

# *On a model with two scalar leptoquarks - $R_2$ and $S_3$*

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*[2103.12504] & [2206.09717]*

# Motivation: LFUV in CC and NC

- Hints of lepton flavor universality violation in  $b \rightarrow s\ell\ell$  and  $b \rightarrow c\ell\nu$

$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\mu\nu)} \quad R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\mathcal{B}(B \rightarrow K^{(*)}e^+e^-)} \Bigg|_{q^2 \in [q_{\min}^2, q_{\max}^2]}$$

- EFT allows for **model-independent** constraints on **New Physics** couplings.
- Can we build an **Explicit Scenario** to explain both anomalies?
  - CC are tree-level in the SM, FCNC are loop-induced.
  - The NP couplings to FCNC must be much smaller than to CC in order to have a common NP scale.

# Low Energy EFT

- Low energy observable,  $m_b \sim m_b^{\overline{\text{MS}}}(m_b) \simeq 4.2 \text{ GeV}$ .
- Assuming NP at a scale  $\Lambda \gtrsim \mathcal{O}(1 \text{ TeV})$ , can be computed using EFT.

Charged Lagrangian :

$$\mathcal{L}_{\text{NP}} \supset -\frac{4G_F V_{ij}}{\sqrt{2}} \sum_X g_X \mathcal{O}_X + \text{h.c.}$$

$$X \in V_L, V_R, S_R, S_L, T$$

Neutral Lagrangian :

$$\mathcal{L}_{\text{NP}} \supset -\frac{4G_F V_{ti} V_{tj}^*}{\sqrt{2}} \sum_X (\delta C_X \mathcal{O}_X + \delta C'_X \mathcal{O}'_X) + \text{h.c.}$$

$$X \in 9, 10, S, P, \dots$$

$$\mathcal{O}_X = (\bar{q}_i \Gamma q_j)(\bar{\ell}_\alpha \Gamma \ell_\beta) \quad \text{with} \quad \Gamma \in P_{L/R}, \gamma^\mu P_{L/R}, \sigma^{\mu\nu} P_L$$

- In the SM:

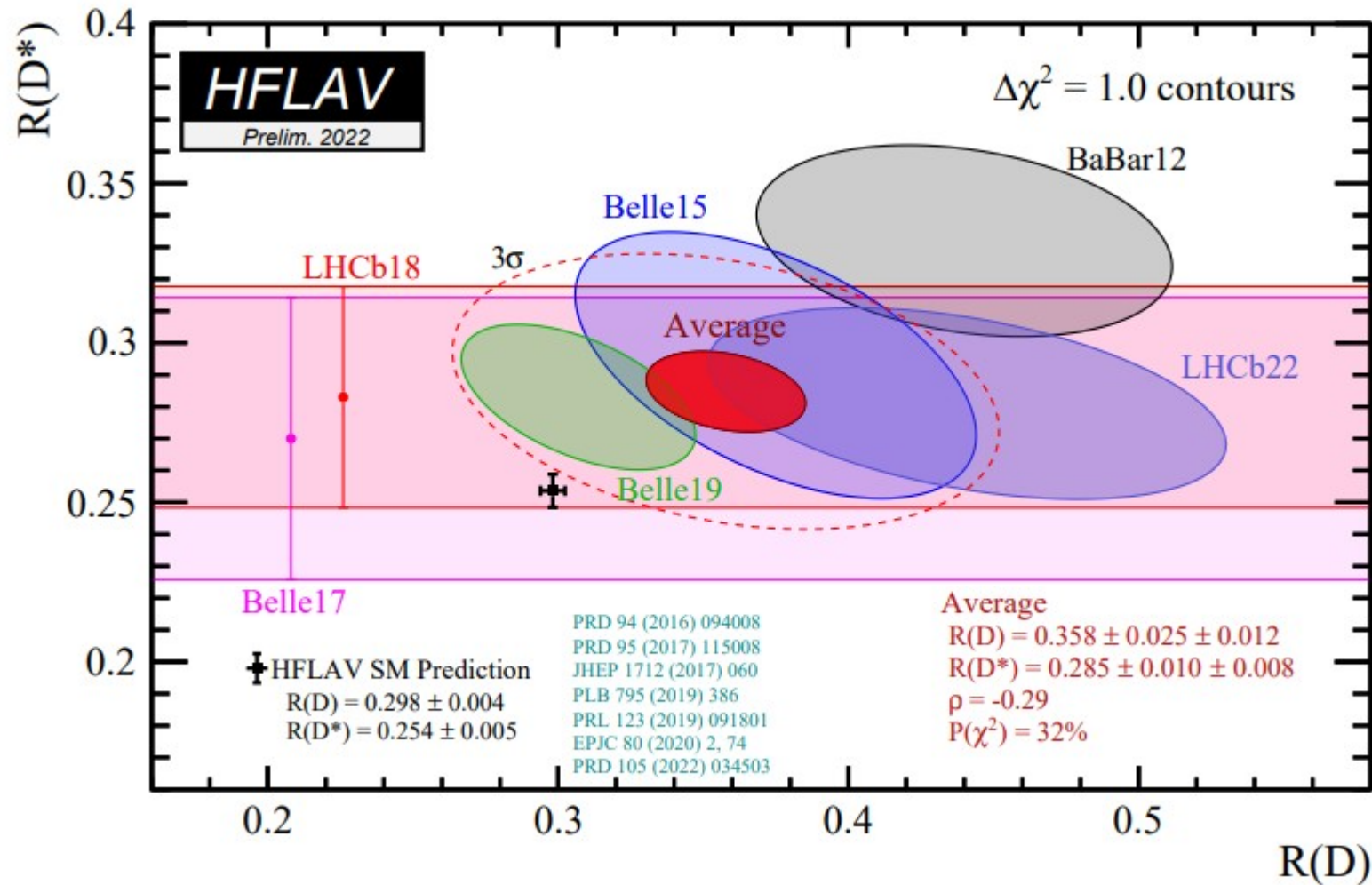
$$g_{V_L} = 1 \quad \text{From tree-level W exchange.}$$

→ Vector – Axial current.

$$g_i = 0 \quad (i \in V_R, S_{R/L}, T)$$

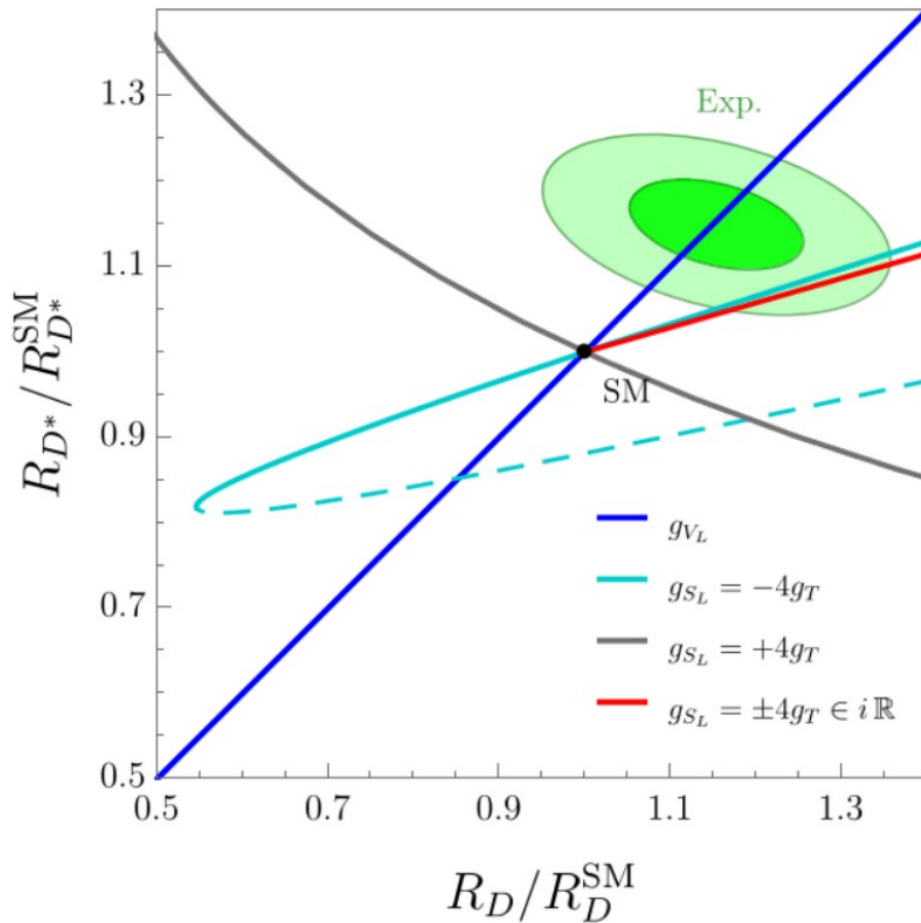
$$\begin{array}{c} \delta C_{9,10} \neq 0 \\ \swarrow \quad \nwarrow \\ \text{Vector} \quad \text{Axial (leptonic)} \end{array}$$

# Experimental Status: Charged currents

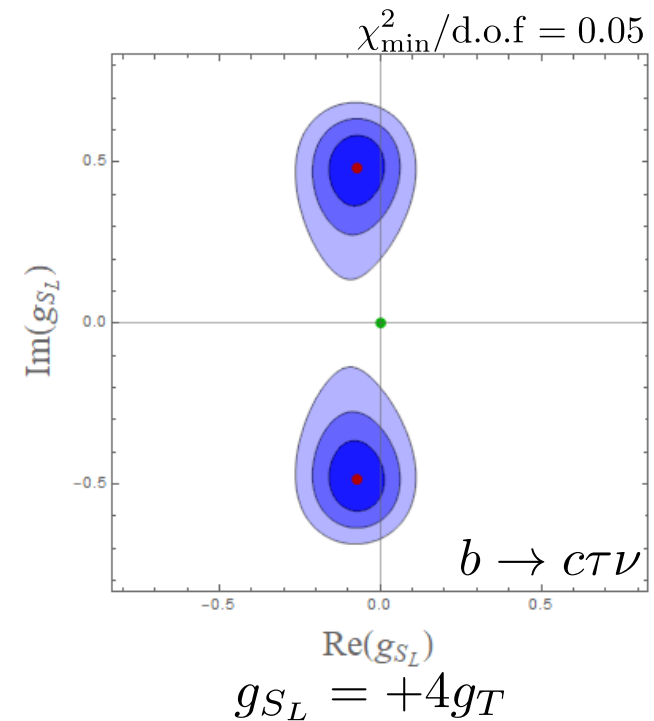


# Charged currents: Fit scenarios

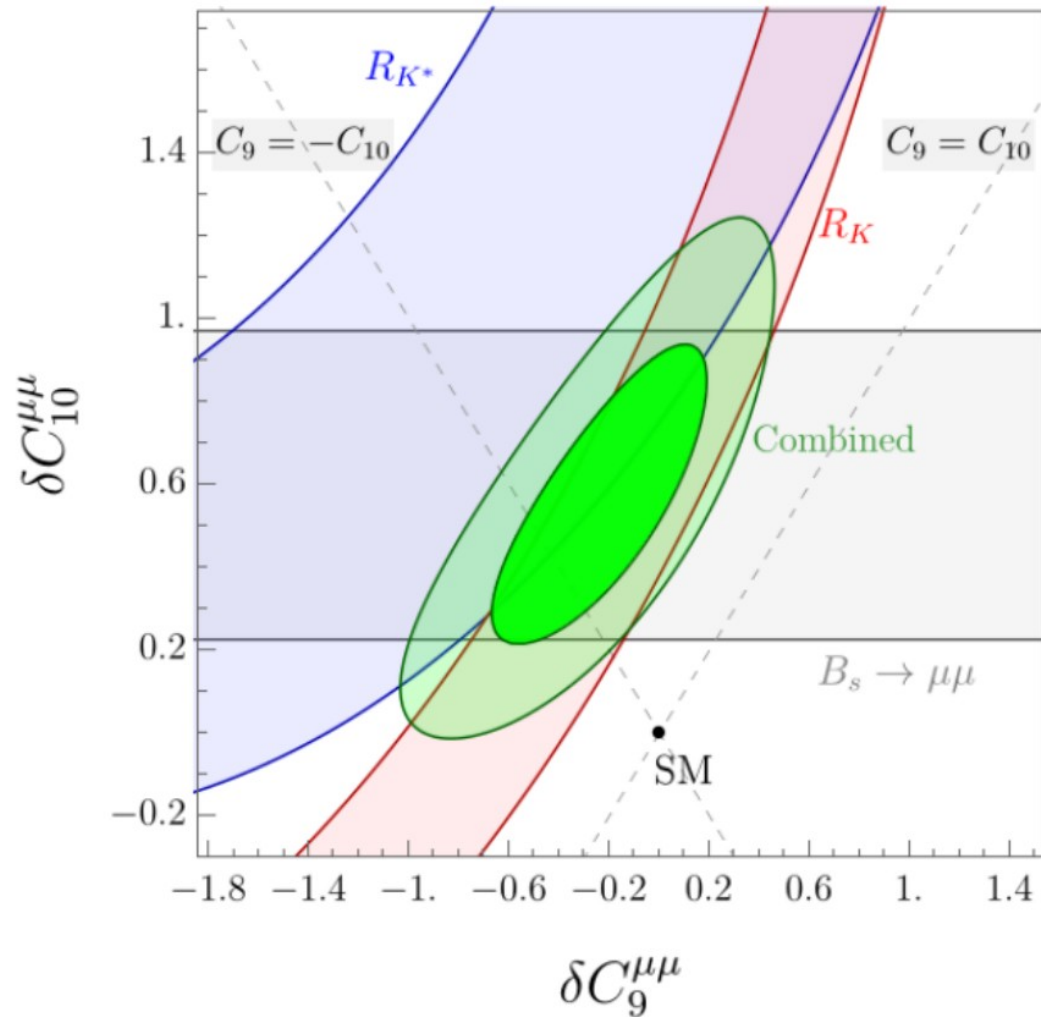
- Single Coefficient fit
- Motivated by NP scenarios



Wilson Coefficient	$R(D)$ and $R(D^*)$	$\chi^2_{\text{min}}/\text{d.o.f}$
$g_{V_L}$	$0.084 \pm 0.029$	0.06
$g_{S_L}$	$-1.47 \pm 0.08$	0.5
$g_T$	$-0.027 \pm 0.011$	1.2
$g_{S_L} = +4g_T \in i\mathbb{R}$	$\pm 0.49 \pm 0.10$	0.9
$g_{S_L} = -4g_T$	$0.16 \pm 0.06$	0.7



# Neutral currents, Fit scenarios

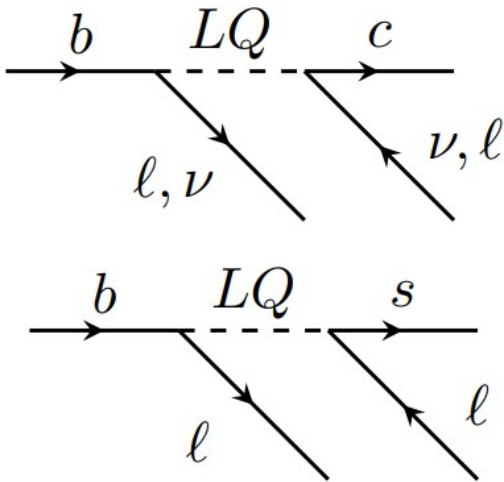
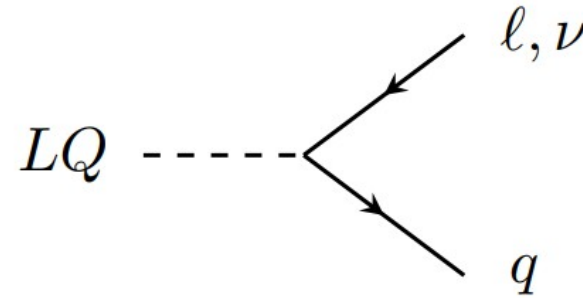


- Using only the cleanest observables.
- See e.g. [W. Altmannshofer, P. Stangl '21] for a global analysis.
- $\delta C_9 = -\delta C_{10} = -0.41 \pm 0.09$
- $4.6\sigma$

# Simplified models: Which NP to explain the anomalies?

- NP mediator should couple to quarks and leptons.
- Should allow for LFUV.

→ **LEPTOQUARKS**



Name	$SU(3)_C \times SU(2)_L \times U(1)_Y$
$S_1$	$(\bar{3}, 1, 1/3)$
$S_3$	$(\bar{3}, 3, 1/3)$
$R_2$	$(3, 2, 7/6)$
$U_1$	$(3, 1, 2/3)$
$U_3$	$(3, 3, 2/3)$

} Scalar LQ  
 } Vector LQ

- FCNC become **tree-level**

# LQ and low energy constraints

- Only  $U_1$  can explain both anomalies.
  - Being a vector state, it requires a UV-completion. [Isidori et al.]
- Combinations of 2 Scalars are also considered.

E.g. [Marzocca '18], [Becirevic '18],[This work]

Model	$R_{D(*)}$	$R_{K(*)}$	$R_{D(*)}&R_{K(*)}$	
$S_1(\bar{3}, 1, 1/3)$	✓	✗	✗	} Scalar LQ
$R_2(3, 2, 7/6)$	✓	✓/✗*	✗	
$S_3(\bar{3}, 3, 1/3)$	✗	✓	✗	
$U_1(3, 1, 2/3)$	✓	✓	✓	} Vector LQ
$U_3(3, 3, 2/3)$	✗	✓	✗	



# $R_2 - S_3$ Model

$$\begin{aligned}
 R_2(3, 2, 7/6) : \quad \mathcal{L}_{R_2} &= Y_R^{ij} \bar{Q}_i \ell_{Rj} R_2 + Y_L^{ij} \bar{u}_{Ri} L_j \widetilde{R_2}^\dagger + \text{h.c.} \\
 &= (V Y_R E_R^\dagger)^{ij} \bar{u}_{Li} \ell_{Rj} R_2^{5/3} + (Y_R E_R^\dagger)^{ij} \bar{d}_{Li} \ell_{Rj} R_2^{2/3} \\
 &\quad + (U_R Y_L)^{ij} \bar{u}_{Ri} \nu_{Lj} R_2^{2/3} - (U_R Y_L)^{ij} \bar{u}_{Ri} \ell_{Lj} R_2^{5/3} + \text{h.c.}
 \end{aligned}$$

$$\begin{aligned}
 S_3(\bar{3}, 3, 1/3) : \quad \mathcal{L}_{S_3} &= Y^{ij} \bar{Q}_i^C i\tau_2 (\tau \cdot S_3) L_j + \text{h.c.} \\
 &= -(Y)^{ij} \bar{d}_{Li}^C \nu_{Lj} S_3^{1/3} + \sqrt{2} (V^* Y)^{ij} \bar{u}_{Li}^C \nu_{Lj} S_3^{-2/3} \\
 &\quad + \sqrt{2} (Y)^{ij} \bar{d}_{Li}^C \ell_{Lj} S_3^{4/3} - (V^* Y)^{ij} \bar{u}_{Li}^C \ell_{Lj} S_3^{1/3} + \text{h.c.}
 \end{aligned}$$

- Assumptions:

$$Y_R E_R^\dagger = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & y_R^{b\tau} \end{pmatrix},$$

- Only 4 NP parameters:

$$y_R^{b\tau}, y_L^{c\mu}, y_L^{c\tau}, \theta.$$

$$\begin{aligned}
 Y = -Y_L = - \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & \sin \theta \\ 0 & -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} 0 & 0 & 0 \\ 0 & y_L^{c\mu} & y_L^{c\tau} \\ 0 & 0 & 0 \end{pmatrix}, & \longrightarrow \begin{aligned} y^{b\mu} &= \sin \theta y_L^{c\mu}, \\ y^{s\mu} &= -\cos \theta y_L^{c\mu}. \end{aligned} \\
 \parallel & \\
 U_R &
 \end{aligned}$$

# $R_2 - S_3$ , simple GUT-inspired model

- $R_2$  and  $S_3$  can be embedded in an  $SU(5)$  grand unified symmetry.
- SM Fermions:  $\bar{\mathbf{5}}_i = (L, \bar{d}_R)_i$ ,  $\mathbf{10}_i = (\bar{e}_R, \bar{u}_R, Q)_i$
- Scalars:  $R_2, R'_2 \in \mathbf{45}, \mathbf{50}$ ,  $S_3 \in \mathbf{45}$
- Couplings:  $\mathbf{10}_i \bar{\mathbf{5}}_j \mathbf{45}$ ,  $\mathbf{10}_i \mathbf{10}_j \mathbf{50}$ ,  ~~$\mathbf{10}_i \bar{\mathbf{10}}_j \mathbf{45}$~~   
→ Forbidden by proton decay
- Mixing:  $\mathbf{45} \bar{\mathbf{50}} \mathbf{24}$   
→  $R_2$  and  $R'_2$  can mix so that only  $R_2$  is light.
- Imposes  $Y = -Y_L$ .

# Matching

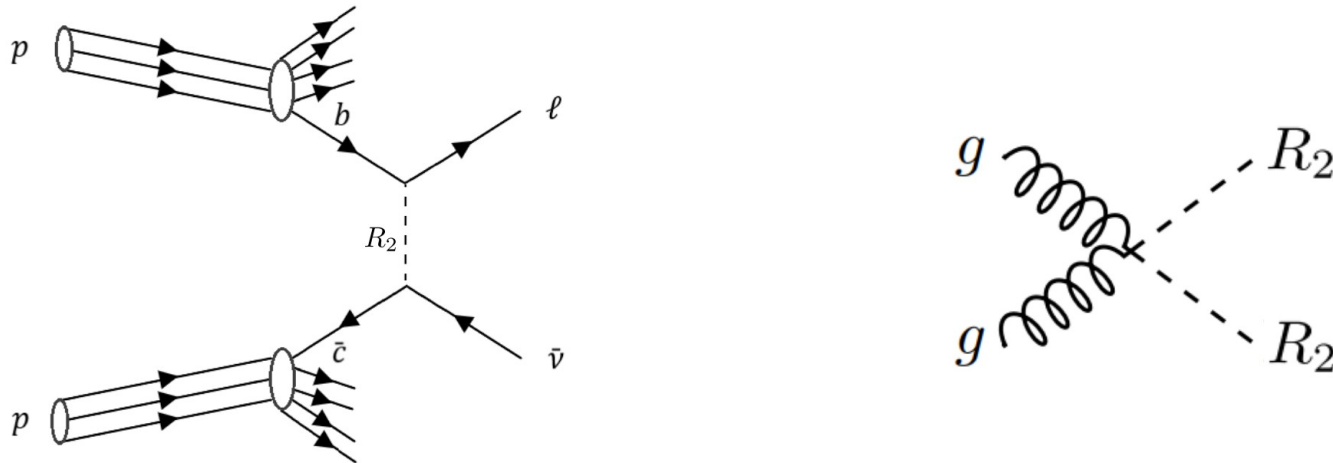
- Charged Currents:  $\mathcal{L} \supset \frac{y_L^{c\tau} y_R^{b\tau*}}{m_{R_2}^2} \left[ (\bar{c}_R b_L)(\bar{\tau}_R \nu_L) + \frac{1}{4} (\bar{c}_R \sigma_{\mu\nu} b_L)(\bar{\tau}_R \sigma_{\mu\nu} \nu_L) \right]$   
 $\longrightarrow g_{S_L} = 4g_T$   
 (At the matching scale)

- Neutral Currents:  $\mathcal{L} \supset \sin(2\theta) \frac{|y_L^{c\mu}|^2}{m_{S_3}^2} (\bar{s}_L \gamma^\mu b_L)(\bar{\mu}_L \gamma_\mu \mu_L)$   
 $\downarrow$   
 Needs to be small  $\longrightarrow C_9 = -C_{10}$

- Contribution to  $\Delta m_{B_s}$ :

$$\propto \frac{\sin(2\theta)^2}{16\pi^2} \frac{(|y_L^{c\mu}|^2 + |y_L^{c\tau}|^2)^2}{m_{S_3}^2} (\bar{s}_L \gamma^\mu b_L)(\bar{s}_L \gamma_\mu b_L) \longrightarrow \text{Safe}$$

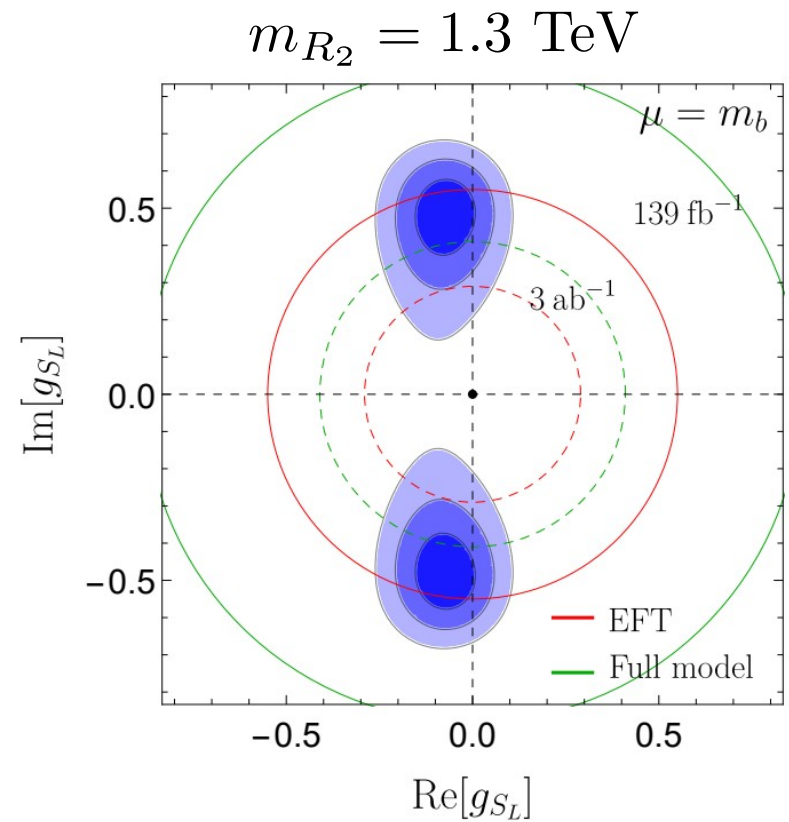
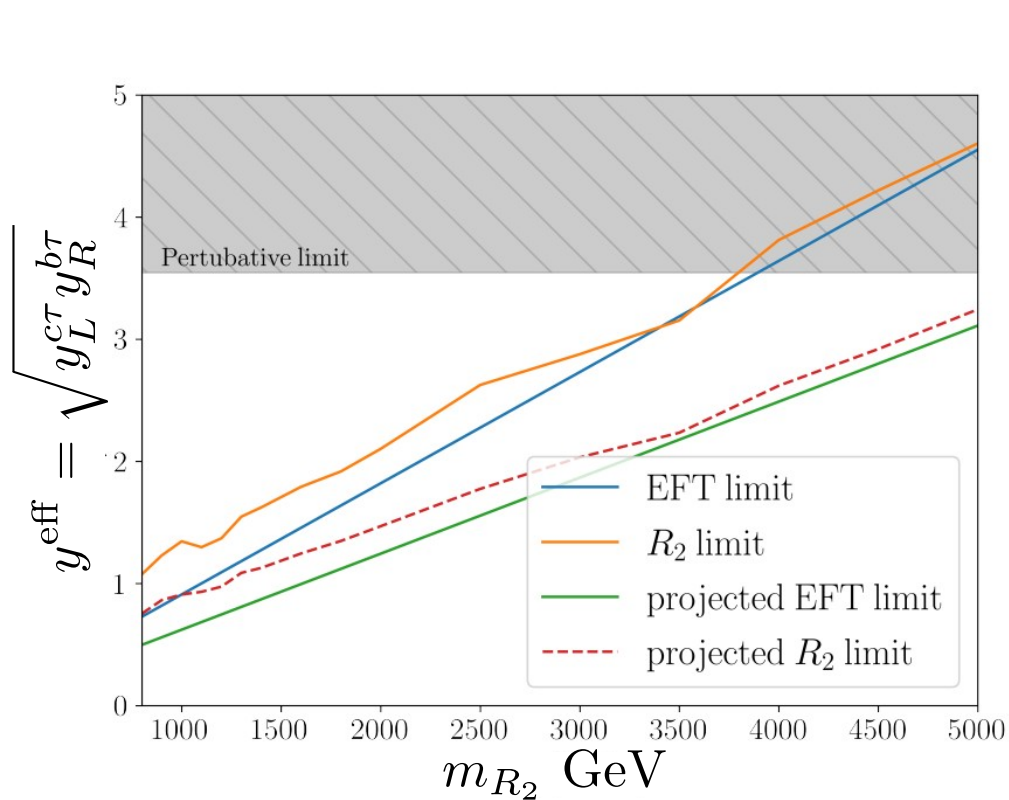
# High- $p_T$ observables



- 2 main signatures at LHC: **pair-production** and **di-lepton**.
- Pair-production gives lower bounds on the masses: 1.3 TeV.
- Di-lepton partonic cross-section is **energy-enhanced** compared to SM.
  - can overcome the heavy quark suppression in the high- $p_T$  tail.

$$\hat{\sigma}(\hat{s}) \simeq \frac{|V_{cb}|^2 G_F^2 \hat{s}}{18\pi} \left[ \frac{3}{4} |g_{SL}|^2 + 4 |g_T|^2 \right]$$

# High- $p_T$ observables

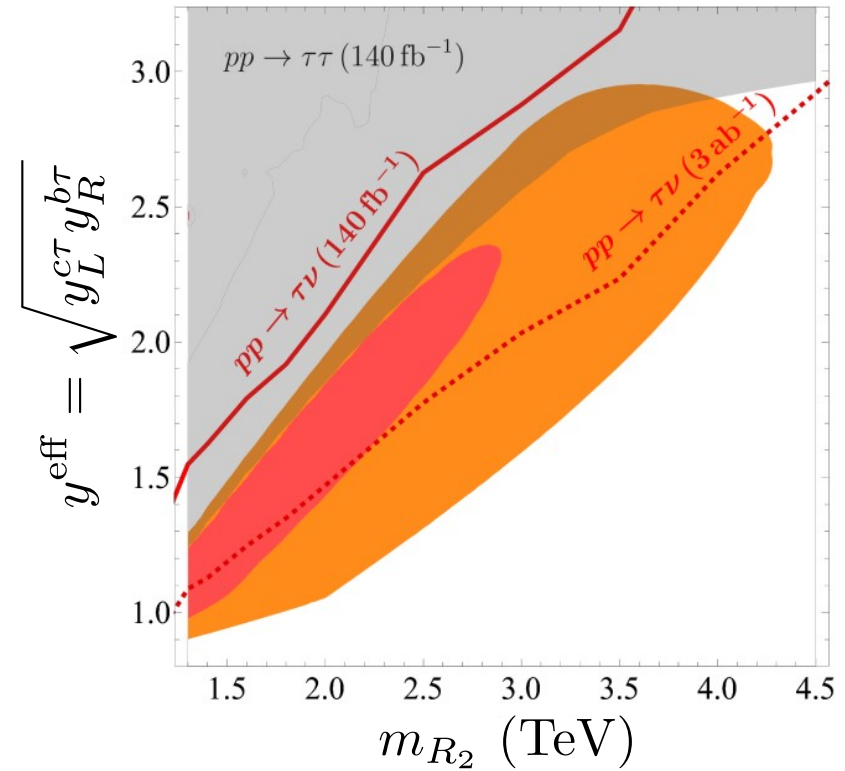
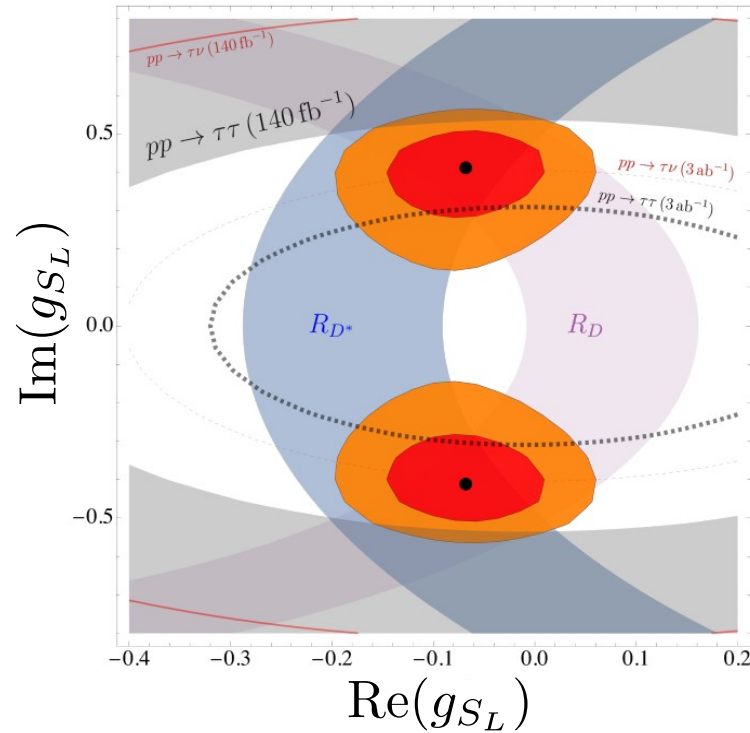


- EFT expansion overestimates the constraints for  $m_{R_2} \lesssim 2 \text{ TeV}$ .
- High- $p_T$  constraints are becoming competitive with flavor.

See talk by **Lukas Allwicher**

# Results

$$m_{R_2} = 1.3 \text{ TeV}, m_{S_3} = 2.0 \text{ TeV}$$



- Big regions of parameter space remains compatible with flavor.
- High- $p_T$  constraints are starting to probe regions allowed by low-energy observables.
- Other constraints from:

$$B_c \rightarrow \tau\nu$$

$$\Delta m_{B_s}$$

$$\tau \rightarrow \mu\phi$$

$$Z \rightarrow \ell\ell$$

$$B \rightarrow K^{(*)}\nu\nu$$

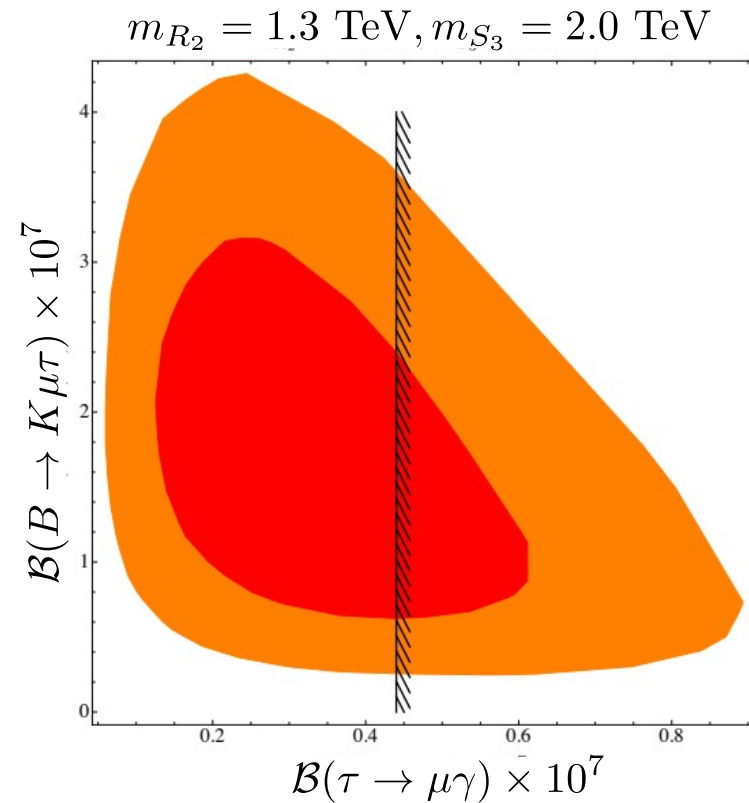
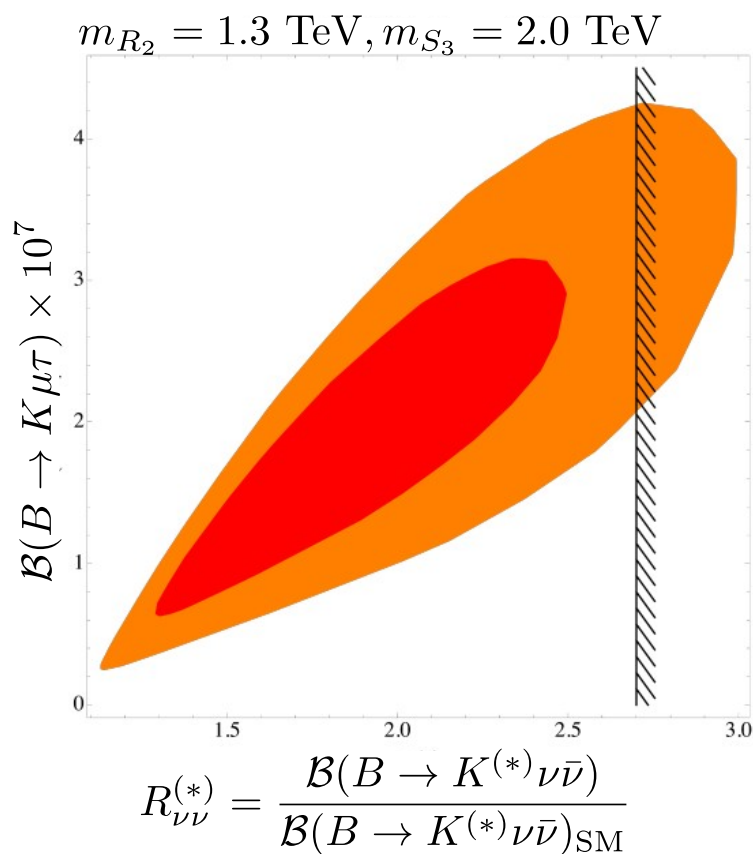
$$B \rightarrow D^{(*)}\mu\nu/e\nu$$

$$W \rightarrow \ell\nu$$

$$D_s \rightarrow \tau\nu/\mu\nu$$

...

# Some predictions : LFV and $R_{\nu\nu}^{(*)}$



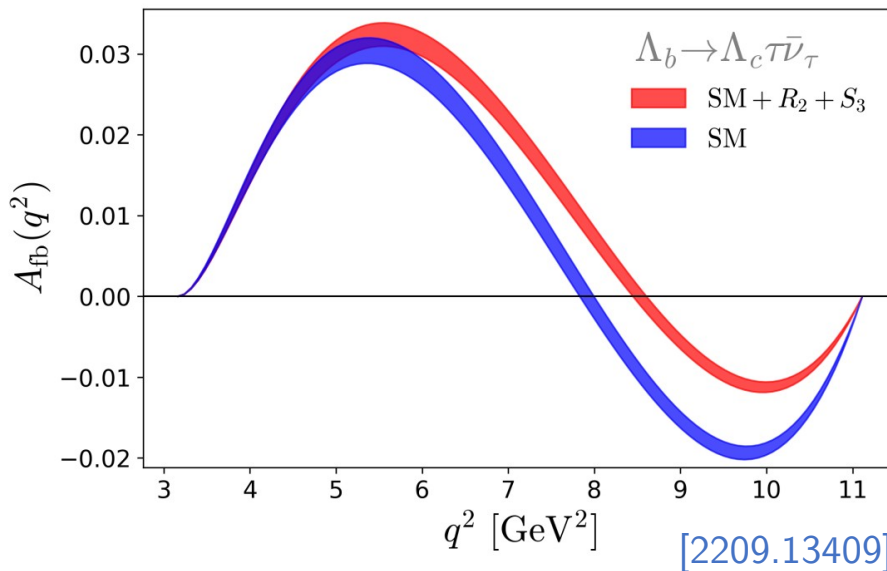
- Large value of  $R_{\nu\nu}^{(*)}$ ,  $\longrightarrow$  can become a very strong constraint in the future.
- Lower bounds for LFV decays !

# Some predictions: angular observables

$$B \rightarrow D\tau\bar{\nu}$$

$$B \rightarrow D^*(\rightarrow D\pi)\tau\bar{\nu}$$

$$\Lambda_b \rightarrow \Lambda_c(\rightarrow \Lambda\pi)\tau\bar{\nu}$$



$$\frac{d^4\Gamma^{\lambda_l}}{dq^2 d\cos\theta d\cos\theta_\Lambda d\phi} = A_1^{\lambda_l} + A_2^{\lambda_l} \cos\theta_\Lambda$$

$$+ \underbrace{\left( B_1^{\lambda_l} + B_2^{\lambda_l} \cos\theta_\Lambda \right)}_{\mathcal{A}_{\text{fb Lepton}}} \cos\theta$$

$$+ \left( C_1^{\lambda_l} + C_2^{\lambda_l} \cos\theta_\Lambda \right) \cos^2\theta$$

$$+ \left( D_3^{\lambda_l} \sin\theta_\Lambda \cos\phi + D_4^{\lambda_l} \sin\theta_\Lambda \sin\phi \right) \sin\theta$$

$$+ \left( E_3^{\lambda_l} \sin\theta_\Lambda \cos\phi + E_4^{\lambda_l} \sin\theta_\Lambda \sin\phi \right) \sin\theta \cos\theta$$

$\mathcal{A}_{\text{fb Baryon}}$

$\mathcal{A}_{\text{fb Lepton}}$

$\text{NP Phase}$

- **Scalar** and **Tensor** operators change the angular structure of semileptonic B decays.
- Some observables are sensitive to the **CP-violating phase** ( $D_4, E_4$ ).

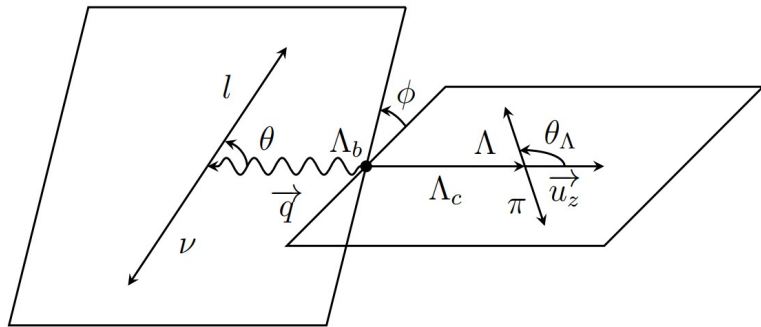


# Conclusion

- Simplified models that can accommodate both kind of anomalies :
  - 1 vector Leptoquark
  - 2 Scalar Leptoquarks
- We proposed and explored a scenario involving  $R_2$  and  $S_3$  .
- With only 4 NP parameters and LQ masses, we can accommodate a plethora of low-energy observables.
- Direct Searches at LHC and the study of high- $p_T$  tails provide complementary and competitive constraints to low-energy observable.
- We make several testable predictions:
  - Lower bounds on LFV decays,
  - $R_{\nu\nu}^{(*)}$ ,
  - Many observable hidden in the angular distributions of b-hadron decays:  $B \rightarrow D^*(\rightarrow D\pi)\tau\bar{\nu}$ ,  $\Lambda_b \rightarrow \Lambda_c(\rightarrow \Lambda\pi)\tau\bar{\nu}$ .

# Some observables

- 40 ~~20~~ 18 observables in total for Baryons.
- Some combinations can be measured by event counting:
  - $\Gamma_{\text{tot}} \propto A_1 + C_1/3$
  - $A_{\text{fb}}^{\ell} \propto B_1$  Forward-Backward Asymmetry (lepton)
  - $A_{\text{fb}}^{\Lambda} \propto A_2 + C_2/3$  Forward-Backward Asymmetry (Baryon)
  - ...



$$\frac{d^4\Gamma^{\lambda_i}}{dq^2 d\cos\theta d\cos\theta_{\Lambda} d\phi} = A_1^{\lambda_i} + A_2^{\lambda_i} \cos\theta_{\Lambda}$$

$$+ (B_1^{\lambda_i} + B_2^{\lambda_i} \cos\theta_{\Lambda}) \cos\theta$$

$$+ (C_1^{\lambda_i} + C_2^{\lambda_i} \cos\theta_{\Lambda}) \cos^2\theta$$

$$+ (D_3^{\lambda_i} \sin\theta_{\Lambda} \cos\phi + D_4^{\lambda_i} \sin\theta_{\Lambda} \sin\phi) \sin\theta$$

$$+ (E_3^{\lambda_i} \sin\theta_{\Lambda} \cos\phi + E_4^{\lambda_i} \sin\theta_{\Lambda} \sin\phi) \sin\theta \cos\theta$$

$A_{\text{fb}}$  Baryon

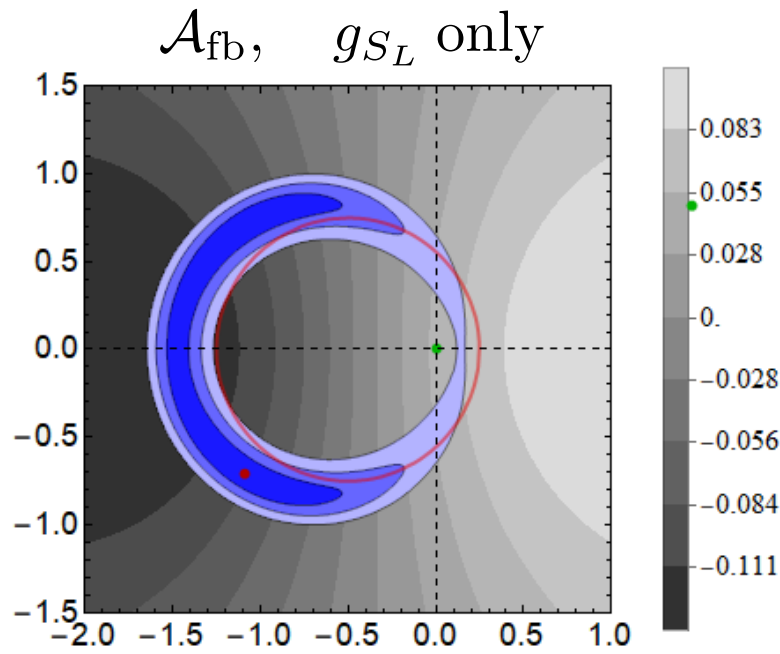
$A_{\text{fb}}$  Lepton

NP Phase

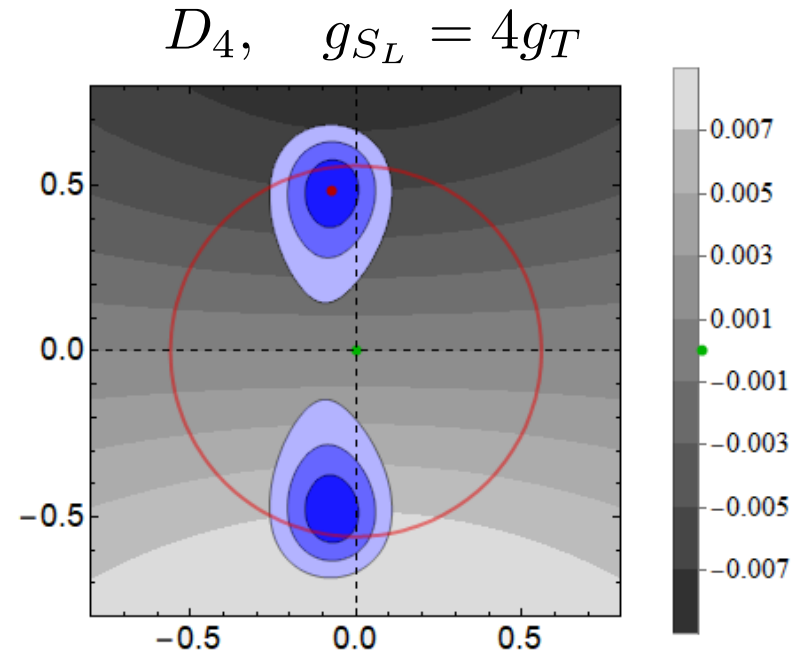
- $g_{VL}$  only affects the total Branching Fraction  $\rightarrow$  Distribution is SM-like.
- $D_4$  and  $E_4$  are sensitive to imaginary part of Wilson Coefficients.

$\longrightarrow$  New Physics phase

# Some observables



$\mathcal{A}_{\text{fb}}$  can easily flip sign.

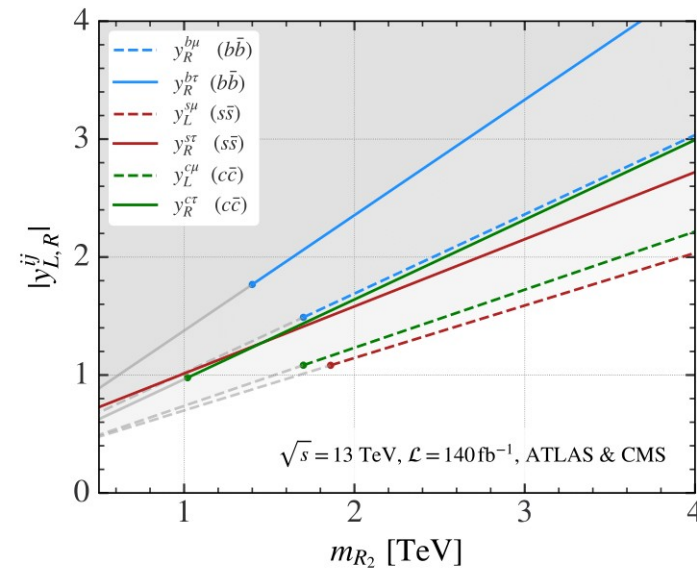
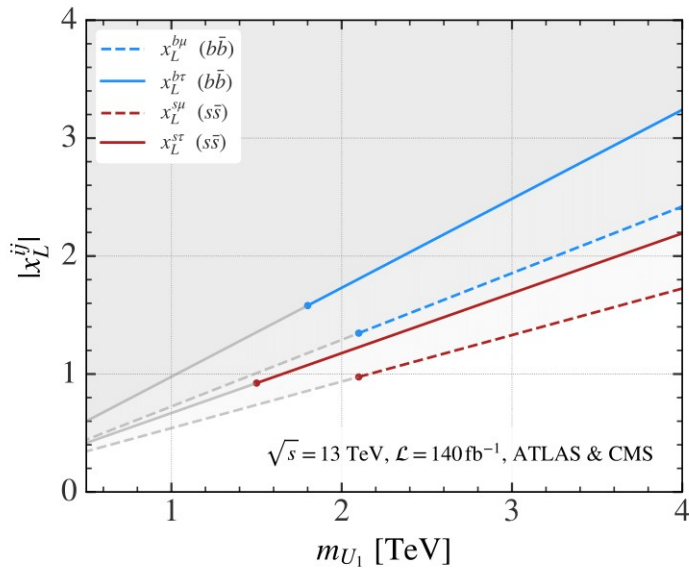
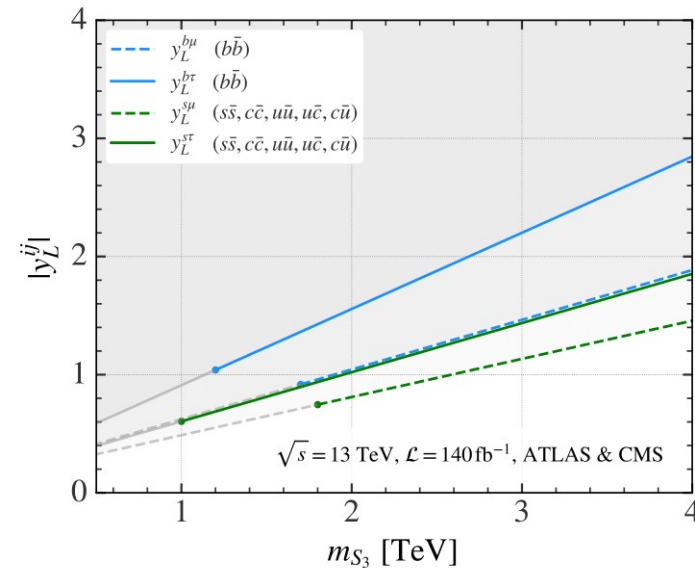
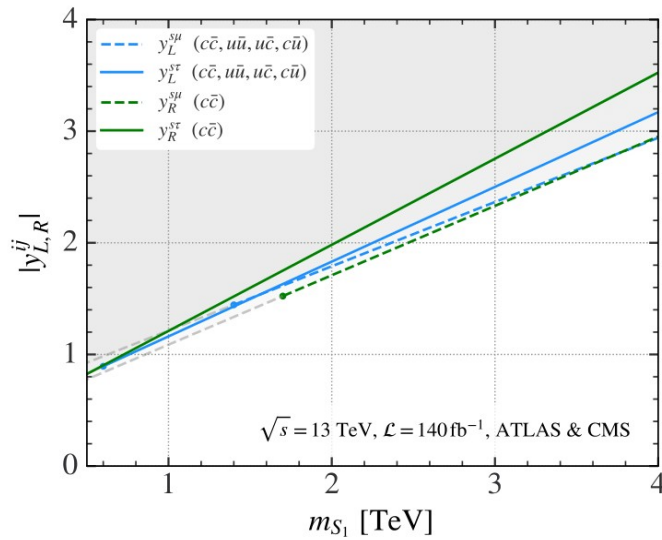


$D_4$  is exactly 0 in the SM.

$D_4$  is sensitive to the CP-phase.

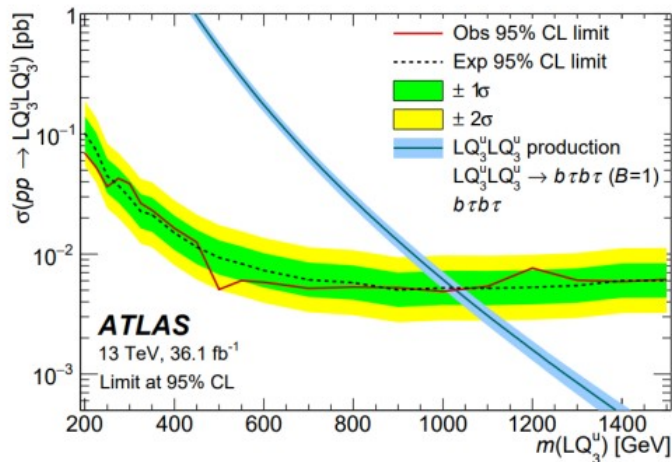
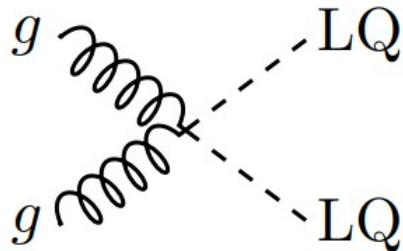
- Angular observables can help discriminate among various scenarios.  
[Even if  $\mathcal{R}(\Lambda_c)$  and  $\mathcal{R}(D^{(*)})$  are compatible with SM !]

# Backup: constraints on Leptoquarks



# Backup: limits from pair production

$LQ(3, X, X)$

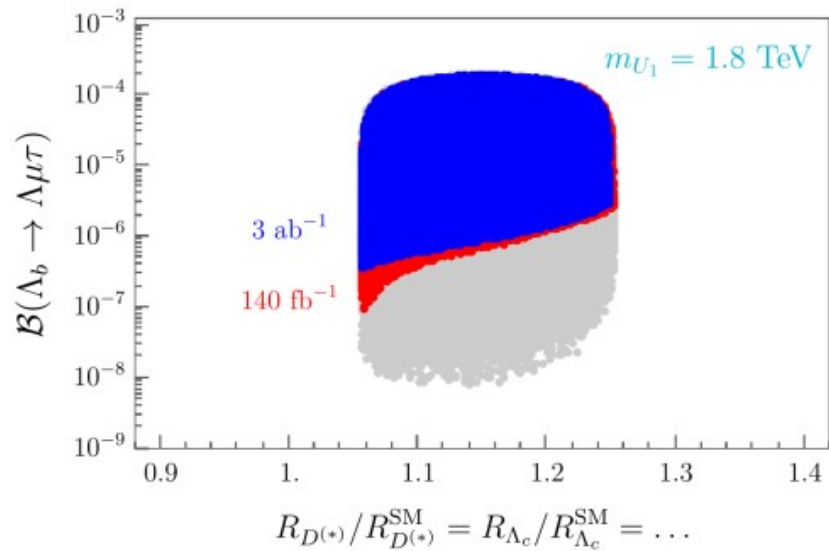
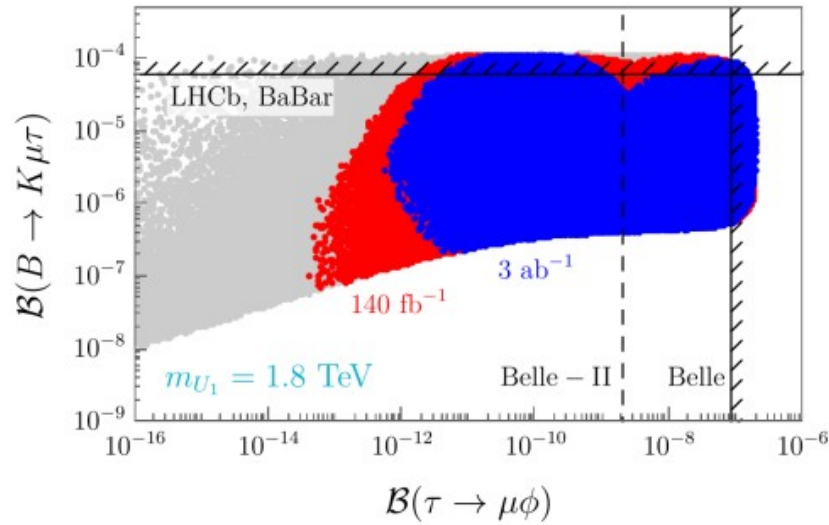


Decays	Scalar LQ limits	Vector LQ limits	$\mathcal{L}_{\text{int}}$
$jj\tau\bar{\tau}$	-	-	-
$b\bar{b}\tau\bar{\tau}$	1.0(0.8) TeV	1.5(1.3) TeV	36 fb <sup>-1</sup>
$t\bar{t}\tau\bar{\tau}$	1.4(1.2) TeV	2.0(1.8) TeV	140 fb <sup>-1</sup>
$jj\mu\bar{\mu}$	1.7(1.4) TeV	2.3(2.1) TeV	140 fb <sup>-1</sup>
$b\bar{b}\mu\bar{\mu}$	1.7(1.5) TeV	2.3(2.1) TeV	140 fb <sup>-1</sup>
$t\bar{t}\mu\bar{\mu}$	1.5(1.3) TeV	2.0(1.8) TeV	140 fb <sup>-1</sup>
$jj\nu\bar{\nu}$	1.0(0.6) TeV	1.8(1.5) TeV	36 fb <sup>-1</sup>
$b\bar{b}\nu\bar{\nu}$	1.1(0.8) TeV	1.8(1.5) TeV	36 fb <sup>-1</sup>
$t\bar{t}\nu\bar{\nu}$	1.2(0.9) TeV	1.8(1.6) TeV	140 fb <sup>-1</sup>

[Atlas, CMS '18-'20]

Assuming a branching fraction of 1 (0.5).

# Backup: LFV decays



$$\left. \begin{array}{l} Z \rightarrow \tau\mu \\ \tau \rightarrow \mu\gamma \end{array} \right\} \text{Loop induced}$$

$$\tau \rightarrow \mu\phi$$

$$B \rightarrow K^{(*)}\tau\mu$$

$$\Lambda_b \rightarrow \Lambda\tau\mu$$

Direct searches  $\Rightarrow$  Minimal bounds on LFV decays.

# Results

- Best fit point :

$$y_L^{c\mu} \in (0.16, 0.33)_{1\sigma}, (0.11, 0.40)_{2\sigma},$$

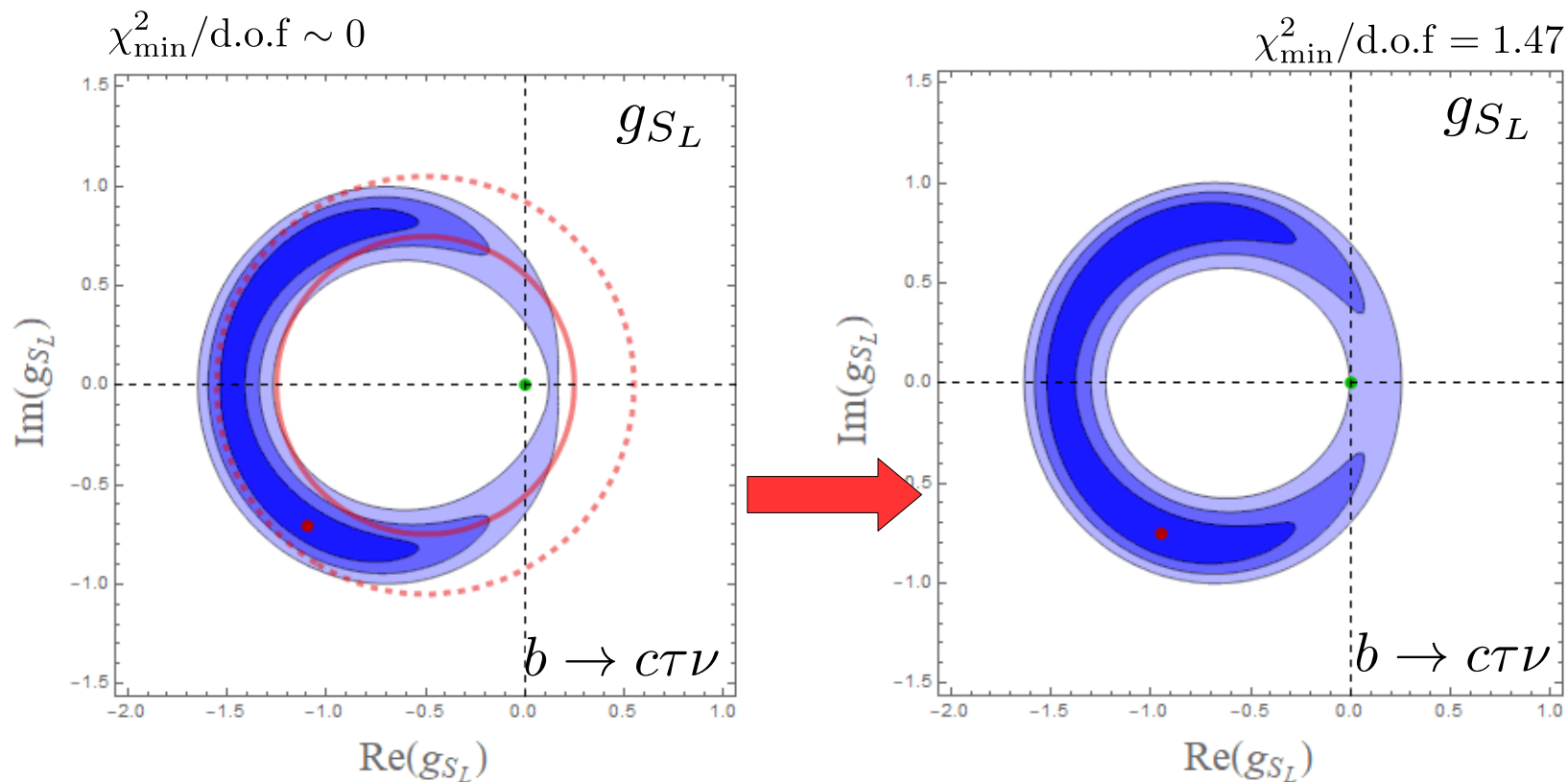
$$y_L^{c\tau} \in (0.87, 1.40)_{1\sigma}, (0.64, 1.54)_{2\sigma},$$

$$\text{Re} [y_R^{b\tau}] \in (-0.37, 0.02)_{1\sigma}, (-0.58, 0.15)_{2\sigma},$$

$$|\text{Im} [y_R^{b\tau}]| \in (0.83, 1.53)_{1\sigma}, (0.61, 1.87)_{2\sigma},$$

$$\theta \in \frac{\pi}{2}(1.01, 1.06)_{1\sigma}, \frac{\pi}{2}(1.01, 1.12)_{2\sigma},$$

# Backup : Old and new constraints



Wilson Coefficient	$R(D)$ and $R(D^*)$	$R(\Lambda_c)$	Combined	$\chi^2_{\min}/\text{d.o.f}$
$g_{V_L}$	$0.084 \pm 0.029$	$-0.15 \pm 0.14$	$0.077 \pm 0.035$	$0.06 \rightarrow 1.3$
$g_{S_L}$	$-1.47 \pm 0.08$	$-0.53 \pm 0.54$	$-1.45 \pm 0.11$	$0.5 \rightarrow 2.1$
$g_T$	$-0.027 \pm 0.011$	$0.13 \pm 0.14$	$-0.026 \pm 0.013$	$1.2 \rightarrow 1.7$
$g_{S_L} = +4g_T \in i\mathbb{R}$	$\pm 0.49 \pm 0.10$	$0.0 \pm 0.39$	$\pm 0.47 \pm 0.13$	$0.9 \rightarrow 1.6$
$g_{S_L} = -4g_T$	$0.16 \pm 0.06$	$0.0 \pm 0.39$	$0.15 \pm 0.07$	$0.7 \rightarrow 1.0$



# Backup: Experimental Status: Neutral currents

- Results for  $b \rightarrow s\ell\bar{\ell}$ : 
$$R_X = \frac{\mathcal{B}(Y \rightarrow X\mu^+\mu^-)}{\mathcal{B}(Y \rightarrow Xe^+e^-)}$$

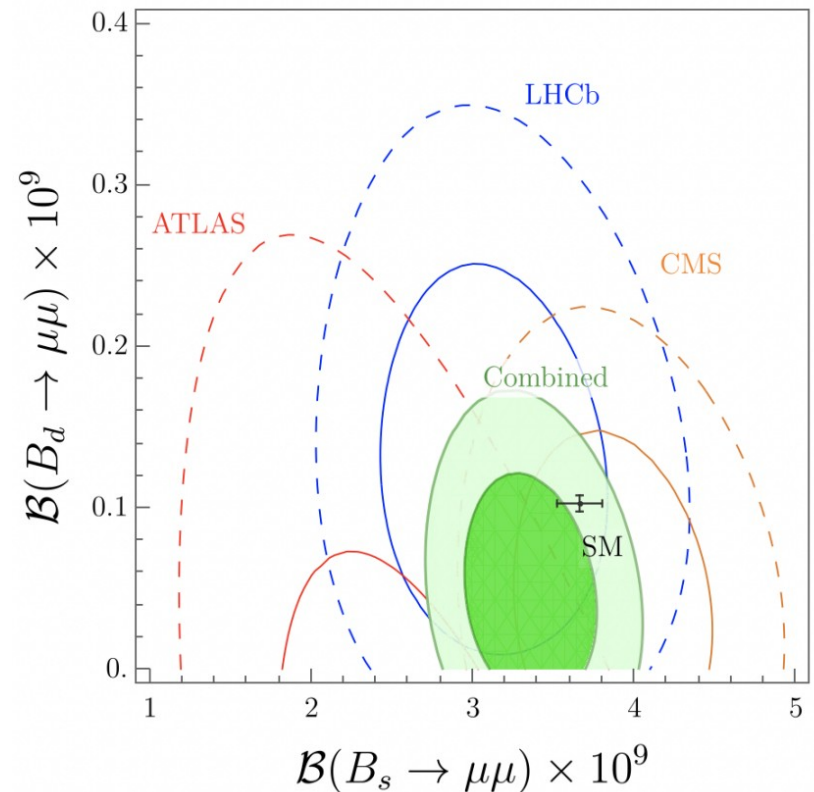
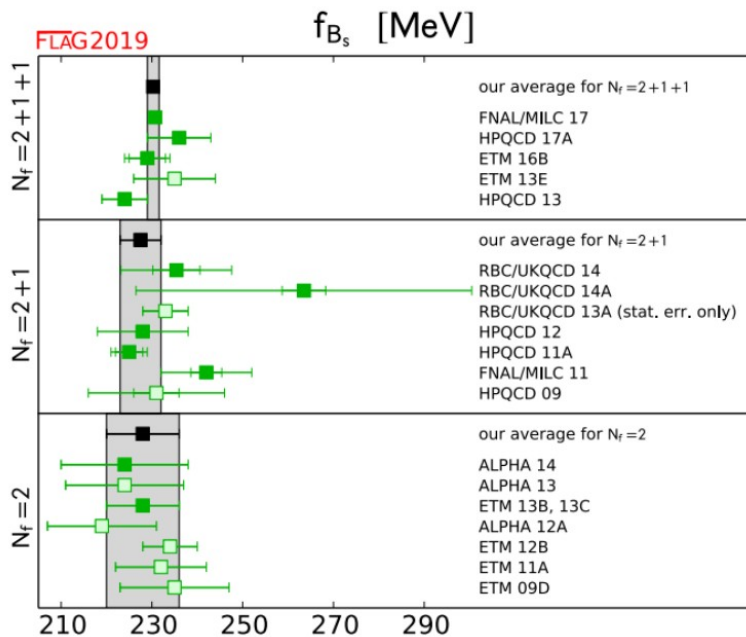
	SM prediction	Measurement	Tension
$R_K^{[1.1,6]}$	1.00(1) [G. Isidori et al.'20]	0.847(42) [LHCb '21]	$3.1\sigma$
$R_{K^*}^{[1.1,6]}$	1.00(1) [M. Bordone et al.'16]	0.69(10) [LHCb '17]	$2.4\sigma$
$R_{K^*}^{[0.045,1.1]}$	0.91(3) [M. Bordone et al.'16]	0.66(10) [LHCb '17]	$2.3\sigma$
$R_{pK}^{[0.1,6]}$	$\simeq 1$	0.85(14) [LHCb]	$1\sigma$

+ Some angular observables, which are more or less “safe”.

# Backup: Another decay: $B_s \rightarrow \mu^+ \mu^-$

- Can also probe the same quark transition  $b\bar{s} \rightarrow \ell\bar{\ell}$ .
- Not a ratio, but hadronic uncertainties are well under control.
- The hadronic matrix element depends on a single quantity:

$$\langle 0 | \bar{s} \gamma^\mu \gamma_5 b | B_s \rangle = i f_{B_s} p^\mu$$



# Backup: FCNC update

