 1$$

Fixed by
T=0 VEV

What class of
models have
 $T_c \rightarrow 0$?

Requires $O(0.1)$ parametric tuning/hierarchy

Mass about origin.

$$T_c \sim \frac{M_{\text{scalar}}}{O(y/5)} \longrightarrow$$

$$M_{\text{scalar}} \ll v$$

NOT the scalar mass at T=0

Can utilize approximate discrete symmetry to guide parametric tuning.

[DC, Long 10] Pragmatic also for big field space dimension (e.g.8).

Enhanced Symmetry

e.g. 1D

$$V(\phi, T) \approx \left[\frac{M^2}{2} + c_1 T^2 \right] \phi^2 - E \phi^3 + \frac{\lambda}{4} \phi^4$$

At $T = T_c$

$$V(\phi, T_c) = \frac{\phi^2}{4\lambda} (\lambda\phi - 2E)^2$$

At this temperature there is an enhanced \mathbb{Z}_2 symmetry:

$$\phi \rightarrow -\phi + \frac{2E}{\lambda}$$

Choose a parameter to build in this enhanced symmetry at $T=0$.

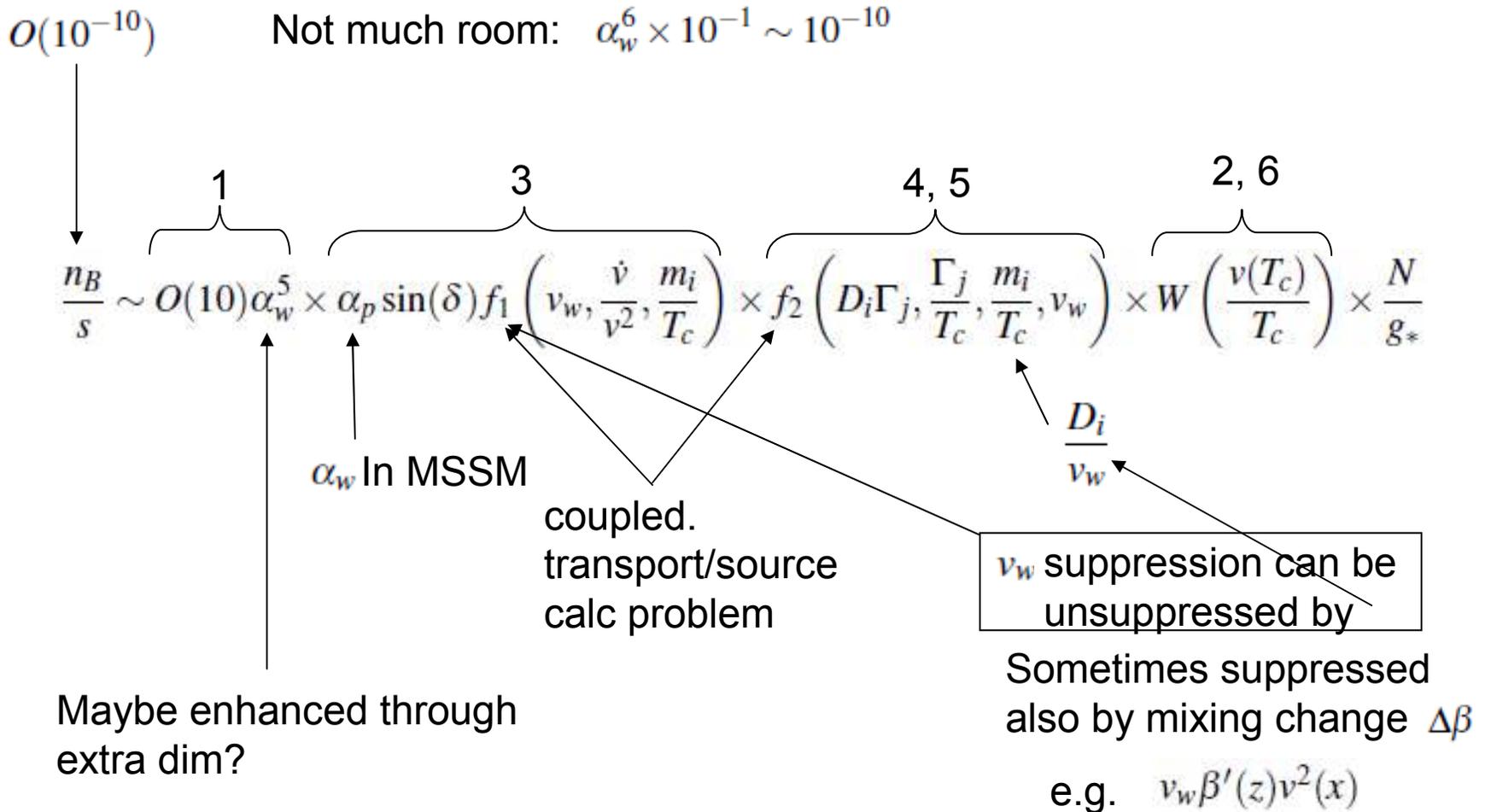
$$\frac{\langle \phi(T_c) \rangle}{T_c} \rightarrow \infty \quad \text{Ideal parametric point!}$$

$\rightarrow 0$ when $E = \sqrt{\frac{\lambda}{2}} M$

Note even in the non-renormalizable operator scenario, there is a symmetry.

BSM ingredients (blue = not generic without singlets; red = tuned):

- 1) High T; 2) bubbles nucleate; 3) bubble coupling to CPV; 4) efficient diffusion; 5) CP charge \rightarrow quarks + leptons;
- 6) B-violating sphaleron suppression in broken phase



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$$\frac{n_B}{s} \sim \overbrace{O(10)\alpha_w^5}^1 \times \overbrace{\alpha_p \sin(\delta) f_1\left(v_w, \frac{\dot{v}}{v^2}, \frac{m_i}{T_c}\right)}^3 \times \overbrace{f_2\left(D_i \Gamma_j, \frac{\Gamma_j}{T_c}, \frac{m_i}{T_c}, v_w\right)}^{4, 5} \times \overbrace{W\left(\frac{v(T_c)}{T_c}\right)}^{2, 6} \times \frac{N}{g_*}$$

α_w In MSSM

coupled.
transport/source
calc problem

Light $m_{\tilde{t}_R}$ for cubic coupling

Higgs mass lower bd

\rightarrow large $m_{\tilde{t}_L} \rightarrow$ decouple

\rightarrow chargino sector

$W\left(\frac{v(T_c)}{T_c}\right)$ corners parameter spaces.

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coupled.
transport/source
calc problem

Enlarge param space with
singlets [Anderson
and Hall 92; Pietroni 93;
many others since then]

Nonrenormalizable ops
[e.g. Zhang 93;
Grojean, Servant, Wells 04;
...; Blum, Nir 08]

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coupled.
transport/source
calc problem

Where the phase occurs allows weaker EDM bounds either through coupling suppression or sector sequestering and/or spontaneous CP violation.

[e.g. recently in sMSSM (4 SM singlets + 2 doublets) Kang, Langacker, Li, Liu 09]

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Picture that emerges:

- 1) The scalar sector will be non-minimal in either d.o.f. and/or physics.
- 2) Either by discrete symmetry or accidental cancellation (0.1 tuning)

$$\frac{v(T_c)}{T_c} \gtrsim 1$$

- 3) CP violation sector is either secluded or we will see EDMs if we continue to push experimental sensitivity.

$$\begin{aligned}
 & O(10^{-10}) \\
 & \downarrow \\
 \frac{n_B}{s} & \sim \overbrace{O(10)\alpha_w^5}^1 \times \alpha_p \sin(\delta) \overbrace{f_1\left(v_w, \frac{\dot{v}}{v^2}, \frac{m_i}{T_c}\right)}^3 \times \overbrace{f_2\left(D_i \Gamma_j, \frac{\Gamma_j}{T_c}, \frac{m_i}{T_c}, v_w\right)}^{4, 5} \times \overbrace{W\left(\frac{v(T_c)}{T_c}\right)}^{2, 6} \times \frac{N}{g_*} \\
 & \alpha_w^6 \times 10^{-1} \sim 10^{-10}
 \end{aligned}$$

coupled.
transport/source
calc problem

A popularly discussed
source of technical
challenges

[Riotto 96; Carena, Quiros, Riotto, Vilja, Wagner 97; Carena, Moreno, Quiros, Seco, Wagner 00; Prokopec, Schmidt, Weinstock 01, 03; Kainulainen, Prokopec, Schmidt, Weinstock 01; Konstandin, Prokopec, Schmidt 04; Huber, Konstandin, Prokopec, Schmidt 06; ...]

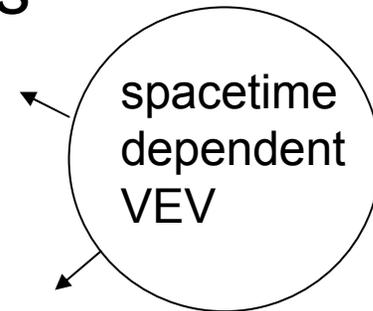
Theoretical Uncertainties

Transport challenges:

- 1) spatially inhomogeneous
- 2) out of equilibrium
- 3) messy thermal kinematics
- 4) many order 1 effects
- 5) BSM can have large number of dof

Approximations involve expansions that can be subtle:

$$\partial_\mu \langle j^\mu(x) \rangle = \int d^4z \left[\underbrace{\Pi^>(x,z)\Delta^<(z,x) - \Delta^>(x,z)\Pi^<(z,x) + \Delta^<(x,z)\Pi^>(z,x) - \Pi^<(x,z)\Delta^>(z,x)}_{\text{Collisions and mixing}} \right]$$



Ideally, want to begin with above

$$v_w \partial_z n_{\hat{H}} - D_{\hat{H}} \partial_z^2 n_{\hat{H}} = -\Gamma_Y \left(\frac{n_{\hat{H}}}{k_{\hat{H}}} - \frac{n_t}{k_t} + \frac{n_q}{k_q} \right) + S_{\hat{H}}^{CPV} + \dots$$

Theoretical Uncertainties

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Collisions and mixing

Ideally, want to begin with above

↓ approximations sometimes very uncertain

$$v_w \partial_z n_{\hat{H}} - D_{\hat{H}} \partial_z^2 n_{\hat{H}} = -\Gamma_Y \left(\frac{n_{\hat{H}}}{k_{\hat{H}}} - \frac{n_t}{k_t} + \frac{n_q}{k_q} \right) + S_{\hat{H}}^{CPV} + \dots$$

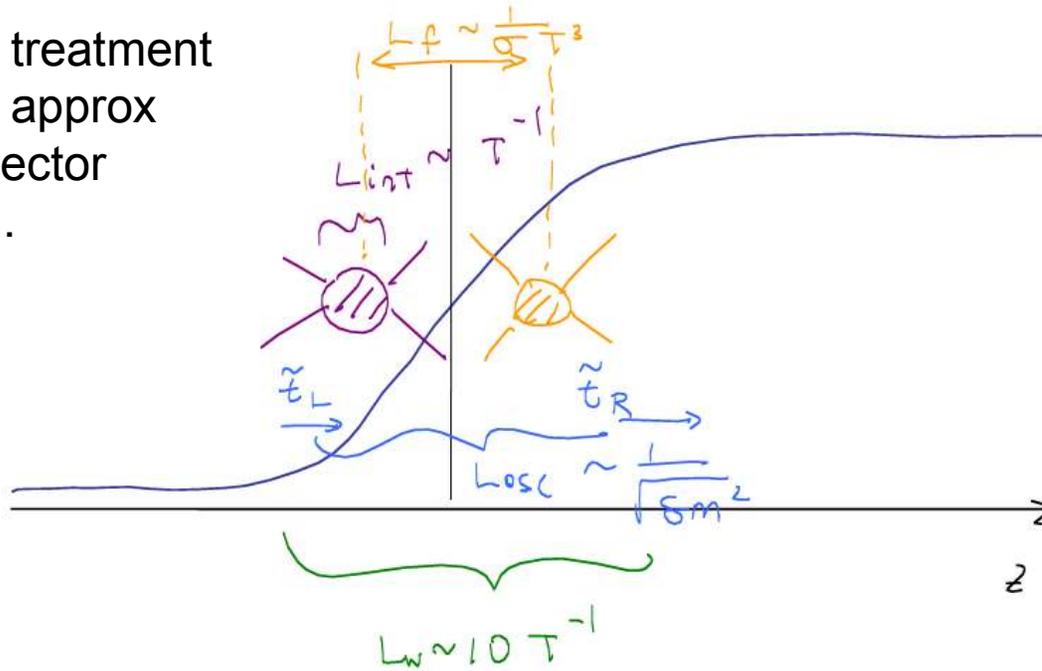
↑ e.g. Resonant regime in MSSM

$\langle j^\mu(x) \rangle$

spacetime
dependent
VEV

[Cirigliano, Lee, Tulin 11] improves upon an aspect of the work by [Konstandin, Prokopec, Schmidt, Seco 05]

Numerical treatment
with fewer approx
in a stop sector
toy model..



$$\epsilon_{\text{coll}} \equiv \frac{L_{\text{int}}}{L_f}$$

$$\epsilon_{\text{wall}} \equiv \frac{L_{\text{int}}}{L_w}$$

$$(u \cdot \partial_x + \mathbf{F} \cdot \nabla_{\mathbf{k}}) f_m(\mathbf{k}, x) = - [i\omega_{\mathbf{k}} + u \cdot \Sigma, f_m(\mathbf{k}, x)] + \mathcal{C}_m[f_m, \bar{f}_m](\mathbf{k}, x)$$

$$[\Sigma, f] = \begin{pmatrix} \Sigma_{12}f_{21} - \Sigma_{21}f_{12} & -\Sigma_{12}(f_{11} - f_{22}) + (\Sigma_{11} - \Sigma_{22})f_{12} \\ \Sigma_{21}(f_{11} - f_{22}) - (\Sigma_{11} - \Sigma_{22})f_{21} & \Sigma_{21}f_{12} - \Sigma_{12}f_{21} \end{pmatrix}$$

$$[\Sigma, f]_{\text{Ref. [9]}} = \begin{pmatrix} 0 & -\Sigma_{12}(n_B(\omega_1) - n_B(\omega_2)) \\ \Sigma_{21}(n_B(\omega_1) - n_B(\omega_2)) & 0 \end{pmatrix} + \mathcal{O}(\epsilon_{\text{wall}}^2)$$

$$\frac{\epsilon_{\text{wall}}^2}{\epsilon_{\text{coll}} v_w} \text{ unsuppression due to integration}$$

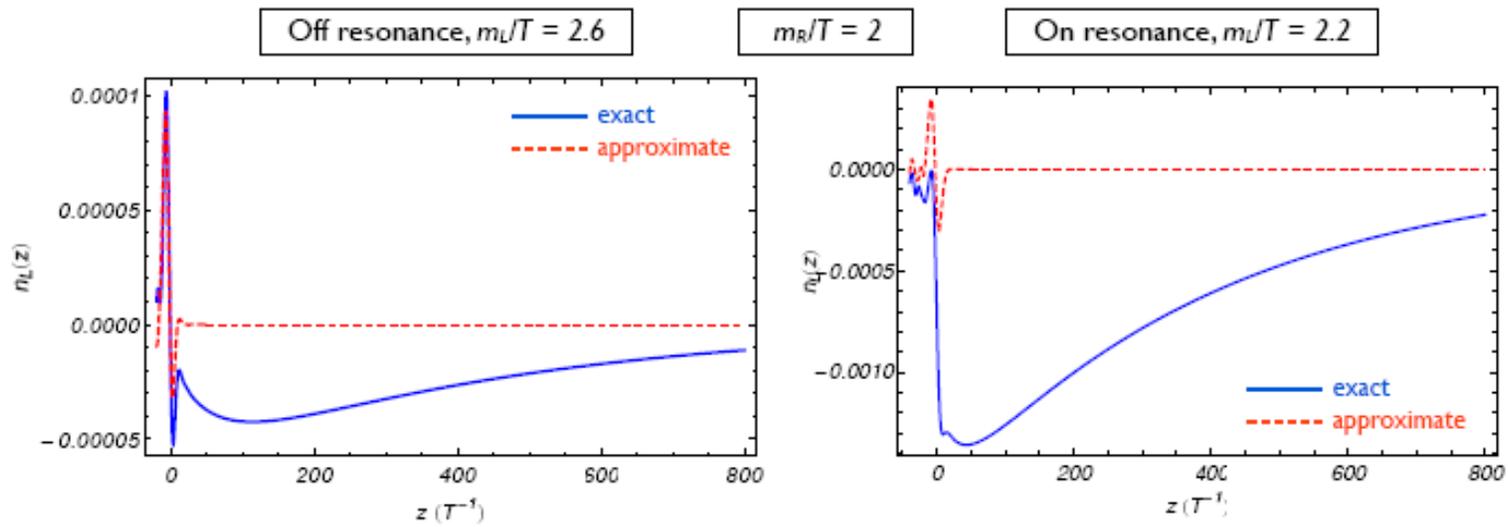


FIG. 7: Charge density profiles $n_L(z)$ from the solution of the full equations (solid line) and the approximate decoupled equations (dashed line) that mimic the procedure of Ref. [9]. The left panel correspond to the off-resonance regime $m_L/T = 2.6, m_R/T = 2$, while the right panel corresponds to the resonant regime $m_L/T = 2.2, m_R/T = 2$.

[Carena, Nardini, Quiros, Wagner 08]

MSSM still viable
based on more
approximate treatment.

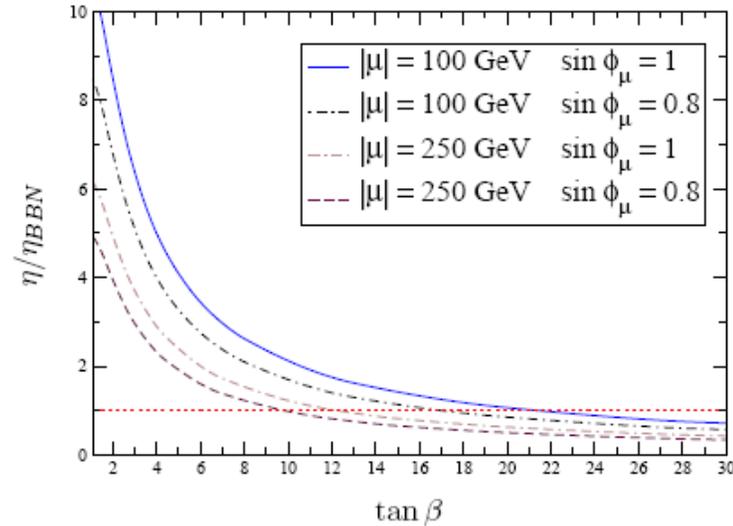


Figure 1: η/η_{BBN} as function of $\tan\beta$ for several values of μ and imposing $\phi(T_H^n)/T_H^n \simeq 1$, $M_1 = M_2 = 200$ GeV, $L_w \simeq 1.7$ and $v_w \simeq 0.1$.

[Konstandin, Prokopec, Schmidt, Seco 05]

MSSM unlikely to be viable

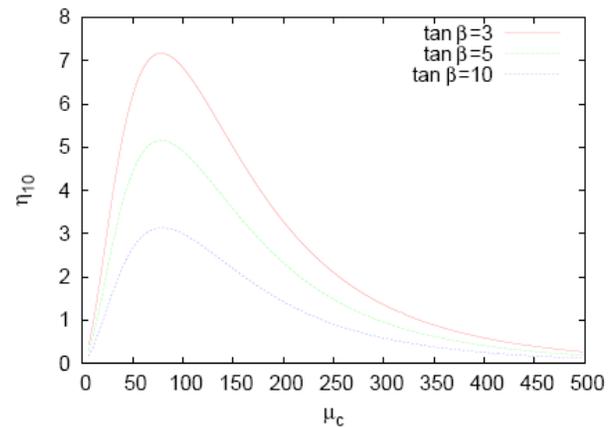


FIG. 6: This plot shows $\eta_{10} = 10^{10}\eta$ as a function of μ_c , $M_2 = \mu_c - 20$ GeV, $m_A = 150$ GeV and for several values of $\tan\beta$.

Although all agree that the window is small,
Its viability is still unclear.

EDM Constraints

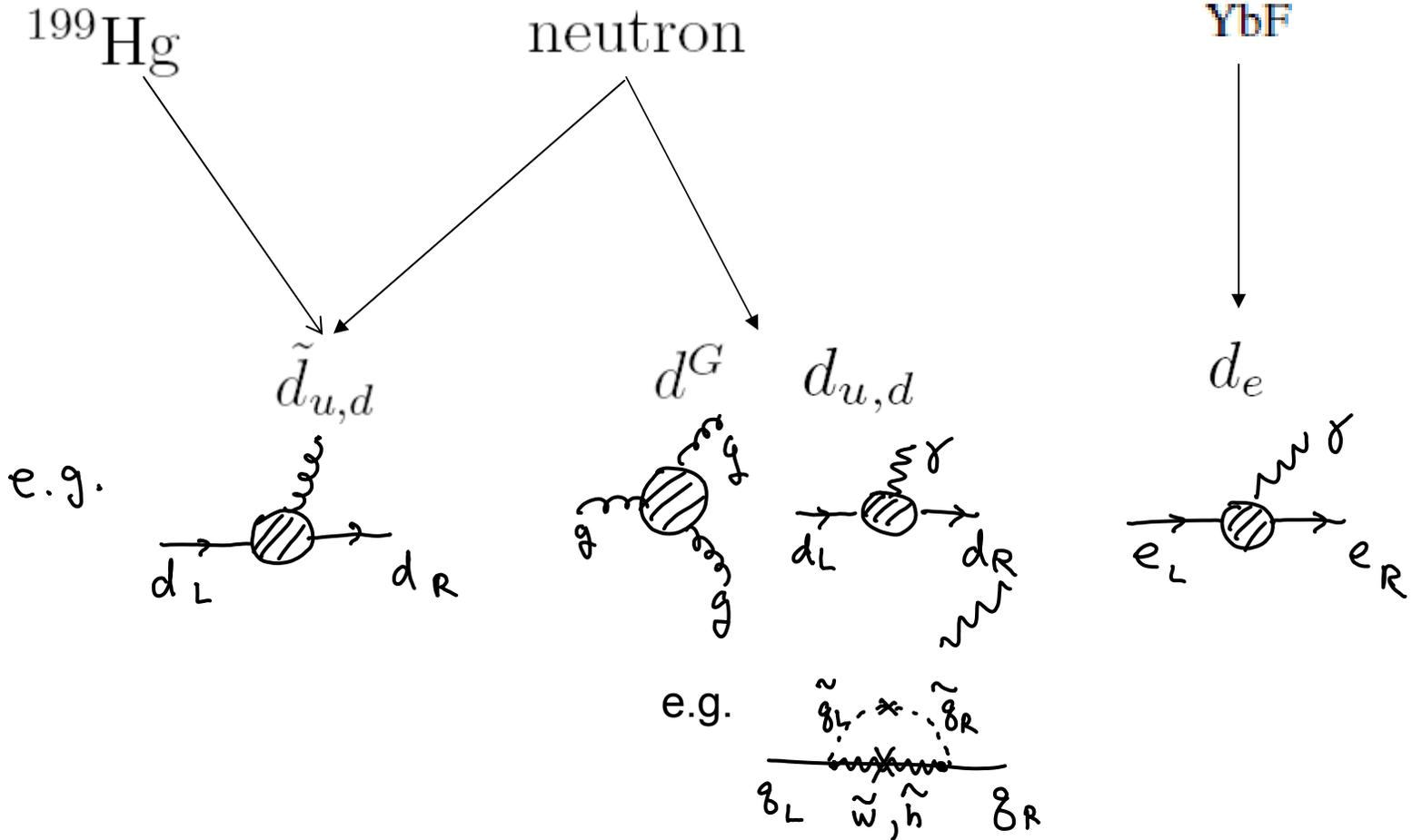
[Baker et al 06; Griffith et al 09; Hudson et al 11]

$$|d_{\text{Hg}}| < 2.9 \times 10^{-29} \text{ e cm}$$

$$|d_n| < 3.5 \times 10^{-26} \text{ e cm}$$

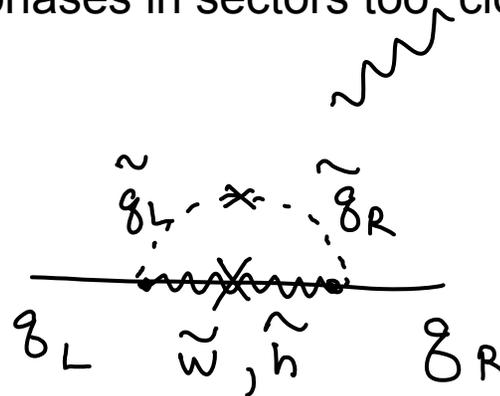
1.5 improvement

$$|d_e| < 10.5 \times 10^{-28}$$



One Loop MSSM

BSM such as MSSM has phases in sectors too "close" to the light particles.



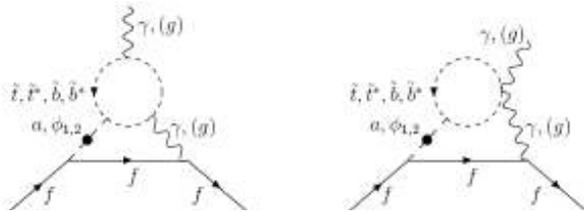
$$\left(\frac{d_{u,d}}{e}\right) \sim (10^{-25} \text{ cm}) \frac{\mathcal{O}(M_2 \mu)}{M_{\tilde{u},\tilde{d}}} \left(\frac{1 \text{ TeV}}{M_{\tilde{u},\tilde{d}}}\right)^2 \left(\frac{m_{u,d}}{10 \text{ MeV}}\right)$$

[Ellis, Ferrara, Nanopoulos 82; Buchmueller and Wyler 83; Polchinski and Wise 83]

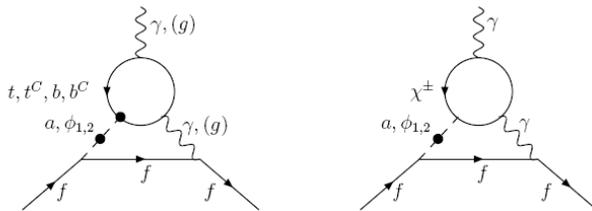
Can make small by taking first two generation sfermion masses large.

2-loops & MSSM Bino

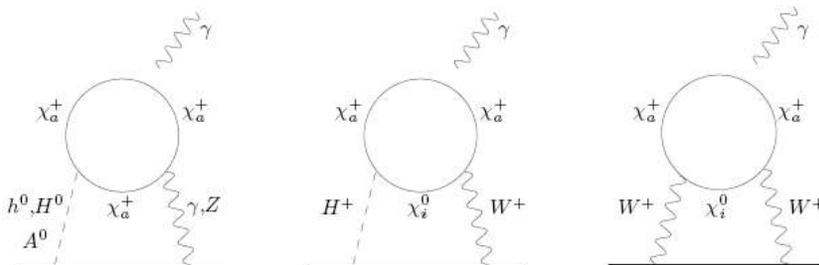
[Barr, Zee (90); Chang, Keung, Pilaftsis (99); Pilaftsis (02)]



$$d_e \propto \tan \beta, \arg(\mu M_2), \frac{1}{M_a}$$



[Li, Profumo, Ramsey-Musolf 08] considered the subdominant neutralino contributions.



$$d_1/d_2 \sim 0.02$$

B-genesis source term is suppressed less, making the tradeoff a good deal.

NMSSM EDM 2-Loop Analysis

[Cheung, Hou, Lee, Senaha 11]

$$W_{\text{NMSSM}} = \widehat{U}^C \mathbf{h}_u \widehat{Q} \widehat{H}_u + \widehat{D}^C \mathbf{h}_d \widehat{H}_d \widehat{Q} + \widehat{E}^C \mathbf{h}_e \widehat{H}_d \widehat{L} + \lambda \widehat{S} \widehat{H}_u \widehat{H}_d + \frac{\kappa}{3} \widehat{S}^3$$

$$(\phi'_\lambda - \phi'_\kappa)$$

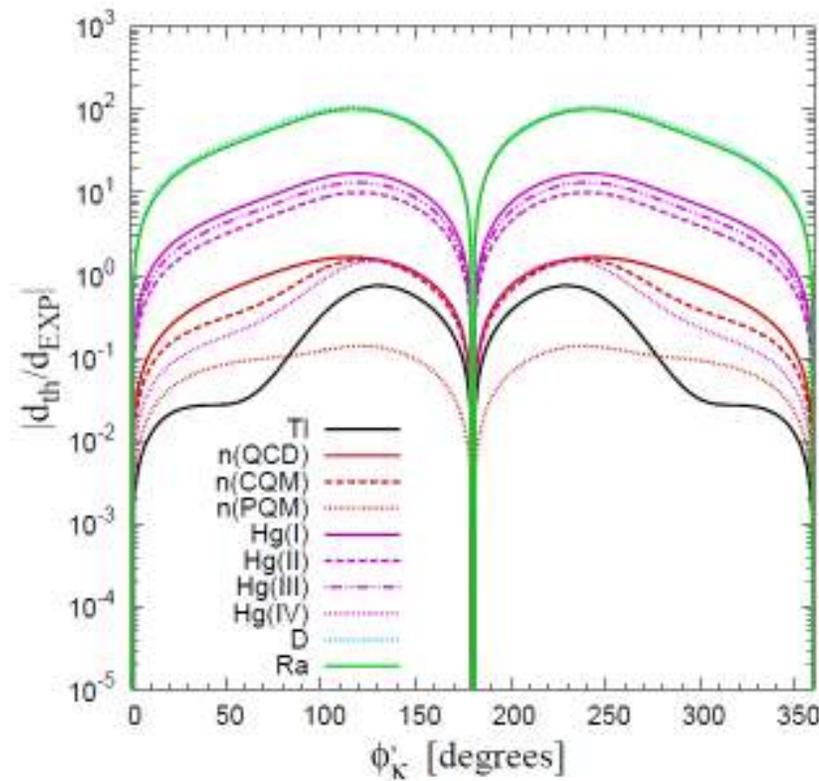


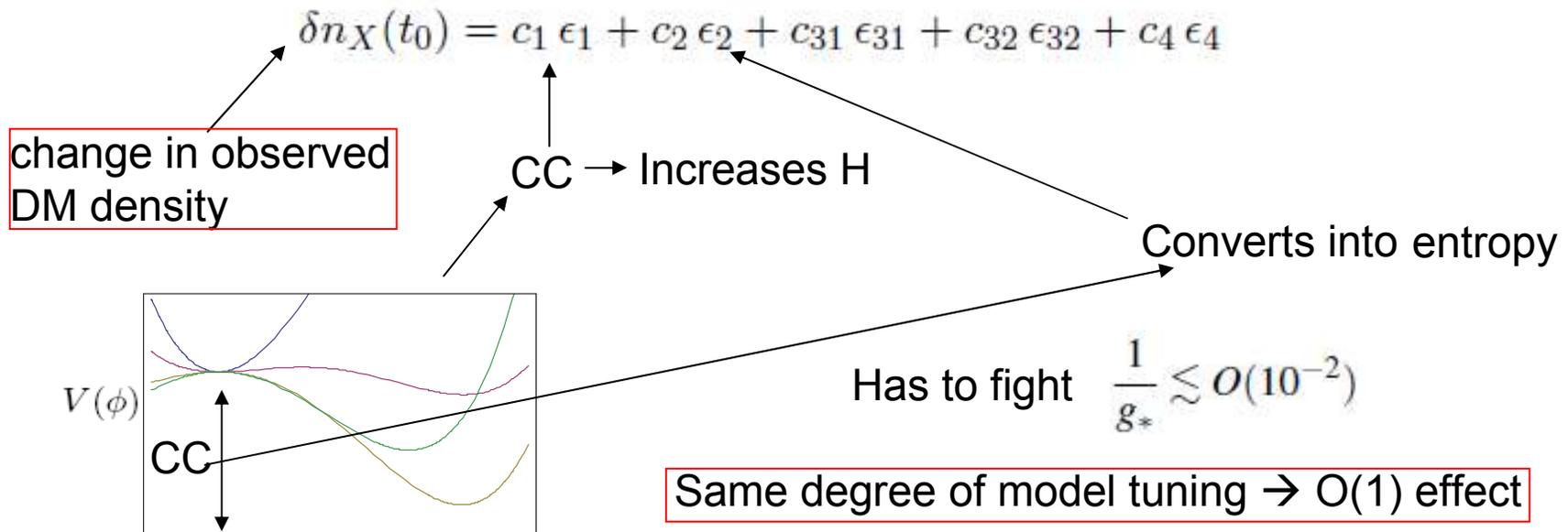
Figure 5: The observable EDMs taking $|\lambda| = 0.81$, $|\kappa| = 0.08$, $|A_\lambda| = 575$ GeV, and $A_\kappa = 110$ GeV. The other parameters are fixed as in Eq. (51)

PT Phenomenon can be correlated

- Electroweak Baryogenesis
- Gravity Waves: Bubble stirs up fluid
- DM: Freeze out physics can be affected
- CC: IR contribution

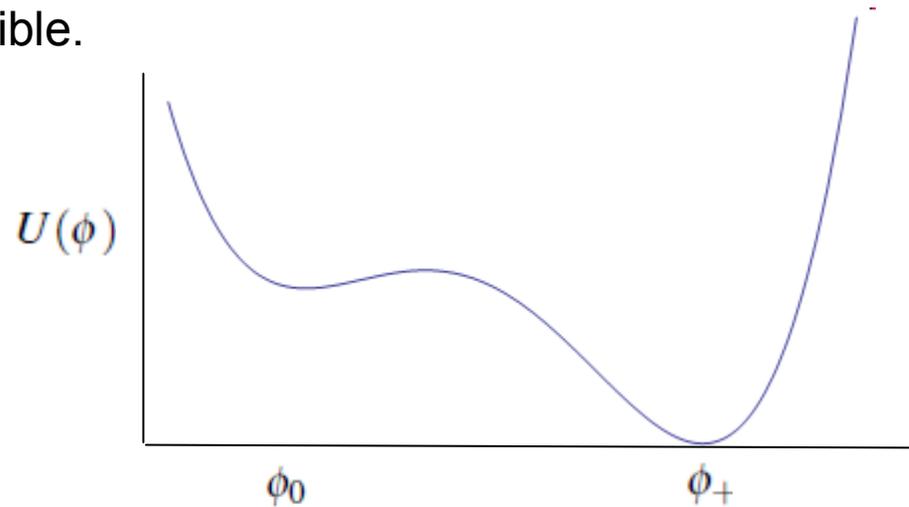
e.g. DM can be used to probe phase transitions

[DC, Long, Wang 11]



For this program to work: reconstruct EWSB PT from collider measurements.

A remarkable feat if possible.



$$\langle \phi_0, \vec{p} | \phi_+, \vec{k} \rangle \propto \lim_{\Omega \rightarrow \infty} \exp(-\Omega^n c) = 0$$

Because Legendre transformation breaks down, no linear source induced shift $\phi_+ \rightarrow \phi_0$ is possible. Dim 0, 1, 2 UV-IR mixing \rightarrow ambiguity in tachyonic region

Hence, remarkable if few particle collisions \longrightarrow non-perturbative condensation information

Question: What are the implicit assumptions that are used in the literature and what alternative assumptions might exist? [work in progress]

Conclusions

- 1) Electroweak Bgenesis predictions:
 - a) The scalar sector will be non-minimal either in d.o.f. and/or physics.
 - b) There is likely to be a discrete symmetry or an accidental cancellation in the scalar sector.
 - c) CP violation sector is either secluded or we will see EDMs if we continue to push experimental sensitivity. If secluded, richer spectrum is likely explaining why we do not see EDMs.
- 2) CPV source/diffusion computation technology is converging, although still incomplete.
- 3) Reconstructibility of the EWPT without non-perturbative data is not obvious. Correlated probes such as DM and gravity waves might provide complementary data.